

# Nucleon spin structure at low $Q$ : Hyperfine view

## Outlook

**A. Deur**

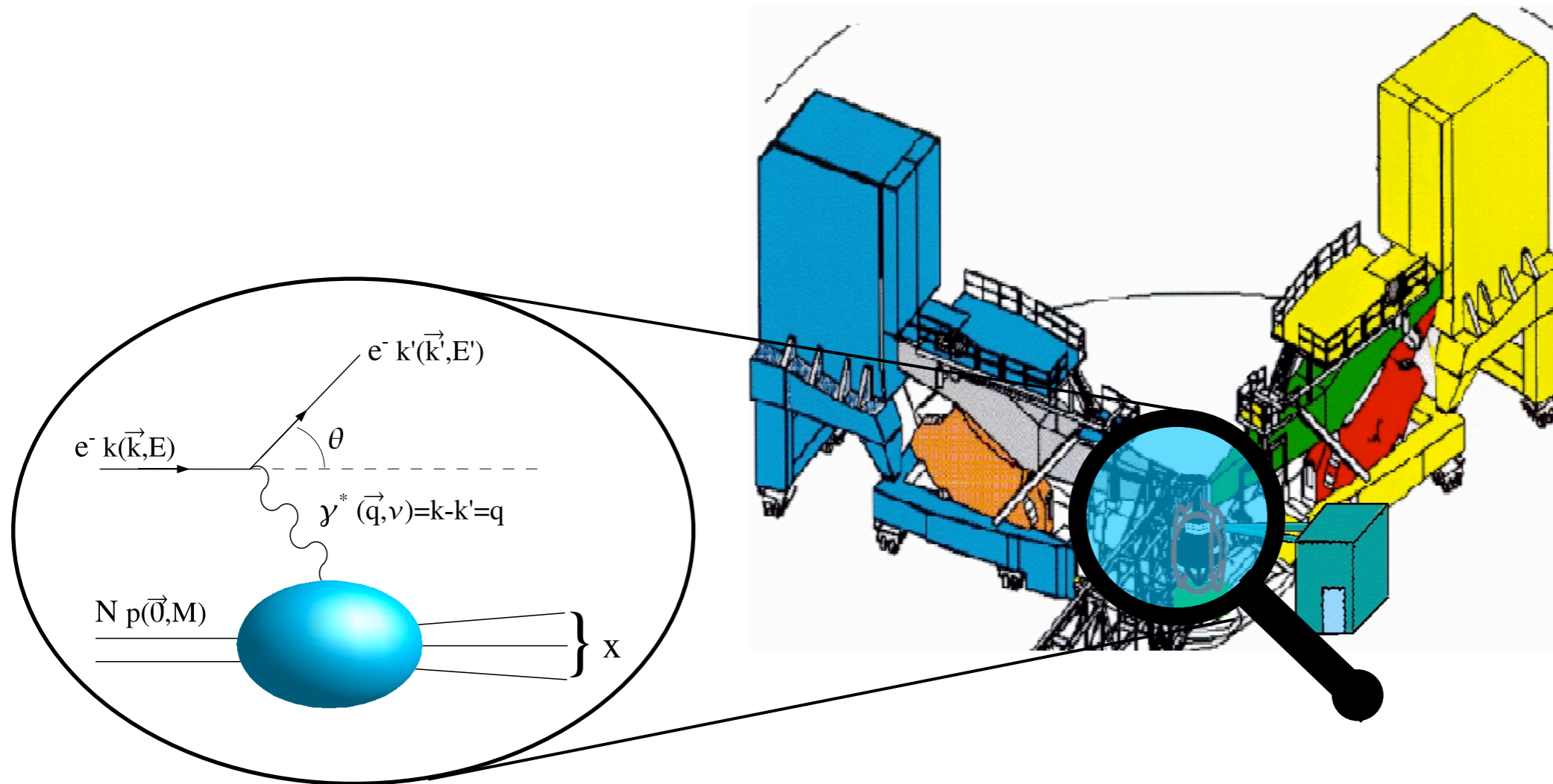
Thomas Jefferson National Accelerator Facility

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# Goals of the workshop

- Review the latest experimental and theoretical developments on:
  - Low  $Q$  nucleon spin structure functions, spin polarizabilities and sum rules
  - Nucleon form factors and polarizabilities
  - The light atoms' hyperfine structure at the intersection between nuclear and atomic physics: High precision atomic measurements  $\Rightarrow$  2-photon exchange,  $G_m$  and above observables needed for hadronic corrections.

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- Interpretation of the new data/comparison

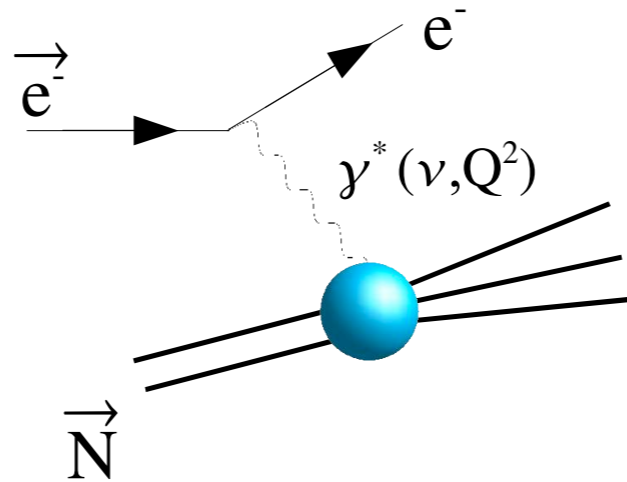
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- What new experiments are needed?
- What theoretical advances are needed?

# Inclusive polarized lepton scattering



## Structure functions:

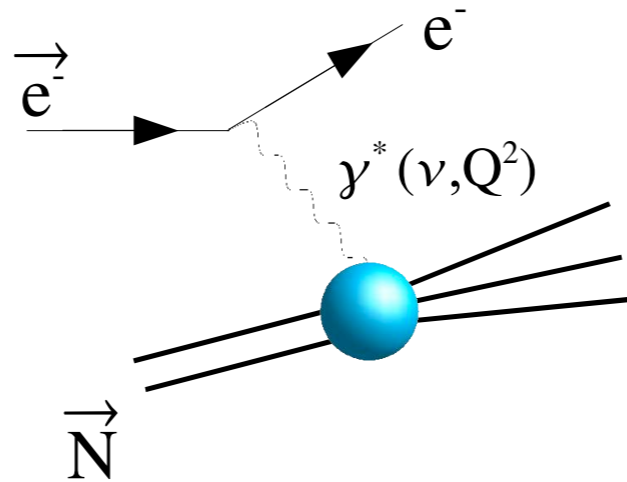
$$\text{cross section} = [\text{cross section}_{\text{pointlike object}}] \times [\alpha F_1(x, Q^2) + \beta F_2(x, Q^2) + (\gamma g_1(x, Q^2) + \delta g_2(x, Q^2))]$$

$\uparrow \qquad \qquad \uparrow \qquad \qquad \uparrow \qquad \qquad \uparrow$   
unpolarized polarized

In Deep Inelastic scattering, interpreted in terms of parton distributions and **polarizations**.

$$x = \frac{Q^2}{2M\nu} \sim \text{momentum of the struck quark normalized to nucleon mom. } (0 < x < 1)$$

# Inclusive polarized lepton scattering



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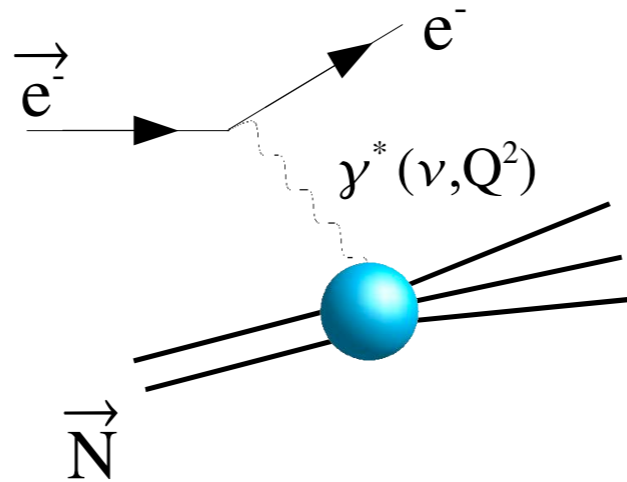
Lower  $Q^2$  response of the (excited) nucleon to virtual photon **spin (T & L)**:

$$\sigma_T \equiv \frac{\sigma_{T,1/2} + \sigma_{T,3/2}}{2} = \frac{8\pi^2\alpha}{M\kappa_{\gamma^*}} F_1, \quad \sigma_L \equiv \sigma_{L,1/2} = \frac{4\pi^2\alpha}{M\kappa_{\gamma^*}} \left[ -F_1(Q^2, \nu) + \frac{M}{\nu} \left(1 + \frac{1}{\gamma^2}\right) F_2(Q^2, \nu) \right]$$

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**x=1: Elastic scattering**

e.g.  ${}^3\text{He}$

$$\frac{d\sigma}{d\Omega} = \sigma_{Mott} \frac{E'}{E} \left( \frac{G_E^2 + \tau_r G_M^2}{1 + \tau_r} + 2\tau_r G_M^2 \tan^2(\theta/2) \right)$$

# Inclusive polarized lepton scattering

$$\Gamma_1 = \int g_1 dx, \Gamma_2 = \int g_2 dx$$

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GDH sum rule:  $\int_{\nu_{\text{thr}}}^{\infty} (\sigma^{1/2} - \sigma^{3/2}) \frac{d\nu}{\nu} = \frac{-2\alpha\pi^2\kappa^2}{M^2}$

Photo-absorption cross sections

Photon energy

anomalous magnetic moment

Measured/being measured at  $Q^2=0$  at MAINZ/ELSA, LEGS and HIGS (see M. Ahmed and P. Martel's talks). But max.  $\nu \sim 3$  GeV may not be enough to test sum rule's convergence  $\nu$

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Originally derived for photo-absorption ( $Q^2=0$ )

Later generalized to  $Q^2 > 0$ :  $\frac{16\alpha\pi^2}{Q^2} \int_0^1 g_1 dx = 2\alpha\pi^2 S_1 \xrightarrow{Q^2 \rightarrow 0} \frac{-2\alpha\pi^2\kappa^2}{M^2}$

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Generalized forward spin polarizability:

$$\gamma_0 = \frac{4e^2M^2}{\pi Q^6} \int x^2 (g_1 - \frac{4M^2}{Q^2} x^2 g_2) dx$$

Longitudinal-Transverse polarizability:

$$\delta_{LT} = \frac{4e^2M^2}{\pi Q^6} \int x^2 (g_1 + g_2) dx$$

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BC sum rule:  $\Gamma_2 = \int_0^1 g_2 dx = 0$

# New sum rules

## sum rule for $I_1$

$$(S_1 - S_1^{\text{pole}})(\nu = 0, Q^2) = \frac{e^2}{2\pi M} I_1(Q^2) \quad \text{with}$$

$$I_1(Q^2) = \frac{2M^2}{Q^2} \int_0^{x_0} dx g_1(x, Q^2)$$

$$I_1'(0) = \frac{\kappa^2}{12} \langle r_2^2 \rangle + \frac{2\pi M^2}{e^2} \gamma_{E1M2} - \frac{3M^3}{2} [P'^{(M1,M1)1}(0) + P'^{(L1,L1)1}(0)]$$

**Sum rules relating RCS, VCS, VVCS  
Can be tested by experiment !**

Both for  $Q^2=0$  and  $Q^2>0$ .

See M. Vanderhaeghen's talk

$$Y_0 = -Y_{E1E1} - Y_{E1M2} - Y_{M1E2} - Y_{M1M1}$$

Components measurable (MAMI, HIGS).

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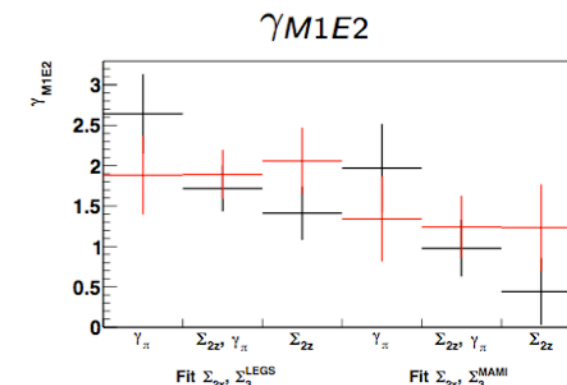
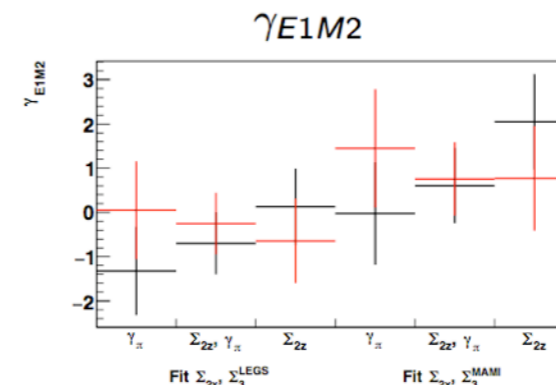
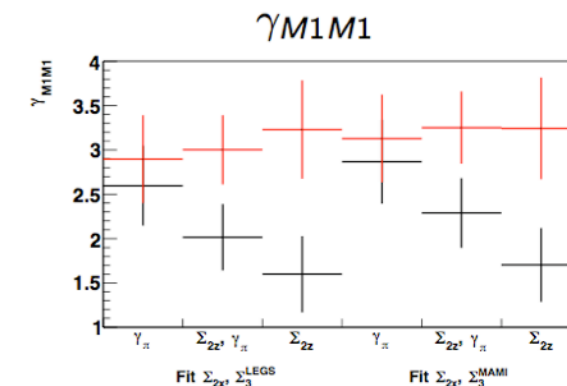
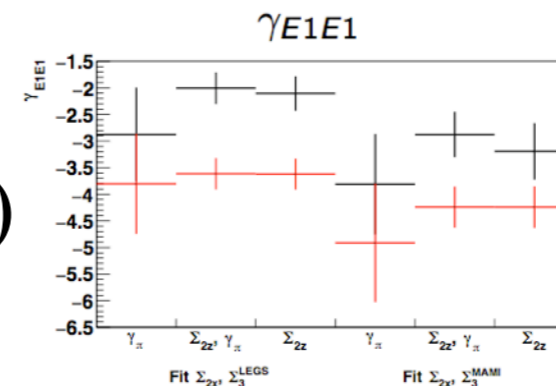
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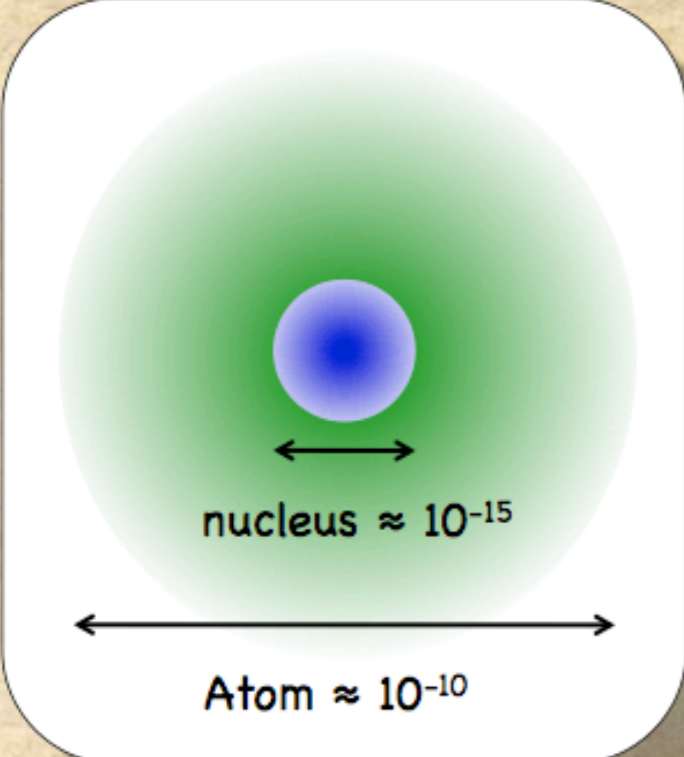
Components measurable (MAMI, HIGS)



See P. Martel's talk  
(see also cool active target development)



# Connection with atomic physics



The diagram shows a central blue nucleus with a diameter indicated by a double-headed arrow and labeled "nucleus  $\approx 10^{-15}$ ". Surrounding the nucleus is a large, light green, diffuse cloud representing the electron's probability distribution. A larger double-headed arrow below the nucleus indicates the overall size of the atom, labeled "Atom  $\approx 10^{-10}$ ".

### Hydrogen HF Splitting

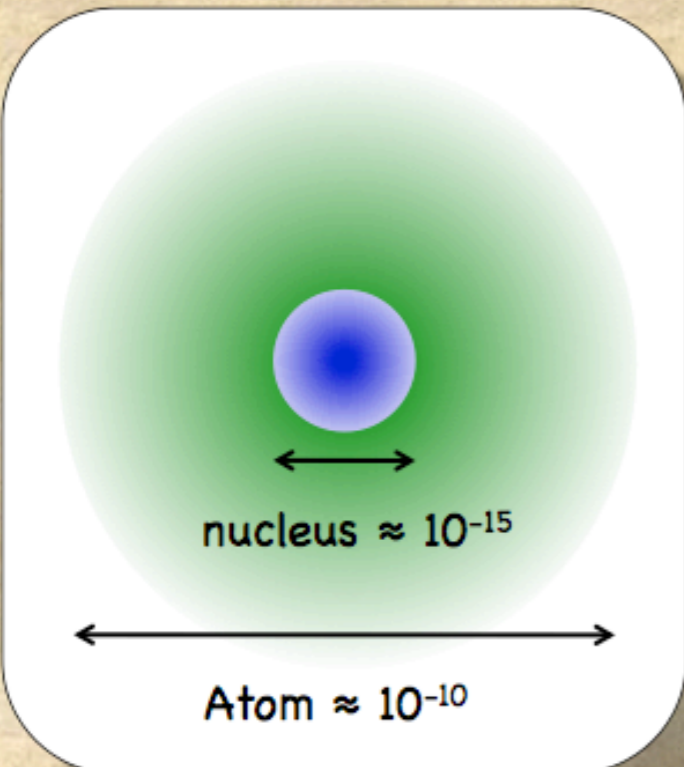
$$\begin{aligned}\Delta E &= 1420.405\,751\,766\,7(9)\text{ MHz} \\ &= (1 + \delta)E_F\end{aligned}$$
$$\delta = (\delta_{QED} + \delta_R + \delta_{small}) + \Delta_S$$

The finite size of the nucleus plays a small but significant role in atomic energy levels.

Priar & Sick PLB **579** 285(2003)

Stolen from K. Slifer's talk

# Connection with atomic physics



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$$\Delta_S = \Delta_Z + \Delta_{POL}$$

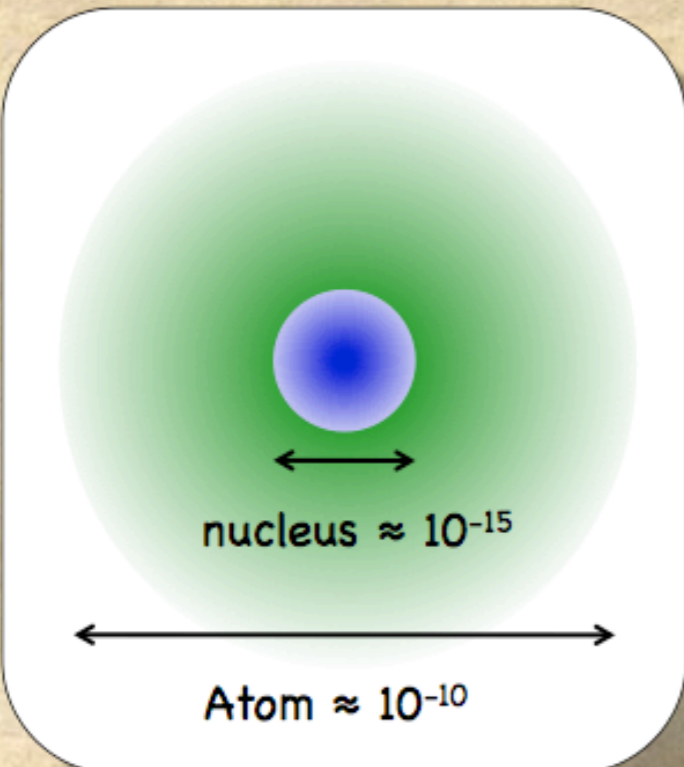
$$\Delta_Z = -2\alpha m_e r_Z (1 + \delta_Z^{rad})$$

$$r_Z = -\frac{4}{\pi} \int_0^\infty \frac{dQ}{Q^2} \left[ G_E(Q^2) \frac{G_M(Q^2)}{1 + \kappa_p} - 1 \right]$$

Elastic Scattering

$\Delta_Z = -41.0 \pm 0.5 \text{ ppm}$

# Connection with atomic physics



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$$\Delta_{POL} = 0.2265 (\Delta_1 + \Delta_2) \text{ ppm}$$

$$\Delta_1 = \frac{9}{4} \int_0^\infty \frac{dQ^2}{Q^2} \left[ \left( \frac{G_M(Q^2) + G_E^2(Q^2)}{1 + \tau} \right)^2 + \frac{8m_p^2}{Q^2} B_1(Q^2) \right]$$

$$B_1(Q^2) = \int_0^{x_{th}} dx \beta_1(\tau) g_1(x, Q^2)$$

$$\Delta_2 = -24m_p^2 \int_0^\infty \frac{dQ^2}{Q^4} B_2(Q^2)$$

$$B_2(Q^2) = \int_0^{x_{th}} dx \beta_2(\tau) g_2(x, Q^2)$$

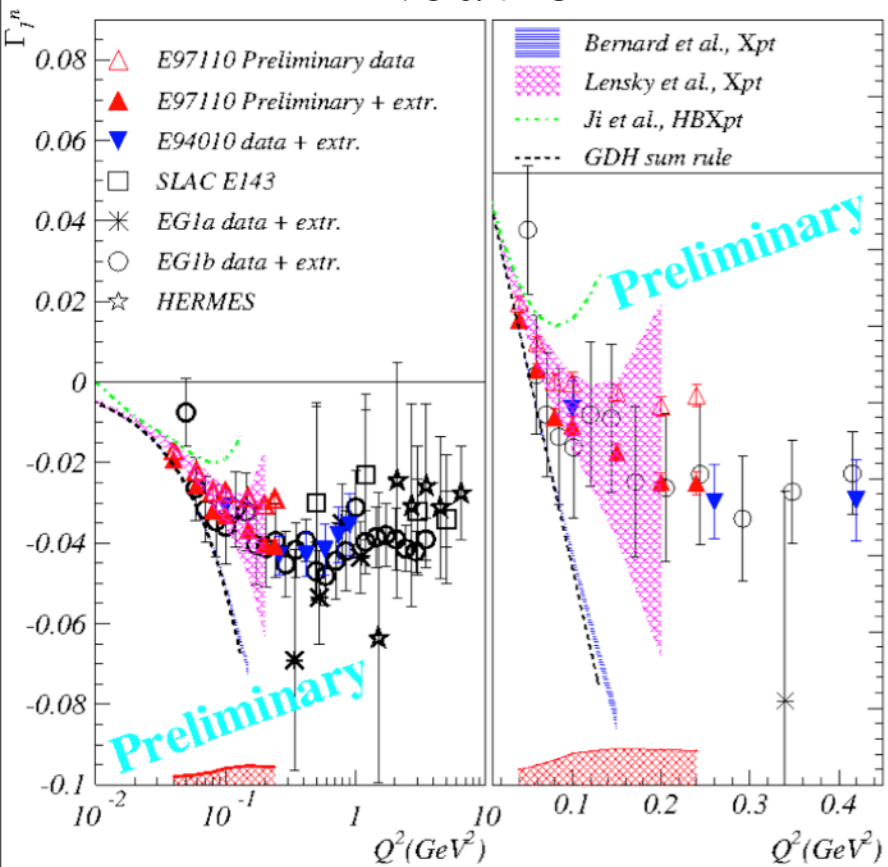
## Latest developments on low Q spin structure functions and spin polarizabilities.

Following the “ $\delta_{LT}$  puzzle” discovered early 2000s, a low Q experimental program was run at JLab to provide a test of  $\chi$ EFT. 4 experiments with focus on:

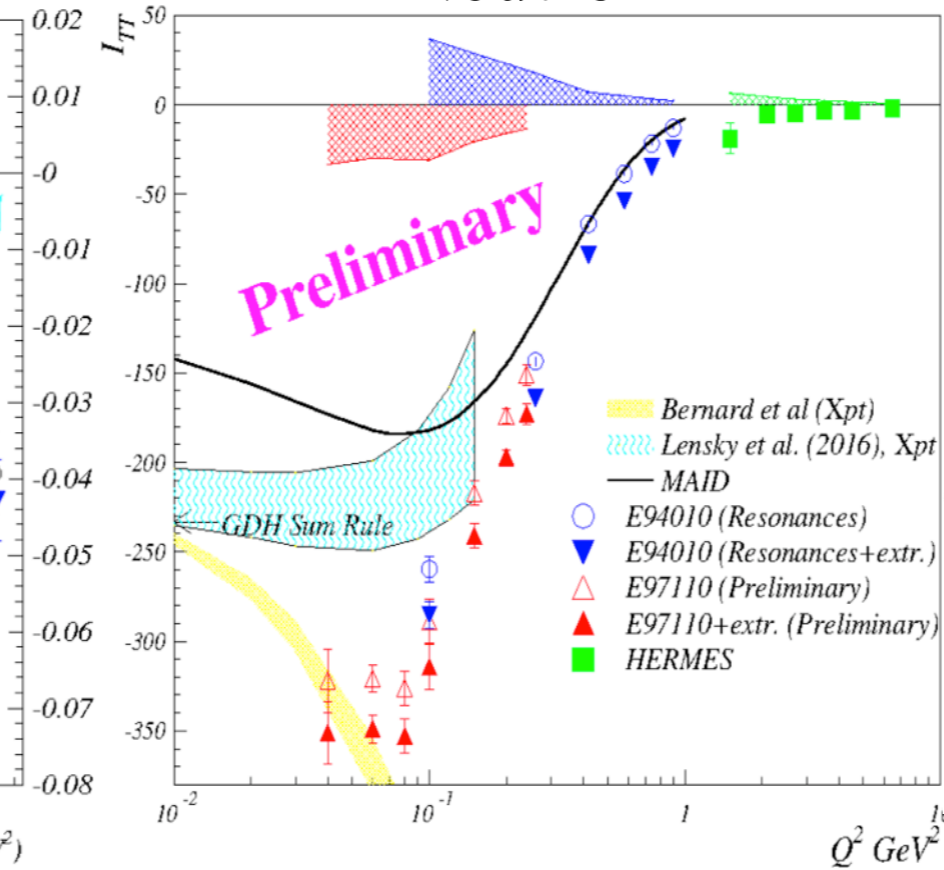
- GDH's  $I_{TT}$  ( $\sigma_{TT}$ , or  $g_1$  and  $g_2$ ) on neutron and  $^3\text{He}$ : J.P. Chen's talk
- GDH's  $\Gamma_1$  ( $g_1$ ) on proton: M. Ripani's talk
- GDH's  $\Gamma_1$  ( $g_1$ ) on neutron (D): M. Ripani's talk
- $\delta_{LT}$  ( $g_2$ ) on proton: K. Slifer's talk

# First moments: GDH sum(s)

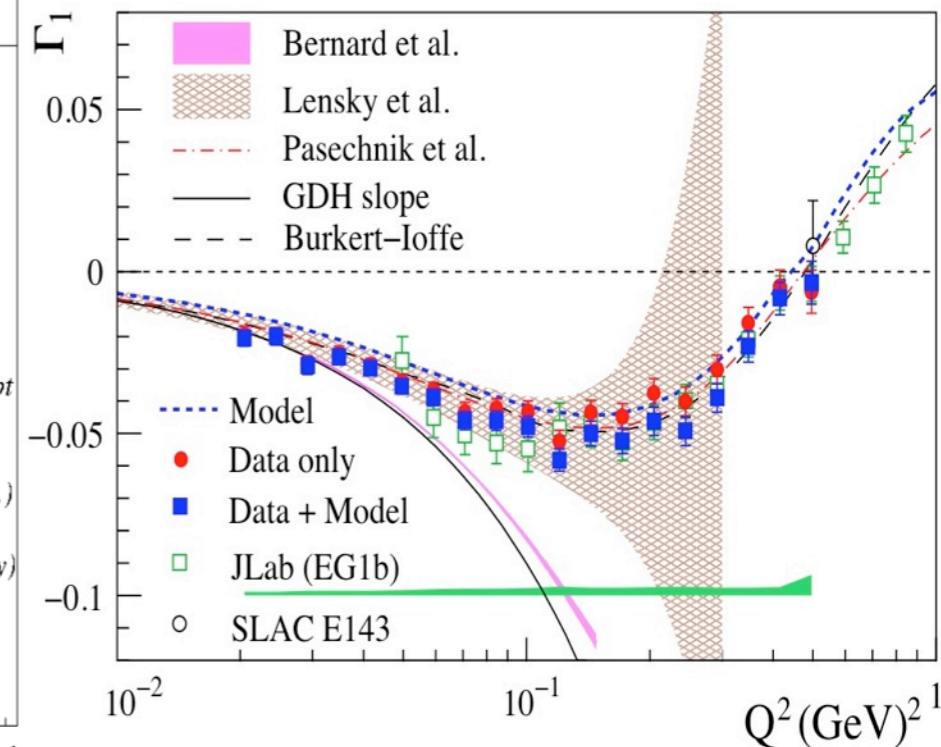
## Neutron



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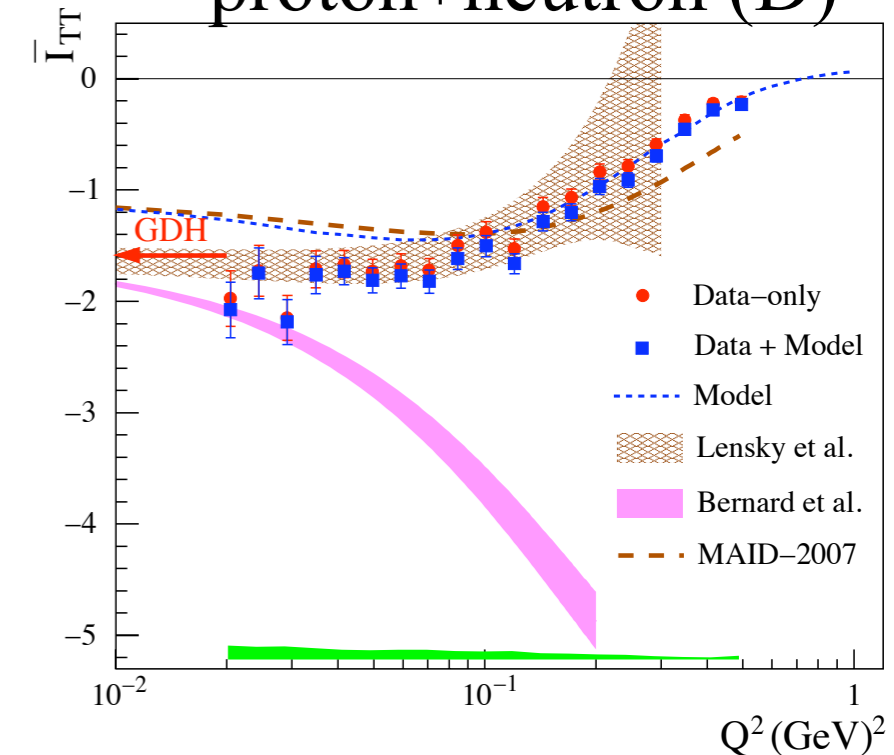


## ~proton+neutron (D)



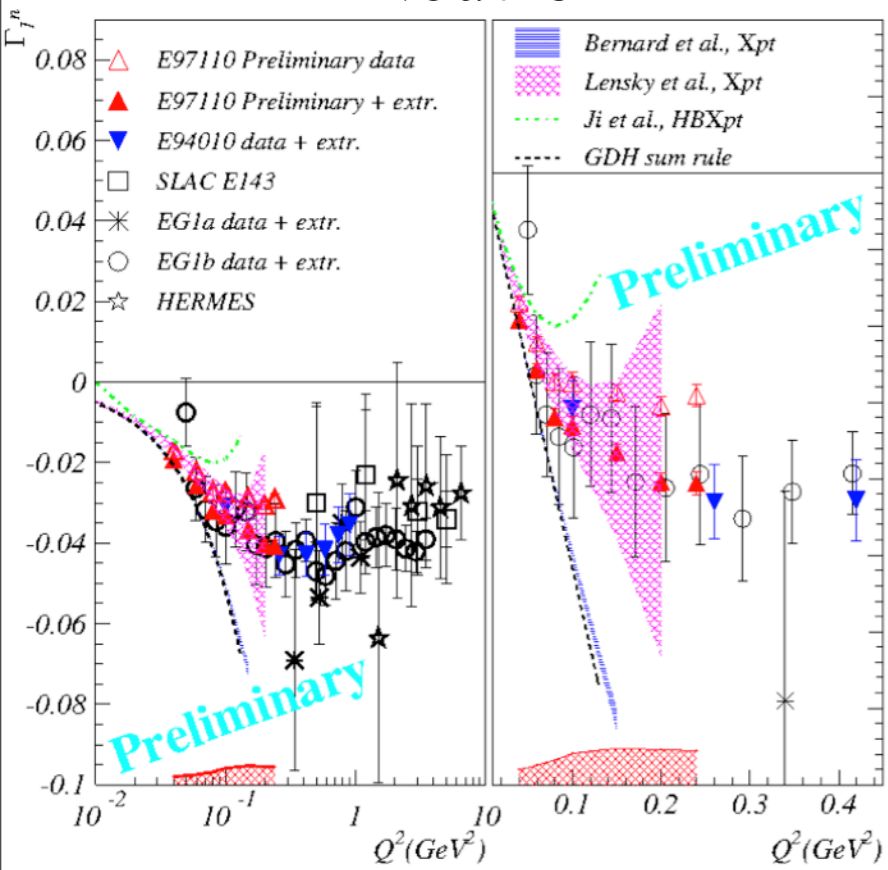
Proton data (JLab Halls A & B) on  $\Gamma_1$  favor Lensky et al., but data still very preliminary.

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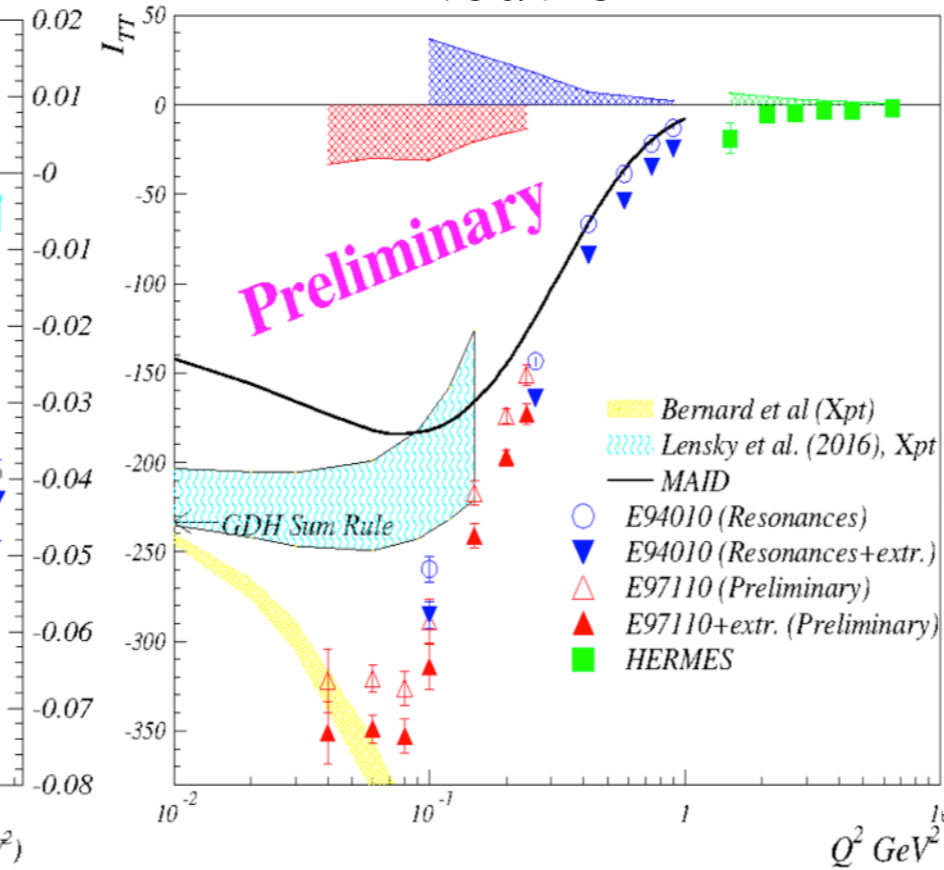


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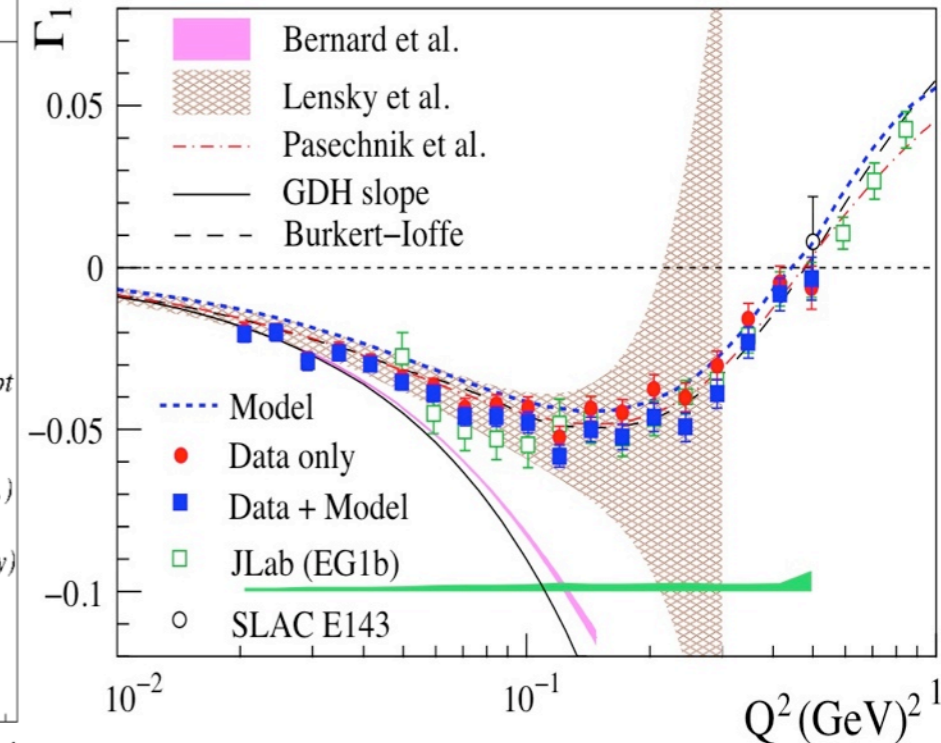
Neutron



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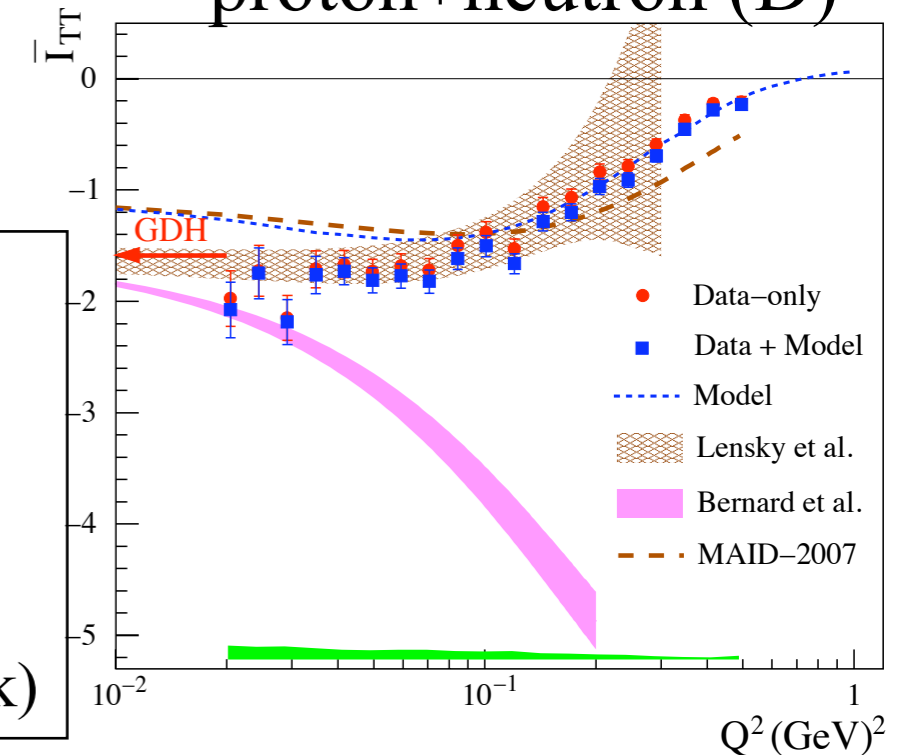


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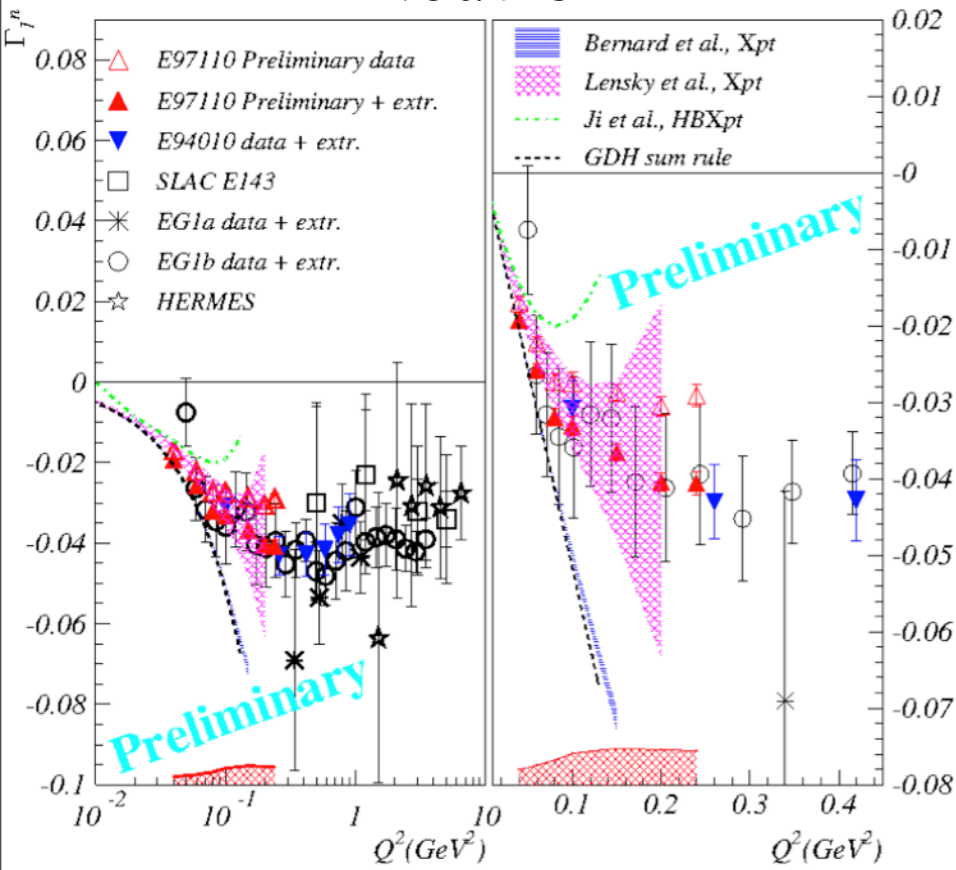
⇒ Lensky et al.  $\chi$ EFT successful with  $\Gamma_1$  but problem with  $\Gamma_2$ ?

Bernard et al.  $\chi$ EFT reliable only at the lowest  $Q^2$ .

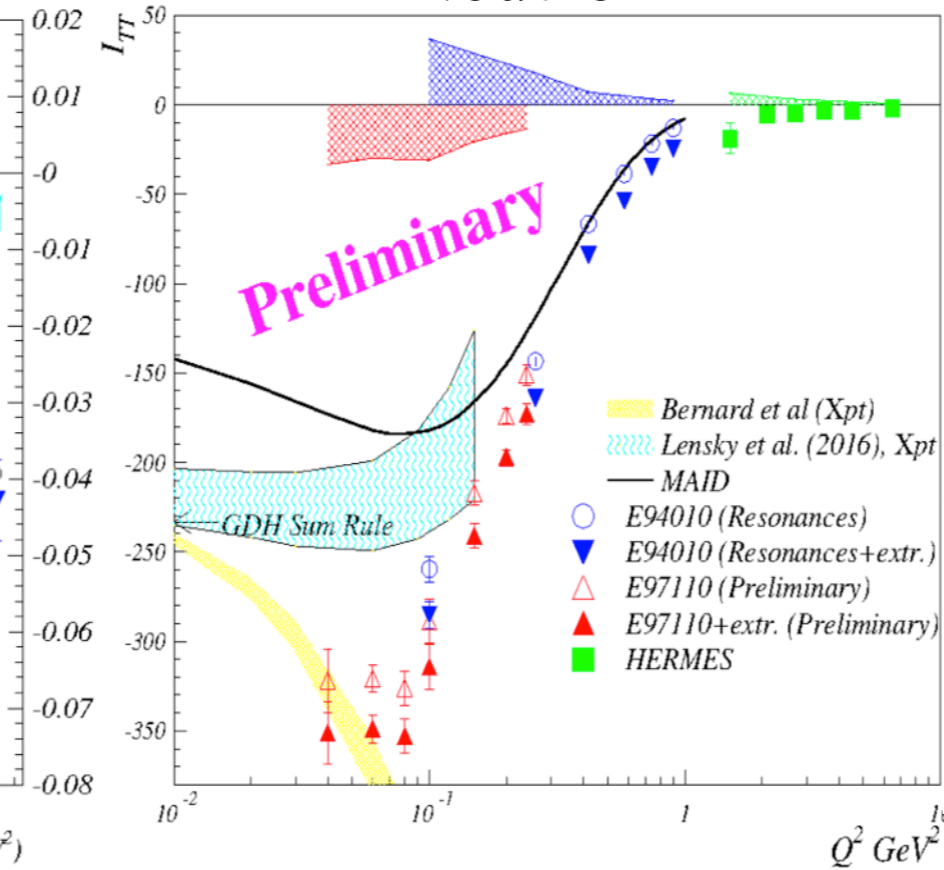
What differs between Lensky et al. and Bernard et al.  $\chi$ EFT calculations? (no big diff. identified, see V. Pascaltusa's talk)

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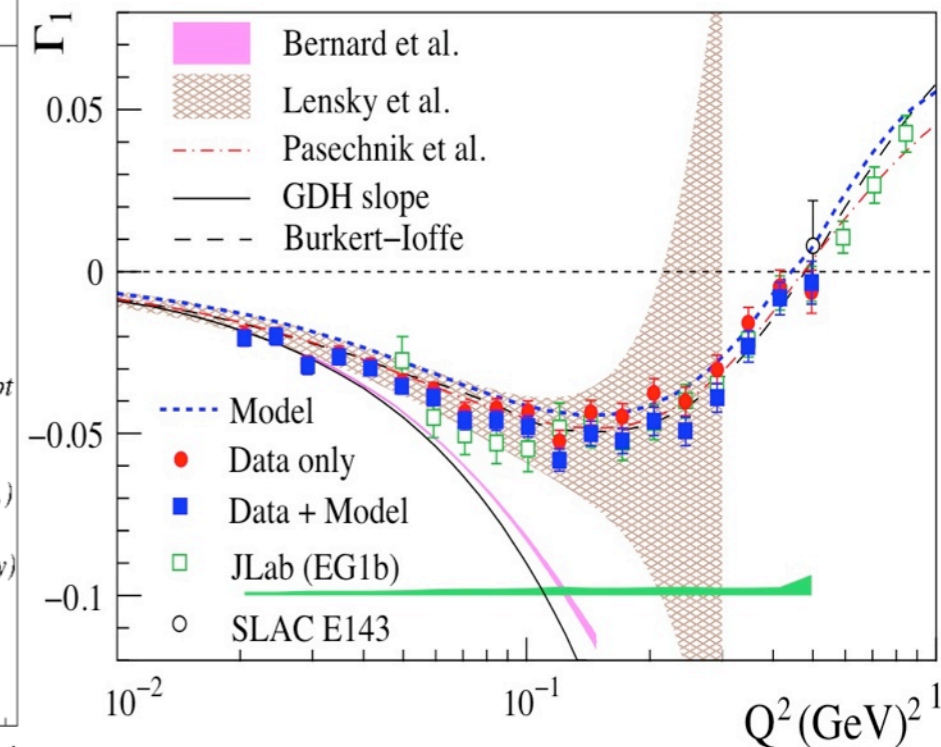
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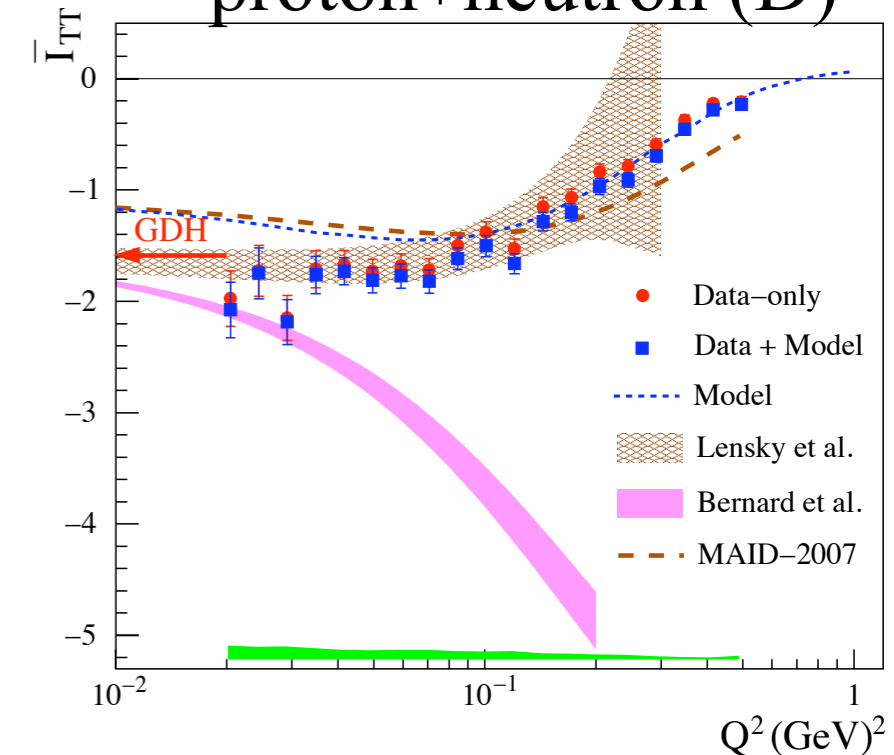
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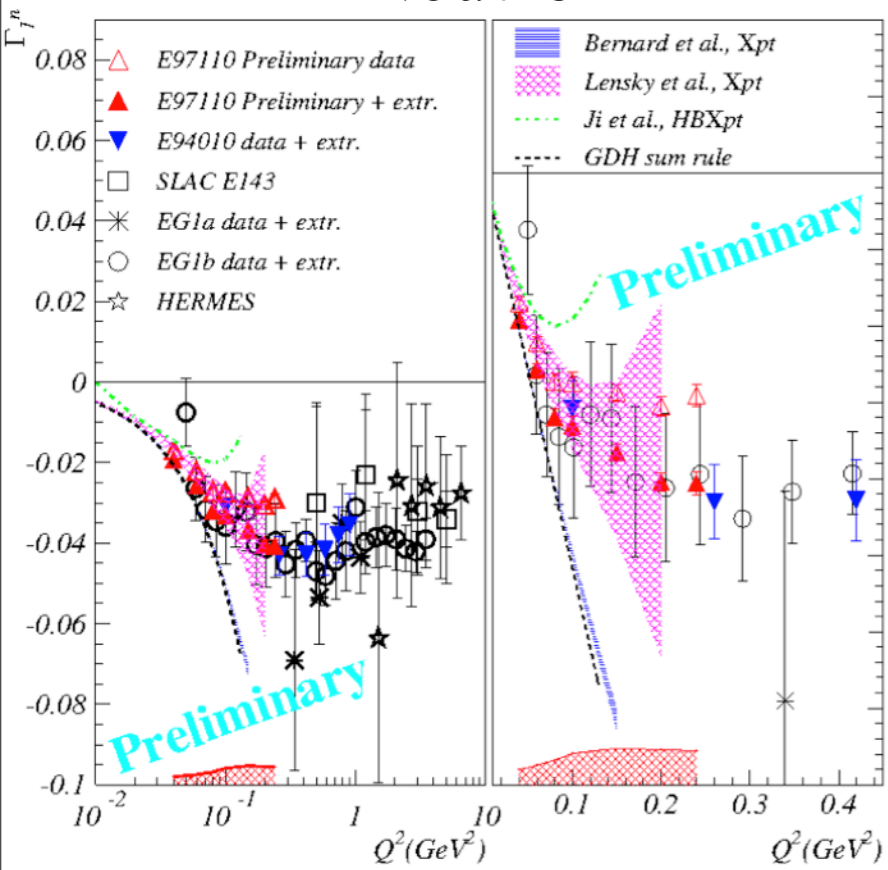
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Need global parameterization of low Q data.

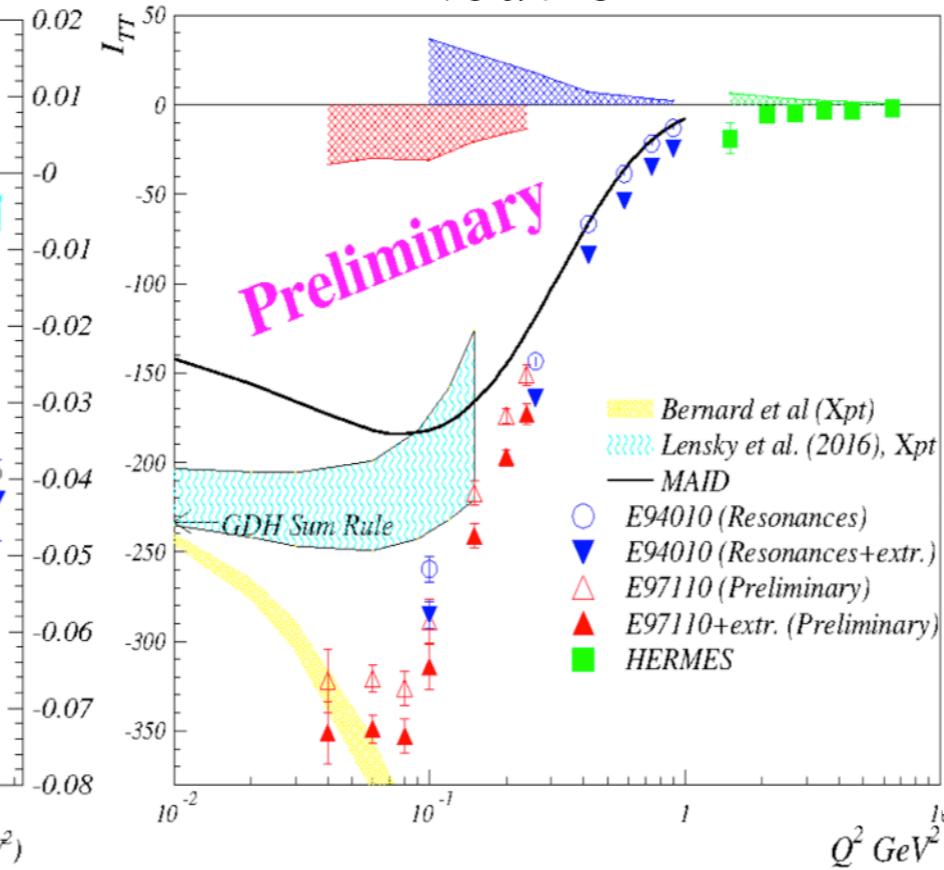
- Sebastian Kuhn Model.
- MAID

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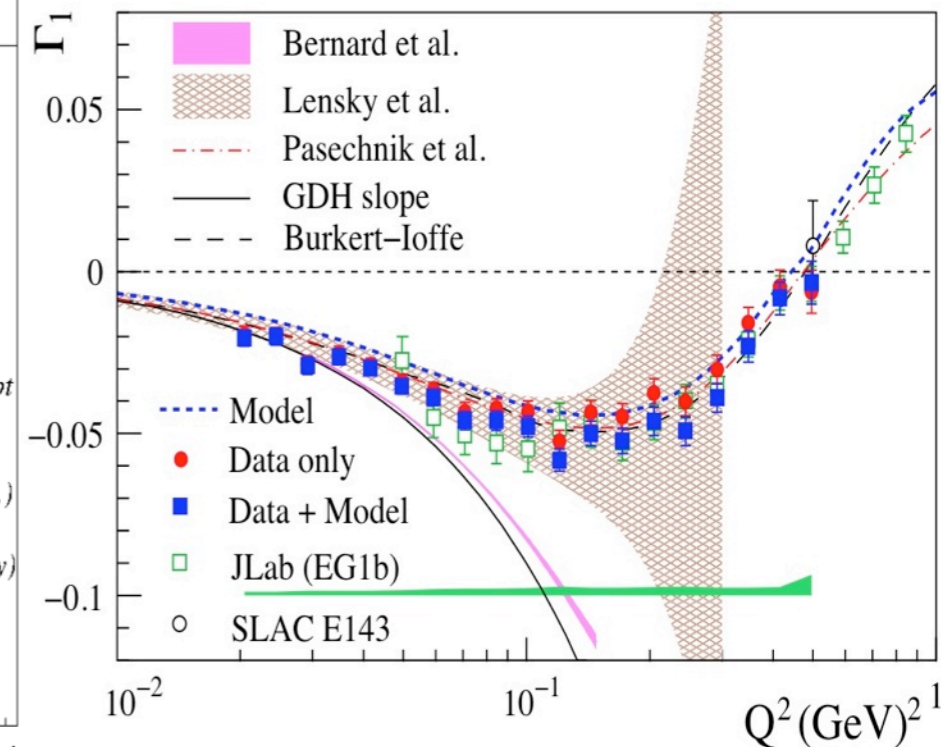
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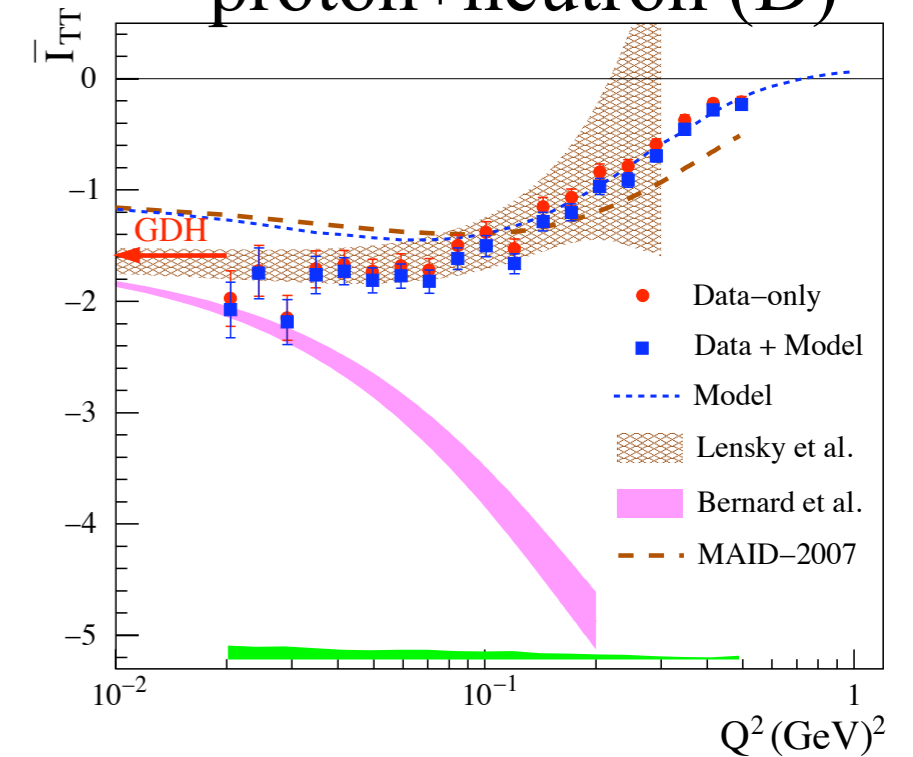
Neutron



~proton+neutron (D)



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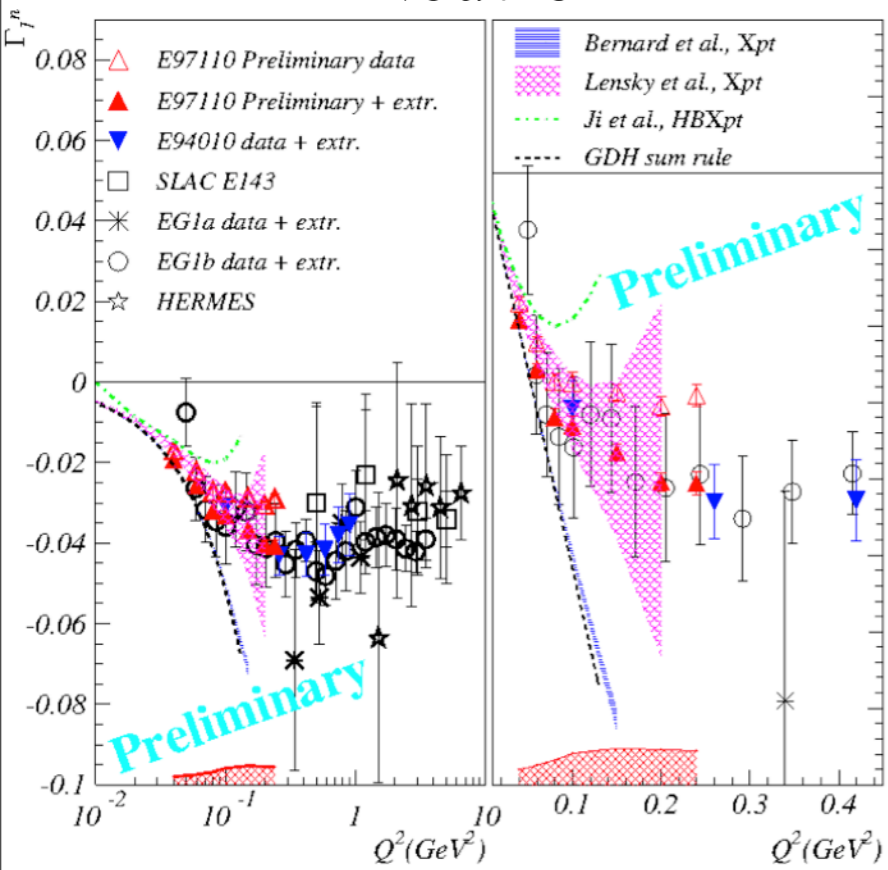
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No Lattice result on moments available yet at low and intermediate  $Q^2$ . Challenge: need to compute 4-point functions.

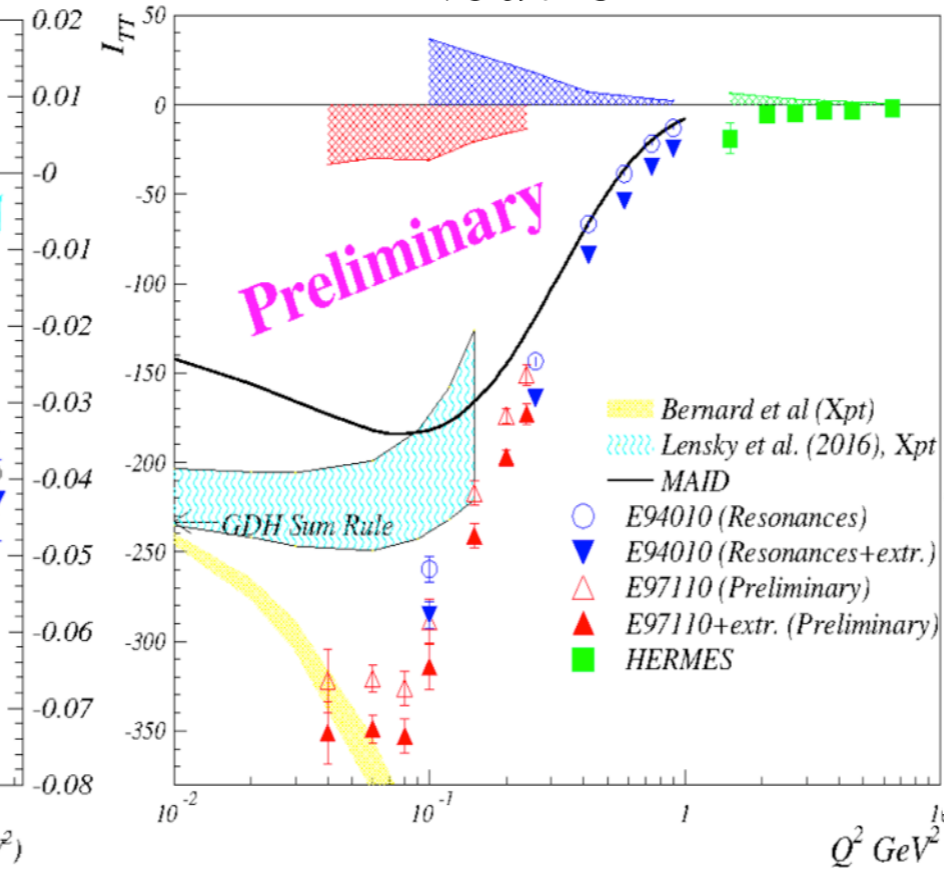


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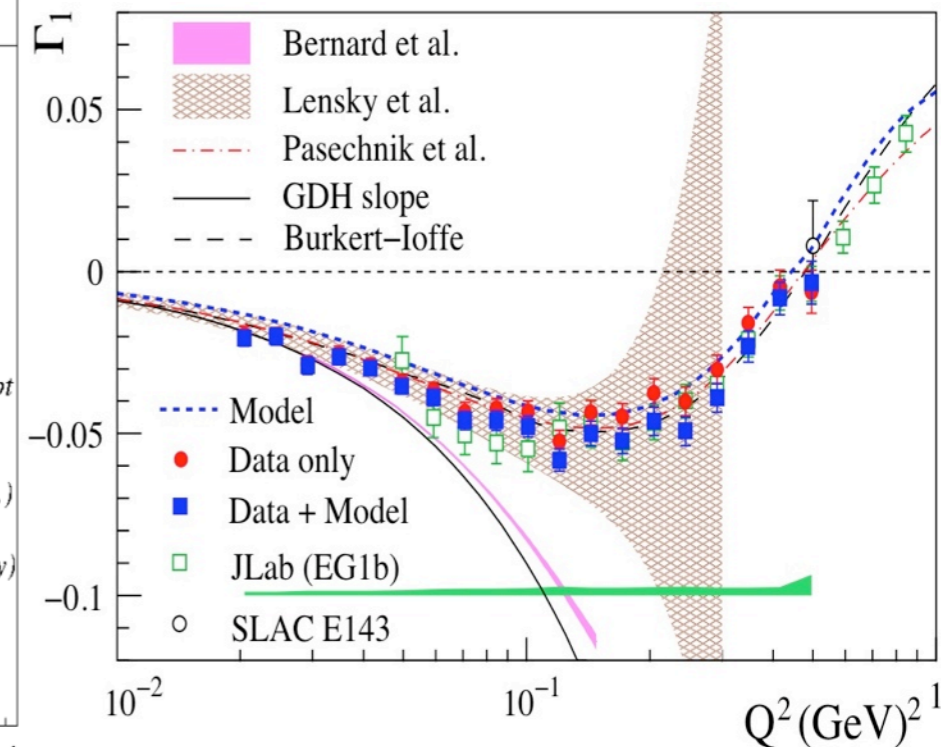
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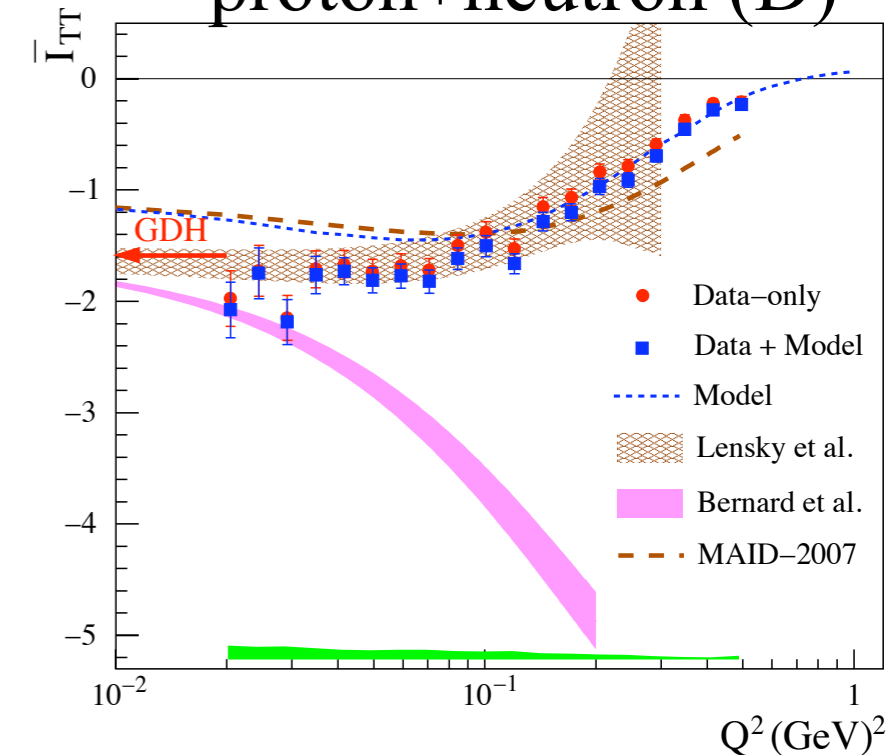
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Full spin decomposition (spin sum rule) at large  $Q^2$ .

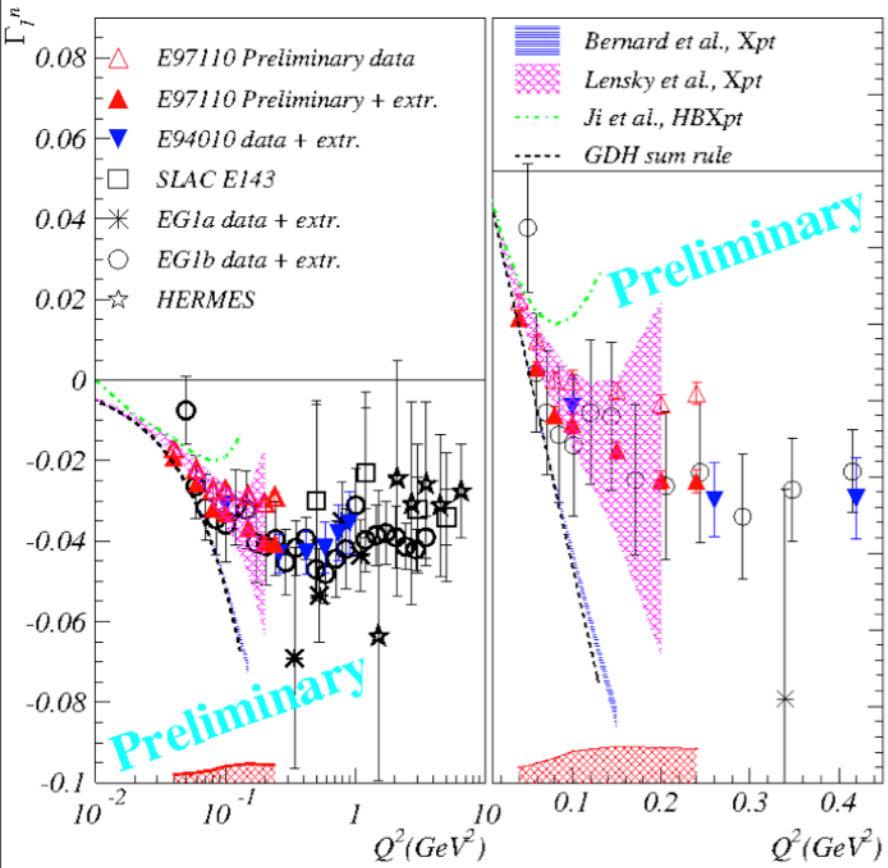
C. Alexandrou's talks

~proton+neutron (D)

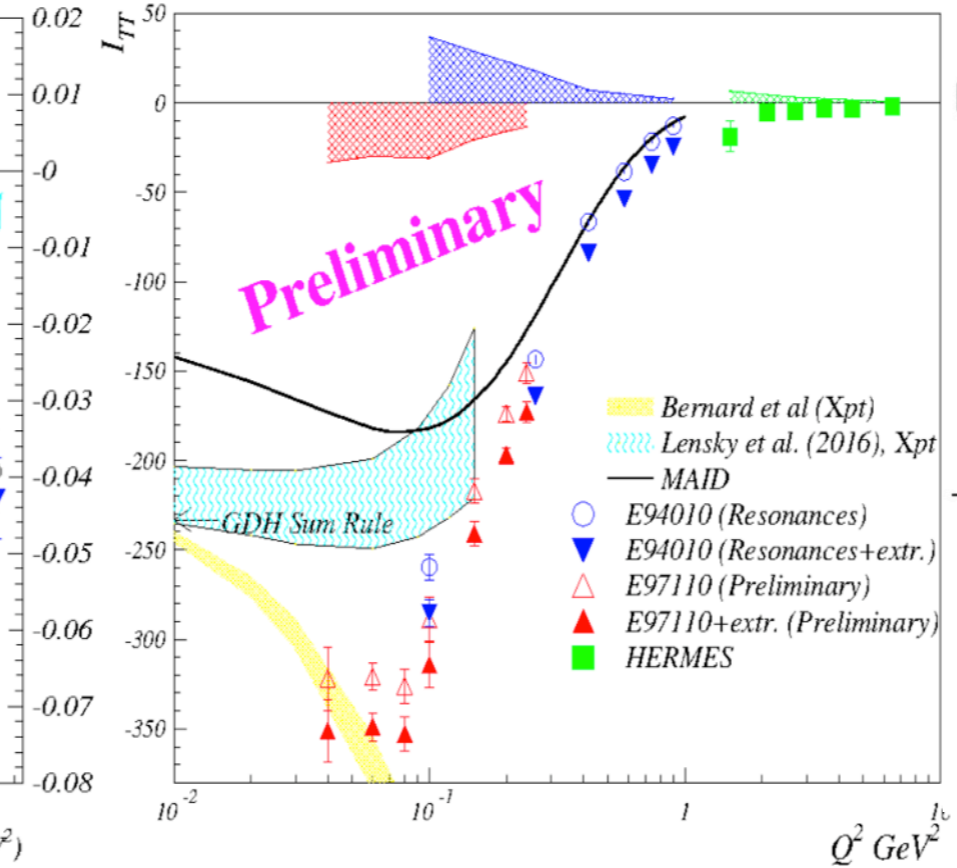


# First moments: GDH sum(s)

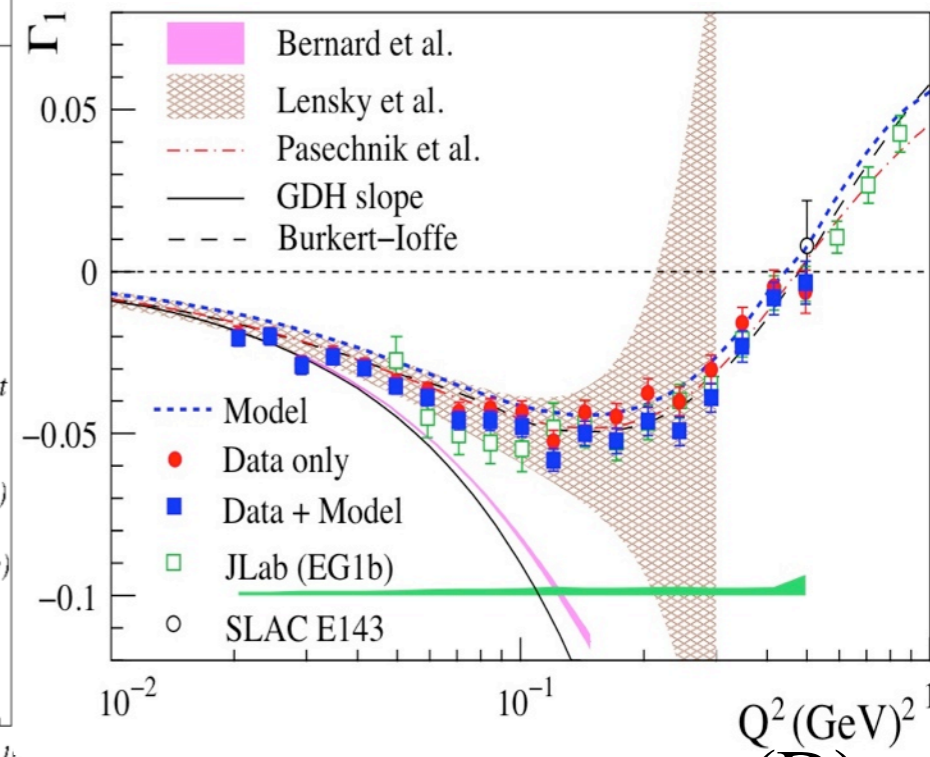
Neutron



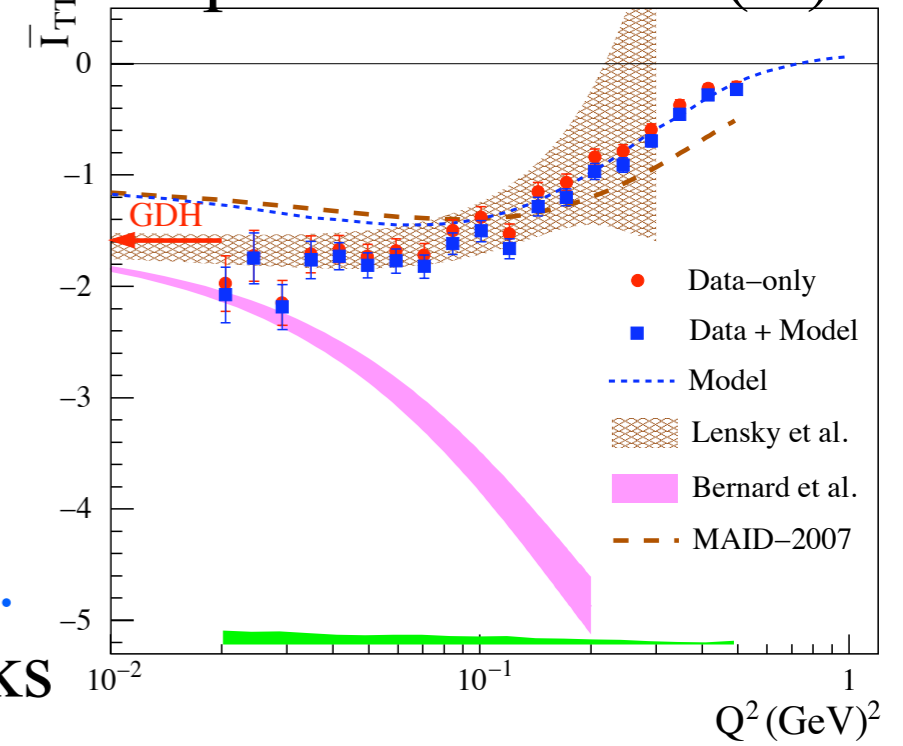
Neutron



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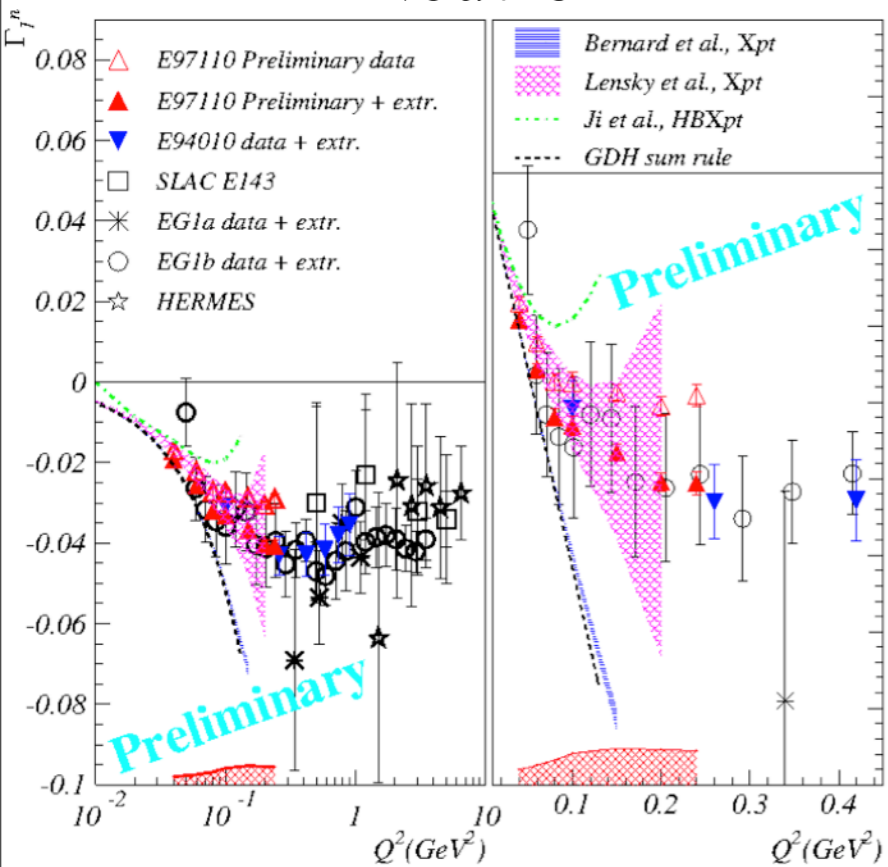
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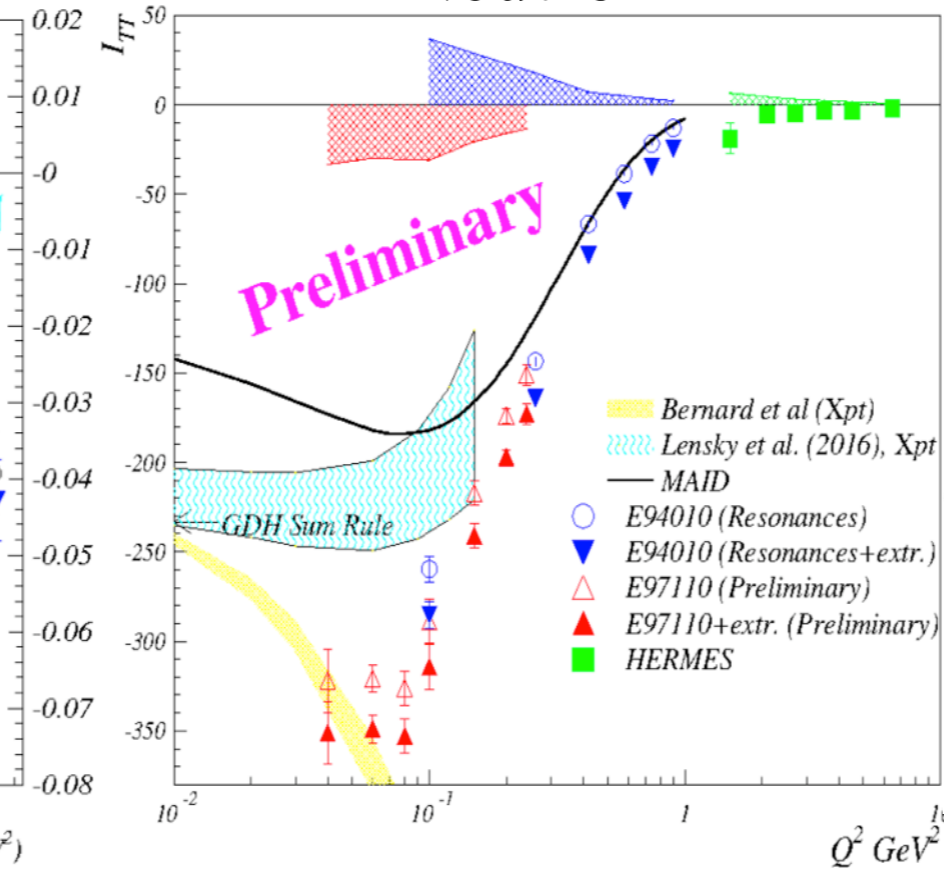
K. Ottnad and C. Alexandrou's talks

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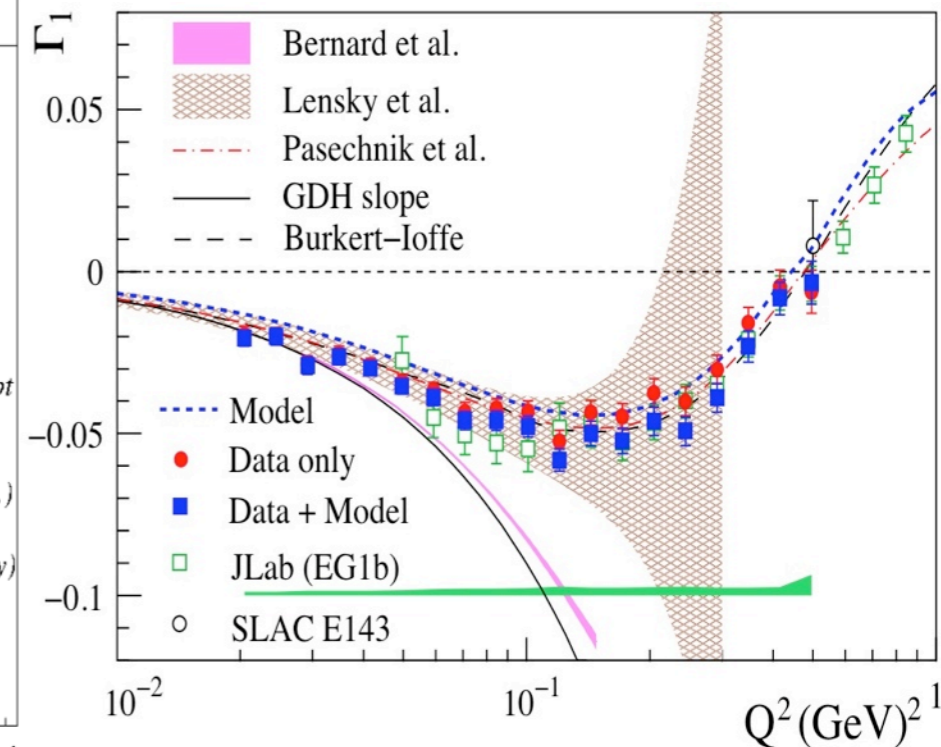
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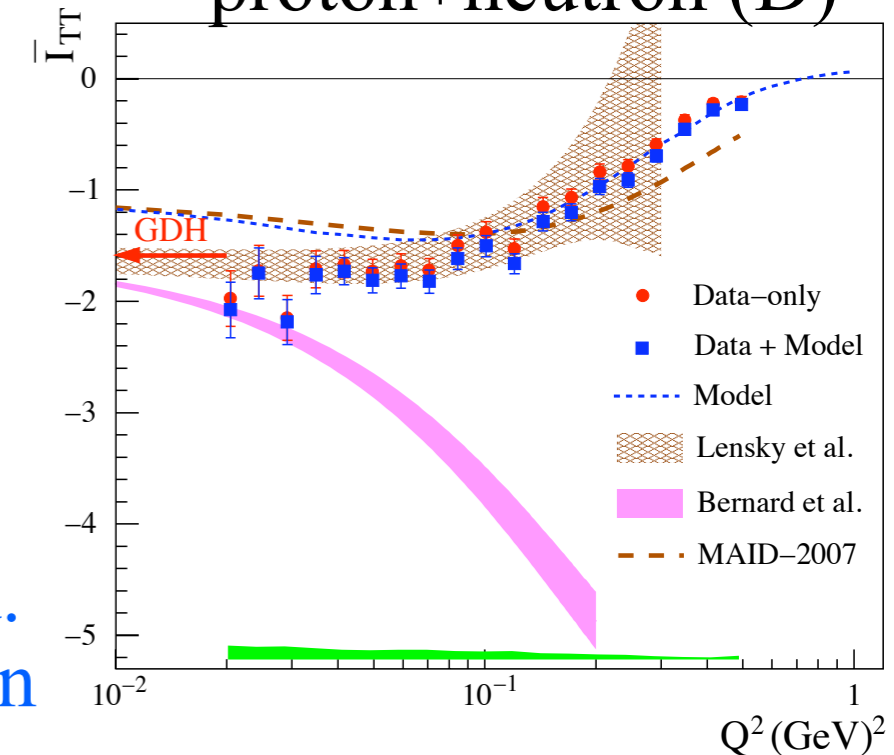
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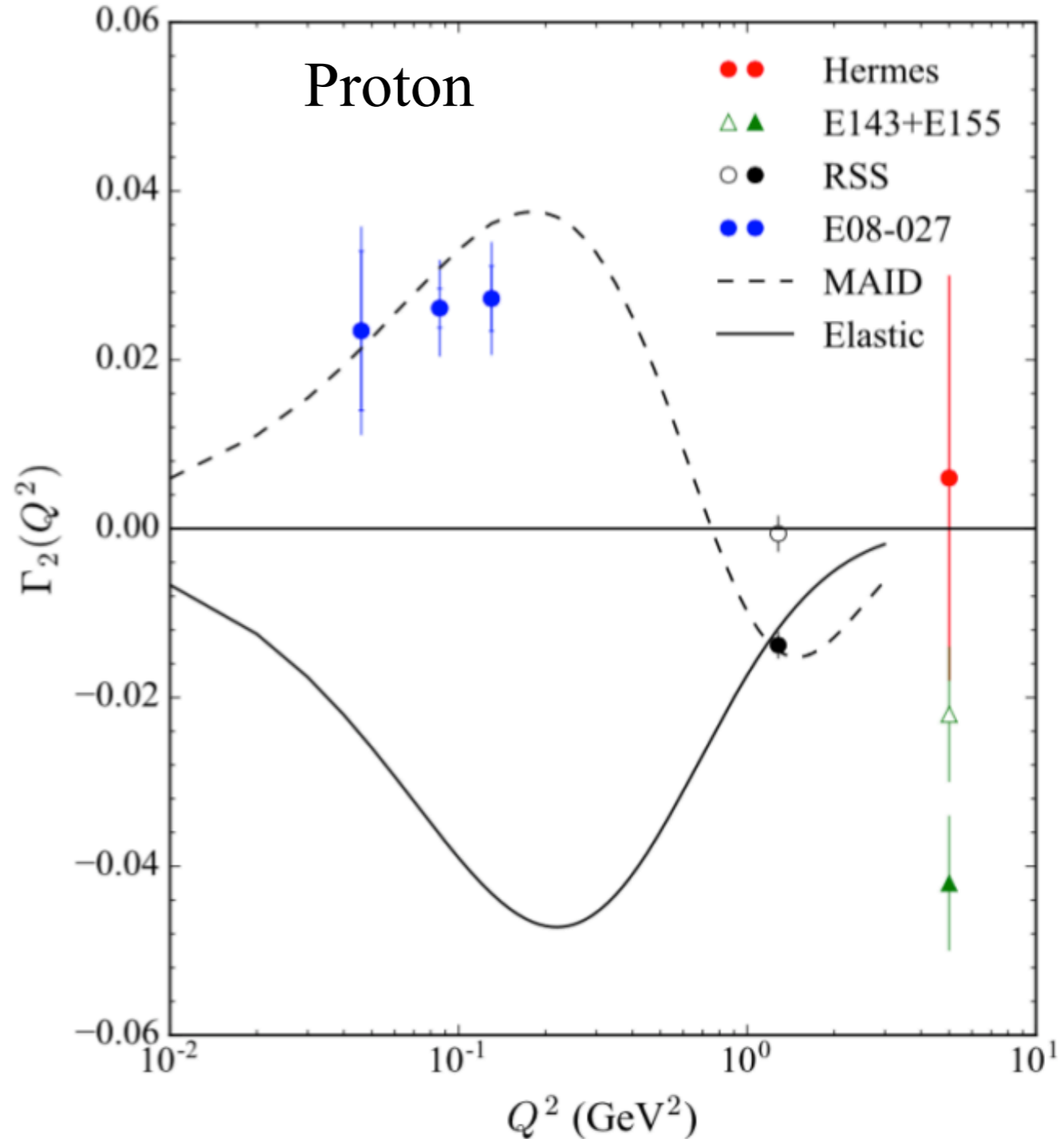
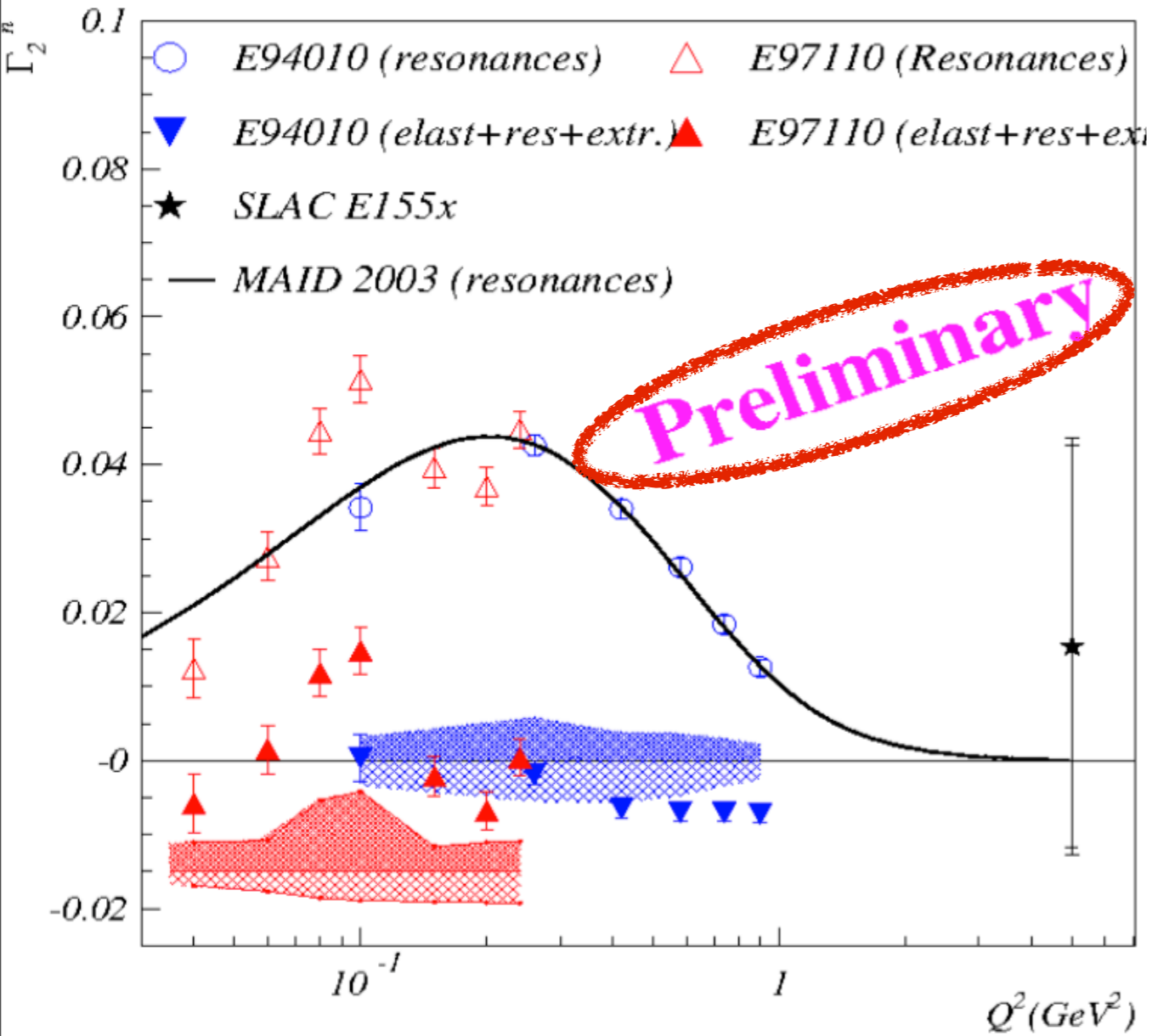
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Full spin decomposition (spin sum rule) at large  $Q^2$ . Axial charges of the nucleon now successfully obtained. Struct. Funct. x-dep: Quasi-PDF: critical development in Lattice QCD. Not applicable at these  $Q^2$ .

H-W Lin and C. Alexandrou's talks

$$\text{BC sum rule: } \Gamma_2 = \int_0^1 g_2 dx = 0$$

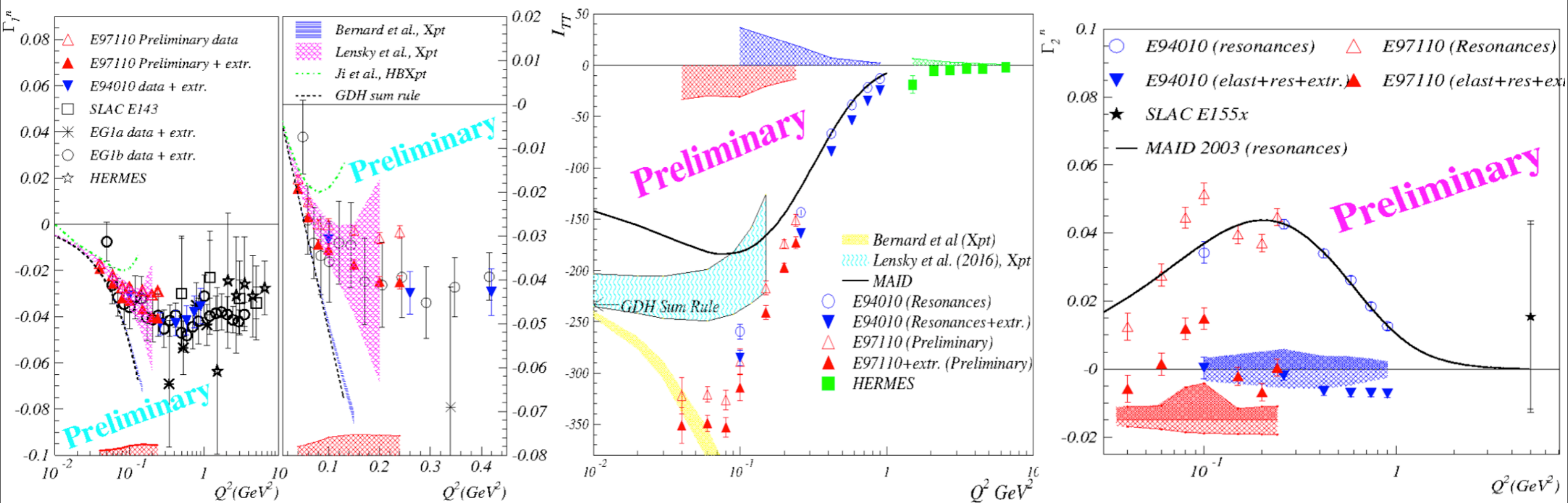
## Neutron



BC sum rule seems valid at low  $Q^2$ .

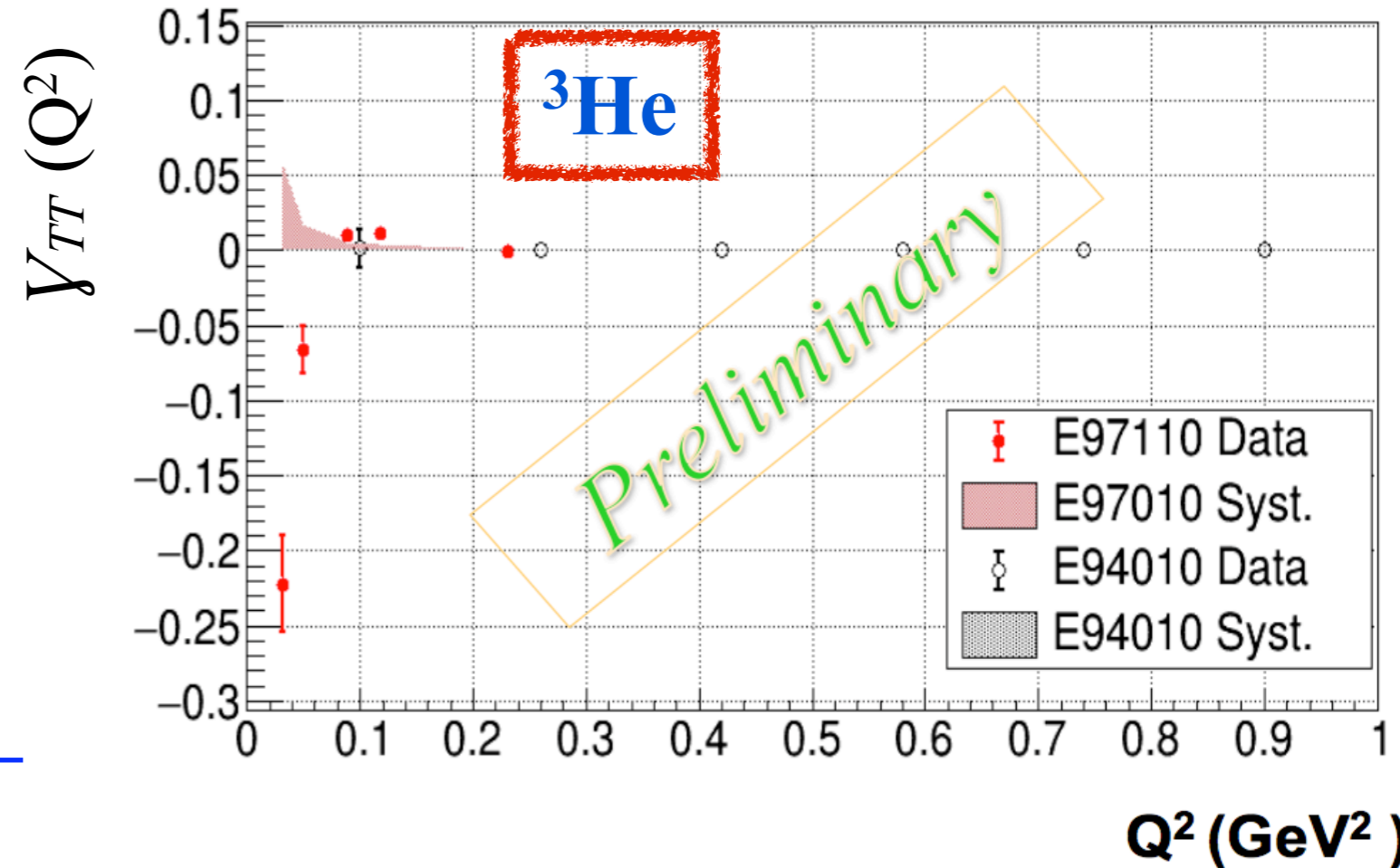
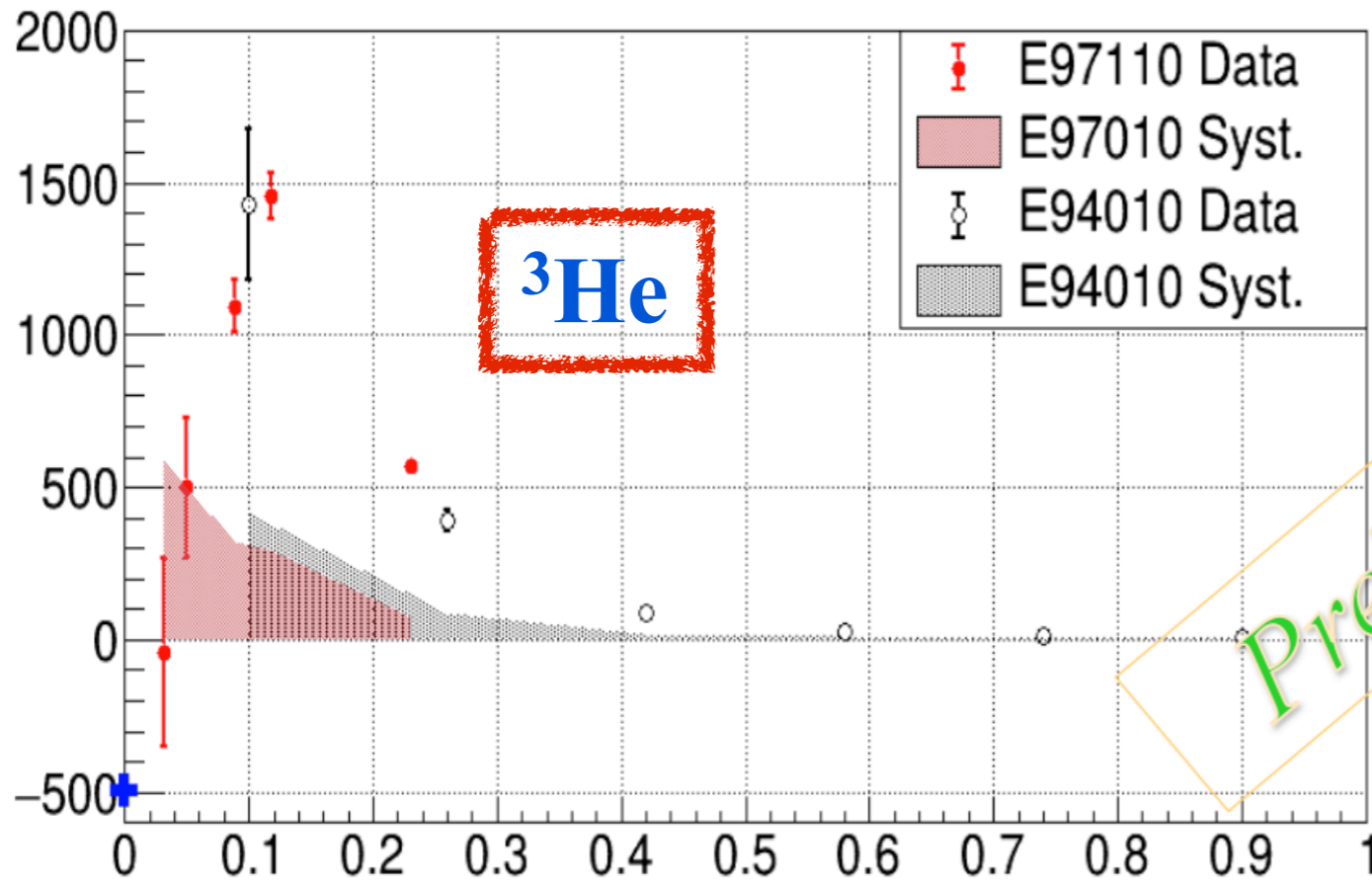
Bump for neutron seems to be due to systematics in interpolation

# Latest developments on low Q spin structure functions and spin polarizabilities.



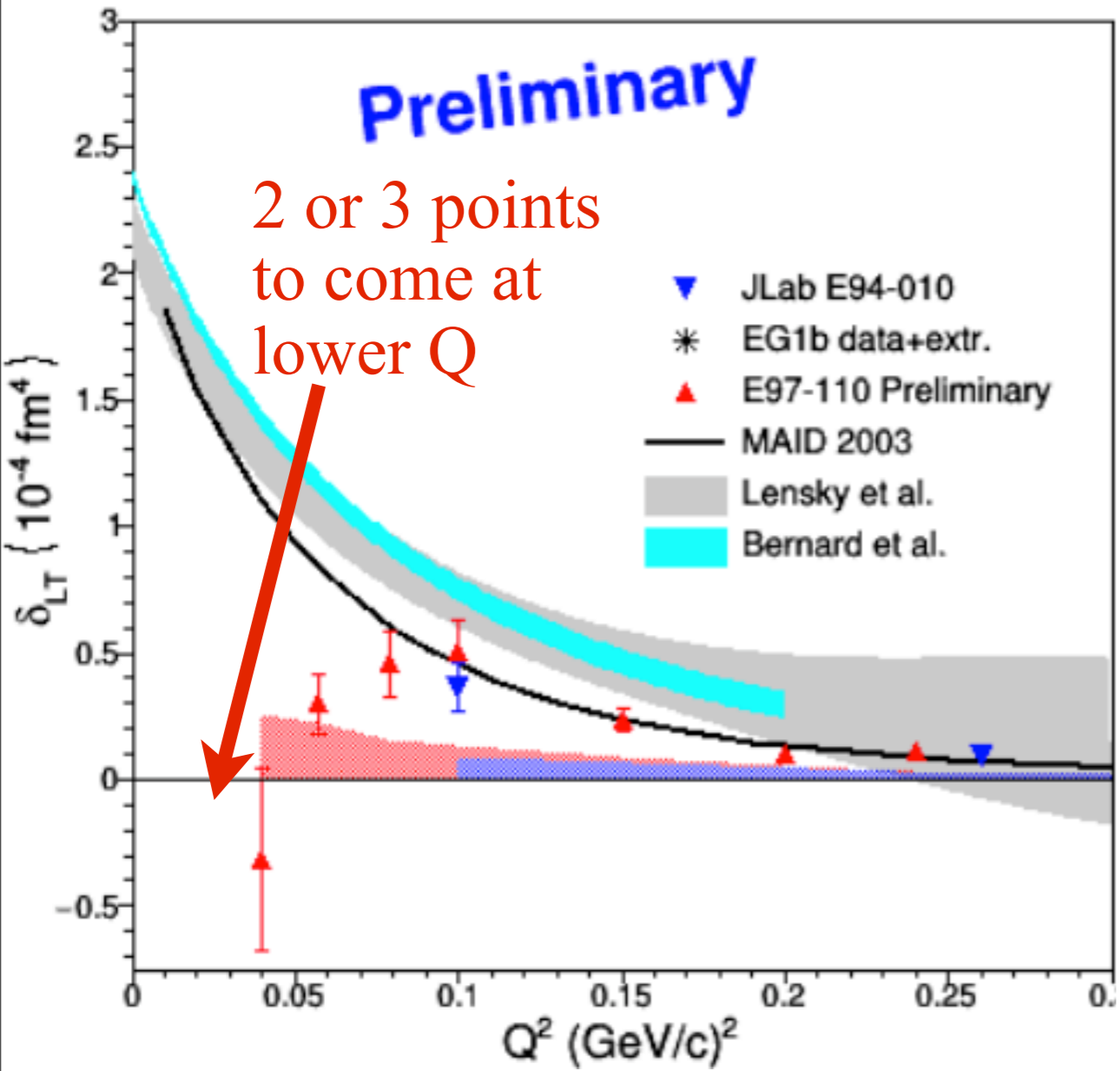
Reliability of extraction of neutron information from  $^3\text{He}$  at very low Q.  
 E. Pace's talk and discussion. Now using Light-Front form approach.  
 E. Pace to revisit 20 year old preliminary estimate on extraction uncertainty.  
 Do the data verify the Schwinger sum rule?

# GDH sum and spin polarizability on $^3\text{He}$ .

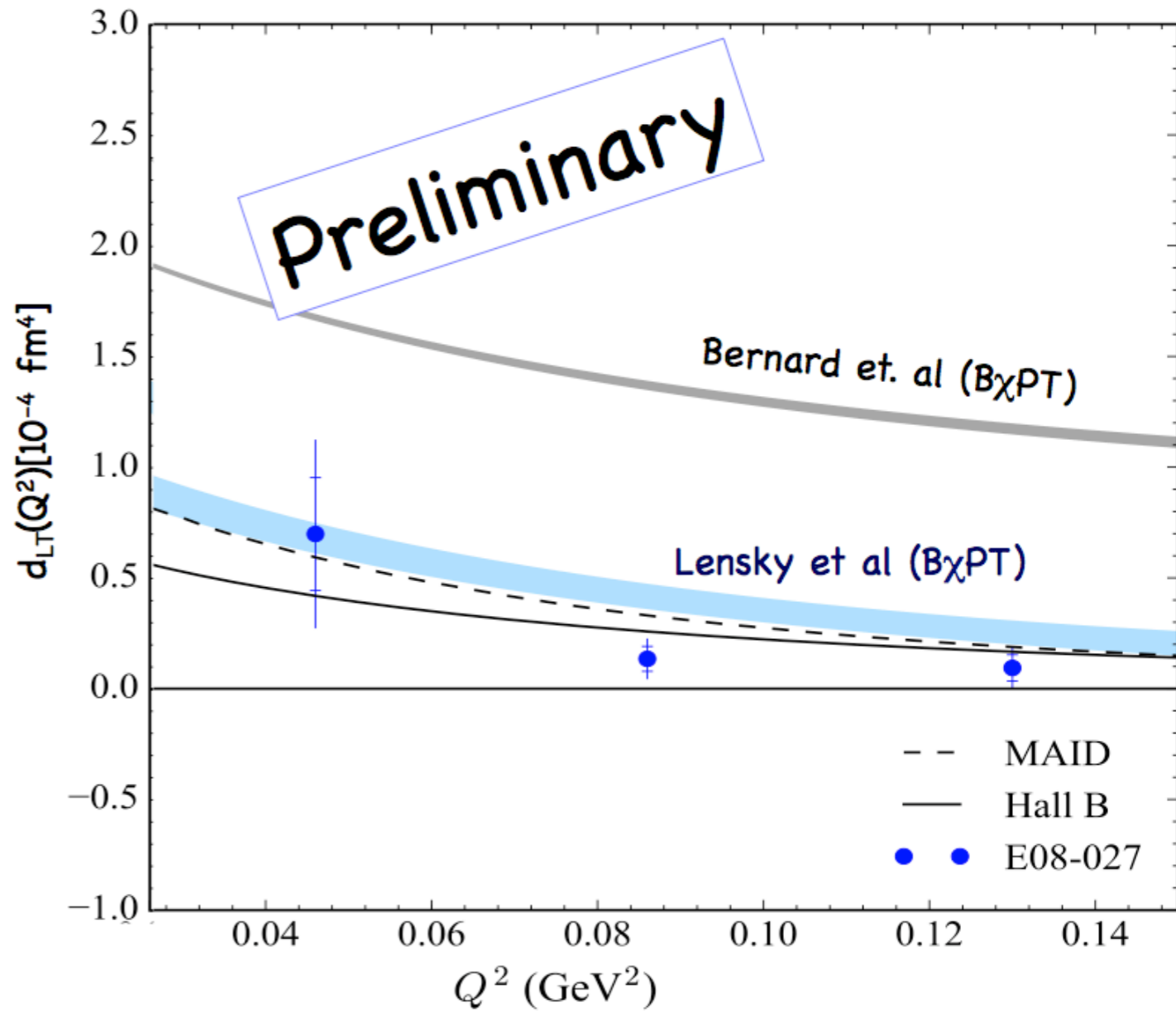


# $\delta_{LT}(Q^2)$ puzzle

Neutron

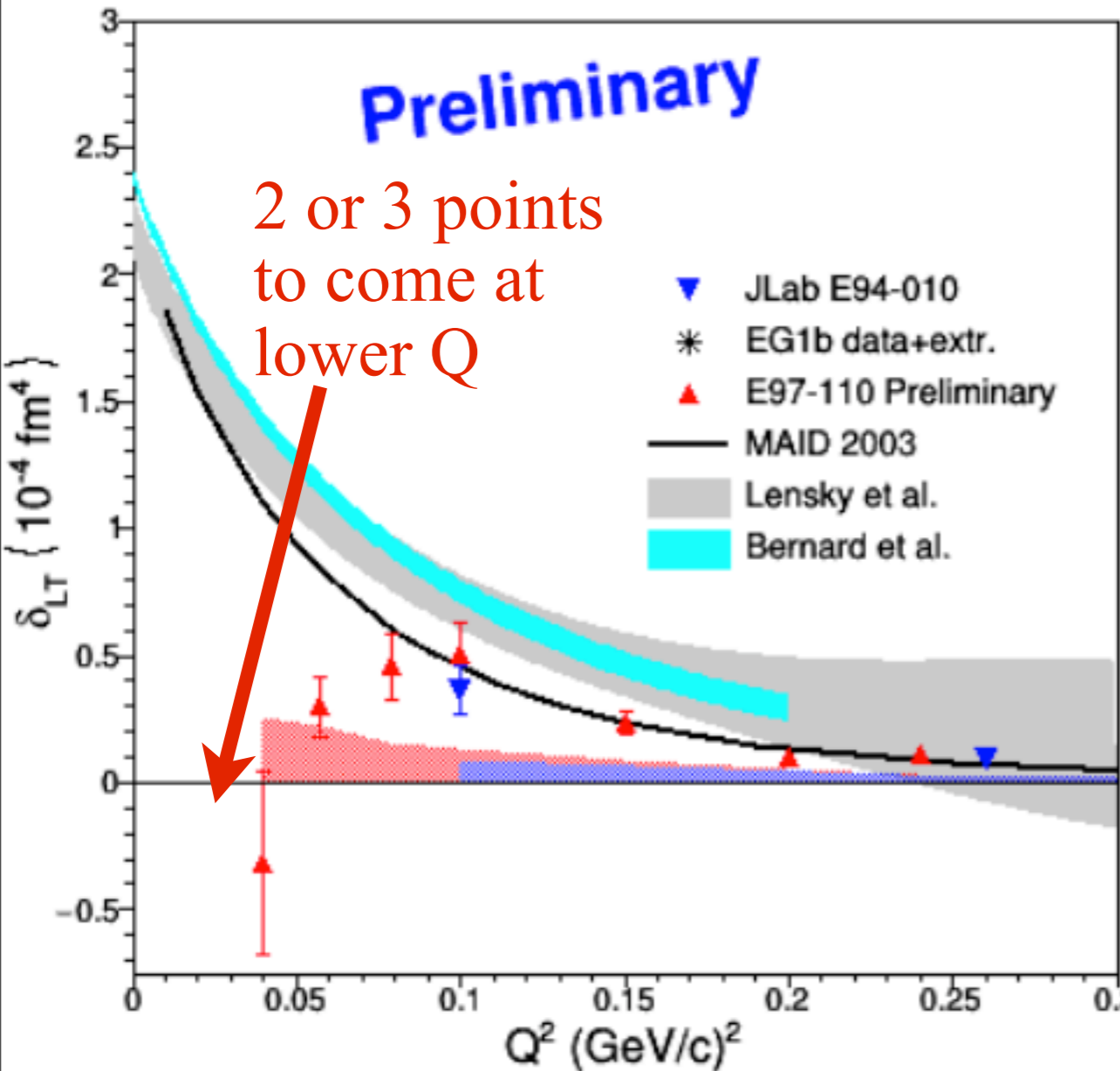


Proton

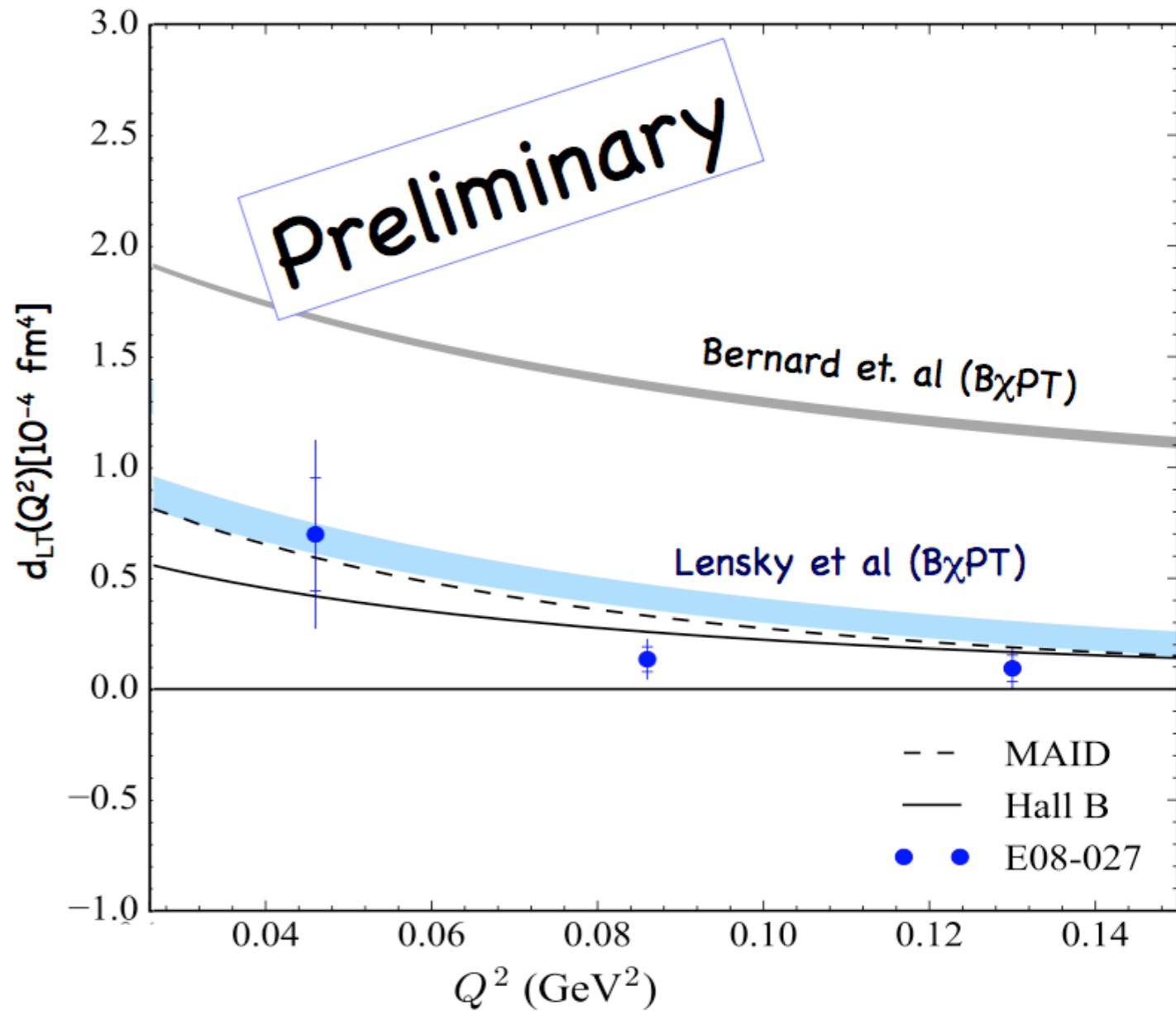


# $\delta_{LT}(Q^2)$ puzzle

Neutron



Proton



Argument that  $\Delta$  does not contribute not exactly true (See V. Pascalutsa's talk).  
 If preliminary analyses confirmed, new  $\delta_{LT}$  puzzle? Consistency with 1-pion production?

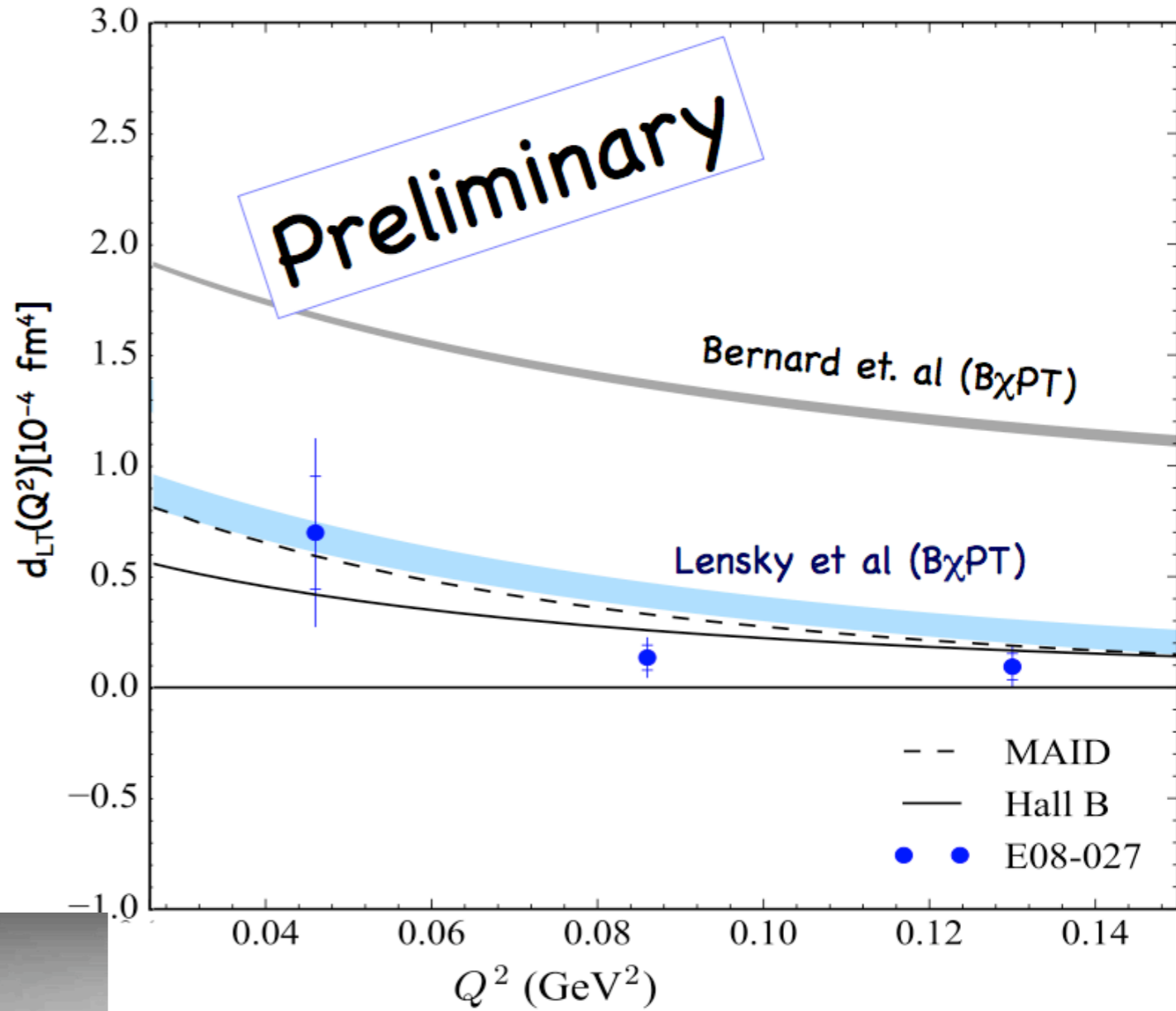
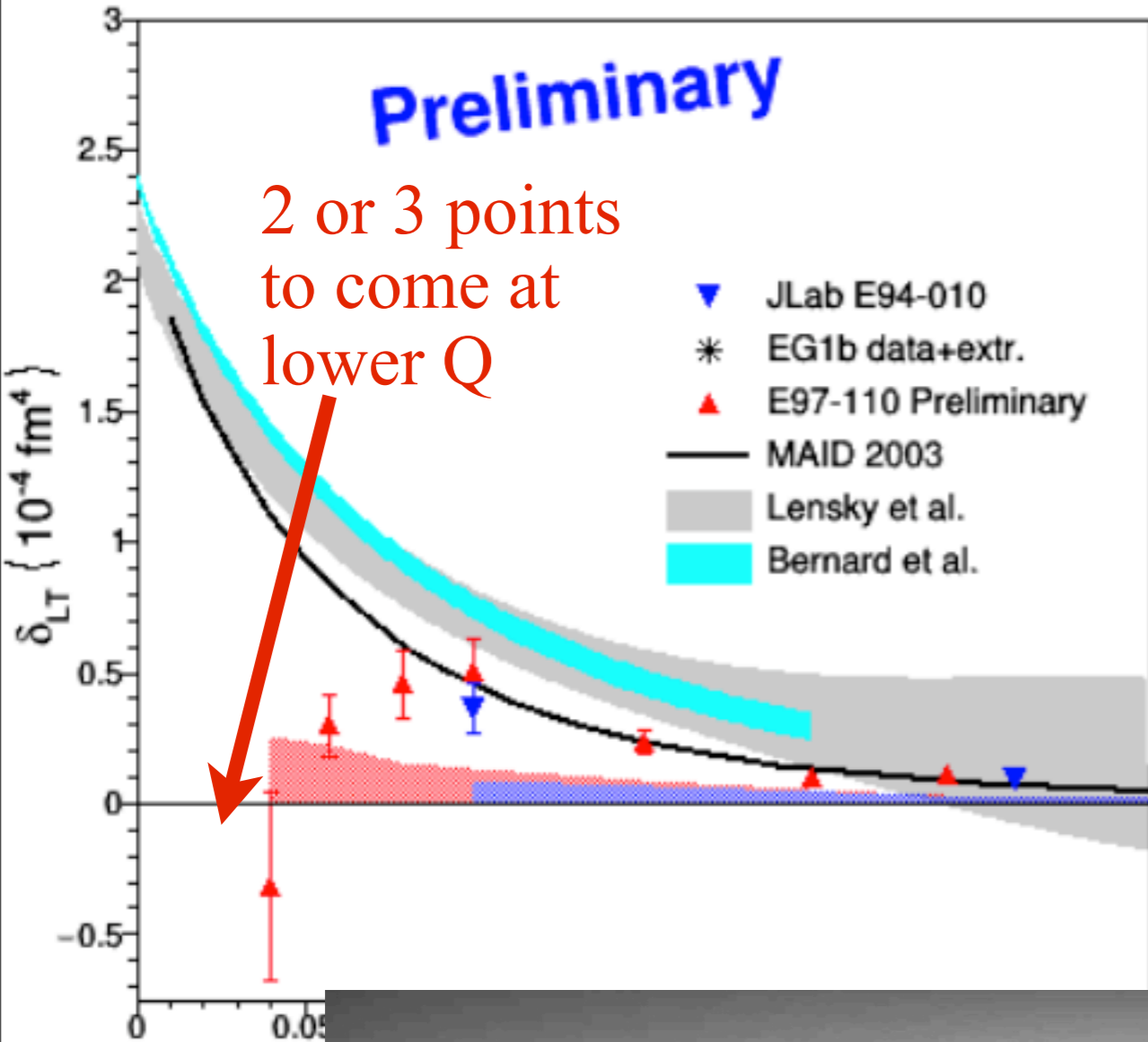
Lensky et al.  $\chi$ EFT calculations and constraints on Lamb shift: V. Lensky's talk.



# $\delta_{LT}(Q^2)$ puzzle

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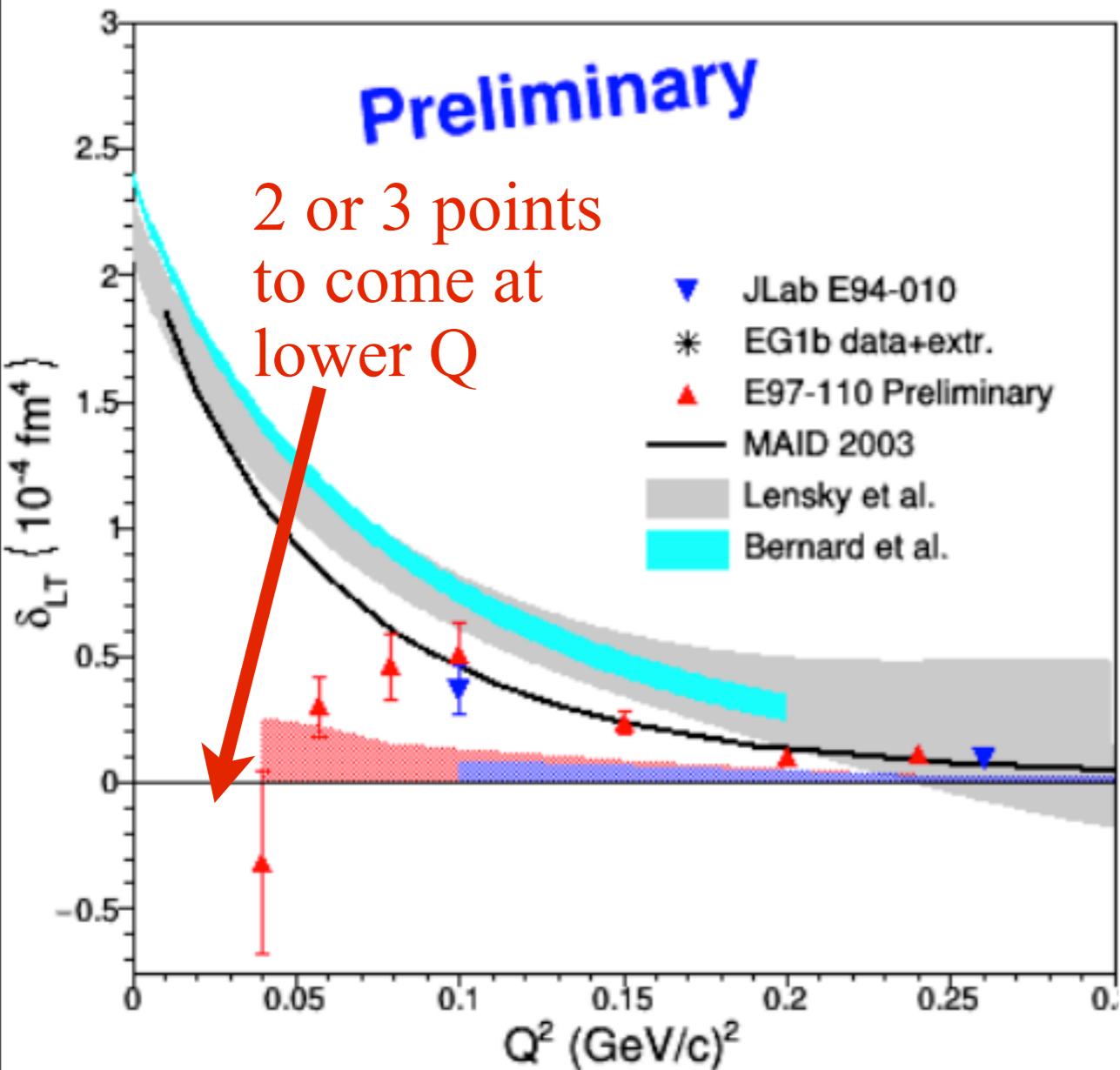
Proton



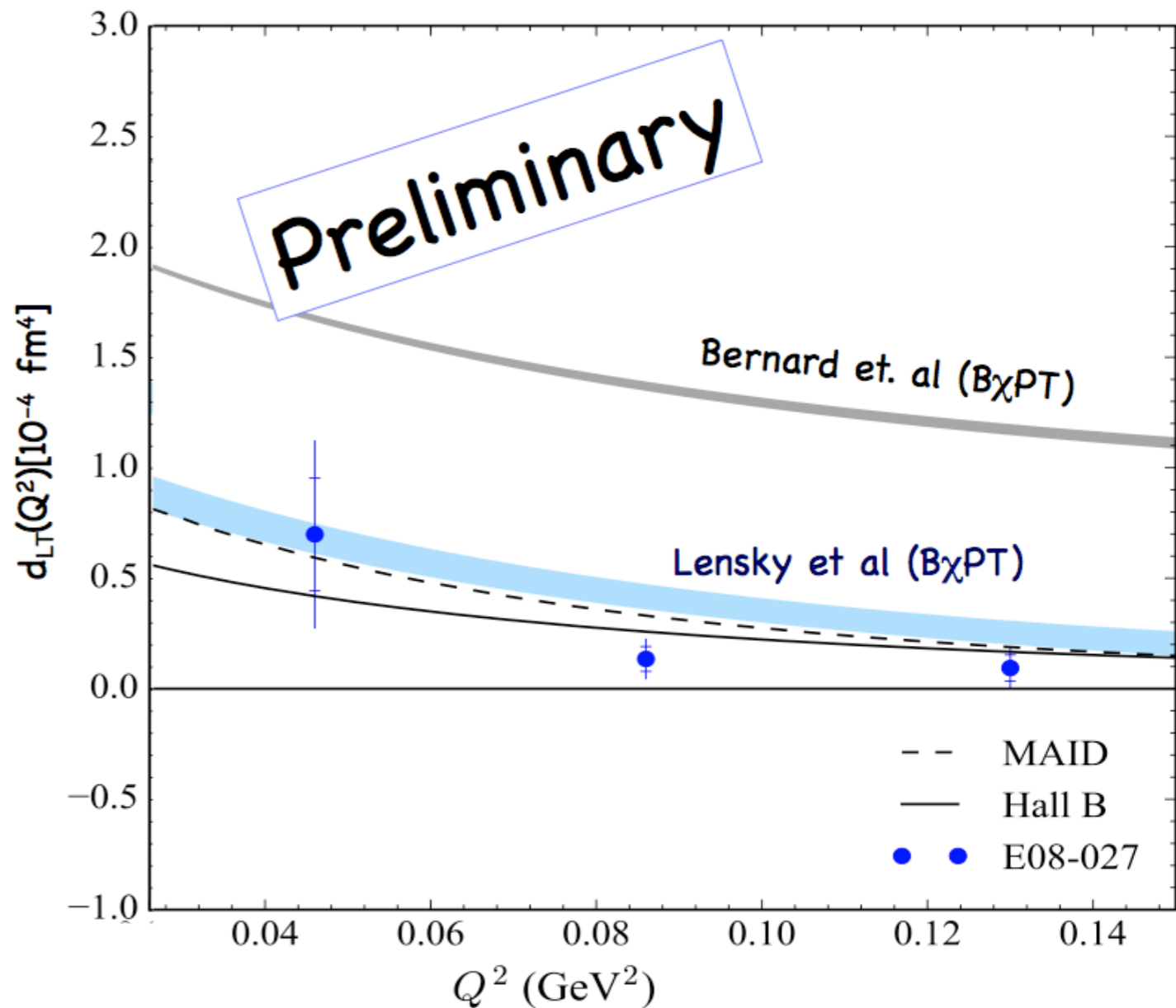
Now,  $\chi$ EFT calculations work at at large  $Q^2$  only !

# $\delta_{LT}(Q^2)$ puzzle

Neutron



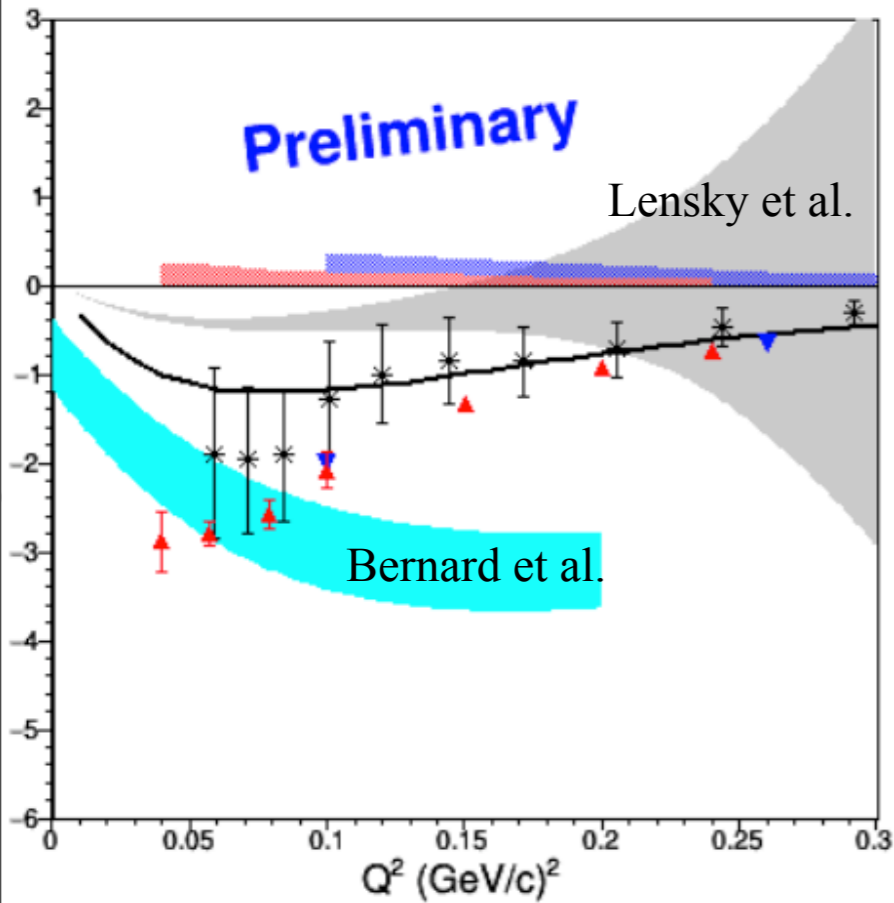
Proton



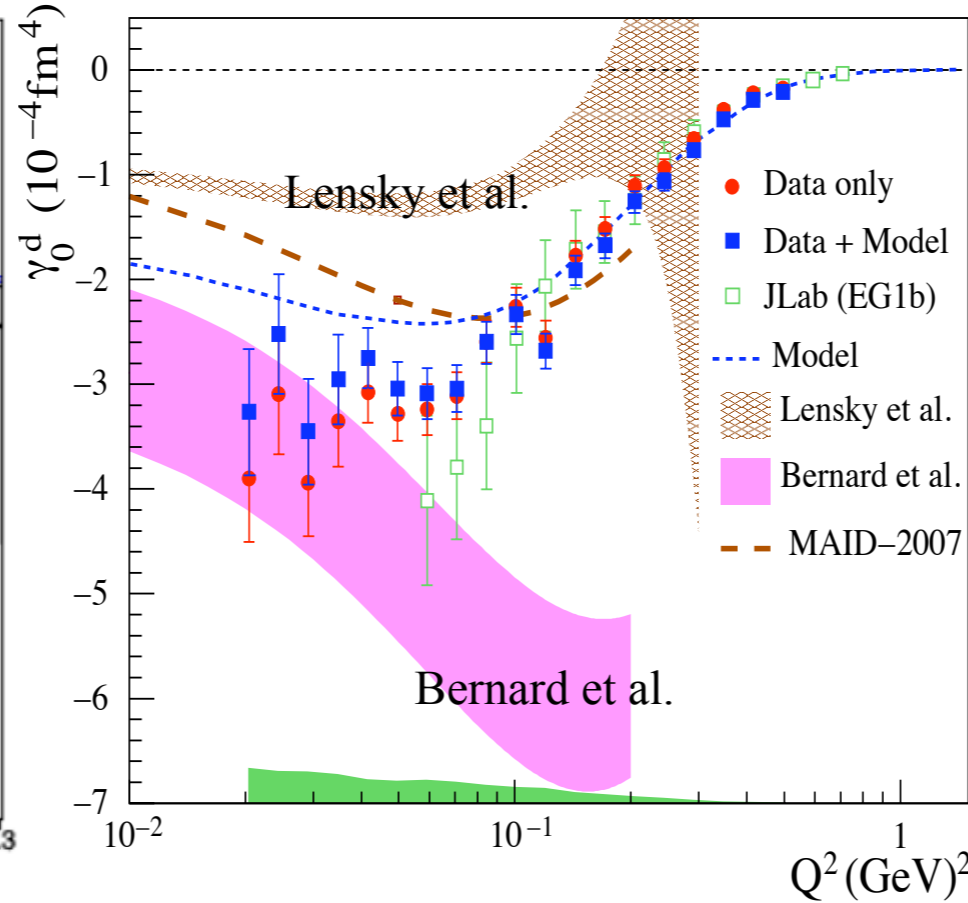
Showing running integrals is useful, see K. Slifer's talk. TBD for neutron and  $^3\text{He}$ .

# Generalized forward spin polarizability $\gamma_0$ on nucleons

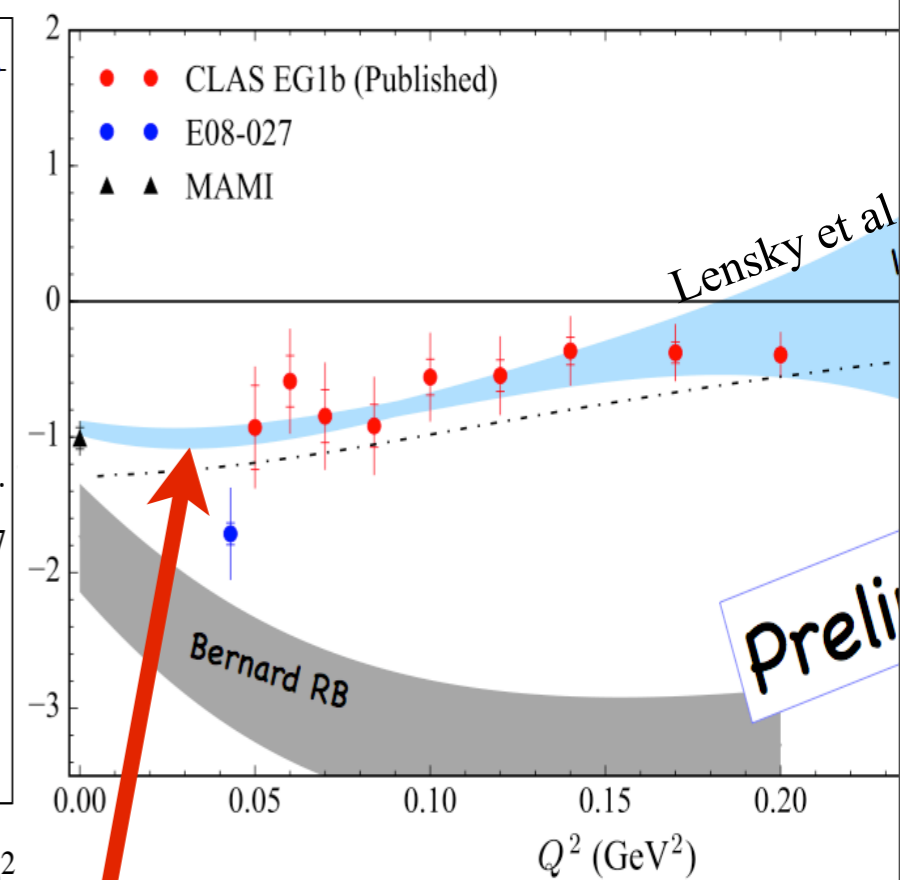
$\gamma_0$  Neutron



$\sim$ proton+neutron



Proton

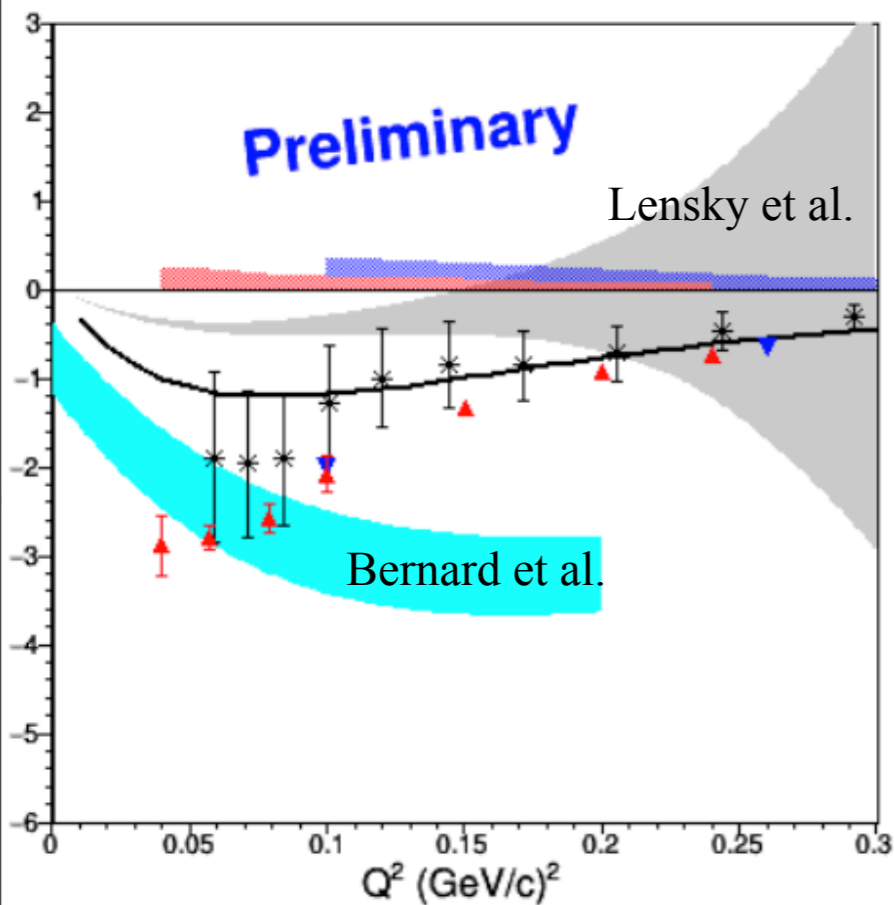


EG4 data  
to come

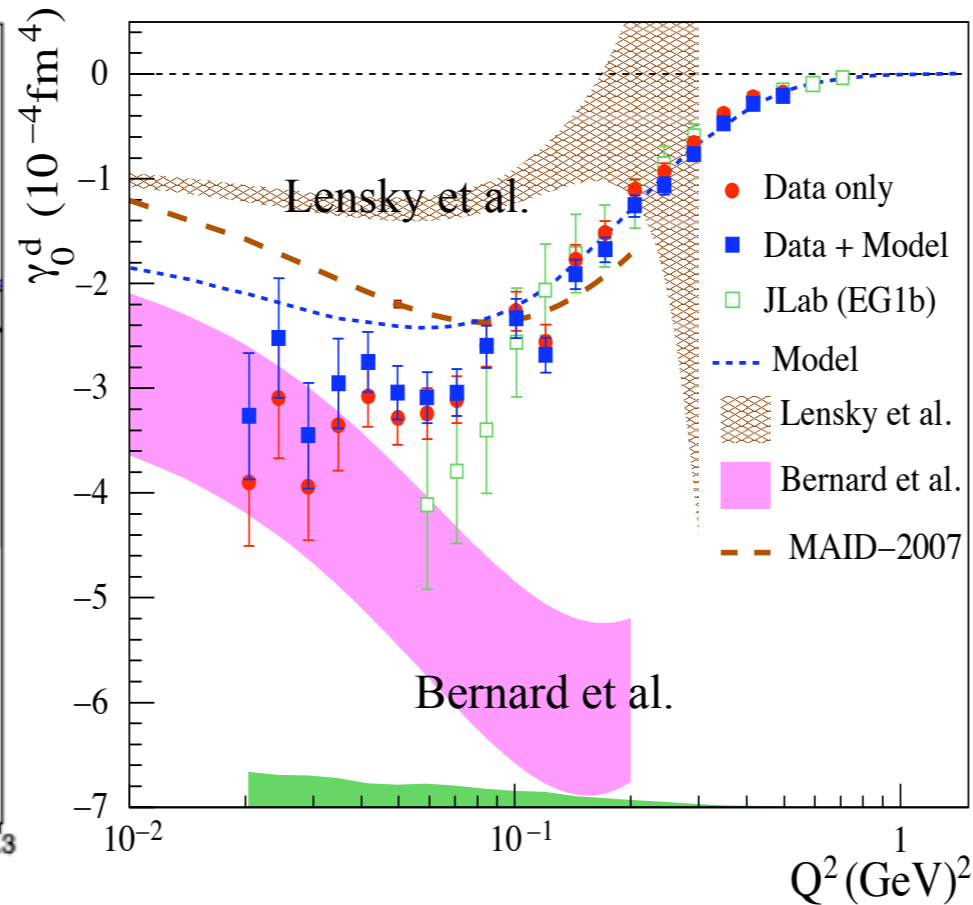
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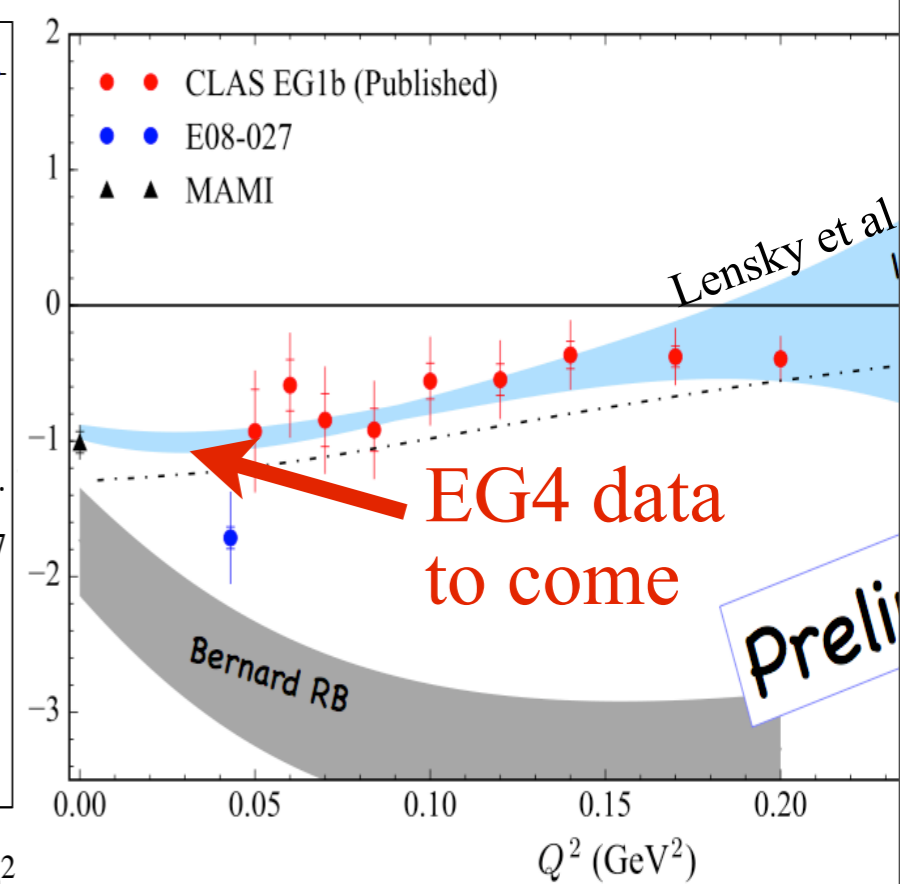
$\gamma_0$  Neutron



$\sim$ proton+neutron



Proton



Lensky et al.  $\chi$ EFT describes proton at larger  $Q^2$  and  $Q^2=0$ . Situation unclear in between. Disagreement for neutron and neutron+proton.  
Bernard et al.  $\chi$ EFT describes  $\gamma_0$  neutron and neutron+proton.

$\Rightarrow$  Need detailed comparison between exp. data sets.  
Need EG4 proton data to clarify situation.

## Latest developments on polarizabilities.

Photon point ( $Q=0$ ). Second order reaction to photon probe (nucleon deformation)  
Can be generalized to  $Q>0$ .

Calculated in  $\chi$ EFT (V. Lensky's talk)

New method for data analysis developed (See talk by S. Sconfiatti)

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Several nice cartoons of what polarizabilities are.

Personal\* request: cartoon for **generalized** polarizabilities.

\*So that Jian-Ping doesn't have to explain me every 2 months what they mean.

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New MAMI experiments in A1 and A2 (ran already).

# Latest developments on polarizabilities.

New MAMI experiments in A1 and A2 (ran already). Polarizabilities:  $\Sigma_{2x}$  results and  $\Sigma_{2x,2z,3}$  preliminary results (P. Martel's talk). Ex:  $\Sigma_3$

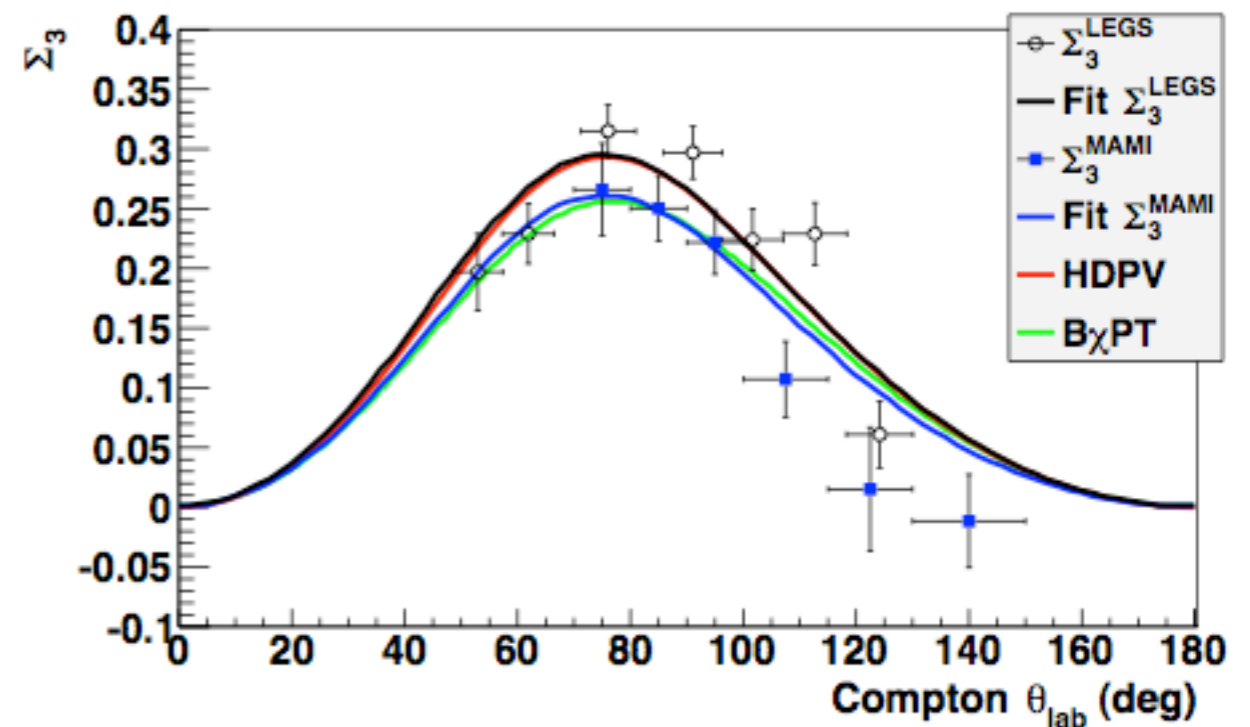
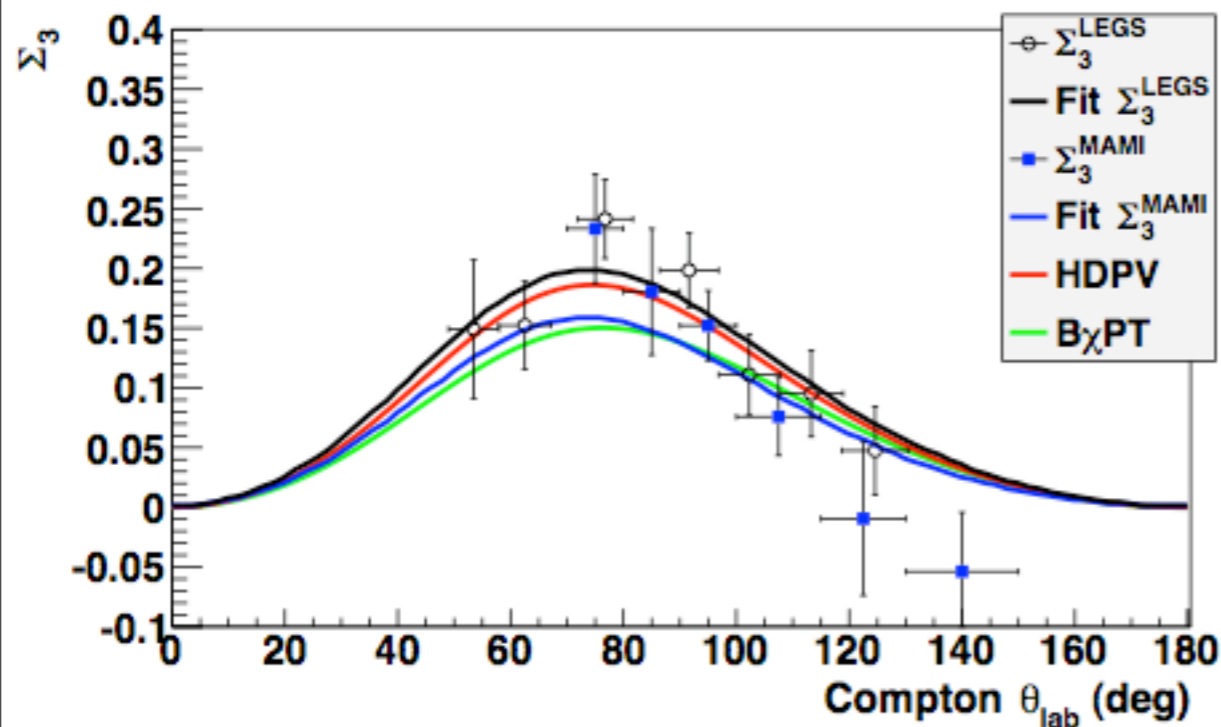
- Linearly polarized photons, unpolarized protons.

$$\Sigma_3 = \frac{N_{\parallel} - N_{\perp}}{N_{\parallel} + N_{\perp}}$$



$E_{\gamma} = 267-287$  MeV

$E_{\gamma} = 287-307$  MeV

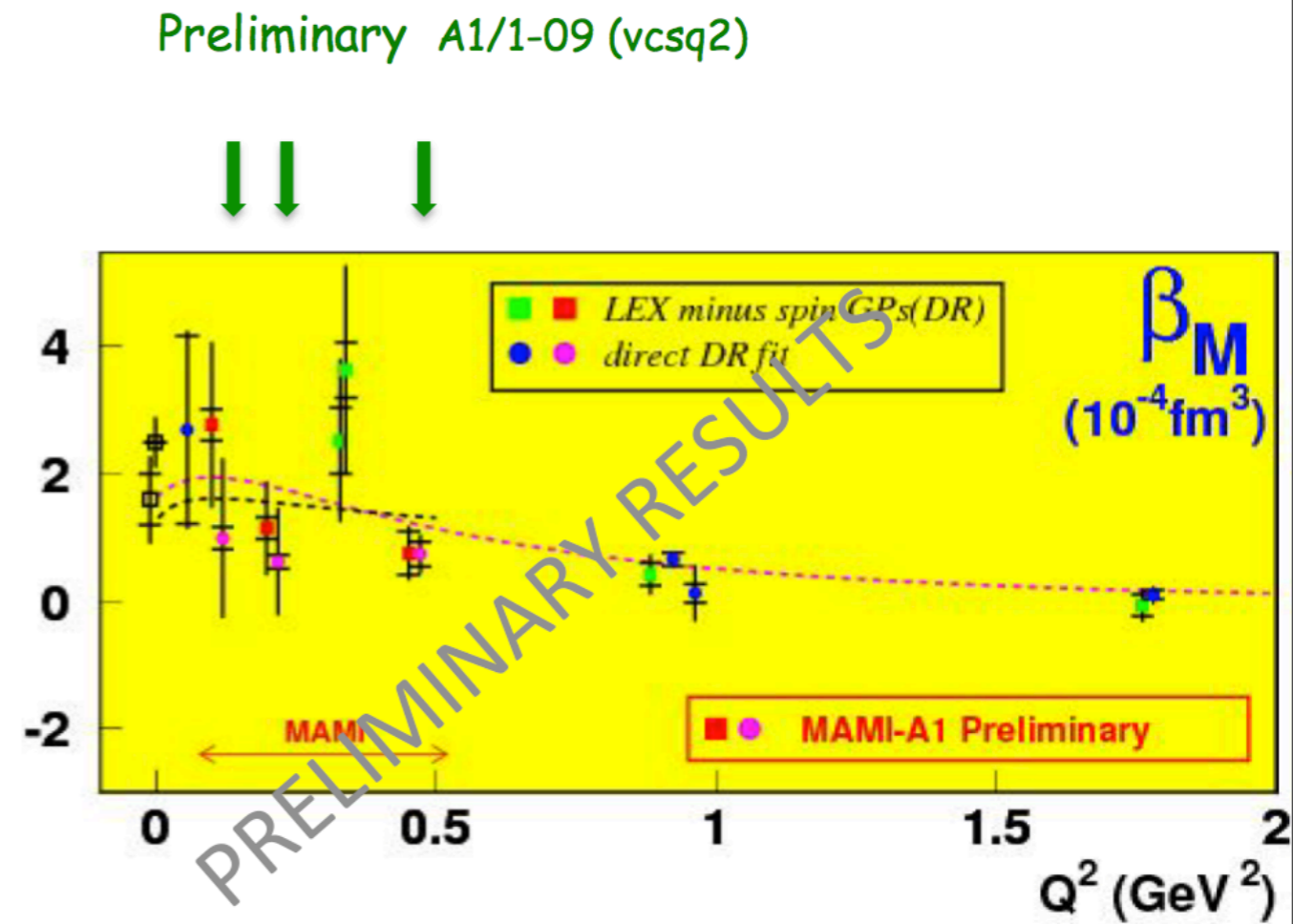
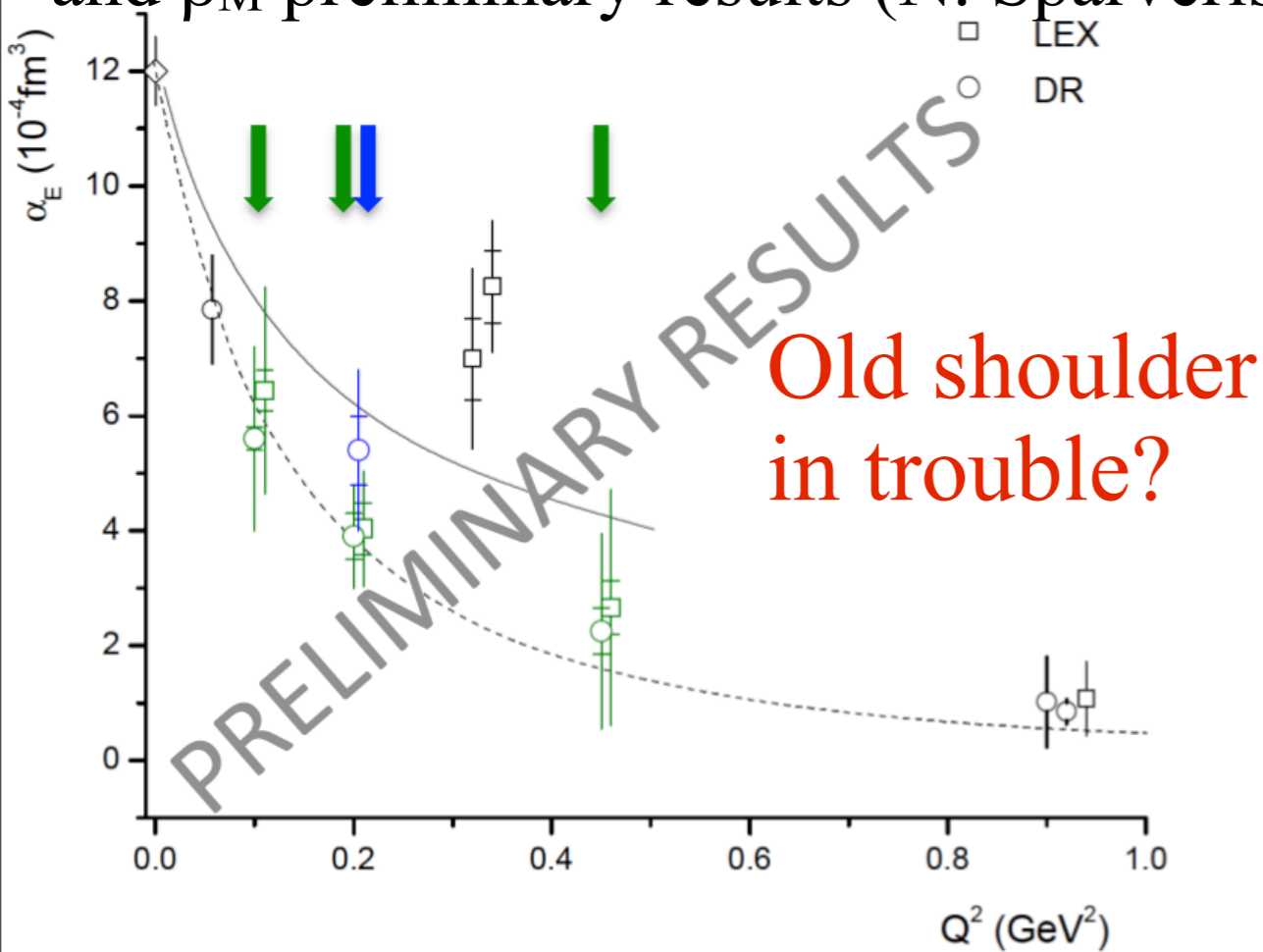


V. Lensky and V. Pascalutsa are developing model-indep. PWA approach to obtain these data.



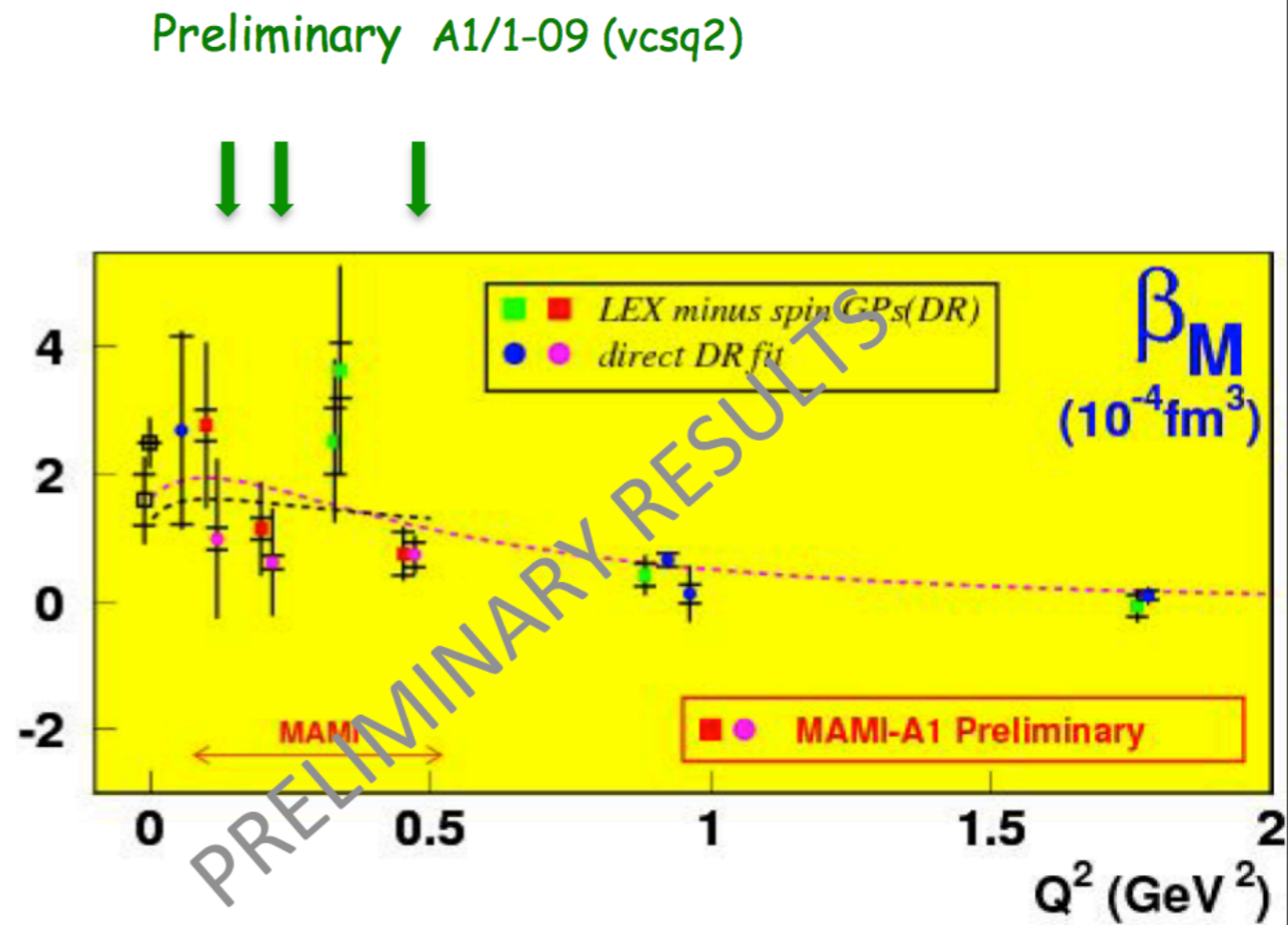
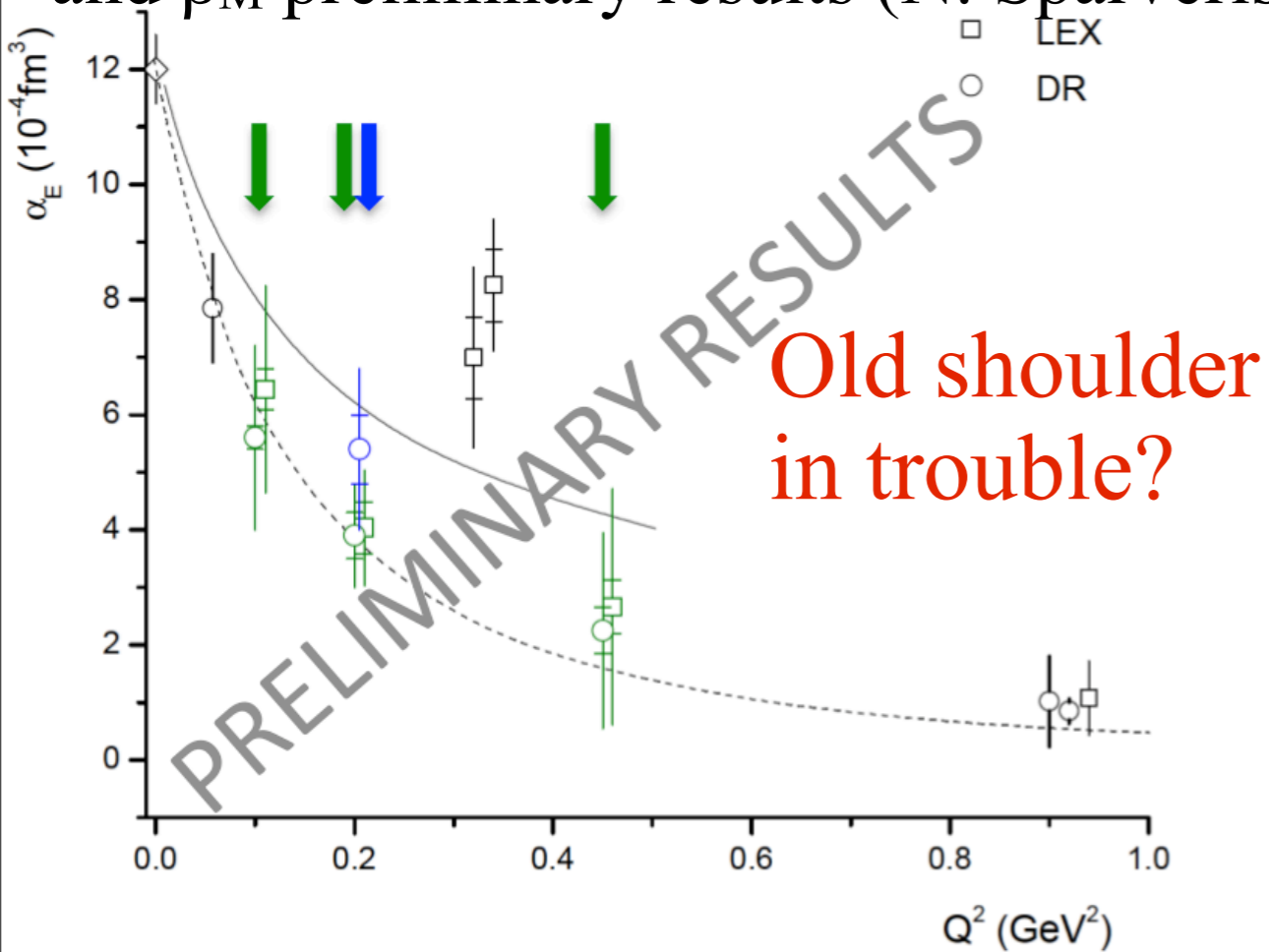
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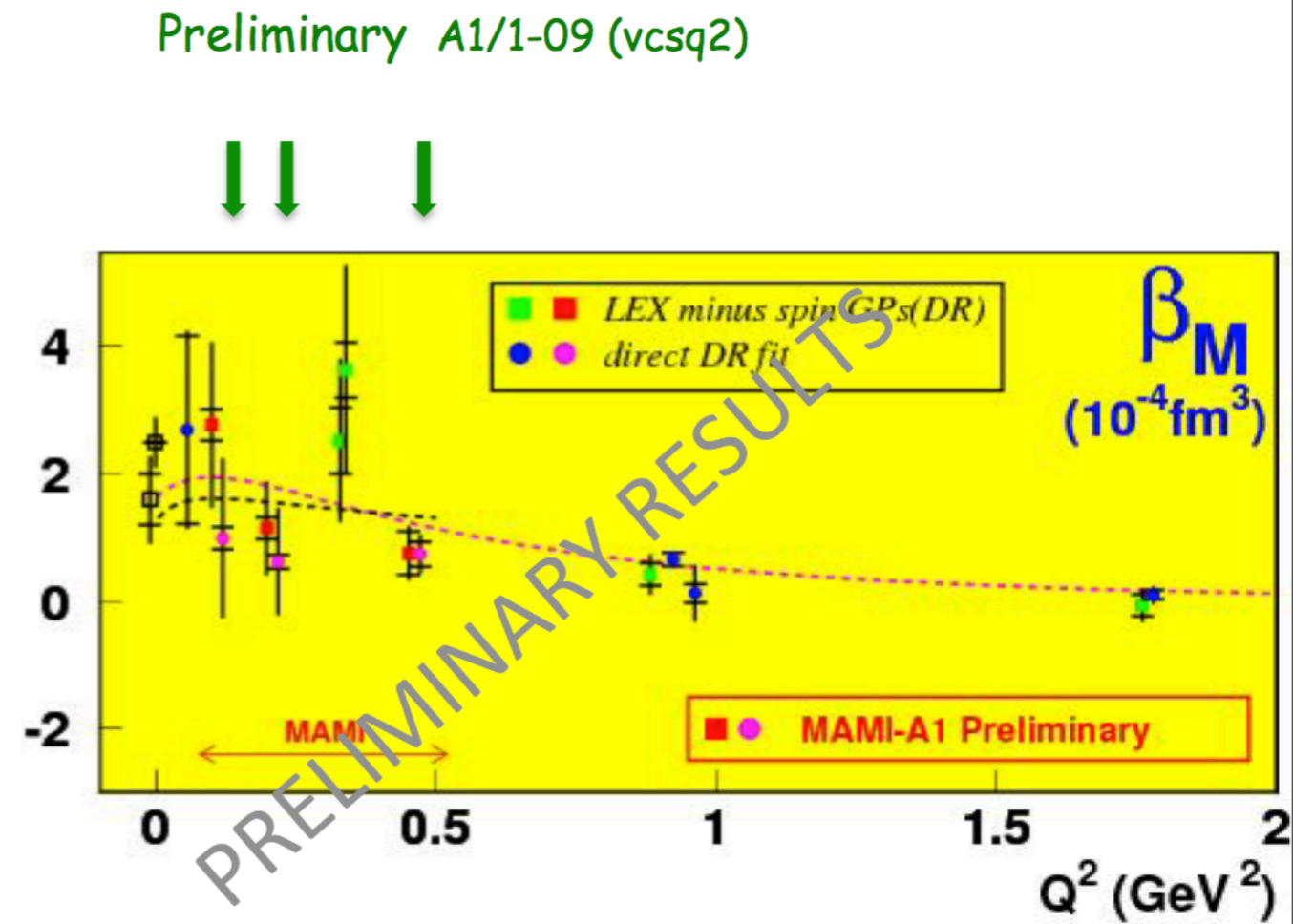
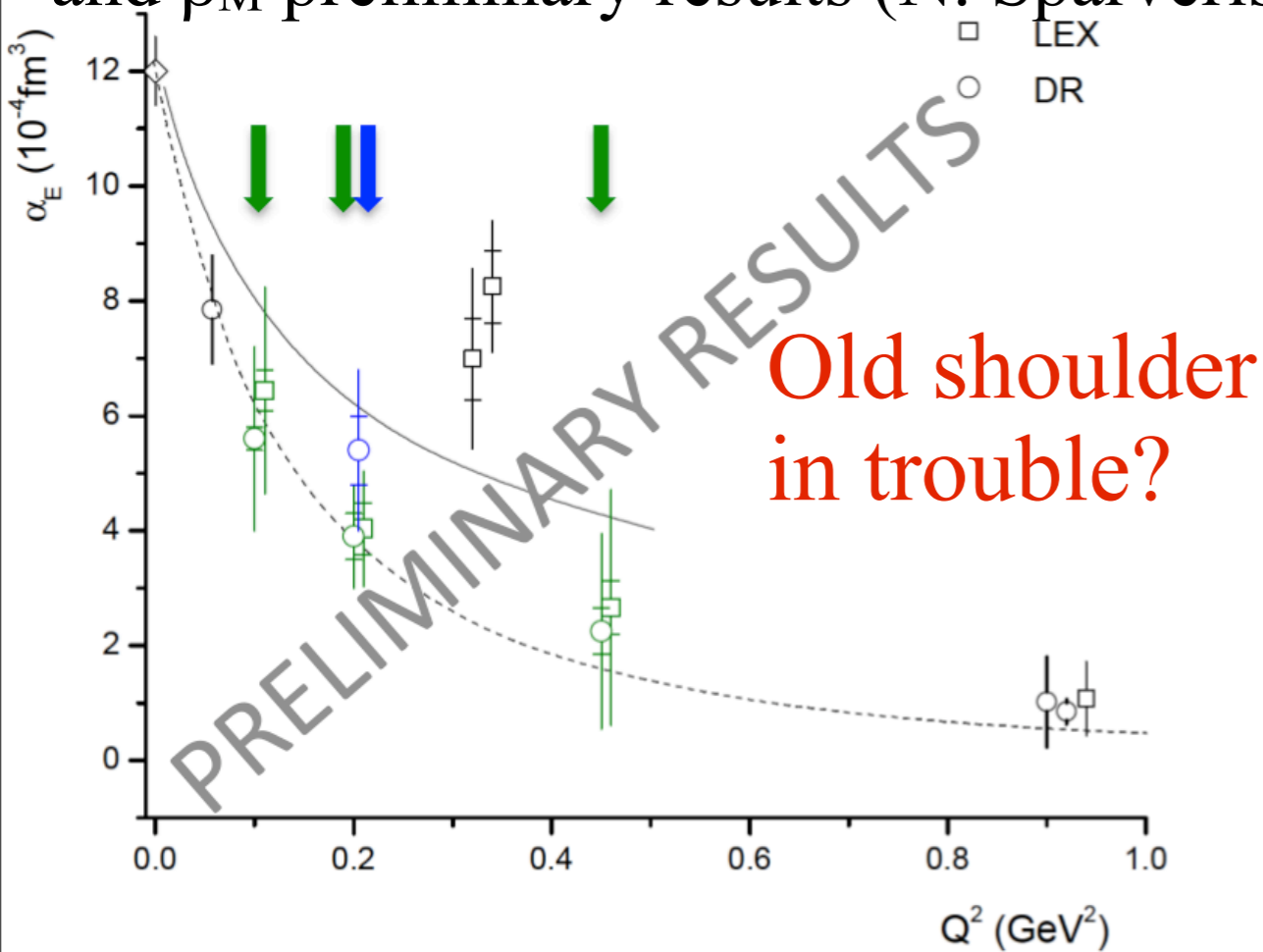
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1 new JLab experiments (to be run in 2019). Will start at  $Q^2 \sim 0.3 \text{ GeV}^2$ .

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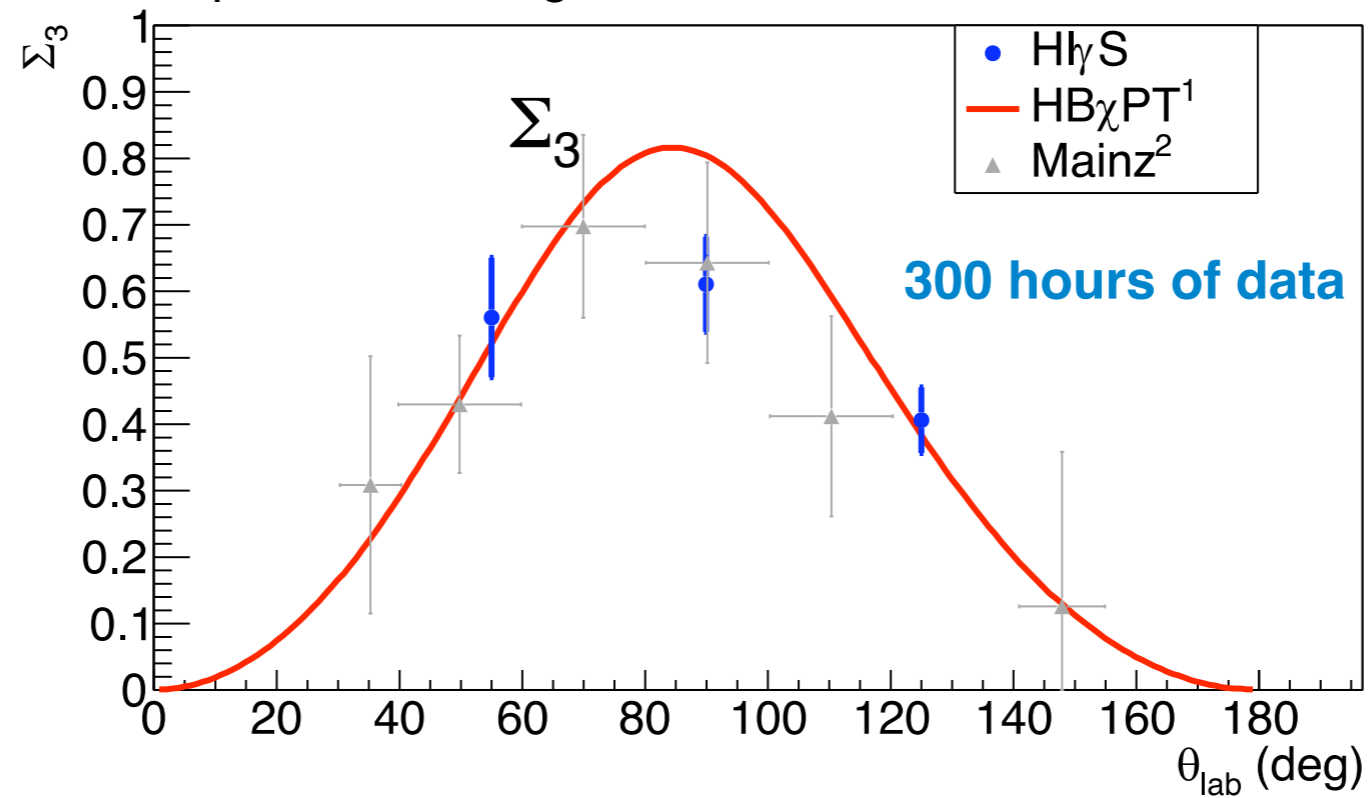
1 new JLab experiments (to be run in 2019). Will start at  $Q^2 \sim 0.3 \text{ GeV}^2$ .

“Old” MAMI data re-analyzed using same analysis method as more recent data.

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RCS experiments at HIGS (M. Ahmed's talk). Proton and light nuclei.

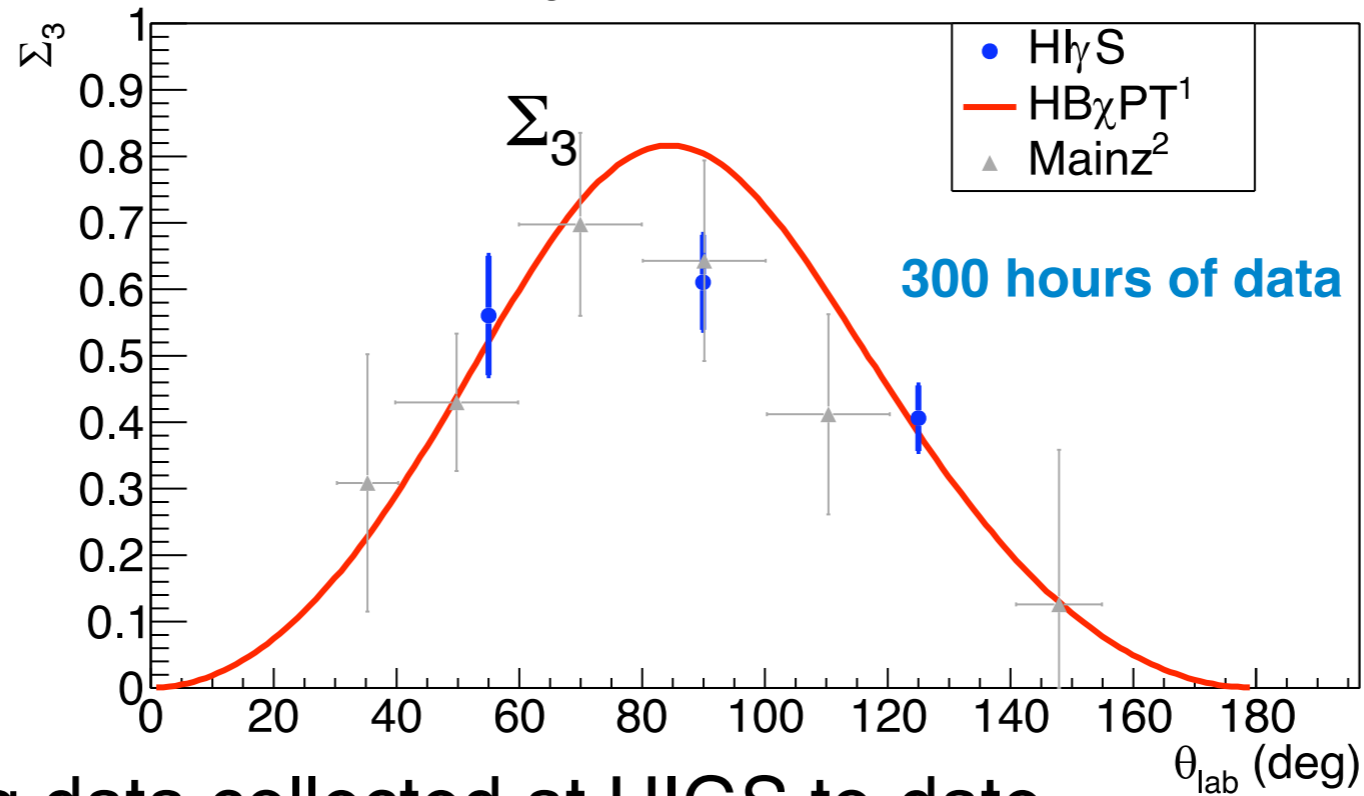
Proton Compton Scattering at 85 MeV with Circular & **Linear** Polarization



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Compton Scattering data collected at HIGS to-date

Target	Z	A	$E_\gamma$ [MeV]	40°	55°	75°	90°	110°	125°	145°	159°
Hydrogen	1	1	84		X		X		X		
Deuterium	1	2	65	X	X	X	X	X	X	X	X
			85	X	X	X	X	X	X	X	X
Helium-4	2	4	61	X	X	X		X	X	X	X
			84		X		X		X		
Lithium-6	3	6	60	X	X	X	X	X	X	X	X
			86	X	X	X	X	X		X	X
Oxygen-16	8	16	60	X	X	X	X	X	X	X	X
			86	X	X	X	X	X		X	X

Plans for next 3 years:  
<sup>3</sup>He/D Compton Scattering

Will double world data on  
D polarizabilities.

## Latest developments on nucleon form factors.

Hot topic: Proton radius crisis, Zemach radius, TPE...

A. Gasparian's talk. Proton radius from PRAD in a few weeks.

Not subject of this workshop but:

Proton radius puzzle remains mysterious, with apparently contradictory measurements

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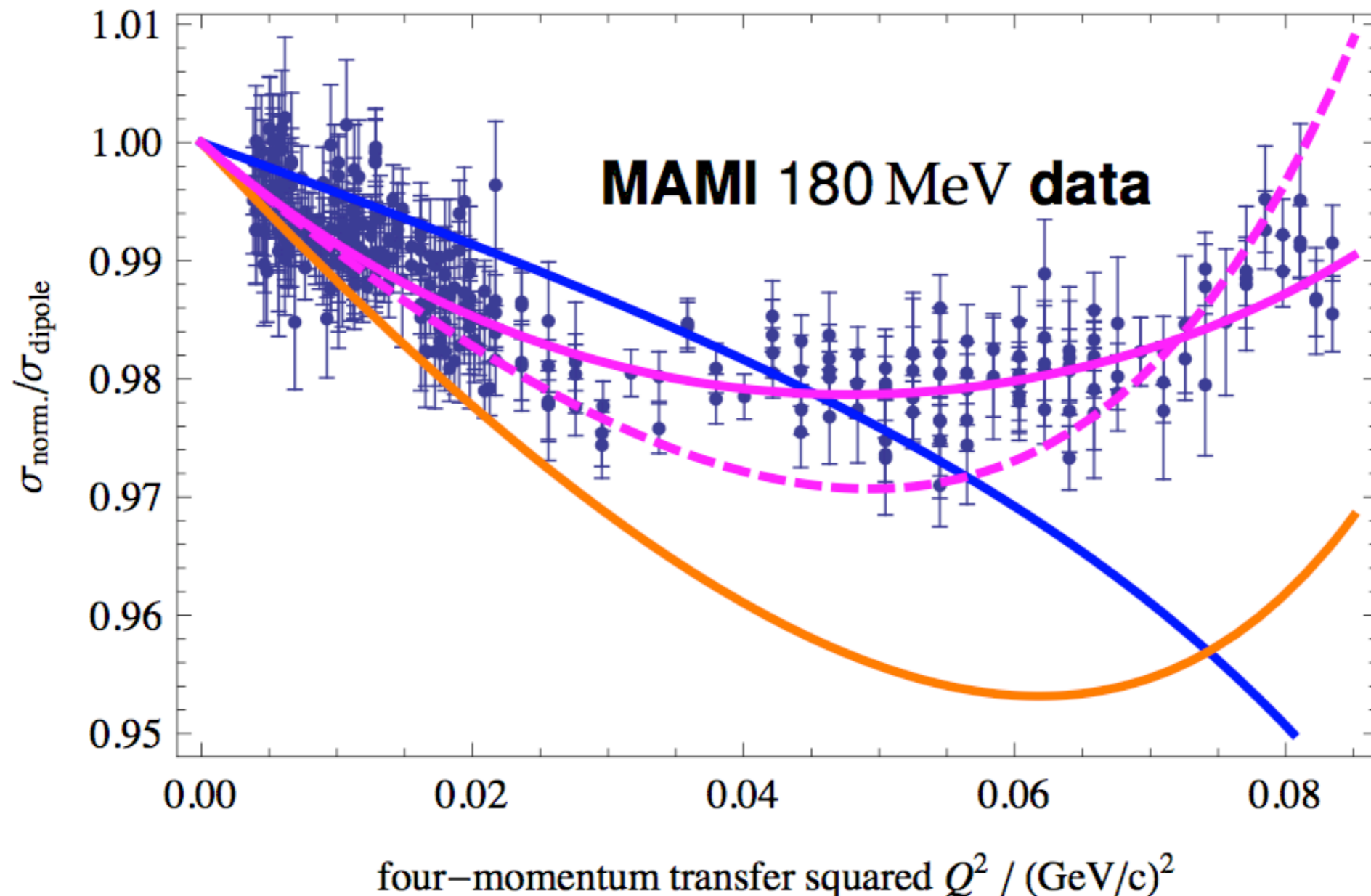
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Consistency check with more recent FF data and direct TPE meas. from other labs.

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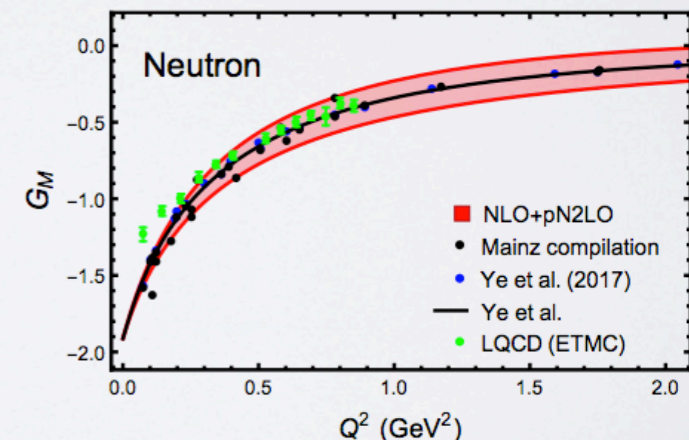
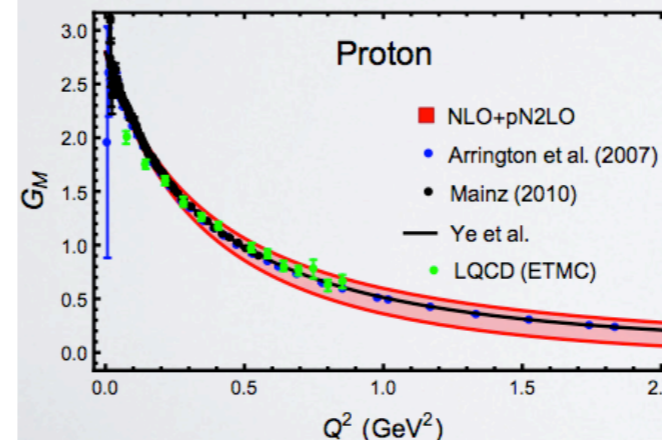
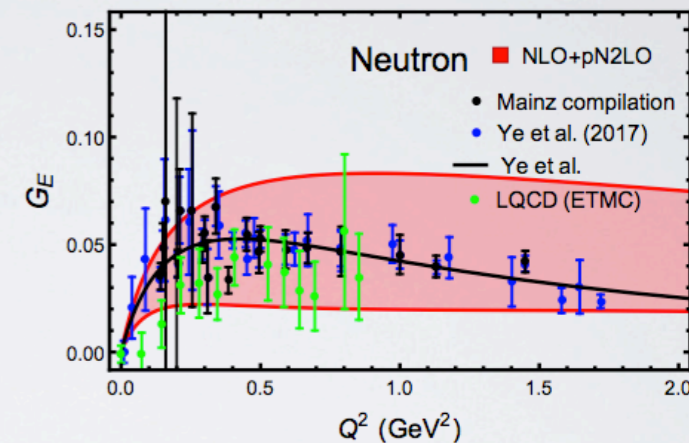
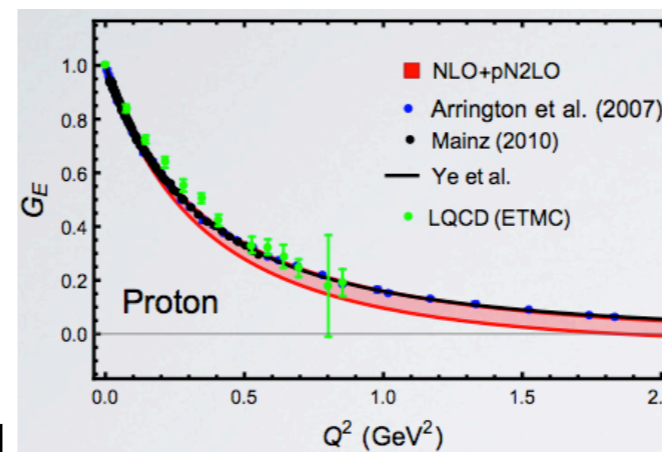
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New approach to compute FF:  
Dispersively improved  $\chi$ EFT.  
See M. Alarcon's talk  
Very recent predictions on proton and  
neutron FF ( $Q^2 > 2 \text{ GeV}^2$  w/  $\chi$ EFT):  
Proton radius  $\sim 0.85 \text{ fm}$   
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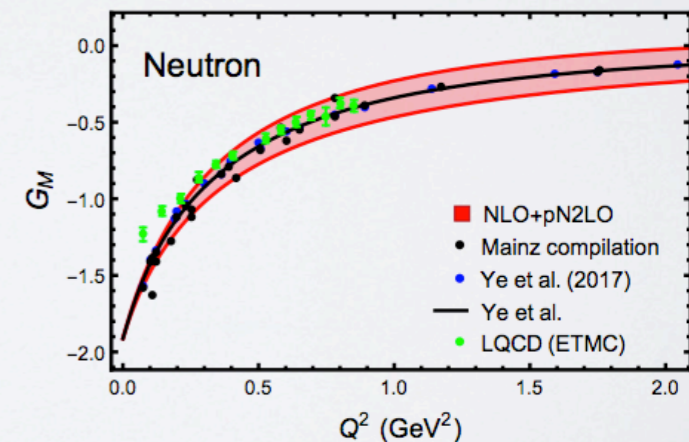
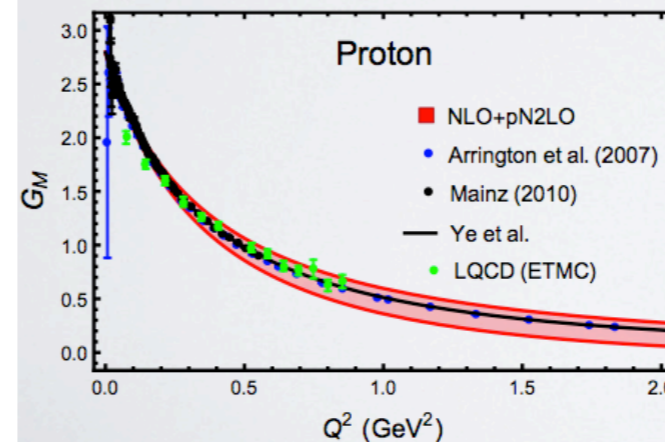
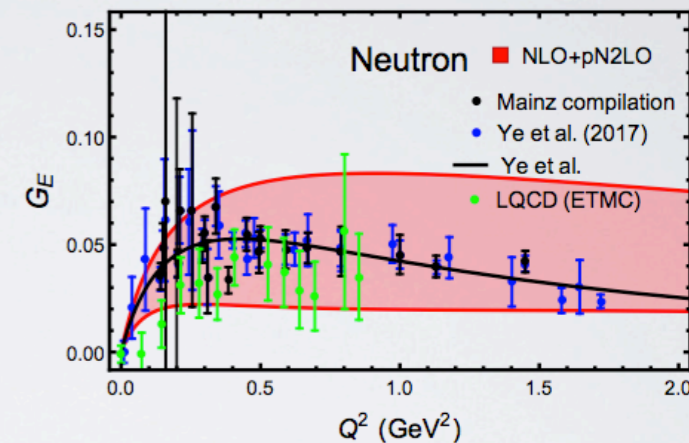
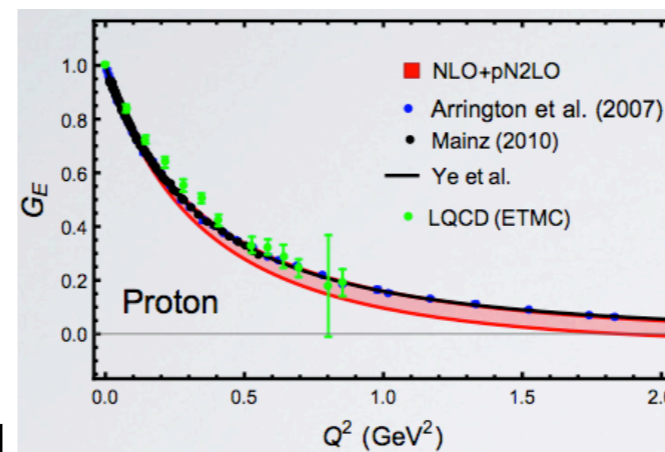
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Jealous ☹️



# Intersection of atomic and nuclear physics: proton radius and HFS

C. Carlson's overview

Potential for physics beyond the standard model (e.g. lepton universality violation).

3 new experiments to run to measure HFS of  $\mu$ -hydrogen at **ppm level**:

C. Carlson's review current precision on ingredients of HFS

- Riken-CAP (S. Kanda's talk): Asymmetry measurement in  $\mu$  decay. 2ppm goal (Zemach radius at 0.03%).
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Different  
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Different  
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TPE dominant uncertainty on HFS calculations. Two calculations approaches:

- $\chi^{\text{EFT}}$  (F. Haegelstein and A. Pineda's talks)
- Dispersion relations+struct. func. data (A. Antognini's talk)

some tensions

$g_2$  data scarce. More  $g_1$  data also welcome.  $1/Q^{4,2}$  weighted, respc.

•  $\delta_{LT}$  ( $g_2$ ) on proton: K. Slifer's talk

# $g_2$ contribution to the Hyperfine Splitting

$$\Delta_2 = -24m_p^2 \int_0^\infty \frac{dQ^2}{Q^4} B_2(Q^2)$$

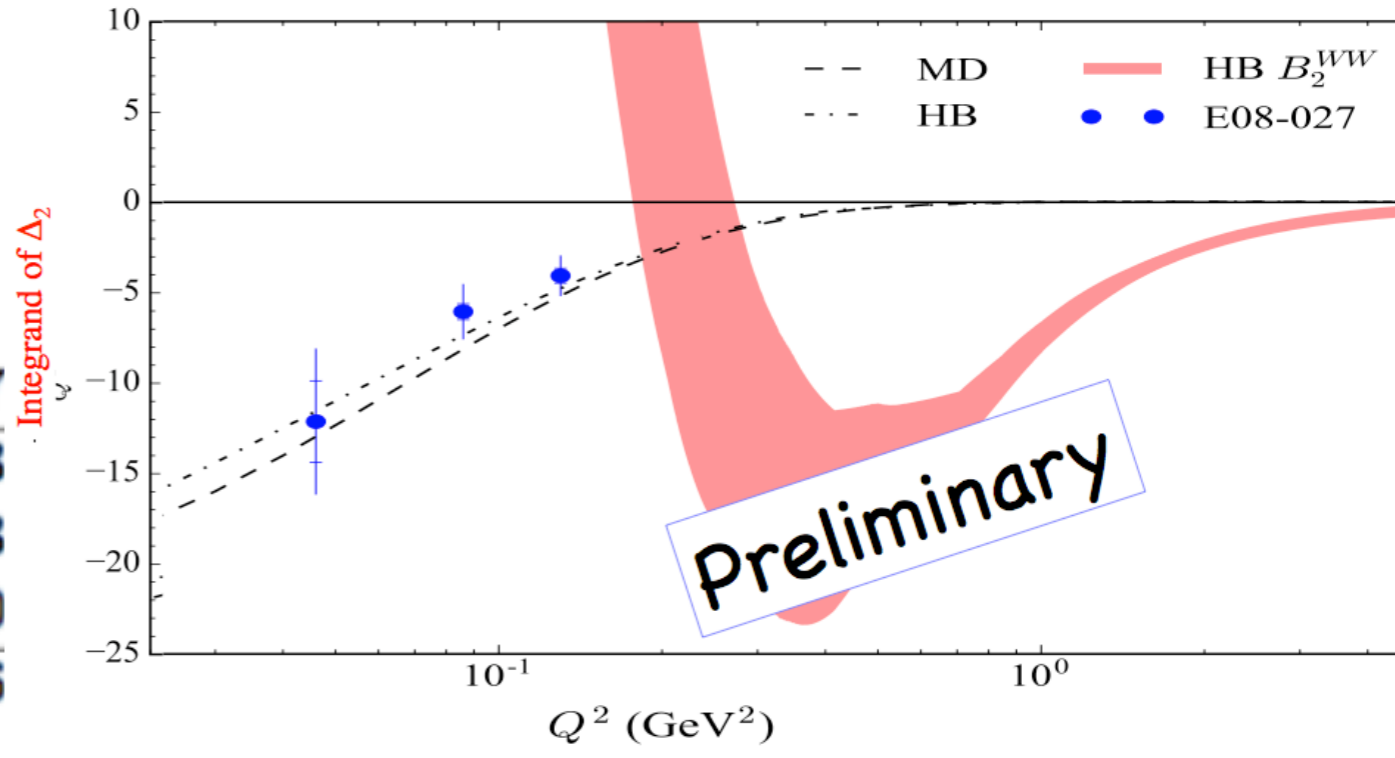
$$B_2(Q^2) = \int_0^{x_{th}} dx \beta_2(\tau) g_2(x, Q^2)$$

$$\beta_2(\tau) = 1 + 2\tau - 2\sqrt{\tau(\tau + 1)}$$

• How do new models compare with previous publications?

Term	$Q^2$ (GeV <sup>2</sup> )	MAID	Hall B	HB 2007
$\Delta_2$	(0,0.05)	-0.87	-0.80	-0.23
	(0.05,20)	-1.26	-1.16	-0.33
	(20,∞)	0.00	0.00	0.00
Total $\Delta_2$		-2.13	-1.96	-0.56

Phys.Rev.A.78.022511



# Conclusions: wish list to find the line

## QED

- ▶ check QED contributions in H to improve the TPE(H)
- ▶ higher-order QED corrections in  $\mu p$
- ▶ Summary of all contributions would be very helpful (at 1 ppm level).

Is the meson exchange already included in the TPE computed with dispersion relations?

## Zemach radius

- ▶ improve determination of Zemach radius, mainly through magnetic FF
- ▶ Study correlations  $R_z$  vs  $R_p$

## Polarisability contribution

- ▶ re-evaluate the pol contribution given the new  $g_1$  and  $g_2$  data
- ▶ improve chPT prediction also in view of interpretation of HFS measurement
- ▶ subtraction term really absent?

*Stolen from A. Antognini's talk*

**A TPE contribution with an accuracy of 25 ppm of HFS is needed to find the line**

## Open issues for theory and experiments.

- $\chi$ EFT consistencies (Mainz/Bonn, proton/neutron). Direct comparison with SSF at low  $Q^2$  and  $\nu$ .



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- $\chi$ EFT consistencies (Mainz/Bonn, proton/neutron). Direct comparison with SSF at low  $Q^2$  and  $\nu$ .
- **Lattice availability**. Low  $Q^2$ : How to compute **4-point correlation functions**?
- **Proton**:
  - **Full parameterization** of  $g_1$  and  $g_2$ . Build on Sebastian Kuhn's Model, MAID, with additional constraints (1-pion production).
- **Neutron**:
  - **Parameterization** of  $g_1$  and  $g_2$ .
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- Low-Q atomic/nuclear collaboration to provides state-of-art on observables and description consistency of theories. ("Low-Q data group"). 1-page summaries, white paper, new workshop (when?).