

# MAMI results for polarizabilities

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A2 Collaboration

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ECT\* - Nucleon Spin Structure at Low Q  
Trento, Italy - 3 July 2018

# Compton Scattering Equations

## Zeroth Order - Mass and Electric Charge

$$H_{\text{eff}}^{(0)} = \frac{\vec{\pi}^2}{2m} + e\phi \quad (\text{where } \vec{\pi} = \vec{p} - e\vec{A})$$

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## First Order - Anomalous Magnetic Moment

$$H_{\text{eff}}^{(1)} = -\frac{e(1+\kappa)}{2m} \vec{\sigma} \cdot \vec{H} - \frac{e(1+2\kappa)}{8m^2} \vec{\sigma} \cdot [\vec{E} \times \vec{\pi} - \vec{\pi} \times \vec{E}]$$

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## First Order - Anomalous Magnetic Moment

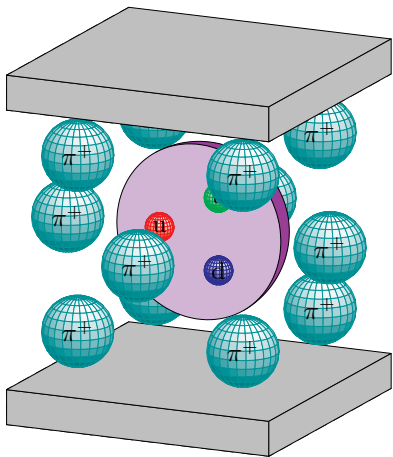
$$H_{\text{eff}}^{(1)} = -\frac{e(1 + \kappa)}{2m} \vec{\sigma} \cdot \vec{H} - \frac{e(1 + 2\kappa)}{8m^2} \vec{\sigma} \cdot [\vec{E} \times \vec{\pi} - \vec{\pi} \times \vec{E}]$$

## Second Order - Electric and Magnetic Polarizabilities

$$H_{\text{eff}}^{(2)} = -4\pi \left[ \frac{1}{2} \alpha_{E1} \vec{E}^2 + \frac{1}{2} \beta_{M1} \vec{H}^2 \right]$$

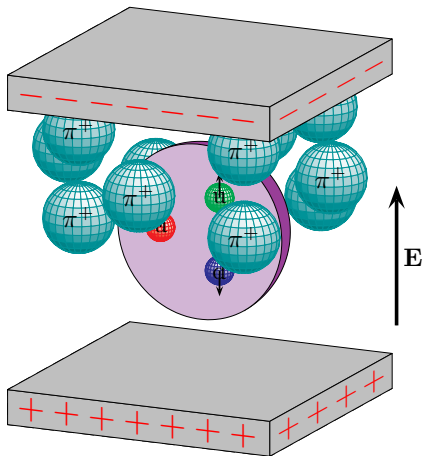
# Electric Polarizability - $\alpha_{E1}$

Describes the response of a proton to an applied electric field.



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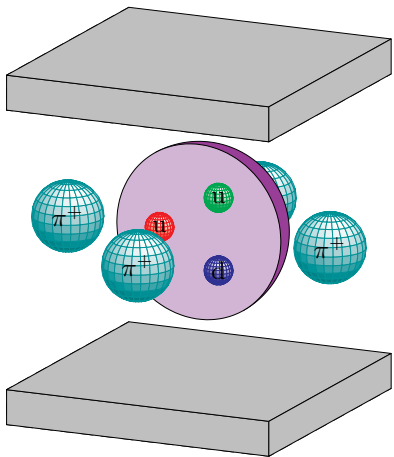


Induces a current in the pion cloud which vertically 'stretches' the proton (stretchability).



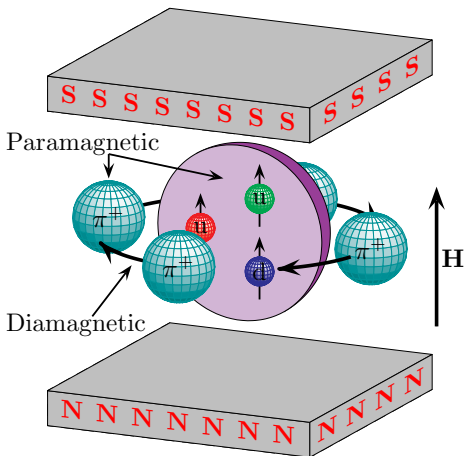
# Magnetic Polarizability - $\beta_{M1}$

Describes the response of a proton to an applied magnetic field.



# Magnetic Polarizability - $\beta_{M1}$

Describes the response of a proton to an applied magnetic field.



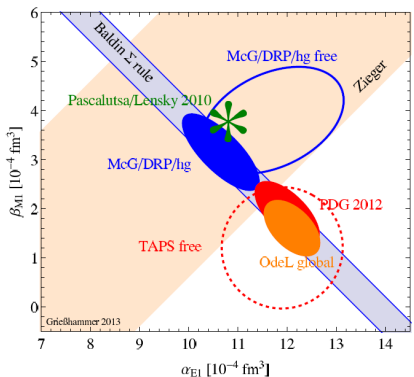
Induces a diamagnetic moment in the pion cloud that opposes the paramagnetic moment of the quarks (alignability).





# Scalar Polarizabilities

Determined using unpolarized Compton scattering (Note, errors are added in quadrature, see papers for details)



OdeL Global

$$\alpha_{E1} = (12.1 \pm 0.6) \times 10^{-4} \text{ fm}^3$$

$$\beta_{M1} = (1.6 \pm 0.7) \times 10^{-4} \text{ fm}^3$$

Baldin (Lapidus) Sum Rule:

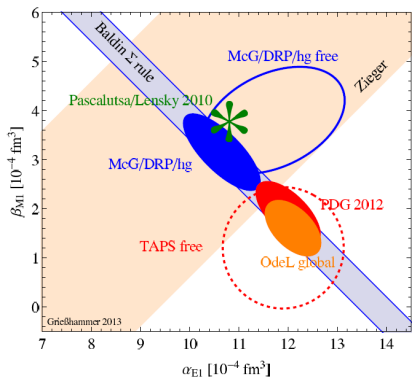
$$\alpha + \beta = \frac{1}{2\pi^2} \int_{\omega_0}^{\infty} \frac{\sigma_{\text{tot}}(\omega)}{\omega^2} d\omega$$

V. Olmos de Leon *et al.* (A2), Eur. Phys. J. A 10, 207 (2001)



# Scalar Polarizabilities

Determined using unpolarized Compton scattering (Note, errors are added in quadrature, see papers for details)



PDG 2012

$$\alpha_{E1} = (12.0 \pm 0.6) \times 10^{-4} \text{ fm}^3$$

$$\beta_{M1} = (1.9 \pm 0.5) \times 10^{-4} \text{ fm}^3$$

Baldin (Lapidus) Sum Rule:

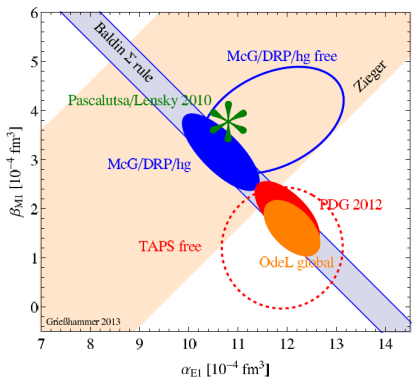
$$\alpha + \beta = \frac{1}{2\pi^2} \int_{\omega_0}^{\infty} \frac{\sigma_{\text{tot}}(\omega)}{\omega^2} d\omega$$

V. Olmos de Leon *et al.* (A2), Eur. Phys. J. A 10, 207 (2001)



# Scalar Polarizabilities

Determined using unpolarized Compton scattering (Note, errors are added in quadrature, see papers for details)



Pascalutsa/Lensky

$$\alpha_{E1} = (10.8 \pm 0.7) \times 10^{-4} \text{ fm}^3$$

$$\beta_{M1} = (4.0 \pm 0.7) \times 10^{-4} \text{ fm}^3$$

Baldin (Lapidus) Sum Rule:

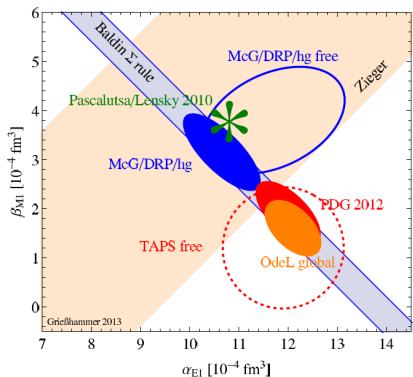
$$\alpha + \beta = \frac{1}{2\pi^2} \int_{\omega_0}^{\infty} \frac{\sigma_{\text{tot}}(\omega)}{\omega^2} d\omega$$

Lensky, Pascalutsa, Eur. Phys. J. C 65, 195 (2010)



# Scalar Polarizabilities

Determined using unpolarized Compton scattering (Note, errors are added in quadrature, see papers for details)



McG/DRP/hg

$$\alpha_{E1} = (10.65 \pm 0.5) \times 10^{-4} \text{ fm}^3$$

$$\beta_{M1} = (3.15 \pm 0.5) \times 10^{-4} \text{ fm}^3$$

Baldin (Lapidus) Sum Rule:

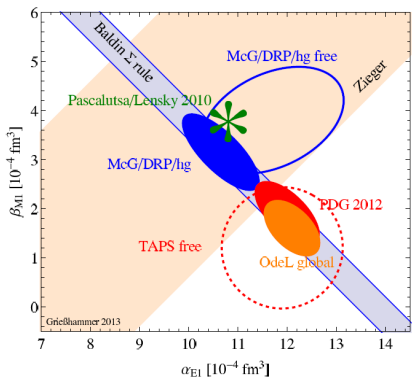
$$\alpha + \beta = \frac{1}{2\pi^2} \int_{\omega_0}^{\infty} \frac{\sigma_{\text{tot}}(\omega)}{\omega^2} d\omega$$

McGovern, Phillips, Grießhammer, Eur. Phys. J. A 49, 12 (2013)



# Scalar Polarizabilities

Determined using unpolarized Compton scattering (Note, errors are added in quadrature, see papers for details)



Perhaps we can do better.

PDG 2013/2014

$$\alpha_{E1} = (11.2 \pm 0.4) \times 10^{-4} \text{ fm}^3$$

$$\beta_{M1} = (2.5 \pm 0.4) \times 10^{-4} \text{ fm}^3$$

Baldin (Lapidus) Sum Rule:

$$\alpha + \beta = \frac{1}{2\pi^2} \int_{\omega_0}^{\infty} \frac{\sigma_{\text{tot}}(\omega)}{\omega^2} d\omega$$



# Compton Scattering Equations

## Third Order - Spin Polarizabilities

$$H_{\text{eff}}^{(3)} = -4\pi \left[ \frac{1}{2} \gamma_{E1E1} \vec{\sigma} \cdot (\vec{E} \times \dot{\vec{E}}) + \frac{1}{2} \gamma_{M1M1} \vec{\sigma} \cdot (\vec{H} \times \dot{\vec{H}}) \right. \\ \left. - \gamma_{M1E2} E_{ij} \sigma_i H_j + \gamma_{E1M2} H_{ij} \sigma_i E_j \right]$$

- These parameters describe the response of the proton **spin** to an applied electric or magnetic field. Analogous to a classical Faraday effect.
- To date, these have not been individually determined. However, two linear combinations of them have been.



# Spin Polarizabilities

## Forward Spin Polarizability

$$\gamma_0 = -\gamma_{E1E1} - \gamma_{E1M2} - \gamma_{M1E2} - \gamma_{M1M1} = (-1.0 \pm 0.08) \times 10^{-4} \text{ fm}^4$$

Determined at MAMI and ELSA through the GDH experiments

J. Ahrens *et al.* (GDH/A2), Phys. Rev. Lett. 87, 022003 (2001)

H. Dutz *et al.* (GDH), Phys. Rev. Lett. 91, 192001 (2003)

## Backward Spin Polarizability

$$\gamma_\pi = -\gamma_{E1E1} - \gamma_{E1M2} + \gamma_{M1E2} + \gamma_{M1M1} = (8.0 \pm 1.8) \times 10^{-4} \text{ fm}^4$$

Determined with dispersive fits to back-angle Compton scattering

M. Camen *et al.* (A2), Phys. Rev. C 65, 032202 (2002)

# Spin Polarizabilities

## Change of Basis

$$\gamma_0 = -\gamma_{E1E1} - \gamma_{E1M2} - \gamma_{M1E2} - \gamma_{M1M1}$$

$$\gamma_\pi = -\gamma_{E1E1} - \gamma_{E1M2} + \gamma_{M1E2} + \gamma_{M1M1}$$

Using the above relations, we can express the two mixed terms

$$\gamma_{E1M2} = -\gamma_{E1E1} - \frac{1}{2}\gamma_0 - \frac{1}{2}\gamma_\pi$$

$$\gamma_{M1E2} = -\gamma_{M1M1} - \frac{1}{2}\gamma_0 + \frac{1}{2}\gamma_\pi$$

This leaves us with two unknown and two known (with error) terms.



# Predicted Values

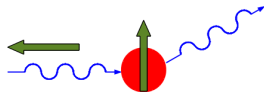
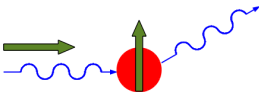
	K-mat.	HDPV	DPV	$L_\chi$	HB $\chi$ PT	B $\chi$ PT
$\gamma_{E1E1}$	-4.8	-4.3	-3.8	-3.7	$-1.1 \pm 1.8$ (th)	-3.3
$\gamma_{M1M1}$	3.5	2.9	2.9	2.5	$2.2 \pm 0.5$ (st) $\pm 0.7$ (th)	3.0
$\gamma_{E1M2}$	-1.8	-0.02	0.5	1.2	$-0.4 \pm 0.4$ (th)	0.2
$\gamma_{M1E2}$	1.1	2.2	1.6	1.2	$1.9 \pm 0.4$ (th)	1.1
$\gamma_0$	2.0	-0.8	-1.1	-1.2	-2.6	-1.0
$\gamma_\pi$	11.2	9.4	7.8	6.1	5.6	7.2

- Spin polarizabilities in units of  $10^{-4} \text{ fm}^4$
- K-matrix: calculation from Kondratyuk *et al.*, Phys. Rev. C 64, 024005 (2001)
- HDPV, DPV: dispersion relation calculations, B.R. Holstein *et al.*, Phys. Rev. C 61, 034316 (2000) and B. Pasquini *et al.*, Phys. Rev. C 76, 015203 (2007), D. Drechsel *et al.*, Phys. Rep. 378, 99 (2003)
- $L_\chi$ : chiral lagrangian calculation, A.M. Gasparyan *et al.*, Nucl. Phys. A 866, 79 (2011)
- HB $\chi$ PT and B $\chi$ PT are heavy baryon and covariant, respectively, chiral perturbation theory calculations, J.A. McGovern *et al.*, Eur. Phys. J. A 49, 12 (2013), V. Lensky *et al.*, Phys. Rev. C 89, 032202 (2014)

# Three Compton Scattering Experiments

- Circularly polarized photons, transversely polarized protons.

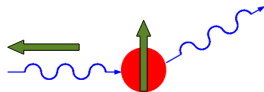
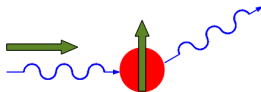
$$\Sigma_{2x} = \frac{N_{+x}^R - N_{+x}^L}{N_{+x}^R + N_{+x}^L}$$



# Three Compton Scattering Experiments

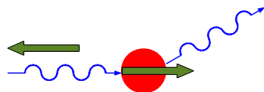
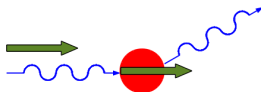
- Circularly polarized photons, transversely polarized protons.

$$\Sigma_{2x} = \frac{N_{+x}^R - N_{+x}^L}{N_{+x}^R + N_{+x}^L}$$



- Circularly polarized photons, longitudinally polarized protons.

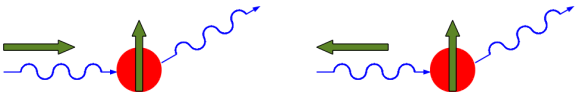
$$\Sigma_{2z} = \frac{N_{+z}^R - N_{+z}^L}{N_{+z}^R + N_{+z}^L}$$



# Three Compton Scattering Experiments

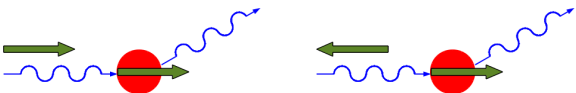
- Circularly polarized photons, transversely polarized protons.

$$\Sigma_{2x} = \frac{N_{+x}^R - N_{+x}^L}{N_{+x}^R + N_{+x}^L}$$



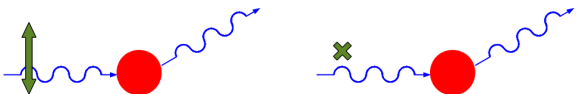
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$$\Sigma_{2z} = \frac{N_{+z}^R - N_{+z}^L}{N_{+z}^R + N_{+z}^L}$$

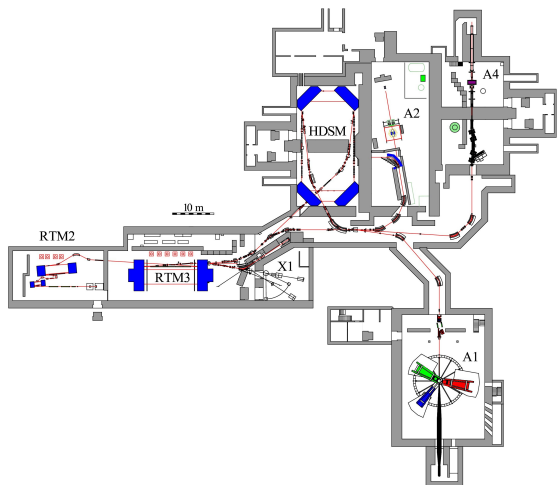


- Linearly polarized photons, unpolarized protons.

$$\Sigma_3 = \frac{N_{\parallel} - N_{\perp}}{N_{\parallel} + N_{\perp}}$$



# Mainz Microtron (MAMI) $e^-$ Beam



- Injector  $\rightarrow$  3.5 MeV
- RTM1  $\rightarrow$  14.9 MeV
- RTM2  $\rightarrow$  180 MeV
- RTM3  $\rightarrow$  883 MeV
- HDSM  $\rightarrow$  1.6 GeV

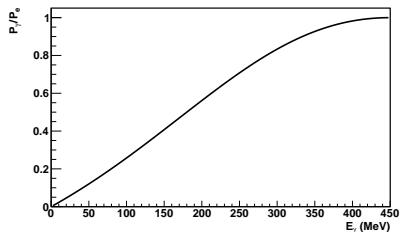
For these experiments only the RTMs are required (450 or 883 MeV).



# Polarized Photon Beam

A high energy electron can produce Bremsstrahlung ('braking radiation') photons when slowed down by a material.

- Longitudinally polarized electron beam produces circularly polarized photon beam (helicity transfer)
- $P_e$  measured with a Mott polarimeter before the RTMs.
- Circular beam helicity flipped by alternating the  $e^-$  beam polarization ( $\approx 1$  Hz).



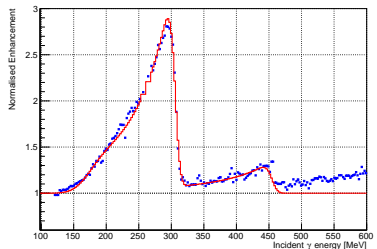
$$P_\gamma = P_e \frac{4E_\gamma E_e - E_\gamma^2}{4E_e^2 - 4E_\gamma E_e + 3E_\gamma^2}$$



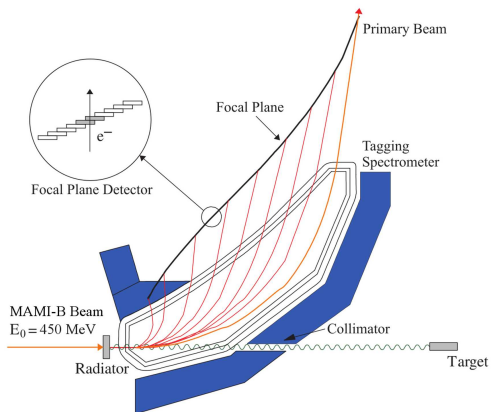
# Polarized Photon Beam

A high energy electron can produce Bremsstrahlung ('braking radiation') photons when slowed down by a material.

- Diamond radiator produces linearly polarized photon beam (coherent Bremsstrahlung)
- Polarization determined by fitting the Bremsstrahlung distribution.
- Linear beam orientation typically flipped every two hours.



# Photon Tagging



- $e^-$  beam with energy  $E_0$ , strikes radiator producing Bremsstrahlung photon beam with energy distribution from 0 to  $E_0$ .
- Residual  $e^-$  paths are bent in a spectrometer magnet.
- With proper magnetic field, array of 352 detectors determines the  $e^-$  energy, and 'tags' the photon energy by energy conservation.





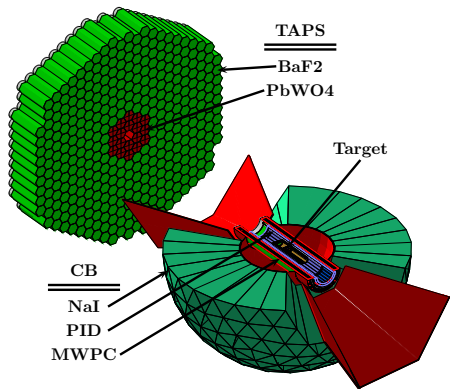
# Frozen Spin Target

How are the protons actually polarized? Through Dynamic Nuclear Polarization (DNP):

- Cool target to 0.2 Kelvin.
- Use 2.5 Tesla magnet to align electron spins.
- Pump  $\approx 70$  GHz microwaves (just above, or below, the Electron Spin Resonance frequency), causing spin-flips between the electrons and protons.
- Cool target to 0.025 Kelvin, 'freezing' proton spins in place.
- Remove polarizing magnet and energize 0.6 Tesla 'holding' coil in the cryostat to maintain the polarization.
- Relaxation times  $> 1000$  hours, polarizations up to 90%.



# Detectors



## Crystal Ball (CB)

- 672 NaI Crystals
- 24 Particle Identification Detector (PID) Paddles
- 2 Multiwire Proportional Chambers (MWPCs)

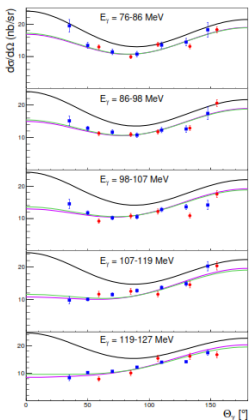
## Two Arms Photon Spectrometer (TAPS)

- 366 BaF<sub>2</sub> and 72 PbWO<sub>4</sub> Crystals
- 384 Veto Paddles

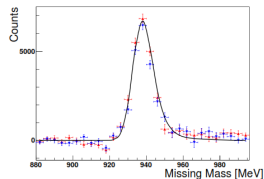
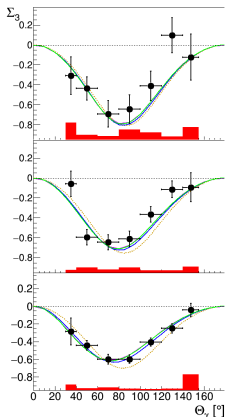


# $\Sigma_3/\sigma_0 - \alpha$ and $\beta$

- Measure  $\sigma_0$  and  $\Sigma_3$  at energies below  $\pi^0$  threshold
- Test run in June 2013, Eur. Phys. J. A 53, 14 (2017)



Need more data!



— N. Krupina and V. Pascalutsa, PRL 110, 262001 (2013)

— B. Pasquini, D. Drechsel, and M. Vanderhaeghen, Phys. Rev. C 76 (2007)

— J. McGovern, D. Phillips, H. Grieshammer, EPJA 49, 12 (2013)

Systematical errors = normalization + polarization + background + phase

# Tagger upgrade



Three weeks of data in Nov 2017, one in Feb 2018,  
three in Mar 2018, and three starting today!



# Beamtimes



## Polarized frozen spin butanol target

- 2 cm - Butanol ( $C_4H_9OH$ )
- $\Sigma_{2x}$  - Sep 2010/Feb 2011 - 500 h
- $\Sigma_{2z}$  - May 2014/Jun 2015 - 600 h

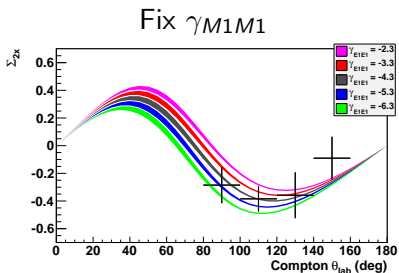
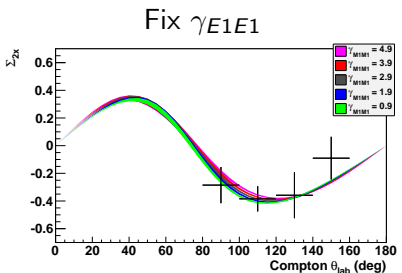


## Unpolarized liquid hydrogen target

- 10 cm - LH2
- $\Sigma_3$  (Delta) - Dec 2012 - 150 h
- $\Sigma_3/\sigma_0$  (Threshold) - Various...



# Transverse Target - $E_\gamma=273-303$ MeV

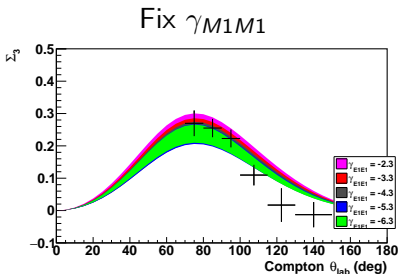
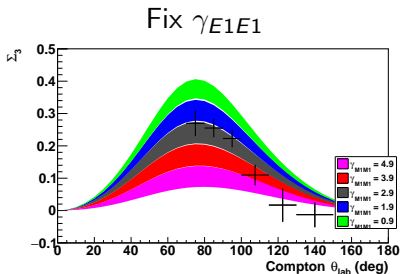


Determine the other two using  $\gamma_0$  and  $\gamma_\pi$ , while allowing them,  $\alpha_{E1}$ , and  $\beta_{M1}$  to vary by their experimental errors.

Martel *et al.* (A2) Phys. Rev. Lett. 114, 112501 (2015)



# Hydrogen Target - $E_\gamma=287-307$ MeV - Preliminary



Determine the other two using  $\gamma_0$  and  $\gamma_\pi$ , while allowing them,  $\alpha_{E1}$ , and  $\beta_{M1}$  to vary by their experimental errors.

C. Collicott, Ph.D. thesis, Dalhousie University (2015)



# Fitting

Dispersion relation fitted to  $\Sigma_{2x}$  along with either  $\Sigma_3^{\text{MAMI}}$  or  $\Sigma_3^{\text{LEGS}}$  - G. Blanpied *et al.*, Phys. Rev. C 64, 025203 (2001)

	$\Sigma_{2x}$ and $\Sigma_3^{\text{LEGS}}$	$\Sigma_{2x}$ and $\Sigma_3^{\text{MAMI}}$
$\bar{\gamma}_{E1E1}$	$-3.5 \pm 1.2$	$-5.0 \pm 1.5$
$\bar{\gamma}_{M1M1}$	$3.16 \pm 0.85$	$3.13 \pm 0.88$
$\bar{\gamma}_{E1M2}$	$-0.7 \pm 1.2$	$1.7 \pm 1.7$
$\bar{\gamma}_{M1E2}$	$1.99 \pm 0.29$	$1.26 \pm 0.43$
$\gamma_0$	$-1.03 \pm 0.18$	$-1.00 \pm 0.18$
$\gamma_\pi$	$9.3 \pm 1.6$	$7.8 \pm 1.8$
$\bar{\alpha} + \bar{\beta}$	$14.0 \pm 0.4$	$13.8 \pm 0.4$
$\bar{\alpha} - \bar{\beta}$	$7.4 \pm 0.9$	$6.6 \pm 1.7$
$\chi^2/\text{dof}$	1.05	1.25

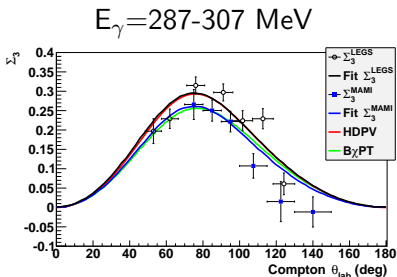
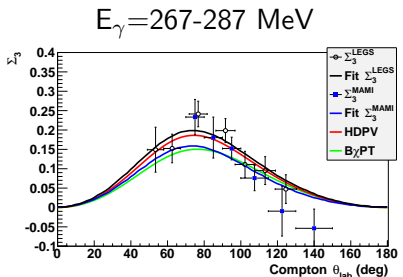
Scalar polarizabilities in units of  $10^{-4} \text{ fm}^3$

Spin polarizabilities in units of  $10^{-4} \text{ fm}^4$





# Hydrogen Target - Preliminary

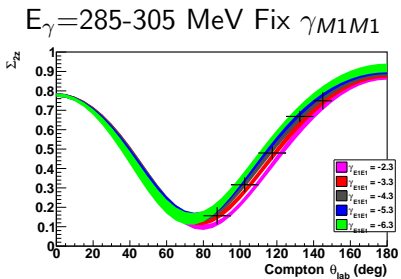
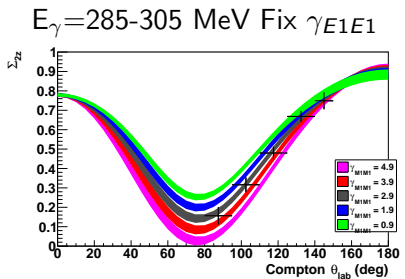
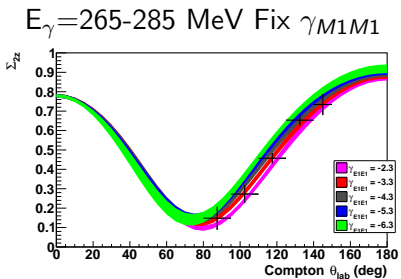
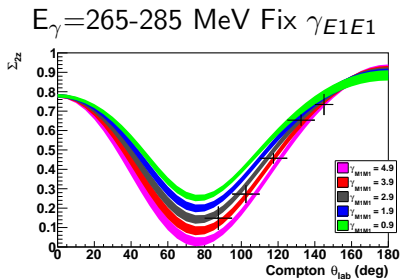


Added dispersion calculations with the fitted polarizability values.  
 Fit with LEGS  $\rightarrow$  HDPV. Fit with MAMI  $\rightarrow$   $B_{\chi PT}$ .

C. Collicott, Ph.D. thesis, Dalhousie University (2015)



# Longitudinal Target - Preliminary



# Why still preliminary?

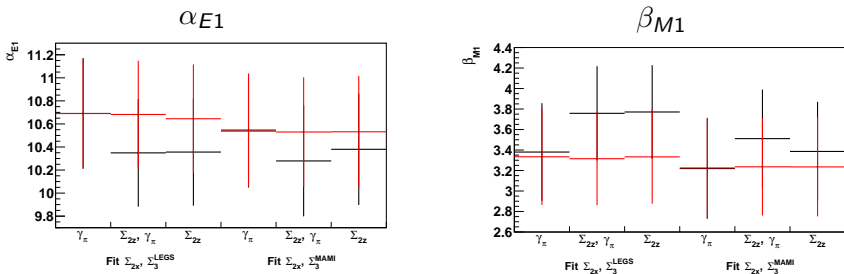
$\Sigma_3$  (Delta) data is 5 1/2 years old, the  $\Sigma_{2z}$  data is 3-4 years old.  
What's the hold-up?

- $\Sigma_3$  is essentially done. Needed some additional checks of the systematics from the polarization of the beam, which have been done. Paper in production now.
- $\Sigma_{2x}$  was done (or so we thought). Paper sent through internal review, found a discrepancy with another analysis. Under investigation now, but all parties appear to be converging. Hopefully submitted soon.

For now, assuming those numbers are correct, how well do they improve our polarizability extraction?



# Fitting - Scalar Polarizabilities

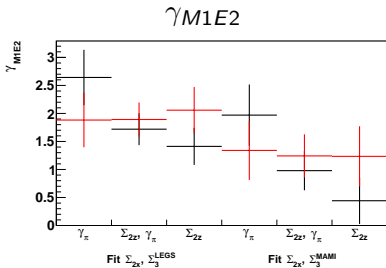
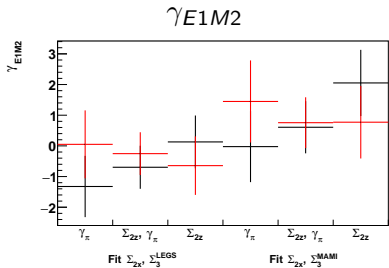
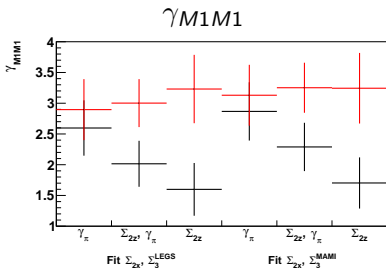
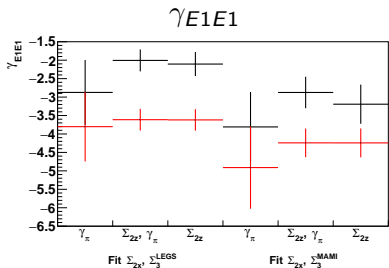


Fitting the  $\Sigma_{2x}$  results as well as either the  $\Sigma_3^{\text{LEGS}}$  (left three points) or the  $\Sigma_3^{\text{MAMI}}$  results (right three points), using B $\chi$ PT (black) or HDPV (red), each set of three points (L-R) represent:

- Using the  $\gamma_\pi$  constraint
- Fitting  $\Sigma_{2z}$  and using the  $\gamma_\pi$  constraint
- Fitting  $\Sigma_{2z}$  without the  $\gamma_\pi$  constraint

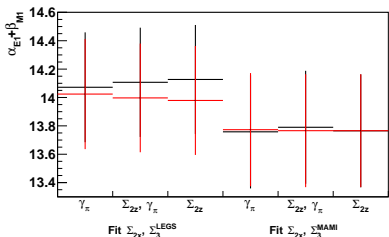


# Fitting - Spin Polarizabilities

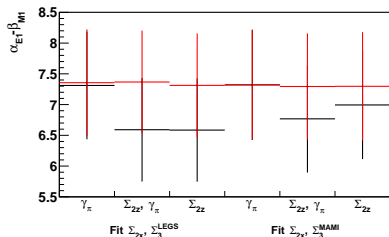


# Fitting - Constraints

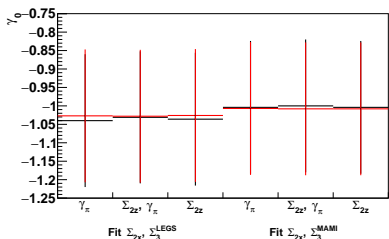
$$\alpha_{E1} + \beta_{M1}$$



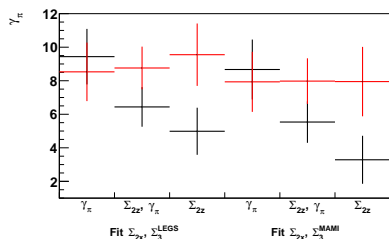
$$\alpha_{E1} - \beta_{M1}$$



$$\gamma_0$$



$$\gamma_\pi$$



# Should we be measuring these asymmetries in the Delta?

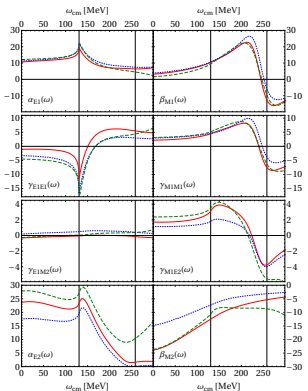


Figure 1: (Colour online) Real parts of the dominant dynamical polarisabilities for low-energy Compton scattering from the proton, plotted as a function of cm photon energy. The units are  $10^{-4} \text{ fm}^3$  where  $n = 3$  for  $\alpha_{E1}$  and  $\beta_{M1}$ ,  $n = 4$  for the  $\gamma_n$ , and  $n = 5$  for  $\alpha_{E2}$  and  $\beta_{M2}$ . Red (solid); this work; green (dashed); DR-based by Pasquini *et al.* [21]; blue (dotted) 2nd-order covariant  $\chi$ PT by Lensky *et al.* [22]. Note that each row has its distinct plot scale.

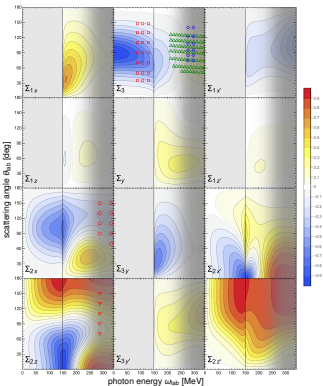


Figure 5: (Colour online) Contour plots of the asymmetries and polarisation-transfer observables; see text and sect. 3.1 for details. Data included as available: for  $\Sigma_2$ : open (green) triangles  $\triangle$  from LEGS [39], open (red) squares  $\square$  from MAMI [9], open (blue) diamonds  $\diamond$  preliminary from MAMI [16, 18]; for  $\Sigma_{2z}$ : open (red) circles  $\circ$  MAMI data from [8, 15]; open (red) inverted triangle  $\nabla$  preliminary from MAMI [18]. Symbol sizes do not reflect error bars, nor the size of energy or angle bins.

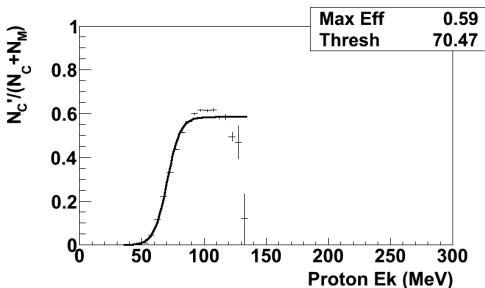
Griesshammer, McGovern, Phillips, Eur. Phys. J. A (2018) 54: 37

# Kinematics Limited by Proton Detection

Event reconstruction relies on detection of the recoil proton to reject backgrounds. Using  $\pi^0$  events, an 'identification' efficiency can be determined.

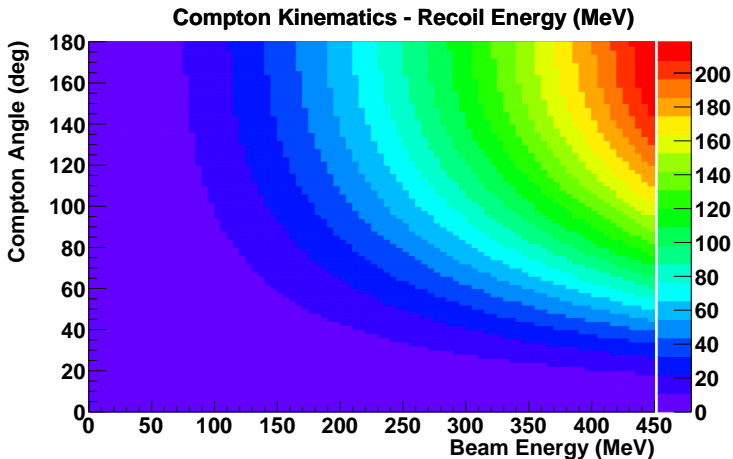
$$\epsilon = \frac{N'_C(\theta_{OA})}{N_C + N_M}$$

- $N'_C(\theta_{OA})$  - charged particle satisfies opening angle cut
- $N_C$  - any charged particle
- $N_M$  - missed recoil particle





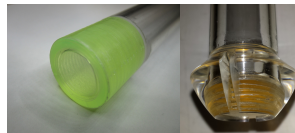
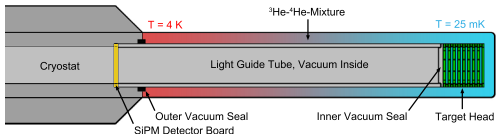
# So what phase space do we have to work with?



Requiring the proton then clearly limits our kinematic range.



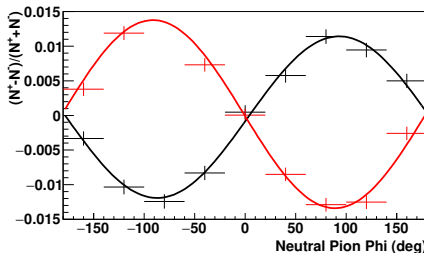
# Active Target



## Requirements

- Polarizable Scintillator
- High light output
- High rate capability
- Low thermal energy input
- Detectors working at 4K

Targets from UMass Amherst  
Tested at MAMI - Pol > 50%



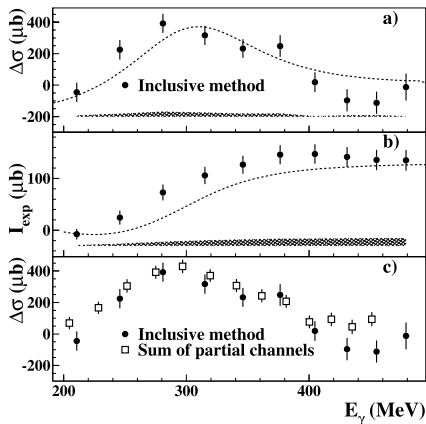
# GDH Sum Rule

Where are the deuteron results from MAMI?

- Longitudinally polarized deuterated butanol data already taken
- Analysis of  $\sigma_P - \sigma_A$  for  $\pi^0$  well underway
- Total inclusive also being looked at

And what about  $^3\text{He}$ ?

Physics Letters B 723 (2013) 7177



# Conclusions

- Test run for  $\Sigma_3$  below threshold published in EPJA
- Full program for  $\Sigma_3$  below threshold wrapping up, analysis should be quite fast.
- $\Sigma_{2x}$ ,  $\Sigma_{2z}$ , and  $\Sigma_3$  have all been measured in the Delta
- $\Sigma_{2x}$  results published in PRL, other two are in production
- Future:
  - Combine with results from all of the  $\alpha_{E1}$  and  $\beta_{M1}$  runs
  - More data for higher energy  $\Sigma_3$ , to address LEGS/MAMI difference (for free from May/Sep 2018 runs on  $\pi^0$  TFF)
  - Implementation of active target to expand kinematic range
  - Improvement in simulation to remove  $\pi^0$  backgrounds and increase statistics
- Rebuild polarized  $^3\text{He}$  target for GDH study?



# Conclusions

Thank you all for listening!



# Backup Slides

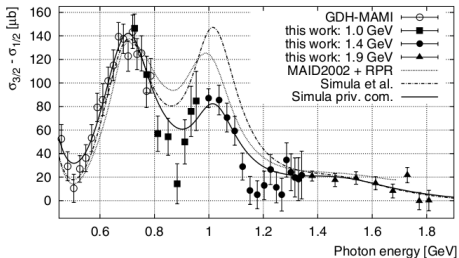
You want more info...



# Forward Spin Polarizability

## GDH Experiments

- MAMI and ELSA
- Circular Photons
- Longitudinal Protons
- Measure Gerasimov, Drell, Hearn (GDH) Sum Rule



$$\frac{2\pi^2\alpha_e\kappa^2}{M^2} = \int_{\omega_0}^{\infty} \frac{\sigma_{3/2}(\omega) - \sigma_{1/2}(\omega)}{\omega} d\omega$$

J. Ahrens *et al.*, Phys. Rev. Lett. 87, 022003 (2001)

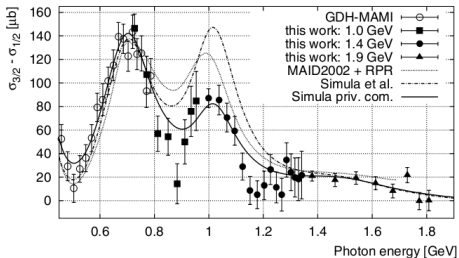
H. Dutz *et al.*, Phys. Rev. Lett. 91, 192001 (2003)



# Forward Spin Polarizability

## GDH Experiments

- MAMI and ELSA
- Circular Photons
- Longitudinal Protons
- Measure Gerasimov, Drell, Hearn (GDH) Sum Rule
- Also get  $\gamma_0$



$$\gamma_0 = -\frac{1}{4\pi^2} \int_{\omega_0}^{\infty} \frac{\sigma_{3/2}(\omega) - \sigma_{1/2}(\omega)}{\omega^3} d\omega$$

$$\gamma_0 = (-1.0 \pm 0.08) \times 10^{-4} \text{ fm}^4$$

J. Ahrens *et al.*, Phys. Rev. Lett. 87, 022003 (2001)

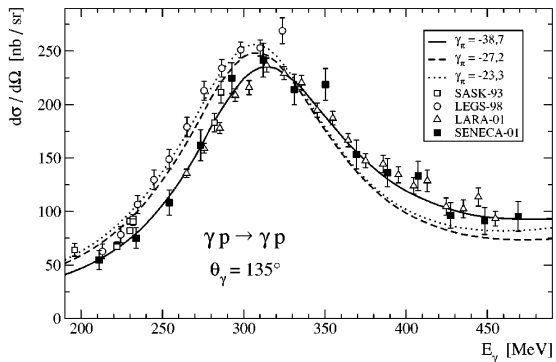
H. Dutz *et al.*, Phys. Rev. Lett. 91, 192001 (2003)





# Backward Spin Polarizability

Determined using a dispersive fitting to backward angle Compton scattering data, such as that taken at MAMI:



M. Camen *et al.*,  
 Phys. Rev. C  
 65 (2002) 032202

$$\gamma_\pi = (8.0 \pm 1.8) \times 10^{-4} \text{ fm}^4$$



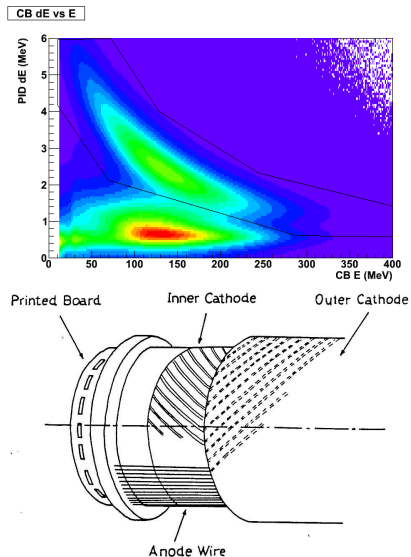
# Crystal Ball - Charged Particle Detection

## Particle Identification Detector (PID)

- Barrel of 24 plastic paddles
- Each covers  $15 < \theta < 159^\circ$ , and  $15^\circ$  in  $\phi$
- Plot  $\Delta E$  in PID vs  $E$  in NaI

## Multiwire Proportional Chamber (MWPC)

- Two chambers: anode wires sandwiched by two layers of cathode strips
- Voltage between wires and strips increases when gas is ionized



# TAPS - Charged Particle Detection

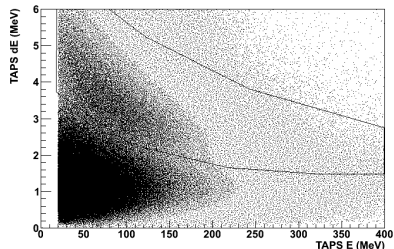
## Veto scintillators

- 5mm plastic scintillators in front of each crystal
- Same method as PID (plot  $\Delta E$  vs  $E$ )

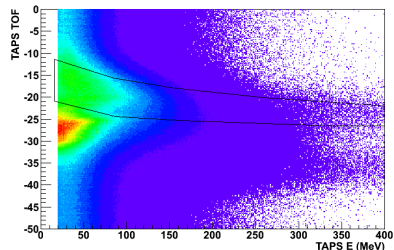
## Time of Flight

- Given its increased distance from the target, massive particles take noticeably longer to reach TAPS
- Plot time vs  $E$ , identify nucleons

TAPS  $dE$  vs  $E$



TAPS Particle TOF



# Backgrounds

## Butanol Target ( $C_4H_9OH$ )

- Compton off H
- Coherent scatter off C (or O)
- Incoherent scatter off C (or O)
- Pion photoproduction off H
- Coherent pion off C (or O)
- Incoherent pion off C (or O)

## Hydrogen Target ( $LH_2$ )

- Compton off H
- Pion photoproduction off H



# Backgrounds

## Butanol Target ( $C_4H_9OH$ )

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## Hydrogen Target ( $LH_2$ )

- Compton off H
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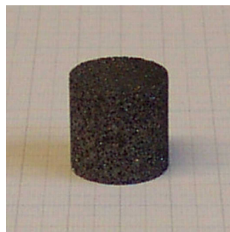
# Backgrounds

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- Pion photoproduction off H
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- Incoherent pion off C (or O)

## Hydrogen Target ( $LH_2$ )

- Compton off H
- Pion photoproduction off H



Subtract data taken on a carbon target, with density chosen to match the number of non-hydrogen nucleons in the butanol target.



# Backgrounds

## Butanol Target ( $C_4H_9OH$ )

- Compton off H
- Coherent scatter off C (or O)
- Incoherent scatter off C (or O)
- Pion photoproduction off H
- Coherent pion off C (or O)
- Incoherent pion off C (or O)

## Hydrogen Target ( $LH_2$ )

- Compton off H
- Pion photoproduction off H



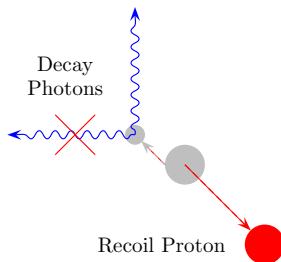
# Backgrounds

## Butanol Target ( $C_4H_9OH$ )

- Compton off H
- Coherent scatter off C (or O)
- Incoherent scatter off C (or O)
- **Pion photoproduction off H**
- Coherent pion off C (or O)
- Incoherent pion off C (or O)

## Hydrogen Target ( $LH_2$ )

- Compton off H
- **Pion photoproduction off H**

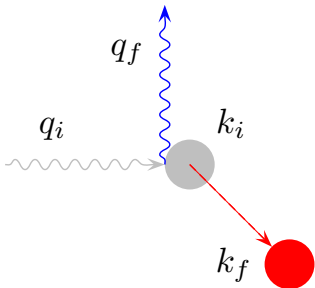


$\pi^0$  photoproduction  $\approx 100$  times more likely. If one of the decay photons is lost, this can look like Compton.





# Compton Missing Mass



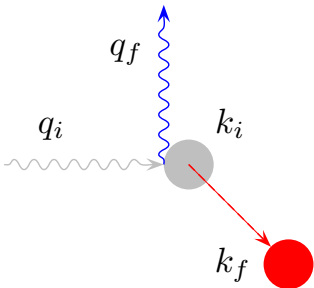
$$k_f = q_i + k_i - q_f$$

$$k_f^2 = m_k^2 = (q_i + k_i - q_f)^2$$

## Missing Mass

$$m_{\text{miss}} = m_k = \sqrt{(E_{\gamma_i} + m_p - E_{\gamma_f})^2 - (\vec{p}_{\gamma_i} - \vec{p}_{\gamma_f})^2} \underset{\text{Compton}}{=} m_p$$

# Compton Missing Mass



$$k_f = q_i + k_i - q_f$$

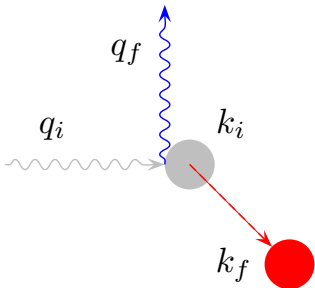
$$k_f^2 = m_k^2 = (q_i + k_i - q_f)^2$$

Q: Why not use the proton information itself?

## Missing Mass

$$m_{\text{miss}} = m_k = \sqrt{(E_{\gamma_i} + m_p - E_{\gamma_f})^2 - (\vec{p}_{\gamma_i} - \vec{p}_{\gamma_f})^2} \underset{\text{Compton}}{=} m_p$$

# Compton Missing Mass



$$k_f = q_i + k_i - q_f$$

$$k_f^2 = m_k^2 = (q_i + k_i - q_f)^2$$

Q: Why not use the proton information itself?

A: Too much energy loss.

## Missing Mass

$$m_{\text{miss}} = m_k = \sqrt{(E_{\gamma_i} + m_p - E_{\gamma_f})^2 - (\vec{p}_{\gamma_i} - \vec{p}_{\gamma_f})^2} \underset{\text{Compton}}{=} m_p$$