



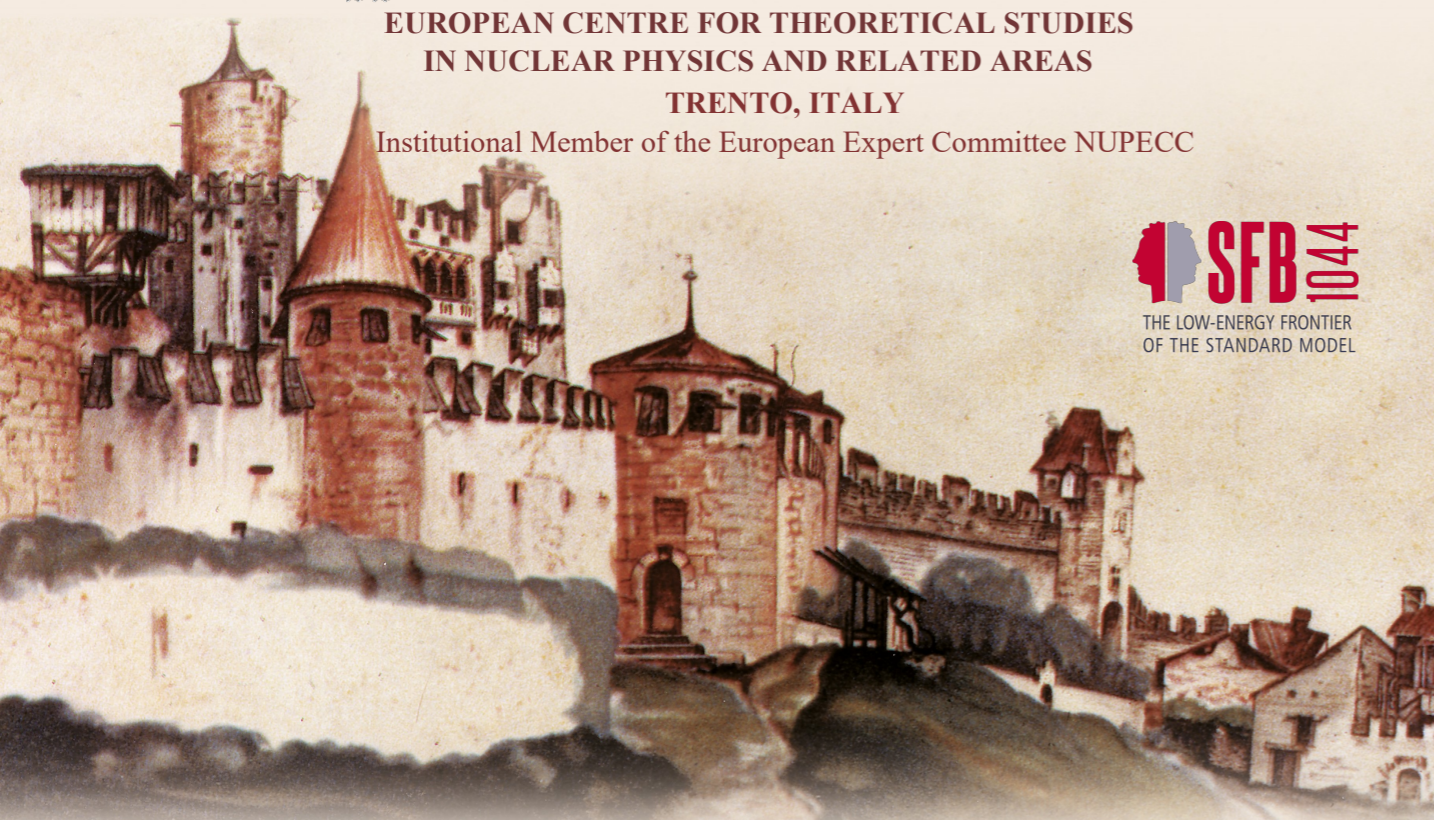
ECT*



EUROPEAN CENTRE FOR THEORETICAL STUDIES
IN NUCLEAR PHYSICS AND RELATED AREAS

TRENTO, ITALY

Institutional Member of the European Expert Committee NUPECC



Castello di Trento ("Trint"), watercolor 19.8 x 27.7, painted by A. Dürer on his way back from Venice (1495). British Museum,

Nucleon Spin Structure at Low Q: A Hyperfine View

Trento, July 2 - 6, 2018

Main Topics

- New measurements of spin structure functions, polarizabilities and form factors
- Sum rules, dispersion relations and empirical parametrizations
- Chiral perturbation theory of nucleon spin polarizabilities
- Progress in lattice QCD of the nucleon spin structure
- Hyperfine structure of muonic hydrogen

Confirmed Speakers

M.W. Ahmed (*Duke University, USA*), J. M. Alarcon (*JLab, USA*), C. Alexandrou (*University of Cyprus, Nicosia, Cyprus*),
 F. Hagelstein (*Universität Bern, Switzerland*), C. Carlson (*College of William and Mary, USA*), S. Kanda (*Riken, Japan*),
 S. Kuhn (*Old Dominion University, USA*), V. Lensky (*Universität Mainz, Germany*), P. Martel (*Universität Mainz, Germany*),
 H.W. Lin (*Michigan State University, USA*), K. Otnad (*Universität Mainz, Germany*), E. Pace (*University of Rome Tor Vergata and INFN, Italy*),
 K. Pachucki (*University of Warsaw, Poland*), A. Pineda (*IFAE, Barcelona, Spain*), Jan Rijneveen (*University of Bochum, Germany*),
 Nora Rijneveen (*University of Bochum, Germany*), M. Ripani (*INFN Genoa, Italy*), S. Sconfiatti (*INFN Pavia, Italy*),
 K. Sliker (*University of New Hampshire, USA*), N. Sparveris (*Temple University, USA*),
 L. Tiator (*Universität Mainz, Germany*), A. Vacchi (*INFN Trieste, Italy*).

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 A. Antognini (*ETH Zurich & PSI, Switzerland*), J.P. Chen (*Thomas Jefferson National Accelerator Facility, USA*)
 V. Pascalutsa (*Universität Mainz, Germany*), M. Vanderhaeghen (*Universität Mainz, Germany*).

Director of the ECT*: Professor Jochen Wambach (ECT*)

The ECT* is sponsored by the "Fondazione Bruno Kessler" in collaboration with the "Assessorato alla Cultura" (Provincia Autonoma di Trento), funding agencies of EU Member and Associated States and has the support of the Department of Physics of the University of Trento.

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THE LOW-ENERGY FRONTIER
OF THE STANDARD MODEL

Nucleon spin structure: highlights and workshop goals

Marc Vanderhaeghen

JOHANNES GUTENBERG
UNIVERSITÄT MAINZ



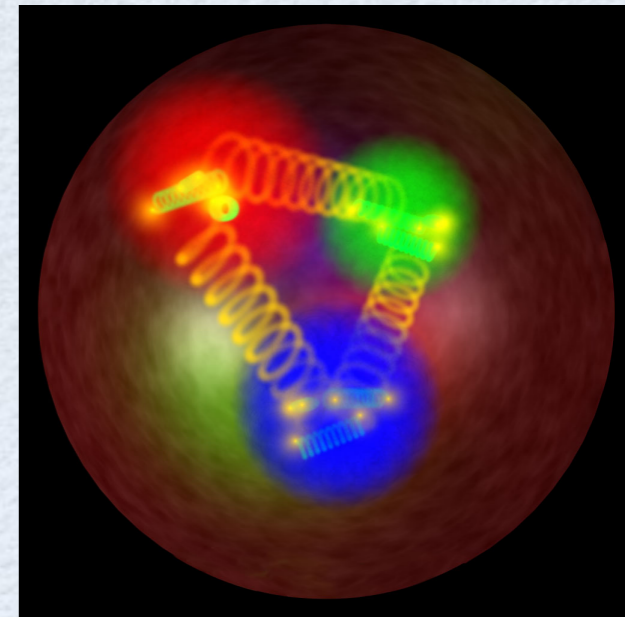
Nucleon spin structure at low Q : dawn of hadron physics



Otto Stern's measurement of the
g-factor of the proton (1932-33):

$$g_{\text{proton}} = 5.586$$

Deviation from point particle value ($g=2$)
indicates that proton has internal structure



Nobel Prize Physics (1943):
“for his contribution to the development of
the molecular ray method and his discovery
of the **magnetic moment of the proton**”

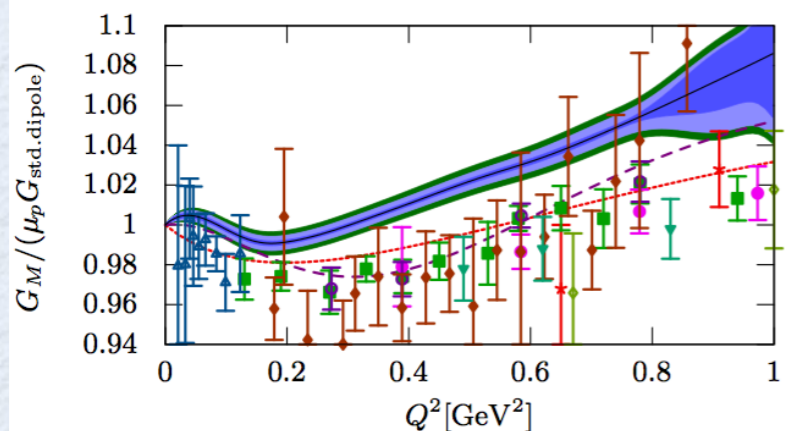
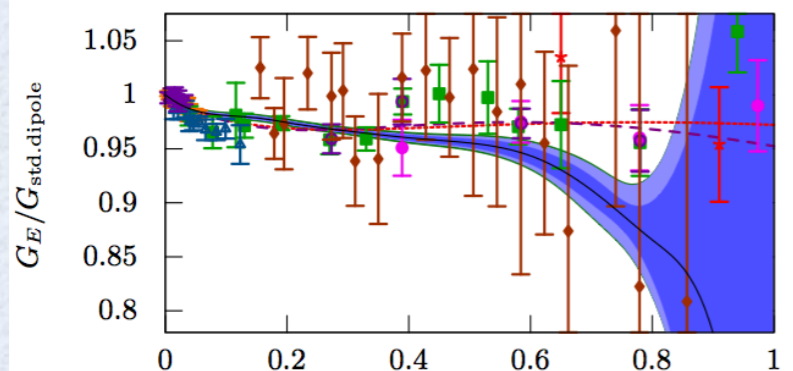
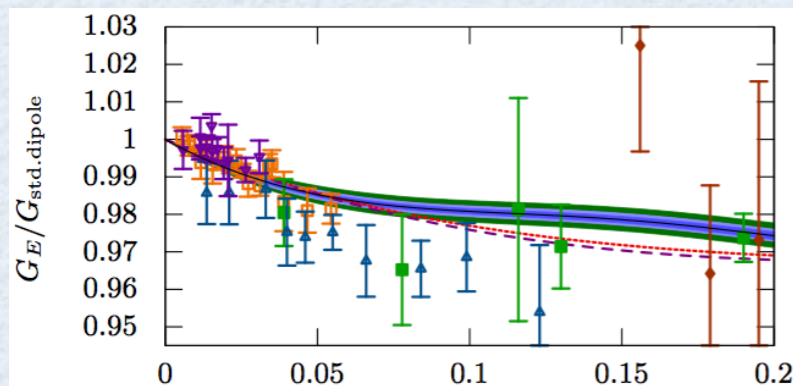
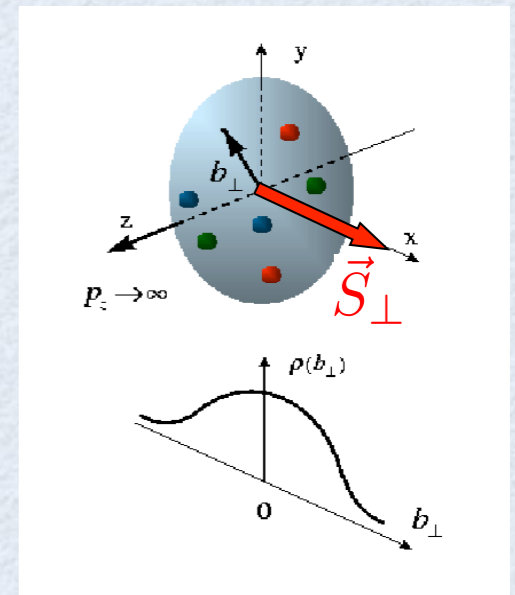
Form factors: 2D densities of hadrons

$$\rho^N(\vec{b}) = \int_0^\infty \frac{dQ}{2\pi} Q J_0(bQ) F_1(Q^2)$$

$$+ \sin(\phi_b - \phi_S) \int_0^\infty \frac{dQ}{2\pi} \frac{Q^2}{2M_N} J_1(bQ) F_2(Q^2)$$

unpolarized
Dirac FF F_1

transverse
polarization
Pauli FF F_2



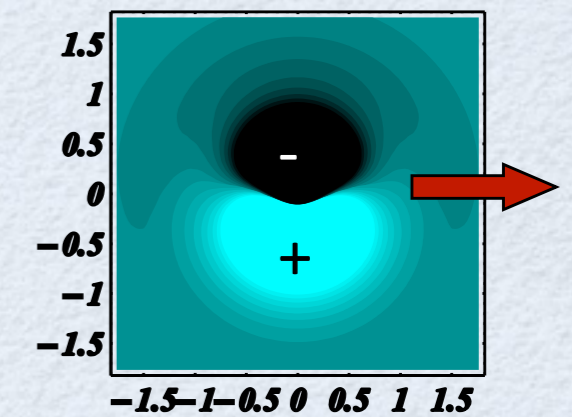
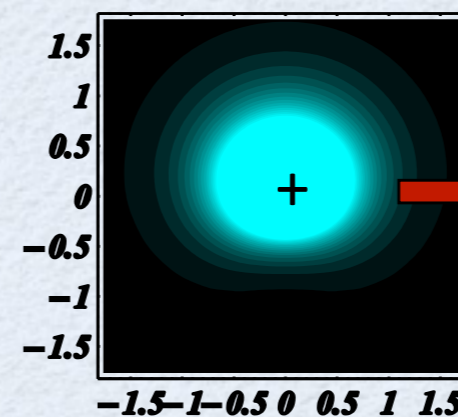
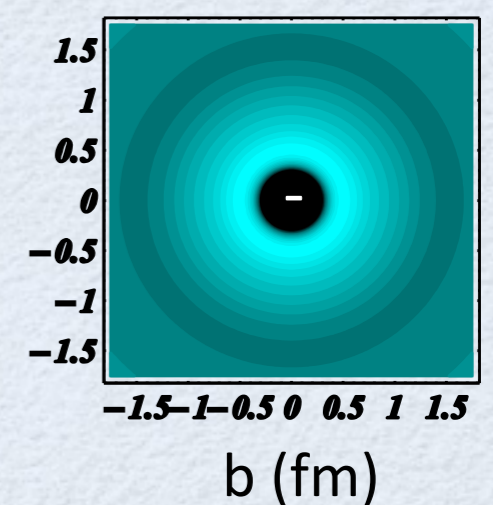
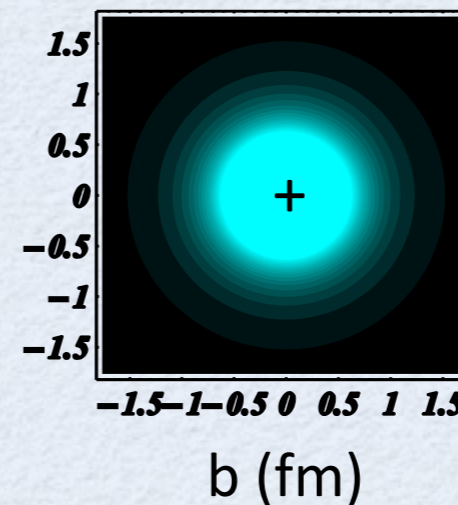
- [3] no TPE ■ Price [65] ■ Borkowski [62]
- - [2] ■ Berger [97] ■ Bartel [99]
- Christy [54] ■ Hanson [98] ■ Murphy [82]
- Simon [58] ■ Janssens [55] ■ Bosted [66]

unpolarized
charge density

density
for transverse
polarization

blue bands:

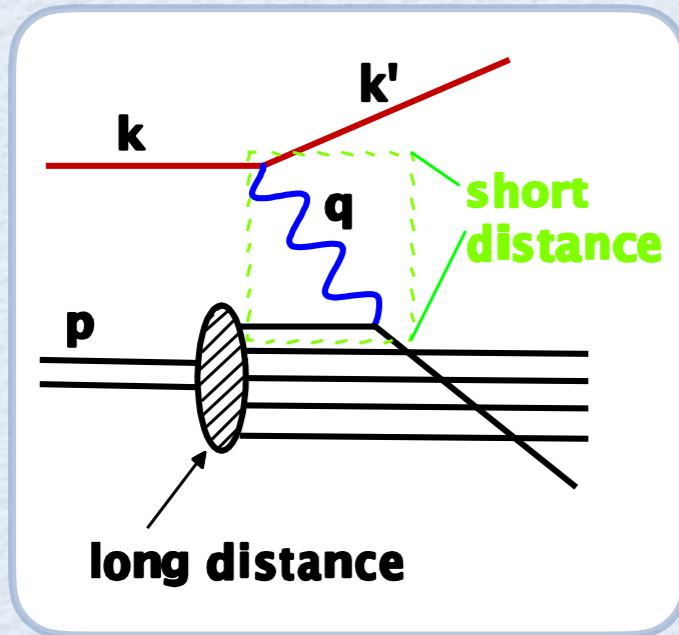
Bernauer et al. (2010, 2013)



Burkardt (2000, 2003)

Miller (2007)
Carlson, Vdh (2008)

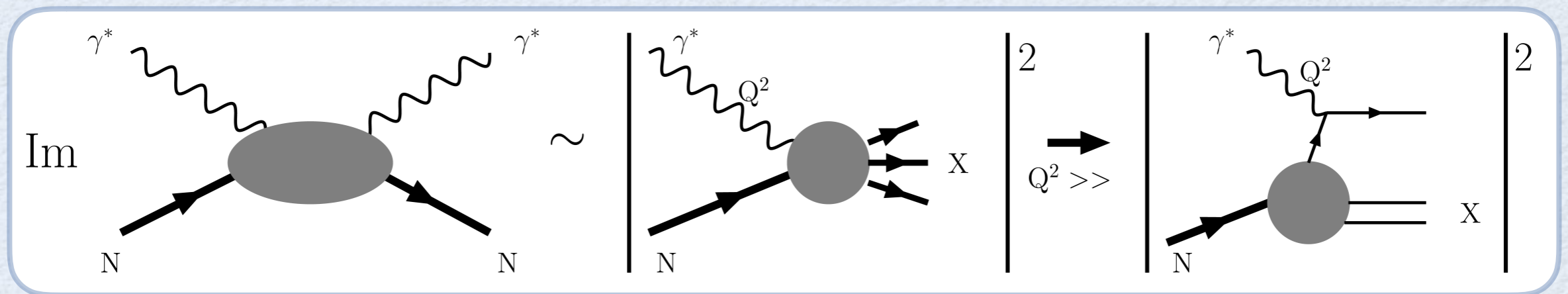
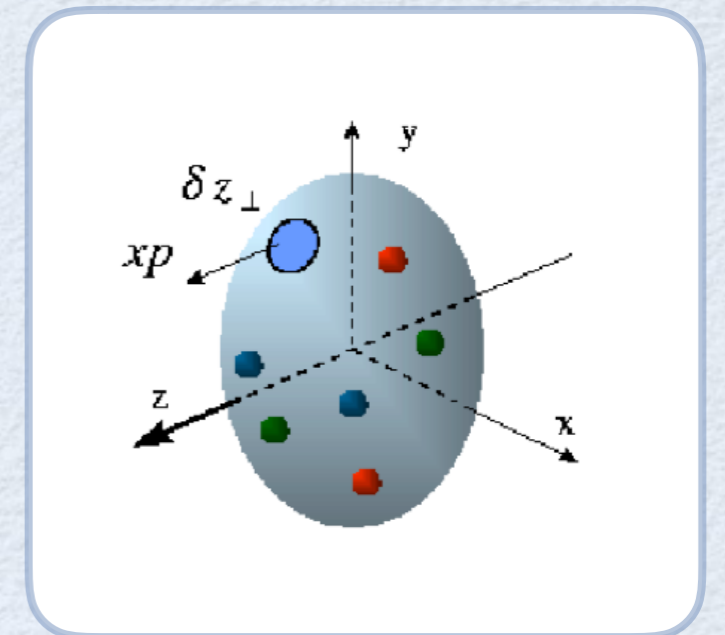
Nucleon spin structure at large Q : Quark-gluon structure



Deep-inelastic scattering

$$Q^2 \gg 1 \text{ GeV}^2$$

$$\text{At fixed } x_B = \frac{Q^2}{2p \cdot q}$$



$$d\sigma \sim L_{\mu\nu} W^{\mu\nu} \quad W_a^{\mu\nu} = \frac{2M_N}{p \cdot q} i\varepsilon^{\mu\nu\alpha\beta} q_{\alpha} \left\{ S_{\beta} g_1(x_B, Q^2) + \left[S_{\beta} - \frac{S \cdot q}{p \cdot q} p_{\beta} \right] g_2(x_B, Q^2) \right\}$$

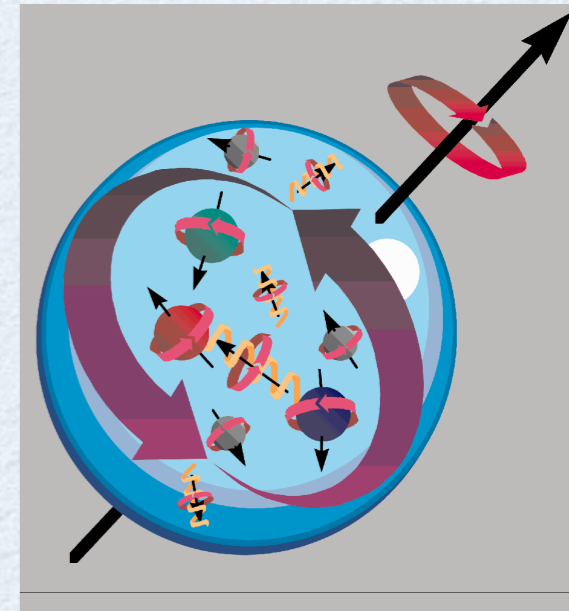
g_1, g_2 : Spin dependent structure functions

Nucleon spin and orbital angular momentum

→ Deep-inelastic experiments:

$$\Delta q \sim 30\% \quad (SIDIS/DIS)$$

$$\Delta G \sim 40\% \quad (RHIC)$$



→ Ji's angular momentum sum rule

Ji (1995)

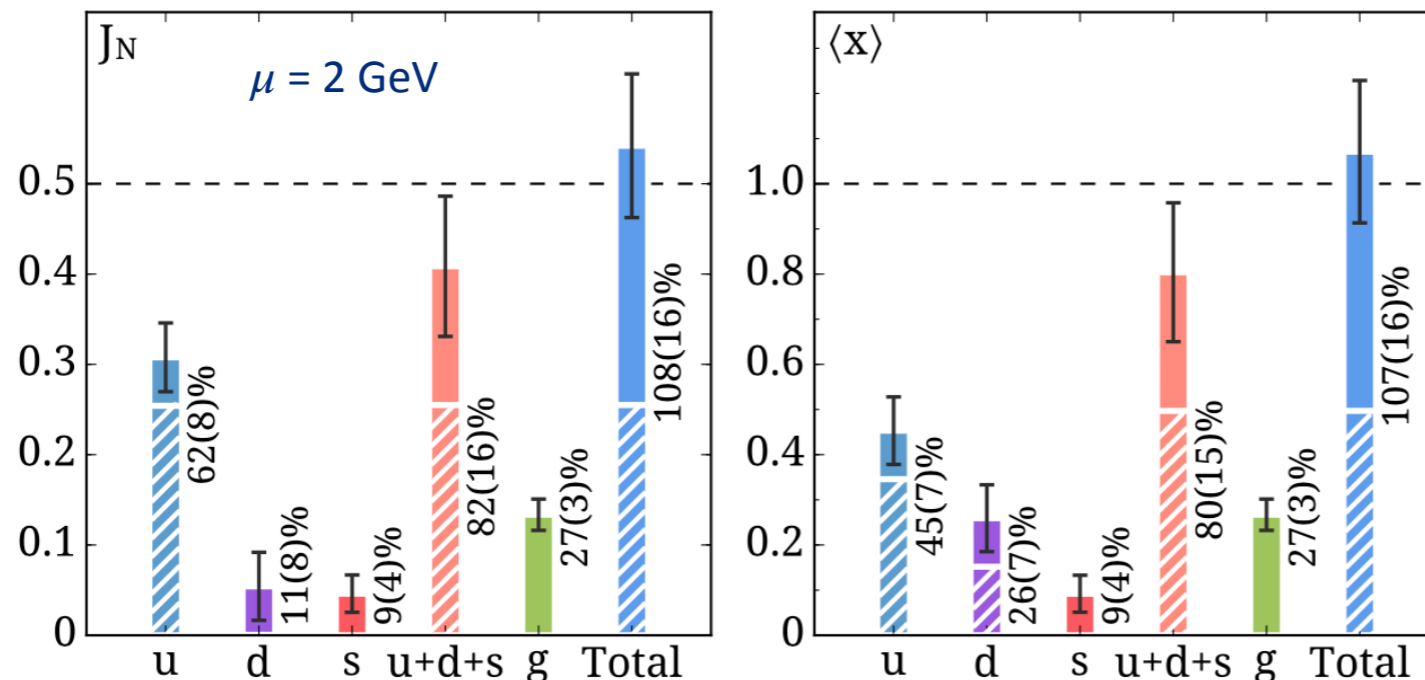
$$\int_{-1}^{+1} dx x \{ H^q(x, \xi, 0) + E^q(x, \xi, 0) \} = A(0) + B(0) = 2J^q$$

H, E : generalized parton distributions (GPDs)

→ lattice QCD calculations at the physical point

see talks: Alexandrou, Lin, Ottnad

Alexandrou et al. (2017)

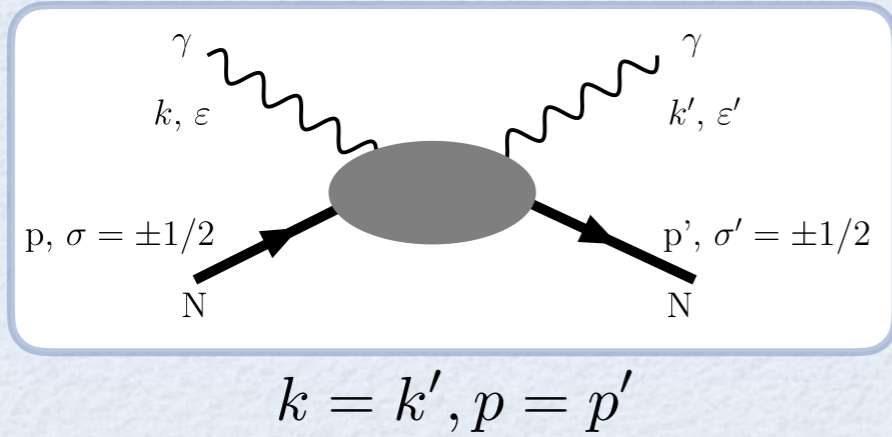


d, s-quarks carry very small total J in proton, u-quark carries around 60%, gluons around 30%

Sharing of momentum and total angular momentum between quarks and gluons identical in proton !

Nucleon spin structure with real photons

→ forward real Compton scattering



$$T(\nu, \theta = 0) = \vec{\varepsilon}'^* \cdot \vec{\varepsilon} f(\nu) + i\vec{\sigma} \cdot (\varepsilon'^* \times \vec{\varepsilon}) g(\nu)$$

low-energy expansion

$$f(\nu) = \frac{-e^2}{4\pi M} + (\alpha_E + \beta_M) \nu^2 + \mathcal{O}(\nu^4)$$

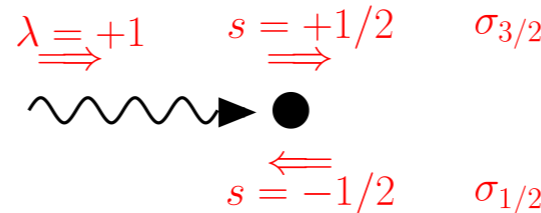
$$g(\nu) = \frac{-e^2 \kappa^2}{8\pi M^2} \nu + \gamma_0 \nu^3 + \mathcal{O}(\nu^5)$$

LET

polarizabilities

→ term in ν : GDH sum rule

$$\frac{e^2 \pi \kappa^2}{2M^2} = \int_{\nu_0}^{\infty} d\nu' \frac{\sigma_{3/2} - \sigma_{1/2}}{\nu'}$$



$$\Delta\sigma = \sigma_{3/2} - \sigma_{1/2} \quad \vec{\gamma} \vec{p} \rightarrow X$$

Gerasimov (1966); Drell, Hearn (1966)

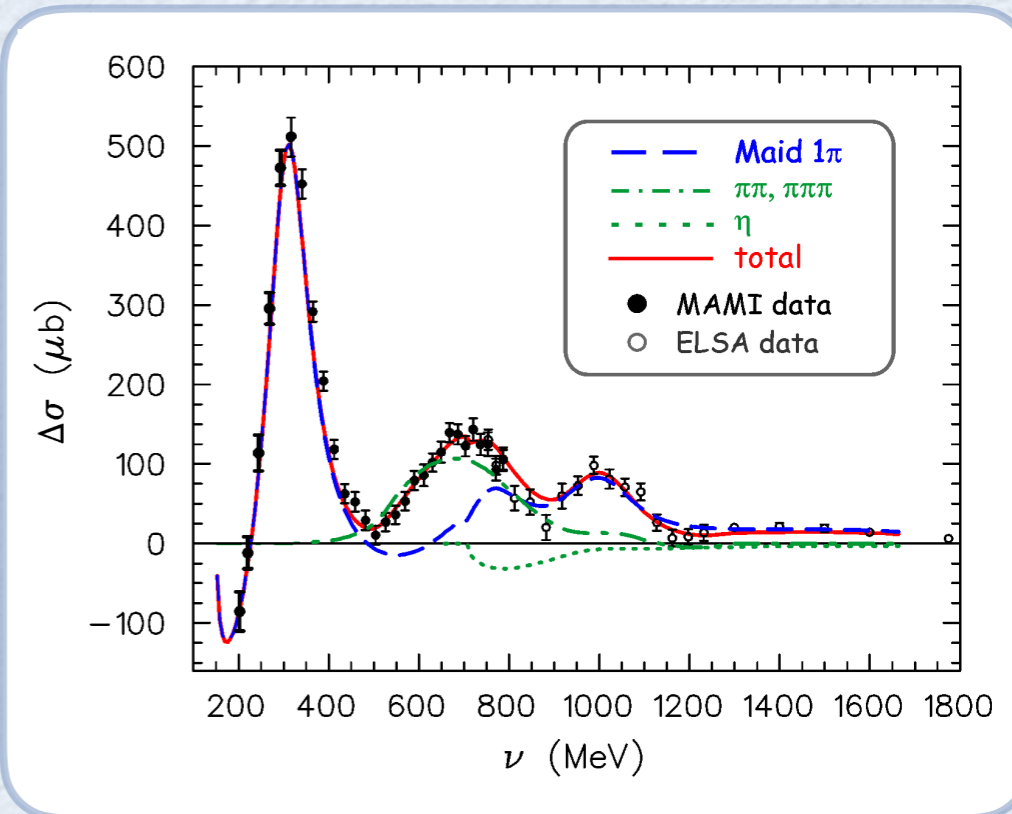
lhs SR: **204 μb** rhs SR: **(211 \pm 15) μb** ✓

→ term in ν^3 : forward spin polarizability sum rule

$$\gamma_0 = -\frac{1}{4\pi^2} \int_{\nu_0}^{\infty} d\nu' \frac{\sigma_{3/2} - \sigma_{1/2}}{\nu'^3}$$

proton:

$$\gamma_0 = -(1.01 \pm 0.08 \pm 0.10) \times 10^{-4} \text{ fm}^4$$



Drechsel, Tiator (2004)

Proton spin polarizabilities

→ effective Hamiltonian (3rd order): nucleon spin polarizabilities

$$H_{\text{eff}}^{(3)} = -4\pi \left[\frac{1}{2} \gamma_{E1E1} \vec{\sigma} \cdot (\vec{E} \times \dot{\vec{E}}) + \frac{1}{2} \gamma_{M1M1} \vec{\sigma} \cdot (\vec{H} \times \dot{\vec{H}}) - \gamma_{M1E2} E_{ij} \sigma_i H_j + \gamma_{E1M2} H_{ij} \sigma_i E_j \right]$$

forward spin polarizability

$$\gamma_0 = -\gamma_{E1E1} - \gamma_{E1M2} - \gamma_{M1E2} - \gamma_{M1M1}$$

→ theory predictions (units $10^{-4} \times \text{fm}^4$): dispersion theory Drechsel, Pasquini, Vdh (2000)
chiral EFT McGovern, Phillips, Griesshammer (2013)

Lensky, McGovern, Pascalutsa (2015)

Pasquini, Vdh: *Ann. Rev. Nucl. Part. Sci.* 68 (2018) 75-103

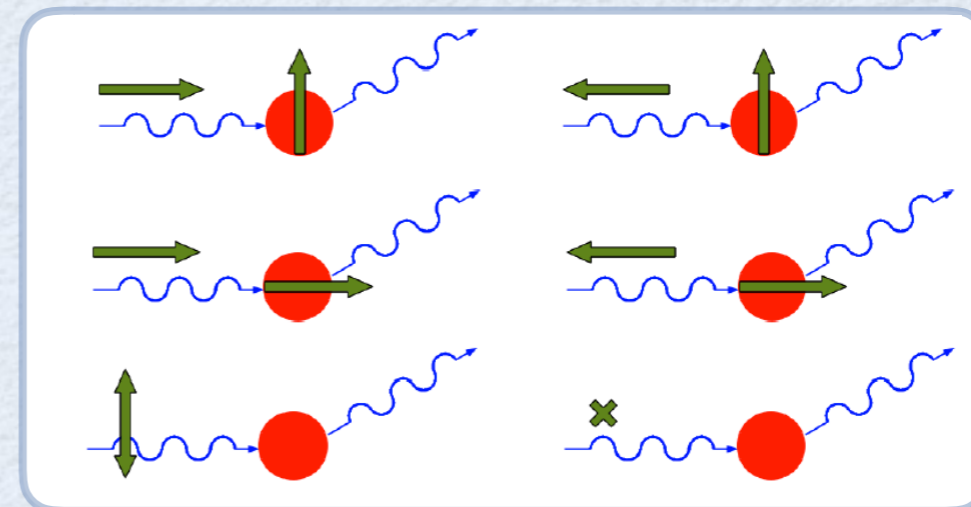
	Σ_{2x} and Σ_3^{LEGS}	Σ_{2x} and Σ_3^{MAMI}	DRs	HChPT	BChPT	L_χ
γ_{E1E1}	-3.5 ± 1.2	-5.0 ± 1.5	-4.5	-1.1 ± 1.8	-3.3 ± 0.8	-3.7
γ_{M1M1}	3.16 ± 0.85	3.13 ± 0.88	3.0	2.2 ± 0.7^a	2.9 ± 1.5	2.5
γ_{E1M2}	-0.7 ± 1.2	1.7 ± 1.7	-0.08	-0.4 ± 0.4	0.2 ± 0.2	1.2
γ_{M1E2}	1.99 ± 0.29	1.26 ± 0.43	2.3	1.9 ± 0.4	1.1 ± 0.3	1.2

MAMI/A2 data Martel et al. (2015)

→ polarized Compton scattering
measure angular dependence of asymmetries

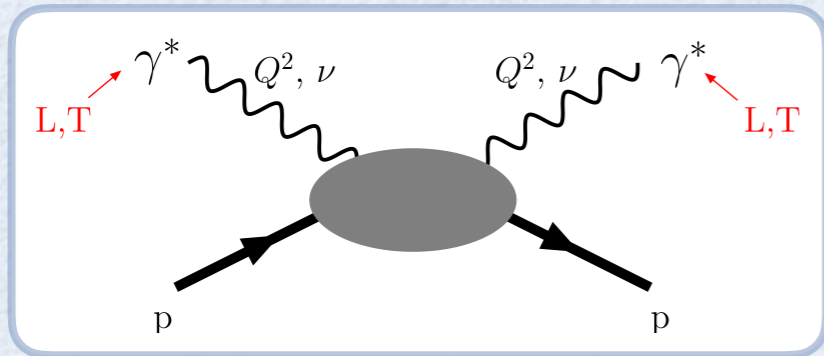
see talks: Ahmed, Martel (exp);

Pascalutsa, Sconfiatti (th)



Nucleon spin structure with virtual photons

forward, virtual Compton scattering



$$T_{spin}^{\mu\nu} = \frac{i}{M} \epsilon^{\nu\mu\alpha\beta} q_\alpha s_\beta S_1(\nu, Q^2) + \frac{i}{M^3} \epsilon^{\nu\mu\alpha\beta} q_\alpha (p \cdot q s_\beta - s \cdot q p_\beta) S_2(\nu, Q^2)$$

$$\text{Im } S_1(\nu, Q^2) = \frac{e^2}{4M} \frac{M}{\nu} g_1(x, Q^2), \quad \text{Im } S_2(\nu, Q^2) = \frac{e^2}{4M} \frac{M^2}{\nu^2} g_2(x, Q^2)$$

spin structure functions

moments of spin structure functions (x_0 : inelastic threshold)

$$\Gamma_1(Q^2) = \int_0^{x_0} dx g_1(x, Q^2)$$

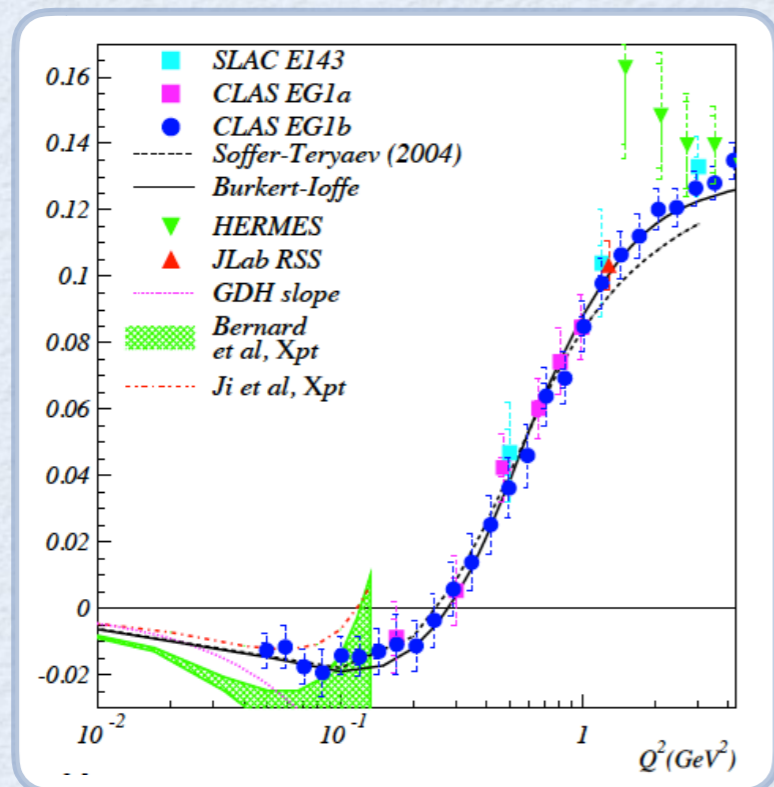
$$\frac{Q^2}{2M^2} \left(-\frac{\kappa^2}{4} \right), \quad Q^2 \rightarrow 0$$

$$\Gamma_1(Q^2)|_{scaling}, \quad Q^2 \rightarrow \infty$$

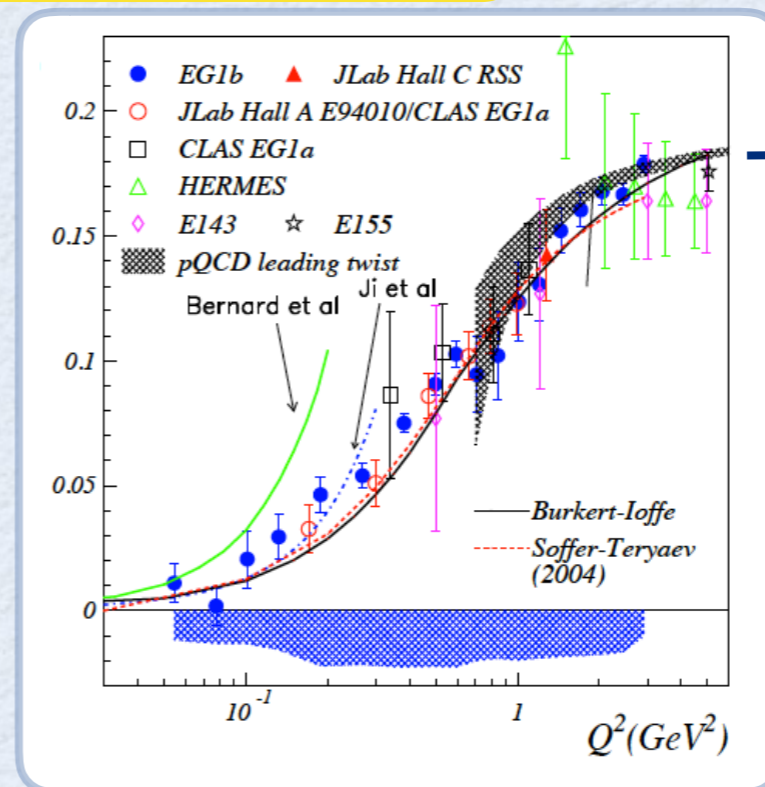
GDH sum rule

parton helicity structure (DIS)

Γ_1^p



Γ_1^{p-n}



$$\frac{1}{6} g_A \left\{ 1 - \frac{\alpha_s}{\pi} + \dots \right\}$$

Bjorken sum rule

see talks:
Kuhn, Chen,
Ripani, Slifer

Chen (2010)

Nucleon spin polarizabilities with virtual photons

➔ higher moments of spin structure functions: spin polarizabilities

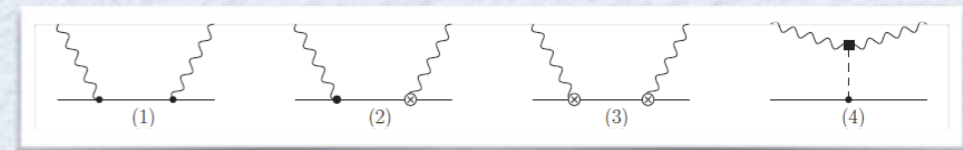
$$\gamma_0(Q^2) = \frac{4M^2 e^2}{\pi Q^6} \int_0^{x_0} dx x^2 \left\{ g_1(x, Q^2) - \frac{4M^2}{Q^2} x^2 g_2(x, Q^2) \right\} \rightarrow \gamma_0, \quad Q^2 \rightarrow 0$$

$$\delta_{LT}(Q^2) = \frac{4e^2 M^2}{\pi Q^6} \int_0^{x_0} dx x^2 \left\{ g_1(x, Q^2) + g_2(x, Q^2) \right\}$$

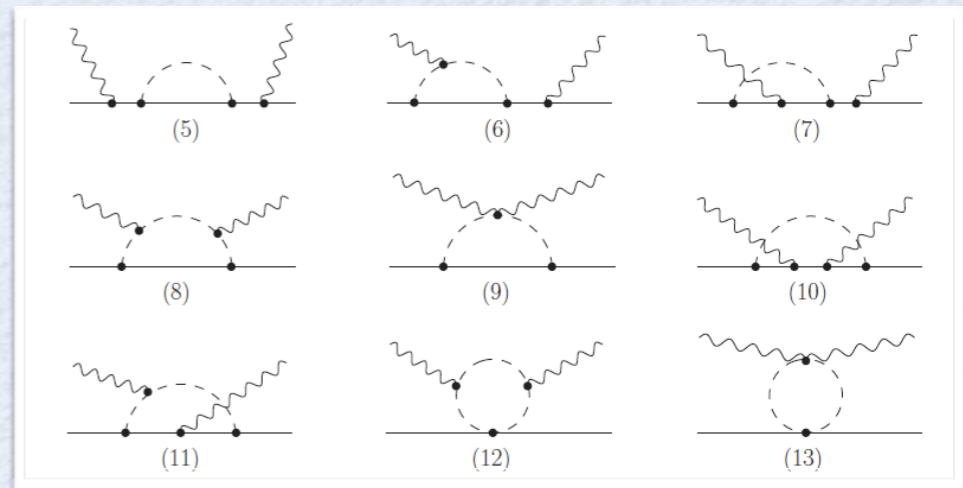
➔ provide strong test for theory:
chiral EFT calculations / lattice QCD

Lensky, Alarcon, Pascalutsa (2014)

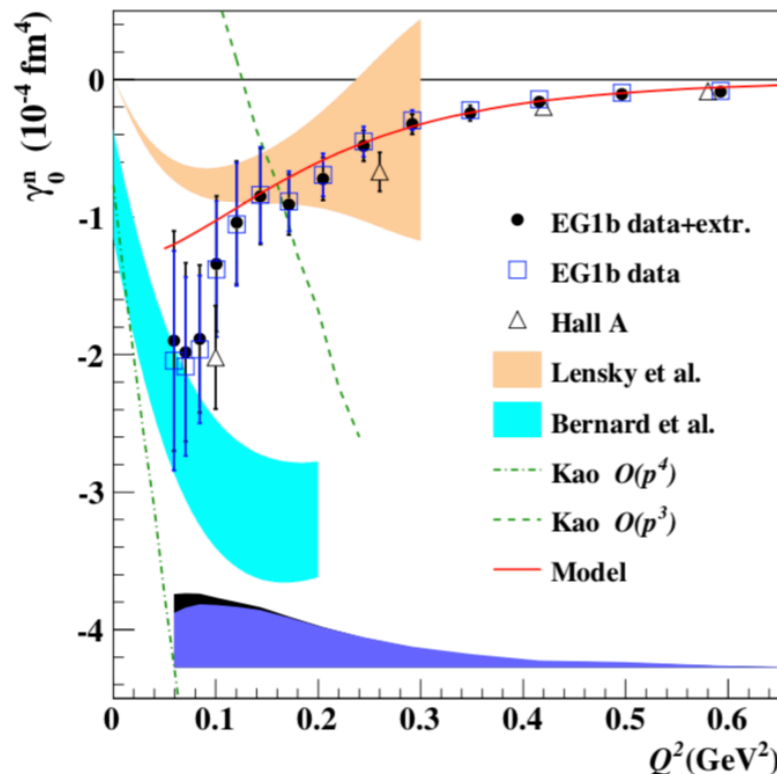
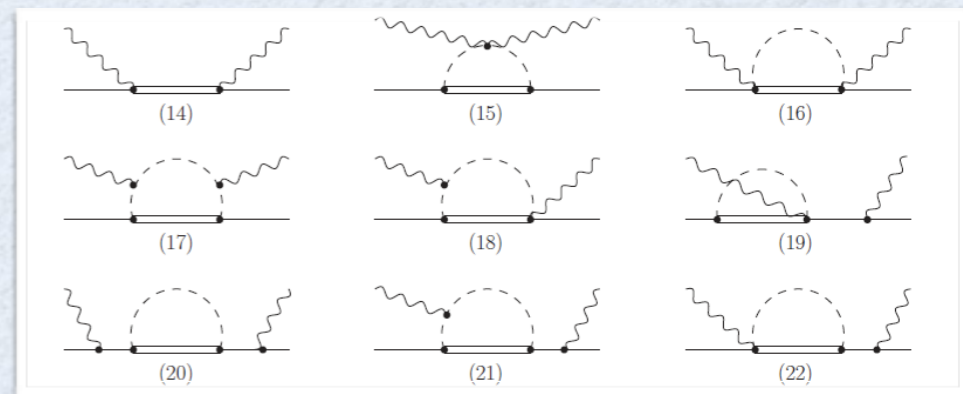
LO



NLO



NNLO



JLab/CLAS data Guller et al. (2015)

see talks: Pascalutsa, Lensky, Rijnvee 9

New spin sum rules with virtual photons at low Q

Can we formulate sum rules relating observables to observables for virtual photons as is the case for real photons (GDH, FSP) ?

→ low-energy expansion for virtual photons

$$(S_1 - S_1^{\text{pole}})(\nu, Q^2) = -\frac{e^2}{8\pi M} \kappa^2 + M\gamma_0 \nu^2 + M\gamma_L Q^2 + \mathcal{O}(Q^4, \nu^4, Q^2\nu^2)$$

$$\gamma_L = \frac{e^2}{24\pi M^2} \kappa^2 \langle r_2^2 \rangle + \gamma_{E1M2} - 3M \frac{e^2}{4\pi} [P'^{(M1,M1)1}(0) + P'^{(L1,L1)1}(0)]$$

$P^{(M1,M1)1}(Q^2), P^{(L1,L1)1}(Q^2)$ Generalized Polarizabilities
 -> measured in Virtual Compton Scattering

→ sum rule for I_1

$$(S_1 - S_1^{\text{pole}})(\nu = 0, Q^2) = \frac{e^2}{2\pi M} I_1(Q^2) \quad \text{with} \quad I_1(Q^2) = \frac{2M^2}{Q^2} \int_0^{x_0} dx g_1(x, Q^2)$$

$$I_1'(0) = \frac{\kappa^2}{12} \langle r_2^2 \rangle + \frac{2\pi M^2}{e^2} \gamma_{E1M2} - \frac{3M^3}{2} [P'^{(M1,M1)1}(0) + P'^{(L1,L1)1}(0)]$$

Pascalutsa, Vdh (2015)

Sum rules relating RCS, VCS, VVCS
 Can be tested by experiment !

New spin sum rules with virtual photons

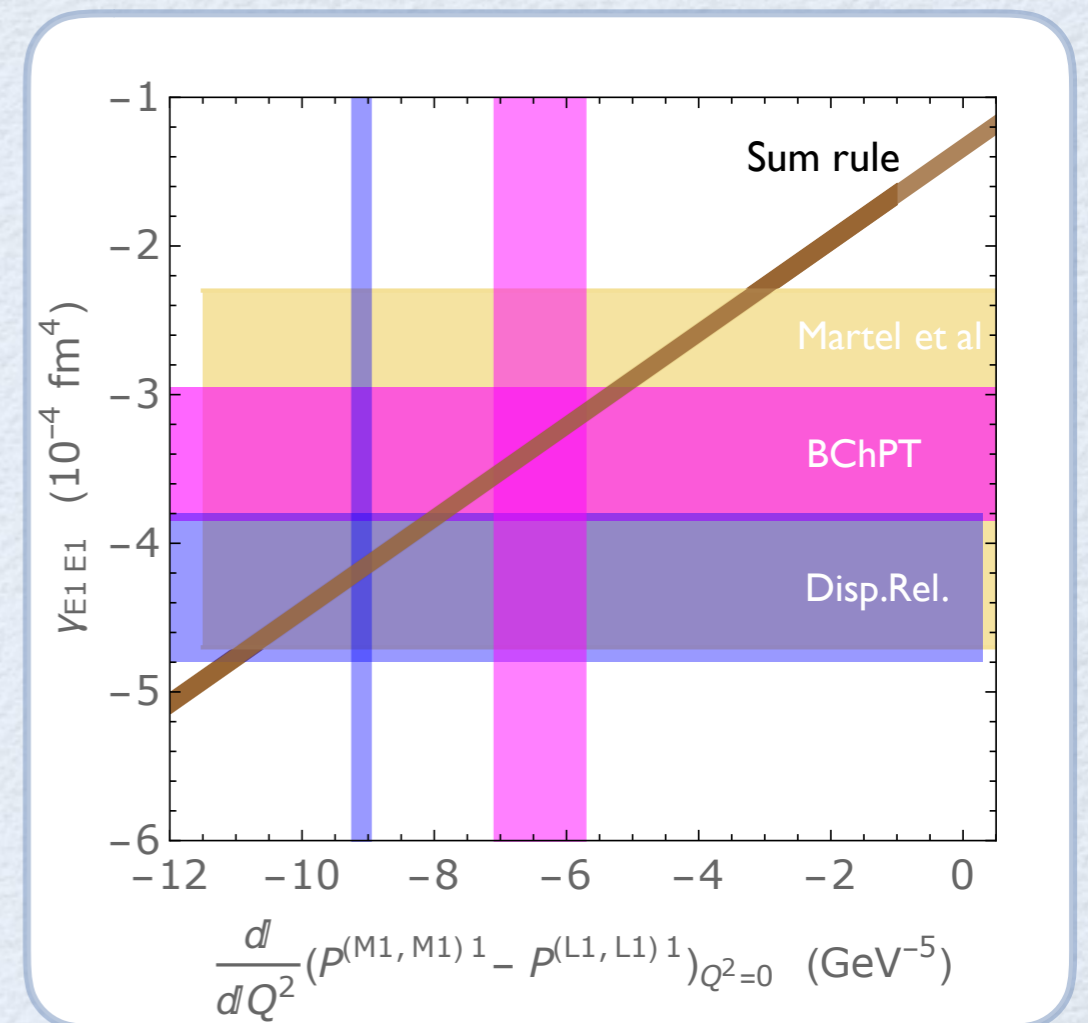
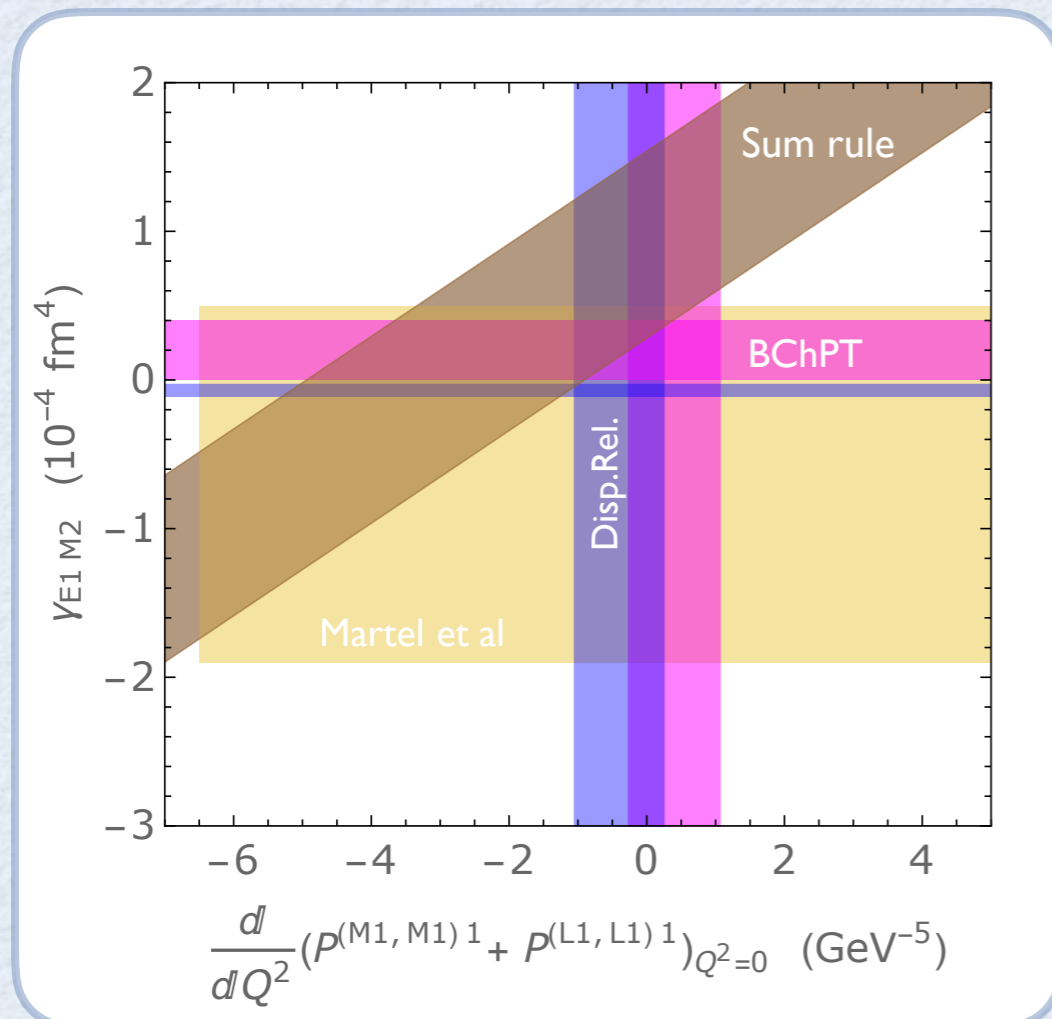
$$I_1(Q^2) = \frac{2M^2}{Q^2} \int_0^{x_0} dx g_1(x, Q^2)$$

$$\delta_{LT}(Q^2) = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} dx x^2 [g_1 + g_2](x, Q^2)$$

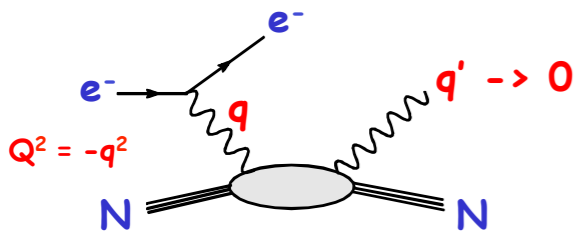
$$I_1'(0) = \frac{\kappa^2}{12} \langle r_2^2 \rangle + \frac{2\pi M^2}{e^2} \gamma_{E1M2} - \frac{3M^3}{2} [P'^{(M1,M1)1}(0) + P'^{(L1,L1)1}(0)]$$

$$\delta_{LT}(0) = -\gamma_{E1E1} + 3M \frac{e^2}{4\pi} [P'^{(M1,M1)1}(0) - P'^{(L1,L1)1}(0)]$$

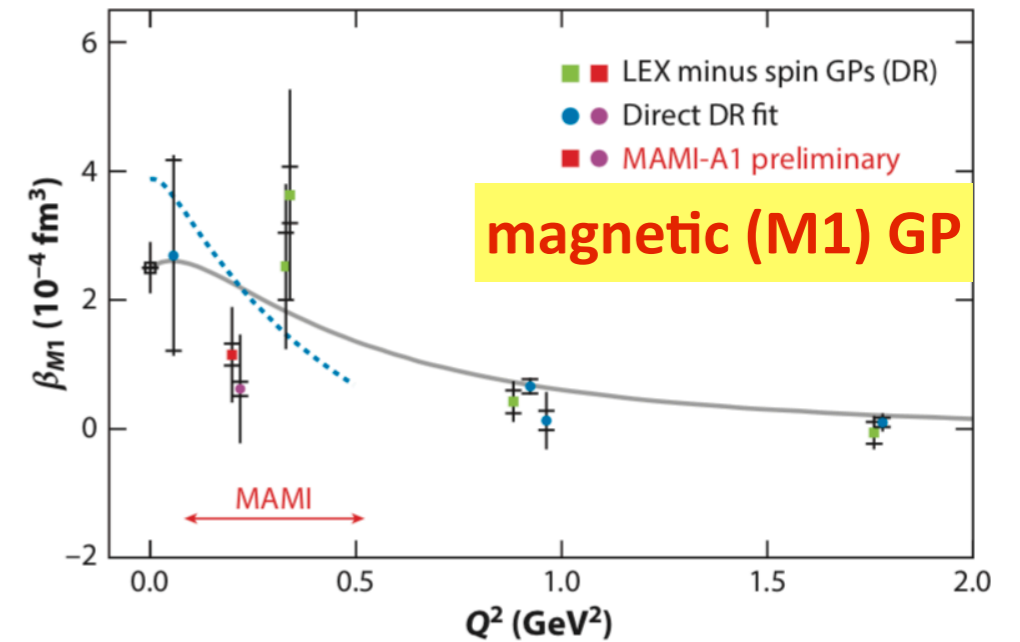
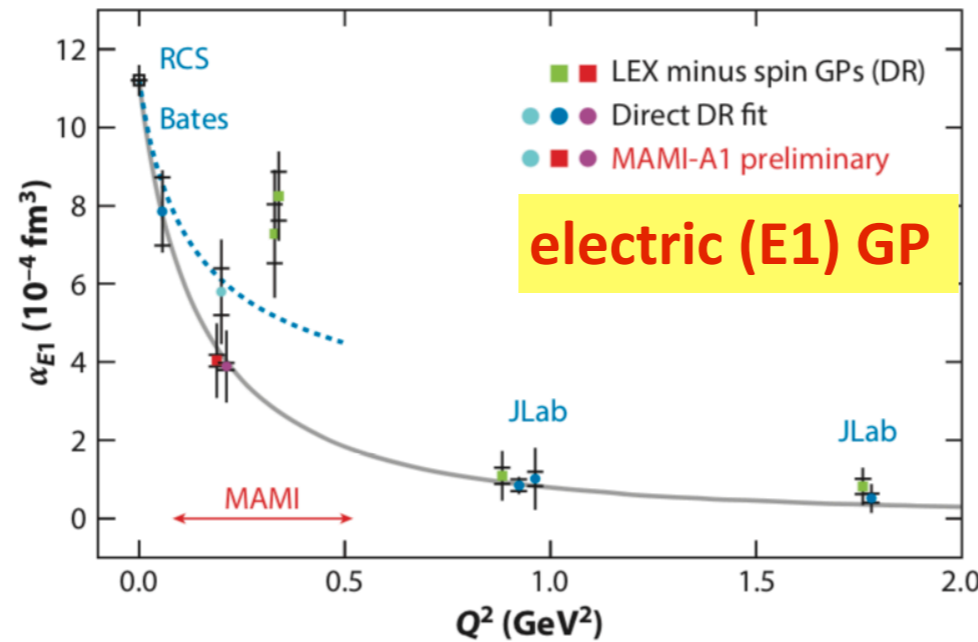
Pascalutsa, Vdh (2015)



Generalized Polarizabilities of nucleon



new MAMI data
 Correa (2016)
 Blomberg (2016)
 see talk: Sparveris



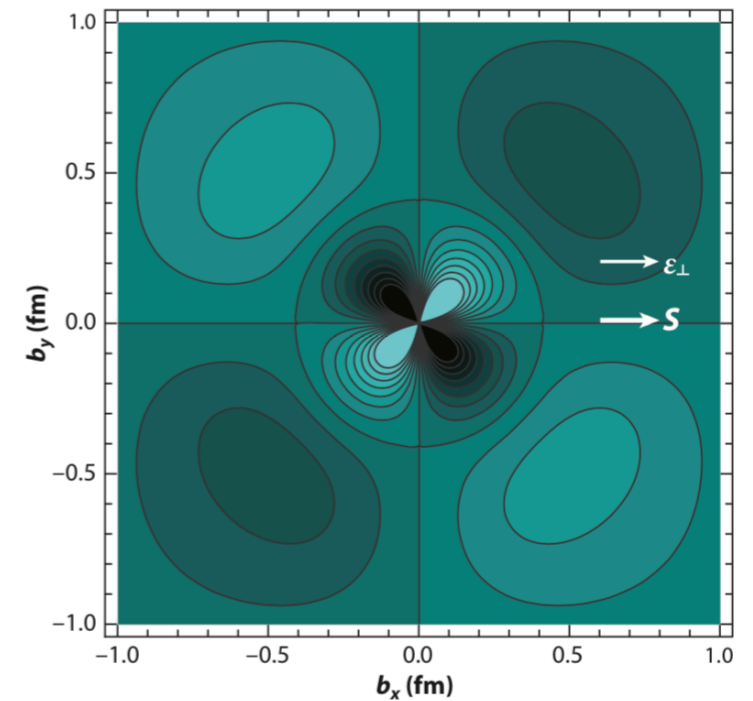
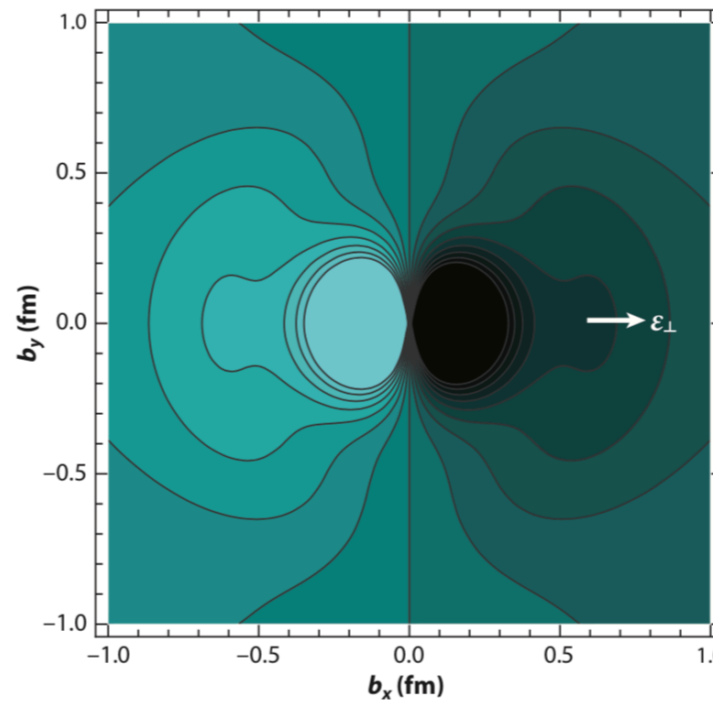
energy shift: $\delta E = -\vec{E} \cdot \vec{P}_0$

induced polarization

$$\vec{P}_0(\vec{b}) = \int \frac{d^2 \vec{q}_\perp}{(2\pi)^2} e^{-i\vec{q}_\perp \cdot \vec{b}} \vec{P}_0(\vec{q}_\perp)$$

$$= \hat{b} \int_0^\infty \frac{dQ}{(2\pi)} Q J_1(bQ) A(Q^2)$$

combination of nucleon
 generalized polarizabilities



Gorchtein, Lorcé, Pasquini, Vdh (2009) ; Pasquini, Vdh (2018)

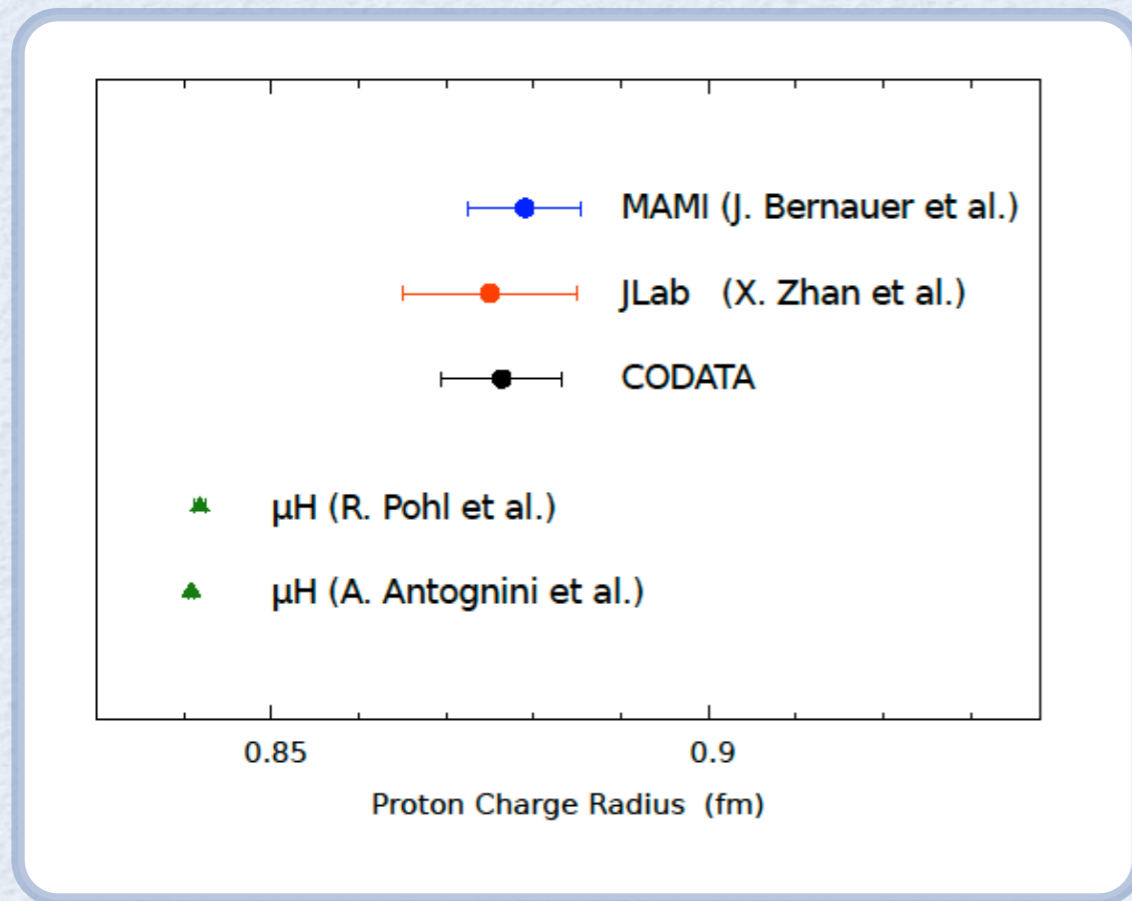
Proton structure in Hydrogen spectroscopy



s-wave leptons have a finite probability to be found at the origin of the proton:

-> sensitivity to the charge/magnetization distribution of the proton

Lamb shift: Proton charge radius puzzle



μH data:

$$R_E = 0.8409 \pm 0.0004 \text{ fm}$$

Pohl et al. (2010)

Antognini et al. (2013)

5.6 σ difference !?

ep data:

$$R_E = 0.8775 \pm 0.0051 \text{ fm}$$

CODATA (2012)

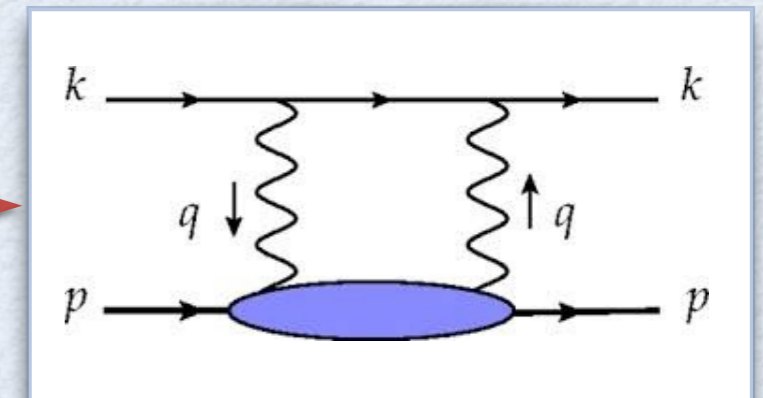
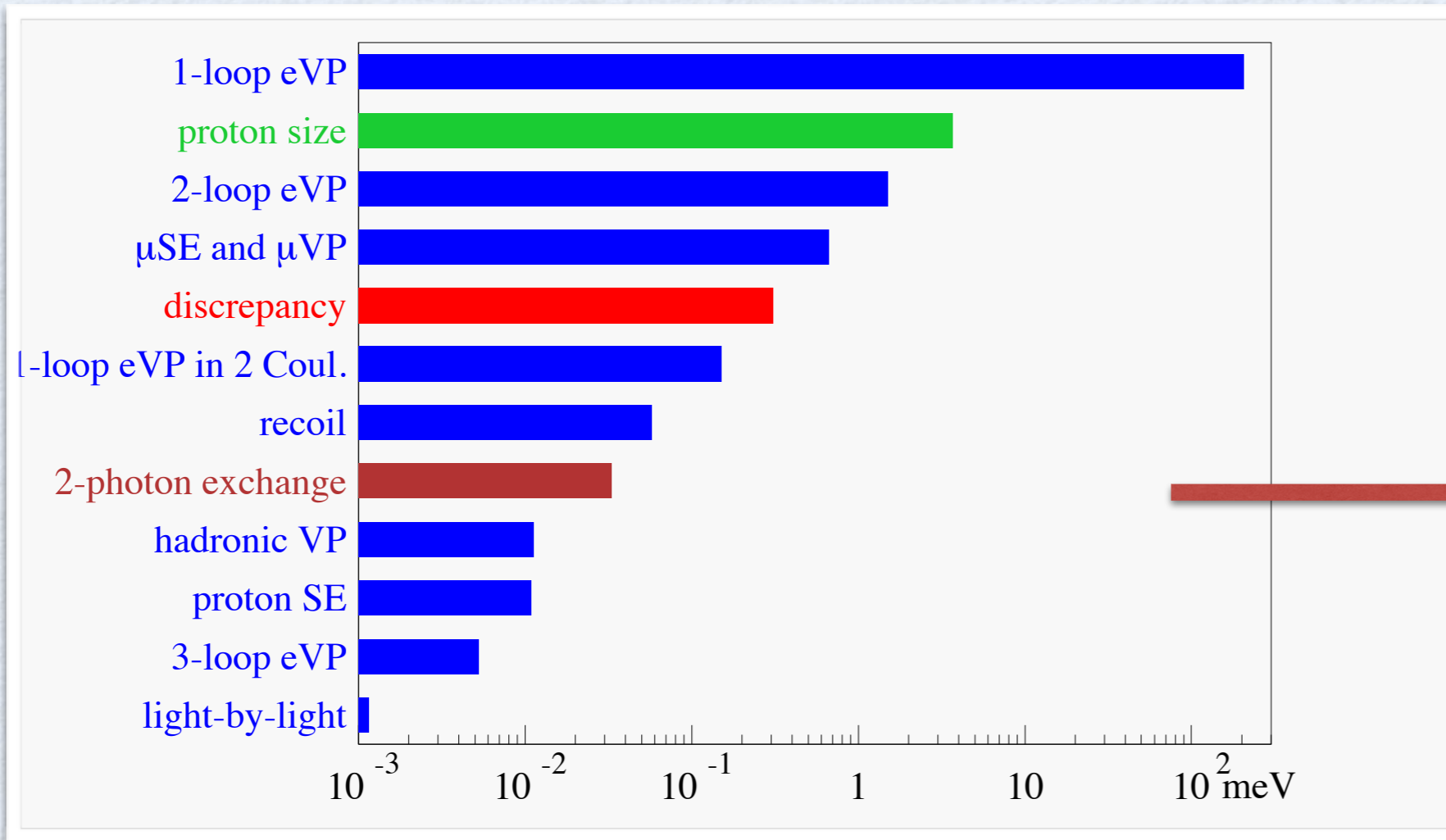
see talks:

Gasparian (exp)

Alarcon (th)

Lamb shift: status of known corrections

μH Lamb shift: summary of corrections



Two-photon exchange: largest theoretical uncertainty

Muonic hydrogen hyperfine splitting: TPE for proton spin dependent amplitude

forthcoming PSI
1S-HFS measurement in μH
with 1 ppm accuracy

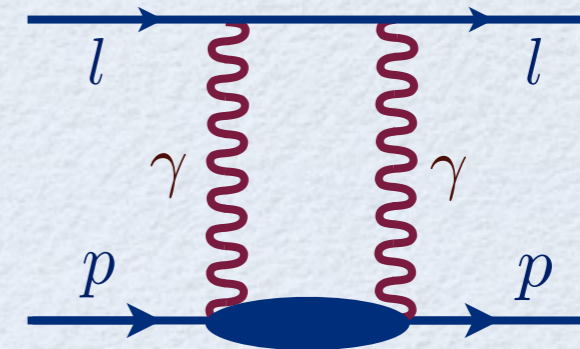
see talks: Antognini, Kanda

1S-HFS in μH

	relative contribution ($\times 10^{-3}$)	relative uncertainty
X=p (Zemach)	-7,36	140 ppm
X=p (recoil)	0,8476	0.8 ppm
X=p, $\pi\text{N}, \dots$ (polarizability)	0,363	86 ppm
total	-6,149	164 ppm

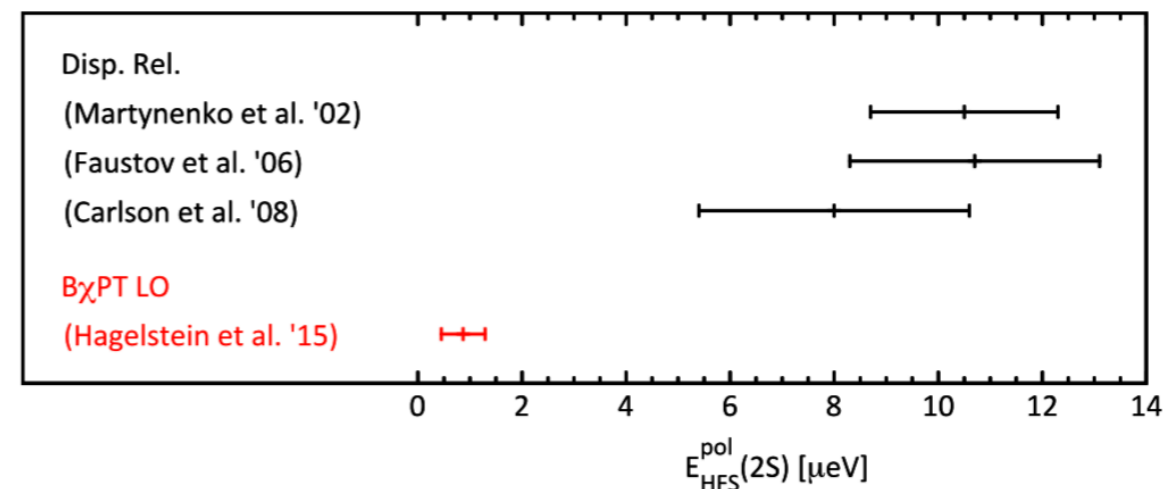
Carlson, Nazaryan, Griffioen (2011) ;

Tomalak et al. (2016)



see talks:

Carlson, Distler, Hagelstein, Pachucki, Pineda

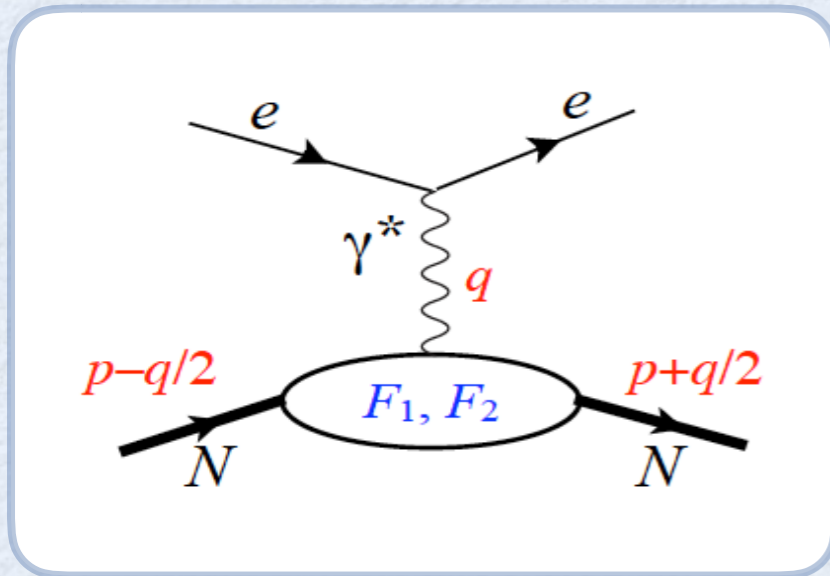


Hagelstein, Miskimen, Pascalutsa

Prog. Part. Nucl. Phys. 88 (2016) 29–97

Impressive 1 ppm accuracy requires improvement on 2χ !!

Precise G_M at low Q^2 needed

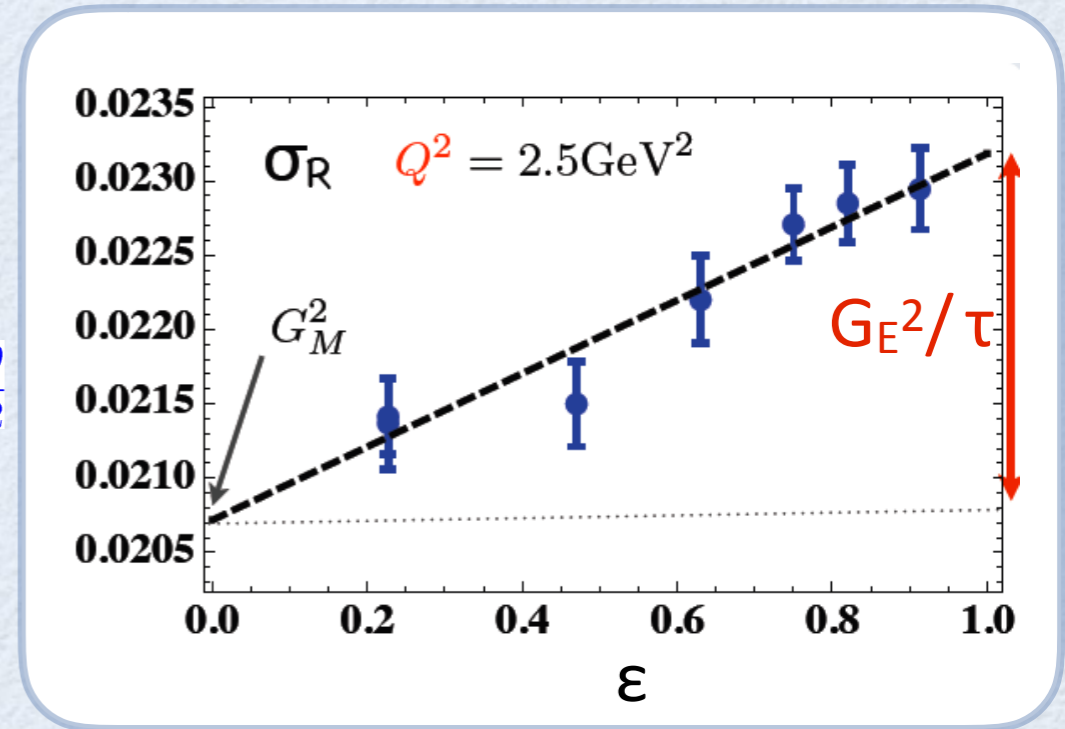


$$G_M = F_1 + F_2$$

$$G_E = F_1 - \tau F_2$$

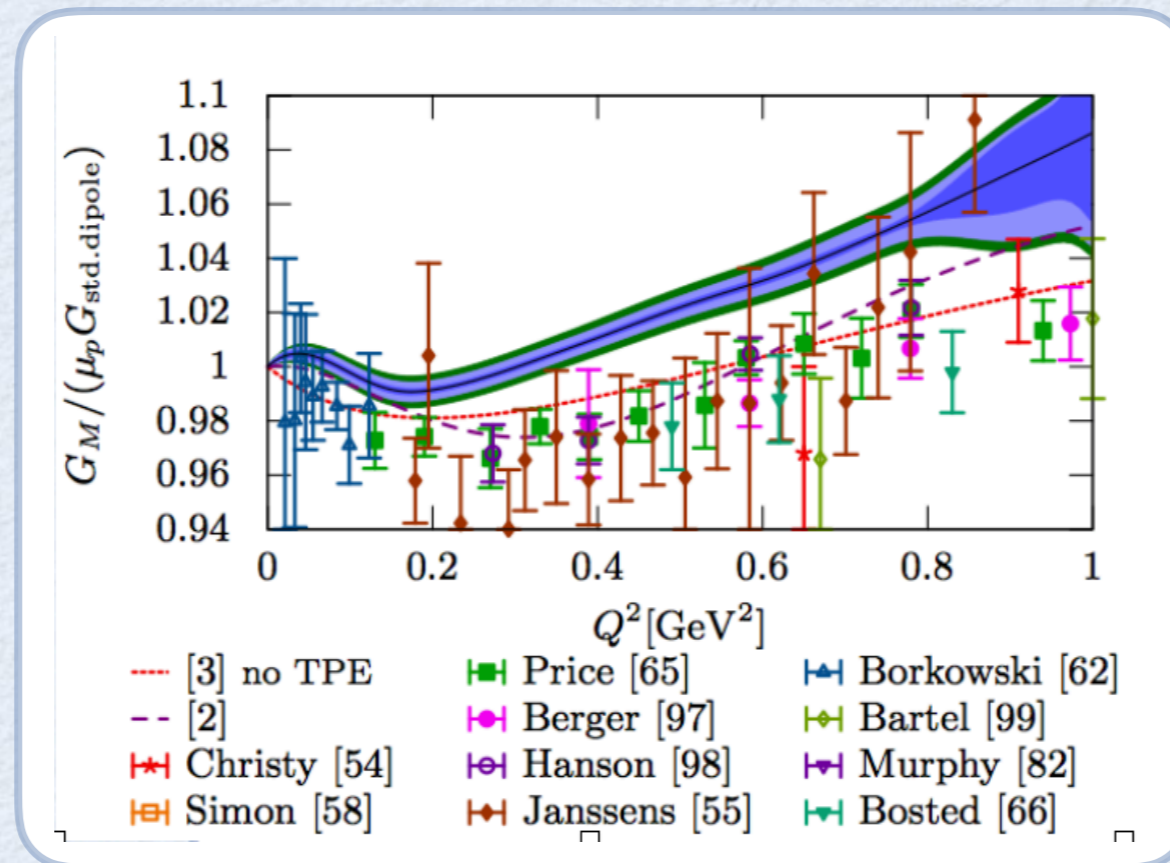
$$\tau \equiv \frac{Q^2}{4M^2} \quad \frac{1}{\varepsilon} \equiv 1 + 2(1 + \tau) \tan^2 \frac{\theta}{2}$$

$$\sigma_R = G_M^2 + \frac{\varepsilon}{\tau} G_E^2$$



Rosenbluth separation technique

Andivahis et al. (1994)



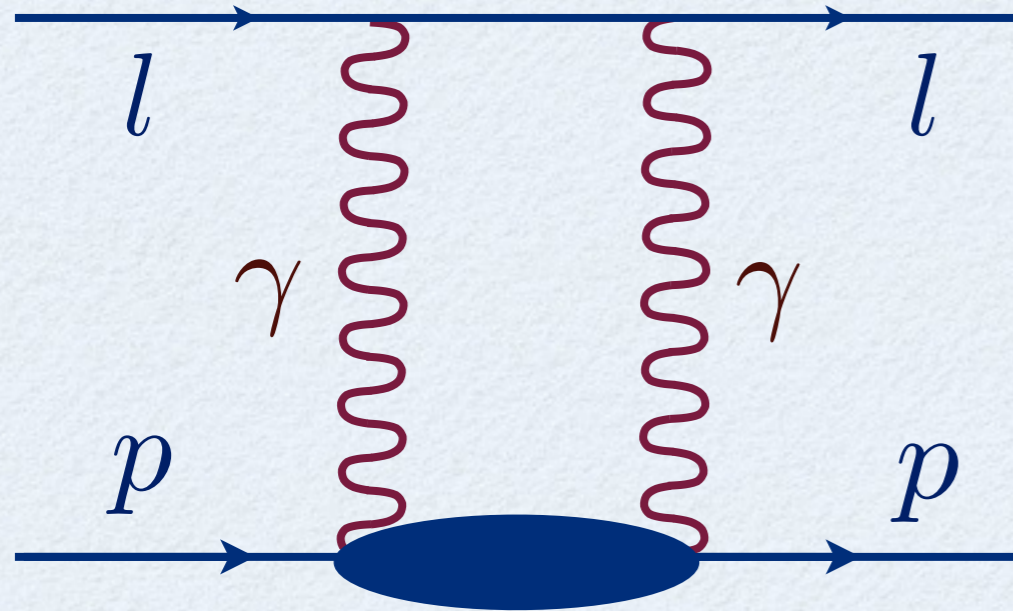
Bernauer et al. (2010, 2013)

see talk:

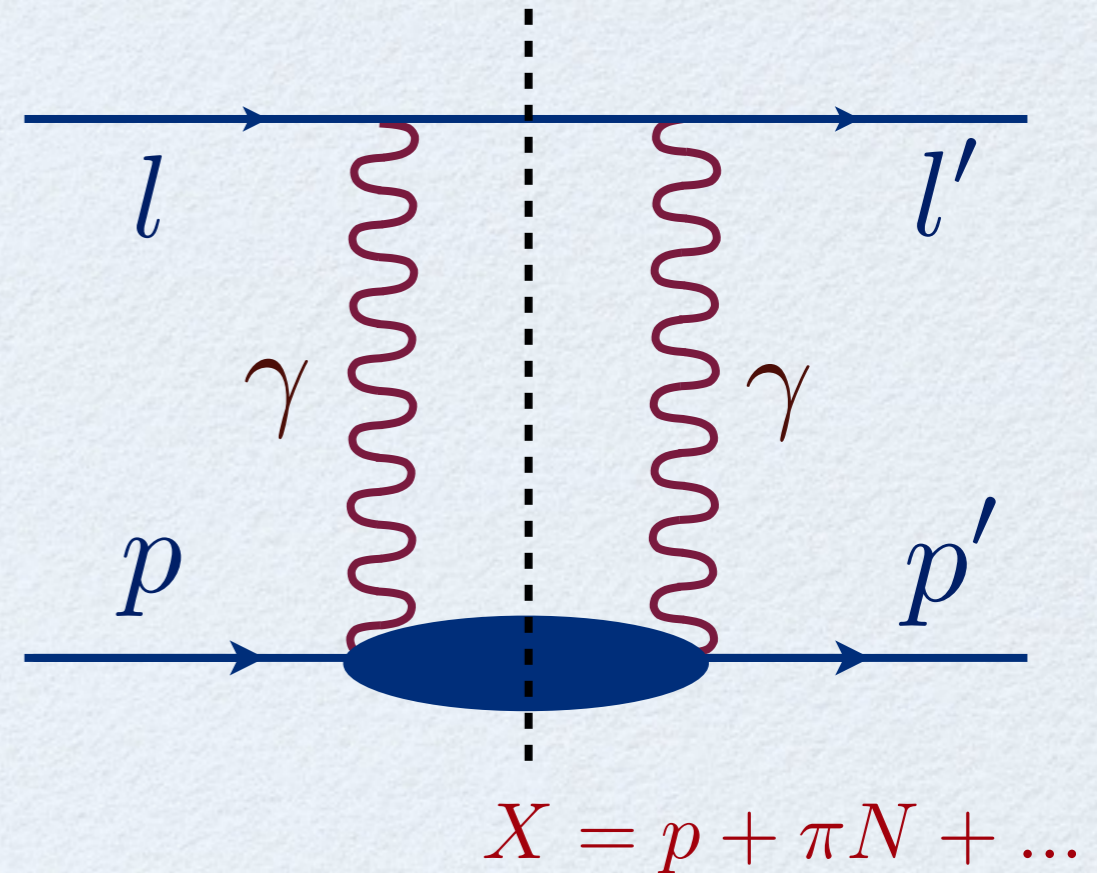
Bernauer

TPE in dispersive framework

forward scattering



non-forward scattering
account for **all inelastic** 2γ



dispersion relations

based on on-shell information

Borisyuk, Kobushkin (2008)

Tomalak, Vdh (2014, 2015, 2016)

Pasquini, Tomalak, Vdh (2017)

2 γ -exchange at low Q^2

$$\delta_{2\gamma} \sim a \sqrt{Q^2} + b Q^2 \ln Q^2 + c Q^2 \ln^2 Q^2$$

Feshbach
inelastic
elastic

McKinley, Feshbach (1948)

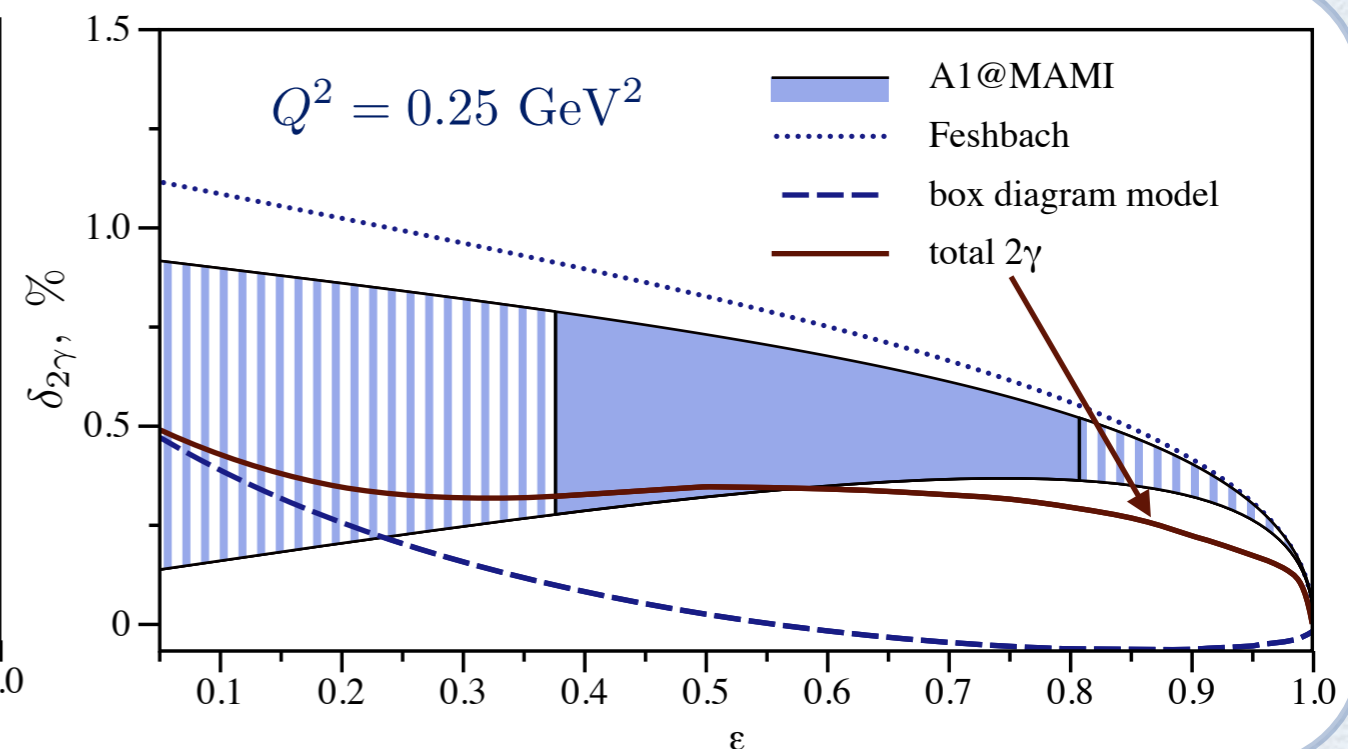
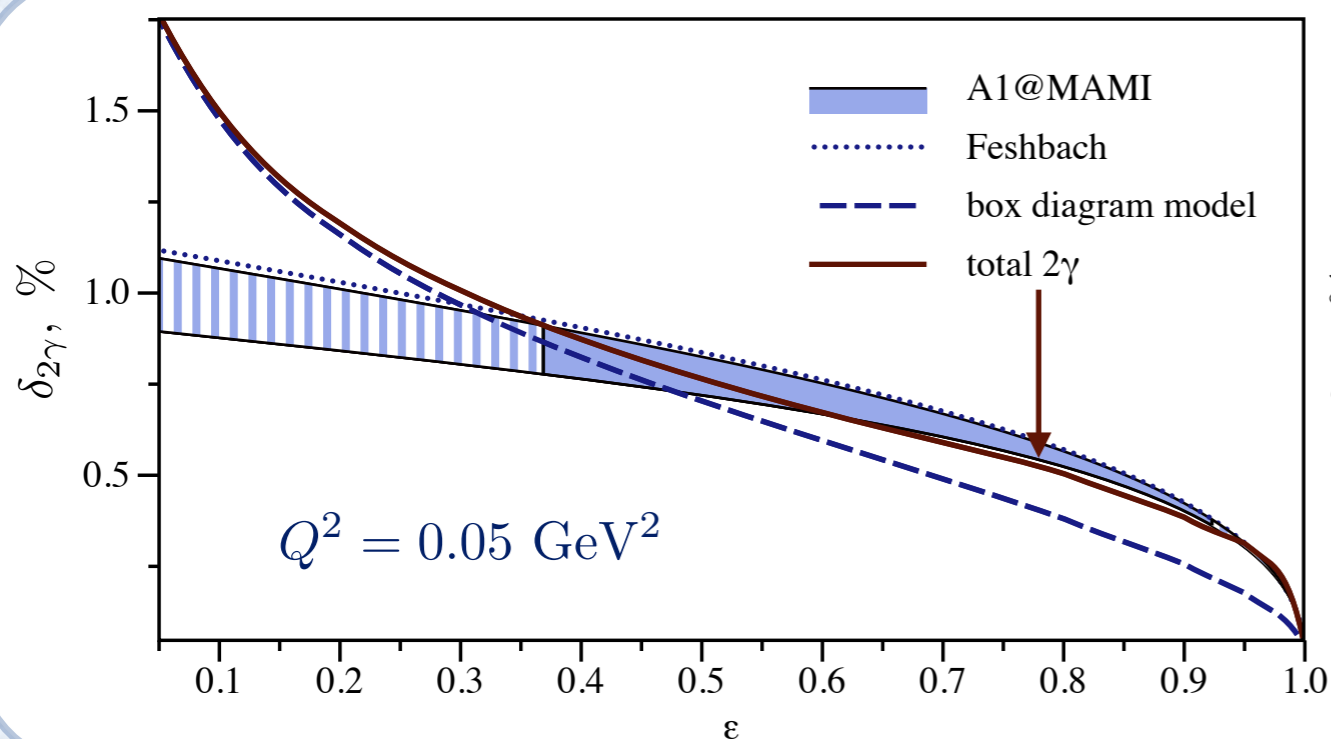
R.W. Brown (1970)

M. Gorchtein (2013)

$$\delta_{2\gamma} = \int d\nu_\gamma d\tilde{Q}^2 (\omega_1(\nu_\gamma, \tilde{Q}^2) \cdot F_1(\nu_\gamma, \tilde{Q}^2) + \omega_2(\nu_\gamma, \tilde{Q}^2) \cdot F_2(\nu_\gamma, \tilde{Q}^2))$$

unpolarized proton structure

Tomalak, Vdh (2016)



- 2 γ at large ϵ agrees with empirical fit: G_E extraction ✓
- deviations from empirical fit seen at low ϵ : G_M extraction sensitive

Workshop goals

- ➔ **Hadronic corrections** to hyperfine splitting in **muonic H**
 - crucial input: G_M , spin polarizabilities, polarized structure functions, ...
- ➔ **Elastic electron scattering** has reached level of precision where TPE effects are clearly visible
 - high precision data forthcoming: PRad@JLab, MAGIX@MESA
 - full assessment of TPE corrections needed
- ➔ **Spin structure functions at low Q^2 : experiment**
 - several JLab 6 GeV analysis completed or near completed
 - polarizability program: RCS, VCS
 - what are next experimental steps?
- ➔ **Theoretical understanding of low Q^2 spin structure:**
 - new sum rules relating RCS, VCS, and VVCS can be tested in exp. in a model independent way
 - what is the state of ChEFT in describing the low Q^2 spin structure
 - test for theory used for calculating the proton spin structure in hyperfine splitting in muonic H

wish you a productive meeting