

---

# A recent paper on FT quarkonium polarization

Physics Letters B 840 (2023) 137871



Contents lists available at [ScienceDirect](#)

Physics Letters B

journal homepage: [www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)



## Low- $p_T$ quarkonium polarization measurements: Challenges and opportunities



Pietro Faccioli<sup>a,\*</sup>, Ilse Krätschmer<sup>b</sup>, Carlos Lourenço<sup>c</sup>

<sup>a</sup> LIP, Lisbon, Portugal

<sup>b</sup> ISTA, Klosterneuburg, Austria

<sup>c</sup> CERN, Geneva, Switzerland

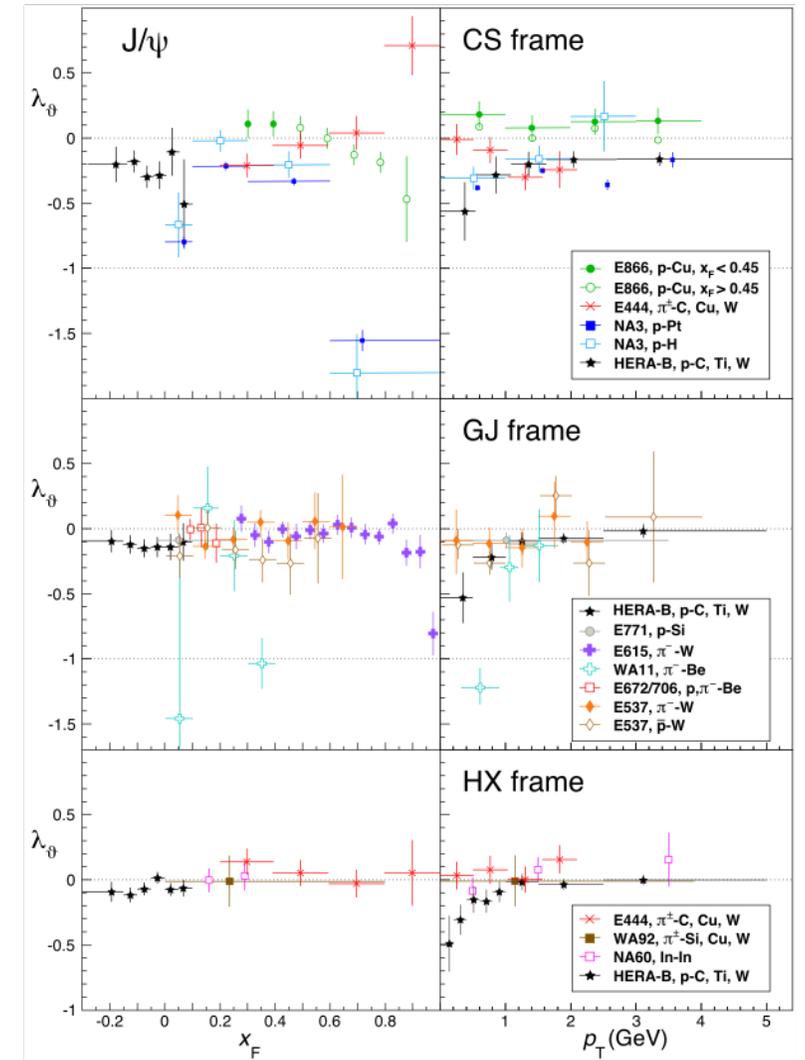
Stephane Platchkov

Paris-Saclay University, CEA/IRFU, France

# Measurements considered: J/psi

*“In this paper we devote our attention to low- $p_T$  quarkonium hadro-production, a kinematical domain complementary to that explored in collider experiments.”*

- ◆ Consider all FT quarkonia polarization data
  - Data in three different frames
  - Different particles ( $p$ ,  $\pi^+$ ,  $\pi^-$ ,  $\bar{p}$ ) and energies
    - sqrt(s) from 15.3 to 41.6 GeV
  - Absence of acceptance correlation between  $\cos\theta$  and  $\varphi$
  - Most polarization values for J/psi are near 0



**Fig. 1.** The  $J/\psi$  polar anisotropy parameter  $\lambda_\theta$  measured in the CS, GJ, and HX frames (top to bottom), vs.  $x_F$  and  $p_T$ .

# Polarization

---

◆  $J/\psi$  is a  $1^-$  particle; its third component is  $J_z = 0, +1, -1$ .

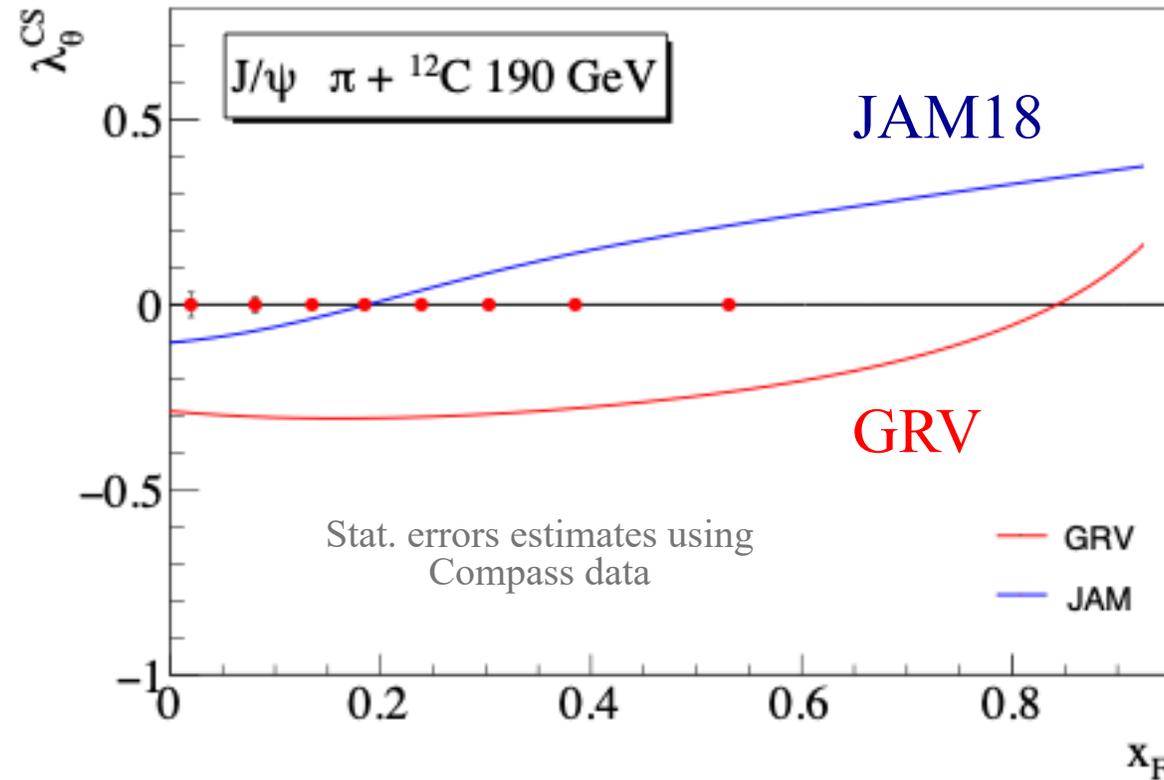
- $\alpha = +1$  : 100% transverse polarization ( $J_z = \pm 1$ )
- $\alpha = 0$  : unpolarized
- $\alpha = -1$  : 100% longitudinal polarization ( $J_z = 0$ )


$$\frac{d\sigma}{d(\cos\theta)} \propto 1 + \alpha \cos^2\theta,$$

◆ Polarization observable

- angular momentum, chirality, parity conservations preserve the properties of the  $J/\psi$ : from production to the  $2\mu$  decay
- Nature wants to help us, for  $q\bar{q}$ :  $\alpha \simeq +1$ , but for  $gg$ :  $\alpha \simeq -1$
- Key variable for understanding the bound state formation

# Polarization: expected results (Cheung and Vogt, priv. comm)



Formulas provided  
by Faccioli

The polarization value as a function of  $x_F$  is sensitive to the shape differences between  $gg$  and  $q\bar{q}$  contributions to the cross section

# Data used

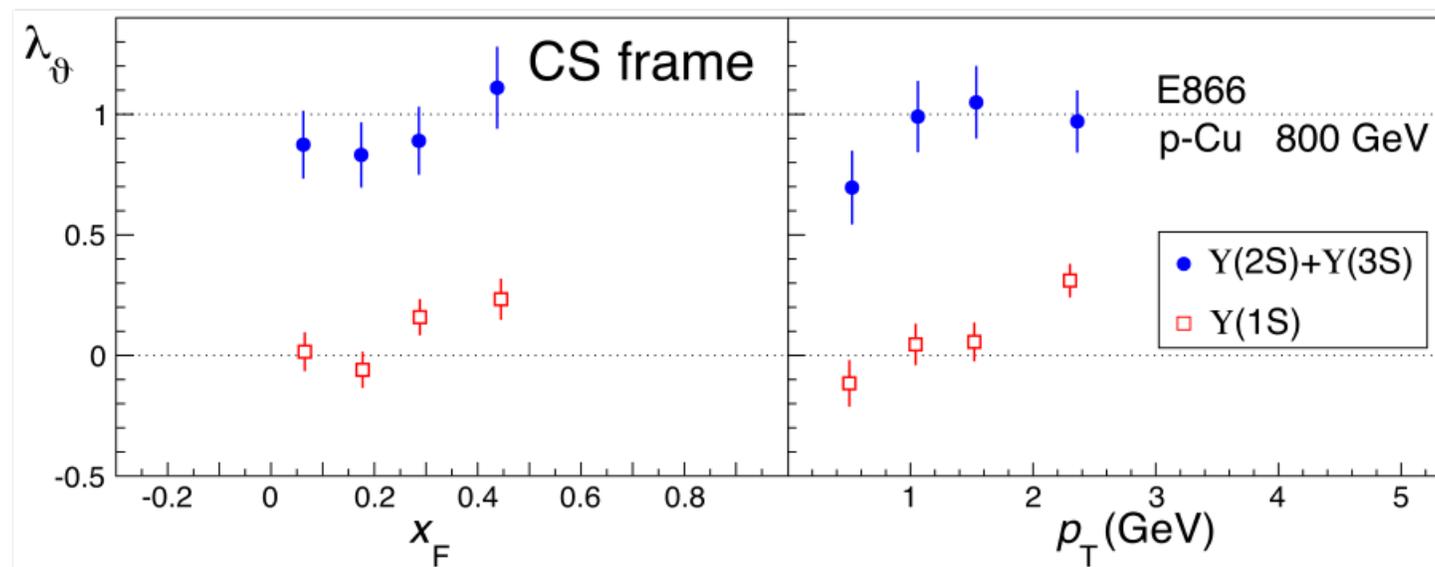
**Table 1**

$J/\psi$  and  $\Upsilon$  polarization measurements in fixed target experiments, characterized by several beam energies ( $E_{\text{lab}}$ ) and angular coverages, denoted using  $x_F$ , centre-of-mass rapidity ( $y_{\text{cms}}$ ) or fractional momentum of the beam partons ( $x_1$ ).

Exp. [Ref.]	Beam	Target	$E_{\text{lab}}$ (GeV)	$\sqrt{s}$ (GeV)	$\Delta x_F$	$\Delta p_T$ (GeV)	$\langle p_T \rangle, \langle p_T^2 \rangle$ (GeV), (GeV <sup>2</sup> )
$J/\psi$							
E537 [31]	$\pi^-, \bar{p}$	W	125	15.3	0.0–0.7	0–2.5	$\langle p_T \rangle = 1.04$
WA11 [32]	$\pi^-$	Be	146	16.6	0.0–0.4	0–2.4	$\langle p_T \rangle = 1.0$
NA60 [33]	In	In	158	17.2	$y_{\text{cms}}: 0-1$	$\approx 0-4$	
E444 [34]	$\pi^\pm$	C, Cu, W	225	20.6	$x_1: 0.2-1.0$	0–2.5	$\langle p_T \rangle = 1.2$
E615 [35]	$\pi^\pm$	W	252	21.8	0.25–1.0	0–5	
NA3 [36]	$\pi^-$	H, Pt	280	22.9	0.0–1.0		$\langle p_T^2 \rangle = 1.52, 1.85$
WA92 [37]	$\pi^-$	Si, Cu, W	350	25.6	$\approx 0.0-0.8$	0–4	
E672/706 [38]	$\pi^-$	Be	515	31.1	0.1–0.8	0–3.5	$\langle p_T \rangle = 1.17$
E672/706 [39]	p	Be	530, 800	31.5, 38.8	0.0–0.6		$\langle p_T \rangle = 1.15, 1.22$
E771 [40]	p	Si	800	38.8	–0.05–0.25	0–3.5	$\langle p_T^2 \rangle = 1.96$
E866 [41]	p	Cu	800	38.8	$\approx 0.0-0.5$	$\approx 0-4$	
HERA-B [42]	p	C, Ti, W	920	41.6	–0.34–0.14	0–5.4	$\langle p_T^2 \rangle = 2.2$
$\Upsilon(1S)$ and $\Upsilon(2S)+\Upsilon(3S)$							
E866 [43]	p	Cu	800	38.8	0.0–0.6	0–4	$\langle p_T \rangle = 1.3$

# Measurements shown: Upsilon

- ◆ Difference between  $Y(1S)$  and  $Y(2S)+Y(3S)$ 
  - "astounding difference"

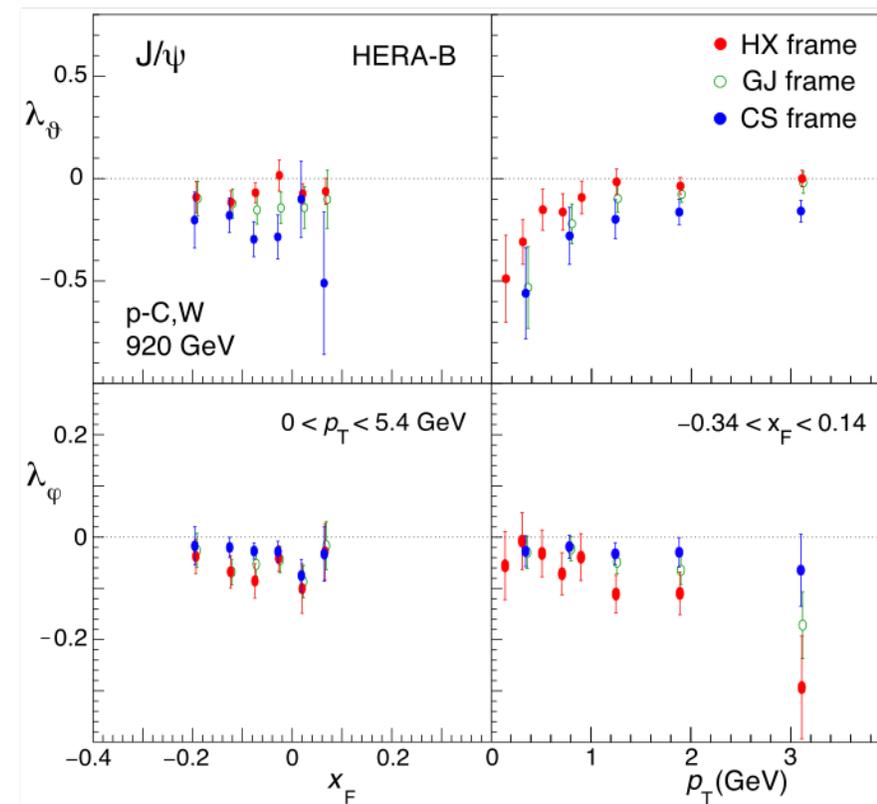


**Fig. 2.** The  $\Upsilon(1S)$  and  $\Upsilon(2S+3S)$  polar anisotropy parameter  $\lambda_\theta$  measured by E866 in the CS frame, vs.  $x_F$  and  $p_T$ .

# HX, GJ, CS frame analysis of HERA-B data

## ◆ Observations

- Inverse hierarchy for Theta and Phi results
- Reflects the difference between the frame definition
- A trend towards longitudinal J/psi polarization at small  $x_F$ .
- Interpretation: gg process is dominant



**Fig. 3.** The  $J/\psi$   $\lambda_\theta$  and  $\lambda_\phi$  parameters measured by HERA-B in the CS, GJ and HX frames, vs.  $x_F$  and  $p_T$ .

# Model used

---

## ◆ Assumptions

- QQ production is dominated by 2-to-1 topologies, so that contributions producing at least one additional object besides the quarkonium, are considered negligible.
- The  $gg \rightarrow QQ$  and  $qq \rightarrow QQ$  processes lead, respectively, to fully longitudinal and fully transverse polarizations of the directly produced  $J/\psi$ ,  $\psi(2S)$ , and  $Y$  mesons.

# Model used

---

- Relative proportion of qqbar and gg:

$$R = \frac{\sum_q [F_1^q(x_1, \hat{s}) F_2^{\bar{q}}(x_2, \hat{s}) + F_1^{\bar{q}}(x_1, \hat{s}) F_2^q(x_2, \hat{s})]}{F_1^g(x_1, \hat{s}) F_2^g(x_2, \hat{s})}, \quad \text{Use the PDFs to calculate it}$$

- Ratio of qqbar and gg cross sections:

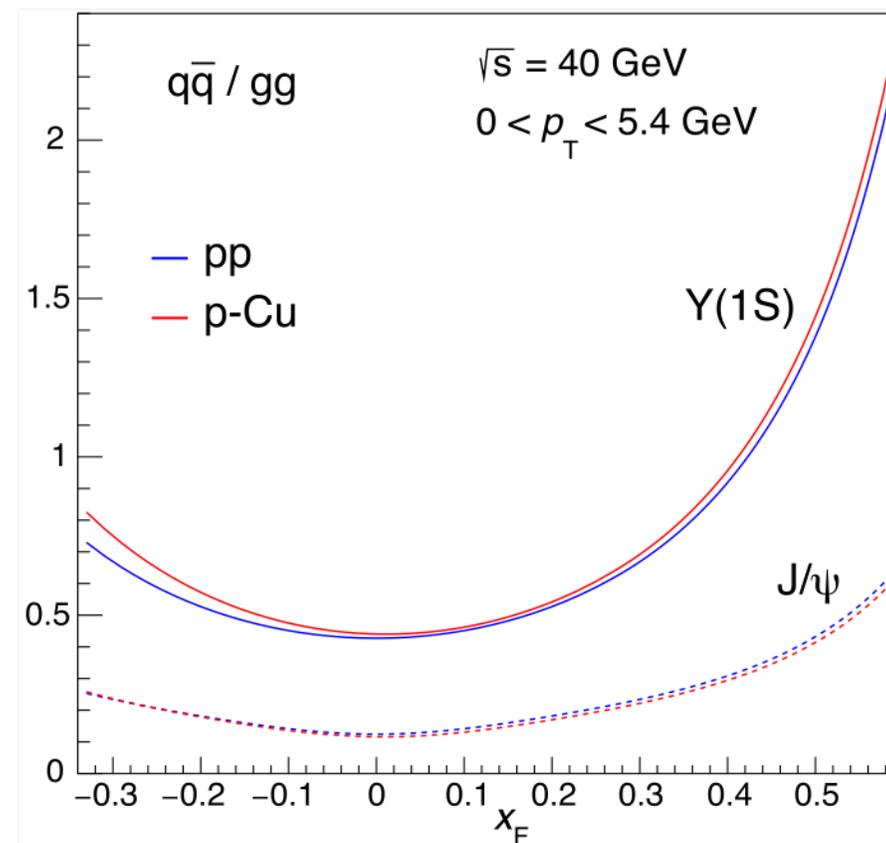
$$r = \frac{\hat{\sigma}(q\bar{q} \rightarrow Q)}{\hat{\sigma}(gg \rightarrow Q)}, \quad \text{Fit } r \text{ to the data: (only parameter)}$$

- Compute the polarization using:  $f_{q\bar{q}} = R \times r / (1 + R \times r)$  and  $f_{gg} = 1 / (1 + R \times r)$ ,

$$\lambda = \frac{f_{q\bar{q}} \lambda_{\vartheta}^{q\bar{q}} / (3 + \lambda_{\vartheta}^{q\bar{q}}) + f_{gg} \lambda_{\vartheta}^{gg} / (3 + \lambda_{\vartheta}^{gg})}{f_{q\bar{q}} / (3 + \lambda_{\vartheta}^{q\bar{q}}) + f_{gg} / (3 + \lambda_{\vartheta}^{gg})}. \quad \text{Assumed polarizations } \lambda_{gg} \text{ and } \lambda_{qq} \text{ (from -1 and +1) to values corrected for feed-down (upp, low, central)}$$

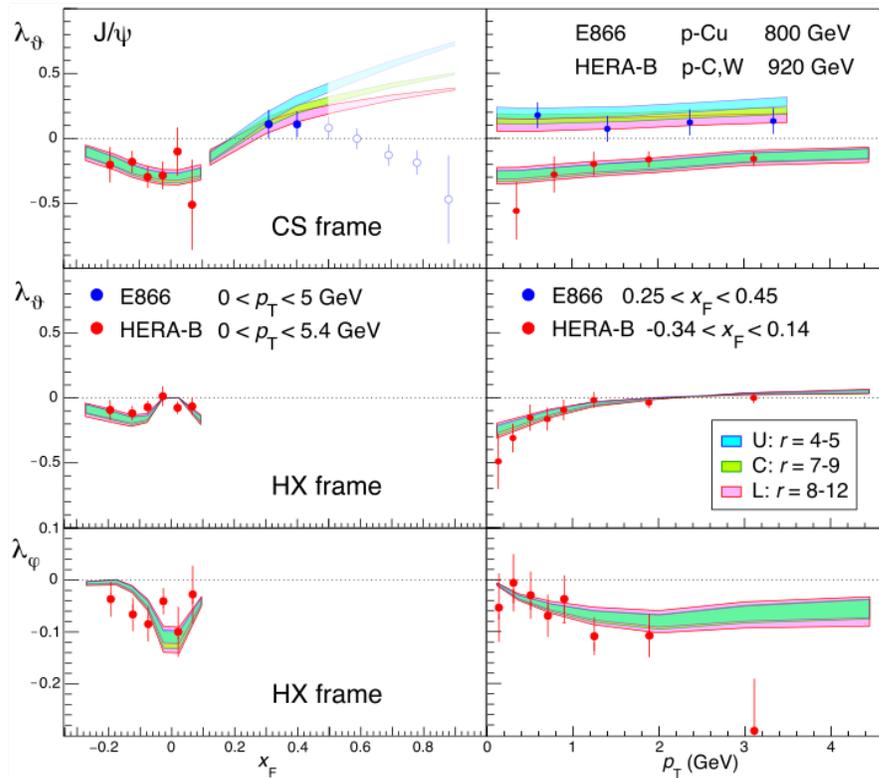
# Ratio of $q\bar{q}$ to $gg$ “luminosities” for a proton beam

- ◆ Luminosity = product of PDFs
- ◆ Observations
  - Dominance of  $gg$  near  $x_F = 0$
  - Large difference  $J/\psi$  vs  $Y$
- ◆ General
  - Low  $p_T$  data: 2 ---> 1 process
  - $qq$  = transverse pol.;  $gg$  = longitudinal pol.

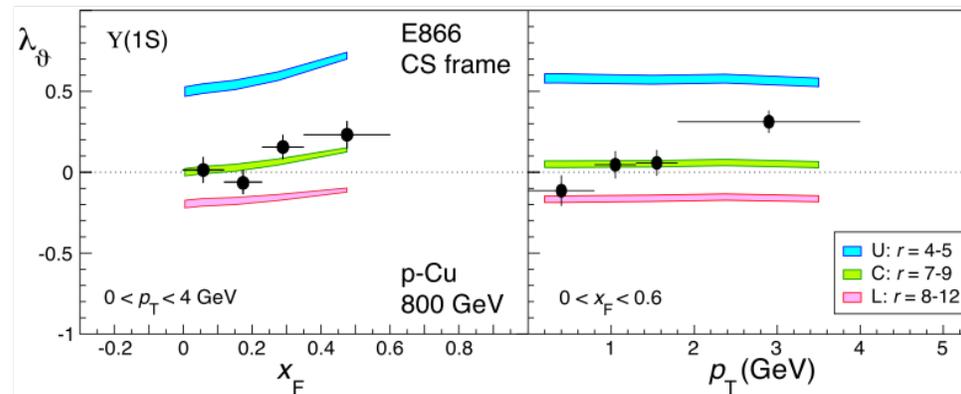


**Fig. 4.** The  $q\bar{q}$  to  $gg$  parton luminosity ratios for  $J/\psi$  and  $Y(1S)$  production, vs.  $x_F$ , illustrated for conditions similar to those of the E866 and HERA-B experiments.

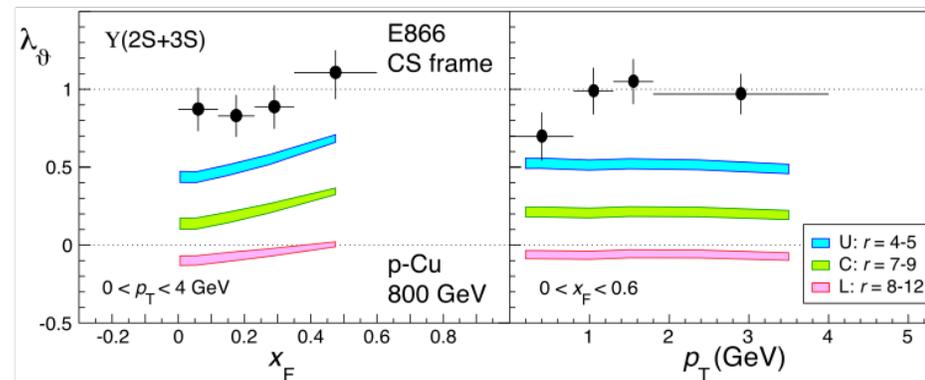
# Model vs Data for proton-nucleus collisions



**Fig. 6.** The  $x_F$  (left) and  $p_T$  (right) dependences of the  $J/\psi$  polarization parameters  $\lambda_\theta$  in the CS (top) and HX (middle) frames, and  $\lambda_\phi$  in the HX frame (bottom), as measured by HERA-B (red points) and E866 (blue points). The cyan, green, and magenta bands represent, respectively, the upper (U), central (C), and lower (L) scenarios described in the text; they are independently computed for the HERA-B and E866 conditions. The departure of the bands from the E866 measurements for  $x_F > 0.45$  (open circles) justifies the conjecture that our model is not valid to describe high- $x_F$  quarkonium production.



**Fig. 7.** Same as Fig. 6, for the  $\Upsilon(1S)$   $\lambda_\theta$  parameter measured by E866 in the CS frame.



**Fig. 8.** Same as Fig. 7, for the  $\Upsilon(2S+3S)$ .

---

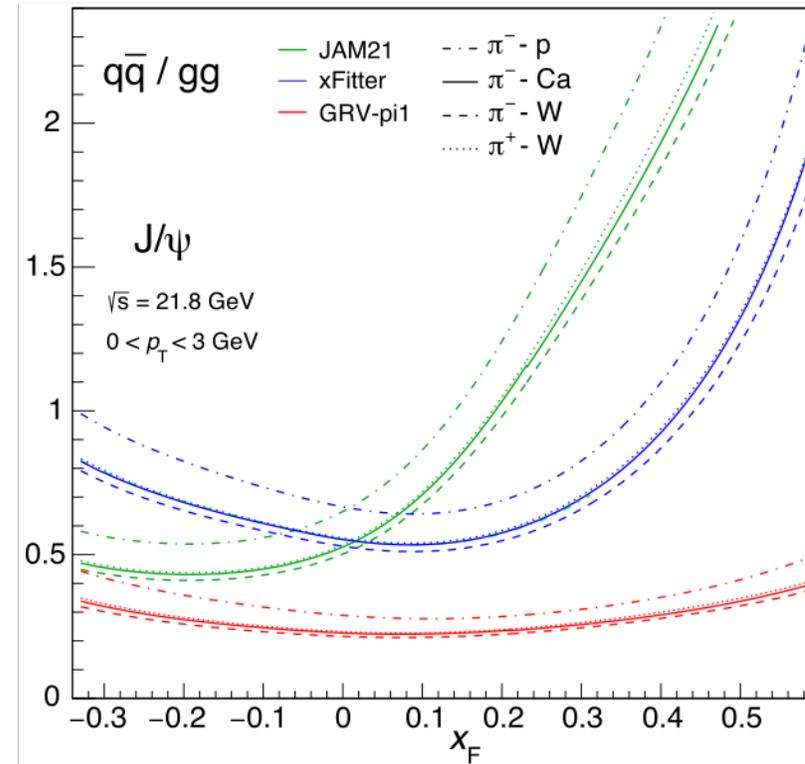
*“As mentioned before, these  $Y(2S+3S)$  measurements are clearly a notable exception in the global panorama of the existing data. Faced with this large discrepancy, we must wonder if there could be some experimental factor causing a difference between the  $Y(2S+3S)$  measurement and the  $J/\psi$  or  $Y(1S)$  measurements.”*

# Pion-nucleus collisions

## ◆ Observations

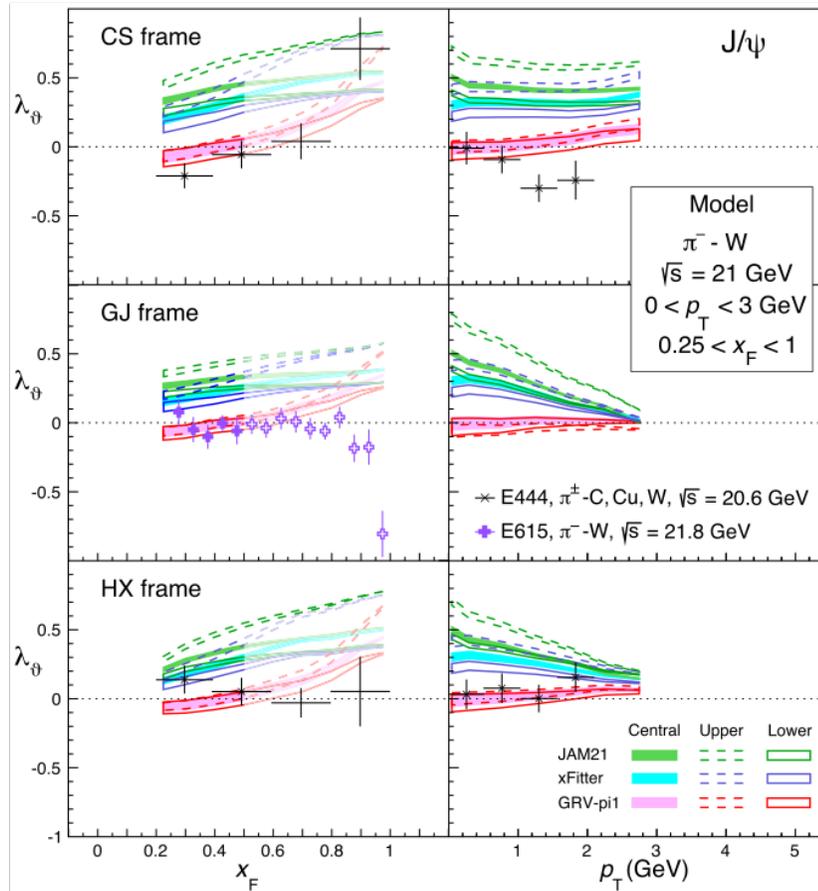
- Very large effect, as expected.

*“The  $x_F$  dependence of this ratio, as well as its average value and the covered  $x_F$  range, depend quite significantly on the chosen PDF set, probably because of the poorly-known gluon density in the pion”*

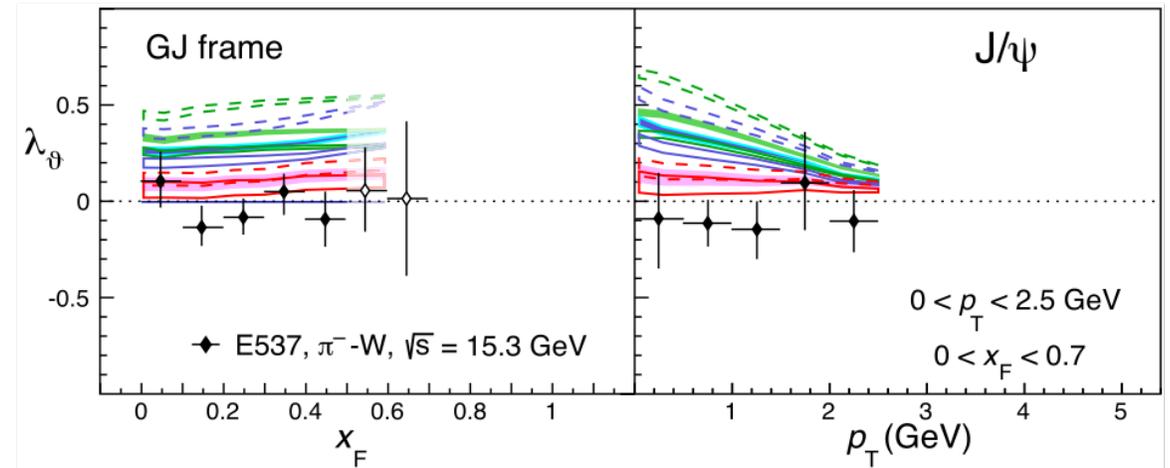


**Fig. 9.** The  $q\bar{q}$  over  $gg$  parton luminosity ratios, vs.  $x_F$ , for  $J/\psi$  production at the collision energy of E615 [35], for the JAM21, xFitter, and GRV-pi1 pion PDF sets, and for the  $\pi^-p$ ,  $\pi^-Ca$ ,  $\pi^-W$ , and  $\pi^+W$  collision systems.

# Pion-nucleus collisions



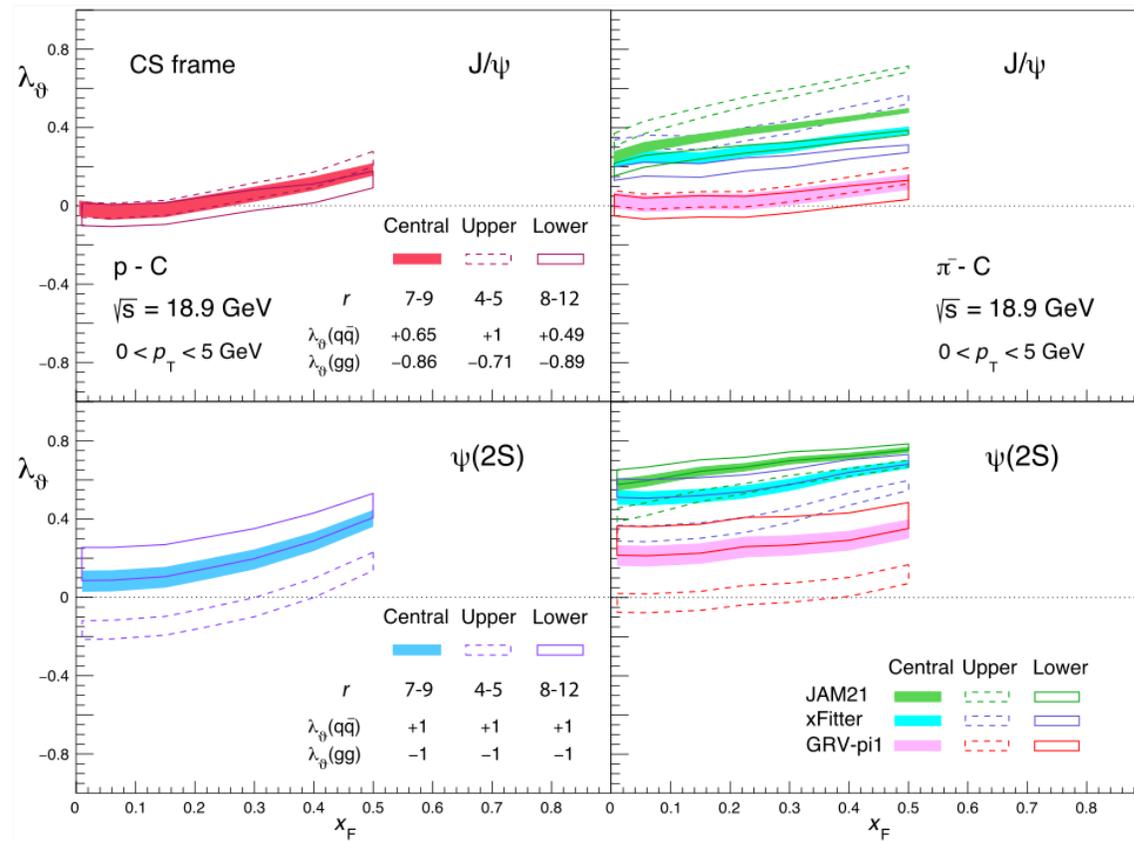
**Fig. 10.** The  $x_F$  and  $p_T$  dependences of the  $J/\psi$   $\lambda_\theta$  parameter, in the CS, GJ, and HX frames, as measured by E444 and E615 in  $\pi^- - W$  collisions. The bands are computed using the JAM21, xFitter, and GRV-pi1 pion PDF sets, for the three feed-down scenarios. As in Fig. 6, the data points and bands are displayed less prominently in the  $x_F > 0.5$  region.



**Fig. 11.** Same as Fig. 10, for the E537 conditions.

Confirmation: GRV produces the best agreement

# Predictions for AMBER



**Fig. 12.** The  $x_F$  dependence of the  $\lambda_\theta$  parameter, in the CS frame, as predicted for  $J/\psi$  (top) and  $\psi(2S)$  (bottom) production in  $p$ -C (left) and  $\pi^-$ -C (right) collisions at  $\sqrt{s} = 18.9$  GeV (corresponding to the conditions of the AMBER experiment), for the three considered  $J/\psi$  feed-down scenarios. The bands on the right panels correspond to the three pion PDF sets.