



Charmonium production: a tool for accessing the gluon distribution in the pion

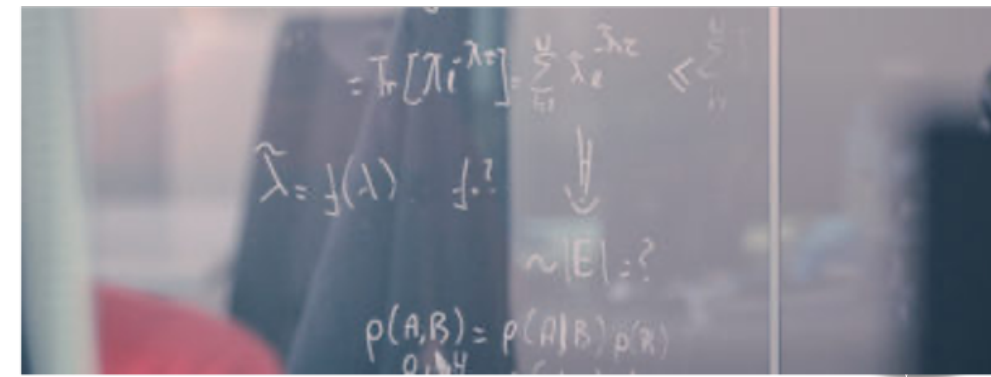
Stephane Platchkov

Paris-Saclay University, CEA/IRFU, France

(collaboration with W.-C. Chang, C.-Y. Hsieh, Y.-S. Lian, J.-C. Peng, and T. Sawada)

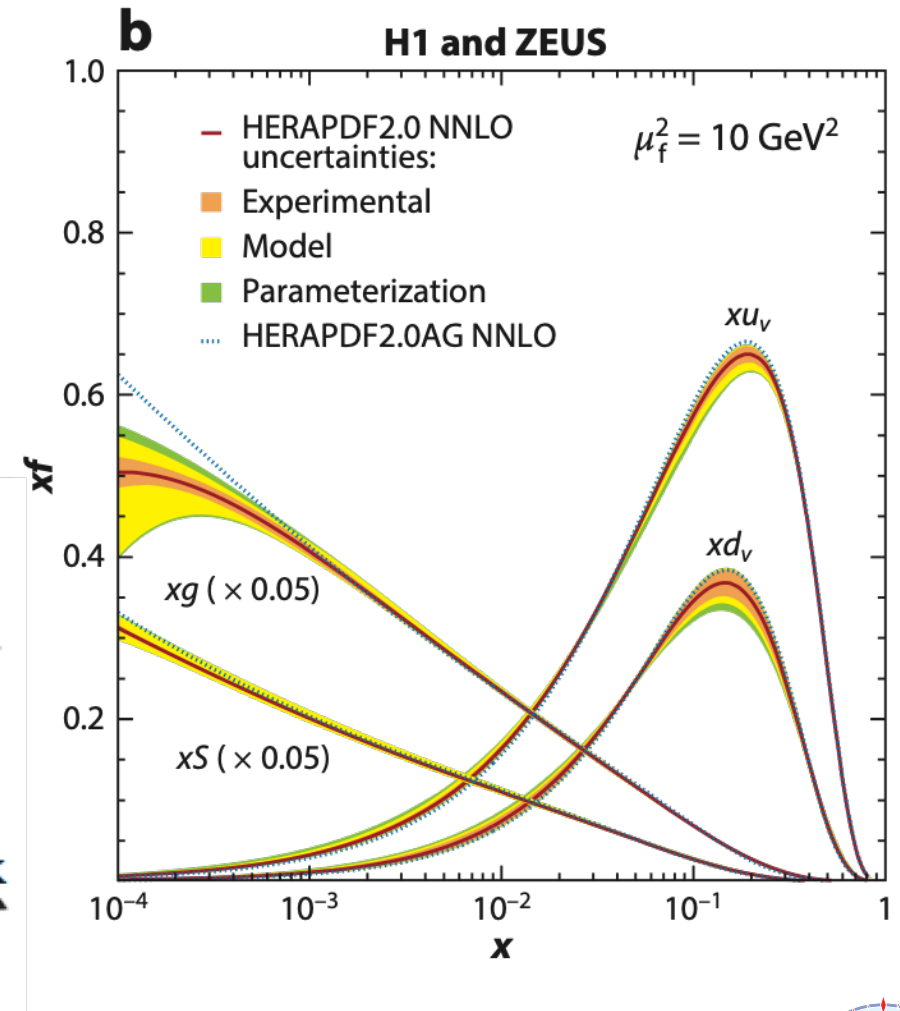
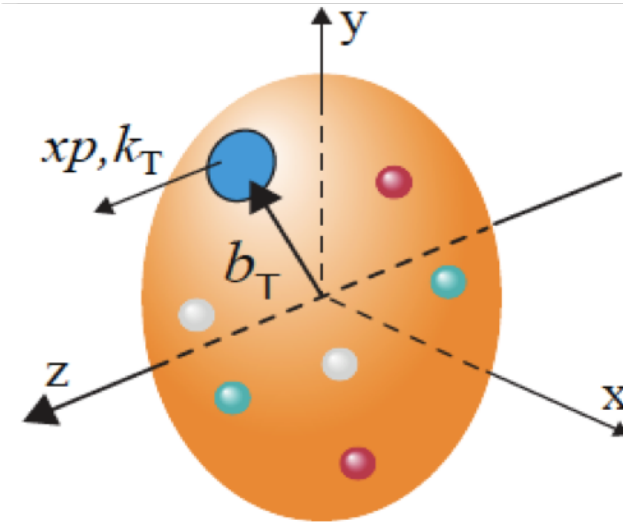
Parton distribution functions at a crossroad

ECT* Trento, 18 – 22 September 2023



Hadron structure: the nucleon

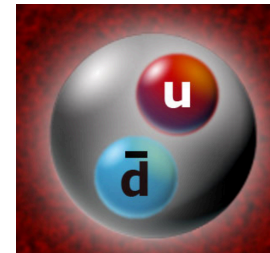
- ◆ Main laboratory for QCD studies
 - More than 4 decades of extensive investigations
 - Hundreds of experiments
 - Parton distributions are well known
 - Perturbative QCD works really well
 - Aim at a full multidimensional picture : GPDs, TMDs:



The nucleon structure is (almost) perfectly known –over few decades in x

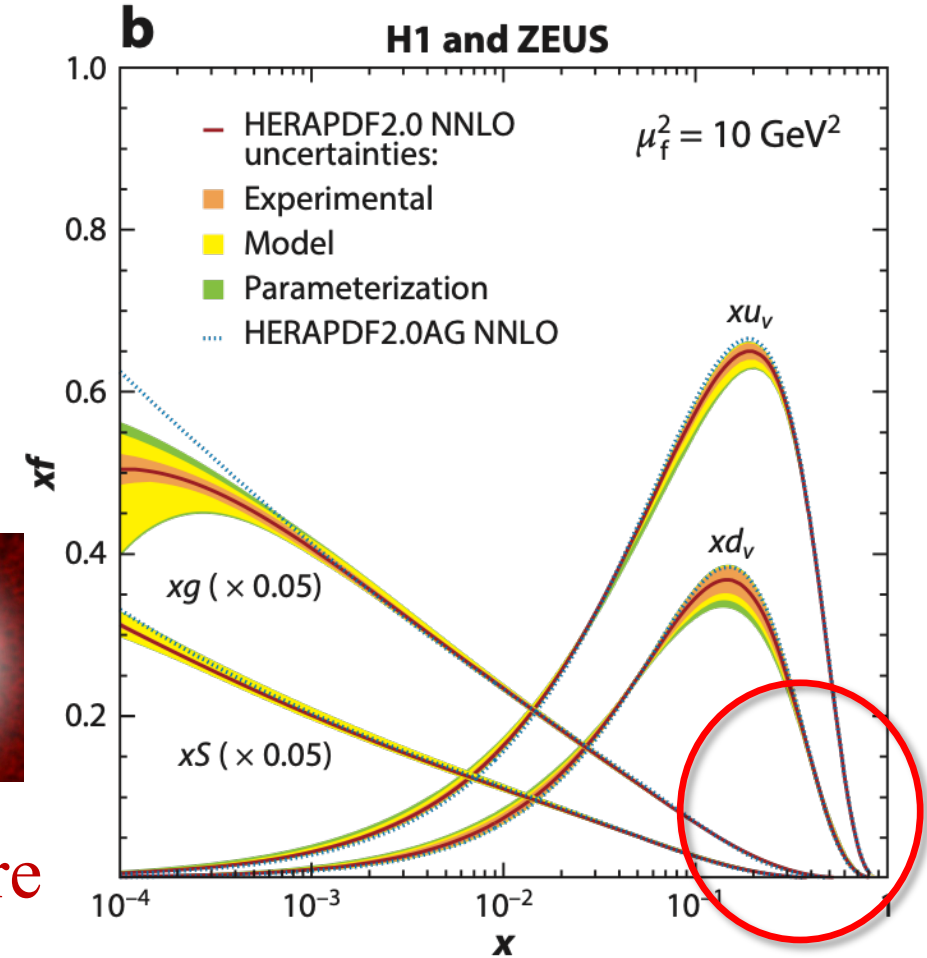
Hadron structure: the pion and the kaon

- ◆ Laboratories for QCD studies
 - Absence of meson targets
 - Few experiments, few decades old
 - Pion parton distributions are quite uncertain
 - Kaon parton distribution are essentially unknown
 - Good news: new data from Compass + Amber, Jlab, EIC



(👉 V. Andrieux, 👉 O. Denisov)

Pion structure



Sharp contrast with the present knowledge on the pion. And on the kaon

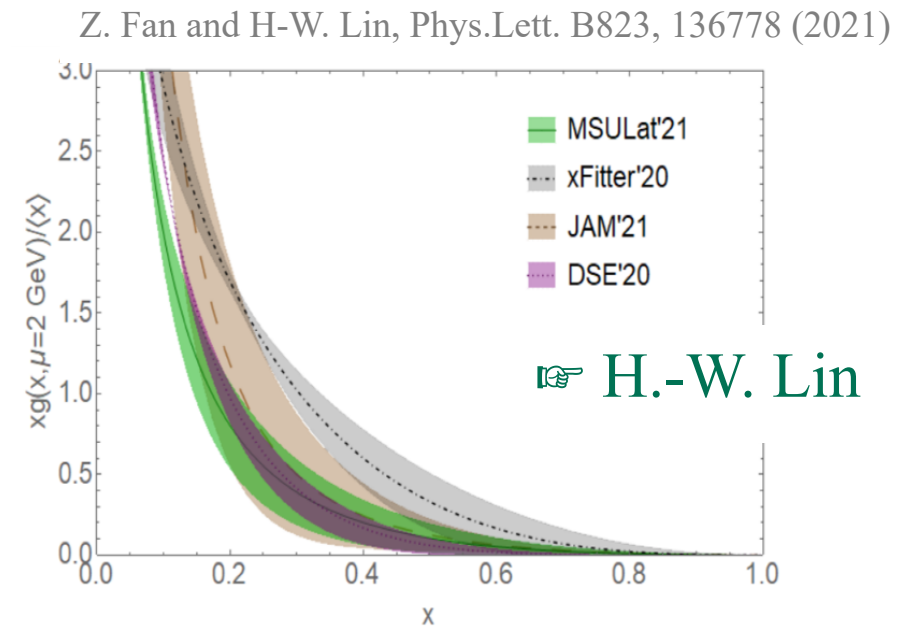
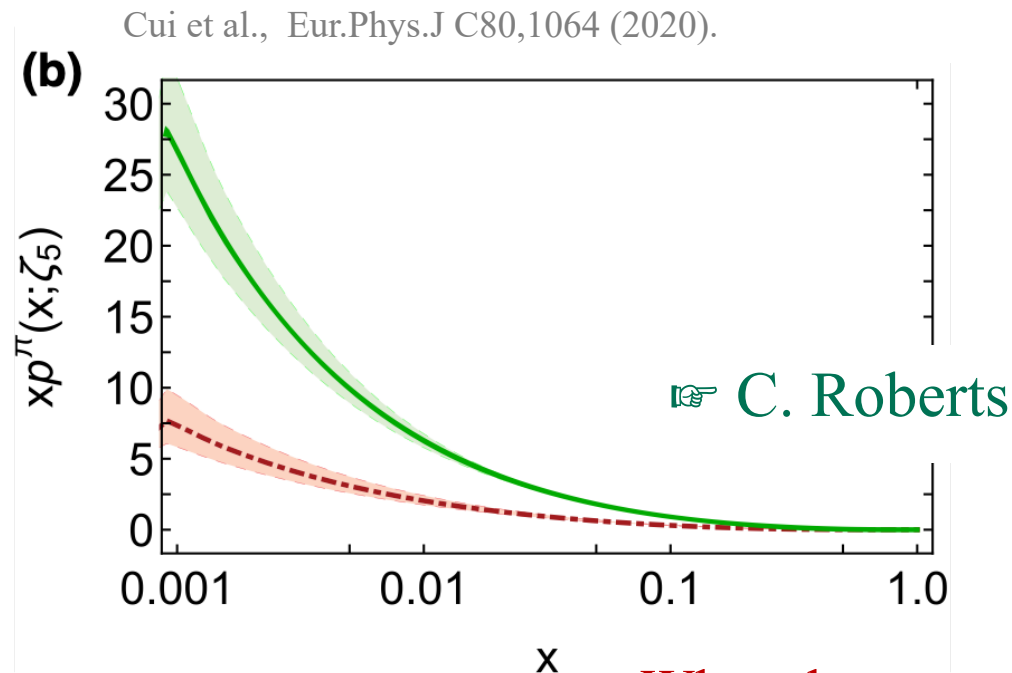
Meson structure in the last few years - theory

- ◆ Remarkable progress in theory

 - Continuum Schwinger method (CSM)

 - Lattice QCD

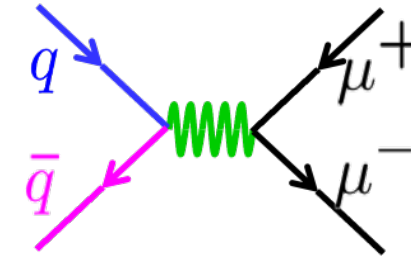
 - ▶ Aim at describing the properties of the two simplest hadrons (e.g. pion gluon PDF):



What about experimental info ?

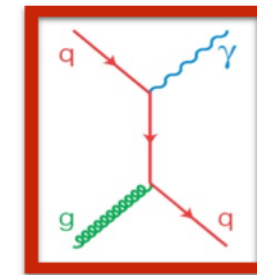
◆ Drell-Yan process

- Pros: well-known and clean process
- Cons: low cross sections (em process)
- Data available: NA3, NA10, E615...

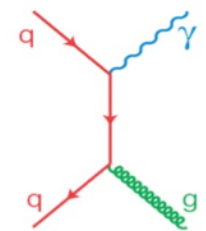


◆ Prompt-photon π -N production

- Pros: sensitive to valence and gluon PDFs
- Cons: high p_T , large background
- Data available: CERN (WA70, NA24)



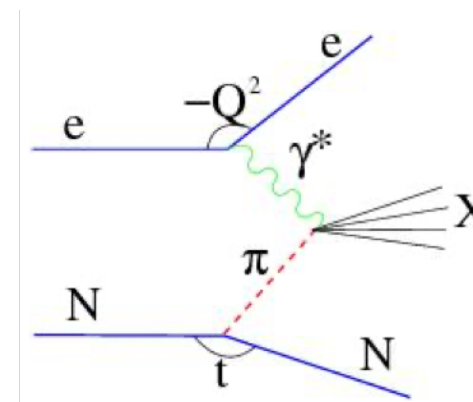
$qg \rightarrow q\gamma$



$q\bar{q} \rightarrow g\gamma$

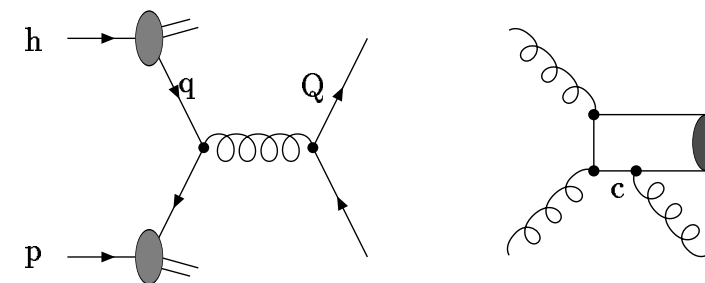
◆ Sullivan (Leading Neutron) process

- Pros: gives access to lower x values of the PDFs (if high energy)
- Cons: theoretical uncertainties
- Data available: HERA (Zeus and H1) + JLab (to come)



◆ Charmonium production

- Pros: sensitive to the gluon PDF, large cross sections
- Cons: production mechanism
- Data available: CERN: NA3, WA39, WA11
FNAL: E537, E672, E705



$q\bar{q}$

gg

Four known methods of inferring the pion PDFs

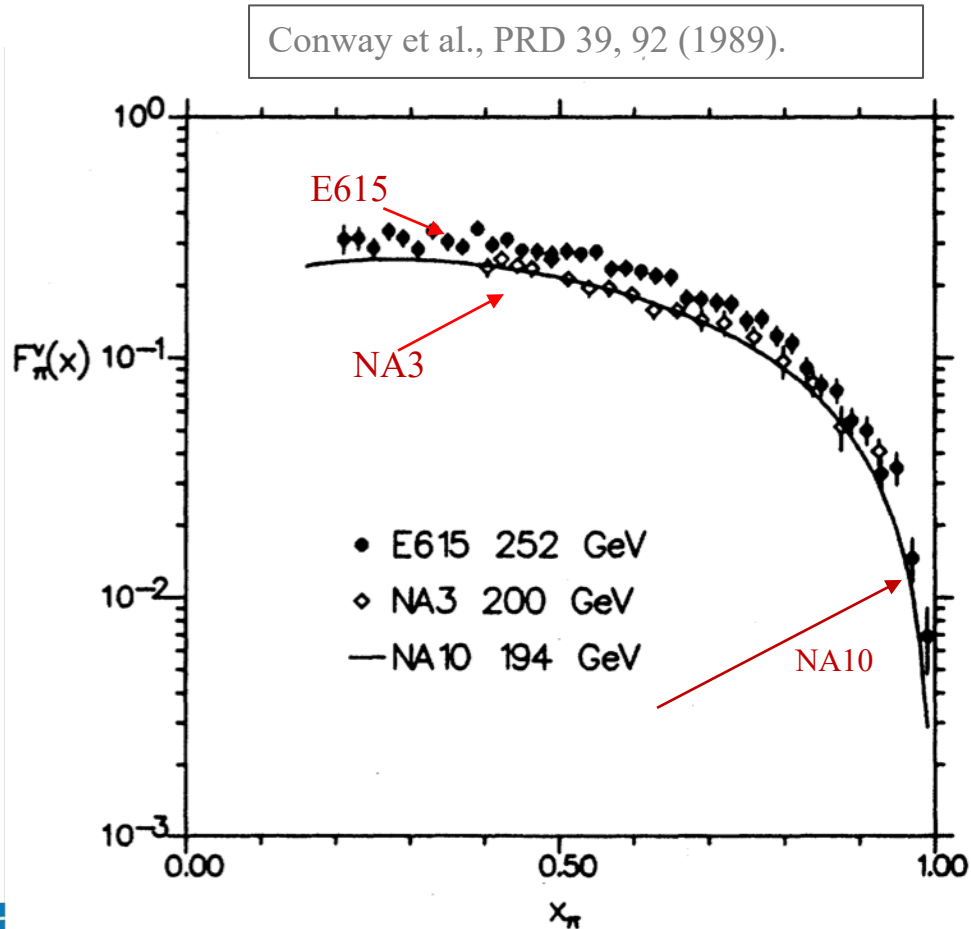
Pion structure – global fits

- ◆ Previous (3 decades old) global fits (+ a couple of others...)
 - SMRS Sutton, Martin, Roberts and Stirling (1992)
 - DY + Direct-photon production
 - GRV(S) Glück, Reya and Vogt (1992), Glück, Reya and Shienbein (1999)
 - Direct-photon production + DY

- ◆ Recent global fits
 - JAM Barry, Sato, Melnitchouk and Ji (2018, 2021)
 - DY + Sullivan process (+NLL corrections in 2021)
 - xFitter Novikov et al., (2020)
 - DY + Direct-photon production

Uncertainties in the present DY data (CERN vs FNAL)

■ Differences



■ Global fits normalizations

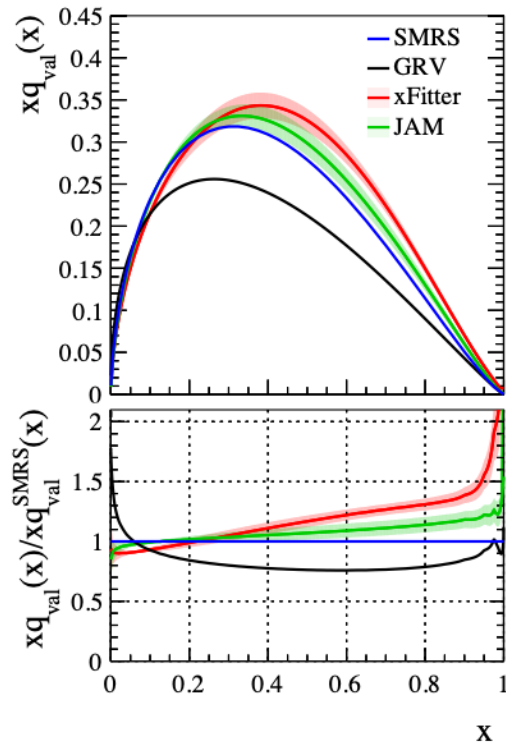
Exp / Global fit	xFitter	JAM	xFitter/JAM
E615	1.160	0.985	1.18
NA10-194 GeV	0.997	0.816	1.22
NA10-286 GeV	0.927	0.758	1.22
WA70 (prompt- γ)	0.737	-	
H1 LN	-	1.170	
Zeus LN	-	0.964	

Global fits – pion PDFs comparison

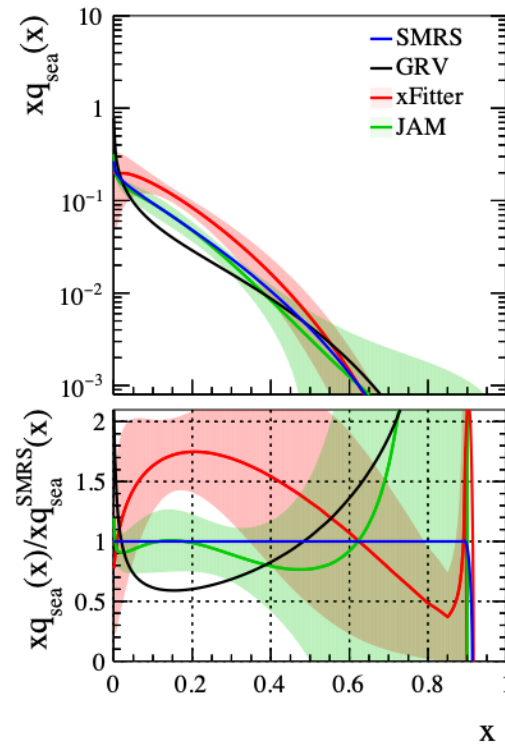
Fixed-target charmonium production and pion parton distributions

Wen-Chen Chang, Jen-Chieh Peng, Stephane Platchkov, and Takahiro Sawada
Phys. Rev. D **107**, 056008 – Published 7 March 2023

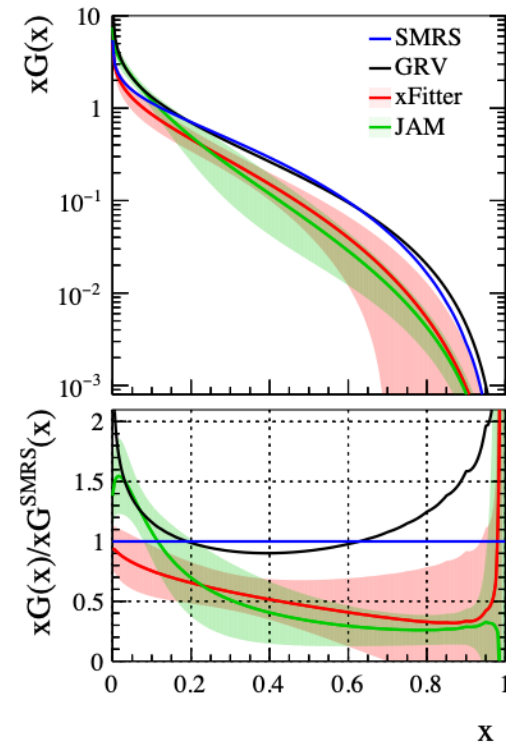
Valence



Sea



Gluons



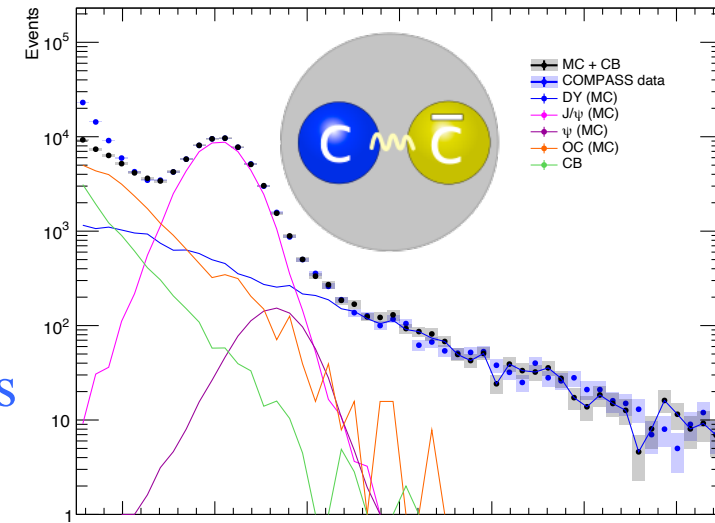
Charmonium production

◆ Several advantages

- Sensitive to valence and glue
- Large cross sections, 30 – 50 times more than Drell-Yan
- Fixed-target energies: dominated by $2 \rightarrow 1$ process
- Large number of π -induced data (from 80s to 00s) on many targets

◆ Present descriptions for charmonium production

- Color Evaporation Model
 - weight of each contribution (qqbar or GG) depends solely on the parton PDFs
 - Only one adjustable parameter
- Non-Relativistic QCD (NRQCD)
 - effective field theory, based on factorization
 - separates pQCD (short distance processes) and npQCD (long-distance dynamics)



First step

- ◆ Compare the “Global Fits” results with the data, using **CEM NLO**.
 - Integrated cross sections
 - x_F – dependent cross sections

Constraining gluon density of pions at large x by pion-induced J/ψ production

Wen-Chen Chang, Jen-Chieh Peng, Stephane Platchkov, and Takahiro Sawada
Phys. Rev. D **102**, 054024 – Published 24 September 2020

Experimental information used

- ◆ Data choice criteria
 - x_F distribution is available
 - Minimize nuclear effects ($A \leq 9$)
- ◆ Additional input
 - proton PDF: CT14nlo
 - nuclear PDFs: EPPS16

Data on heavier targets are also available

TABLE II. The J/ψ production datasets with π^- beam used in the analysis, listed in order of decreasing beam momentum.

Experiment	P_{beam} (GeV/c)	Target	Normalization ^a	References
FNAL E672, E706	515	Be	12.0	[68]
FNAL E705	300	Li	9.5	[69]
CERN NA3 ^b	280	p	13.0	[70]
CERN NA3 ^b	200	p	13.0	[70]
CERN WA11 ^b	190	Be	^c	[72]
CERN NA3 ^b	150	p	13.0	[70]
FNAL E537	125	Be	6.0	[73]
CERN WA39 ^b	39.5	p	15.0	[74]

^aPercentage of uncertainty in the cross section normalization.

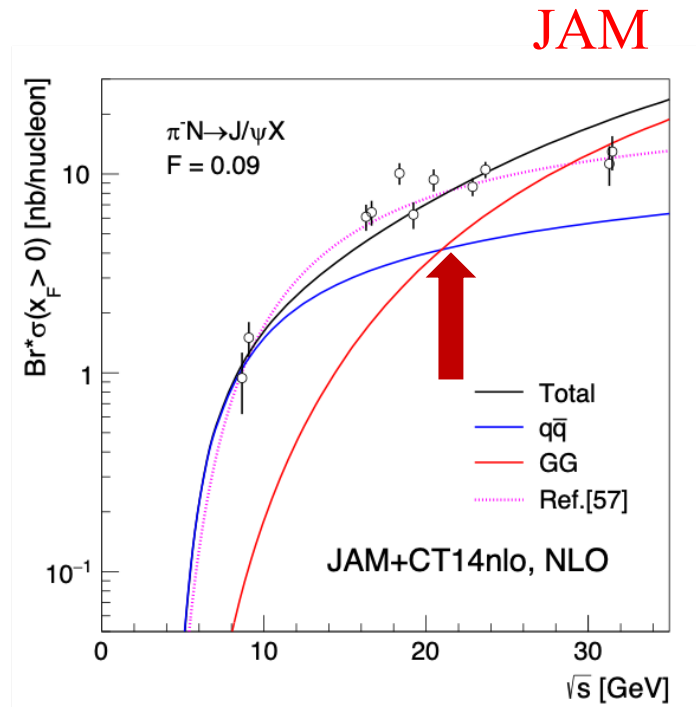
^bThe numerical information was taken from figures.

^cInformation not available.

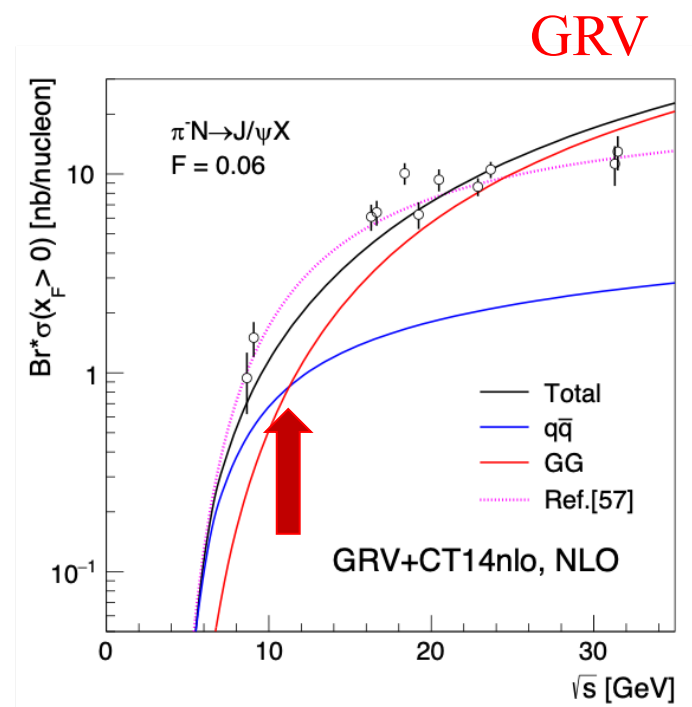
Eight data sets with π beam, published 1981 - 1996

Integrated ($x_F > 0$) J/psi cross sections vs CEM NLO calculations

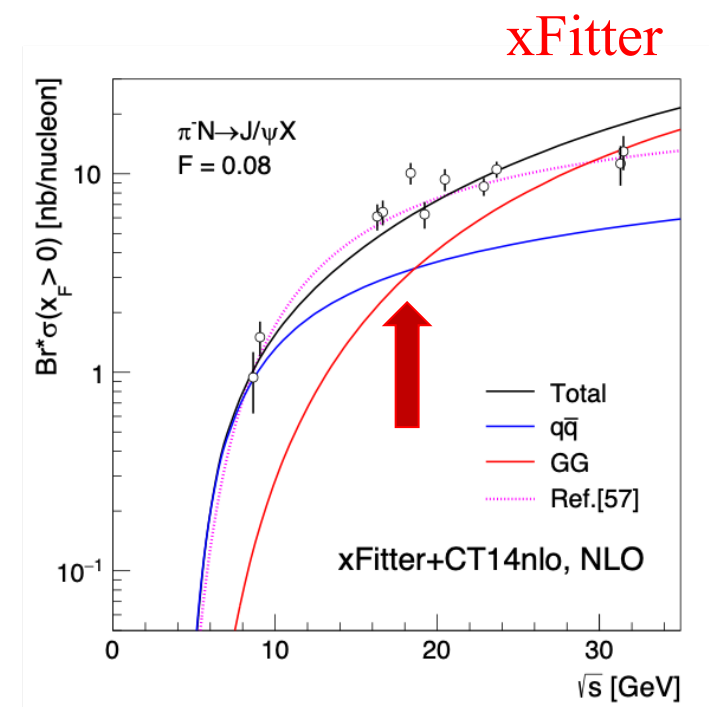
◆ Global fit dependence



GG vs $q\bar{q}$ crossing: 21 GeV



12 GeV

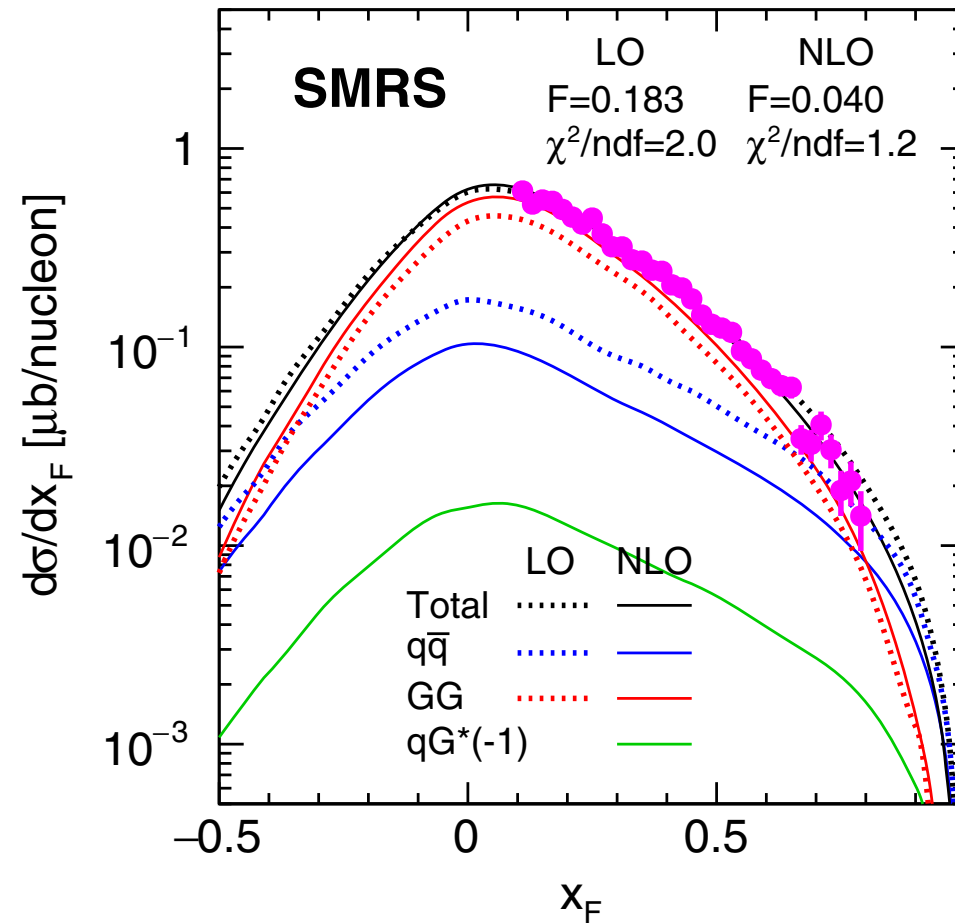


20 GeV

Overall good agreement, but large GG vs $q\bar{q}$ variations

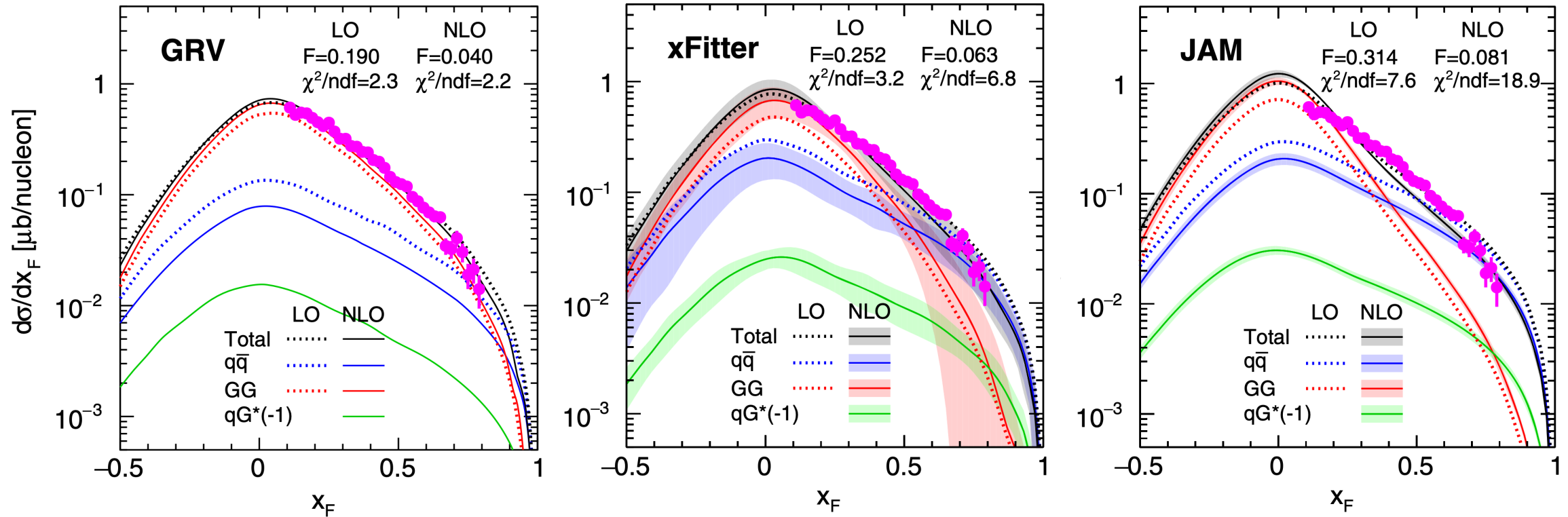
E672/E706: $\pi + \text{Be}$ for $E = 515 \text{ GeV}$

◆ CEM LO vs NLO



NLO: minor improvement in Chi2

◆ GRV vs xFitter vs JAM

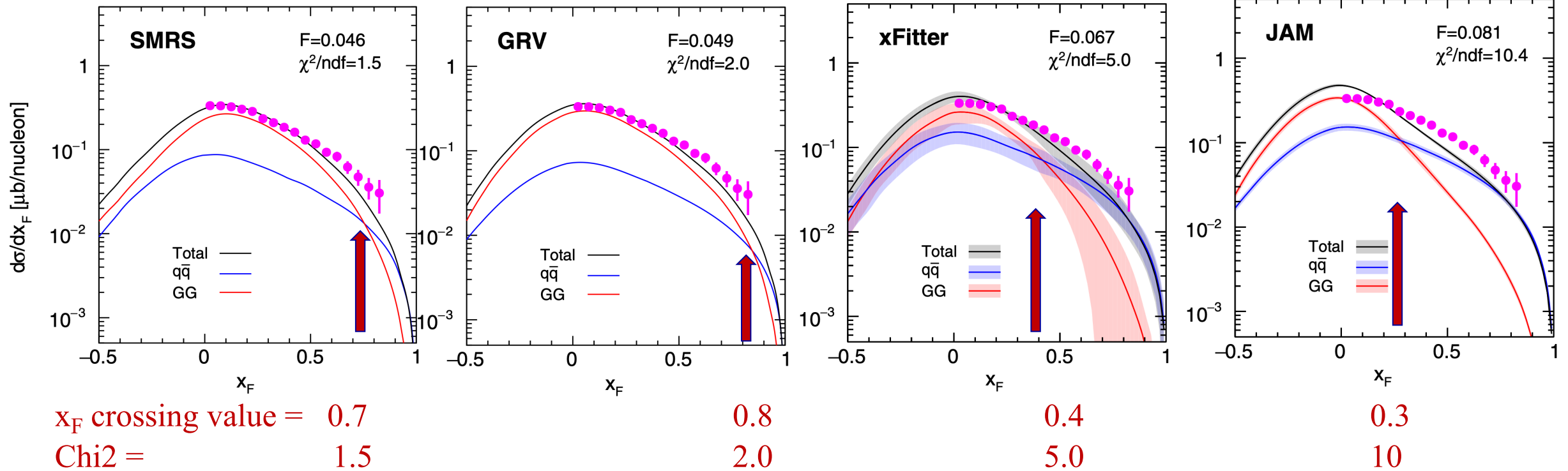


Different $q\bar{q}$ and GG contributions, and different χ^2/ndf

NA3: $\pi + p$ for $E = 280$ GeV

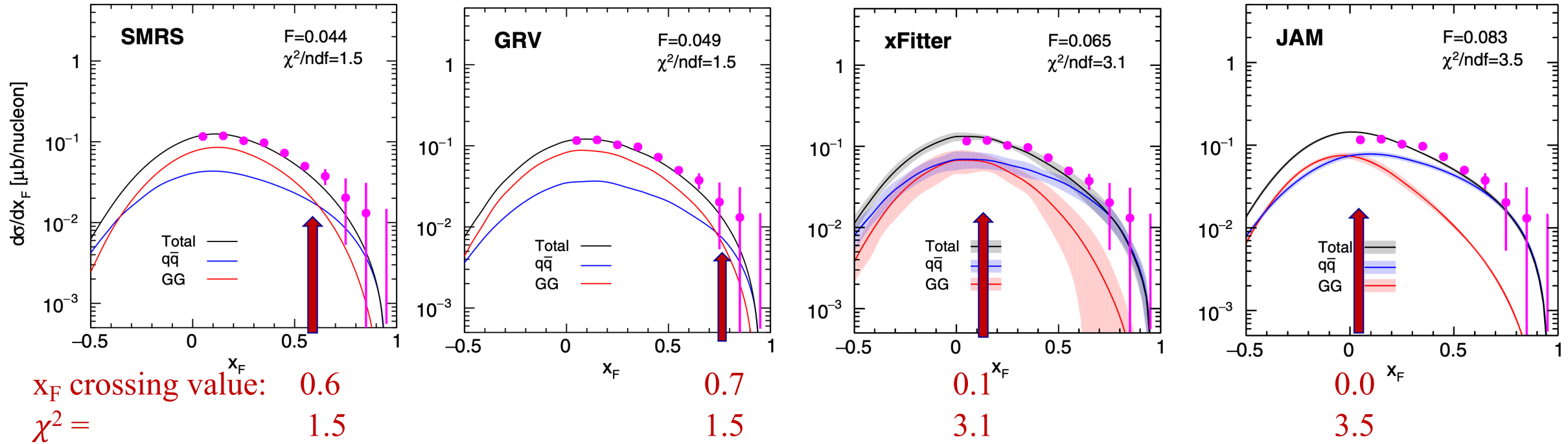
◆ SMRS vs GRV vs xFitter vs JAM

arrows = crossing points



Smaller GG contribution \implies larger χ^2

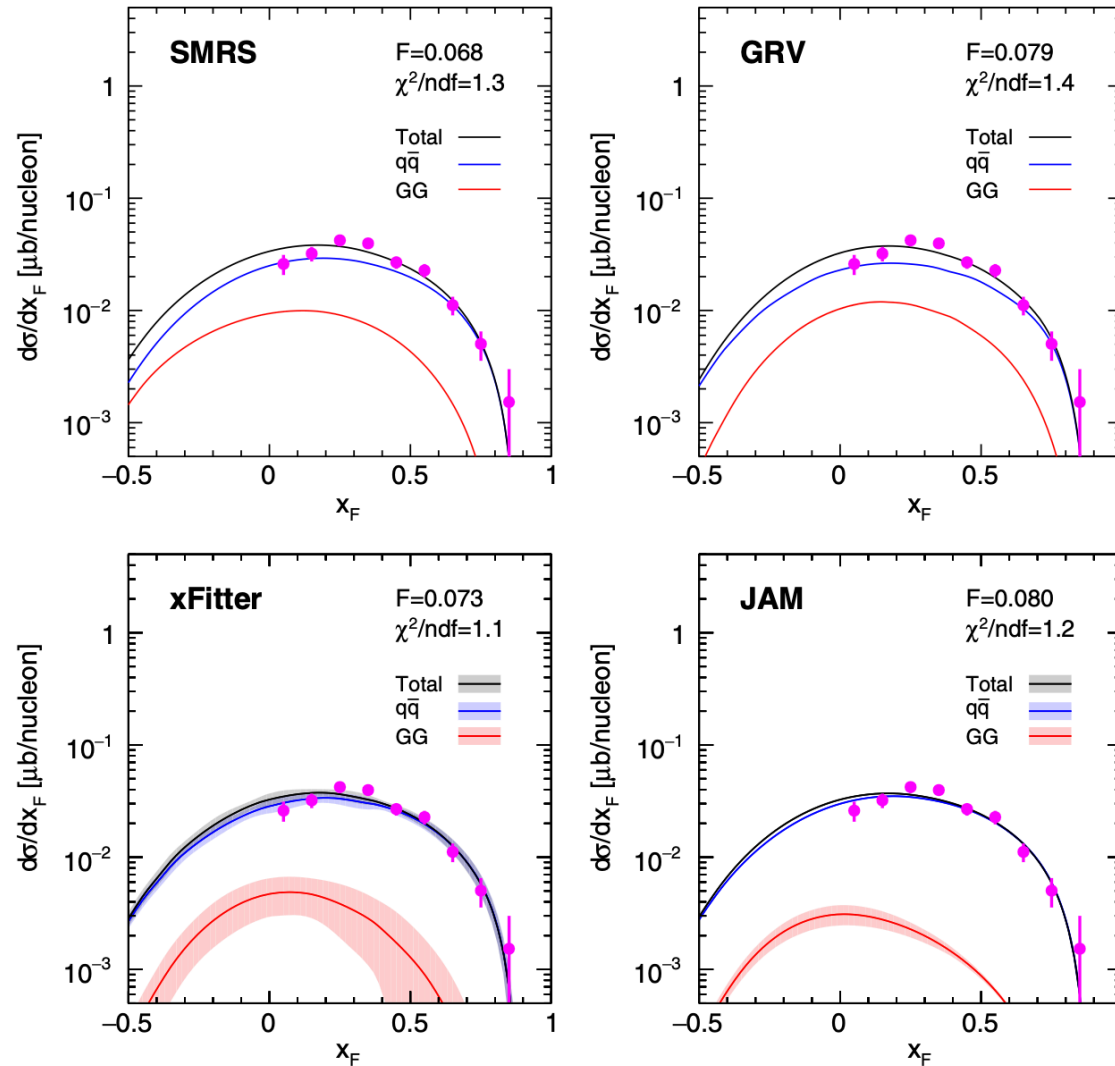
◆ SMRS vs GRV vs xFitter vs JAM



Smaller GG contribution \implies larger χ^2
 Decreasing energy = decreasing GG contribution

WA39: $\pi + p$ for $E = 39.5$ GeV

$\pi^- + p$ at 39.5 GeV/c, NLO



Are charmonium data compatible with the pion PDFs?

◆ Conclusions from the CEM NLO study

- The gg fusion process becomes increasingly important with the increase of the (FT) energies
- Data are sensitive to the amount of $g(x)$ in the pion
- Global fits with larger gluon contributions (GRV, SMRS) are favored

Would a different production model entail different conclusions?

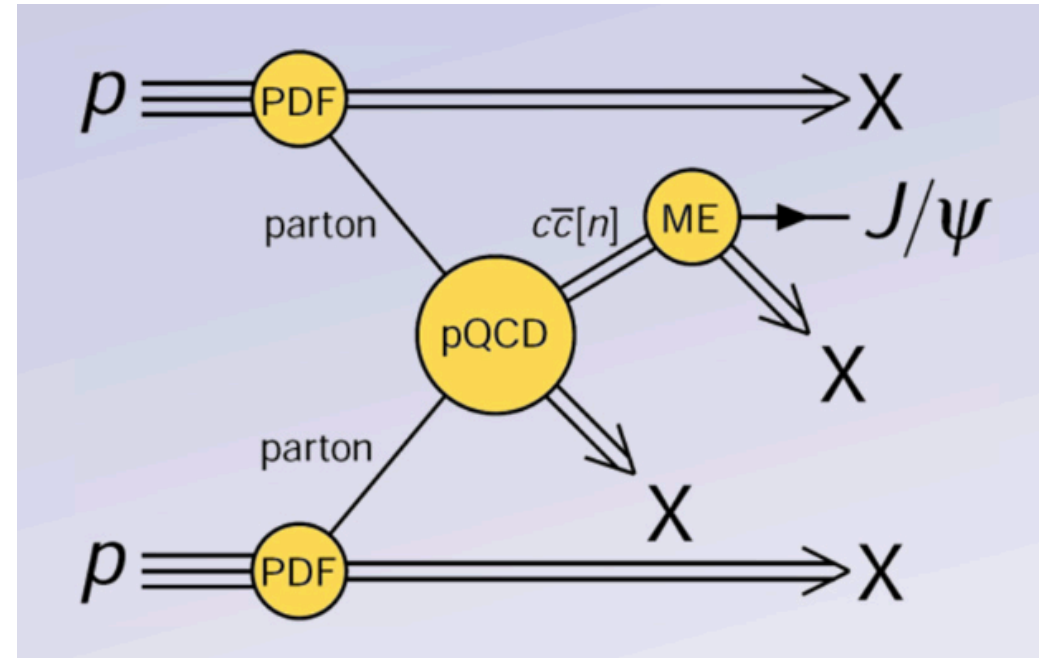


Second step:

- ◆ Use **NRQCD** instead of CEM. Needed are:
 - Beam and Target PDFs
 - Short Distance cross sections (pQCD)
 - Long-Distance Matrix Elements (phen.)
 - Factorization

- ◆ Start with integrated cross sections only

Hsieh, Lian, Chang, Peng, Platchkov and Sawada, Chin. J. Phys. 73 (2021) 13



A word on the LDMEs...

- ◆ Sensitivity to the different subprocesses

- Color Octet LDMEs (Color Singlet LDMEs are fixed to the values used in the literature)

H	$q\bar{q}$	GG	qG
$J/\psi, \psi(2S)$	$\langle \mathcal{O}_8^H [^3S_1] \rangle (\alpha_s^2)$	$\Delta_8^H (\alpha_s^2)$ $\langle \mathcal{O}_1^H [^3S_1] \rangle (\alpha_s^3)$	
χ_{c0}	$\langle \mathcal{O}_8^H [^3S_1] \rangle (\alpha_s^2)$	$\langle \mathcal{O}_1^H [^3P_0] \rangle (\alpha_s^2)$	
χ_{c1}	$\langle \mathcal{O}_8^H [^3S_1] \rangle (\alpha_s^2)$	$\langle \mathcal{O}_1^H [^3P_1] \rangle (\alpha_s^3)$	$\langle \mathcal{O}_1^H [^3P_1] \rangle (\alpha_s^3)$
χ_{c2}	$\langle \mathcal{O}_8^H [^3S_1] \rangle (\alpha_s^2)$	$\langle \mathcal{O}_1^H [^3P_2] \rangle (\alpha_s^2)$	

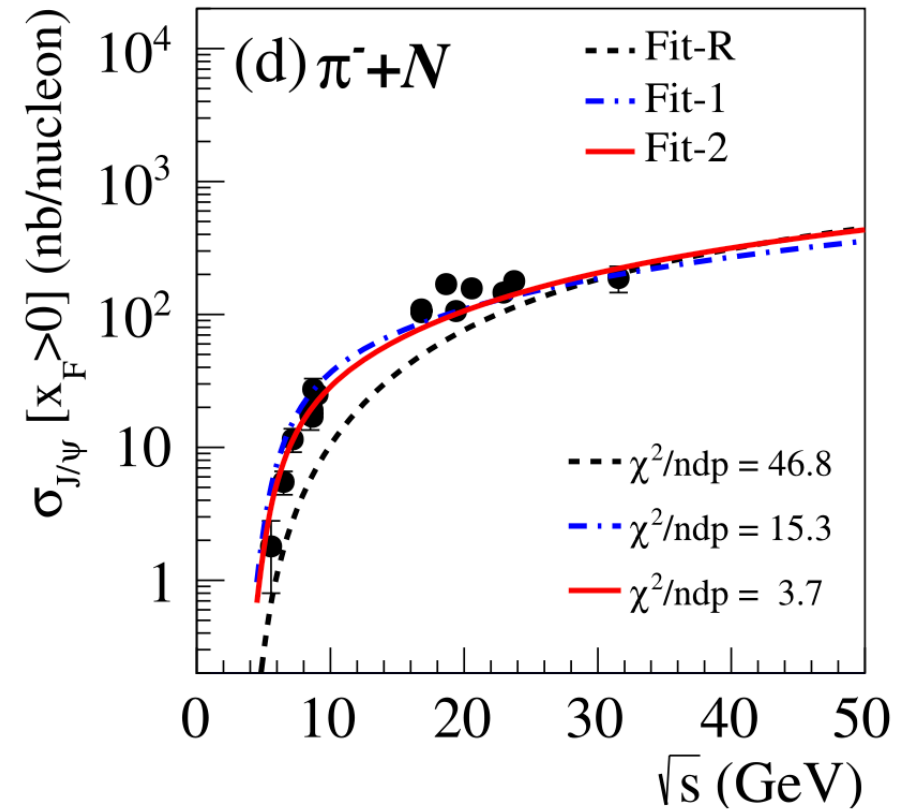
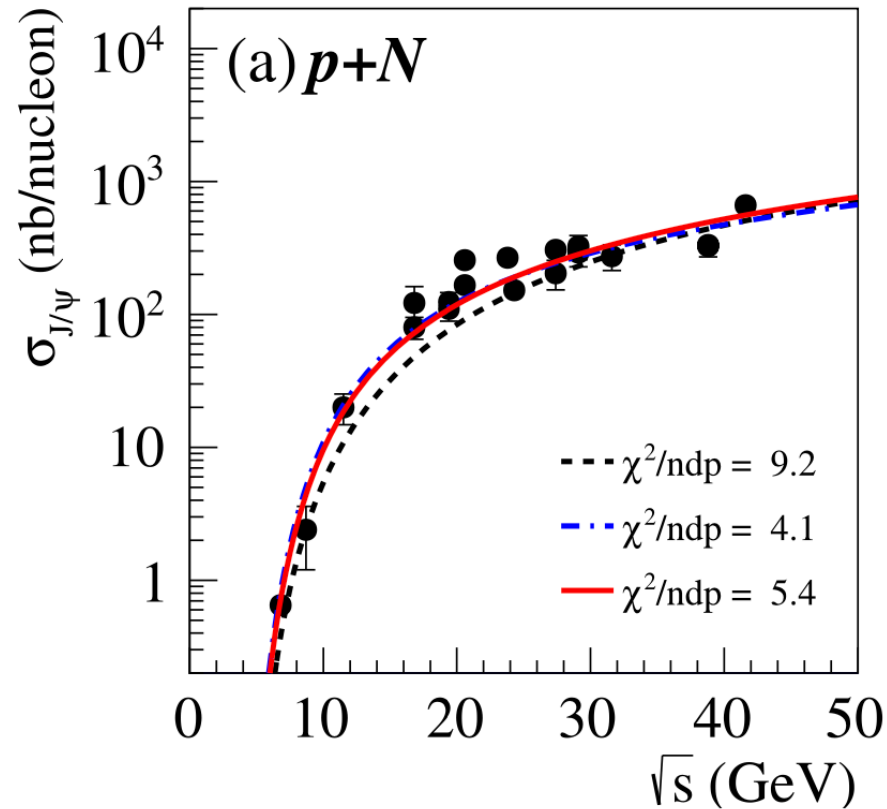
$$\Delta_8^H = \langle \mathcal{O}_8^H [^1S_0] \rangle + \frac{3}{m_c^2} \langle \mathcal{O}_8^H [^3P_0] \rangle + \frac{4}{5m_c^2} \langle \mathcal{O}_8^H [^3P_2] \rangle.$$

- ◆ Data used: only integrated cross sections

- π -induced J/ψ and $\psi(2S)$
- p -induced J/ψ and $\psi(2S)$

NRQCD results – integrated cross sections

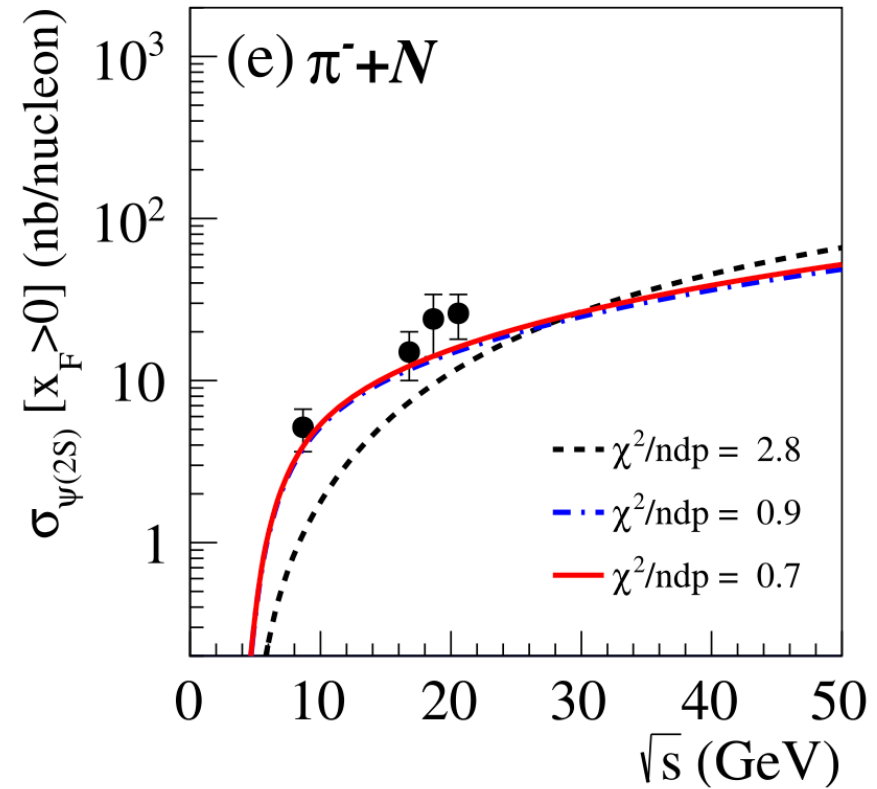
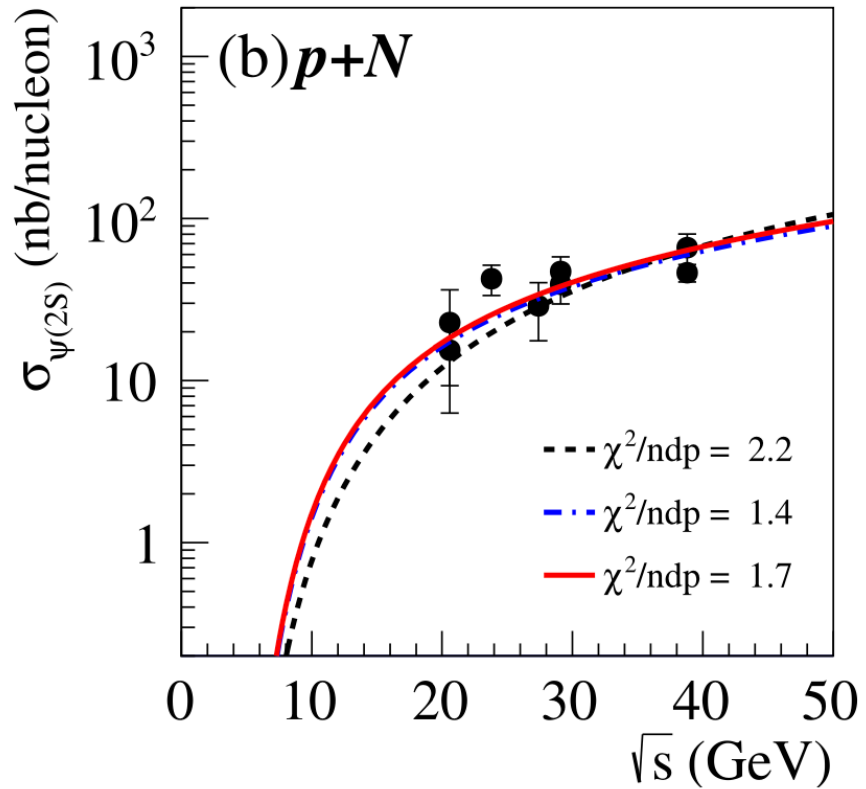
◆ Charmonium J/ψ data



Good common fit to both pion and proton-induced data

NRQCD results – integrated cross sections

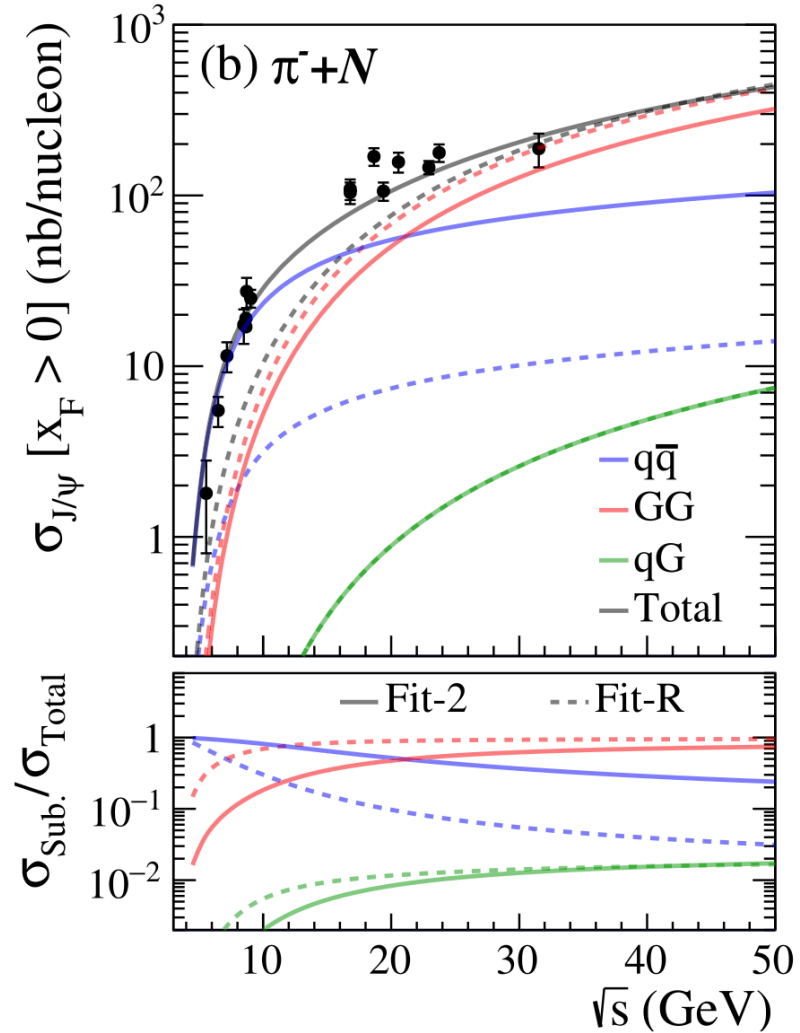
◆ Charmonium $\psi(2S)$ data



Good common fit to both J/ψ and $\psi(2S)$ states

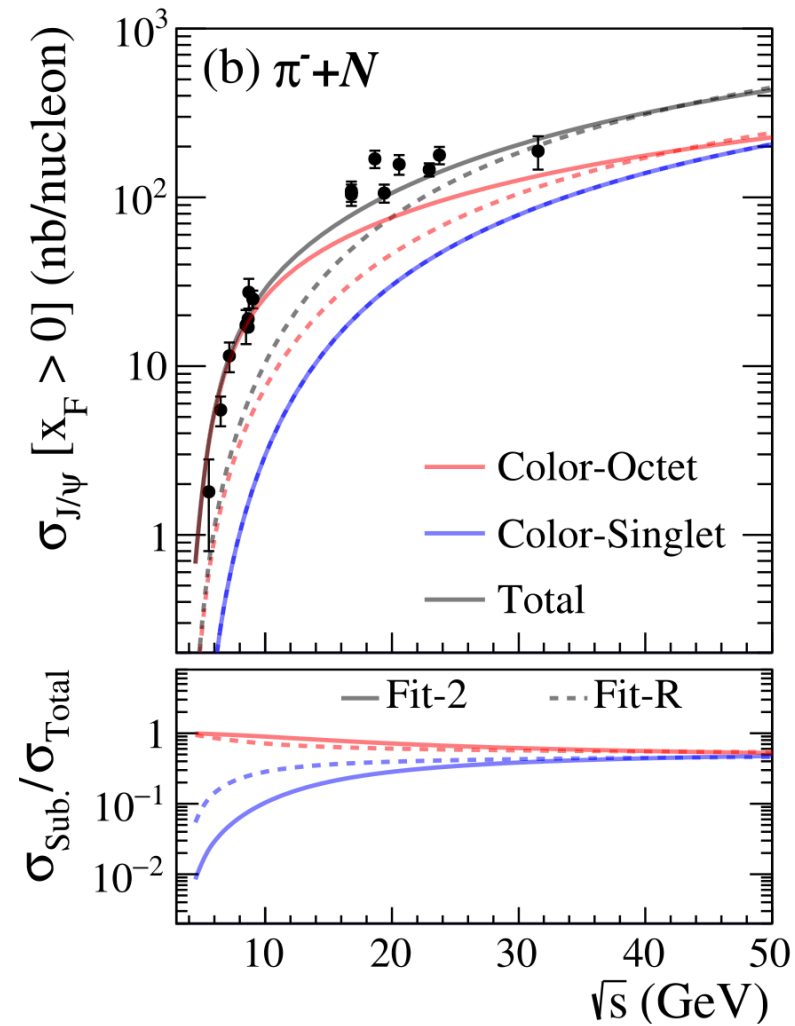
NRQCD results – integrated cross sections

◆ J/ψ subprocesses



NRQCD results – integrated cross sections

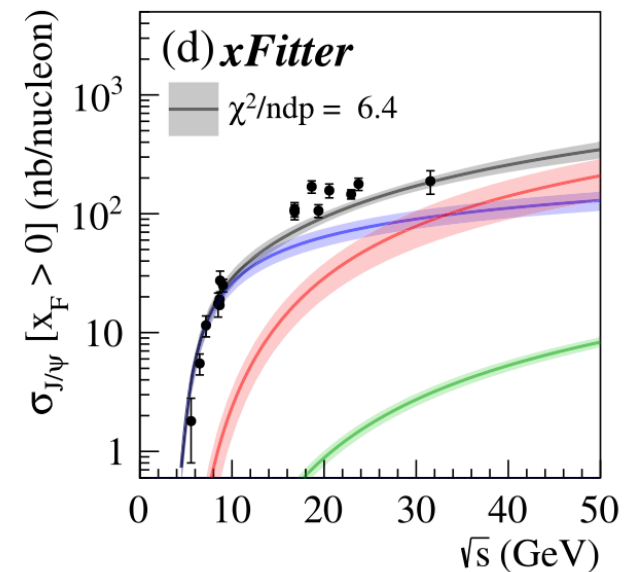
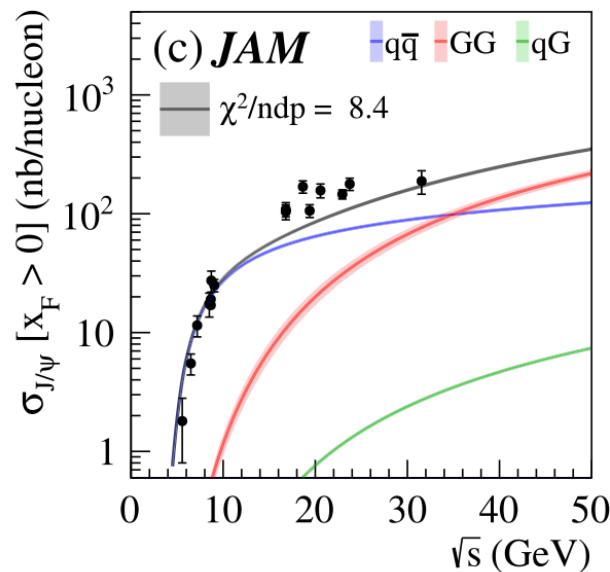
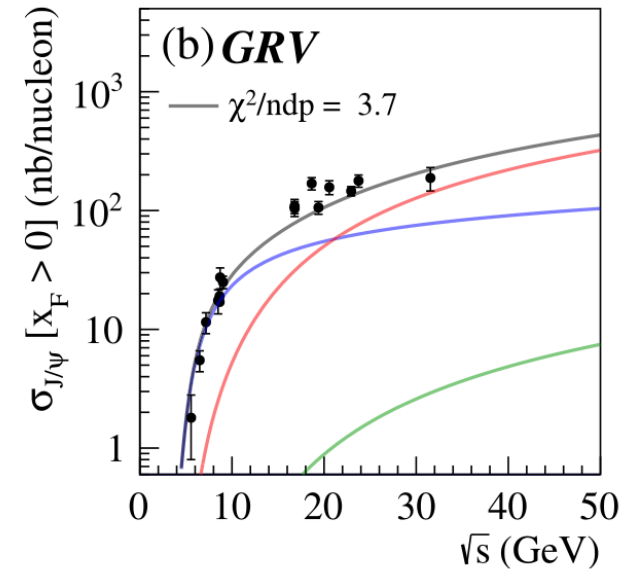
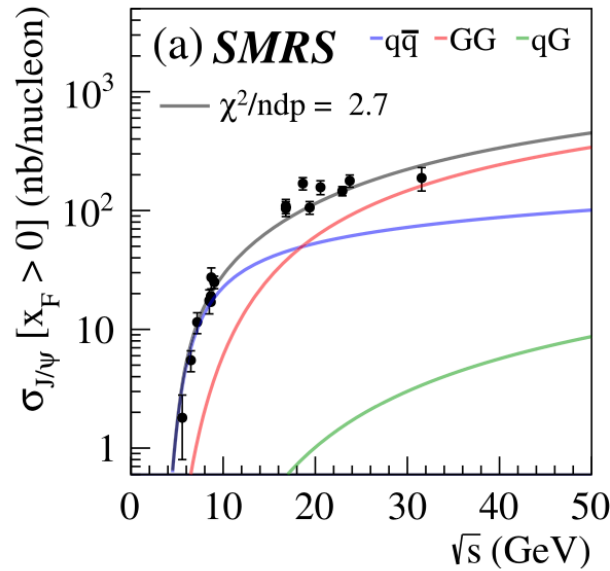
◆ J/ψ CO vs CS



The Color Octet process dominates the cross section

NRQCD results – integrated cross sections

◆ PDF dependence



Use of SMRS and GRV leads to better χ^2 values

Further study:
integrated cross section AND x_F -dependent data



NRQCD fits including x_F -dependent data

- ◆ Data used (Chang et al., PRD 107, 2023)
 - Atomic numbers < 10 , both proton and pion-induced data, for J/ψ and $\psi(2S)$

TABLE II. Differential cross sections datasets for charmonium production [J/ψ , $\psi(2S)$ and $R_\psi(x_F)$] used in the study, listed in order of decreasing beam momentum.

Experiment	Beam	P_{beam} (GeV/c)	Target	Data	x_F	ndf	Norma. ^a	Reference
FNAL E672, E706	π	515	Be	$\sigma^{J/\psi}$	[0.11, 0.79]	35	12.0	[82]
FNAL E705	π	300	Li	$\sigma^{J/\psi}$	[-0.10, 0.45]	12	9.5	[83]
CERN NA3 ^b	π	280	p	$\sigma^{J/\psi}$	[0.025, 0.825]	17	13.0	[84]
CERN NA3 ^b	π	200	p	$\sigma^{J/\psi}$	[0.05, 0.75]	8	13.0	[84]
CERN WA11 ^b	π	190	Be	$\sigma^{J/\psi}$	[-0.35, 0.75]	12	^c 10.0	[85]
CERN NA3 ^b	π	150	p	$\sigma^{J/\psi}$	[0.025, 0.925]	19	13.0	[84]
FNAL E537	π	125	Be	$\sigma^{J/\psi}$	[0.05, 0.95]	10	6.0	[86]
CERN WA39 ^b	π	39.5	p	$\sigma^{J/\psi}$	[0.05, 0.85]	9	15.0	[87]
FNAL E672, E706	π	515	Be	$\sigma^{\psi(2S)}$	[0.17, 0.73]	5	16.0	[82]
FNAL E615	π	253	W	$\sigma^{\psi(2S)} / \sigma^{J/\psi}$	[0.275, 0.975]	15		[88]
HERA-B	p	920	W	$\sigma^{\psi(2S)} / \sigma^{J/\psi}$	[-0.3, 0.075]	8		[78]
CERN NA50	p	450	W	$\sigma^{\psi(2S)} / \sigma^{J/\psi}$	[-0.075, 0.075]	4		[89]
FNAL E789	p	800	Au	$\sigma^{\psi(2S)} / \sigma^{J/\psi}$	[0.00, 0.12]	5		[90]
FNAL E771	p	800	Si	$\sigma^{\psi(2S)} / \sigma^{J/\psi}$	[0.00, 0.20]	6		[91]
FNAL E705	p	300	Li	$\sigma^{J/\psi}$	[-0.10, 0.45]	12	10.1	[83]
CERN NA3 ^b	p	200	p	$\sigma^{J/\psi}$	[0.05, 0.75]	8	13.0	[84]

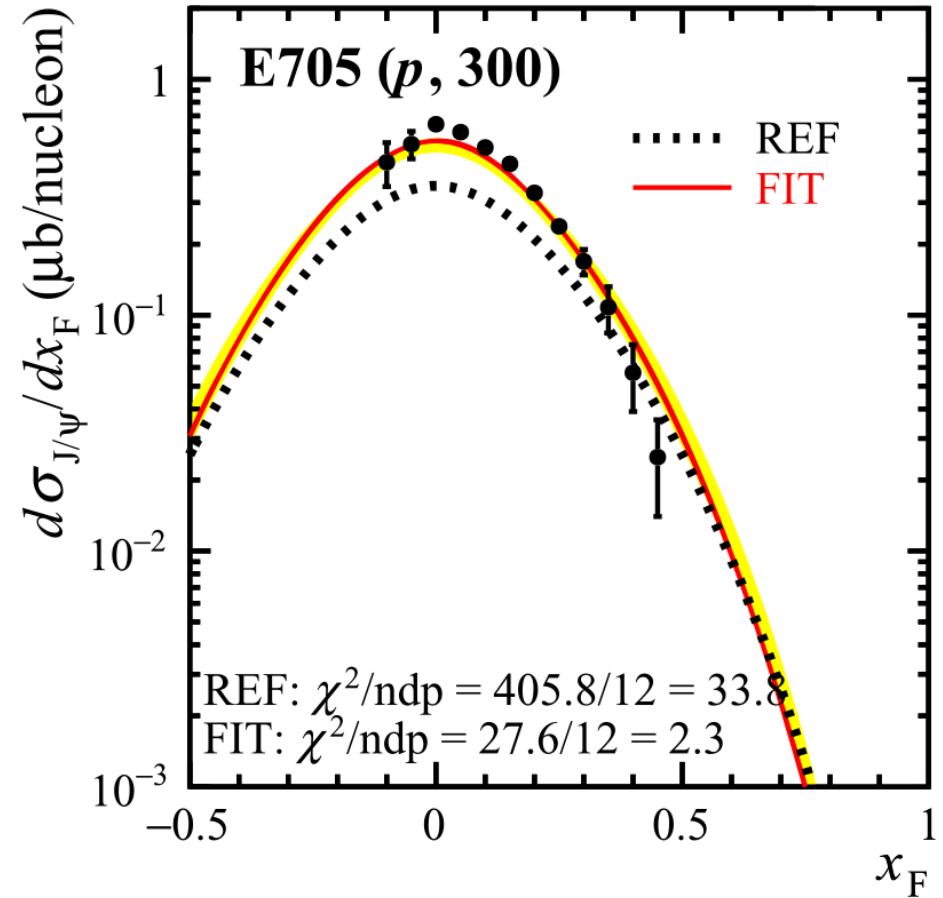
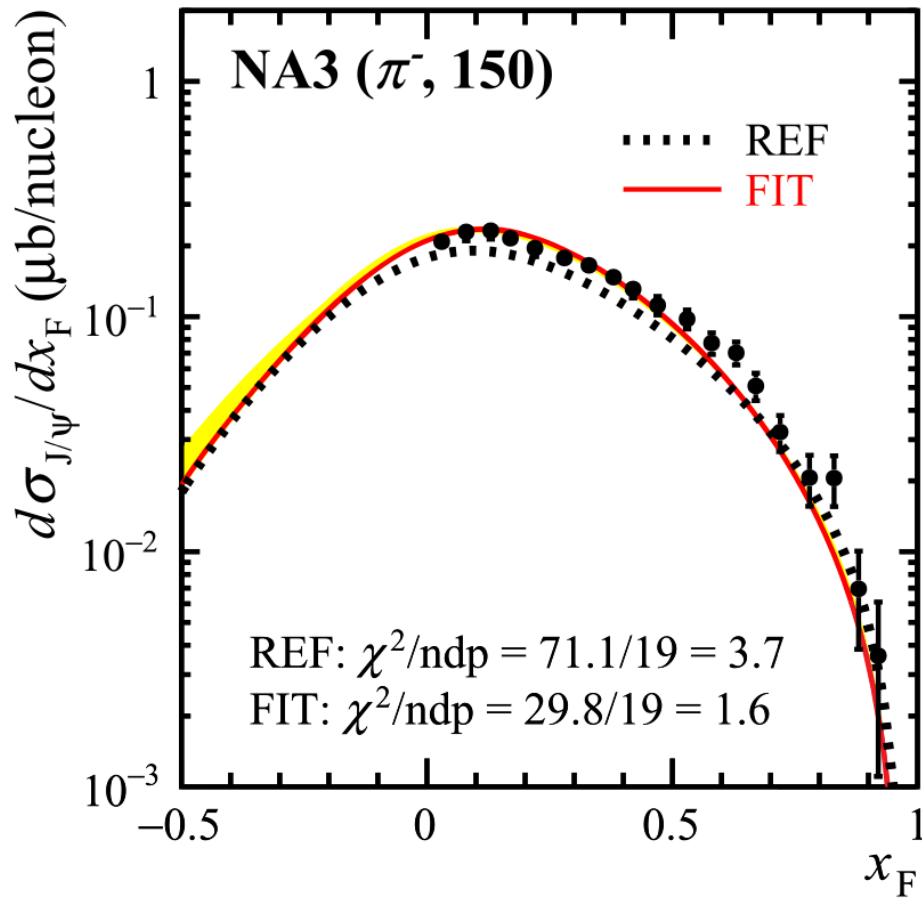
pion
164 points

proton
82 points

16 data sets

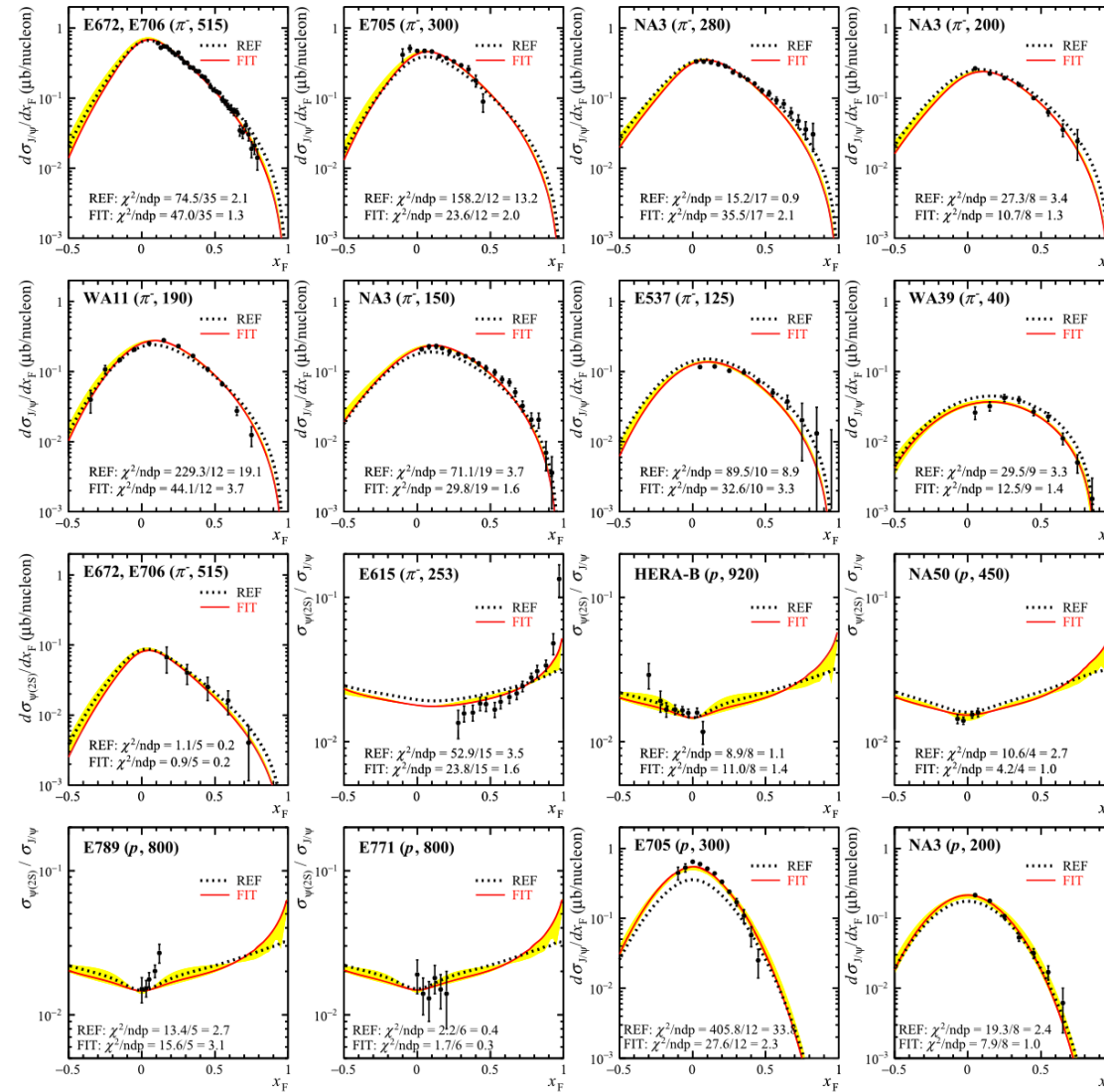


Fit results: examples for π and p-induced data



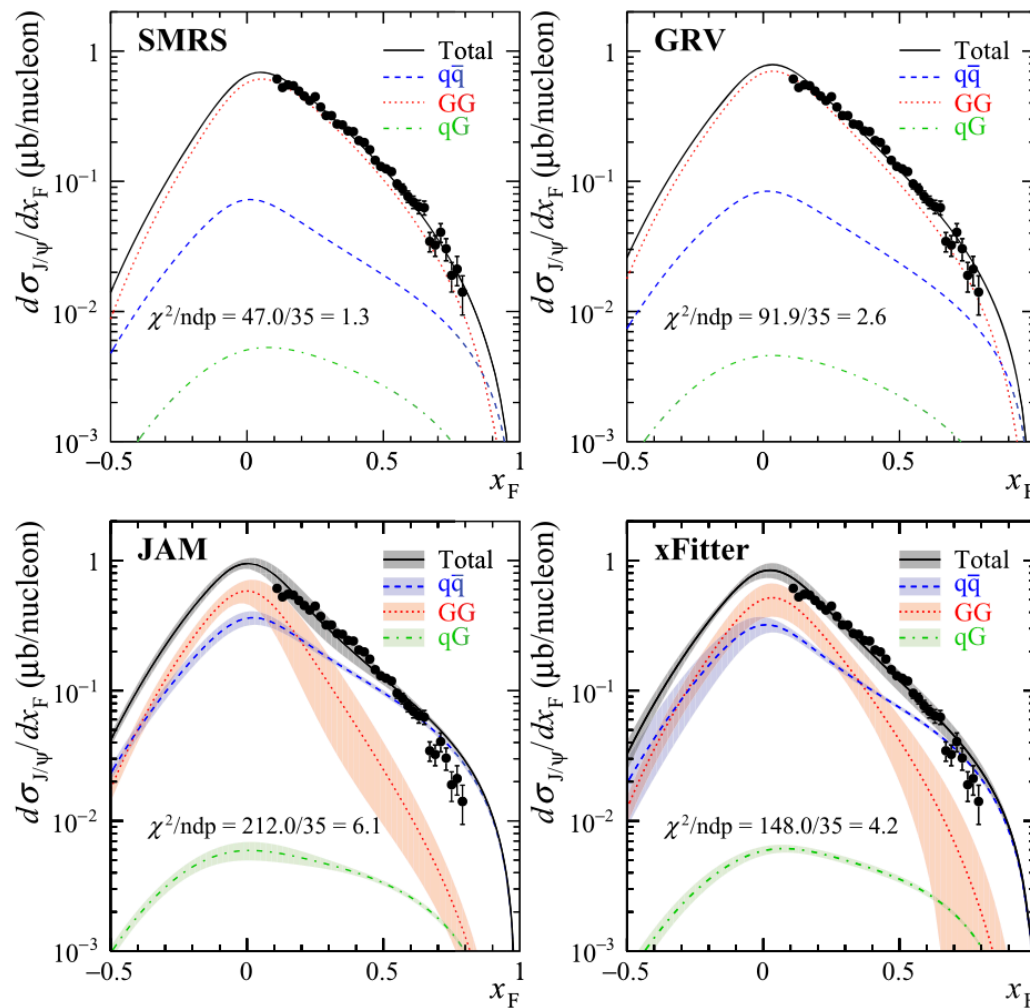
Good fit on both π and p data

Fit results: all data sets



NRQCD fit results: dependence on the pion PDFs

- J/ψ π -induced data at 515 GeV/c

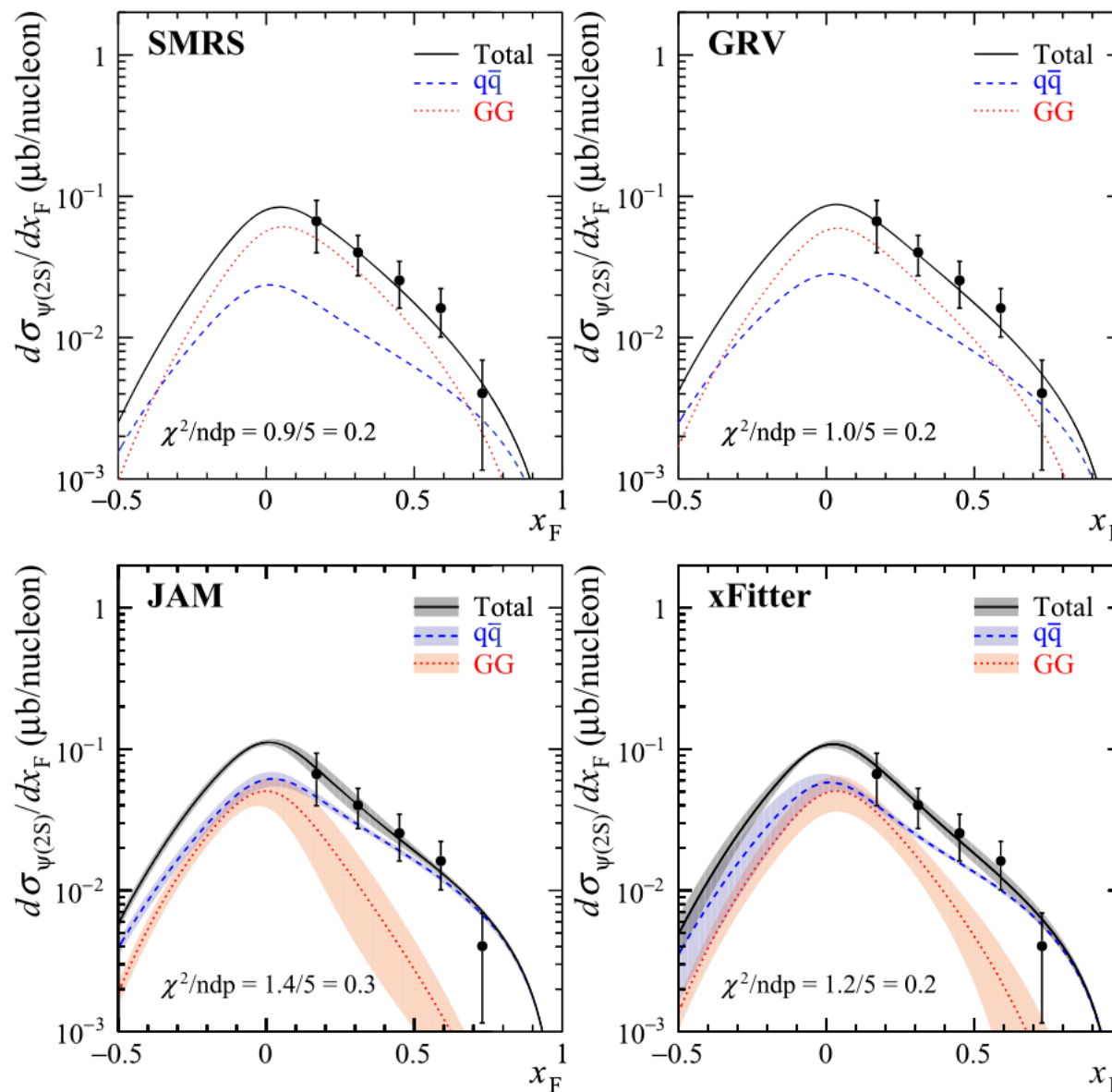


NRQCD fit results: dependence on the pion PDFs

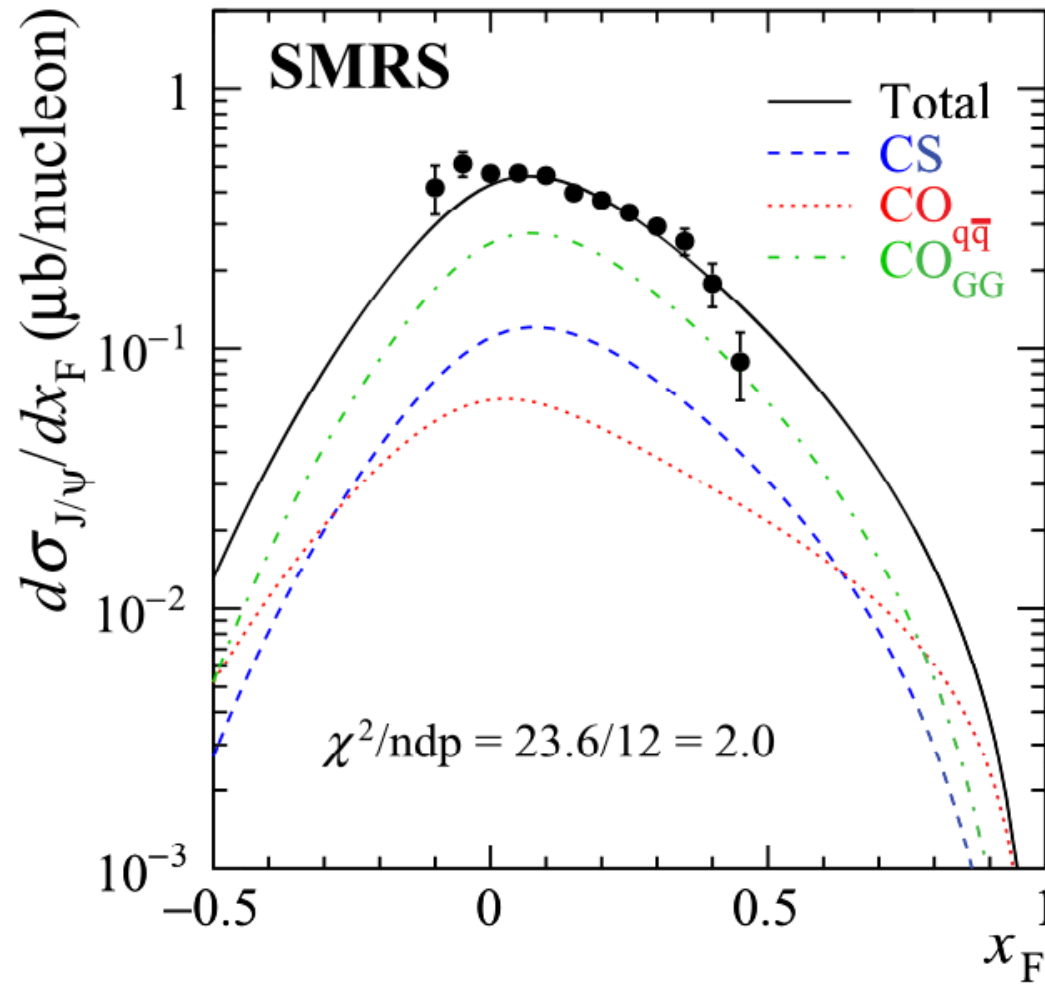
- $\psi(2S)$ π -induced data at 515 GeV/c

Data from E672/E706

E = 515 GeV



Sensitivity of the FT data to the CO component



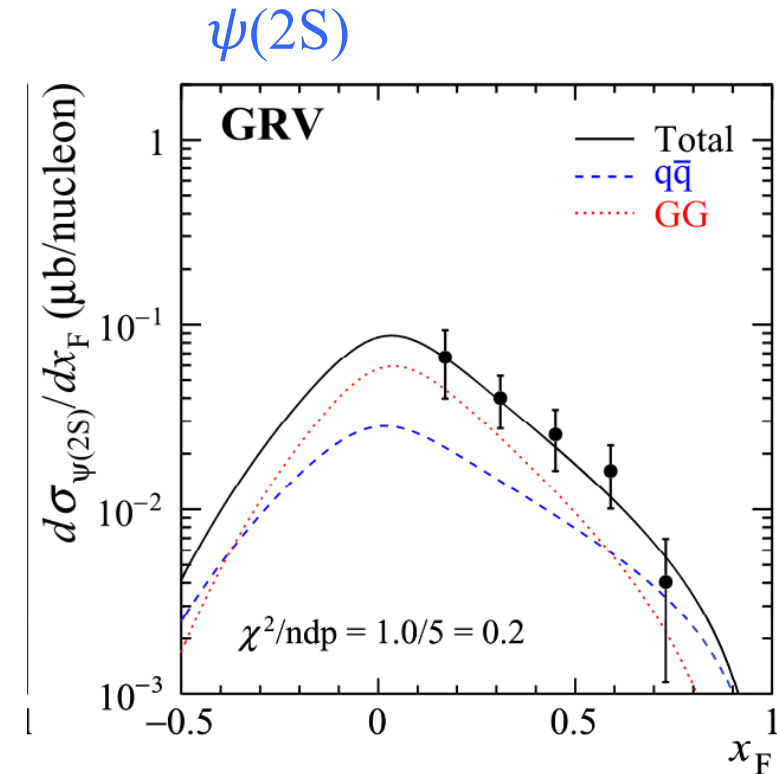
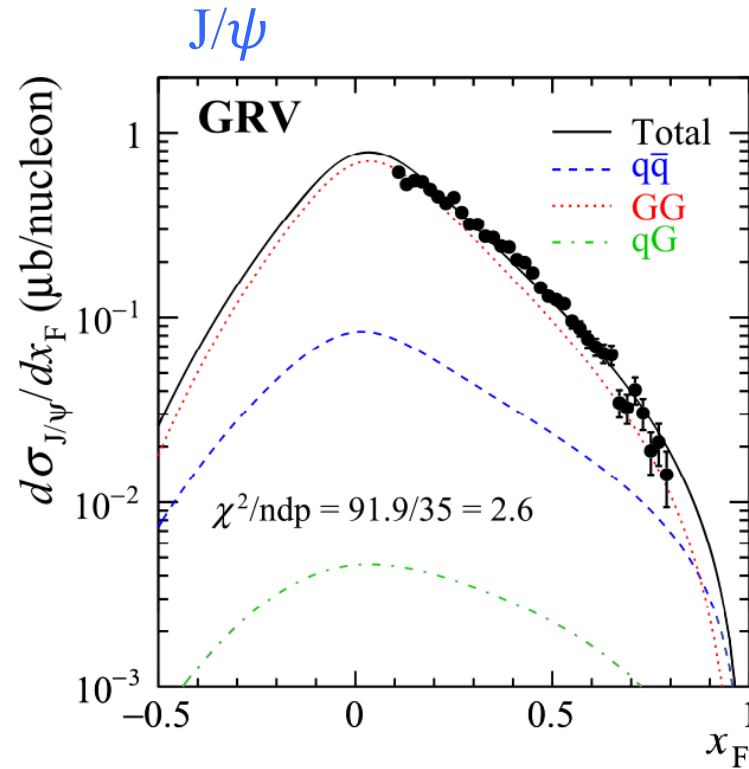
Data from
E705

$E = 300 \text{ GeV}$

The CO gg contribution dominates the cross section

Comparison between J/ψ and $\psi(2S)$

- ◆ π -induced data
at 515 GeV/c



- ◆ Differences
 - size of cross section: about an order of magnitude!
 - larger $q\bar{q}$ contribution for $\psi(2S)$!

Further evidences for different J/ψ and $\psi(2S)$ behaviors

■ LDMEs (SMRS)

■ $\Delta_8 (J/\psi) = 0.0560 \pm 0.0016$

$\Delta_8 (\psi(2S)) = 0.0057 \pm 0.0003$

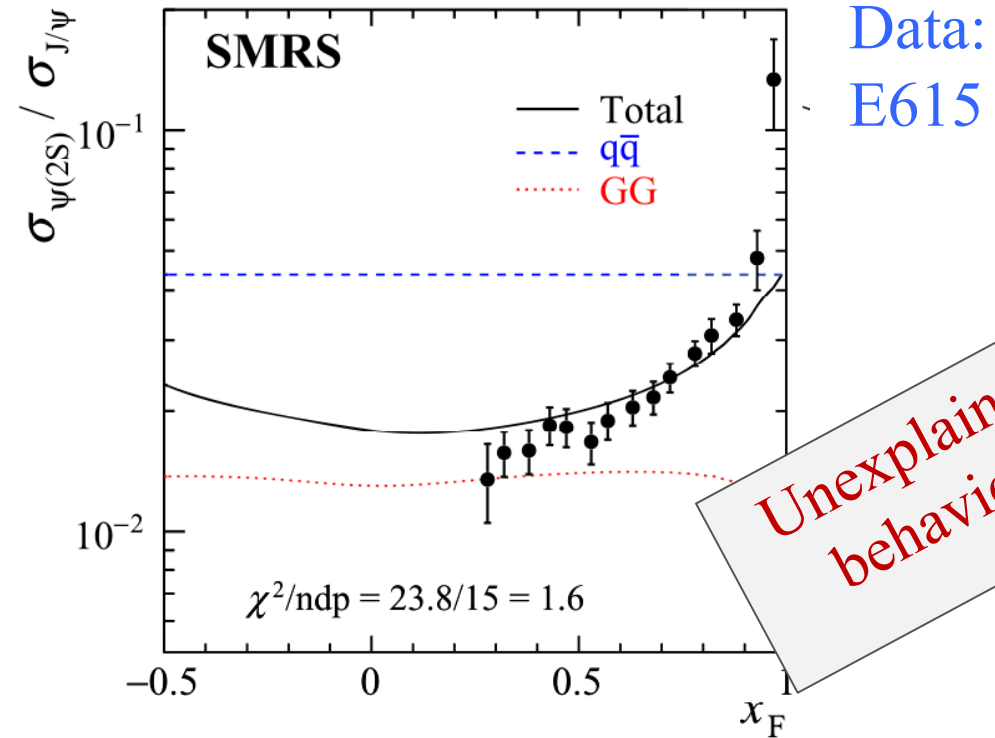
Ratio: $= \sim 10$

■ $\langle 0_8[{}^3S_1] (J/\psi) = 0.0259 \pm 0.0023$

$\langle 0_8[{}^3S_1] (\psi(2S)) = 0.0132 \pm 0.0009$

Ratio: $= \sim 2 !$

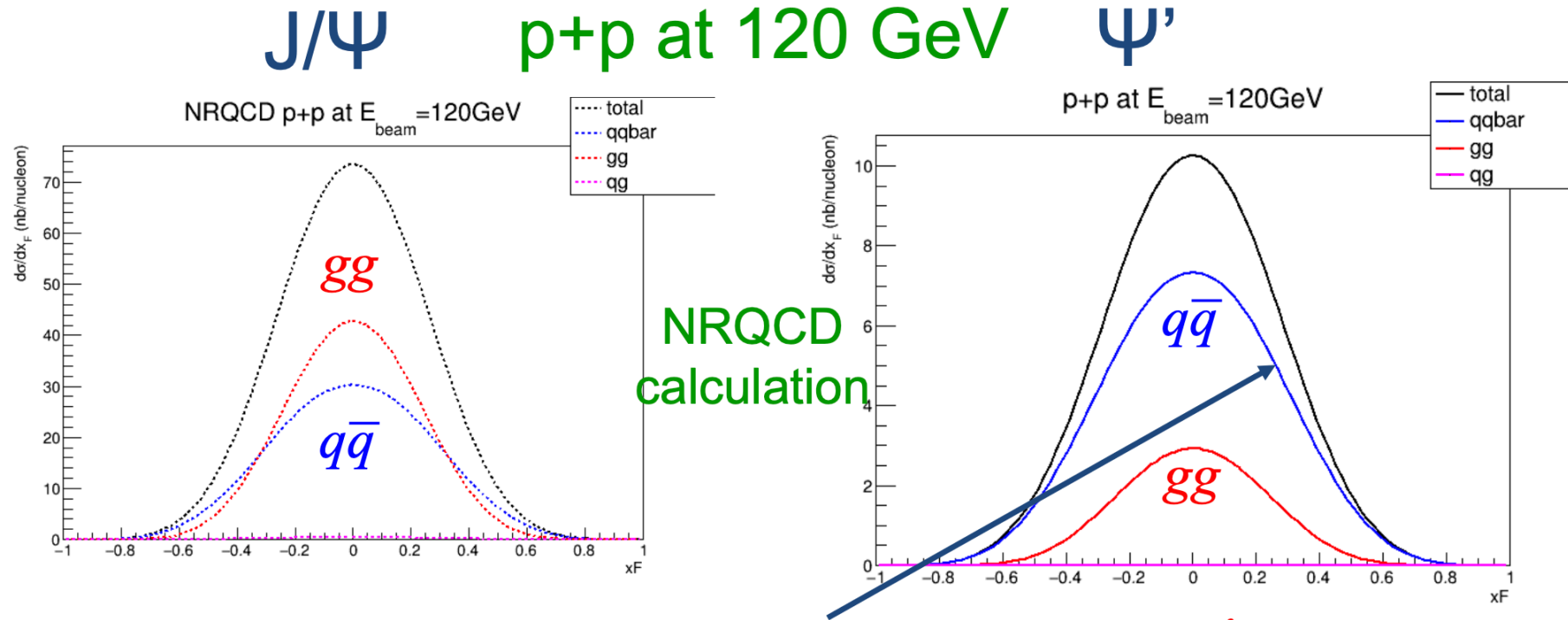
■ Cross section ratio at $E = 252$ GeV



The $q\bar{q}$ contribution in $\psi(2S)$ is much larger than in J/ψ
 The behavior of the data cannot be explained using CEM

Comparison between J/ψ and $\psi(2S)$ for p+p at 120 GeV

- ◆ Calculation: W.-C. Chang



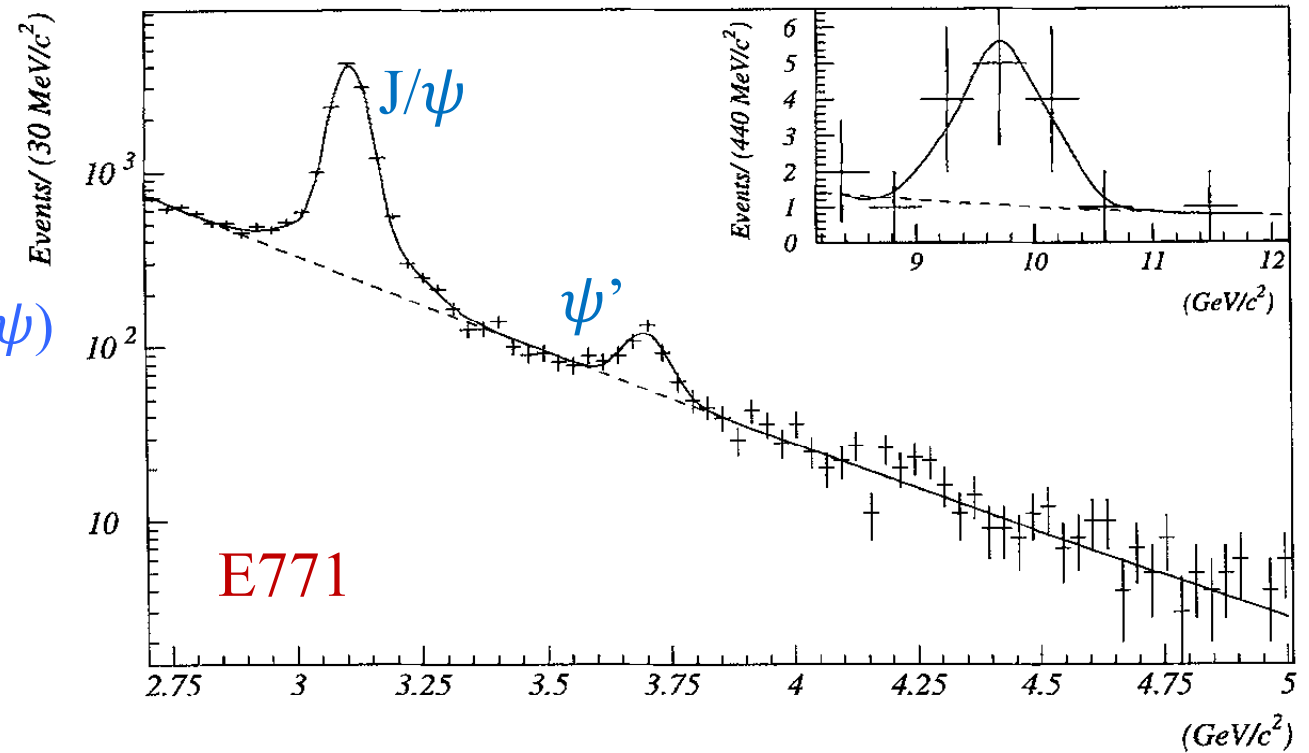
Combined use of J/ψ and $\psi(2S)$ data would greatly help in separating $q\bar{q}$ and gg contributions

$\Rightarrow \psi(2S)$ could be considered as a Drell-Yan surrogate

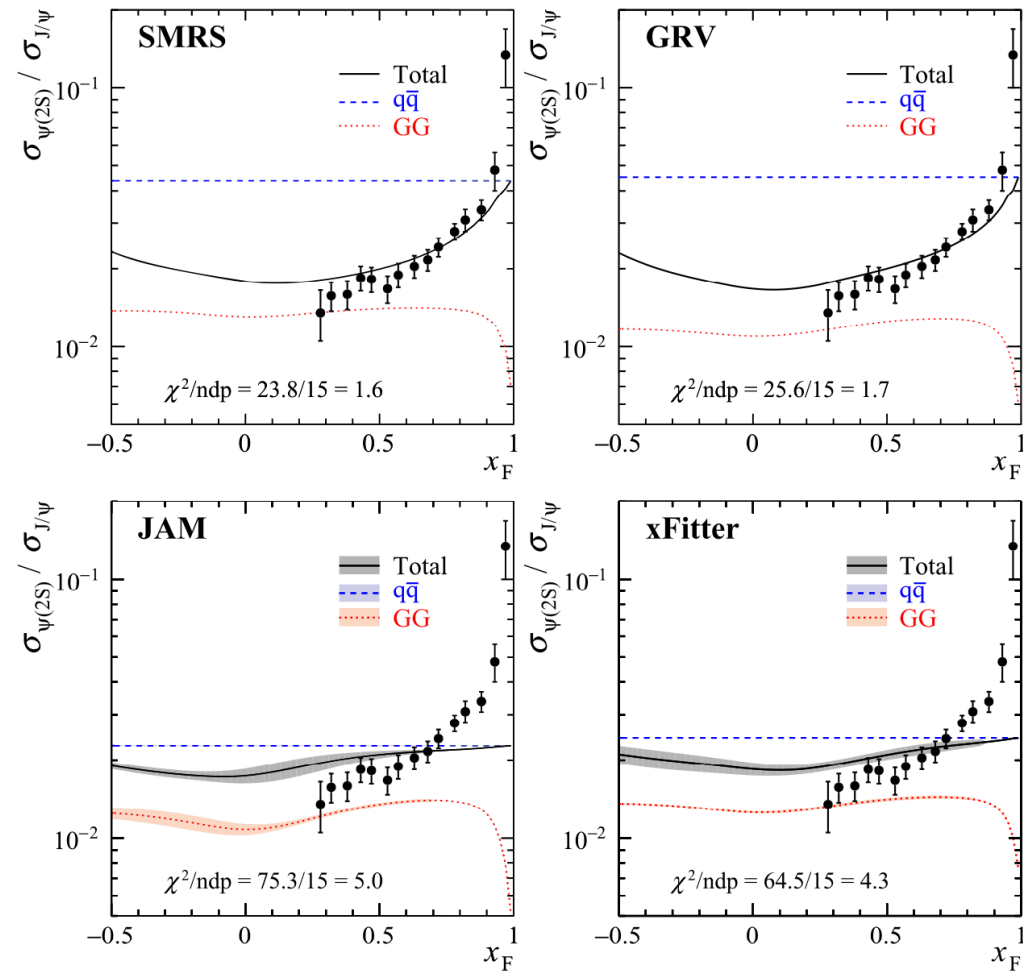
Why measure $\psi(2S)$ cross sections?

- ◆ Pros:
 - Different sensitivity to $g(x)$ and $q(x)$
 - No feeddown contributions
- ◆ Cons:
 - Low counting rates (factor of 50 ! vs J/ψ)
 - Very good resolution required
- ◆ AMBER could/should? do it

E771 Collaboration / Physics Letters B 374 (1996) 271–276



Dependence on the pion PDFs



SMRS and GRV fits do (AGAIN!) a better job

LDMEs compared to collider energies fits values

◆ J/ψ production	$\langle O_8^{J/\psi} [^3S_1] \rangle$ (GeV ³)	
■ Present work	$(2.59 \pm 0.23) \times 10^{-2}$	PRD 107, 2023
■ Buttenshoen-Kniehl	$(0.31 \pm 0.06) \times 10^{-2}$	PRL 106, 2011
■ Chao, Ma et al.,	$(0.30 \pm 0.12) \times 10^{-2}$	PRL 108, 2012
■ Zhang, Sun et al.,	$(1.00 \pm 0.30) \times 10^{-2}$	PRL 114, 2015
■ Bodwin et al.,	$(1.10 \pm 1.00) \times 10^{-2}$	PRL 114, 2015
◆ $\psi(2S)$ production	$\langle O_8^{\psi(2S)} [^3S_1] \rangle$ (GeV ³)	
■ Present work	$(1.32 \pm 0.09) \times 10^{-2}$	PRD 107, 1023
■ Gong, Wan et al.,	$(0.34 \pm 0.12) \times 10^{-2}$	PRL 106, 2011
■ Buttenshoen-Kniehl, Fit1	$(0.15 \pm 0.01) \times 10^{-2}$	PRD 107, 2023
■ Buttenshoen-Kniehl, Fit4	$(0.28 \pm 0.01) \times 10^{-2}$	PRD 107, 2023

Price for a good fit: values for $\langle O_8[^3S_1] \rangle$ between a factor of 2.5 and 10 larger
(Note: high-energy fits are usually limited to values of $p_T > 5$ or 7 GeV/c)

- ◆ The present NRQCD analysis could be further refined if the following items are considered:
 - Include higher order terms of NRQCD
 - Add data from heavier targets
 - Note: FT data are limited to small p_T values ($\lesssim 4$ GeV/c)

- ◆ An optional next step
 - Include charmonium production data in a global fit

◆ Conclusions

- A common NRQCD fit to FT pion and proton-induced charmonium data is made
- A good fit to J/ψ and $\psi(2S)$ data, as well as to their ratios
- Better fit results for SMRS and GRV, in comparison with the recent JAM and xFitter PDFs
- Explained by larger gluon contributions, particularly at large x_F
- Use of either CEM or NRQCD leads to qualitatively similar results

◆ And a surprise

- The data for $\psi(2S)$ favor a much larger $q\bar{q}$ contribution than that for J/ψ