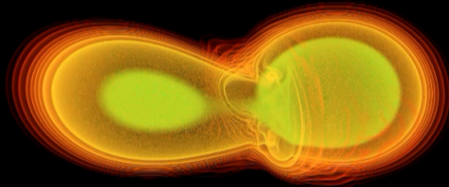


Quasi-universal relations of gravitational wave signal from binary neutron star mergers

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Motivation:

- ▶ easily identifiable frequencies in the GW signal strongly correlate with
 - ▶ total mass of the system M_{tot} ,
 - ▶ mass ratio of the components q ,
 - ▶ EOS-specific quantities, e.g. tidal deformability $\kappa_2^T = \kappa_2^T(\text{EOS})$

Here:

- ▶ propose new, accurate universal relations for these frequencies
- ▶ investigate the subdominant $m = 1$ mode and its secular growth
- ▶ report findings consistent across 3 codes and 3 initial data solvers



- ▶ waveforms from GU group^{1 2}, and others³ (CoRe database)
- ▶ in total, ~ 120 simulations in GRHD (no B field, $s_1 = s_2 = 0, e < 0.01$)
- ▶ 12 EOS, some including a strong 1-st order PT and deconfined quark phase
- ▶ $M_{\text{tot}} \in [2.4, 3.33]M_{\odot}, q \in [0.485, 1.0], \kappa_2^T \in [33, 458]$

¹Tootle et al.; Astrophys.J.Lett. **922** (2021) 1, L19

²Tootle et al.; SciPost Phys. **13** (2022) 109

³Gonzalez et al.; 2022, Class.Quant.Grav. **40** (2023) 8, 085011

Waveform - amplitude, frequency, spectral density

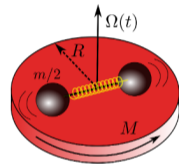
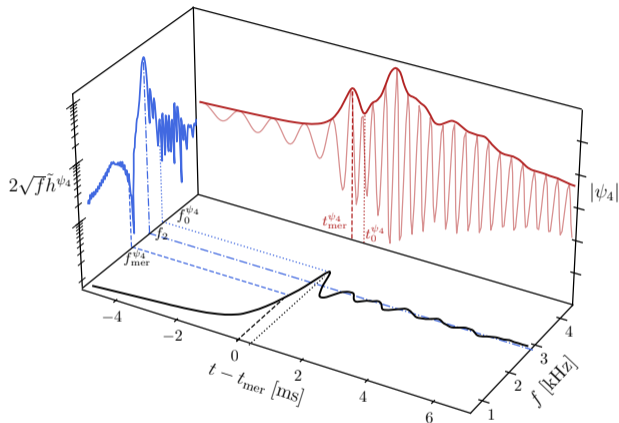


Figure: *

Takami et al.;
Phys.Rev.D **91**,
064001 (2015)

Three characteristic frequencies identifiable:

- ▶ merger frequency f_{mer}
- ▶ quenched-quadrupole moment frequency f_0
- ▶ long-lived post-merger frequency f_2

Parametrizing the dependence



Relation between

$$(f_{\text{mer}}, f_0, f_2) \leftrightarrow (M_{\text{tot}}, q, \kappa_2^T) ?$$

Augment previous Ansatz ^{4 5} with **mass ratio corrections**:

$$\log_{10} \left[\frac{M_{\text{tot}}}{M_{\odot}} \frac{f}{\text{Hz}} \right] = a_0 + (b_0 + b_1 q + b_2 q^2) (\kappa_2^T)^n$$

5 parameters a_0, b_0, b_1, b_2, n sufficient, previous Ansatz had 3.

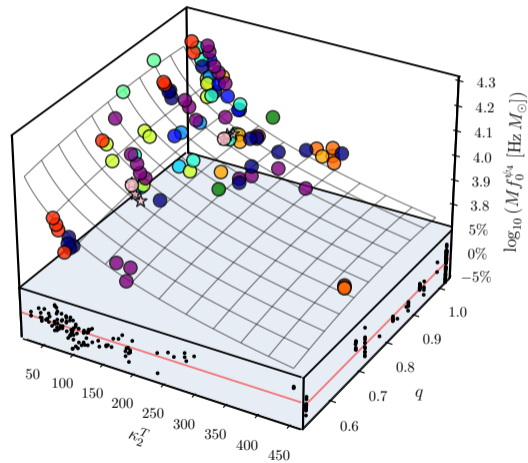
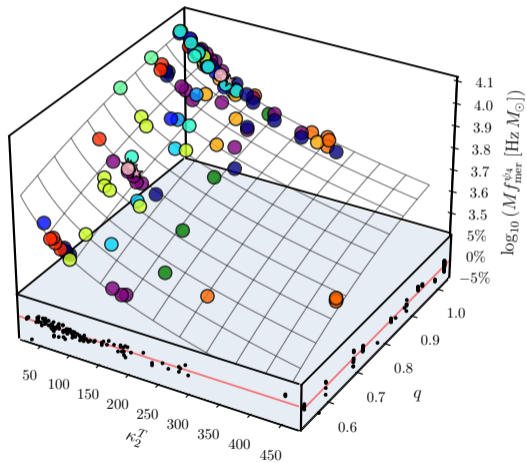
⁴Rezzolla, Takami; Phys.Rev.D **93**, 124051 (2016)

⁵Read et al.; Phys. Rev. D **88**, 044042 (2013)

Result of the fits



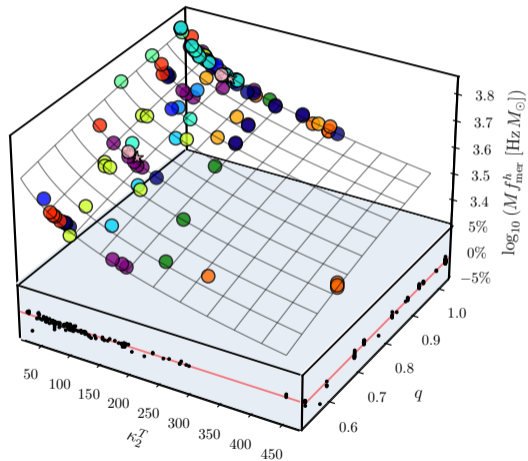
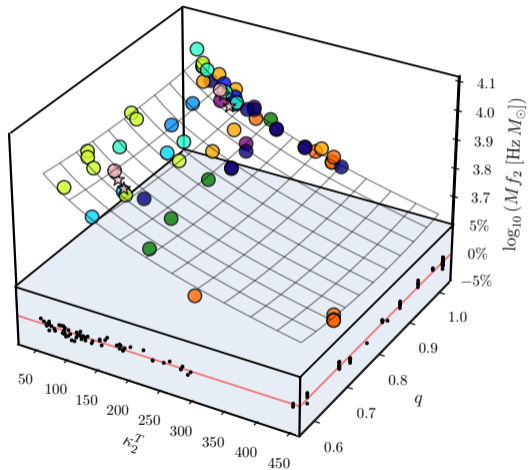
- TNTY
- LS220
- H4
- ALF2
- BLQ
- BHB1p
- MS1b
- SLy
- MPA1
- SFHo
- DD2
- VQCD



Result of the fits



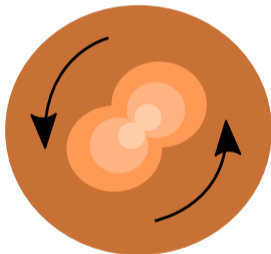
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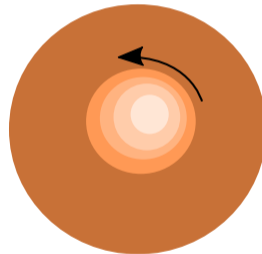
Modes of radiation



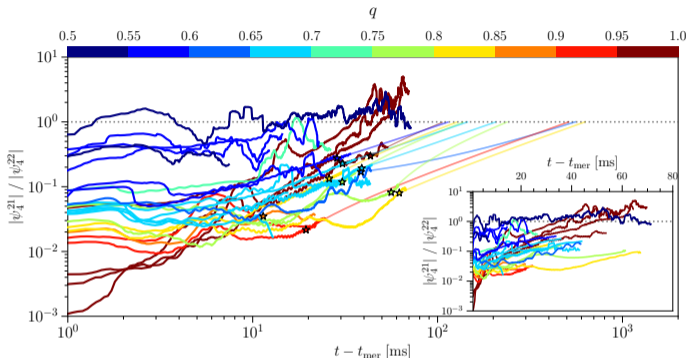
$m=2$



$m=1$



Secular growth of the subdominant mode



- ▶ contribution of the $m = 1$ mode to the overall strength of the signal is generic
- ▶ initial (~ 10 ms) contribution dependent on mass asymmetry
- ▶ secular growth of the $m = 1$ mode, might dominate as early as $\sim 20 - 50$ ms
- ▶ dominant $m = 1$ frequency is $\sim \frac{1}{2} f_2$

Accurate universal relations on large datasets can be useful for:

- ▶ informing the phase part of the waveform models;
 $(M_{\text{tot}}, q, \text{EOS}) \rightarrow (f_{\text{mer}}, f_0, f_2) \rightarrow f_{\text{GW}}(t)$
- ▶ identifying universality-breaking physics (HQ PT, new DOF, etc.)
- ▶ inference of the underlying EOS and/or parameters of binary

Dominance of the subdominant mode long-term:

- ▶ potential for detection by present detectors with high SNR or by 3G detectors
- ▶ might couple to post-merger differently from $m = 2$ mode (viscosity, phase transitions)

In summary:

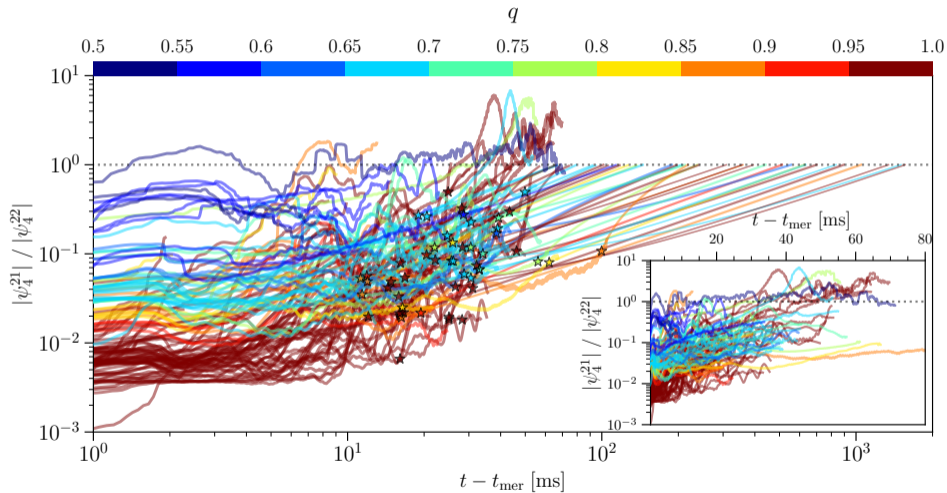
- ▶ suggest new functional relations for the merger and post-merger frequencies

$$\log_{10} \left[\frac{M_{\text{tot}}}{M_{\odot}} \frac{f}{\text{Hz}} \right] = a_0 + (b_0 + b_1 q + b_2 q^2) (\kappa_2^T)^n$$

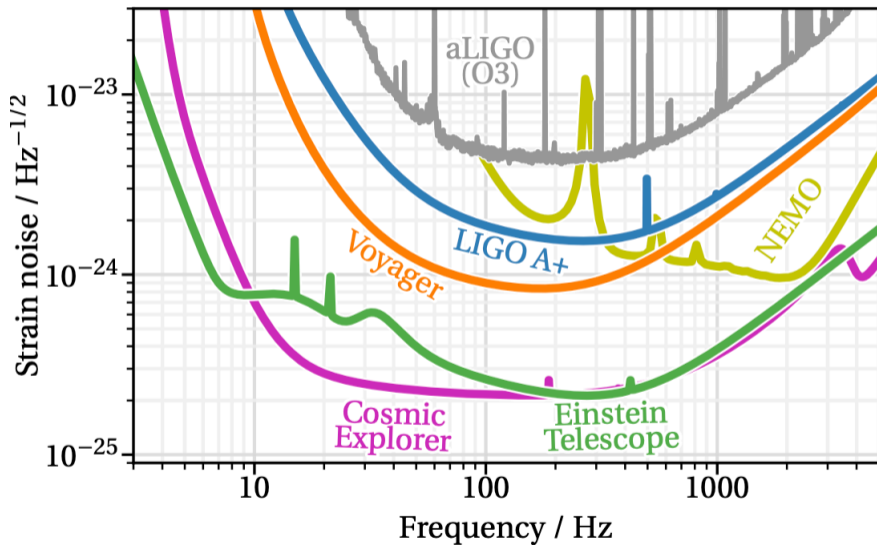
which use a smaller number of parameters and are more accurate

- ▶ identify a new frequency f_0 and explain its origin using a toy model
- ▶ confirm the secular growth of the $m = 1$ mode for generic binaries

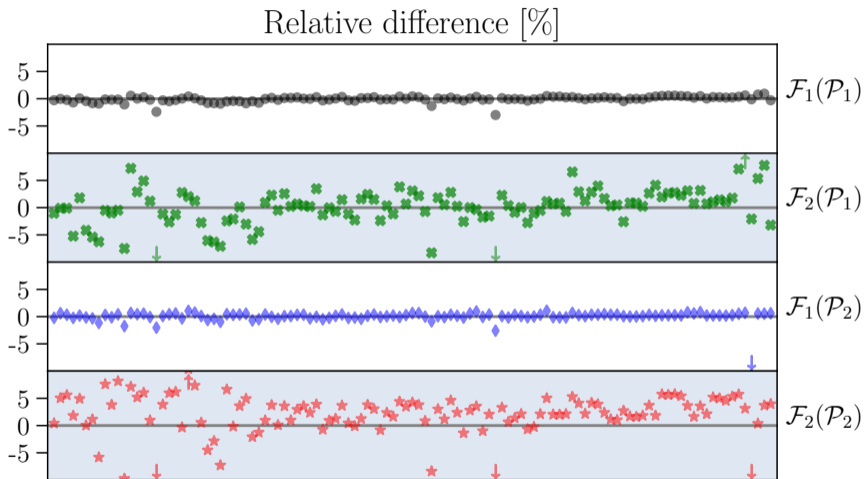
Secular growth - all datasets



Detector sensitivity



Comparing the fits



Quantifying the equation of state dependence



Tidal forces acting on a companion star impact the GW frequency. To lowest order, this influence is related to:

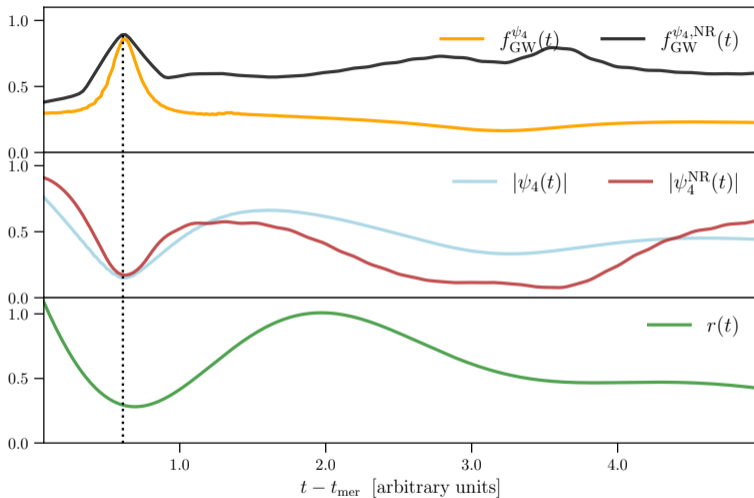
$$k_2 = \frac{Q_{ij}}{\mathcal{E}_{ij}} \quad \left(\frac{\text{response}}{\text{tidal field}} \right)$$

We then define $\Lambda = \frac{2}{3} \frac{k_2}{\mathcal{E}^5}$, with $\mathcal{E} = \frac{M_{ADM}}{R}$. Finally, we parametrize the joint interaction with:

$$\kappa_2^T = \frac{M_1 M_2}{M^2} \left[\left(\frac{M_1}{M} \right)^3 \Lambda_1 + \left(\frac{M_2}{M} \right)^3 \Lambda_2 \right] = \kappa_2^T(M_{\text{total}}, q, \text{EOS})$$

By invoking *quasi-universality*, we mean that we can construct fits for the frequencies that involve κ_2^T , but that it does not matter which EOS this κ_2^T comes from originally (degeneracy).

Toy model for the f_0 frequency



- ▶ with tuning of the initial parameters, the f_0 frequency can be mimicked

Fit parameters



Freq.	a_0	b_0	b_1	b_2	n	$\langle \Delta f / f \rangle$ [%]	$\max(\Delta f / f)$ [%]	χ^2	χ_{red}^2 $\times 10^{-3}$	R^2
$f_{\text{mer}}^{\psi_4}$	4.589	-0.581	0.543	-0.236	0.20	0.65	4.52	0.135	1.19	0.934
f_{mer}^h	4.201	-0.330	0.198	-0.067	0.20	0.32	2.99	0.035	0.30	0.957
$f_{\text{mer}}^{\psi_4}$	6.067	-2.142	0.970	-0.410	0.07^\dagger	0.59	4.24	0.114	1.00	0.938
f_{mer}^h	4.457	-0.578	0.262	-0.087	0.14^\dagger	0.32	2.94	0.034	0.30	0.957
$f_0^{\psi_4}$	6.550	-2.099	0.518	-0.304	0.06^\dagger	1.38	4.22	0.477	4.92	0.611
f_2	4.617	-0.170	-0.264	0.160	0.20^\dagger	0.45	1.34	0.030	0.48	0.926

Table 1. Best-fit values for the coefficients of the functional form \mathcal{F}_1 . Also reported are the maximal and average relative difference, as well as the χ^2 , χ_{red}^2 and R^2 coefficients of the fit. Indicated with a \dagger are the best-fit values of n when this coefficient is constrained by the fit.