




**ECT*-APCTP joint workshop: Exploring
resonance structure with transition GPDs**

August 21 - 25 2023, Trento

**Experimental investigation of
transition GPDs with CLAS12 at
JLAB and future opportunities**

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Generalized Parton Distributions

Generalized Parton Distributions (GPD)



3-D nucleon images in the transverse coordinate and longitudinal momentum space

4 chiral even and 4 chiral odd GPDs

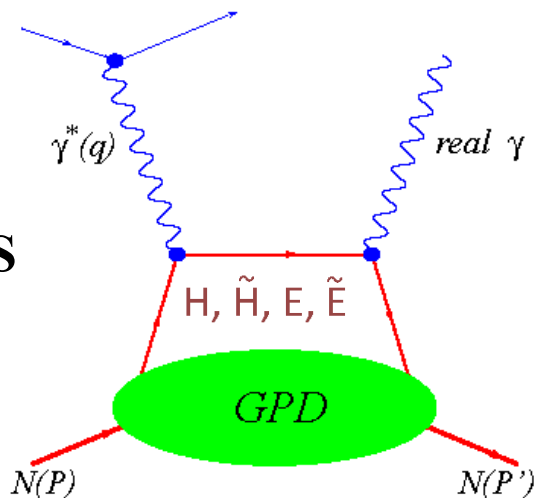
quark pol.

N/q	U	L	T
U	H		\bar{E}_T
L		\tilde{H}	\tilde{E}_T
T	E	\tilde{E}	H_T, \tilde{H}_T

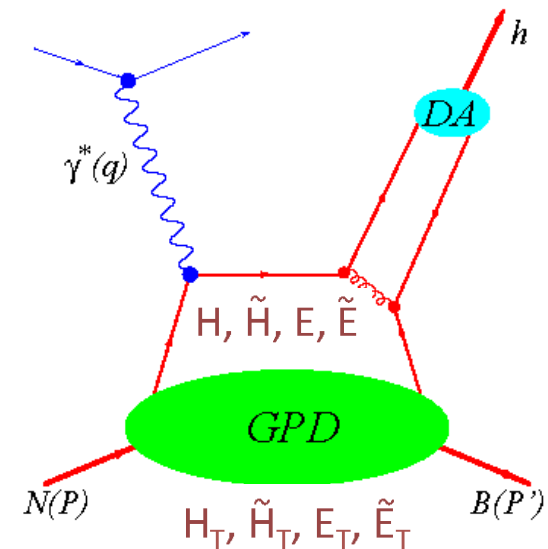
nucleon pol.

$$\bar{E}_T = 2\tilde{H}_T + E_T$$

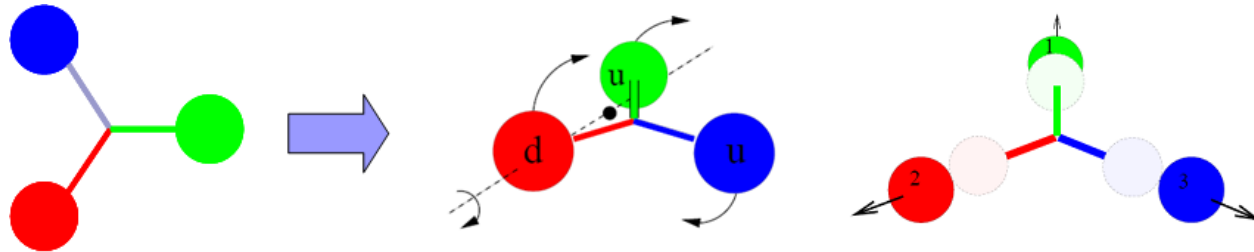
DVCS



DVMP



From the Ground State Nucleon to Resonances



How does the excitation affect the **3D structure** of the nucleon?

→ Pressure distributions, mass, tensor charge, ... of resonances?

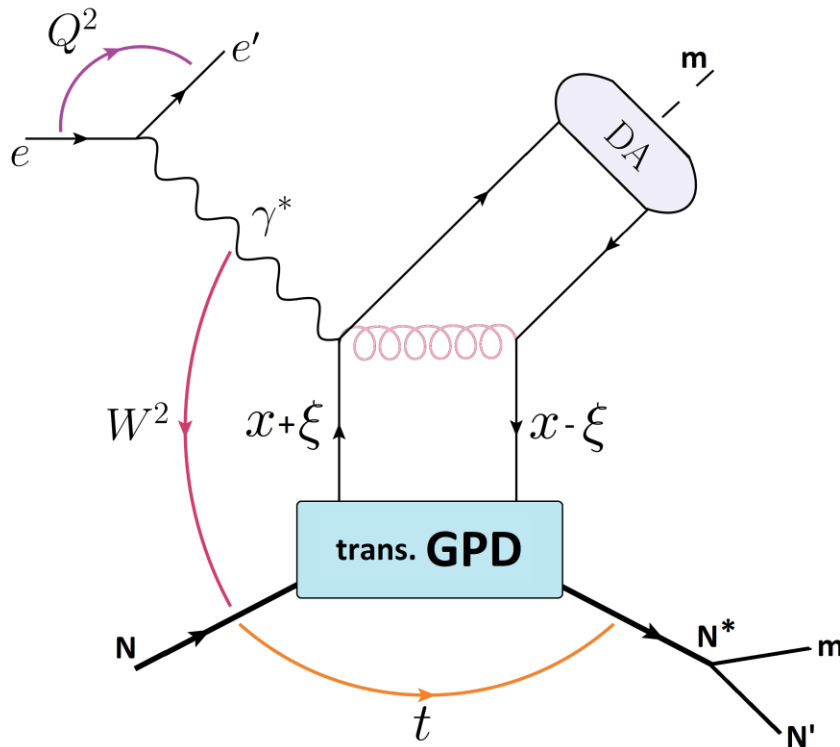
Traditional way: Study of transition form factors (**2D picture** of transv. position)

3D picture of the excitation process: Encoded in **transition GPDs**

Simplest case: $N \rightarrow \Delta$ transition → **16 transition GPDs**

- **8 helicity non-flip transition GPDs (twist 2)**
→ $N \rightarrow N^*$ DVCS
- **8 helicity flip transition GPDs (twist-3, transversity)**
→ $N \rightarrow N^*$ DVMP

The $N \rightarrow N^*$ DVMP processes



Factorisation expected for:

$$-t / Q^2 \ll 1, x_B \text{ fixed} \\ \text{and } Q^2 > M_{N^*}^2$$

$$ep \rightarrow eN^* m \rightarrow e(Nm_2)m_1$$

p \rightarrow Δ transition:

$$ep \rightarrow e\Delta^0 \pi^+ \rightarrow e(p\pi^-)\pi^+ \\ \rightarrow e(n\pi^0)\pi^+$$

$$ep \rightarrow e\Delta^+ \pi^0 \rightarrow e(n\pi^+)\pi^0 \\ \rightarrow e(p\pi^0)\pi^0$$

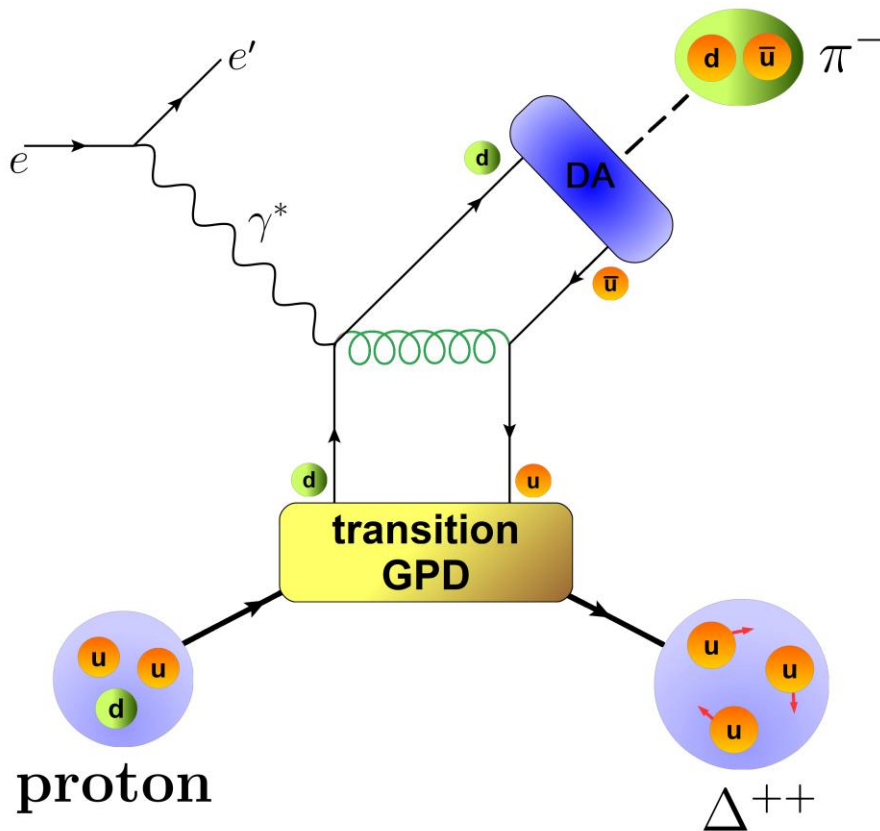
$$ep \rightarrow e\Delta^{++} \pi^- \rightarrow ep\pi^+ \pi^-$$

$$ep \rightarrow e\Delta^{++} \pi^- \rightarrow ep\pi^+ \pi^-$$

Hard Exclusive $\pi^-\Delta^{++}$ Electroproduction

$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow ep\pi^+\pi^-$$

$$I_z = +3/2$$



→ The $p\pi^+$ final state can **only** be populated by **Δ -resonances**

→ Large gap between $\Delta(1232)$ and higher resonances

→ Provides access to the **d-quark** content of the nucleon

→ Provides access to **p- Δ transition GPDs**

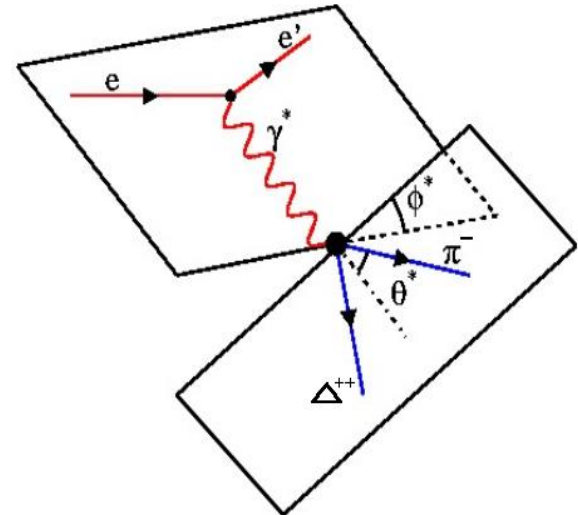
S. Diehl et al. (CLAS Collaboration), Phys. Rev. Lett. 131, 021901 (2023).

<https://doi.org/10.1103/PhysRevLett.131.021901>

Hard Exclusive π^- Electroproduction and BSA

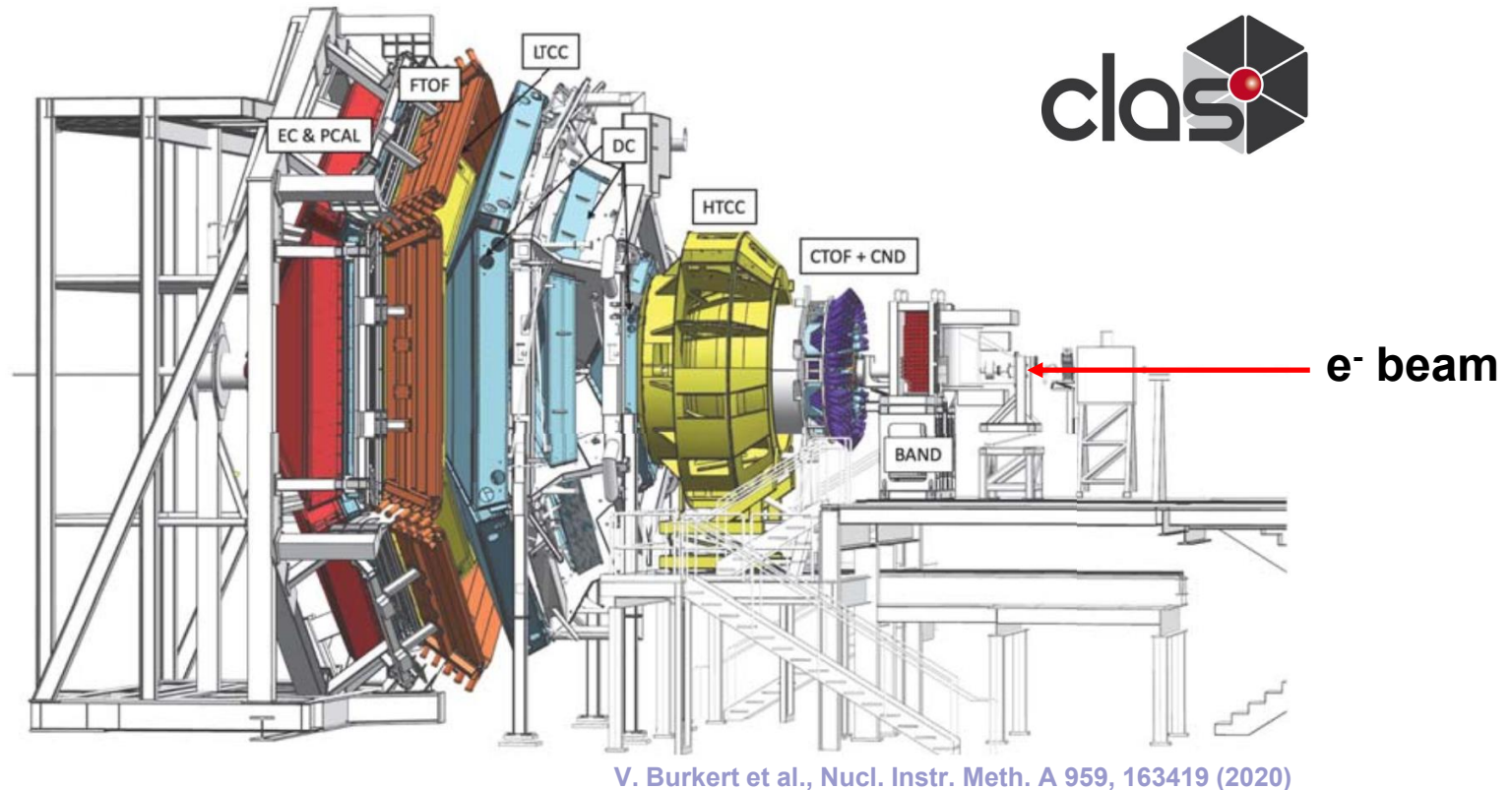
Cross section (longitudinally pol. beam and unpol. target):

$$\begin{aligned}
 2\pi \frac{d^2\sigma}{dt d\phi} &= \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \epsilon \cdot \cos(2\phi) \frac{d\sigma_{TT}}{dt} \\
 &\quad + \sqrt{2\epsilon(1+\epsilon)} \cdot \cos(\phi) \frac{d\sigma_{LT}}{dt} \\
 &\quad + h \cdot \sqrt{2\epsilon(1-\epsilon)} \cdot \sin(\phi) \frac{d\sigma_{LT'}}{dt}
 \end{aligned}$$



$$BSA(t, \phi, x_B, Q^2) = \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-} = \frac{\sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi}{1 + \sqrt{2\epsilon(1+\epsilon)} \frac{\sigma_{LT}}{\sigma_0} \cos \phi + \epsilon \frac{\sigma_{TT}}{\sigma_0} \cos 2\phi}$$

CLAS12 at JLAB



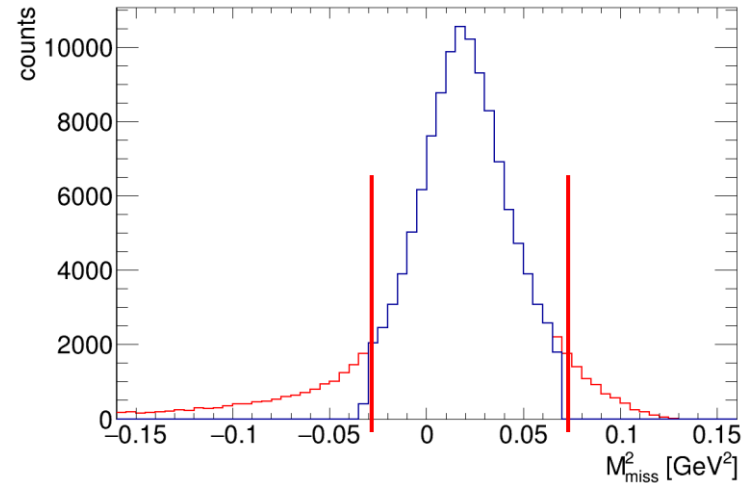
- ➔ Data recorded with CLAS12 during fall 2018 and spring 2019 (RG-A)
 - ➔ 10.6 GeV / 10.2 GeV electron beam ~ 86 % average polarization
 - ➔ liquid H₂ target

Event Selection and Kinematic Cuts

Event selection: $ep \rightarrow ep\pi^- X$

$$X = \pi^+$$

→ 2 sigma cut around the missing π^+



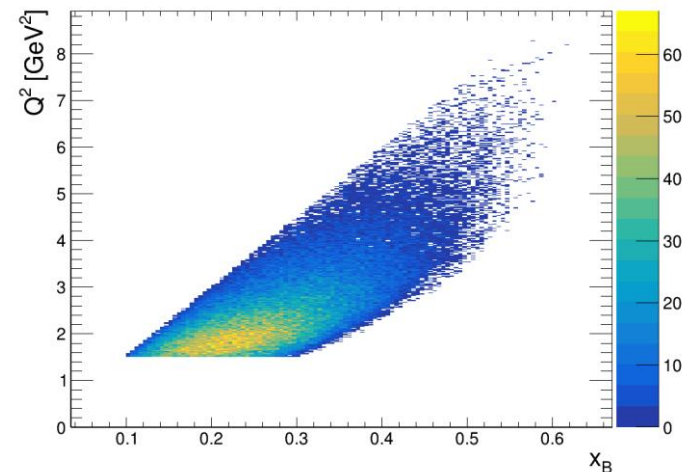
Kinematic cuts:

$$Q^2 > 1.5 \text{ GeV}^2$$

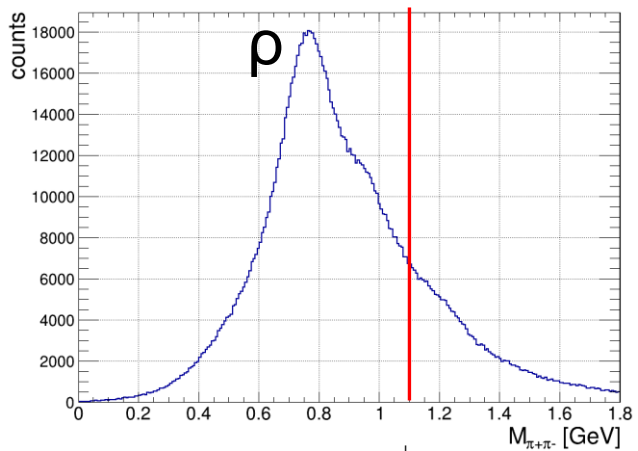
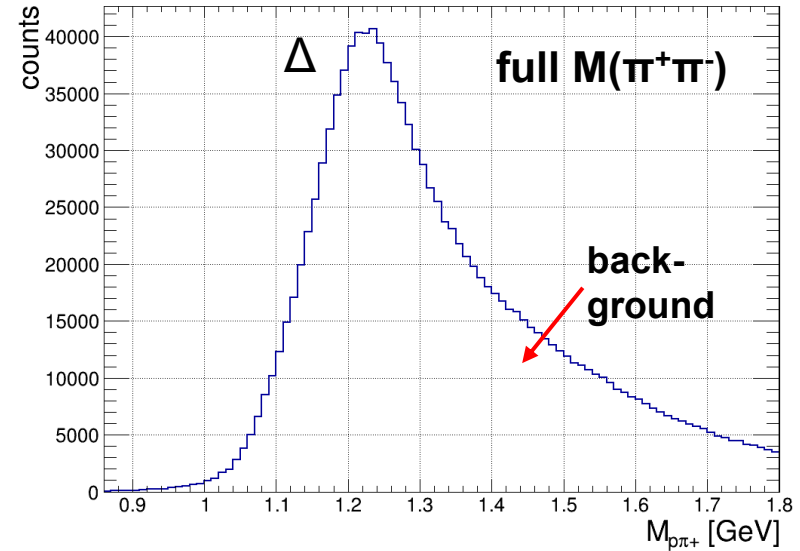
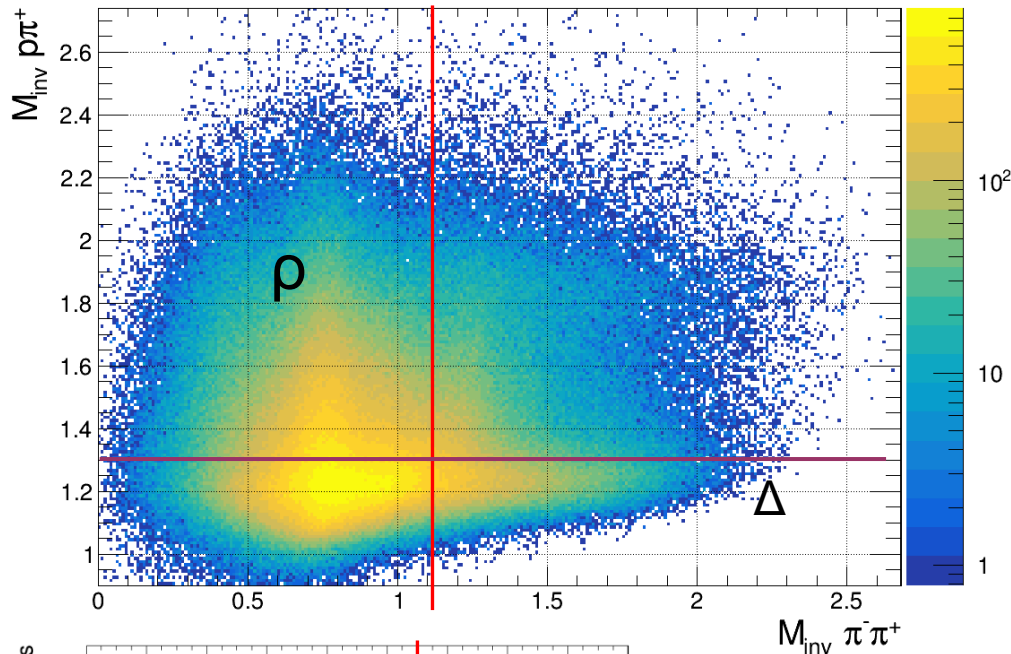
$$W > 2 \text{ GeV}$$

$$y < 0.75$$

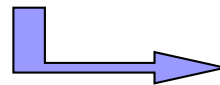
$$-t < 1.5 \text{ GeV}^2$$



Event Selection and Background Rejection

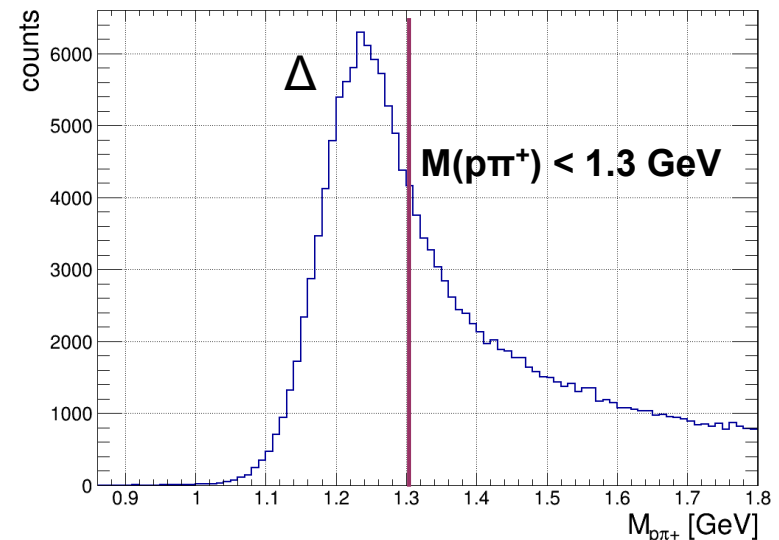


$M(\pi^+\pi^-) > 1.1$ GeV



ρ contamination

$< 0.8\%$



$M(p\pi^+) < 1.3$ GeV

$ep \rightarrow ep\rho \rightarrow ep\pi^+\pi^-$

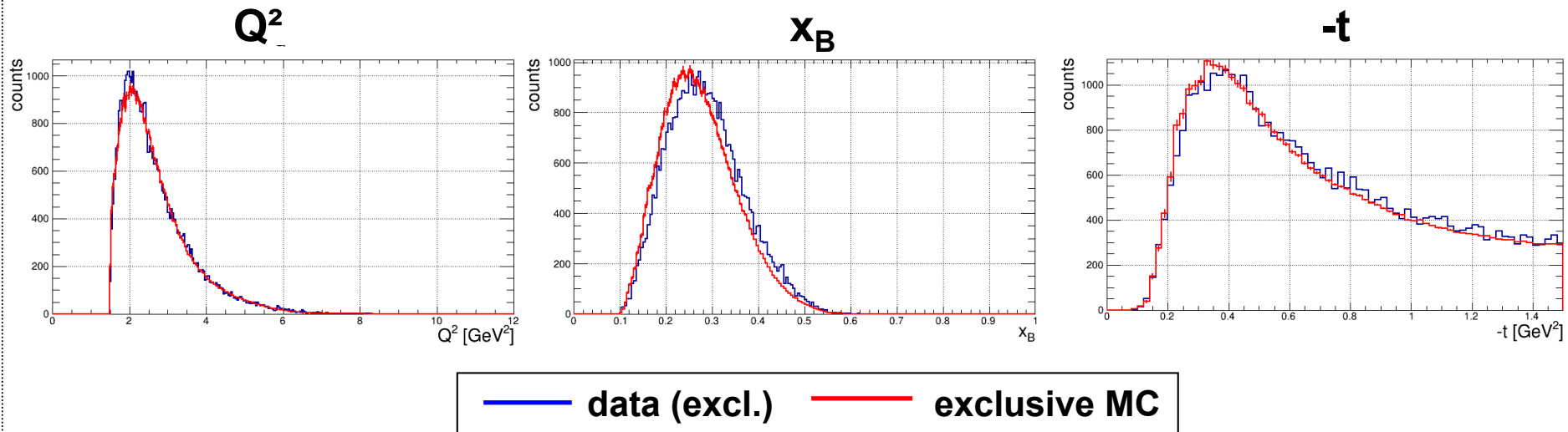
Monte Carlo Simulations

Background: Full deep inelastic scattering MC

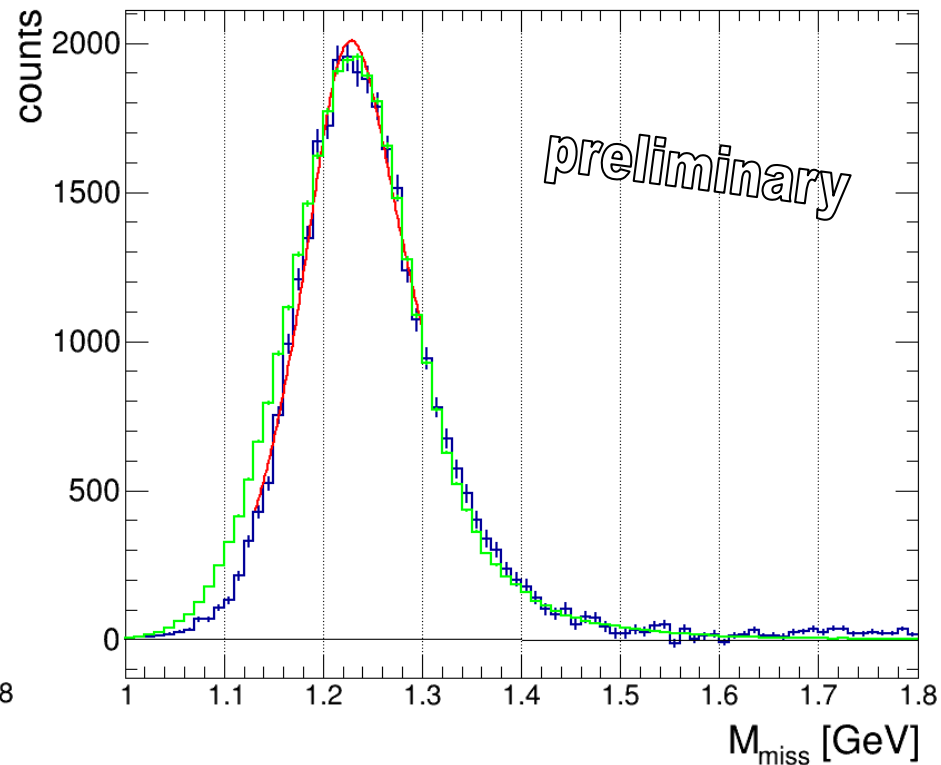
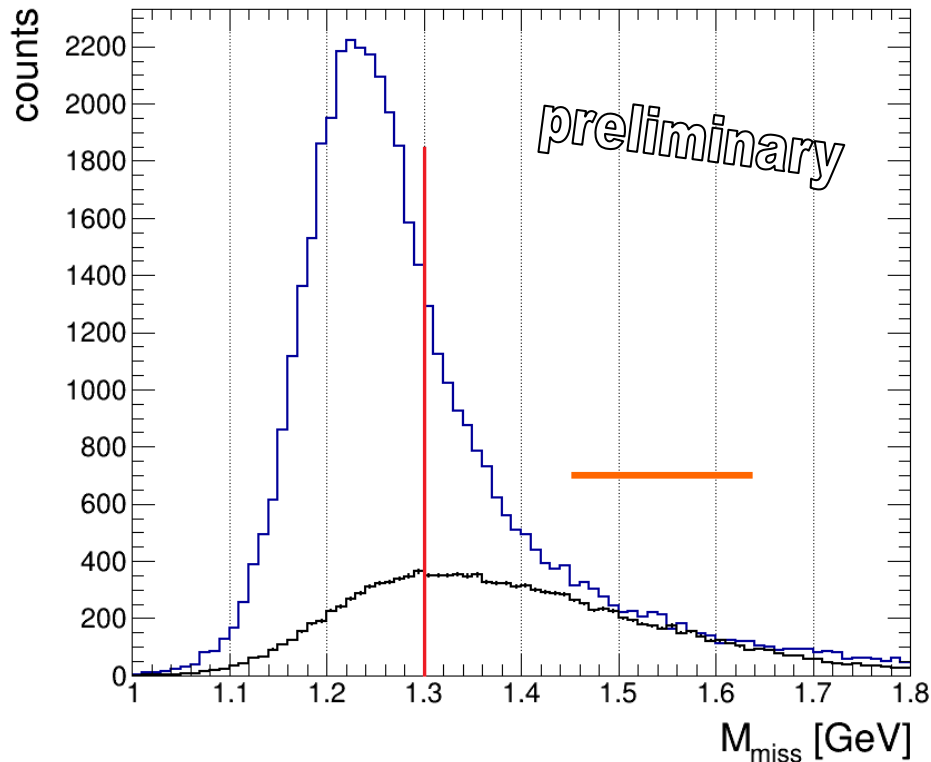
- Does not contain the exclusive $\pi\Delta^{++}$ production in the GPD regime ($-t < 1.5 \text{ GeV}^2$)
- Contains non-resonant background as well as ρ production and other potential background channels

Signal: Exclusive $\pi\Delta^{++}$ MC

- Phase space simulation with a weight added to match the experimental data
- Δ peak with PDG mass and FWHM



Event Selection and Background Estimate



— experimental data

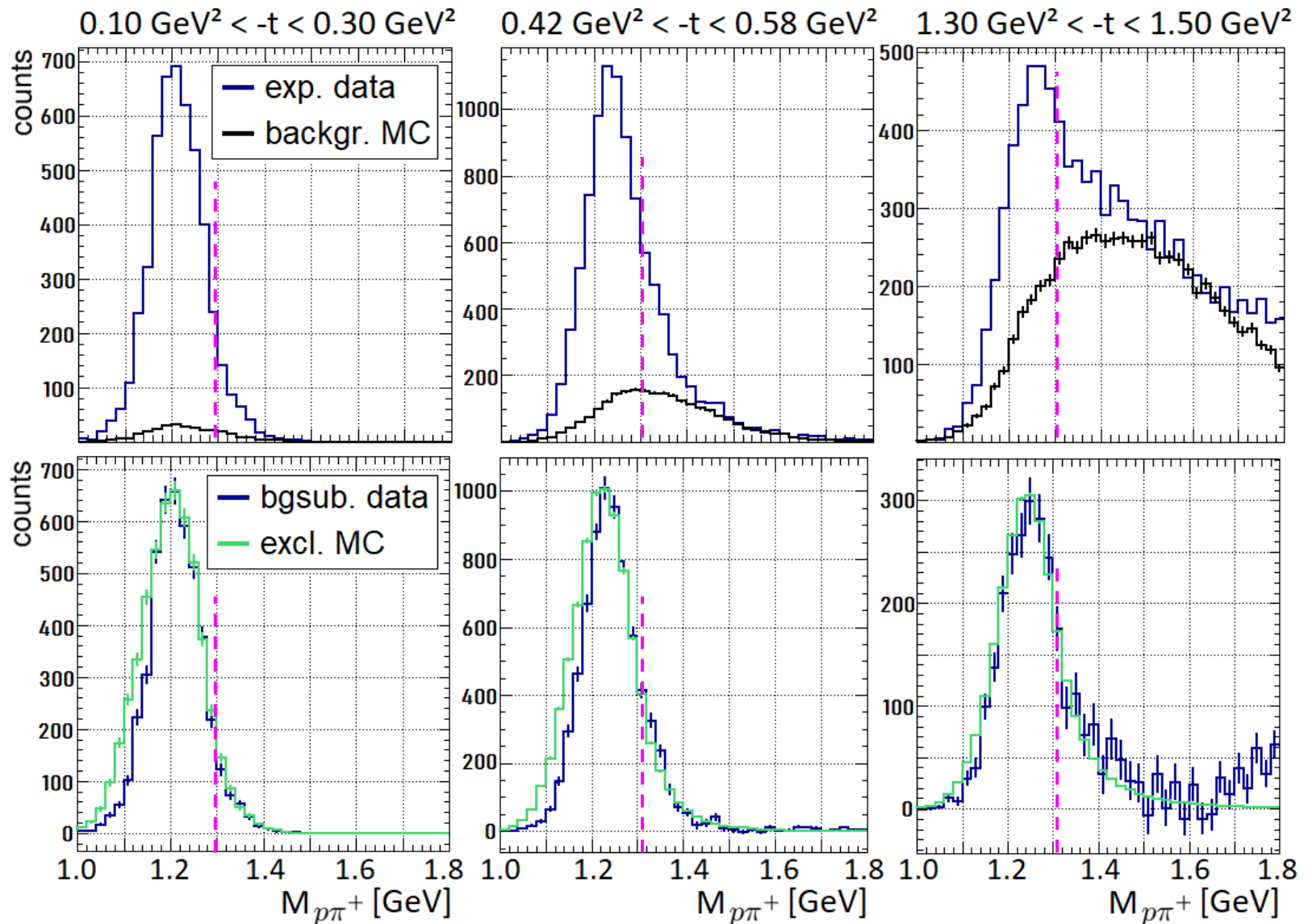
— SIDIS MC (same cuts)

— data after SIDIS MC subtraction

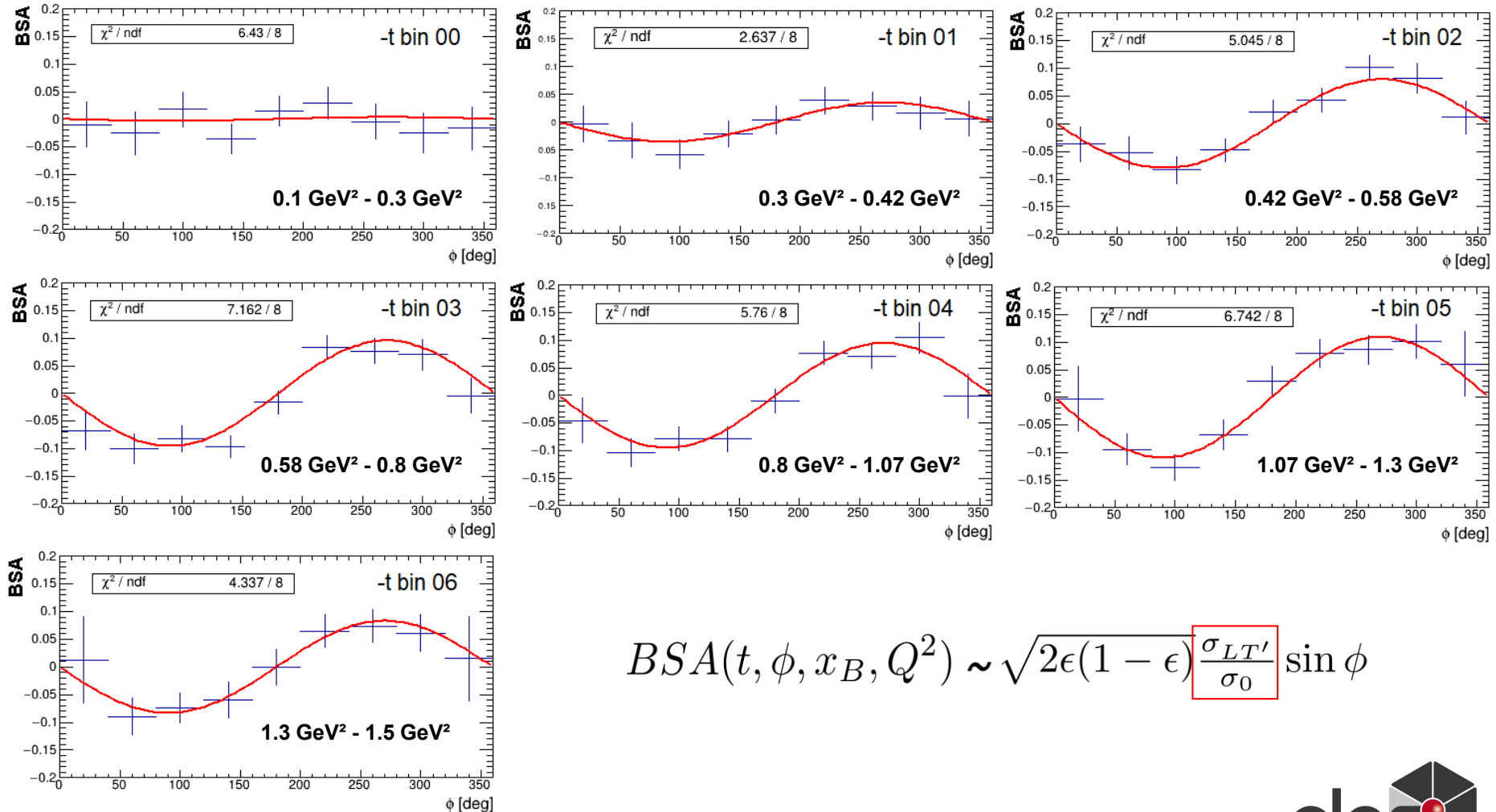
— fit of a Sill function (BW with thr. effects)

— exclusive MC (for comparison)

Signal and Background Separation



Resulting Beam Spin Asymmetries (Q^2 - x_B integrated)



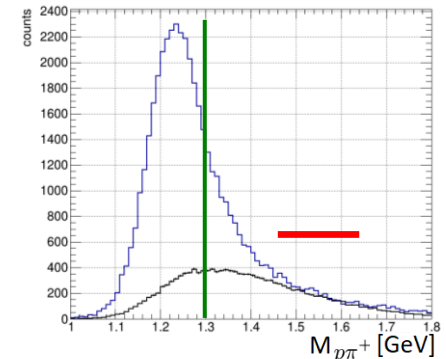
$$BSA(t, \phi, x_B, Q^2) \sim \sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi$$



Background Subtraction

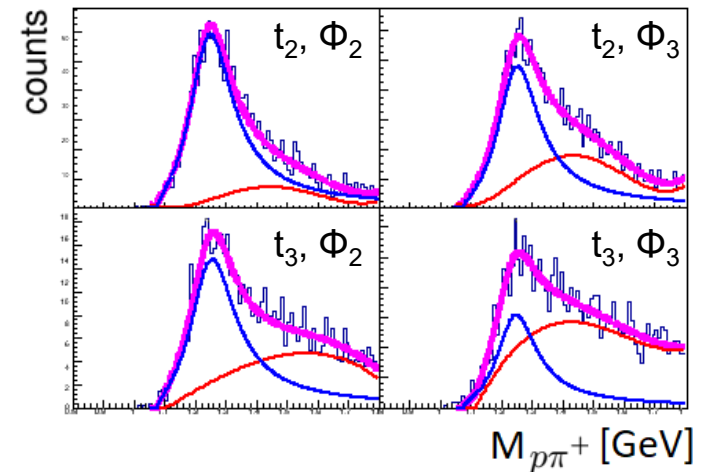
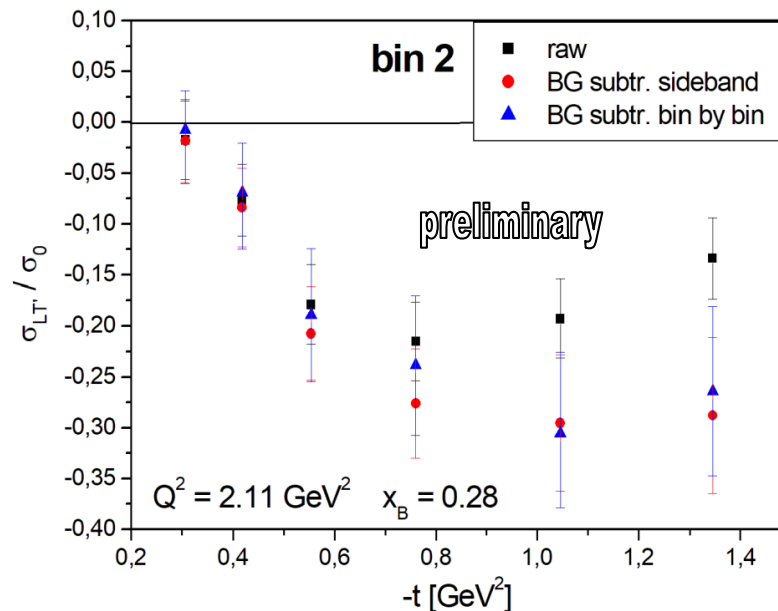
Method 1: A sideband based background subtraction

- S/B ratio from a fit of the signal shape and background asymmetry from the sideband



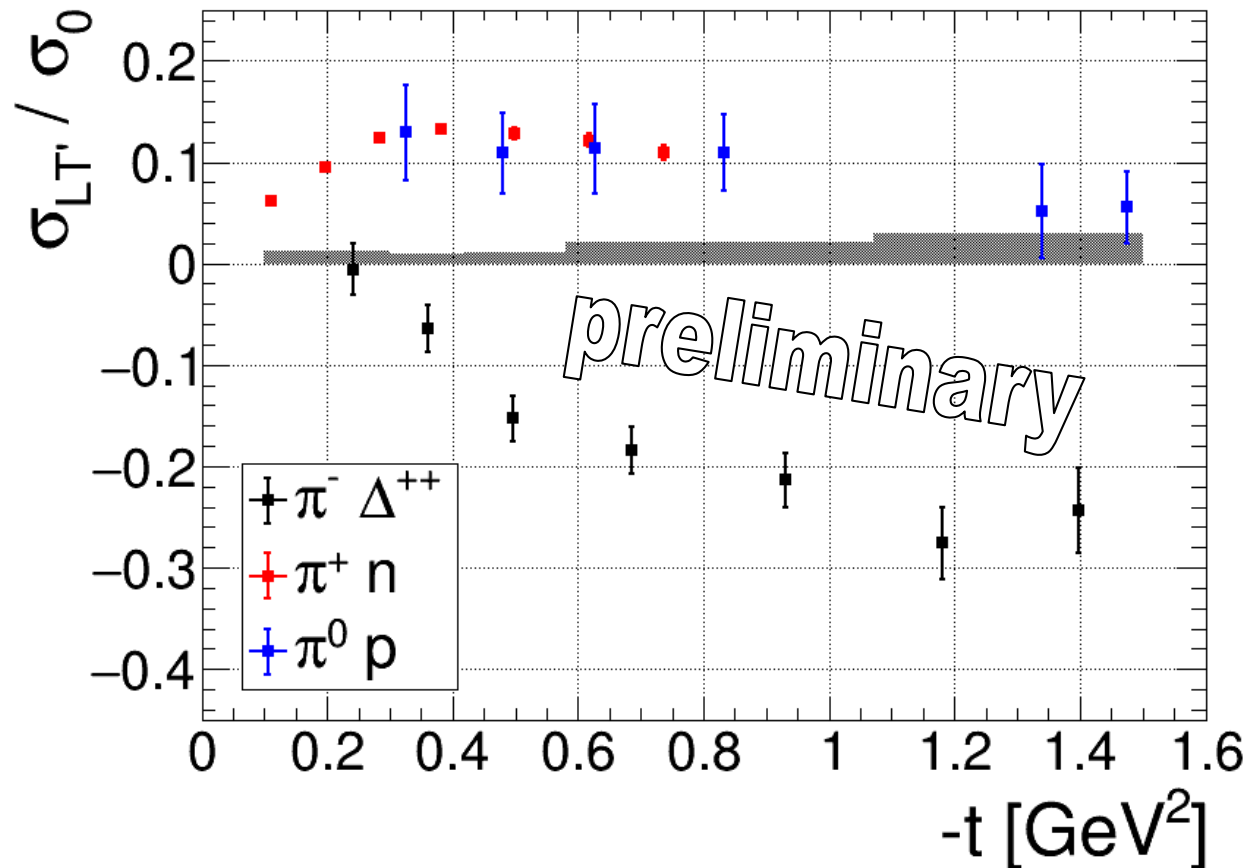
Method 2: A bin-by-bin background subtraction

- Fit of the $p\pi^+$ inv. mass with a „Sill“ function and a 5th order polynomial in each Q^2 , x_B , $-t$, Φ bin.



$Q^2 - x_B$ Integrated Result

$$\langle Q^2 \rangle = 2.48 \text{ GeV}^2, \langle x_B \rangle = 0.27$$

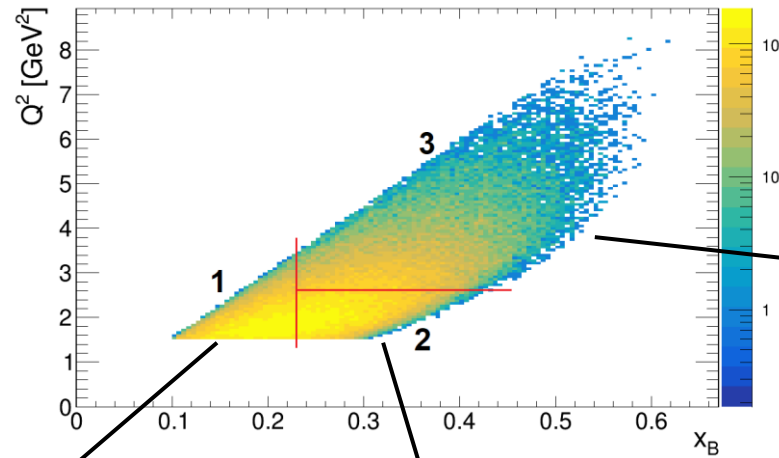


Different sources of systematic uncertainty have been studied:
 beam polarisation, background subtraction, fiducial volume, extraction method,
 acceptance, bin migration, radiative effects

Multidimensional Results



S. Diehl et al. (CLAS Collaboration),
 Phys. Rev. Lett. 131, 021901 (2023).
<https://doi.org/10.1103/PhysRevLett.131.021901>

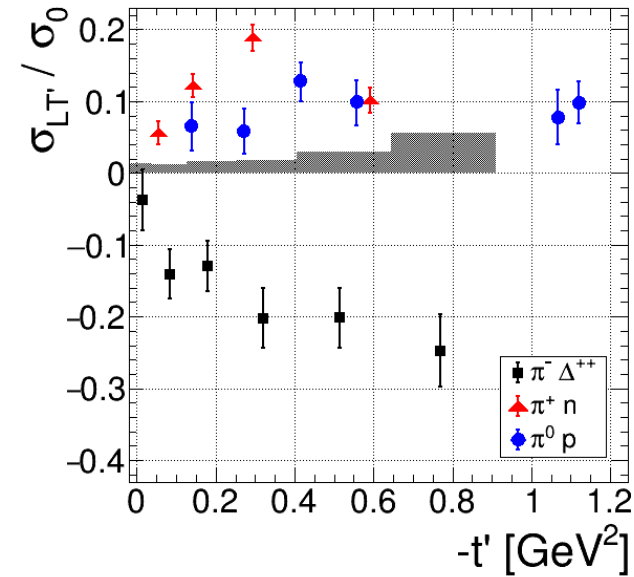
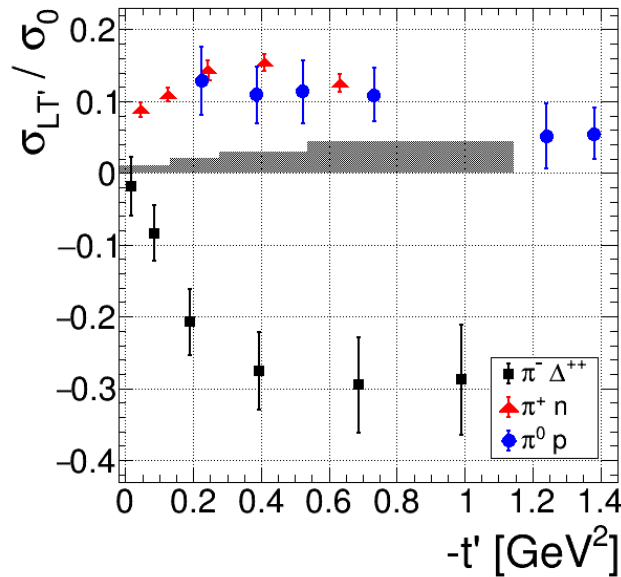
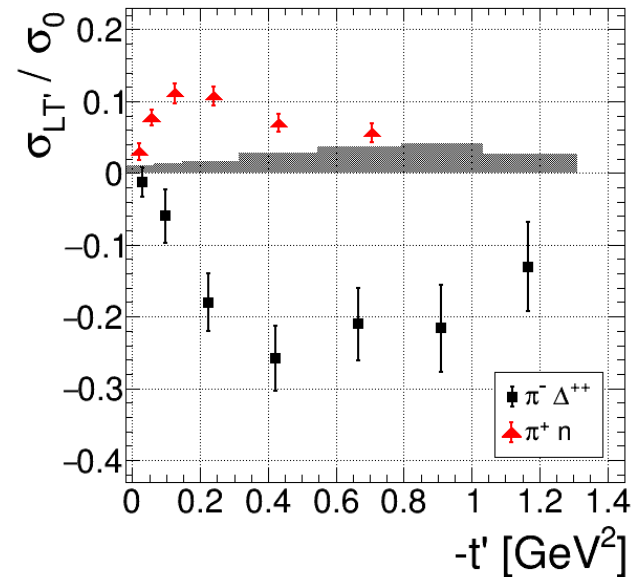


proton (uud)
 \rightarrow neutron (udd)
 π^+ ($|u\bar{d}\rangle$)
 $\rightarrow \Delta^{++}$ (uuu)
 π^- ($|d\bar{u}\rangle$)

bin 1 ($\langle Q^2 \rangle = 1.95 \text{ GeV}^2$, $\langle x_B \rangle = 0.19$)

bin 2 ($\langle Q^2 \rangle = 2.11 \text{ GeV}^2$, $\langle x_B \rangle = 0.28$)

bin 3 ($\langle Q^2 \rangle = 3.38 \text{ GeV}^2$, $\langle x_B \rangle = 0.34$)



Physics Content of the Observable

Theoretical description of the process:

P. Kroll, K. Passek-Kumericki, Phys. Rev. D **107**, 054009 (2023).

see talk by Peter Kroll

~ helicity non-flip transition GPDs \tilde{G}_3 and \tilde{G}_4

$$\sigma_{LT'} \sim \sqrt{-t'} \Im \left[G_{T_5}^3 \cdot A + c G_{T_7}^3 \cdot A' \right]$$

helicity flip transition GPDs

$$G_{T_5}^{(3)} + \frac{1}{2} G_{T_7}^{(3)} = -\frac{3}{2} (H_T^u - H_T^d)$$

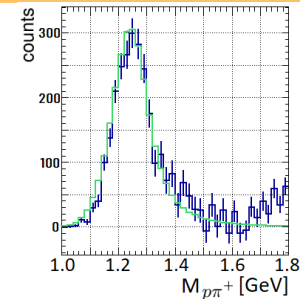
→ tensor charge of the proton / resonance: $\delta_T^u = \int dx H_T^u(x, \xi, t = 0)$

Extension to Other DVMP Channels / Why is $\pi^-\Delta^{++}$ Special?

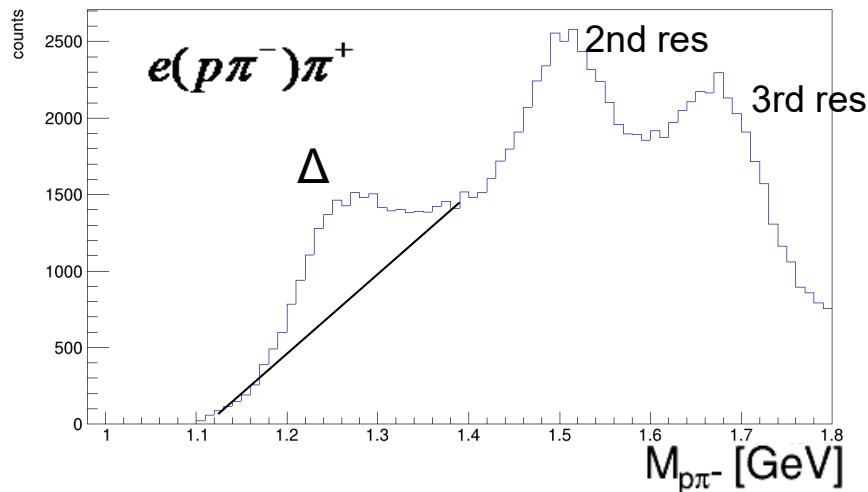
$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow ep\pi^+\pi^-$$

→ The $p\pi^+$ final state can **only** be populated by **Δ -resonances**

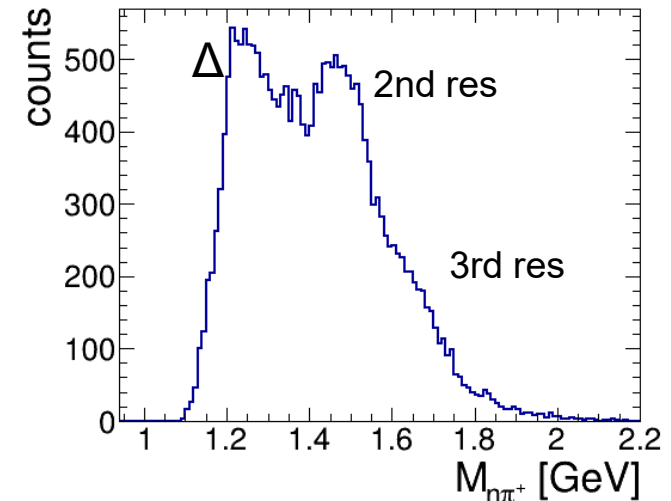
→ Large gap between $\Delta(1232)$ and higher resonances



$$ep \rightarrow e\Delta^0\pi^+ \rightarrow e(p\pi^-)\pi^+ \quad | \quad \rightarrow e(n\pi^0)\pi^+$$



$$\gamma^* p \rightarrow N^* \gamma \rightarrow p \text{ meson } \gamma$$

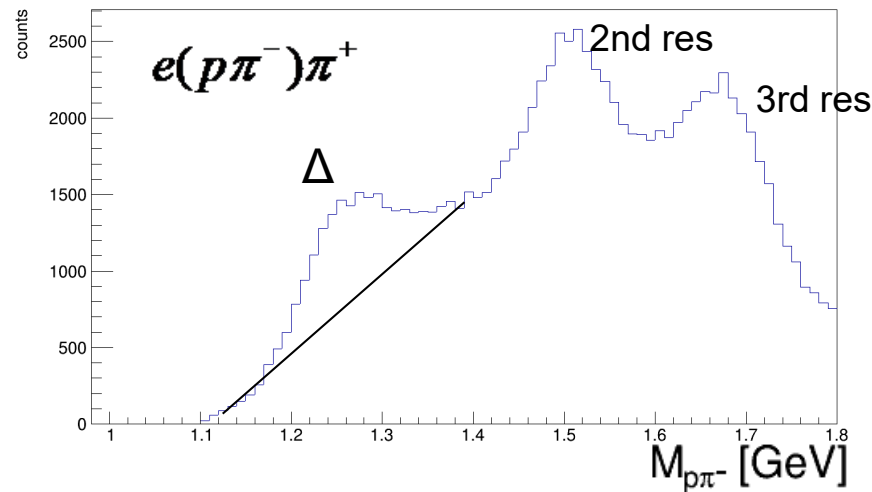


Similar picture for: $ep \rightarrow e\Delta^+\pi^0 \rightarrow e(n\pi^+)\pi^0 \quad | \quad \rightarrow e(p\pi^0)\pi^0$

→ The resonances for all cases have isospin $I_z = \pm 1/2$ → **N and Δ resonances possible!**

Discussion: Extension to other DVMP channels

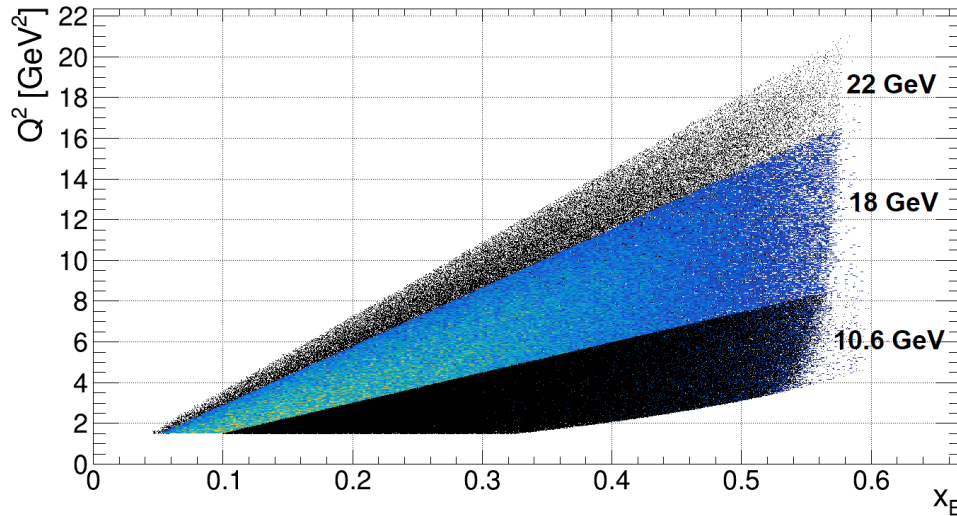
$$ep \rightarrow e\Delta^0\pi^+ \rightarrow e(p\pi^-\pi^+ | \rightarrow e(n\pi^0)\pi^+$$



→ Access to higher resonances?

→ Full fit? PWA?

Perspectives for a 22 GeV JLAB Upgrade



Better signal / background separation

→ Higher efficiency

Transition GPDs are part of the science program for a 22 GeV JLAB upgrade:

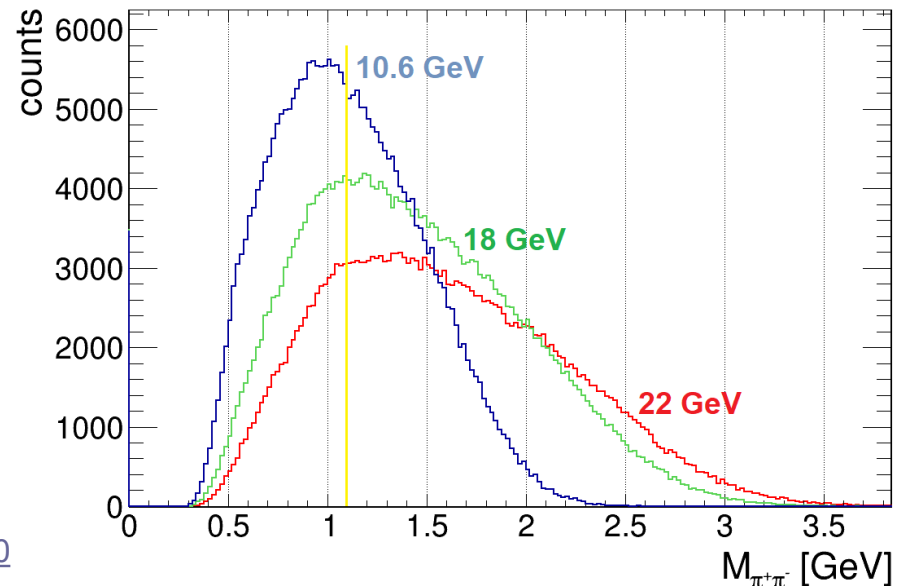
A. Accardi, P. Achenbach, D. Adhikari et al., Strong Interaction Physics at the Luminosity Frontier with 22 GeV Electrons at Jefferson Lab (2023). <https://doi.org/10.48550/arXiv.2306.09360>

$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow ep\pi^+\pi^-$$

$$ep \rightarrow e\Delta^+\gamma \rightarrow en\pi^+\gamma$$

Extended Q^2 range

→ Advantage for factorisation



Conclusion and Outlook

- Transition GPDs can help us to better understand the 3D structure of resonances and the excitation process itself.
- Hard exclusive $\pi\Delta^{++}$ production can be well measured with CLAS12
- The extracted $\pi\Delta^{++}$ BSA is a first published observable sensitive to $p\rightarrow\Delta$ transition GPDs
- Next steps: Extract A_{LL} from the $\pi\Delta^{++}$ process based on CLAS12 RG-C
→ Theory predictions exist! (Kroll et al.)
- A JLAB energy and luminosity upgrade will help to significantly improve these measurements and the extraction of transition GPDs
- Feasibility studies with COMPASS / AMBER are planned