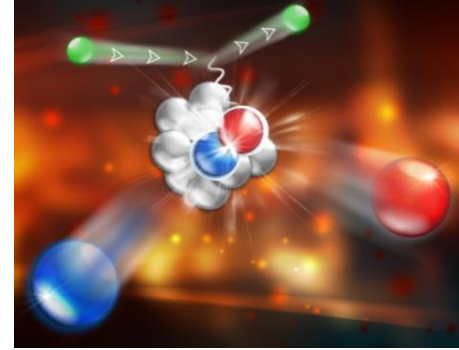
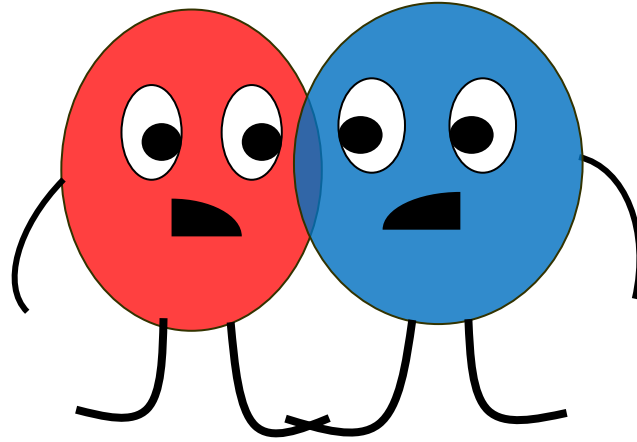
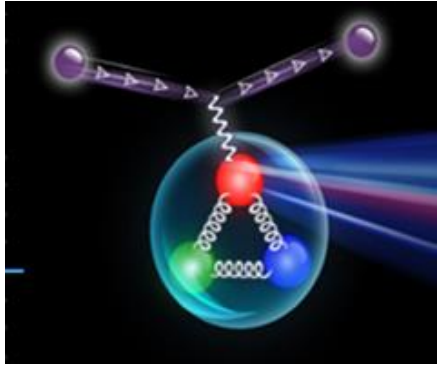


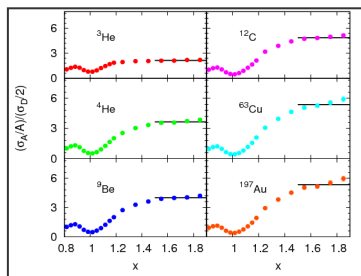
# Inclusive Data Overview



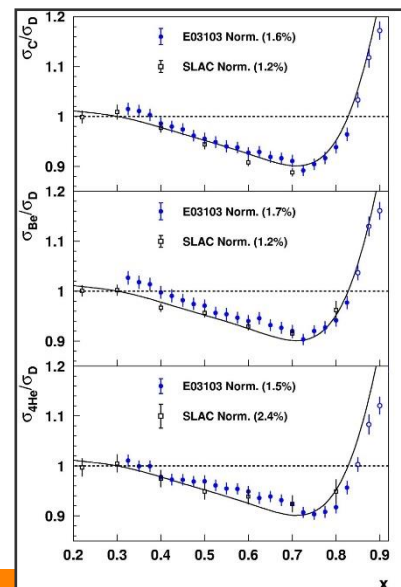
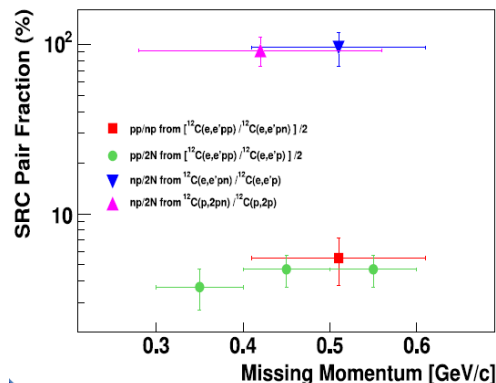
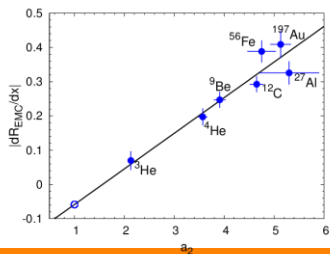
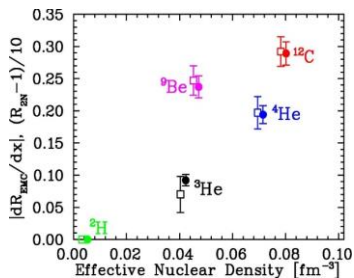
Nadia Fomin

July 17, 2023

# What have we learned from Jlab's 6GeV era?



- Scaling of  $x > 1$  cross sections relative to the deuteron
  - implies high momentum tail is a result of short-range correlations
- NP dominance of short-range pairs
  - tensor interaction
- No trivial ( $A$  or density) dependence for SRC behavior or EMC effect
  - from high-precision light nuclei data
- Suggestive correlation between EMC effect and SRC plateaus

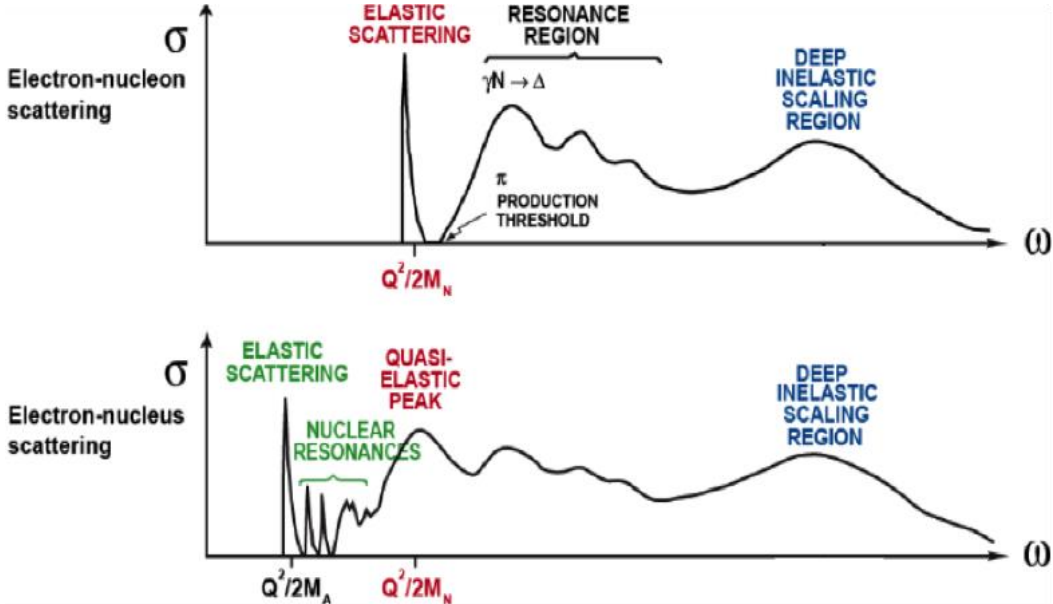


THE END

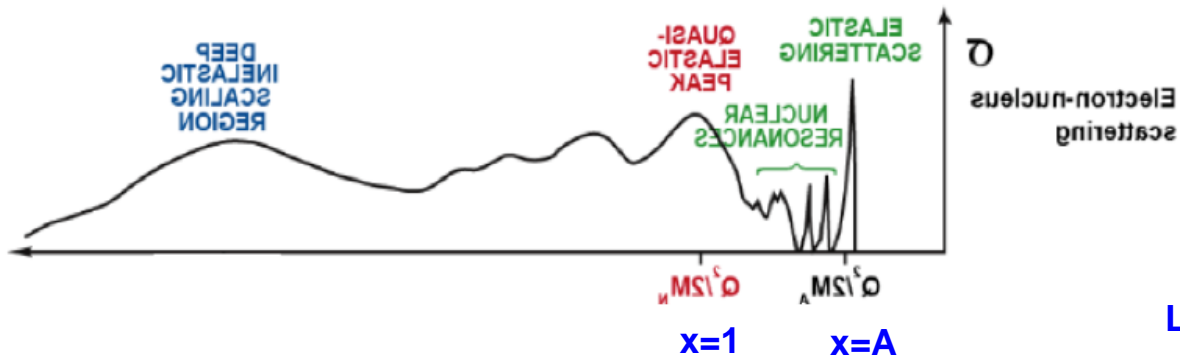
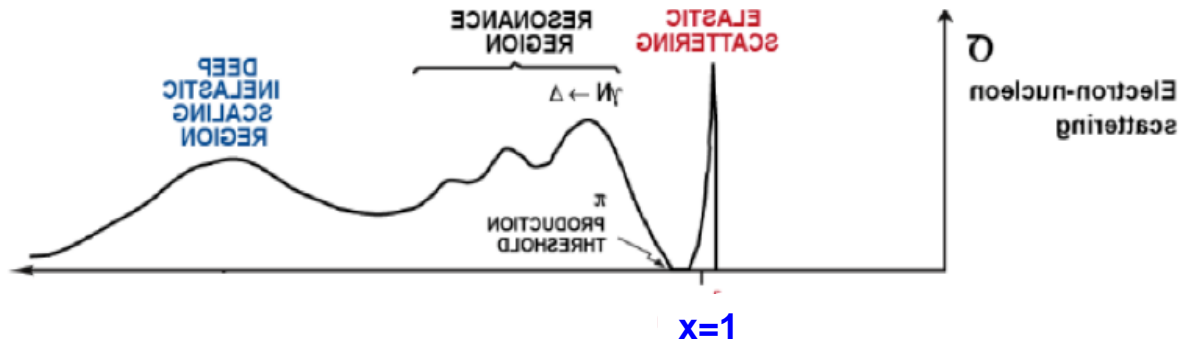
# Choosing an Appropriate Microscope



$$\lambda \approx \frac{1}{q}$$



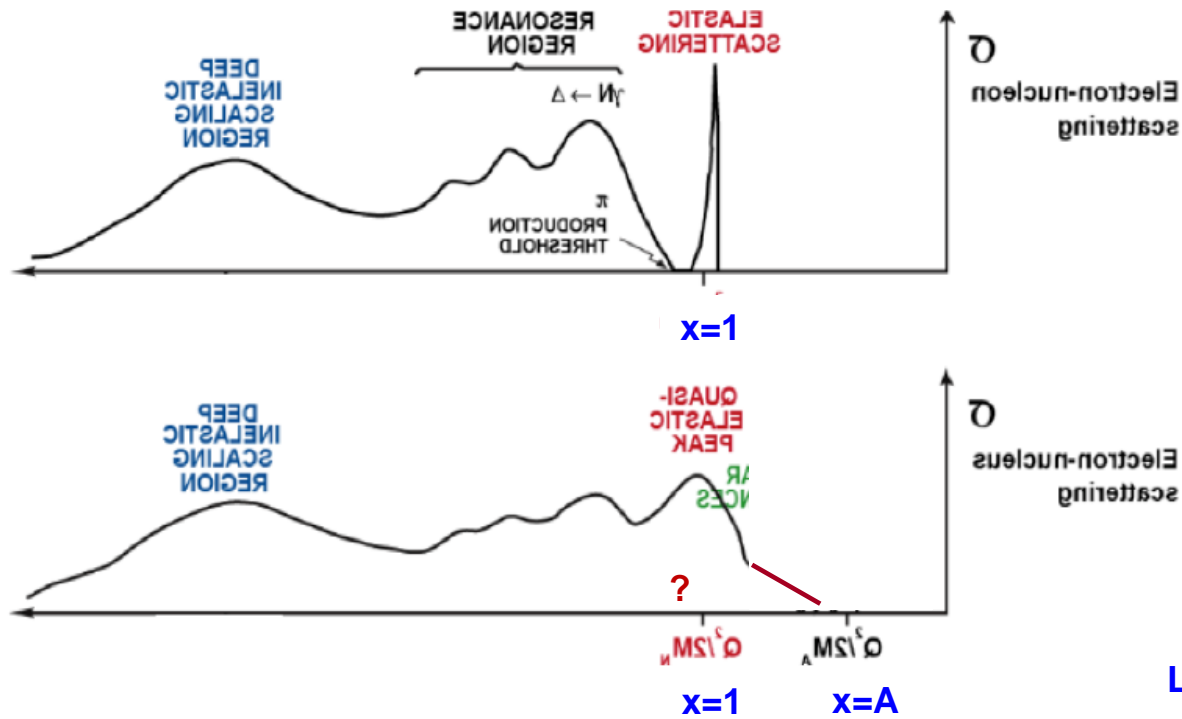
# Choosing an Appropriate Microscope



Log-ish( $x_{Bj}$ )  
Log-ish( $x_{Bj}$ )

$1 < x < 2$  is combination of 2-body and 1\*-body contributions; 3+ body effect assumed to be small (\*=Fermi-smear)

# Choosing an Appropriate Microscope



Log-ish( $x_{Bj}$ )

$1 < x < 2$  is combination of 2-body and 1\*-body contributions; 3+ body effect assumed to be small (\*=Fermi-smear)

# High momentum tails in $A(e,e'p)$

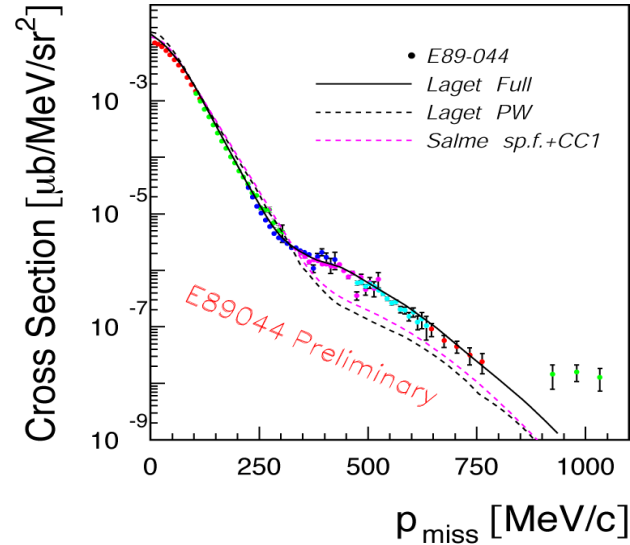
- E89-004: Measure of  ${}^3\text{He}(e,e'p)d$
- Measured far into high momentum tail:  
Cross section is  $\sim 5\text{-}10\times$  expectation

## Difficulty

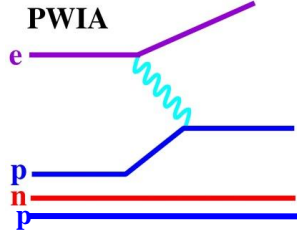
- High momentum pair can come from SRC (initial state)

OR

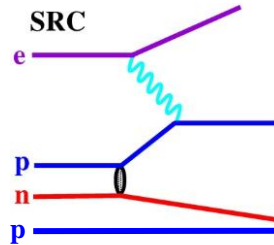
- Final State Interactions (FSI) and Meson Exchange Contributions (MEC)



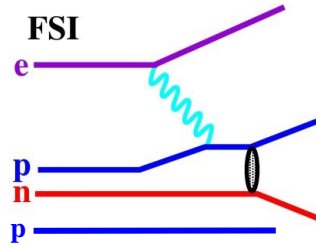
“slow”  
nucleons



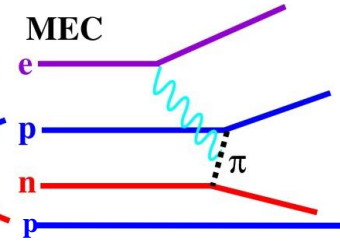
“fast” nucleons



**FSI**



**MEC**



# $A(e,e'p)$

$^2\text{H}(e,e'p)$  Mainz  
PRC 78 054001 (2008)

$E = 0.855$  GeV  
 $\theta = 45^\circ$   
 $E' = 0.657$  GeV  
 $Q^2 = 0.33$  GeV $^2$   
 $x = 0.88$

Unfortunately: FSI, MECs overwhelm the high momentum nucleons

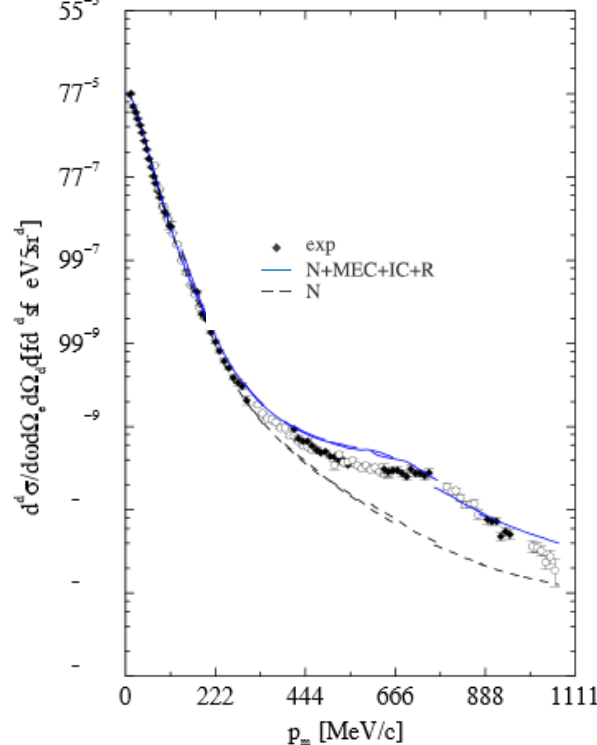


FIG. 1: The experimental  $D(e,e'p)n$  cross section as a function of missing momentum measured at MAMI for  $Q^2 = 0.33$  (GeV/c) $^2$  [4] compared to calculations [5] with (solid curve) and without (dashed curve) MEC and IC. Both calculations include FSI. The low  $p_m$  data have been re-analyzed and used in this work to determine  $f_{LT}$  (color online).



# Inclusive Scattering

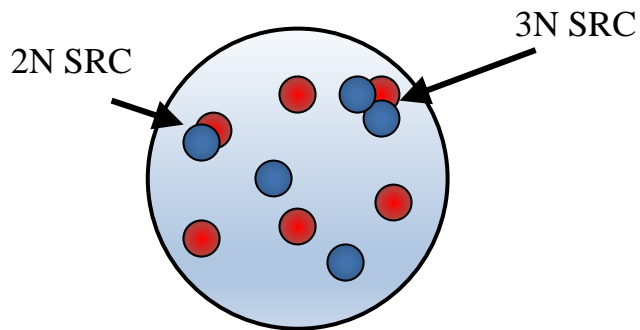
- Relative measurement
- Reduced FSI
- Test scaling in  $x$  and  $Q^2$
- No direct information on isospin structure
  - Only via target isospin structure
- No direct information on momentum distribution for  $A > 2$

# Inclusive Scattering

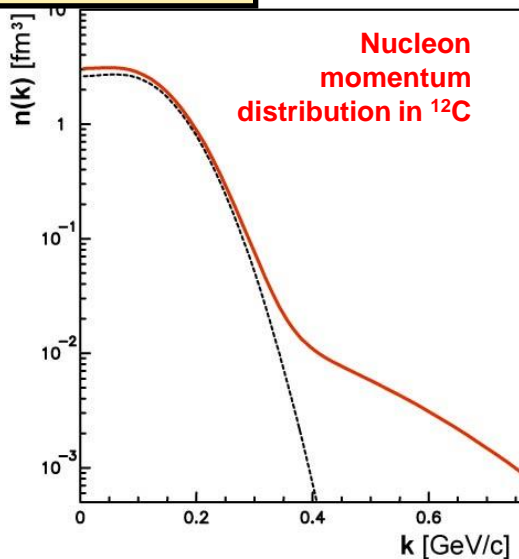
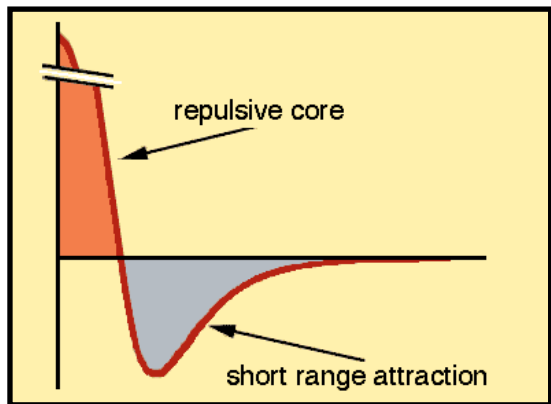
- Relative measurement
- **Reduced FSI**
- Test scaling in  $x$  and  $Q^2$
- No direct information on isospin structure
  - Only via target isospin structure
- No direct information on momentum distribution for  $A > 2$

# High momentum nucleons

- Short Range Correlations



Try inclusive scattering!  
Select kinematics such that the initial  
nucleon momentum  $> k_f$



# High momentum nucleons - Short Range Correlations

$$\frac{d\sigma^{QE}}{d\Omega dE'} \propto \int d\vec{k} \int dE \sigma_{ei} S_i(k, E) \delta(\text{Arg})$$

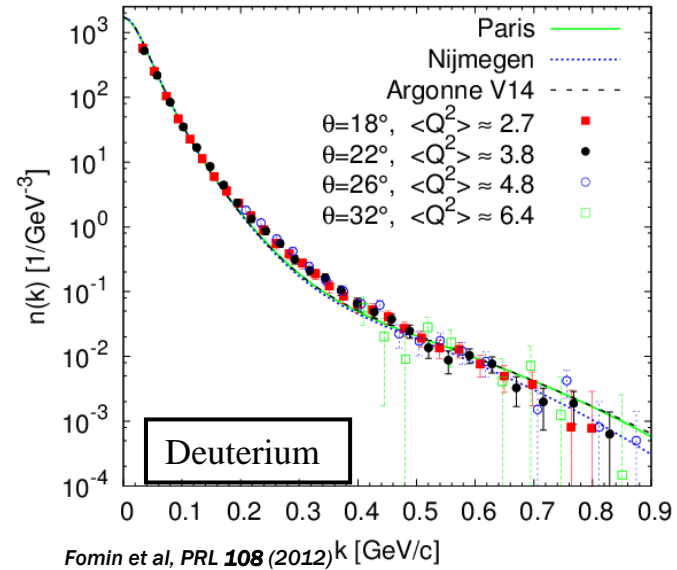
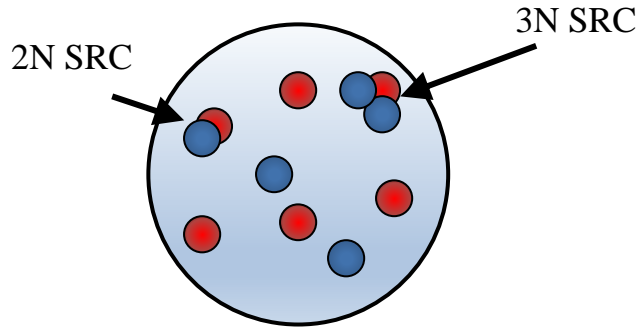
$$\text{Arg} = \nu + M_A - \sqrt{M^2 + p^2} - \sqrt{M_{A-1}^{*2} + k^2}$$



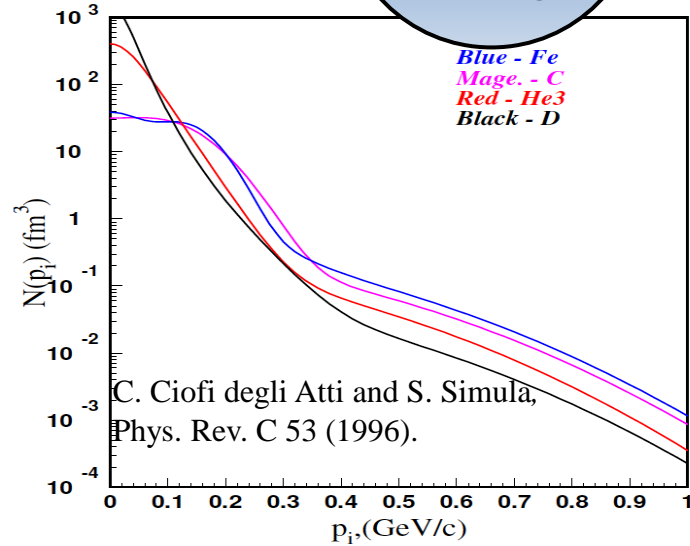
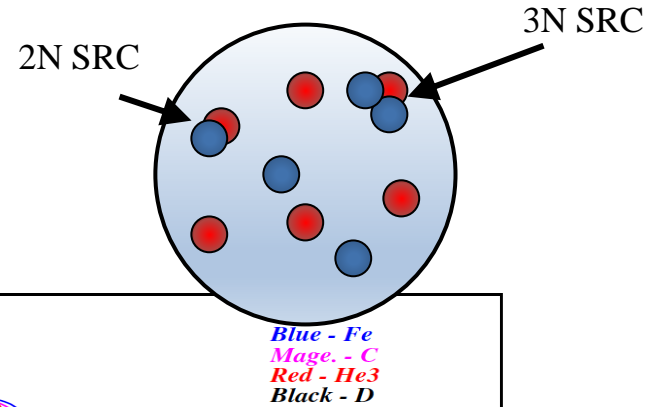
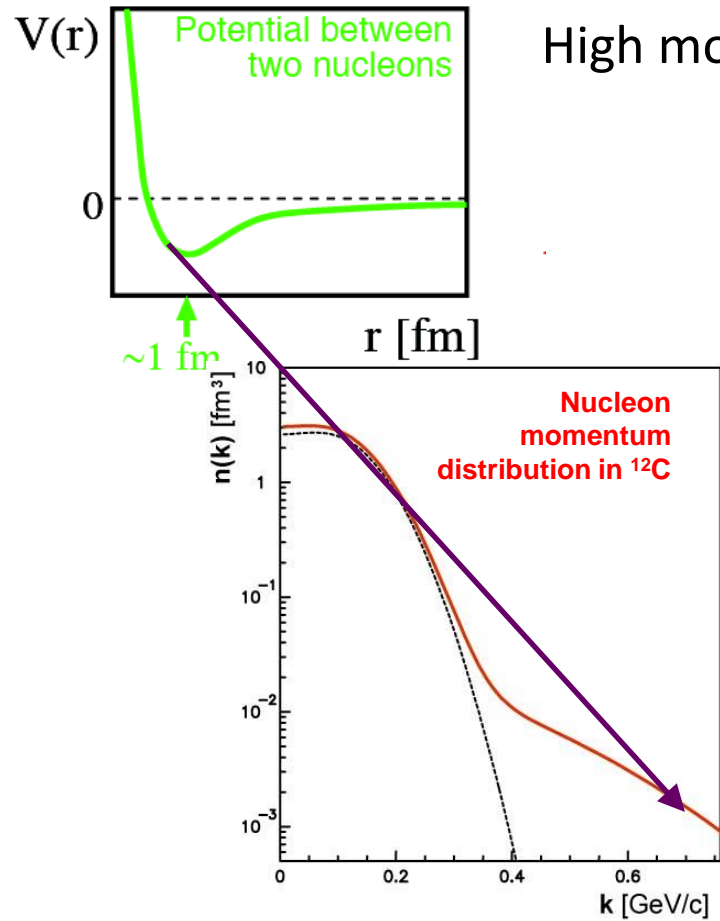
$$F(y, \mathbf{q}) = \frac{d^2\sigma}{d\Omega d\nu} \frac{1}{(Z\sigma_p + N\sigma_n)} \frac{\mathbf{q}}{\sqrt{M^2 + (y+q)^2}}$$

$$= 2\pi \int_0^\infty n(k) k dk$$

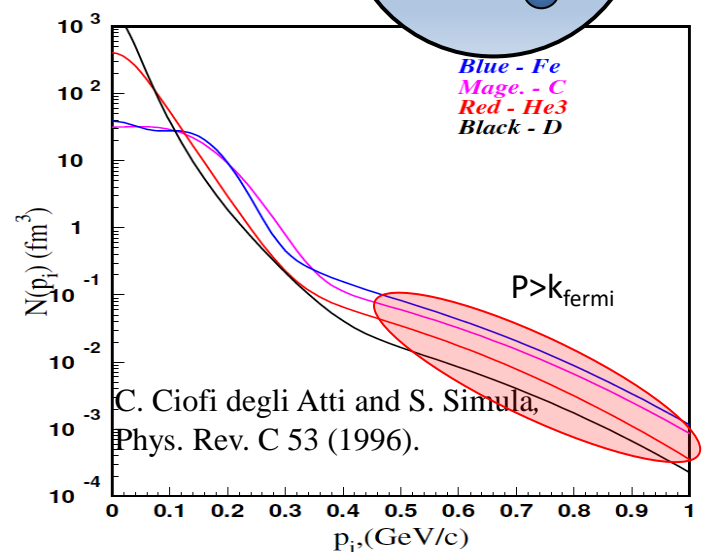
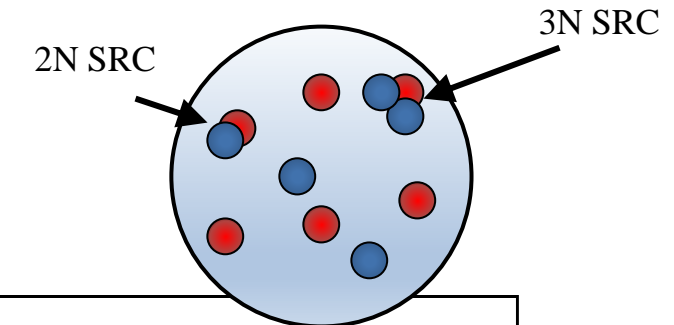
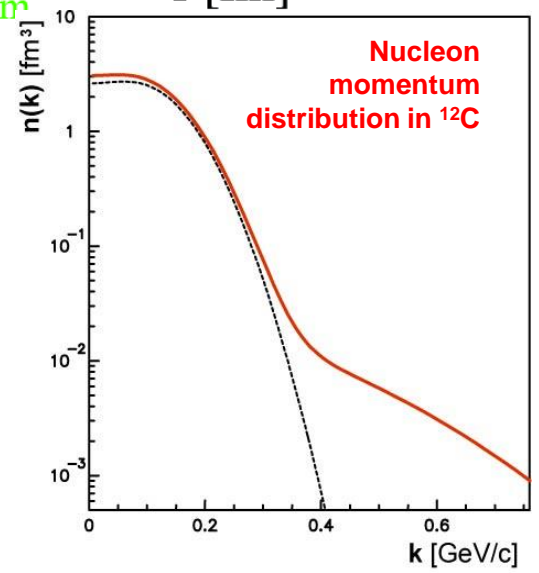
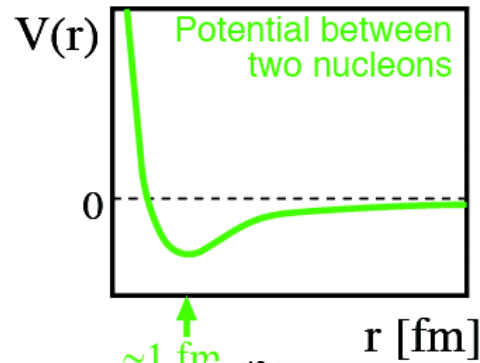
**Ok for  
A=2**



# High momentum nucleons - Short Range Correlations



# High momentum nucleons - Short Range Correlations

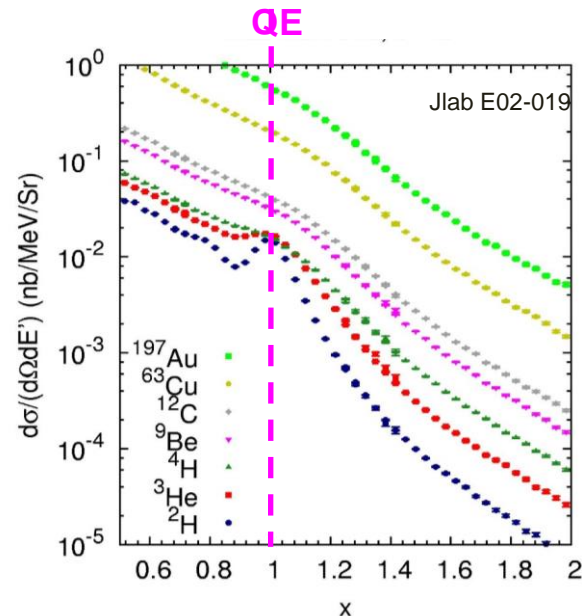


# Short Range Correlations

- To experimentally probe SRCs, must be in the high-momentum region ( $x > 1$ )
- To measure the relative probability of finding a correlation, ratios of heavy to light nuclei are taken
- In the high momentum region, FSIs are thought to be confined to the SRCs and therefore, cancel in the cross section ratios

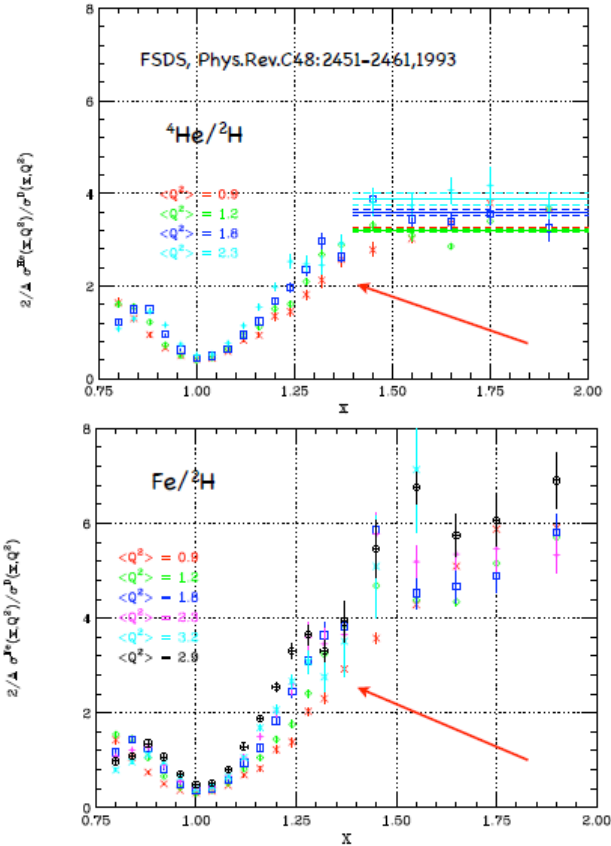
$$\begin{aligned}\sigma(x, Q^2) &= \sum_{j=1}^A A \frac{1}{j} a_j(A) \sigma_j(x, Q^2) \\ &= \frac{A}{2} a_2(A) \sigma_2(x, Q^2) + \\ &\quad \frac{A}{3} a_3(A) \sigma_3(x, Q^2) + \dots\end{aligned}$$

$$\frac{2}{A} \frac{\sigma_A}{\sigma_D} = a_2(A)$$



**1.4 < x < 2 => 2 nucleon correlation**

# 20<sup>th</sup> Century Data



- Moderate  $Q^2$  data from SLAC
- Originally analyzed in the  $y$ -scaling picture

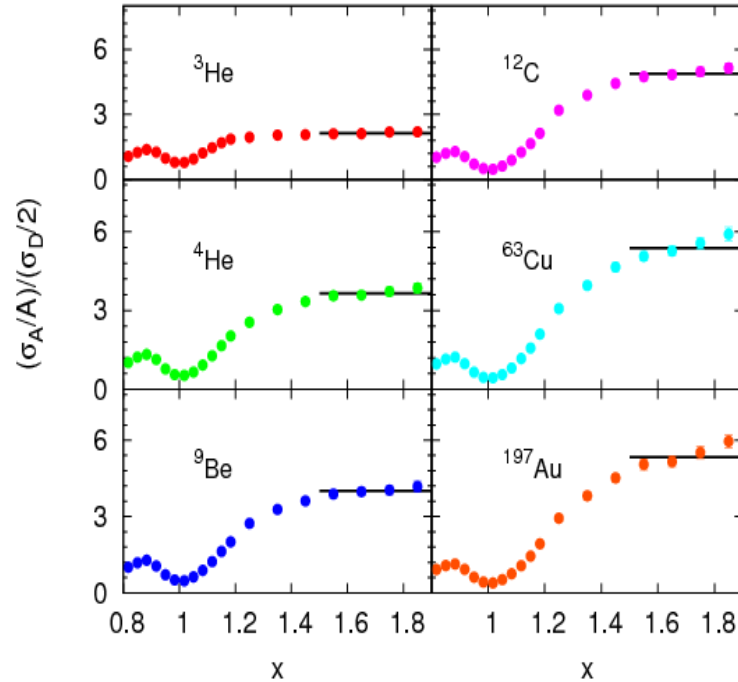
$$\begin{aligned} \sigma(x, Q^2) &= \sum_{j=1}^A A \frac{1}{j} a_j(A) \sigma_j(x, Q^2) \\ &= \frac{A}{2} a_2(A) \sigma_2(x, Q^2) + \\ &\quad \frac{A}{3} a_3(A) \sigma_3(x, Q^2) + \dots \end{aligned}$$



# Jlab E02-019: 2N correlations in A/D ratios (early 21<sup>st</sup> century)

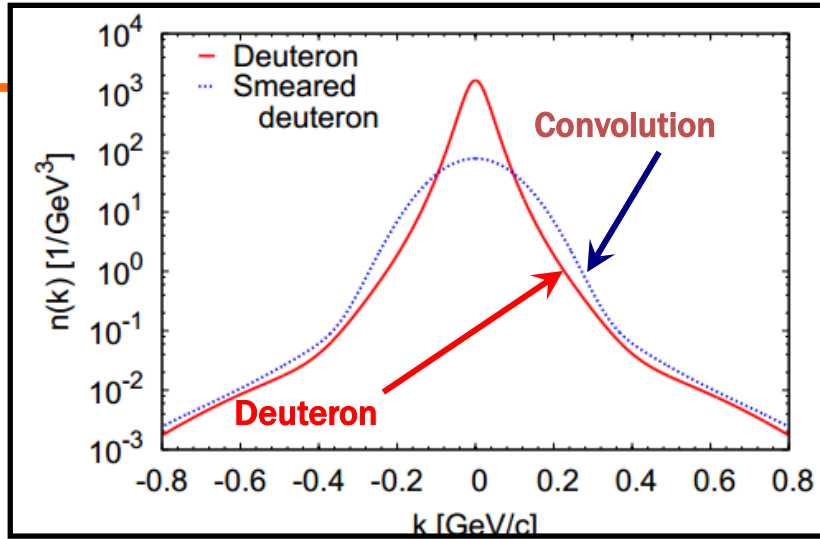
A	$\theta_e=18^\circ$
$^3\text{He}$	$2.14 \pm 0.04$
$^4\text{He}$	$3.66 \pm 0.07$
Be	$4.00 \pm 0.08$
C	$4.88 \pm 0.10$
Cu	$5.37 \pm 0.11$
Au	$5.34 \pm 0.11$
$\langle Q^2 \rangle$	$2.7 \text{ GeV}^2$
$x_{\min}$	1.5

$\langle Q^2 \rangle = 2.7 \text{ GeV}^2$



Fomin et al, PRL **108** (2012) Jlab E02-019

# Note: ( $a_2 = \sigma_A / \sigma_D$ ) != Relative #of SRCs



$n_D^{CONV}(k)$  is the convolution of  $n_D(k)$  with the CM motion of correlated pairs in iron

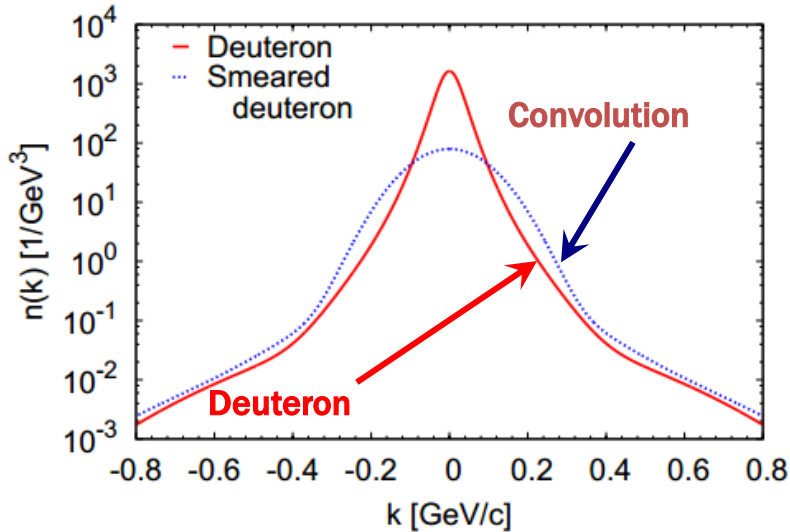
Following prescription from C. Ciofi degli Atti and S. Simula, *Phys. Rev. C* 53 (1996)

	E02-019	SLAC	CLAS	$R_{2n}$ -ALL	$a_2$ -ALL
$^3\text{He}$	$1.93 \pm 0.10$	$1.8 \pm 0.3$	-	$1.92 \pm 0.09$	$2.13 \pm 0.04$
$^4\text{He}$	$3.02 \pm 0.17$	$2.8 \pm 0.4$	$2.80 \pm 0.28$	$2.94 \pm 0.14$	$3.57 \pm 0.09$
Be	$3.37 \pm 0.17$	-	-	$3.37 \pm 0.17$	$3.91 \pm 0.12$
C	$4.00 \pm 0.24$	$4.2 \pm 0.5$	$3.50 \pm 0.35$	$3.89 \pm 0.18$	$4.65 \pm 0.14$
Al	-	$4.4 \pm 0.6$	-	$4.40 \pm 0.60$	$5.30 \pm 0.60$
Fe	-	$4.3 \pm 0.8$	$3.90 \pm 0.37$	$3.97 \pm 0.34$	$4.75 \pm 0.29$
Cu	$4.33 \pm 0.28$	-	-	$4.33 \pm 0.28$	$5.21 \pm 0.20$
Au	$4.26 \pm 0.29$	$4.0 \pm 0.6$	-	$4.21 \pm 0.26$	$5.13 \pm 0.21$

$a_2 = \sigma_A / \sigma_D \rightarrow$  relative measure of high momentum nucleons

$R_{2n} \rightarrow$  relative measure of correlated pairs

**NOTE:  $a_2 = \frac{\sigma_A}{\sigma_D} ! = \text{RELATIVE \#OF SRCS}$**



$a_2 = \frac{\sigma_A}{\sigma_D} \rightarrow$  relative measure of high momentum nucleons

$R_{2n} \rightarrow$  relative measure of correlated pairs

$n_D^{CONV}(k)$  is the convolution of  $n_D(k)$  with the CM motion of correlated pairs in iron

Following prescription from C. Ciofi degli Atti and S. Simula, Phys. Rev. C 53 (1996)

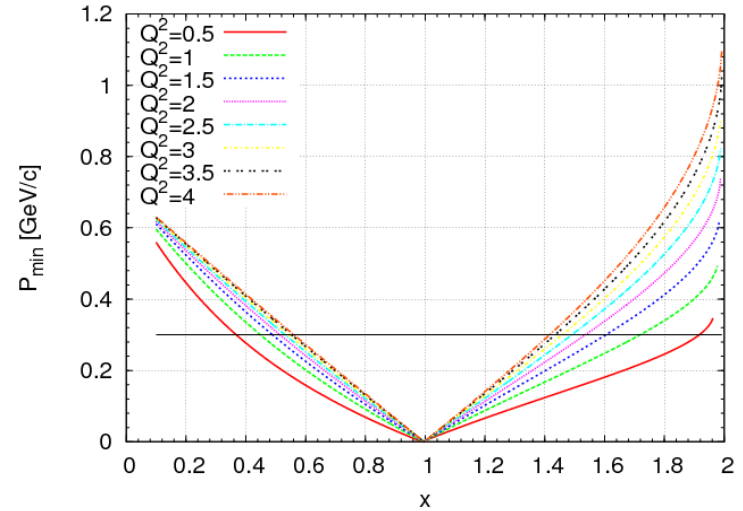
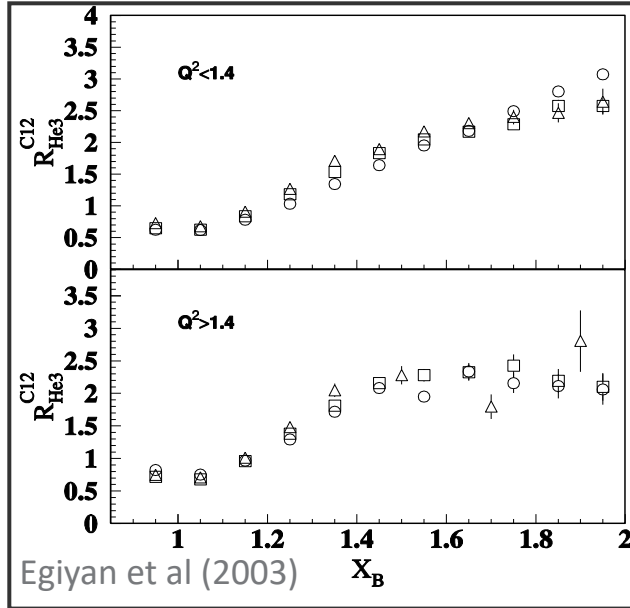
	E02-019	SLAC	CLAS	$R_{2N-ALL}$	$a_2-ALL$
$^3\text{He}$	$1.93 \pm 0.10$	$1.8 \pm 0.3$	–	$1.92 \pm 0.09$	$2.13 \pm 0.04$
$^4\text{He}$	$3.02 \pm 0.17$	$2.8 \pm 0.4$	$2.80 \pm 0.28$	$2.94 \pm 0.14$	$3.57 \pm 0.09$
Be	$3.37 \pm 0.17$	–	–	$3.37 \pm 0.17$	$3.91 \pm 0.12$
C	$4.00 \pm 0.24$	$4.2 \pm 0.5$	$3.50 \pm 0.35$	$3.89 \pm 0.18$	$4.65 \pm 0.14$
Al	–	$4.4 \pm 0.6$	–	$4.40 \pm 0.60$	$5.30 \pm 0.60$
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Au	$4.26 \pm 0.29$	$4.0 \pm 0.6$	–	$4.21 \pm 0.26$	$5.13 \pm 0.21$

# Inclusive Scattering

- Relative measurement
- Reduced FSI
- **Test scaling in  $x$  and  $Q^2$**
- No direct information on isospin structure
  - Only via target isospin structure
- No direct information on momentum distribution for  $A > 2$

# Inclusive Scattering

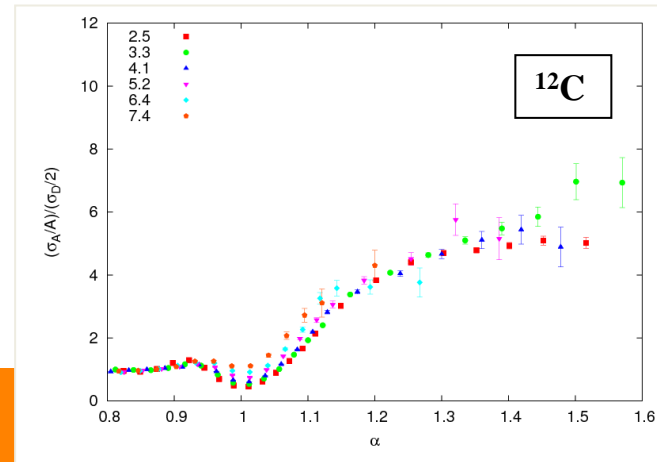
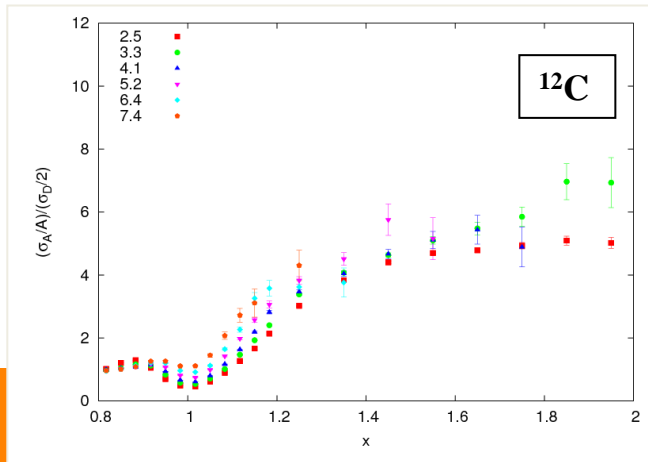
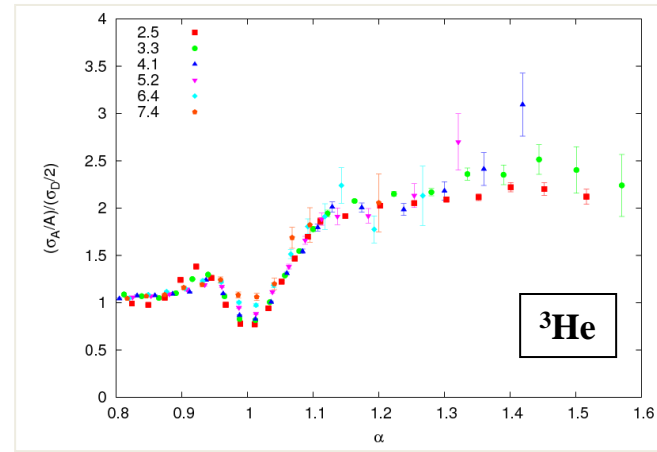
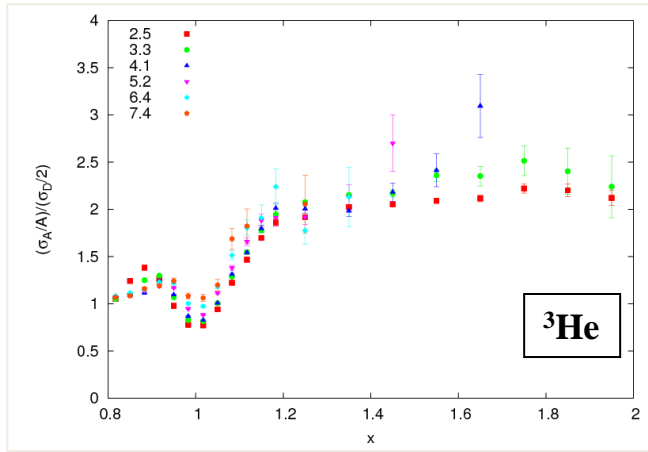
- Test scaling in  $x$  and  $Q^2$



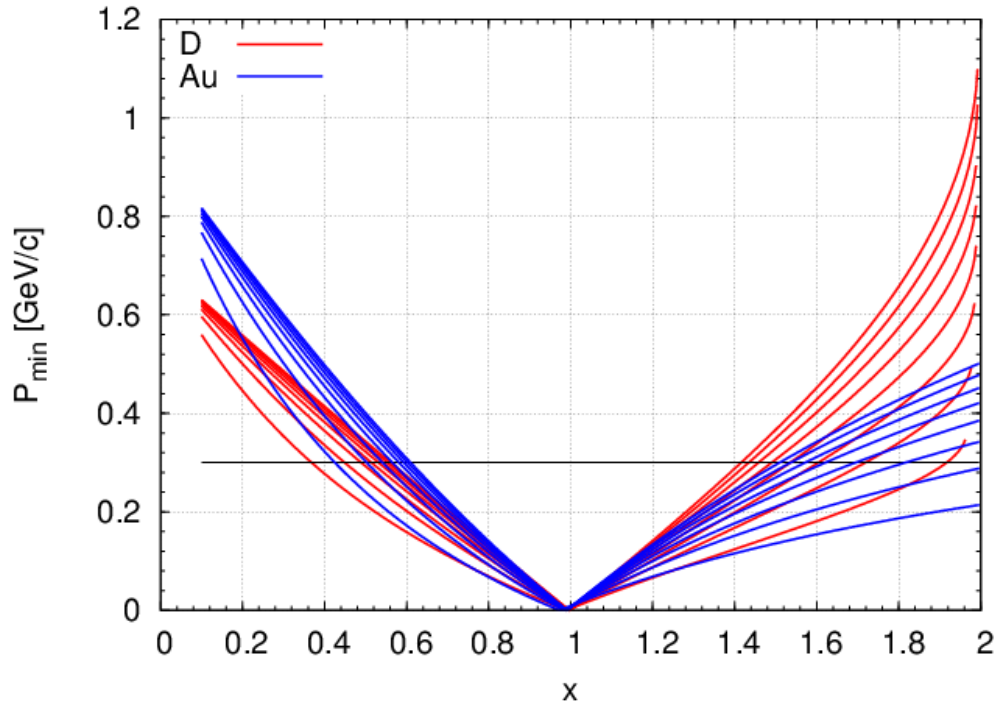
Calculation for  $A=2$

# Test scaling in $x$ and $Q^2$

$$\alpha = 2 - \frac{q^- + 2M}{2M} \left( 1 + \frac{\sqrt{W^2 - 4M^2}}{W} \right)$$



# Kinematic cutoff is A-dependent

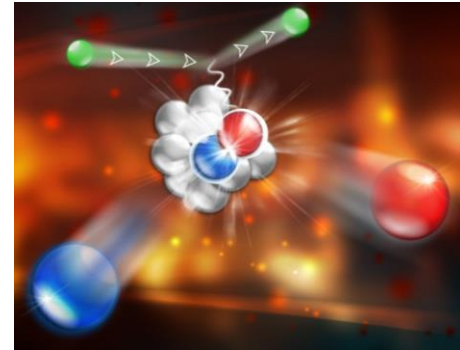


- For heavy nuclei, the minimum momentum changes  $\rightarrow$  heavier recoil system requires less kinetic energy to balance the momentum of the struck nucleon
- Larger fermi momenta for  $A > 2 \rightarrow$  MF contribution persists for longer
- Imperfect plateau, but the picture still holds

# 2N knockout experiments establish NP dominance

- Knockout high-initial-momentum proton, look for correlated nucleon partner.
- For  $300 < P_{\text{miss}} < 600$  MeV/c all nucleons are part of 2N-SRC pairs: 90% np, 5% pp (nn)

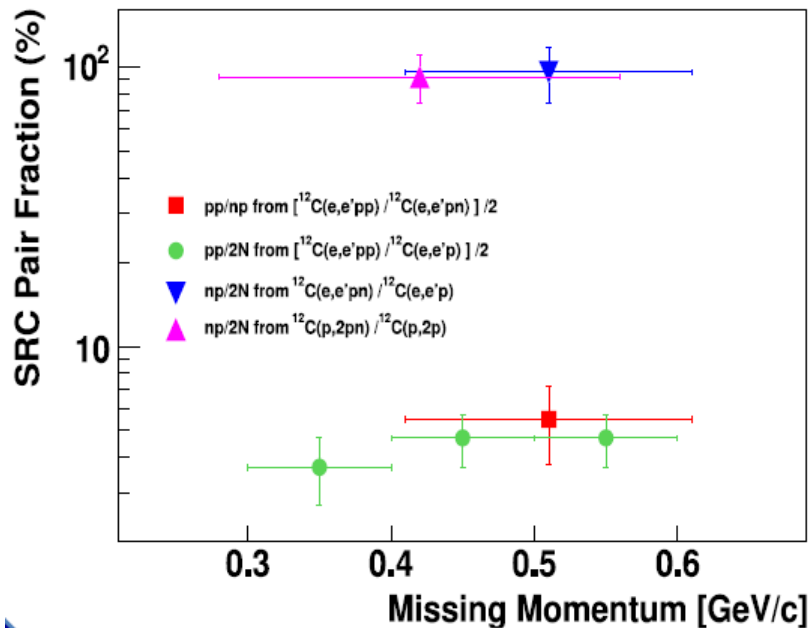
R. Subedi et al., *Science*  
320, 1476 (2008)



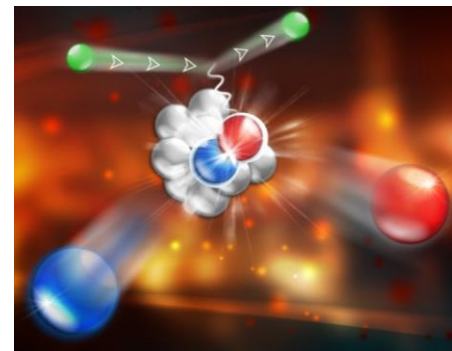
R. Shneor et al.,  
*PRL* 99, 072501 (2007)



# 2N knockout experiments establish NP dominance



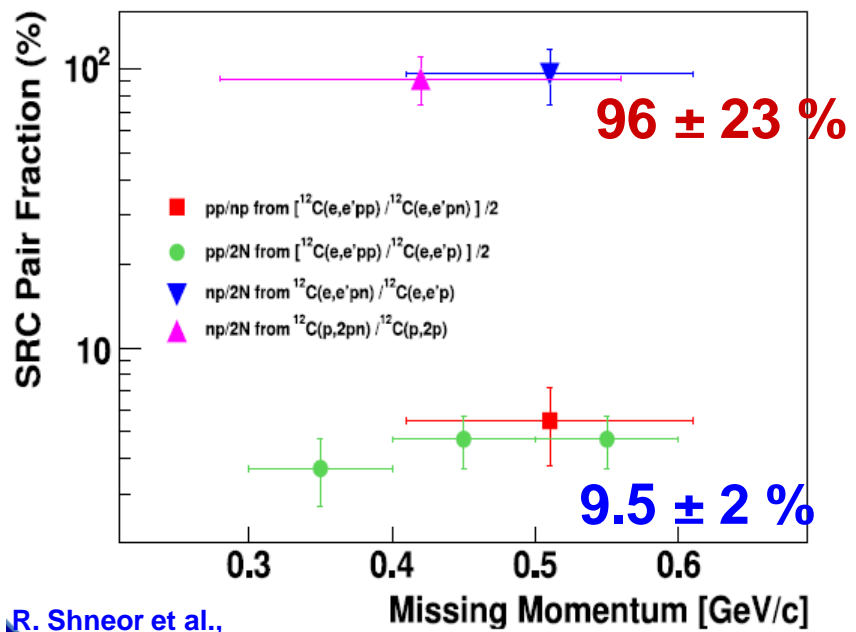
R. Subedi et al., *Science*  
320, 1476 (2008)



R. Shneur et al.,  
*PRL* 99, 072501 (2007)

*Relevant for interpretation of inclusive data*

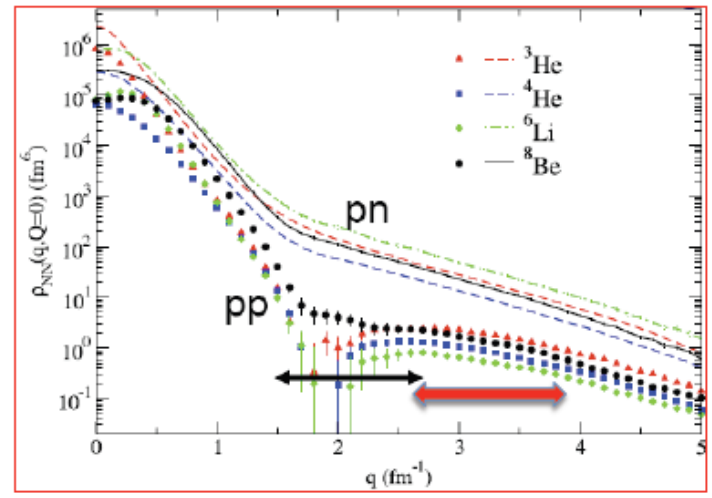
# NP dominance



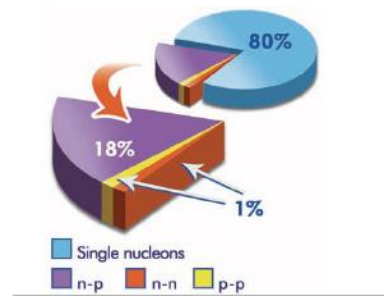
R. Shneor et al.,  
 PRI 99 072501 (2007)

also

- Ciofi and Alvioli PRL 100, 162503 (2008)
- Sargsian, Abrahamyan, Strikman, Frankfurt PR C71 044615 (2005)



R. Schiavilla, R. B. Wiringa, S. C. Pieper, J. Carlson, Phys. Rev. Lett. **98** (2007) 132501



# Where are we now? Publishing Nature Papers

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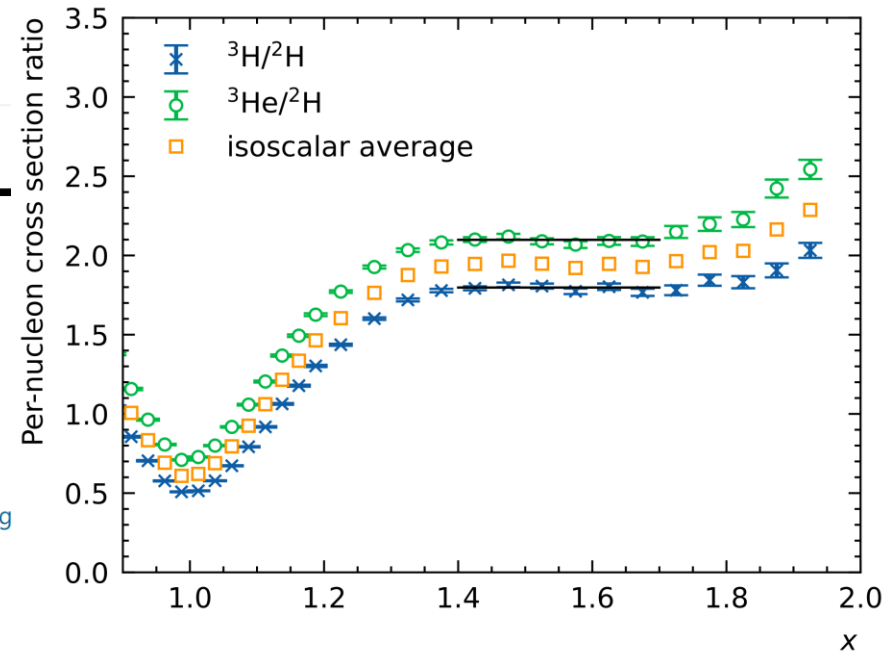
Article | [Published: 31 August 2022](#)

## Revealing the short-range structure of the mirror nuclei ${}^3\text{H}$ and ${}^3\text{He}$

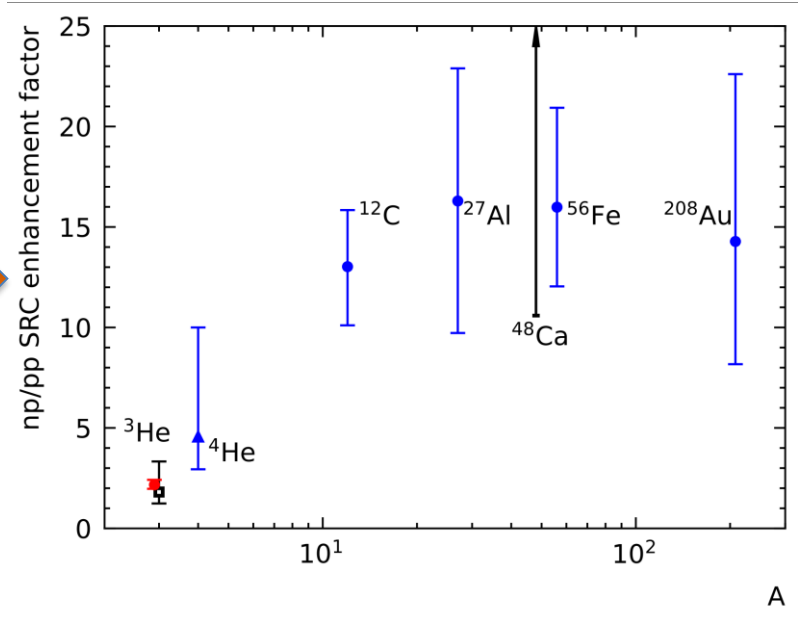
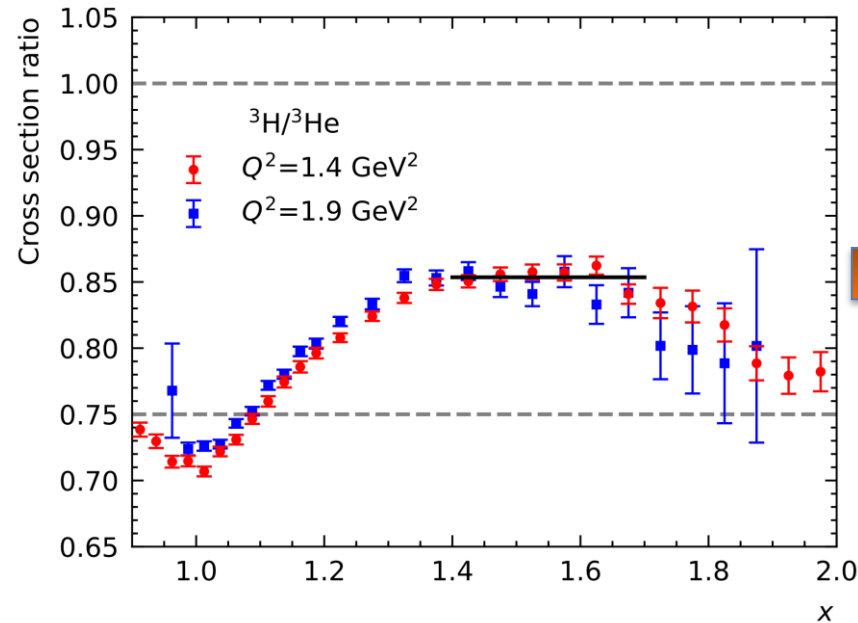
[S. Li](#), [R. Cruz-Torres](#), [N. Santiesteban](#), [Z. H. Ye](#), [D. Abrams](#), [S. Alsalmi](#), [D. Androic](#), [K. Aniol](#), [J. Arring](#)

*Inclusive measurement on  $A=3$  nuclei*

*S. Li, et al., Nature 609, 41 (2022)*



# Where are we now? Publishing Nature Papers

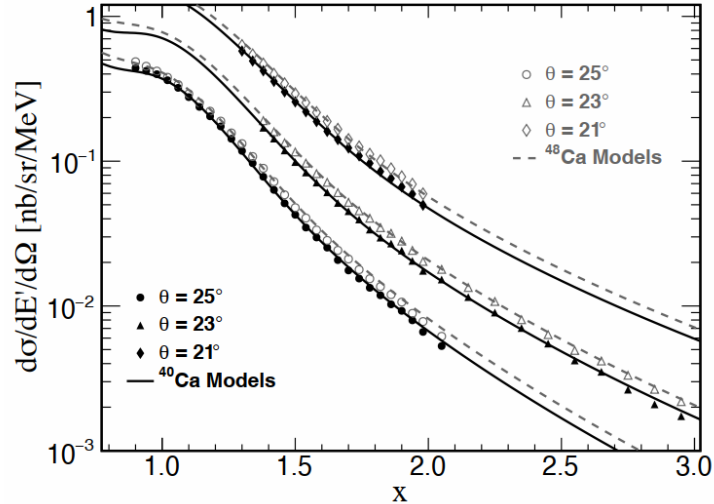


*Inclusive measurement on  $A=3$  nuclei*

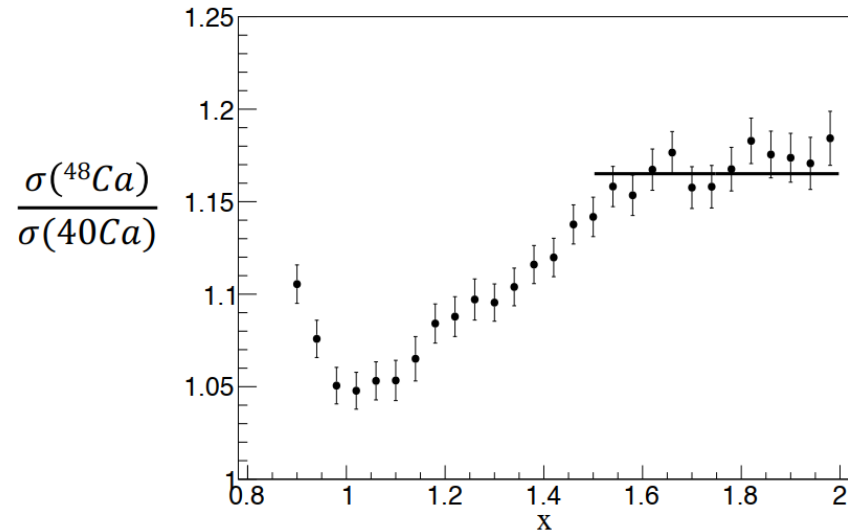
*S. Li, et al., Nature 609, 41 (2022)*

# Inclusive Ca48/Ca40 Ratios

Absolute (e,e') cross-sections



More SRC pairs in  $^{48}\text{Ca}$ !

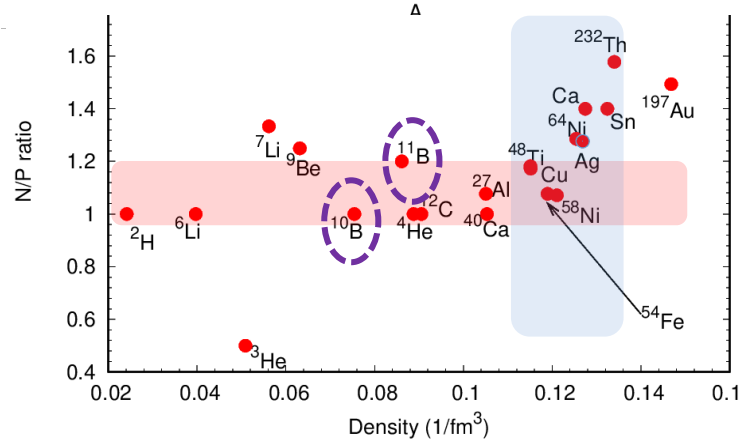
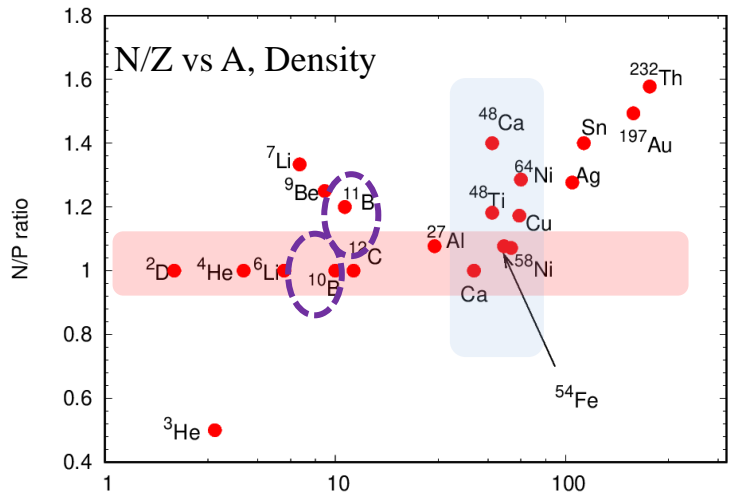
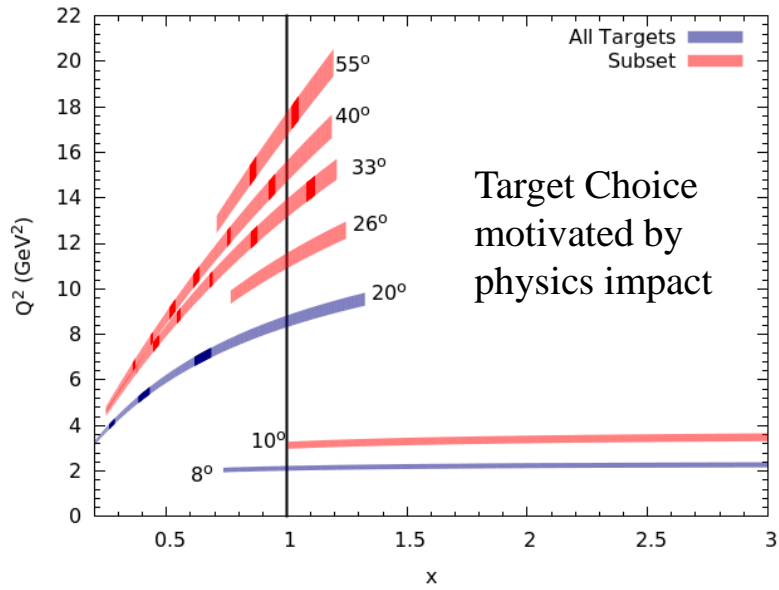


Courtesy Dien Nguyen

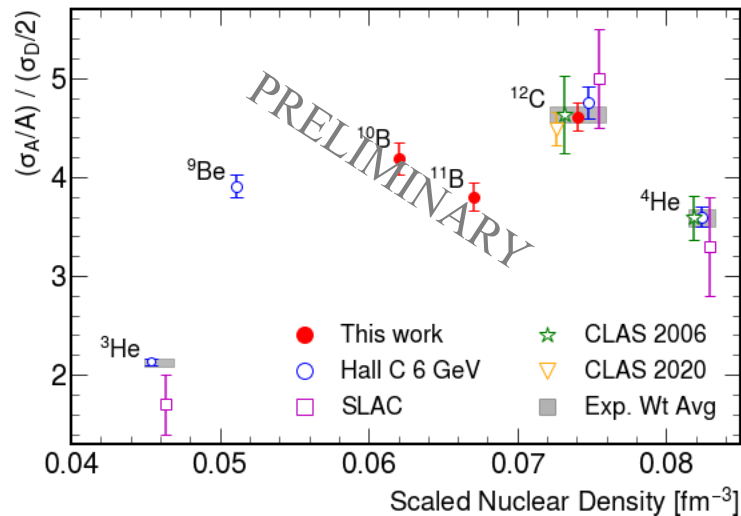
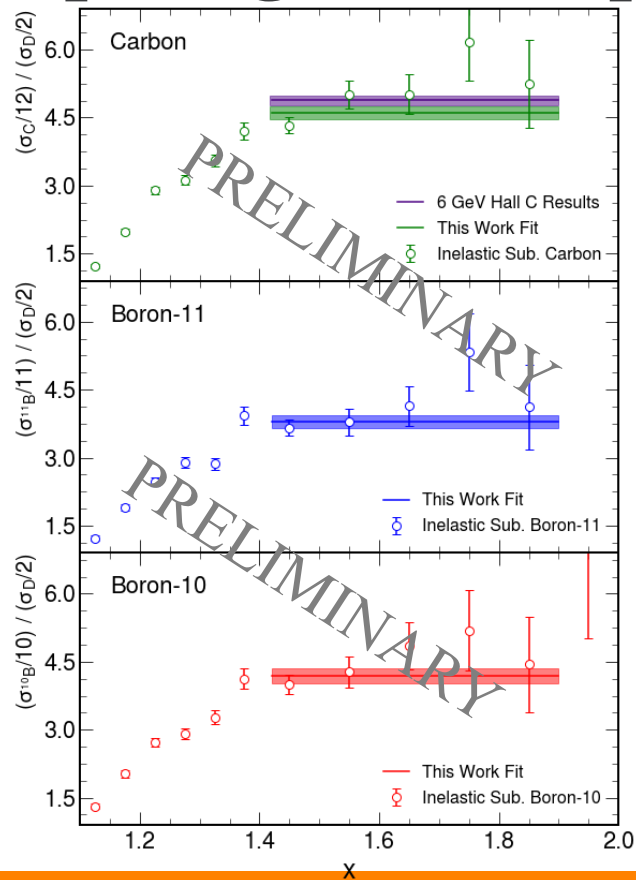
*Potentially in tension with upcoming results (see Justin's afternoon talk)*

**E12-10-008:** J. Arrington, A Daniel, NF, D. Gaskell:  
 Detailed Studies of the nuclear dependence of  $F_2$  in light nuclei

**E12-06-105:** J. Arrington, D. Day, NF, P. Solvignon:  
 Inclusive Scattering from Nuclei at  $x > 1$  in the quasielastic and deeply inelastic regimes

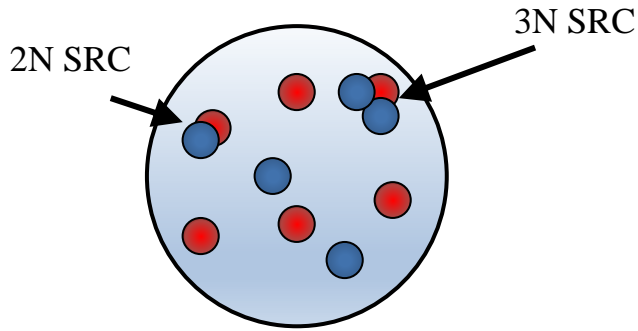


# Preparing 2N SRC publication as well



*Analysis by Casey Morean (UTK)*

# More nucleons in a correlation



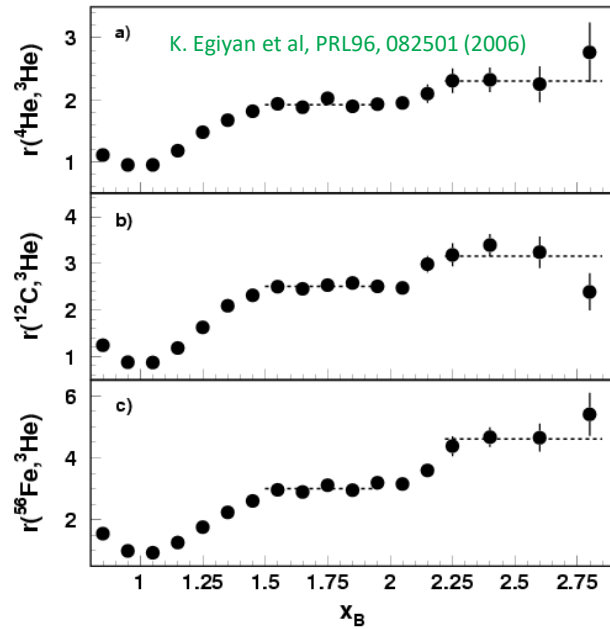
$1.4 < x < 2 \Rightarrow$  2 nucleon correlation

$2.4 < x < 3 \Rightarrow$  3 nucleon correlation

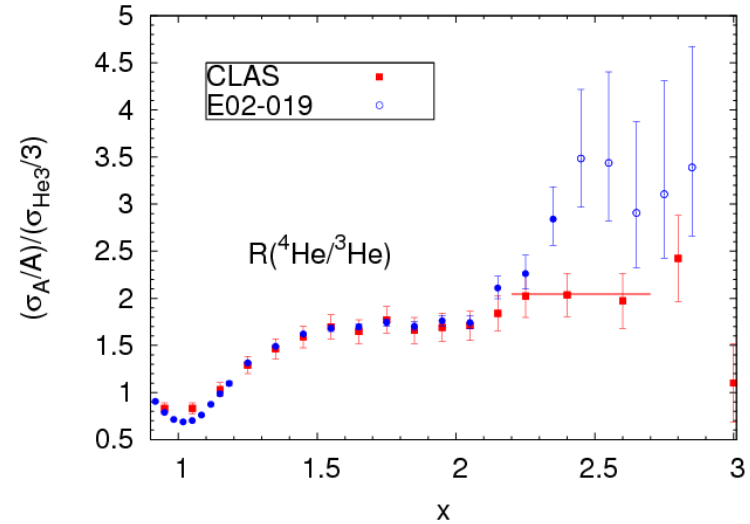
$$\begin{aligned}\sigma(x, Q^2) &= \sum_{j=1}^A A \frac{1}{j} a_j(A) \sigma_j(x, Q^2) \\ &= \frac{A}{2} a_2(A) \sigma_2(x, Q^2) + \\ &\quad \frac{A}{3} a_3(A) \sigma_3(x, Q^2) + \dots\end{aligned}$$



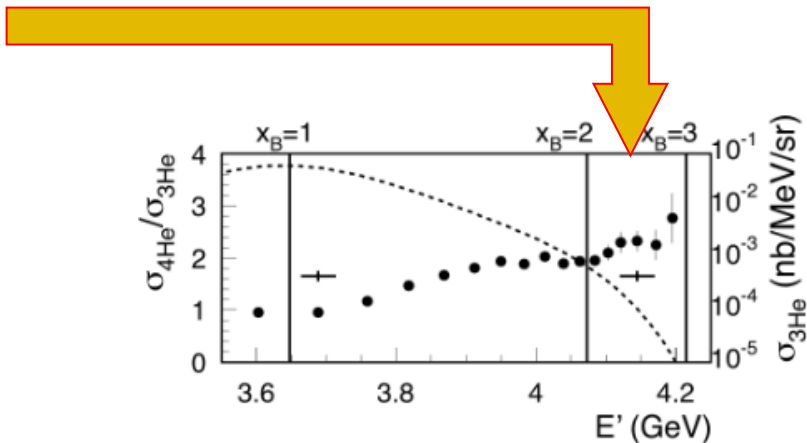
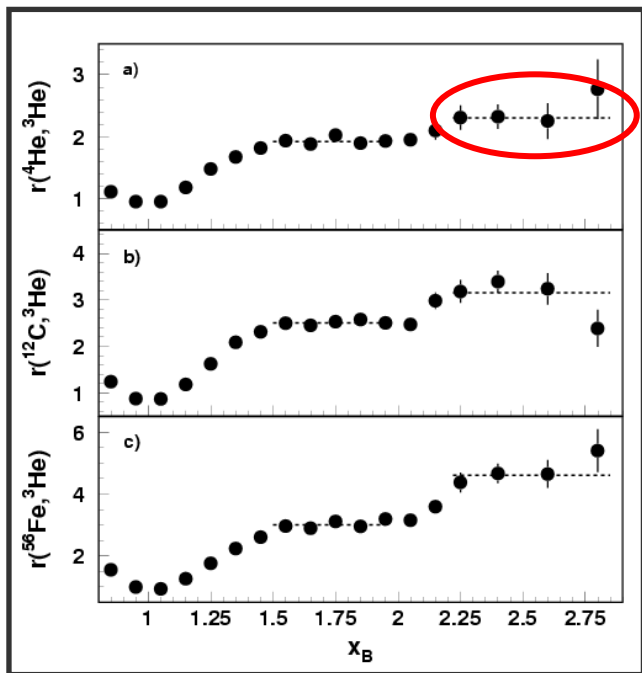
# 3N correlations ( $x > 2$ inclusive scattering)



$\langle Q^2 \rangle$  (GeV<sup>2</sup>): CLAS: 1.6      E02-019: 2.7



# Have we actually seen 3N SRC in ratios?



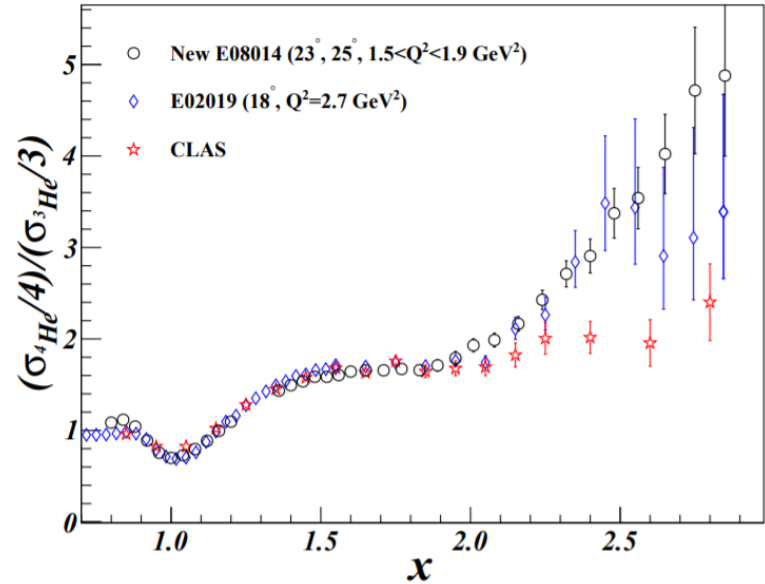
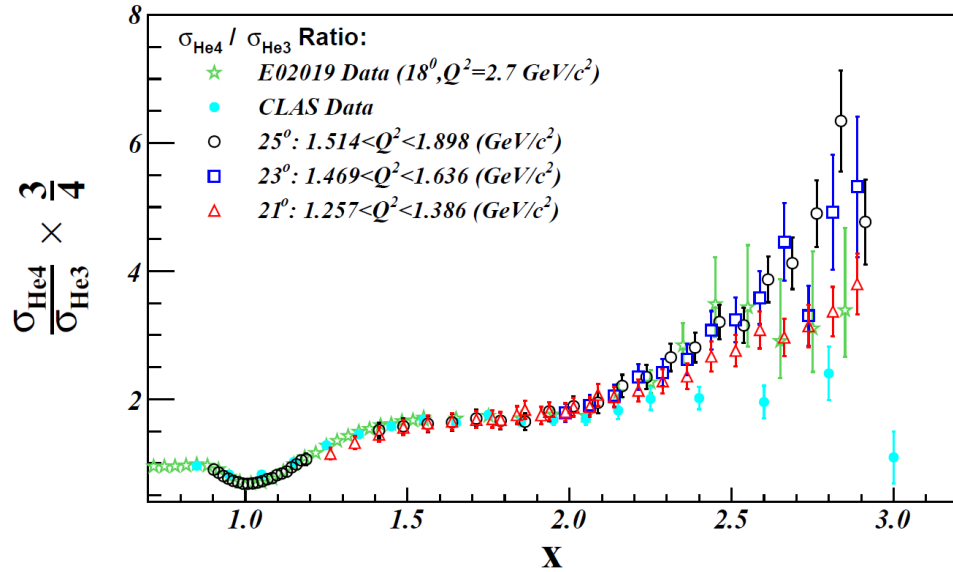
Comment on “Measurement of 2- and 3-nucleon short range correlation probabilities in nuclei”

Douglas W. Higinbotham<sup>1</sup> and Or Hen<sup>2</sup>

<sup>1</sup>Jefferson Lab, Newport News, VA 23606, USA

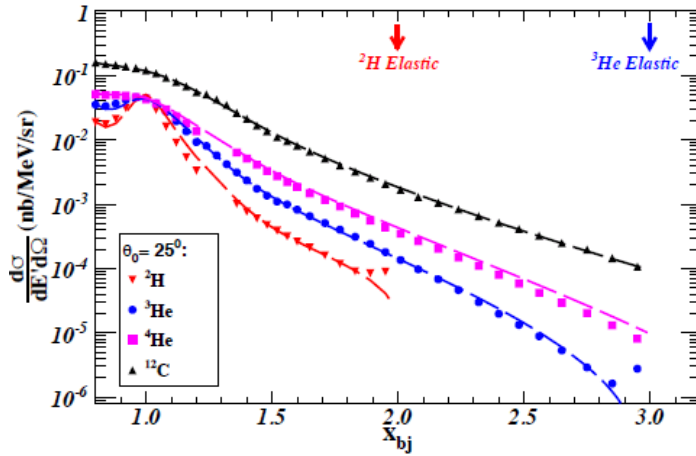
<sup>2</sup>Tel Aviv University, Tel Aviv, Israel

# 3N correlations - still looking



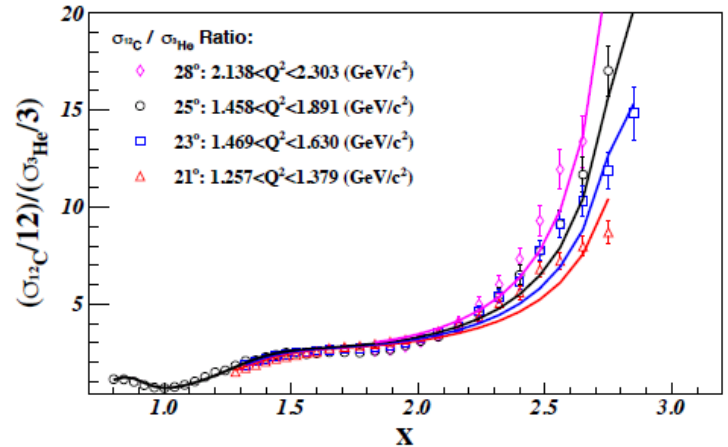
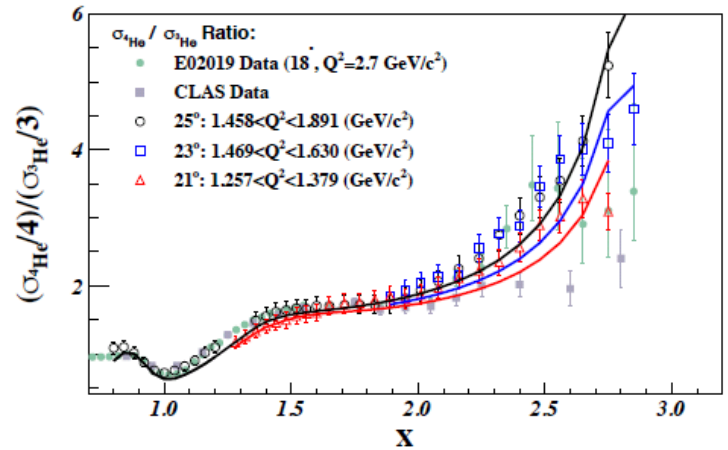
Z. Ye et al, PRC 97 (2018) 6

# Can we see a second plateau?



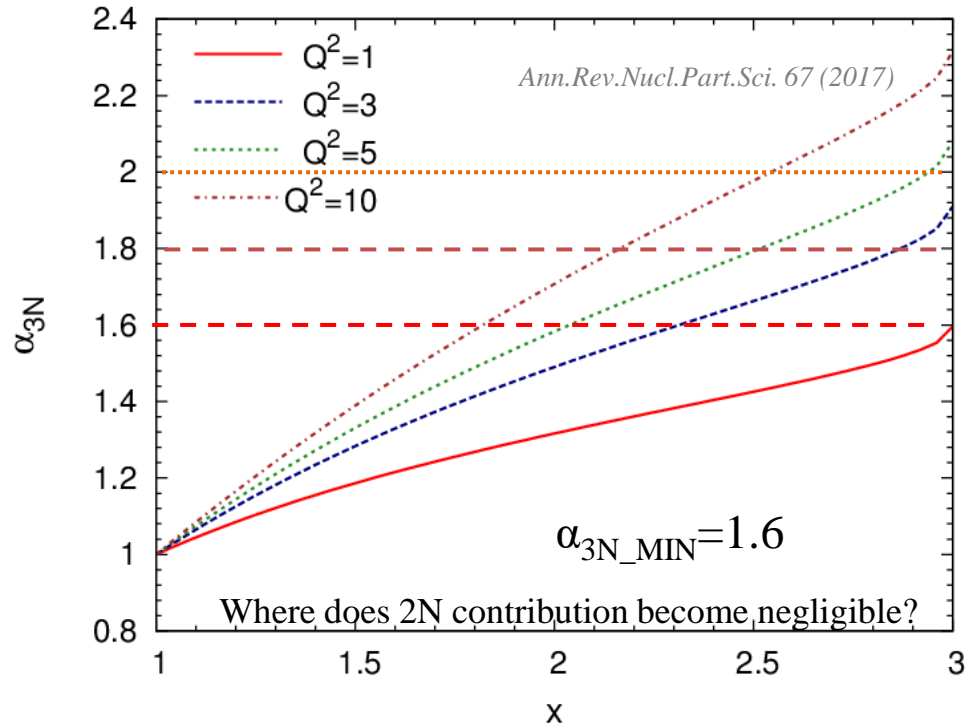
Deuteron: smeared SRC similar to 2H (A/D is ~flat) until  $x > 1.8$

$^3\text{He}$ : cross section of stationary 3N-SRC begins to fall off closer to  $x = 2.6$ . Sets in EARLIER at high  $Q^2$



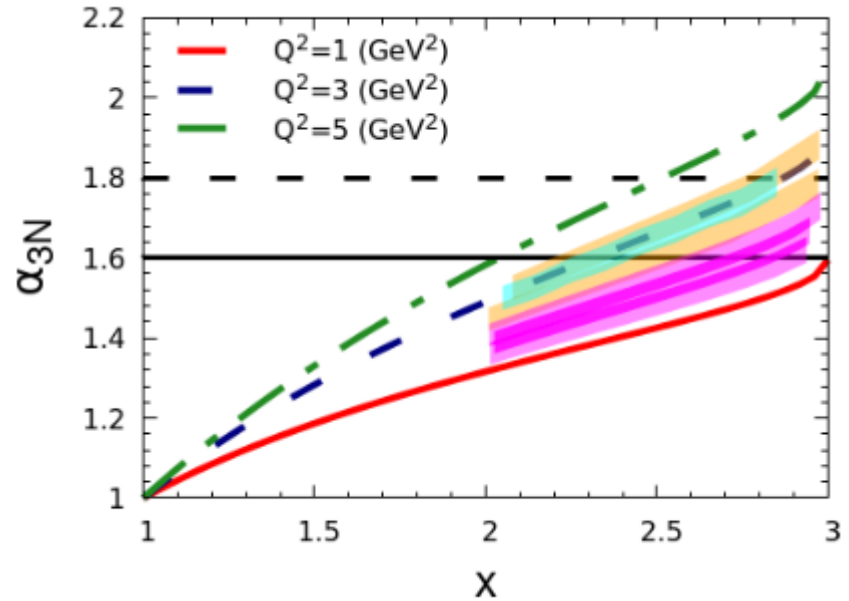
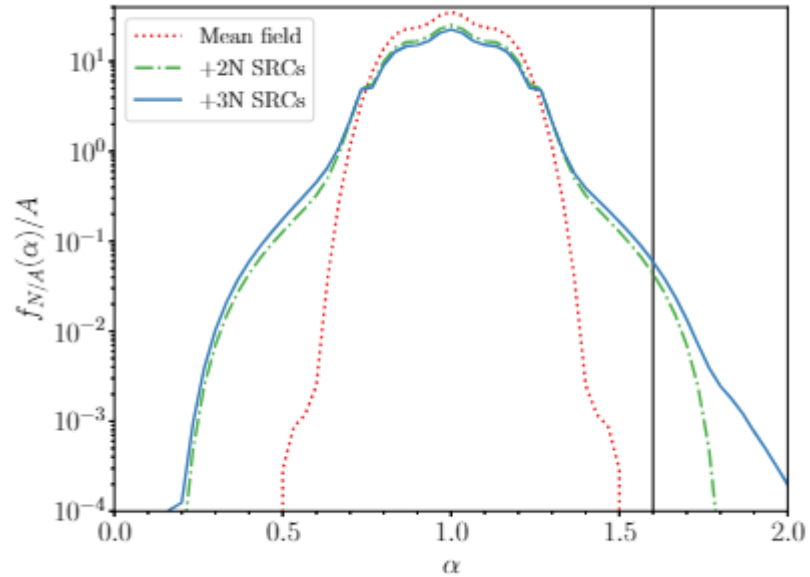


# 3N correlations – are we there yet?

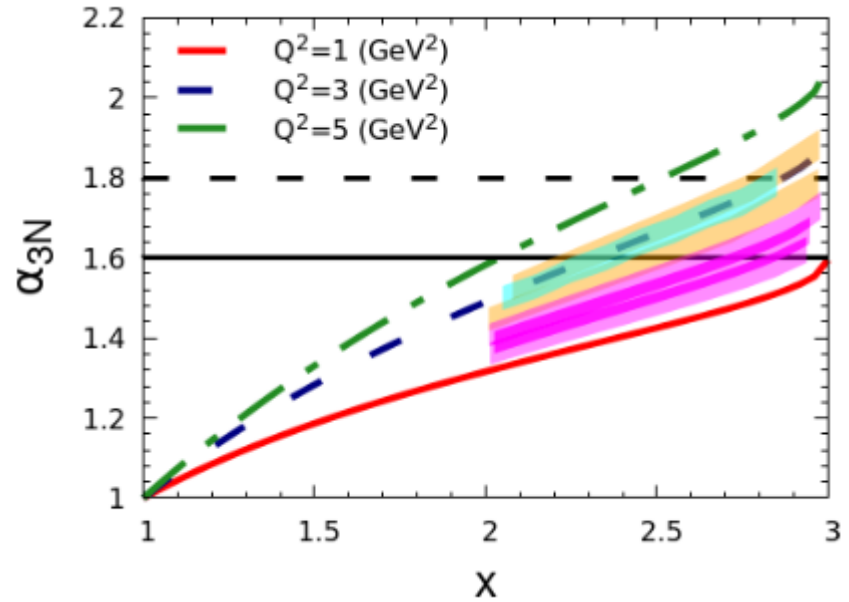
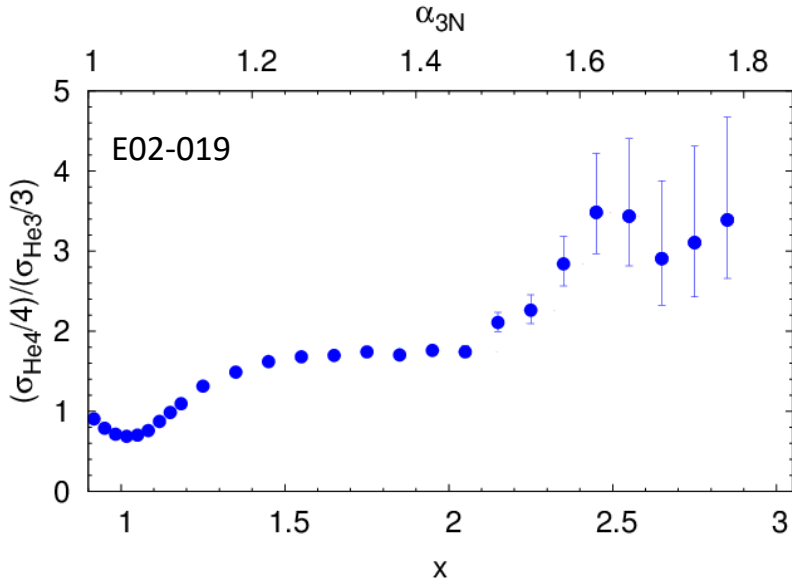


$\alpha$  represents the light-cone momentum fraction of 3N SRCs carried by the correlated nucleon  $i$

# We were so close at 6 GeV in Hall C



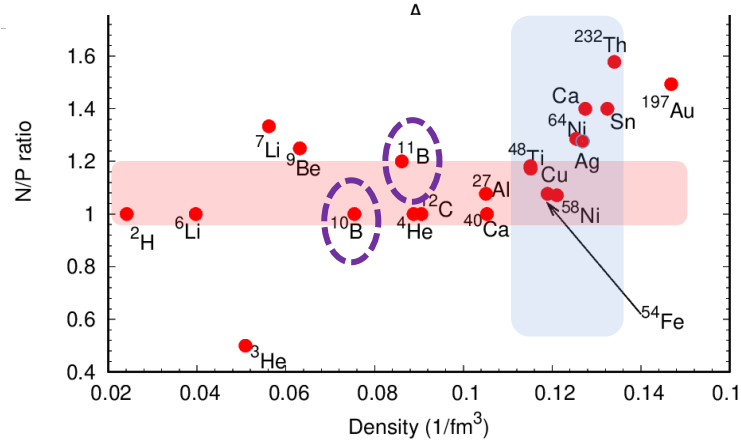
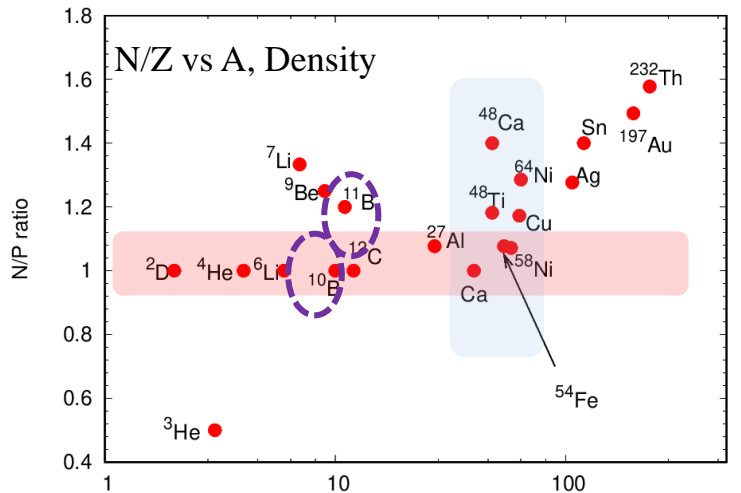
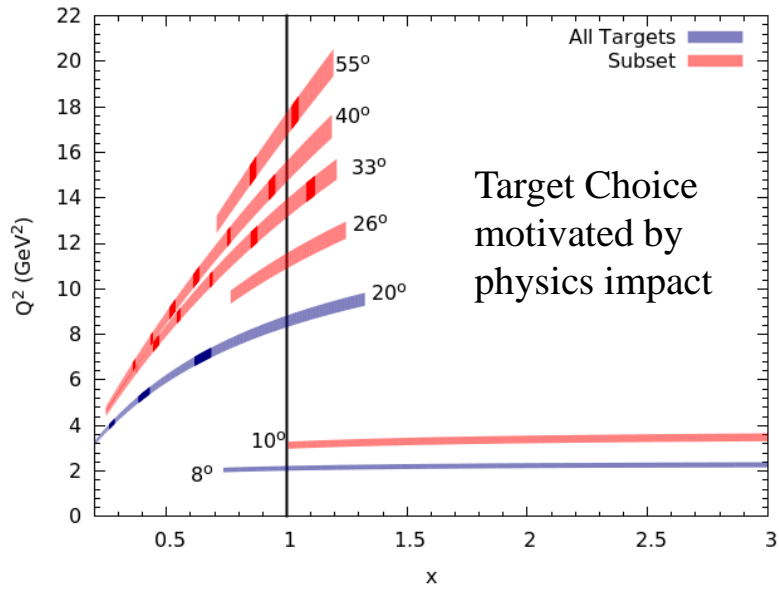
# We were so close at 6 GeV in Hall C





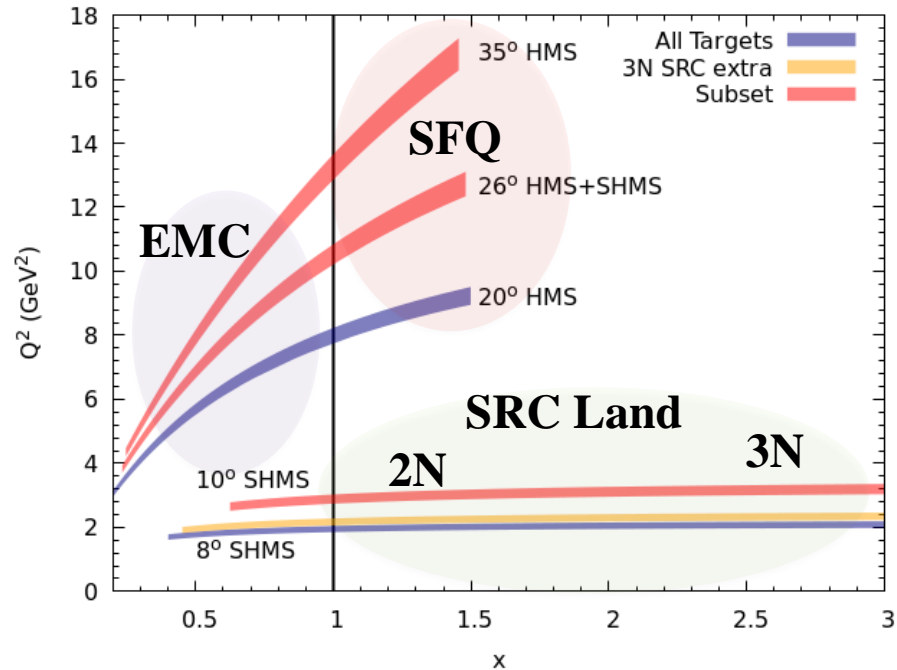
**E12-10-008:** J. Arrington, A Daniel, NF, D. Gaskell:  
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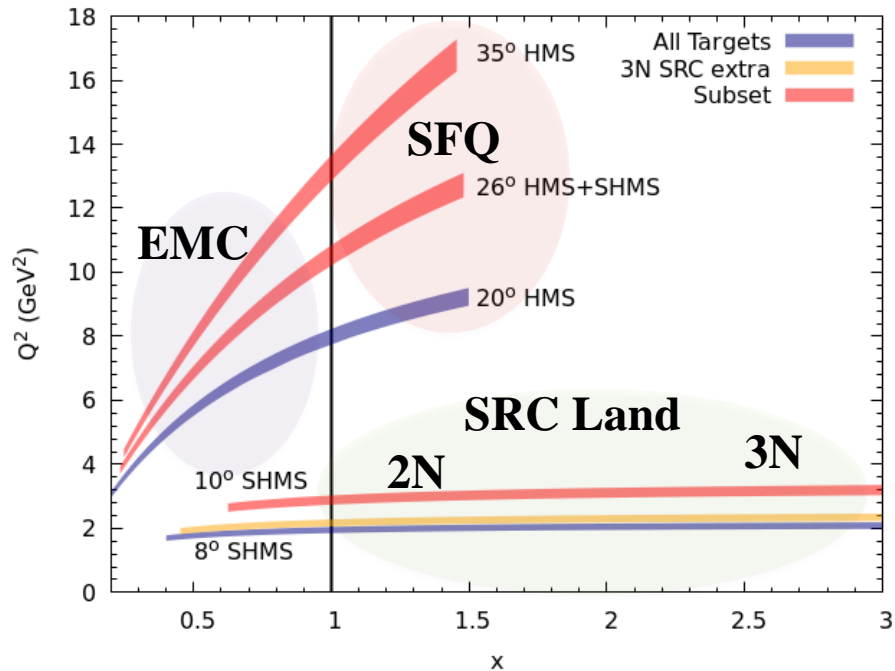
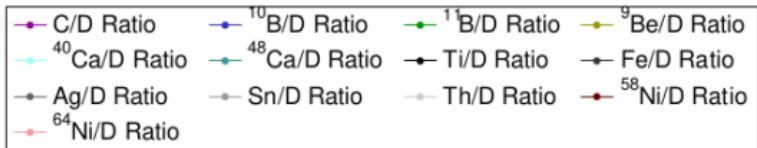
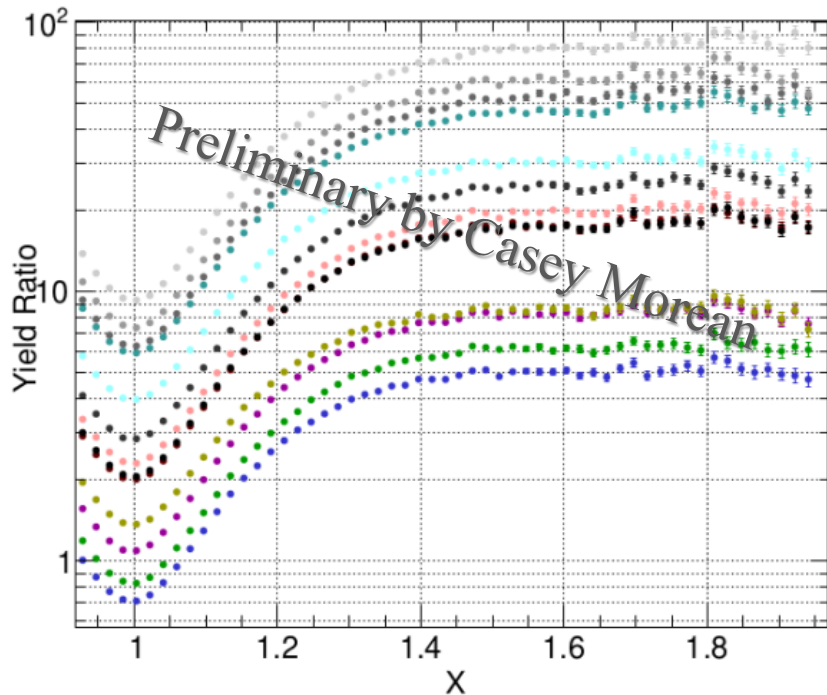


# XEM2: Data taking completed

Ladder 1	Ladder 2
Hydrogen/He3	Hydrogen /He3
Deuterium/He4	Deuterium/He4
Dummy	Dummy
Optics	Optics
Carbon hole	Carbon hole
12C	12C
40Ca	6Li*
48Ca	7Li*
10B	10B
11B	11B
9Be	9Be
54Fe	Al
58Ni	Cu
64Ni	Au
Ag	1 mm
Sn	1 mm
232Thorium	1 mm
Titanium	Thicker carbon?



# XEM2: 2N correlations in A/D ratios



# Summary

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- Studies of SRCs continue at Jlab in the 12 GeV era with inclusive Scattering
- First observation of 3N SRC existence is yet to come
- New results in the next few years!
- This work was supported by DOE Award DE-SC0013615