

# **Machine learning for lattice field theory and beyond**

## **Report of Contributions**

Contribution ID: 1

Type: **not specified**

## <sup>4</sup> Scalar Neural Network Field Theory

*Friday, 30 June 2023 10:00 (25 minutes)*

Neural Network (NN) architectures at initialization define field theories. Certain large width limits of architectures result in free field theories due to Central Limit Theorem (CLT); deviations from CLT via finite width, and correlated, dissimilar NN parameters turn on field interactions. Edgeworth method provides a way to construct NN field theory actions using connected Feynman diagrams, where internal vertices correspond to connected correlators of NN field theories. Further, specific interacting field theories can be engineered via the NN parameter framework, where non-Gaussianities due to statistical independence breaking of NN parameters tune the action deformations. As an example, I will present the construction of <sup>4</sup> scalar field theory in infinite width NNs.

**Primary authors:** Dr MAITI, Anindita (Harvard University); Prof. HALVERSON, James (Northeastern University); Prof. SCHWARTZ, Matthew D.; Dr DEMIRTAS, Mehmet (Northeastern University)

**Presenters:** Dr MAITI, Anindita (Harvard University); MAITI, Anindita (Harvard University)

Contribution ID: 2

Type: **not specified**

## Renormalization Group Approach for Machine Learning Hamiltonian

*Wednesday, 28 June 2023 11:30 (25 minutes)*

Reconstructing, or generating, Hamiltonian associated with high dimensional probability distributions starting from data is a central problem in machine learning and data sciences. We will present a method —The Wavelet Conditional Renormalization Group—that combines ideas from physics (renormalization group theory) and computer science (wavelets, Monte-Carlo sampling, etc.). The Wavelet Conditional Renormalization Group allows reconstructing in a very efficient way classes of Hamiltonians and associated high dimensional distributions hierarchically from large to small length scales. We will present the method and then show its applications to data from statistical physics and cosmology.

**Primary author:** OZAWA, Misaki (CNRS, Univ. Grenoble Alpes, France)

**Presenter:** OZAWA, Misaki (CNRS, Univ. Grenoble Alpes, France)

Contribution ID: 3

Type: **not specified**

## Continuous flows and transfer learning

*Tuesday, 27 June 2023 15:30 (25 minutes)*

We explore continuous flows as generative models, focusing on their architectural flexibility in implementing equivariance, and test them on the  $^4$  theory. Using this setup, we show how a machine-learning approach enables transfer between lattice sizes and allows us to learn for a continuous range of theory parameters at once. Investigating the sample efficiency of training, we find that the expressivity of continuous flows may justify their higher numerical cost due to integration.

**Primary authors:** GERDES, Mathis (University of Amsterdam); DE HAAN, Pim

**Co-authors:** RAINONE, Corrado; BONDESAN, Roberto; CHENG, Miranda C. N.

**Presenter:** GERDES, Mathis (University of Amsterdam)

Contribution ID: 4

Type: **not specified**

## Gradient estimators without action derivative in Schwinger model.

*Tuesday, 27 June 2023 15:00 (25 minutes)*

When training normalizing flows to approximate Boltzmann probability distribution, the usual approach to calculating gradients, based on the “reparametrization trick” requires backpropagation through the action. In the case of more complicated actions like fermionic action in QCD, this raises performance issues as well as problems with numerical stability. We present an estimator based on the REINFORCE algorithm that avoids this problem and demonstrate its efficacy in the case of the two-dimensional Schwinger model.

**Primary author:** BIALAS, Piotr (Jagiellonian University)

**Co-authors:** Prof. KORCYL, Piotr (Jagiellonian University); Dr STEBEL, Tomasz

**Presenter:** BIALAS, Piotr (Jagiellonian University)

Contribution ID: 5

Type: **not specified**

## Interpretable order parameters from persistent homology in non-Abelian lattice gauge theory

*Thursday, 29 June 2023 11:00 (25 minutes)*

Finding interpretable order parameters for the detection of critical phenomena and self-similar behavior in and out of equilibrium is a challenging endeavour in non-Abelian gauge theories. Tailored to detect and quantify topological structures in noisy data, persistent homology allows for the construction of sensitive observables. Based on hybrid Monte Carlo simulations of SU(2) lattice gauge theory I will show how the persistent homology of filtrations by chromoelectric and -magnetic fields, topological densities and Polyakov loops can be used to gauge-invariantly and partly without cooling algorithms uncover a multifaceted picture of the confinement-deconfinement phase transition. In classical-statistical simulations far from equilibrium the topological observables reveal self-similar scaling related to a non-thermal fixed point. The results showcase the extensive versatility of persistent homology in non-Abelian gauge theories, with promising perspectives in relation to topological machine learning for lattice field theories.

This talk is based on joint works with Jürgen Berges, Kirill Boguslavski, Jan Pawłowski and Julian Urban.

**Primary author:** SPITZ, Daniel (Institute for Theoretical Physics, Heidelberg University)

**Presenter:** SPITZ, Daniel (Institute for Theoretical Physics, Heidelberg University)

Contribution ID: 6

Type: **not specified**

## Deep Learning Inverse Problems in Extreme QCD Matter Study

*Monday, 26 June 2023 16:00 (25 minutes)*

In this talk we introduce how deep learning helps in solving inverse problems in the scope of extreme QCD matter study. The study of QCD matter under extreme conditions presents numerous challenging inverse problems, where the forward problem is straightforward but the inversion is not, such as in-medium interaction retrieval, spectral function reconstruction, nuclear matter equation of state inference, etc. Deep Learning methods have been explored in these problems, with several different strategies including data-driven supervised learning and physics-driven unsupervised learning approaches. We will talk about these recent trials with also summary from the methodology point of view.

**Primary author:** ZHOU, Kai (Frankfurt Institute for Advanced Studies)

**Presenter:** ZHOU, Kai (Frankfurt Institute for Advanced Studies)

Contribution ID: 7

Type: **not specified**

# Machine Learned Thermodynamics of Physical Systems Across Critical Phases

*Thursday, 29 June 2023 09:30 (25 minutes)*

In recent years, there has been a growing interest in the application of normalizing flows for sampling in lattice field theory. Successful achievements have been made in various domains, including scalar field theories,  $U(1)$  and  $SU(N)$  pure gauge theories, as well as fermionic gauge theories. Furthermore, recent developments have shown promising results for full Lattice QCD. Although these flow-based sampling methods remain challenging to scale for desired systems, they possess desirable properties that make them an attractive tool, despite their current limitations.

In particular, the combination of normalizing flows with importance sampling has demonstrated accurate measurement of thermodynamic observables. These quantities are typically difficult to estimate using standard sampling algorithms such as HMC. However, it is worth noting that normalizing flows are typically trained through self-sampling in this specific context, which introduces the risk of assigning extremely low probability mass to certain modes of the theory. This issue may lead to substantially biased estimators of physical observables, due to mode-collapse during the training phase of the algorithm.

In this work, we first introduce a framework that allows for the derivation of asymptotically unbiased estimators for thermodynamic observables. Secondly, we investigate the mode-mismatch phenomenon, both theoretically and numerically. We provide a detailed analysis of the mode-seeking nature of the standard self-sampling-based training procedure and compare it with alternative training objectives. Finally, we present numerical and theoretical results, including a derived bound on the bias of the estimator for physical observables. This proposal offers a natural metric to quantify the extent of mode-collapse in the sampler.

**Primary author:** Dr NICOLI, Kim (University of Bonn - HISKP)

**Presenter:** Dr NICOLI, Kim (University of Bonn - HISKP)



Contribution ID: 8

Type: **not specified**

## Inferring effective couplings with Restricted Boltzmann Machines

*Wednesday, 28 June 2023 15:30 (25 minutes)*

Restricted Boltzmann Machines (RBMs) are stochastic neural networks, known for learning a latent representation of the data and generating statistically similar new data. From the statistical physicist's point of view, an RBM is a highly familiar object: a disordered Ising spin Hamiltonian, in which the spins are distributed on a bipartite lattice. Such energy function can be expanded as an Ising-like Hamiltonian with interaction terms up to any desired order. In this work, we used RBMs to face a generalized Ising problem. First, we generated spin configurations with a generalized Ising Hamiltonian and used such configurations to train an RBM. Then, we inferred the coupling tensor of the effective Ising model learned in each case. It is shown that there is a direct equivalence between the RBM parameters and the interactions of the generalized Ising model. Moreover, considering that previous attempts to solve the inverse Ising model with RBMs were limited to 2-body interactions, our work extends such previous approaches as we demonstrate that RBMs can indeed capture high-order correlations.

**Primary authors:** NAVAS GOMEZ, Alfonso (Complutense University of Madrid); DECELLE, Aurélien (Universidad Complutense de Madrid); Dr SEOANE, Beatriz (Complutense University of Madrid); Dr FURTLEHNER, Cyril (Paris-Saclay University)

**Presenter:** NAVAS GOMEZ, Alfonso (Complutense University of Madrid)

Contribution ID: 9

Type: **not specified**

## Machine learning a fixed point action

*Wednesday, 28 June 2023 10:00 (25 minutes)*

Lattice gauge-equivariant convolutional neural networks (LGE-CNNs) can be used to form arbitrarily shaped Wilson loops and can approximate any gauge-covariant or gauge-invariant function on the lattice. Here we use LGE-CNNs to describe fixed point (FP) actions which are based on inverse renormalization group transformations. FP actions are classically perfect, i.e., they have no lattice artefacts on classical gauge-field configurations satisfying the equations of motion, and therefore possess scale invariant instanton solutions. FP actions are tree-level Symanzik-improved to all orders in the lattice spacing and can produce physical predictions with very small lattice artefacts even on coarse lattices. They may therefore provide a solution to circumvent critical slowing down towards the continuum limit.

**Primary author:** WENGER, Urs

**Co-authors:** IPP, Andreas (TU Wien); MÜLLER, David; HOLLAND, Kieran (University of the Pacific)

**Presenter:** WENGER, Urs

Contribution ID: 10

Type: **not specified**

## Machine learning a fixed point action

*Wednesday, 28 June 2023 10:30 (25 minutes)*

Lattice gauge-equivariant convolutional neural networks (LGE-CNNs) can be used to form arbitrarily shaped Wilson loops and can approximate any gauge-covariant or gauge-invariant function on the lattice. Here we use LGE-CNNs to describe fixed point (FP) actions which are based on inverse renormalization group transformations. FP actions are classically perfect, i.e., they have no lattice artefacts on classical gauge-field configurations satisfying the equations of motion, and therefore possess scale invariant instanton solutions. FP actions are tree-level Symanzik-improved to all orders in the lattice spacing and can produce physical predictions with very small lattice artefacts even on coarse lattices. They may therefore provide a solution to circumvent critical slowing down towards the continuum limit.

**Primary author:** HOLLAND, Kieran (University of the Pacific)

**Co-authors:** IPP, Andreas (TU Wien); MÜLLER, David; WENGER, Urs

**Presenter:** HOLLAND, Kieran (University of the Pacific)

Contribution ID: 11

Type: **not specified**

## Data-driven discovery of relevant information in many-body problems: from spin lattice models to quantum field simulators

*Thursday, 29 June 2023 11:30 (25 minutes)*

Recent advancements in large-scale computing and quantum simulation have revolutionized the study of strongly correlated many-body systems. These developments have granted us access to extensive data, including spatially resolved snapshots that contain comprehensive information about the entire many-body state. However, interpreting such data poses in general significant challenges, often relying on various assumptions. In this talk, I will demonstrate how unsupervised machine learning offers a versatile toolkit to tackle these difficulties. Specifically, I will present an unsupervised approach based on intrinsic dimension and spectral entropies of principal components for automatic discovery of relevant information in many-body snapshots. As illustrations, I will showcase two examples: (i) investigating critical phenomena in classical Ising models, and (ii) ranking experimental observations in a quantum field simulation far from equilibrium.

**Primary author:** VERDEL, Roberto (ICTP)

**Presenters:** VERDEL, Roberto (ICTP); VERDEL ARANDA, Roberto (The Abdus Salam International Centre for Theoretical Physics (ICTP))

Contribution ID: 12

Type: **not specified**

## Global and local symmetries in neural networks

*Tuesday, 27 June 2023 11:00 (25 minutes)*

Incorporating symmetries into neural network architectures has become increasingly popular. Convolutional Neural Networks (CNNs) leverage the assumption of global translational symmetry in the data to ensure that their predicted observable transforms properly under translations. Lattice gauge equivariant Convolutional Neural Networks (L-CNNs) [1] are designed to respect local gauge symmetry, which is an essential component in lattice gauge theories. This property makes them effective in approximating gauge covariant functions on a lattice. Since many observables exhibit additional global symmetries to translations, an extension of the L-CNN to a more general symmetry group, including e.g. rotations and reflections [2], is desirable.

In this talk, I will present some of the essential L-CNN layers and motivate why they can approximate gauge equivariant functions on a lattice. I will comment on the robustness of such a network against adversarial attacks along gauge orbits in comparison to a traditional CNN. Then, I will provide a geometric formulation of L-CNNs and show how convolutions in L-CNNs arise as a special case of gauge equivariant neural networks on  $SU(N)$  principal bundles. Finally, I will discuss how the L-CNN layers can be generalized to respect global rotations and reflections in addition to translations.

[1] M. Favoni, A. Ipp, D. I. Müller, D. Schuh, Phys. Rev. Lett. 128 (2022), 032003, [arXiv:2012.12901]

[2] J. Aronsson, D. I. Müller, D. Schuh [arXiv:2303.11448]

**Primary author:** SCHUH, Daniel (TU Wien)

**Co-authors:** IPP, Andreas (TU Wien); MÜLLER, David (TU Wien); ARONSSON, Jimmy (Chalmers University of Technology); FAVONI, Matteo (TU Vienna)

**Presenter:** SCHUH, Daniel (TU Wien)

Contribution ID: 13

Type: **not specified**

## Training a Gomoku-Agent using DRL

*Thursday, 29 June 2023 15:30 (25 minutes)*

Exploratory study of training a Gomoku-Agent (generalization of tic tac toe) using pure Deep Reinforcement Learning. Different training approaches and neural network architectures are studied. The performance of the resulting agents is compared to tree search based competitors of the Gomocup.

**Primary author:** HAJIZADEH, Ouraman

**Presenter:** HAJIZADEH, Ouraman

Contribution ID: 14

Type: **not specified**

## Visualizing the inner workings of L-CNNs

*Tuesday, 27 June 2023 10:00 (25 minutes)*

Lattice Gauge Equivariant Convolutional Neural Networks (L-CNNs) leverage convolutions with proper parallel transport and bilinear layers to combine basic plaquettes into arbitrarily shaped Wilson loops of growing length and area [1]. These networks provide a powerful framework for addressing challenging problems in lattice field theory.

In this talk, we explore the inner workings of L-CNNs, aiming to gain insight into the contributions of the different layers. Through visualization techniques, we analyze the patterns and structures of the Wilson loops that emerge, studying to what degree L-CNN architectures exhibit redundancy in the parameters. With our findings we aim to provide a deeper understanding of L-CNN behavior and improve its interpretability.

[1] M. Favoni, A. Ipp, D. I. Müller, D. Schuh, Phys. Rev. Lett. 128 (2022), 032003, [arXiv:2012.12901]

**Primary author:** IPP, Andreas (TU Wien)

**Co-authors:** SCHUH, Daniel (TU Wien); MÜLLER, David; FAVONI, Matteo (TU Vienna)

**Presenter:** IPP, Andreas (TU Wien)

Contribution ID: 15

Type: **not specified**

## Using equivariant neural networks as maps of gauge field configurations

*Tuesday, 27 June 2023 11:30 (25 minutes)*

Lattice gauge equivariant convolutional neural networks (L-CNNs) are neural networks consisting of layers that respect gauge symmetry. They can be used to predict physical observables [1], but also to modify gauge field configurations. The approach proposed here is to treat a gradient flow equation as a neural ordinary differential equation parametrized by L-CNNs. Training these types of networks with standard backpropagation usually requires to store the intermediate states of the flow time evolution, which can easily lead to memory saturation issues. A solution to this problem is offered by the adjoint sensitivity method. We present our derivation and test our approach on toy models.

[1] M. Favoni, A. Ipp, D. I. Müller, D. Schuh, Phys.Rev.Lett. 128 (2022), 032003, [arXiv:2012.12901]

**Primary author:** FAVONI, Matteo (TU Vienna)

**Co-authors:** IPP, Andreas (TU Wien); SCHUH, Daniel (TU Wien); MÜLLER, David

**Presenter:** FAVONI, Matteo (TU Vienna)



Contribution ID: 16

Type: **not specified**

## Path gradient estimators for CNFs in Lattice Gauge Theory

*Tuesday, 27 June 2023 16:00 (25 minutes)*

In recent work, we have developed continuous normalizing flows (CNFs) for lattice gauge theories. CNFs are well suited to address symmetrical problems due to the ease of implementing equivariances. We have demonstrated that CNFs can achieve state-of-the-art performance with few, but physically meaningful parameters.

In this talk, I will present our results for 4d Yang-Mills theory. Our architecture can substantially outperform any other proposed model on this task but is still insufficient to scale to physically relevant coupling values and lattice sizes. Particular emphasis will be put on low variance path gradient estimators to CNF. These gradient estimators are a powerful technique for doubly stochastic variational inference. They are low variance estimators which we demonstrate to improve the performance also in the case of the CNFs applied to gauge theory.

**Primary authors:** VAITL, Lorenz (TU Berlin); Dr KESSEL, Pan (Prescient Design); Dr BACCHIO, Simone (CyI); Dr SCHAEFER, Stefan (DESY)

**Presenter:** VAITL, Lorenz (TU Berlin)

Contribution ID: 17

Type: **not specified**

## Normalizing Flows for Effective String Theory

*Monday, 26 June 2023 15:30 (25 minutes)*

Effective String Theory (EST) is a non-perturbative framework used to describe confinement in Yang-Mills theory through the modeling of the interquark potential in terms of vibrating strings. An efficient numerical method to simulate such theories where analytical studies are not possible is still lacking. However, in recent years a new class of deep generative models called Normalizing Flows (NFs) has been proposed to sample lattice field theories more efficiently than traditional Monte Carlo methods. In this talk, we show a proof of concept of the application of NFs to EST regularized on the lattice. Namely, we use as case study the Nambu-Goto string in order to use the well-known analytical results of this theory as a benchmark for our methods.

**Primary author:** CELLINI, Elia (University of Turin/ INFN Turin)

**Co-authors:** Prof. CASELLE, Michele (University of Turin/ INFN Turin); Dr NADA, Alessandro (University of Turin/ INFN Turin); Prof. PANERO, Marco (University of Turin/ INFN Turin)

**Presenter:** CELLINI, Elia (University of Turin/ INFN Turin)

Contribution ID: 18

Type: **not specified**

## Gauge-equivariant multigrid neural networks

*Wednesday, 28 June 2023 12:00 (25 minutes)*

In the interesting physical limits, the numerical solution of the Dirac equation in an  $SU(3)$  gauge field suffers from critical slowing down, which can be overcome by state-of-the-art multigrid methods. We introduce gauge-equivariant neural networks that can learn the general paradigms of multigrid. These networks can perform as well as standard multigrid but are more general and therefore have the potential to address a larger range of research questions.

**Primary authors:** LEHNER, Christoph; WETTIG, Tilo (University of Regensburg)

**Presenter:** WETTIG, Tilo (University of Regensburg)

Contribution ID: 19

Type: **not specified**

## Trivializing map as a coarse-graining map

*Wednesday, 28 June 2023 09:30 (25 minutes)*

To deal with the topological freezing in gauge systems, we develop a variant of trivializing map proposed in Luecher 2019. We in particular consider the 2D U(1) pure gauge model, which is the simplest gauge system having the topology. The trivialization is divided into several stages that each stage corresponds to integrating out local degrees of freedom, and thus can be seen as a coarse-graining. The simulation using the map has gain in autocorrelation in wall clock time compared to conventional HMC that likely survives in the continuum limit.

**Primary author:** MATSUMOTO, Nobuyuki (RIKEN BNL)

**Presenter:** MATSUMOTO, Nobuyuki (RIKEN BNL)

Contribution ID: 20

Type: **not specified**

## Statistical mechanics of deep learning beyond the infinite-width limit

*Friday, 30 June 2023 11:00 (25 minutes)*

Decades-long literature testifies to the success of statistical mechanics at clarifying fundamental aspects of deep learning. Yet the ultimate goal remains elusive: we lack a complete theoretical framework to predict practically relevant scores, such as the train and test accuracy, from knowledge of the training data. Huge simplifications arise in the infinite-width limit, where the number of units  $N_\ell$  in each hidden layer ( $\ell = 1, \dots, L$ , being  $L$  the finite depth of the network) far exceeds the number  $P$  of training examples.

This idealisation, however, blatantly departs from the reality of deep learning practice, where training sets are larger than the widths of the networks. Here, we show one way to overcome these limitations.

The partition function for fully-connected architectures, which encodes information about the trained models, can be evaluated analytically with the toolset of statistical mechanics.

The computation holds in the thermodynamic limit where both  $N_\ell$  and  $P$  are large and their ratio  $\alpha_\ell = P/N_\ell$ , which vanishes in the infinite-width limit, is now finite and generic.

This advance allows us to obtain (i) a closed formula for the generalisation error associated to a regression task in a one-hidden layer network with finite  $\alpha_1$ ;

(ii) an approximate expression of the partition function for deep architectures (technically, via an effective action that depends on a finite number of order parameters); (iii) a link between deep neural networks in the proportional asymptotic limit and Student's  $t$  processes; (iv) a simple criterion to predict whether finite-width networks (with ReLU activation) achieve better test accuracy than infinite-width ones.

As exemplified by these results, our theory provides a starting point to tackle the problem of generalisation in realistic regimes of deep learning.

**Primary author:** ROTONDO, Pietro (University of Parma)

**Presenter:** ROTONDO, Pietro (University of Parma)

Contribution ID: 21

Type: **not specified**

## Machine Learning assisted real-time simulations with Complex Langevin

*Monday, 26 June 2023 12:00 (25 minutes)*

The direct simulation of the real-time dynamics of strongly correlated quantum fields remains an open challenge in both nuclear and condensed matter physics due to the notorious sign problem. Here we present a novel machine-learning inspired strategy [1] that significantly improves complex Langevin simulations of quantum real-time dynamics.

Our approach combines two central ingredients: 1) we revive the idea of deploying a kernel in the stochastic Langevin dynamics to improve the convergence properties of the approach. 2) Taking inspiration from the reinforcement learning paradigm of machine learning we propose to systematically find optimal kernels based on prior information.

The fact that our approach infuses the complex Langevin simulation with system specific prior information promises a way to overcome the NP-hardness of the sign-problem for which no generic solution approach is believed to exist.

[1] D. Alevestad, R. Larsen, A.R. JHEP 04 (2023) 057 (<https://arxiv.org/abs/2211.15625>)

**Primary author:** ROTHKOPF, Alexander (University of Stavanger)

**Presenter:** ROTHKOPF, Alexander (University of Stavanger)

Contribution ID: 22

Type: **not specified**

## Disentangling representations in Restricted Boltzmann Machines without adversaries

*Thursday, 29 June 2023 15:00 (25 minutes)*

A goal of unsupervised machine learning is to build representations of complex high-dimensional data, with simple relations to their properties. Such disentangled representations make it easier to interpret the significant latent factors of variation in the data, as well as to generate new data with desirable features. The methods for disentangling representations often rely on an adversarial scheme, in which representations are tuned to avoid discriminators from being able to reconstruct information about the data properties (labels). Unfortunately, adversarial training is generally difficult to implement in practice. In this talk, I will describe a simple, effective way of disentangling representations without any need to train adversarial discriminators, and apply our approach to Restricted Boltzmann Machines, one of the simplest representation-based generative models. Our approach relies on the introduction of adequate constraints on the weights during training, which allows us to concentrate information about labels on a small subset of latent variables. The effectiveness of the approach is illustrated with four examples: the CelebA dataset of facial images, the two-dimensional Ising model, the MNIST dataset of handwritten digits, and the taxonomy of protein families. In addition, we show how our framework allows for analytically computing the cost, in terms of the log-likelihood of the data, associated with the disentanglement of their representations.

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**Co-author:** Dr MONASSON, Remi

**Presenter:** FERNANDEZ DE COSSIO DIAZ, Jorge (ENS PARIS)

Contribution ID: 23

Type: **not specified**

## Mitigating signal-to-noise problems using learned contour deformations

*Monday, 26 June 2023 10:00 (25 minutes)*

Complex contour deformations of the path integral have previously been used to mitigate sign problems associated with non-zero chemical potential and real-time evolution in lattice field theories. This talk details their application to lattice calculations where the vacuum path integral is instead real and positive – allowing Monte Carlo sampling – but observables are afflicted with a sign and signal-to-noise problem. This is for example the case for many lattice calculations targeting QCD phenomenology. In this context, contour deformations allow one to rewrite observables to minimize sign fluctuations while preserving their expectation value. We apply machine learning techniques to define and optimize families of contour deformations for  $SU(N)$  variables and demonstrate exponential improvements in the signal-to-noise ratio of Wilson loops in proof-of-principle applications to  $U(1)$  and  $SU(N)$  lattice gauge theories.

**Primary author:** KANWAR, Gurtej (University of Bern)

**Presenter:** KANWAR, Gurtej (University of Bern)



Contribution ID: 24

Type: **not specified**

## Stochastic normalizing flows as out-of-equilibrium transformations

*Thursday, 29 June 2023 10:00 (25 minutes)*

Normalizing Flows are a class of deep generative models recently proposed as a promising alternative to conventional Markov Chain Monte Carlo in lattice field theory simulations. Such architectures provide a new way to avoid the large autocorrelations that characterize Monte Carlo simulations close to the continuum limit. In this talk we explore the novel concept of Stochastic Normalizing Flows (SNFs), in which neural-network layers are combined with out-of-equilibrium stochastic updates: in particular, we show how SNFs share the same theoretical framework of Monte Carlo simulations based on Jarzynski's equality. The latter is a well-known result in non-equilibrium statistical mechanics which proved to be highly efficient in the computation of free-energy differences in lattice gauge theories. We discuss the most appealing features of this extended class of generative models using numerical results in the  $\phi^4$  scalar field theory in 2 dimensions.

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**Presenter:** NADA, Alessandro (Università degli Studi di Torino)

Contribution ID: 25

Type: **not specified**

## The Restricted Boltzman Machine: Phase Diagram, Generation and Interpretability

*Wednesday, 28 June 2023 15:00 (25 minutes)*

The Restricted Boltzmann Machine (RBM) was introduced many years ago as an extension of the Boltzmann Machine (BM) (or the inverse Ising problem). In BM, one aimed to infer the couplings of an Ising model such that it reproduces the statistics of a given dataset. Within such an approach, it is necessary to specify the structure of the interacting variables in order to correctly reproduce the moments of an empirical target distribution. The RBM is more general in this sense and can potentially balance correlation statistics of any order thanks to its bipartite structure that mixes observable nodes and latent ones that are not observed in the dataset. In this talk, I will introduce this generative model and show how it can model very complex datasets. I will then discuss in detail the various characteristics such as the phase diagram, the learning behavior, and the connection between the parameters of the models and the effective interactions between variables.

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**Presenter:** DECELLE, Aurélien (Universidad Complutense de Madrid)

Contribution ID: 26

Type: **not specified**

## Deforming complex-valued distributions via machine learning

*Tuesday, 27 June 2023 09:30 (25 minutes)*

Sign problems in lattice QCD prevent us from non-perturbatively calculating many important properties of dense nuclear matter both in and out of equilibrium. In this talk, I will discuss recent developments in numerical methods for alleviating sign problems in lattice field theories. In these methods, the distribution function in the path integral is modified via machine learning such that the sign problem is tamed. I will demonstrate these methods in the  $\phi^4$  scalar field theory and the Thirring model in 1+1-dimensions.

**Primary author:** YAMAUCHI, Yukari (The Institute for Nuclear Theory)

**Presenter:** YAMAUCHI, Yukari (The Institute for Nuclear Theory)

Contribution ID: 27

Type: **not specified**

## Instantaneous gauge field generation with approximate trivializing maps

*Friday, 30 June 2023 12:00 (25 minutes)*

While approximations of trivializing field transformations for lattice path integrals were considered already by early practitioners, more recent efforts aimed at ergodicity restoration and thermodynamic integration formulate trivialization as a variational generative modeling problem. This enables the application of modern machine learning algorithms for optimization over expressive parametric function classes, such as deep neural networks. After a brief review of the origins and current status of this research program, I will focus on spectral coupling flows as a particular parameterization of gauge-covariant field diffeomorphisms. The concept will be introduced by explicitly constructing a systematically improvable semi-analytic solution for SU(3) gauge theory in (1+1)d, followed by a discussion and outlook on recent results in (3+1)d from a proof-of-principle application of machine-learned flow maps.

**Primary authors:** HACKETT, Daniel (Massachusetts Institute of Technology, United States); ROMERO-LOPEZ, Fernando (MIT); URBAN, Julian (Institute for Theoretical Physics Heidelberg); SHANAHAN, Phiala (Massachusetts Institute of Technology, United States)

**Presenter:** URBAN, Julian (Institute for Theoretical Physics Heidelberg)

Contribution ID: 28

Type: **not specified**

## Learning about the Hubbard Model

*Monday, 26 June 2023 11:30 (25 minutes)*

The Hubbard model is a foundational model of condensed matter physics. Formulated on a honeycomb lattice it provides a crude model for graphene; on a square lattice it may model high-Tc superconductors. I will present first-principles numerical results characterizing the quantum phase transition of the Hubbard model on a honeycomb lattice between a Dirac semimetal to an antiferromagnetic Mott insulator, and then present some results away from half-filling, where the model develops a sign problem.

Phase transition:

2005.11112 Phys.Rev.B 102 (2020) 24, 245105

2105.06936 Phys.Rev.B 104 (2021) 15, 155142

Sign problem:

2006.11221 Phys.Rev.B 103 (2021) 12, 125153

2203.00390 Phys.Rev.B 106 (2022) 12, 125139

**Primary author:** BERKOWITZ, Evan (Forschungszentrum Jülich)

**Presenter:** BERKOWITZ, Evan (Forschungszentrum Jülich)

Contribution ID: 29

Type: **not specified**

## Thimbology and Qubits

*Monday, 26 June 2023 10:30 (25 minutes)*

I will review a method for taming sign problems in lattice field theory called “path integral contour deformations”, or, “thimbology”. I will describe how to use thimbology to understand qubit systems, and argue that machine-learned contour deformations may offer a competitive route to simulating qubits in real-time.

**Primary author:** WARRINGTON, Neill (Institute for Nuclear Theory)

**Presenter:** WARRINGTON, Neill (Institute for Nuclear Theory)

Contribution ID: 30

Type: **not specified**

## Scalar field Restricted Boltzmann Machine as an ultraviolet regulator

*Friday, 30 June 2023 09:30 (25 minutes)*

Restricted Boltzmann Machines (RBMs) are well known tools used in Machine Learning to learn probability distribution functions from data. We analyse RBMs with scalar fields on the nodes from the perspective of lattice field theory. Starting with the simplest case of Gaussian fields, we show that the RBM acts as an ultraviolet regulator, with the cutoff determined by either the number of hidden nodes or a model mass parameter. We verify these ideas in the scalar field case, where the target distribution is known, and explore implications for cases where it is not known using the MNIST data set.

**Primary authors:** LUCINI, Biagio (Swansea University); PARK, Chan Ju (Swansea University); Prof. AARTS, Gert (Swansea University, UK)

**Presenter:** PARK, Chan Ju (Swansea University)

Contribution ID: 31

Type: **not specified**

## EFT-inspired generative models for simulations of quantum field theories

*Friday, 30 June 2023 11:30 (25 minutes)*

In this talk, we present new neural network architectures inspired by effective field theories, designed to improve the scaling of the training cost for the generation of lattice field theory configurations using normalizing flows. Initially, we deal with poor acceptance rates in simulations of large lattices for scalar field theory in two dimensions and then discuss possible extensions to gauge theories in higher dimensions.

**Primary author:** KOMIJANI, Javad (ETH Zurich)

**Presenter:** KOMIJANI, Javad (ETH Zurich)



Contribution ID: 32

Type: **not specified**

## Discussion

*Friday, 30 June 2023 14:00 (1h 30m)*