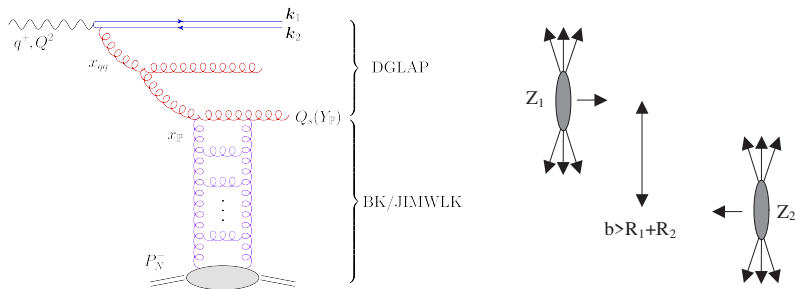


Probing gluon saturation via diffractive jets in nucleus-nucleus UPCs

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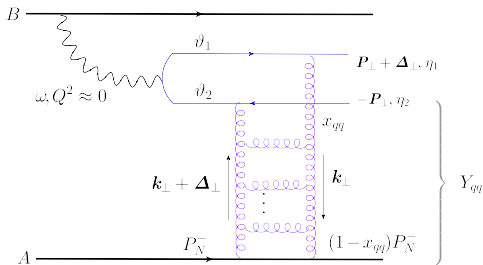
with A.H. Mueller, D.N. Triantafyllopoulos, and S.-Y. Wei
arXiv:2304.12401



- Diffractive dijet production in photon-nucleus interactions at high energy:
a golden channel to study saturation
 - electron-nucleus DIS at the future EIC (LHeC ?)
 - nucleus-nucleus UPCs at the LHC: this talk
- Why diffraction ?
 - since controlled by strong scattering in the black disk limit
 - it lives at the hardest scale where scattering is still strong
 - if saturation exists ($Q_s \gg \Lambda$), this scale is Q_s
- Why jets (hard jets/hadrons with $P_\perp \gg Q_s$) ?
 - easy to measure; a priori well described by collinear factorisation
- Why should saturation be relevant for hard jets/hadrons ?
 - to have strong scattering, the hard dijets must be accompanied by semi-hard radiation (at least, one additional gluon with $K_\perp \sim Q_s$)
 - such a 2+1 event can be computed in the CGC
- Collinear (actually, TMD) factorisation emerges from the CGC

Exclusive dijets in AA UPCs

- Colour dipole picture: $q\bar{q}$ dipole undergoing **elastic** scattering
- Coherent process: target nucleus does not break: $\Delta_{\perp} \sim 1/R_A \sim 30 \text{ GeV}$
- Hard dijets: $P_{\perp} \gg Q_s \gg \Delta_{\perp}$, $\vartheta_1 \sim \vartheta_2 \sim 1/2$



$$\omega = \frac{P_{\perp}}{2} (e^{\eta_1} + e^{\eta_2})$$

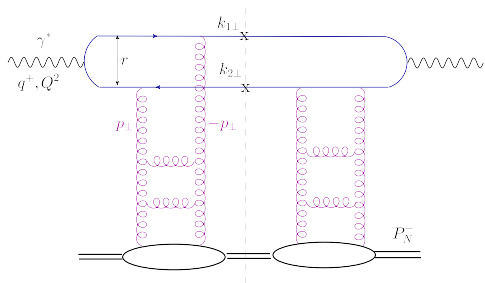
$$x_{q\bar{q}} P_N^- = \frac{P_{\perp}}{\sqrt{2}} (e^{-\eta_1} + e^{-\eta_2})$$

$\eta_1 \simeq \eta_2$: can have any sign

- Pomeron rapidity gap: $Y_{q\bar{q}} = \ln \frac{1}{x_{q\bar{q}}}$: phase-space for target evolution
- Pseudo-rapidity gap: $\Delta\eta_{q\bar{q}} = \eta_{1,2} - \eta_A = \ln \frac{2}{x_{q\bar{q}}} + \ln \frac{P_{\perp}}{M_N}$: measurable

Exclusive dijets is higher twist

- Elastic scattering: $\sigma_{\text{el}}(P_{\perp}) \propto |T_{q\bar{q}}(r)|^2$ with $r \sim 1/P_{\perp} \ll 1/Q_s$
- Small dipole \implies weak scattering (“colour transparency”)



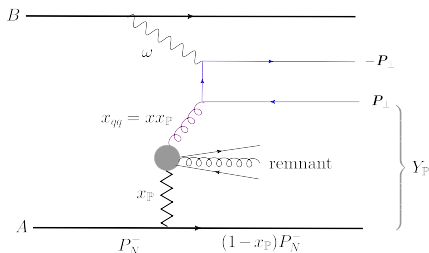
$$T_{q\bar{q}}(r) \simeq \begin{cases} r^2 Q_s^2, & \text{for } rQ_s \ll 1 \\ 1, & \text{for } rQ_s \gtrsim 1 \end{cases}$$

$$\sigma_{\text{el}}(P_{\perp}) \propto \frac{Q_s^4}{P_{\perp}^6}$$

- “Higher twist”: strongly suppressed at large $P_{\perp} \gg Q_s$
- For comparison: inclusive dijet cross-section: $\sigma_{\text{incl}}(P_{\perp}) \propto \frac{Q_s^2}{P_{\perp}^4}$
- Exclusive dijets are **truly rare events**: ignored in the collinear factorisation

Collinear factorisation: leading twist

- The $q\bar{q}$ dipole does not directly couple to the Pomeron
 - it rather couples to a gluon component of the Pomeron
- The final state also contains a set of “remnants” with overall gluon quantum numbers and $k_{\perp} \ll P_{\perp}$: **semi-inclusive diffractive dijets**



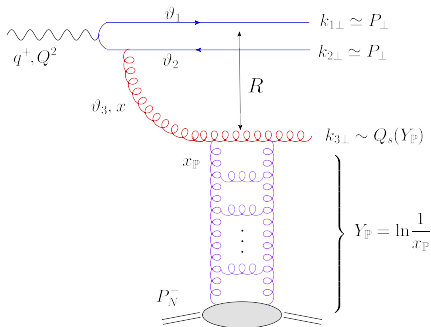
- The gluon carries a fraction $x = \frac{x_{q\bar{q}}}{x_P}$
- Pomeron rapidity gap $Y_P = \ln \frac{1}{x_P}$
- Distribution in $x \leq 1$ & in $Y_P \leq Y_{q\bar{q}}$
- DGLAP evolution for the remnants

$$\frac{d\sigma_{2+1}^{AB \rightarrow q\bar{q}XAB}}{d\eta_1 d\eta_2 d^2\mathbf{P} dY_P} = \omega \frac{dN_B}{d\omega} H(\eta_1, \eta_2, P_{\perp}^2) x G_P^A(x, x_P, P_{\perp}^2) + (A \leftrightarrow B)$$

- Energy flux \times Hard factor \times Gluon distribution of the Pomeron (diff PDF)

Colour dipole picture: 2+1 jets

- In collinear factorisation, $xG_{\mathbb{P}}(x, x_{\mathbb{P}}, P_{\perp}^2)$ is a “black box”
 - for a proton target: determined via fits to HERA
 - for a nuclear target: resort on models (Pomeron flux, shadowing ...)
- For small $x_{\mathbb{P}} \lesssim 10^{-2}$ and $A = 200$, one has $Q_s(A, Y_{\mathbb{P}}) \gtrsim 1 \text{ GeV}$
 $\implies xG_{\mathbb{P}}(x, x_{\mathbb{P}}, P_{\perp}^2)$ can be computed from first principles: CGC
- Leading order: 2 hard ($P_{\perp} \gg Q_s$) and 1 semi-hard ($K_{\perp} \sim Q_s$) jets



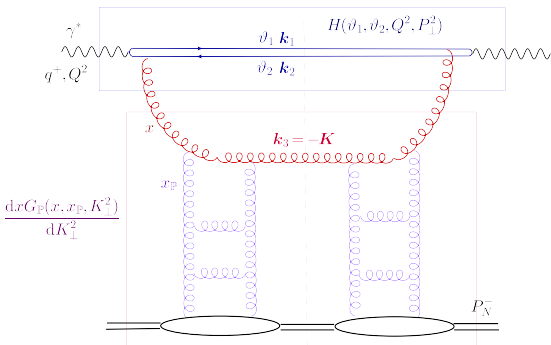
$$R \sim \frac{1}{Q_s} \gg r \sim \frac{1}{P_{\perp}}$$

- Effective gluon-gluon dipole
- Strong scattering: $T_{gg}(R, Y_{\mathbb{P}}) \sim 1$
- Leading twist: $\sim Q_s^2/P_{\perp}^4$

TMD factorisation for diffractive 2+1 jets

(E.I., A.H. Mueller, D.N. Triantafyllopoulos, *Phys.Rev.Lett.* 128 (2022) 20)

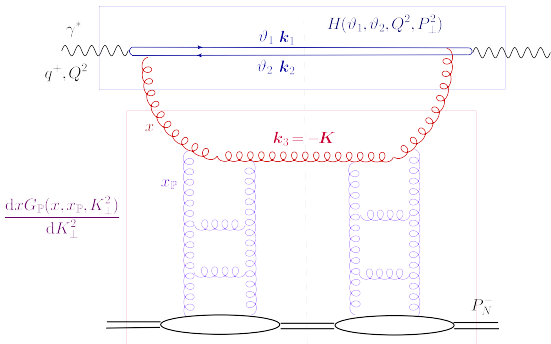
- At high $P_{\perp} \gg Q_s$, collinear factorisation emerges from the dipole picture
 - the gluon can alternatively be seen as a part of the Pomeron
 - essential condition: the gluon is relatively soft $\vartheta_3 \sim \frac{Q_s^2}{Q^2} \ll 1$



- Actually: the “unintegrated” (TMD) version of collinear factorisation

TMD factorisation for diffractive 2+1 jets

$$\frac{d\sigma_{2+1}^{\gamma^* A \rightarrow q\bar{q}gA}}{d\vartheta_1 d\vartheta_2 d^2\mathbf{P} d^2\mathbf{K} dY_{\mathbb{P}}} = H_{T,L}(\vartheta_1, \vartheta_2, Q^2, P_{\perp}^2) \frac{dx G_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}}$$



- **The hard factor:** the same as for **inclusive dijets** (same physics)

$$H_T = \alpha_{\text{em}} \alpha_s \left(\sum e_f^2 \right) \vartheta_1 \vartheta_2 (\vartheta_1^2 + \vartheta_2^2) \frac{1}{P_{\perp}^4} \quad \text{when } Q^2 \ll P_{\perp}^2$$

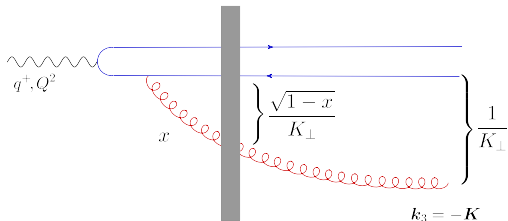
The Pomeron UGD: a diffractive TMD

$$\frac{dx G_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2 K} = \frac{S_{\perp}(N_c^2 - 1)}{4\pi^3} \underbrace{\frac{[\mathcal{G}(x, x_{\mathbb{P}}, K_{\perp}^2)]^2}{2\pi(1-x)}}_{\text{occupation number } \Phi}$$

- Explicitly computed in terms of the gluon-gluon dipole amplitude $T_{gg}(R, Y_{\mathbb{P}})$

$$\mathcal{G} = \mathcal{M}^2 \int_0^{\infty} dR R J_2(K_{\perp} R) K_2(\mathcal{M} R) T_{gg}(R, Y_{\mathbb{P}}) \quad \text{with} \quad \mathcal{M}^2 \equiv \frac{x}{1-x} K_{\perp}^2$$

- the gluon dipole size R is limited by the virtuality: $R \lesssim 1/M$



- Operatorial definition clarified by *Hatta, Xiao, and Yuan (2205.08060)*

The Pomeron UGD (2)

- Strong scattering: $R \gtrsim \frac{1}{Q_s}$, but $R \lesssim \frac{\sqrt{1-x}}{K_\perp} \implies K_\perp^2 \lesssim (1-x)Q_s^2$
- Effective saturation momentum: $\tilde{Q}_s^2(x, Y_{\mathbb{P}}) = (1-x)Q_s^2(Y_{\mathbb{P}})$

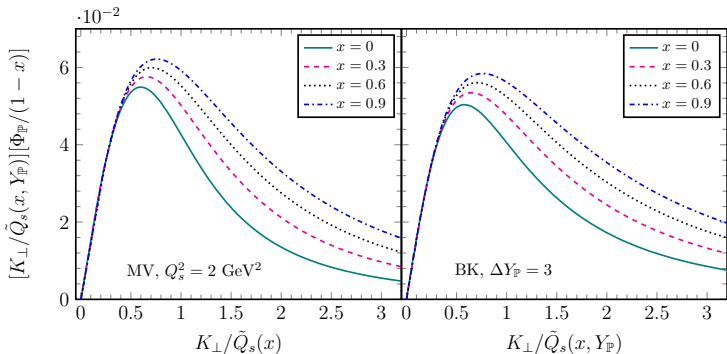
$$\Phi(x, x_{\mathbb{P}}, K_\perp^2) \simeq (1-x) \begin{cases} 1, & K_\perp \lesssim \tilde{Q}_s(x) \\ \frac{\tilde{Q}_s^4(x)}{K_\perp^4}, & K_\perp \gg \tilde{Q}_s(x) \end{cases}$$

- Very fast decrease $\sim 1/K_\perp^4$ at large gluon momenta $K_\perp \gg \tilde{Q}_s(x)$
 - bulk of the distribution lies in the saturation domain at $K_\perp \lesssim \tilde{Q}_s(x)$
- Contrast with the WW UGD (inclusive dijets): $\Phi_{WW} \sim Q_s^2/K_\perp^2$ at high K_\perp
- Suppression when $x \rightarrow 1$: endpoint of the phase-space for gluon emission
- Geometric scaling after dividing through $1-x$: a function of $K_\perp/\tilde{Q}_s(x)$

Numerical results

(E.I., A.H. Mueller, D.N. Triantafyllopoulos, S.-Y. Wei, arXiv:2207.06268)

- Occupation number Φ multiplied by K_{\perp}/\tilde{Q}_s and divided by $1-x$
- Pronounced peak at $K_{\perp} \simeq \tilde{Q}_s$: **diffraction is controlled by saturation**



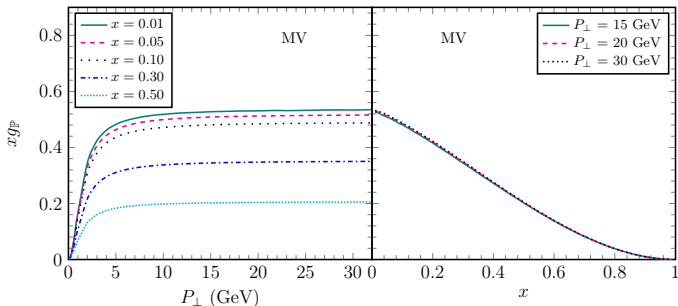
- **BK evolution of $T_{gg}(R, Y_{\mathbb{P}})$** : evolution of $\Phi_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp})$ in $x_{\mathbb{P}}$ and K_{\perp}
 - increasing $Q_s^2(Y_{\mathbb{P}})$ & approximate geometric scaling

The gluon diffractive PDF

- By integrating the gluon momentum K_{\perp} : the usual collinear factorisation

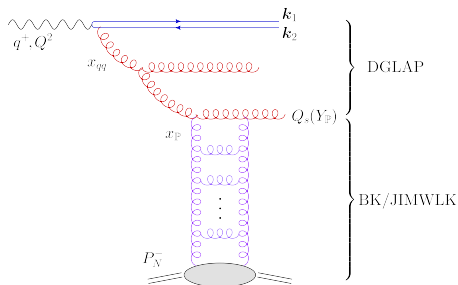
$$xG_{\mathbb{P}}(x, x_{\mathbb{P}}, P_{\perp}^2) \equiv \int^{P_{\perp}} d^2\mathbf{K} \frac{dx G_{\mathbb{P}}^A(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}} \propto (1-x)^2 Q_s^2(A, Y_{\mathbb{P}})$$

- ... but with an **explicit result** for the gluon diffractive PDF.
- The integral is rapidly converging and effectively **cut off at** $K_{\perp} \sim \tilde{Q}_s(x)$
- The $(1-x)^2$ vanishing at the end point is a hallmark of saturation



The quantum evolution of the Pomeron

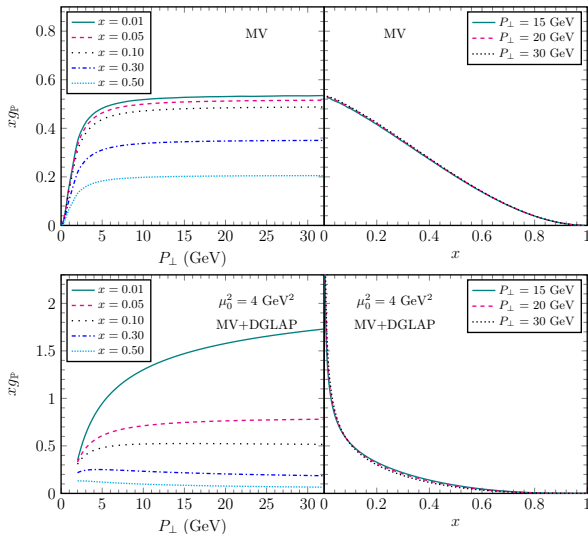
- The **unintegrated** distrib. (the gluon diff TMD) undergoes **BK/JIMWLK**
 - the evolution of the internal structure of the Pomeron (colour sources)
 - this affects the dependencies upon $x_{\mathbb{P}}$ and K_{\perp} , but not upon x
- The **integrated** distribution (the gluon diff PDF) obeys **DGLAP**
 - the evolution of the partons emitted by the Pomeron
 - this affects the dependencies upon x and P_{\perp} , but not upon $x_{\mathbb{P}}$



- additional DGLAP gluons
- intermediate transverse momenta
 $Q_s \ll k_{\perp} \ll P_{\perp}$

- The solution to BK acts as a **source** in the DGLAP equation

Adding DGLAP

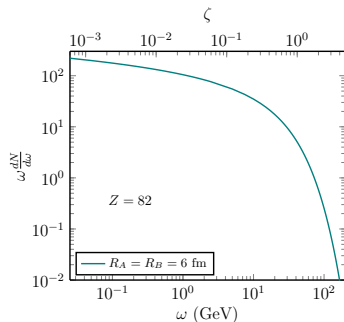
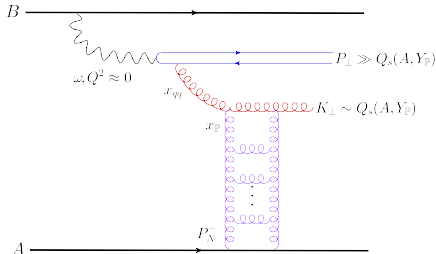


- increase for very small $x \leq 0.01$, slight decrease for $x > 0.05$
- when $x \rightarrow 1$, the distribution vanishes even faster

Back to AA UPCs (1)

$$\frac{d\sigma_{2+1}^{AB \rightarrow q\bar{q}gAB}}{d\eta_1 d\eta_2 d^2\mathbf{P} d^2\mathbf{K} dY_{\mathbb{P}}} = \omega \frac{dN_B}{d\omega} H(\eta_1, \eta_2, P_{\perp}^2) \frac{dx G_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}} + (A \leftrightarrow B)$$

- LHC: $\sqrt{s_{NN}} = 2E_N = 5 \text{ TeV}$, yet $\sqrt{s_{\gamma N}} = \sqrt{4\omega_{\max} E_N} \simeq 650 \text{ GeV}$

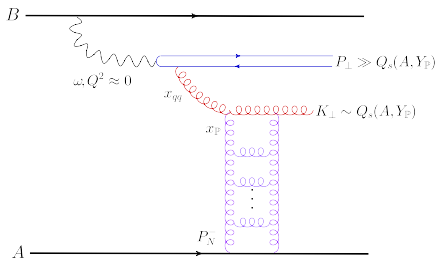


- quasi-real photon: virtuality $Q^2 = (\omega/\gamma)^2$ with $\gamma = \text{Lorentz factor}$
- upper energy cutoff: $b \sim \frac{1}{Q} > 2R_A \Rightarrow \omega < \frac{\gamma}{2R_A} \equiv \omega_{\max} \simeq 40 \text{ GeV}$

Back to AA UPCs (2)

$$\frac{d\sigma_{2+1}^{AB \rightarrow q\bar{q}gAB}}{d\eta_1 d\eta_2 d^2\mathbf{P} d^2\mathbf{K} dY_{\mathbb{P}}} = \omega \frac{dN_B}{d\omega} H(\eta_1, \eta_2, P_{\perp}^2) \frac{dx G_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}} + (A \leftrightarrow B)$$

- LHC: Very hard dijets $P_{\perp} \geq 15 \text{ GeV} \Rightarrow$ non-forward physics: $x_{q\bar{q}} \gtrsim 0.005$



$$\omega = P_{\perp} (e^{\eta_1} + e^{\eta_2})/2$$

$$x_{q\bar{q}} E_N = P_{\perp} (e^{-\eta_1} + e^{-\eta_2})/2$$

$$P_{\perp} \sim \omega_{\max} \Rightarrow |\eta_{1,2}| \lesssim 1$$

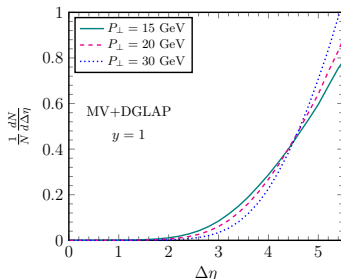
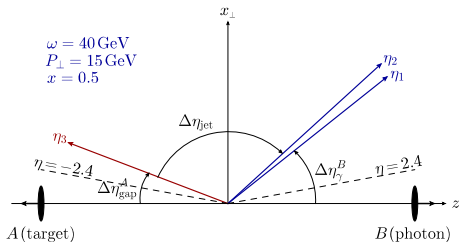
$$x_{\mathbb{P}} = \frac{x_{q\bar{q}}}{x} \text{ is even larger}$$

- Not the ideal small $x_{\mathbb{P}}$ set-up! **Decreasing P_{\perp}** would greatly help!
- $K_{\perp} \sim Q_s \sim 1 \div 2 \text{ GeV}$: not really a jet! **Could be measured as a hadron**
- Hard dijet imbalance $|\mathbf{k}_1 + \mathbf{k}_2| \gg K_{\perp}$ controlled by **final-state radiation**

A high-energy event

- Assume the photon to be a **right mover**: it has been emitted by nucleus B
- Optimal conditions**: highest $\omega = 40$ GeV, lowest $P_{\perp} = 15$ GeV, large $x = 0.5$

$$x_{\mathbb{P}} = 2x_{q\bar{q}} \simeq 4 \times 10^{-3}, \quad Y_{\mathbb{P}} = 5.4, \quad \eta_{1,2} \simeq 1, \quad \Delta\eta_{\text{jet}} = 2.7$$



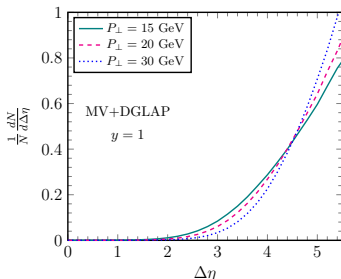
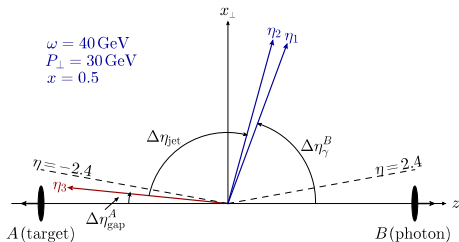
$$\Delta\eta_{\text{jet}} = \eta_{1,2} - \eta_3 = \ln \frac{2(1-x)}{x} + \ln \frac{P_{\perp}}{K_{\perp}} \gtrsim \ln \frac{2P_{\perp}}{Q_s} \simeq 2 \div 3$$

- The 3rd “jet” could have been seen as a hadron by CMS: $|\eta_3| < |\eta_{\text{max}}| = 2.4$

A high-energy event

- Assume the photon to be a **right mover**: it has been emitted by nucleus B
- Optimal conditions**: highest $\omega = 40$ GeV, lowest $P_{\perp} = 15$ GeV, large $x = 0.5$

$$x_{\mathbb{P}} = 2x_{q\bar{q}} \simeq 0.02, \quad Y_{\mathbb{P}} = 4, \quad \eta_{1,2} \simeq 0.3, \quad \Delta\eta_{\text{jet}} = 3.4$$



$$\Delta\eta_{\text{jet}} = \eta_{1,2} - \eta_3 = \ln \frac{2(1-x)}{x} + \ln \frac{P_{\perp}}{K_{\perp}} \gtrsim \ln \frac{2P_{\perp}}{Q_s} \simeq 2 \div 3$$

- Yet, CMS measured $P_{\perp} = 30$ GeV... so they missed it! ([arXiv:2205.00045](https://arxiv.org/abs/2205.00045))

A more inclusive observable

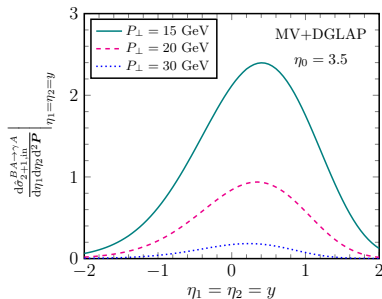
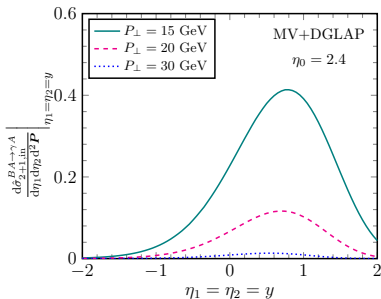
- What is the cross-section to observe the 3rd jet in a **hadronic tracker with rapidity acceptance η_0** (with any K_\perp) ? (e.g. $\eta_0 = 2.4$ at CMS)
 - integrate the 3rd jet over K_\perp up to P_\perp
 - any $|\eta_3| < \eta_0 \implies$ integrate over $x > x_0$
 - assume $\eta_1 = \eta_2 \equiv y$ for simplicity

$$\left. \frac{d\hat{\sigma}_{2+1,\text{in}}^{BA \rightarrow \gamma A}}{d\eta_1 d\eta_2 d^2\mathbf{P}} \right|_{\eta_0} = \omega \frac{dN_B}{d\omega} \int_{x_0}^1 \frac{dx}{x} x G_{\mathbb{P}}^A(x, x_{\mathbb{P}}, P_\perp^2), \quad x_0 = \frac{1}{1 + \frac{Q_s}{2P_\perp} e^{y+\eta_0}}$$

- “Reduced cross-section”: we removed the trivial hard factor $H \propto 1/P_\perp^4$.
- Plot as a function of y for various values of P_\perp and η_0
- As before, we assume the photon to be a **right mover**

The cross-section for seeing the 3rd jet

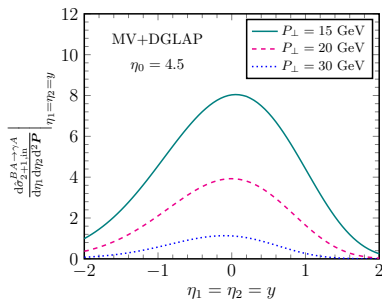
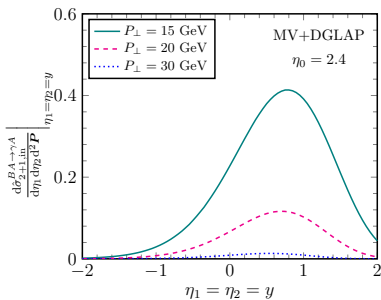
$$\left. \frac{d\hat{\sigma}_{2+1,\text{in}}^{BA \rightarrow \gamma A}}{d\eta_1 d\eta_2 d^2\mathbf{P}} \right|_{\eta_0} = \omega \frac{dN_B}{d\omega} \int_{x_0}^1 \frac{dx}{x} x G_{\mathbb{P}}^A(x, x_{\mathbb{P}}, P_{\perp}^2), \quad x_0 = \frac{1}{1 + \frac{Q_s}{2P_{\perp}} e^{y+\eta_0}}$$



- Suppression at **large positive y** due to the energy cutoff in the photon flux
- Suppression at **large negative y** and also at large P_{\perp} because
 - x_0 increases when y decreases and/or P_{\perp} increases
 - $x G_{\mathbb{P}}^A(x, x_{\mathbb{P}}, P_{\perp}^2)$ vanishes like $(1-x)^2$ when $x \rightarrow 1$

The cross-section for seeing the 3rd jet

$$\left. \frac{d\hat{\sigma}_{2+1,\text{in}}^{BA \rightarrow \gamma A}}{d\eta_1 d\eta_2 d^2\mathbf{P}} \right|_{\eta_0} = \omega \frac{dN_B}{d\omega} \int_{x_0}^1 \frac{dx}{x} x G_{\mathbb{P}}^A(x, x_{\mathbb{P}}, P_{\perp}^2), \quad x_0 = \frac{1}{1 + \frac{Q_s}{2P_{\perp}} e^{y+\eta_0}}$$

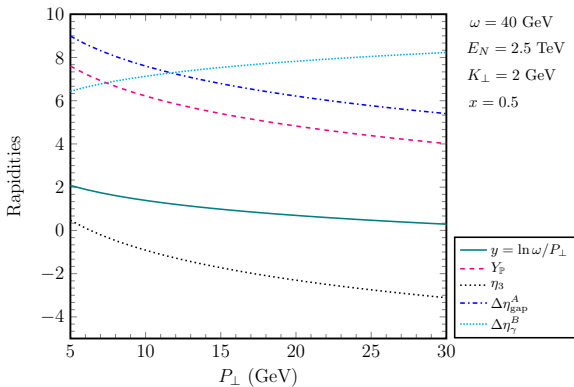


- Slight bias in favour of **positive** y (dijets in the direction of the photon)
- ... which however decreases when **increasing** P_{\perp} and/or η_0
- By observing the hard dijets **alone**, one cannot decide the photon direction

Why is the 3rd jet so useful

- Experimentally observing the semi-hard, 3rd jet would be **highly beneficial**
- Distinguish the nucleus which emitted the photon from the target nucleus
 - the third jet propagates opposite to the photon
 - one could deduce the photon energy ω , hence the value of $x_{q\bar{q}}$
- Confirm the **physical picture expected in pQCD/CGC**
 - a semi-hard transverse momentum $K_{\perp} \sim Q_s \sim 1 \div 2 \text{ GeV}$
 - a large pseudo-rapidity separation $\Delta\eta_{\text{jet}} \gtrsim 2 \div 3$ from the hard dijets
- ... hence the phenomenon of **gluon saturation**
- It would allow one to deduce the Pomeron gap: $Y_{\mathbb{P}} = \ln \frac{1}{x_{q\bar{q}}} - \ln \frac{1}{x}$
- ... hence the importance of **high energy evolution**

Can one measure jets with lower P_{\perp} ?



$$\omega = P_{\perp} e^y$$

$$x_{q\bar{q}} E_N = P_{\perp} e^{-y}$$

$$Y_{\mathbb{P}} = \ln \frac{1}{x_{q\bar{q}}} - \ln \frac{1}{x}$$

$$y - \eta_3 = \ln \frac{2(1-x)}{x} + \ln \frac{P_{\perp}}{K_{\perp}}$$

- Reducing P_{\perp} increases the chances to detect the 3rd jet & improves the case for saturation
 - increases $\eta_{1,2} \equiv y$, decreases $\Delta \eta = y - \eta_3$, increases $Y_{\mathbb{P}}$
- For $P_{\perp} \leq 10 \text{ GeV}$, the 3rd jet would propagate at nearly central rapidities !