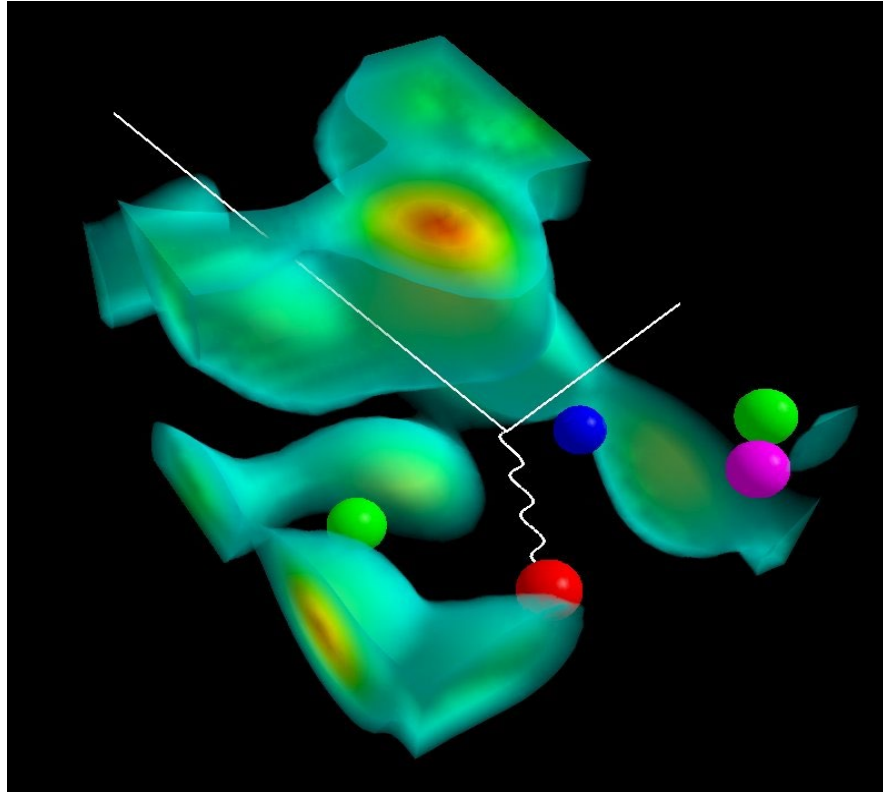


PDFs and GPDs of Light Nuclei



Anthony W. Thomas

GPD Workshop

Trento – 11-30pm November 10th 2022

Outline

- I. The EMC Effect – deep-inelastic structure of nuclei is *different*

- II. Test the SRC explanation of the EMC effect in the deuteron

- III. Structure functions in ^3He and ^3H
– analysis of the Marathon experiment

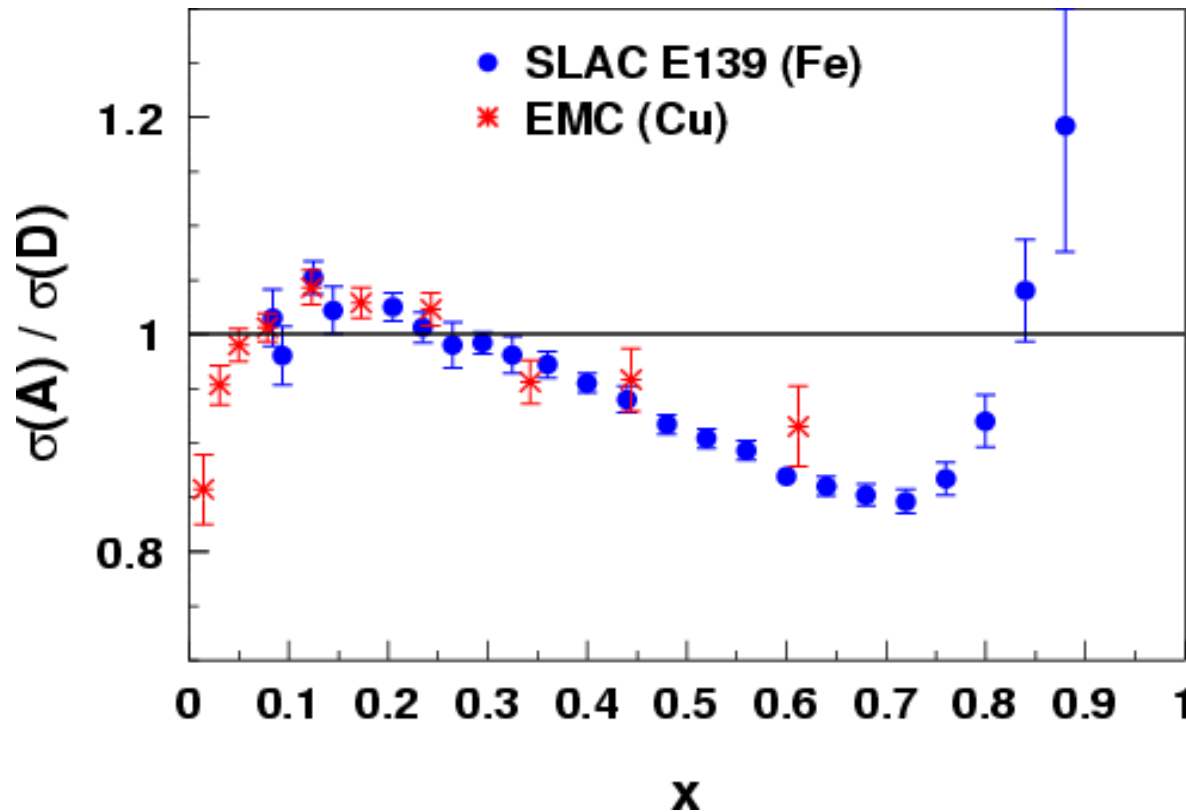
- IV. GPDs as a probe of medium modification in ^4He

The EMC Effect



The EMC Effect: Nuclear PDFs

- Observation stunned and electrified the HEP and Nuclear communities 39 years ago
- What is it that alters the quark momentum in the nucleus?



J. Ashman *et al.*, *Z. Phys. C57*, 211 (1993)

J. Gomez *et al.*, *Phys. Rev. D49*, 4348 (1994)

Short-range correlations (SRC) or mean-field modification?

Mean-Field Calculations for Finite Nuclei

(There is also a spin dependent EMC effect - as large as unpolarized)

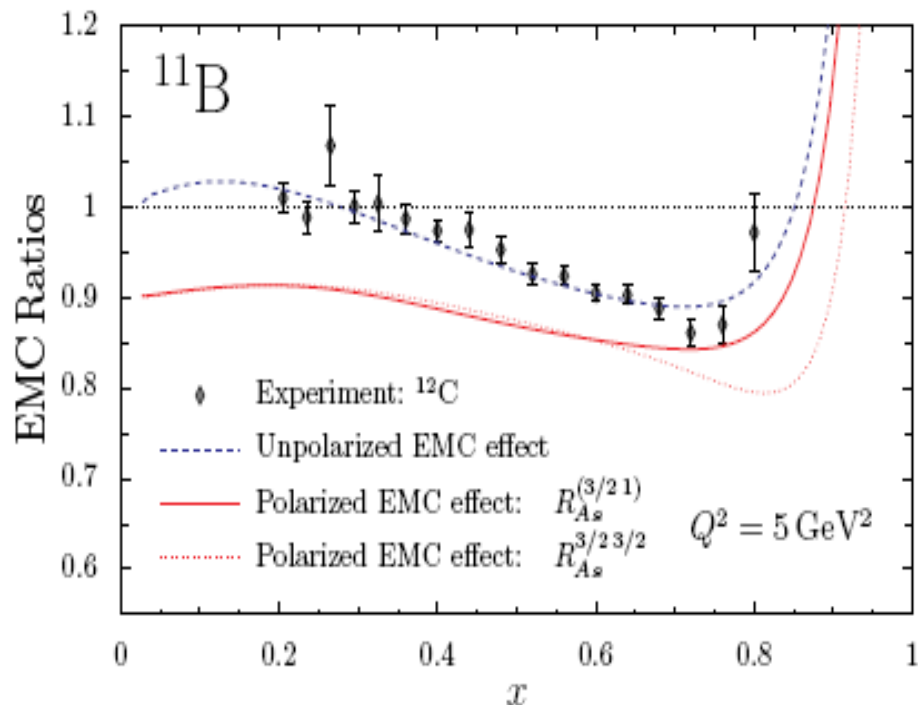


FIG. 7: The EMC and polarized EMC effect in ^{11}B . The empirical data is from Ref. [31].

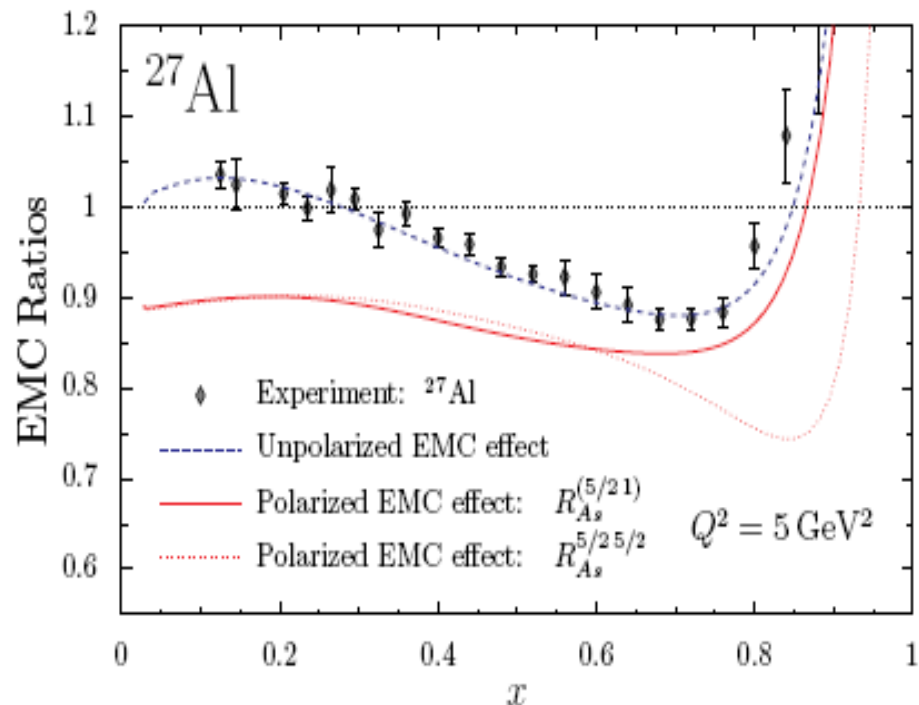
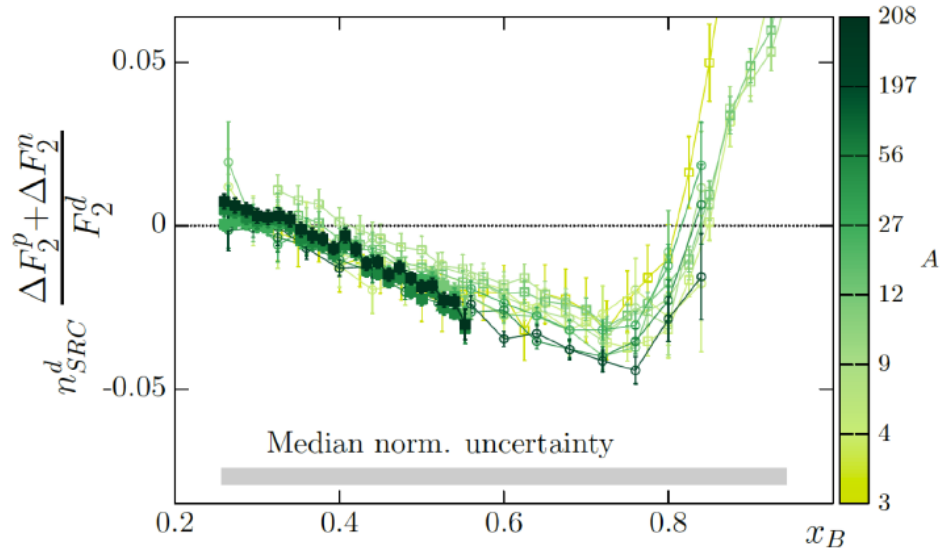
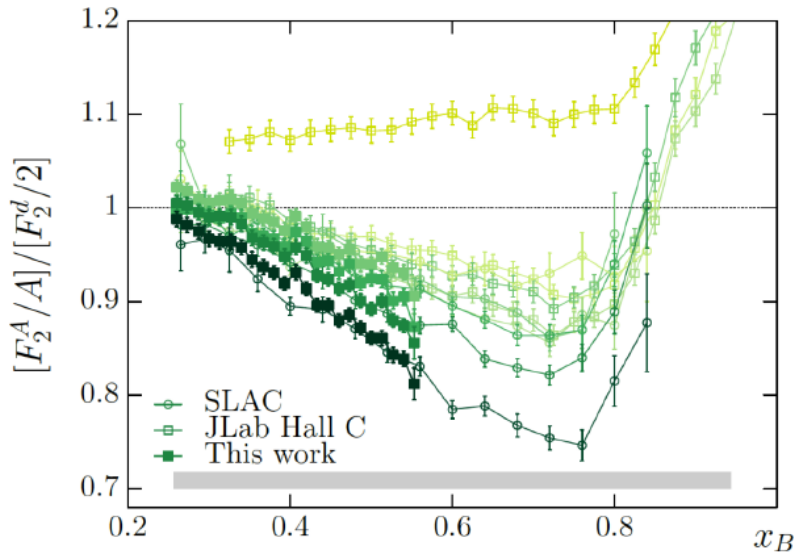


FIG. 9: The EMC and polarized EMC effect in ^{27}Al . The empirical data is from Ref. [31].

Linear relation of # in SRC vs Slope of EMC effect

SRC explain the EMC effect

B. Schmookler *et al.*, Nature 566 (2019) 354-358.

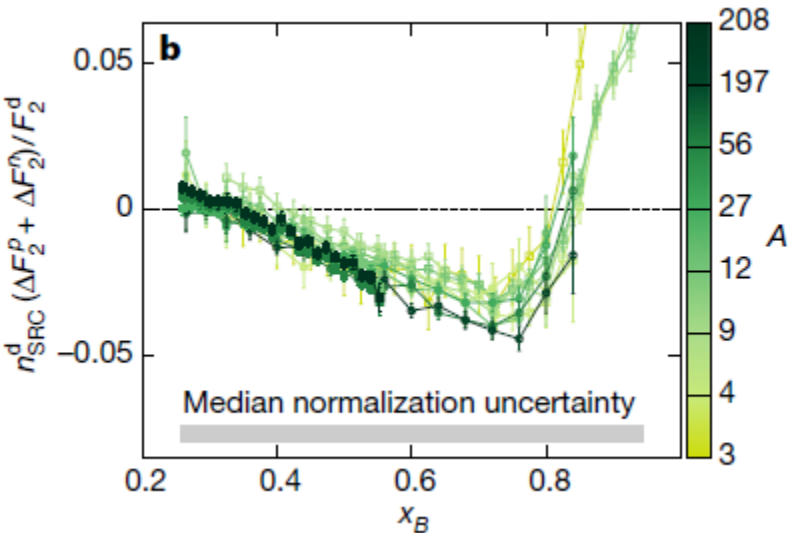


$$F_2^A = (Z - n_{SRC}^A)F_2^p + (N - n_{SRC}^A)F_2^n + n_{SRC}^A(F_2^{p*} + F_2^{n*})$$

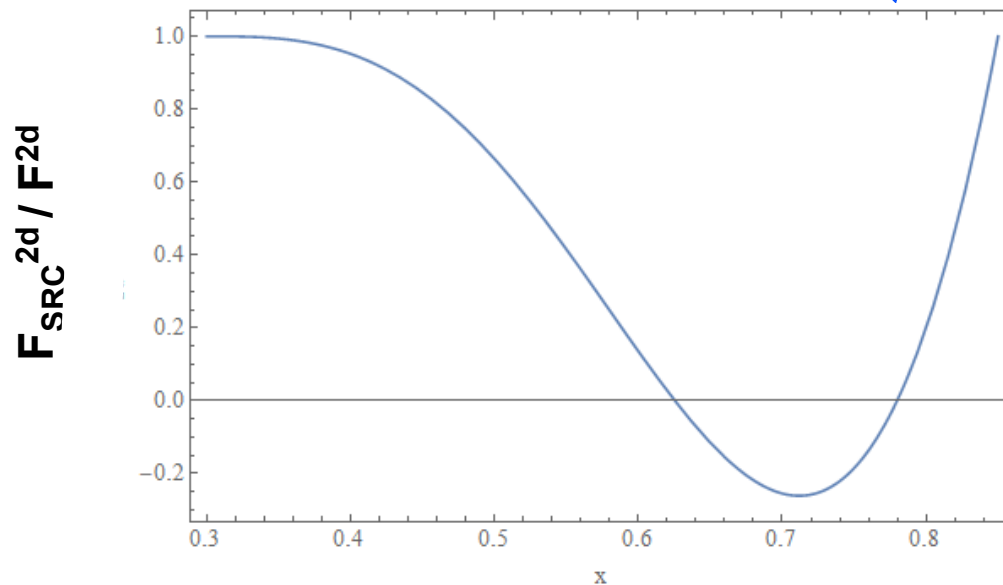
$$= ZF_2^p + NF_2^n + n_{SRC}^A(\Delta F_2^p + \Delta F_2^n),$$

Entire EMC effect from the change in SF of nucleons in SRC

Further: change in F_2 is dramatic in SRC approach



- Does not look so bad but n^d_{SRC} is of order 0.03 (p > 0.3 GeV: only ~80 MeV off-shell)
- Hence suppression of structure of correlated nucleons is greater than or of order 100% in the valence region



Such a dramatic change does not appear viable

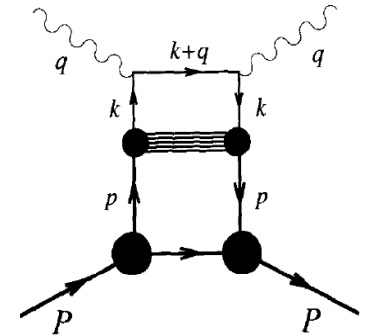
Wang *et al.*, Phys Rev Lett 125 (2000) 262002

The Deuteron



Simple Model calculation of F_2^D

$$q^D(x) = \frac{1}{2\pi^2} \int dy dp^2 (\mathcal{A}_0 \chi_0 + \mathcal{A}_1 \cdot p \chi_1 + \mathcal{A}_1 \cdot q \chi_2)$$



Free nucleon: $q^N(x/y) = 4M \chi_0^{\text{on}} + 4M^2 \chi_1^{\text{on}} + 4p \cdot q \chi_2^{\text{on}}$

Deuteron: $q^D(x) = \int_x^1 \frac{dy}{y} \varphi(y) q^N(x/y) + \delta^{(\mathcal{A})} q^D(x) + \delta^{(x)} q^D(x)$

$$\delta^{(x)} q^D(x) = \frac{1}{2\pi^2} \int dy dp^2 (\mathcal{A}_0 \chi_0^{\text{off}} + \mathcal{A}_1 \cdot p \chi_1^{\text{off}} + \mathcal{A}_1 \cdot q \chi_2^{\text{off}})$$



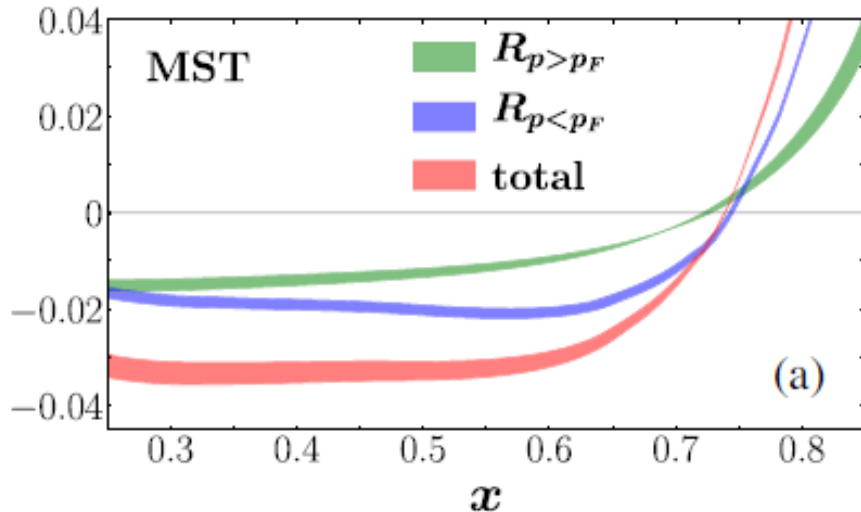
Off-shell effect in PDF

Nuclear correction from wave function

$$\delta^{(\mathcal{A})} q^D(x)$$

$$\begin{aligned} &= \frac{M_D}{2} \int_x^1 dy \int_{-\infty}^{p_{\text{max}}^2} dp^2 \left\{ \left[\frac{1}{2} \left(1 - \frac{E_p}{p_0} \right) q^N(x/y) \right. \right. \\ &+ \left. \left(\frac{E_p}{M_D} \chi_1^{\text{on}} - \frac{P \cdot q}{M_D^2} \chi_2^{\text{on}} \right) (p^2 - M^2) \right] C \\ &+ \left[-2M \chi_0^{\text{on}} + 2p^2 \chi_1^{\text{on}} \right. \\ &+ \left. \left(1 - y - \frac{E_p}{M_D} \right) P \cdot q \chi_2^{\text{on}} \right] P \\ &+ \left[M \chi_0^{\text{on}} + M^2 \chi_1^{\text{on}} \right. \\ &+ \left. \left. \frac{M^2}{p^2} \left(1 - y - \frac{E_p}{M_D} \right) P \cdot q \chi_2^{\text{on}} \right] D \right\} \end{aligned} \quad (8)$$

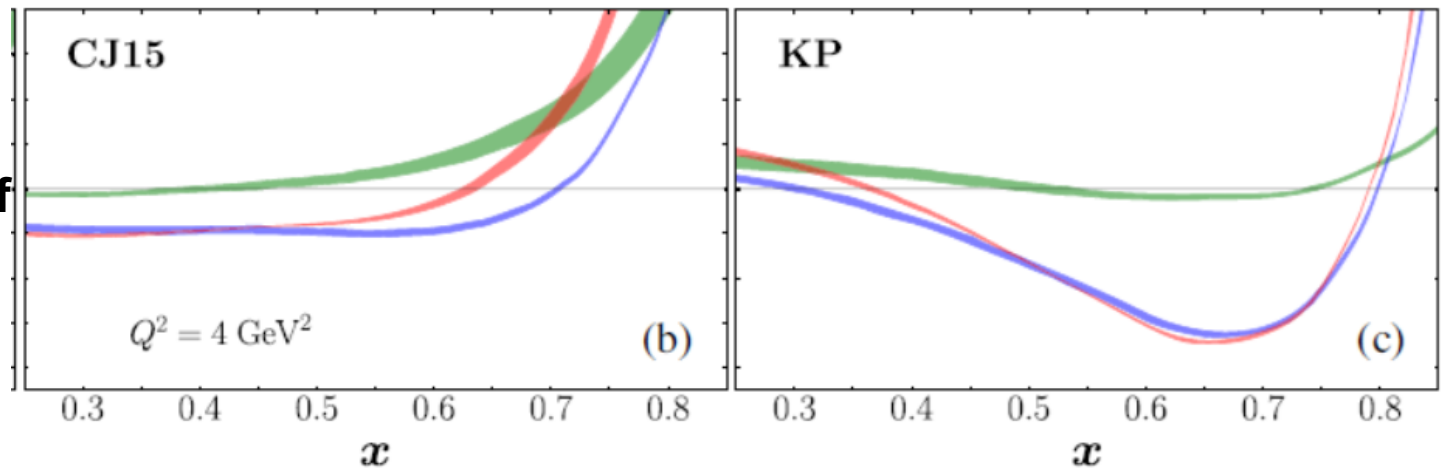
Careful study of the EMC effect in the deuteron



Microscopic model of Melnitchouk *et al.*, shows little of valence EMC effect in D arises from nucleons in SRC

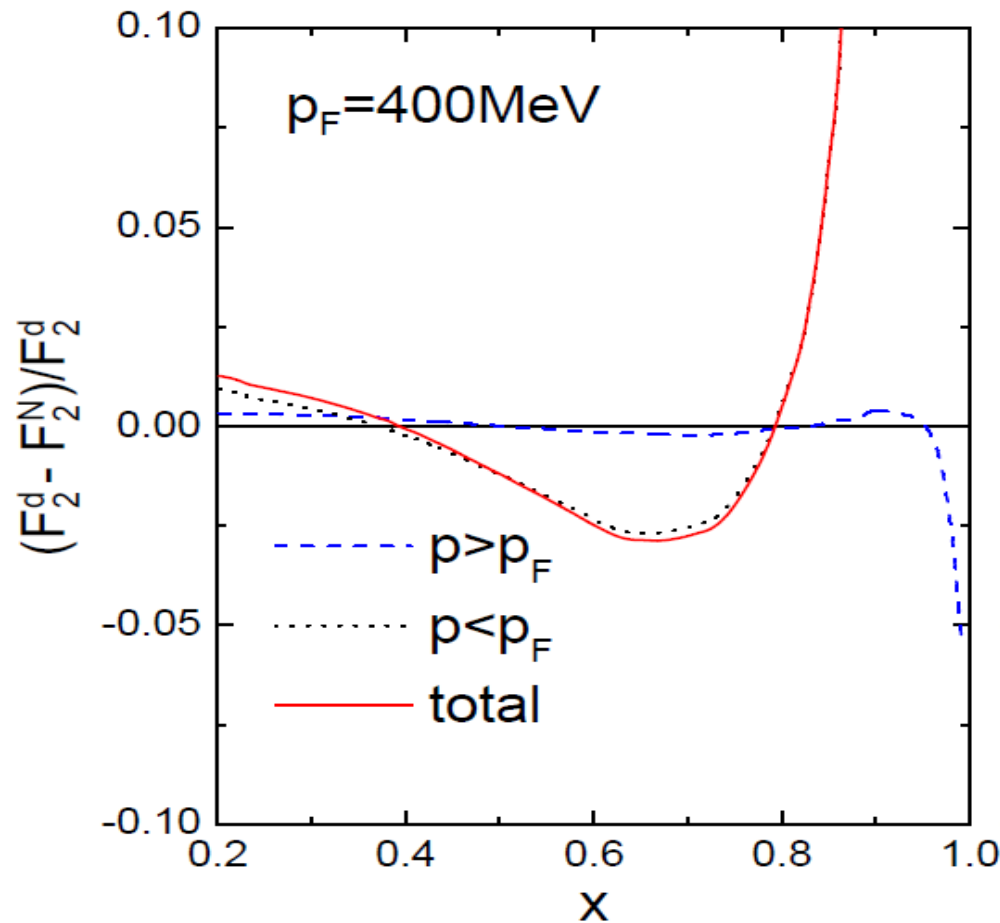
$$p_F = 300 \text{ MeV}/c$$

Even more emphatic in off-shell models of Kulagin-Petti and CTEQ-JLab

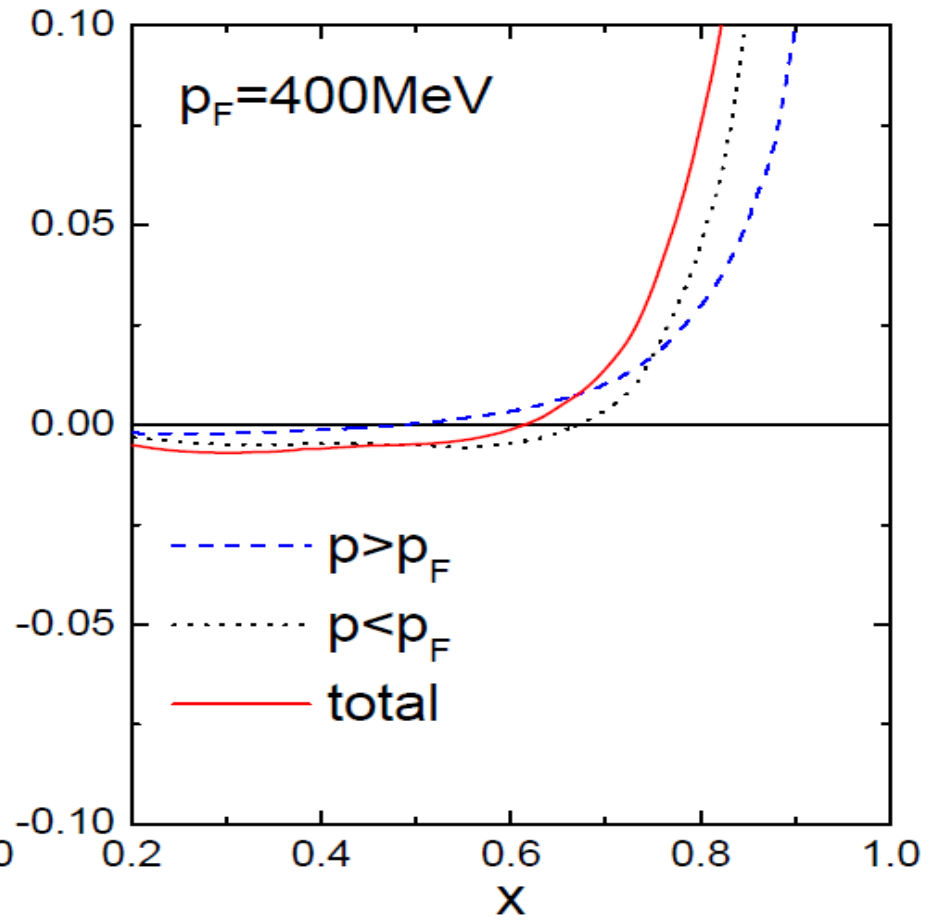


Wang *et al.*, Phys Rev Lett 125 (2020) 262002

$$p_F = 400 \text{ MeV}/c$$



(a) Kulagin-Petti



(b) CJ15

Analysis of the Marathon experiment



Isvector EMC Effect from Global QCD Analysis with MARATHON Data

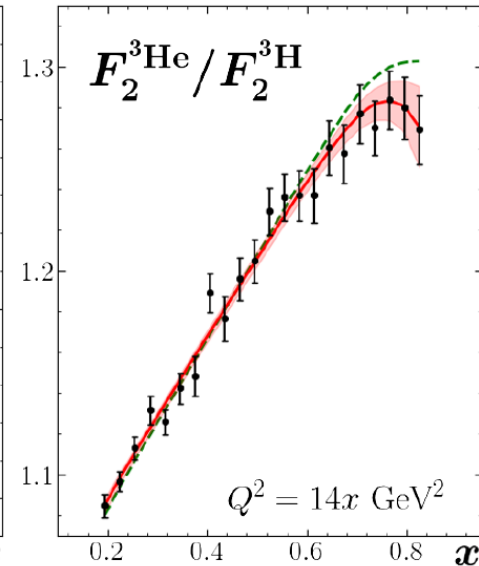
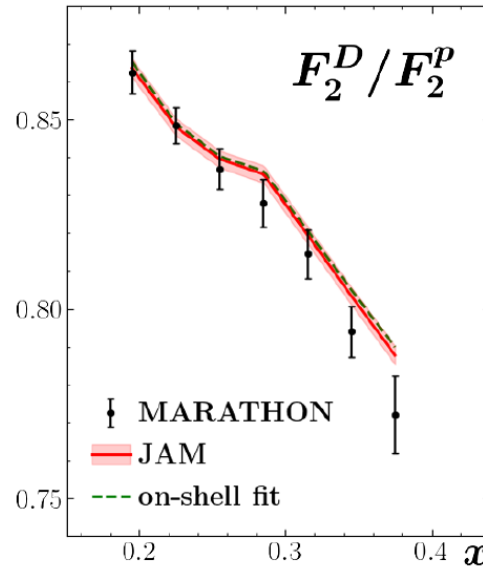
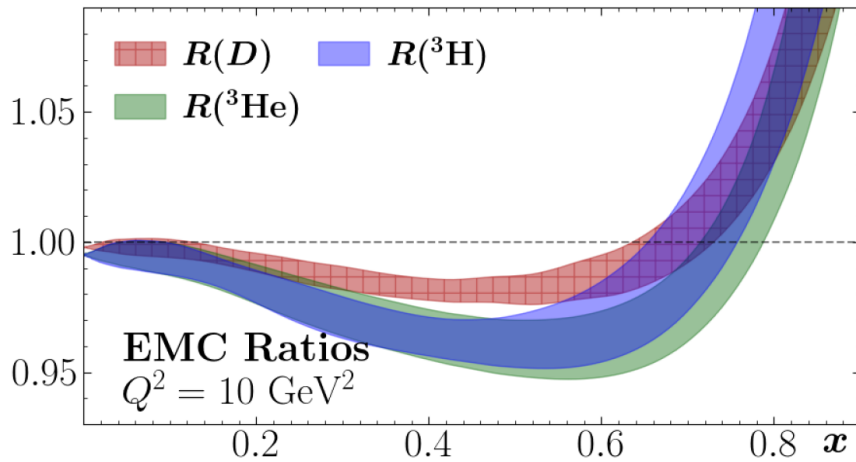
C. Cocuzza,¹ C. E. Keppel², H. Liu³, W. Melnitchouk², A. Metz,¹ N. Sato,² and A. W. Thomas⁴

PHYSICAL REVIEW LETTERS **127**, 242001 (2021)

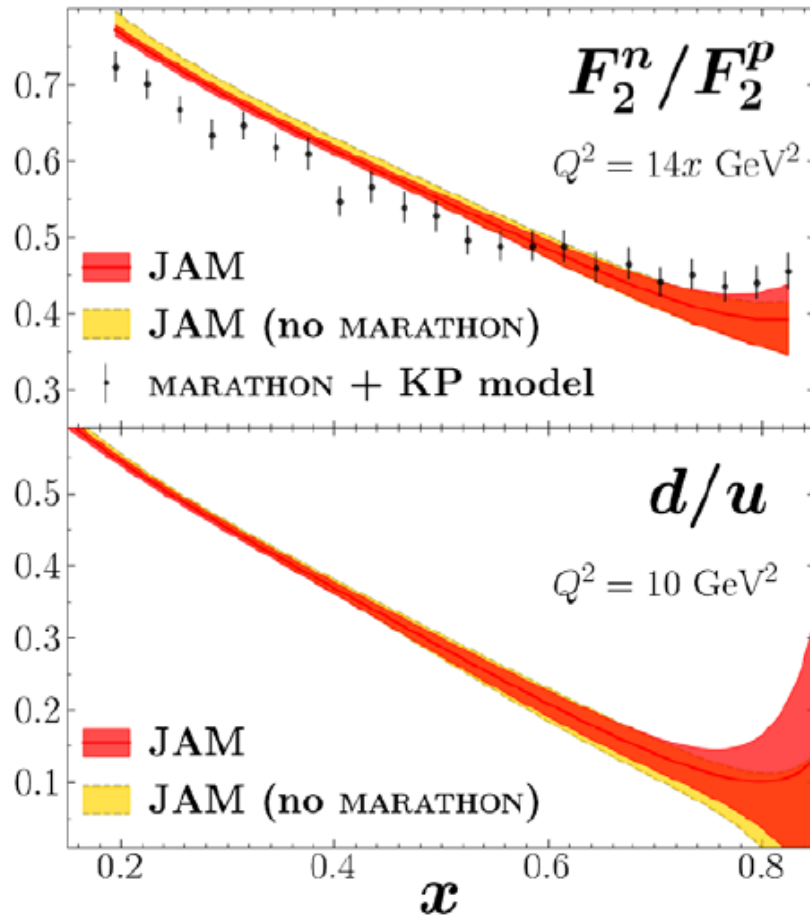
- **Remarkable measurement with a tritium target at JLab has given us important data on DIS in ^3H**
Abrams et al., Phys. Rev. Lett. 128 (2022) 13, 132003
- **In combination with earlier data on ^3He this provides new insight into potential isovector effects in nuclear DIS**
- **In a relativistic mean-field treatment of the EMC effect for nuclei with $N > Z$ this shifts momentum from *all* u quarks to *all* d quarks**
- **Along with CSV this provides a major correction in the context of the NuTeV anomaly**
I. C. Cloët et al., Phys. Rev. Lett. 102, 252301 (2009)

Results for D and $^3\text{He}/^3\text{H}$ Ratio

Analysis of Cocuzza et al., including allowance for isovector nuclear corrections



d/u ratio extracted from the data

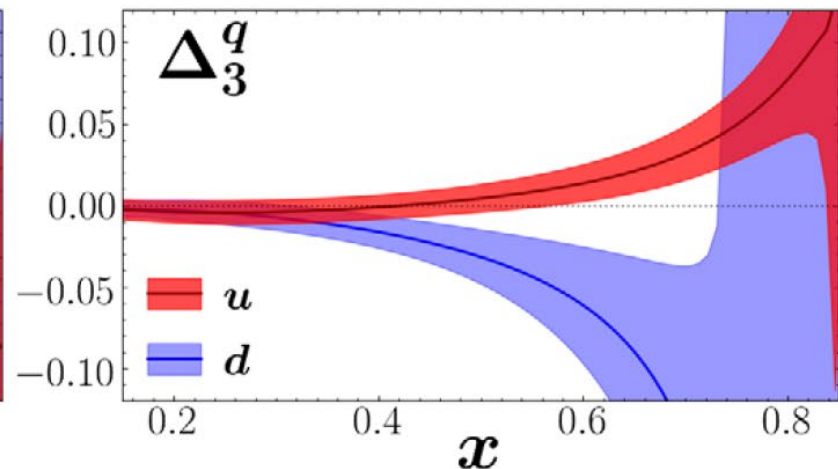
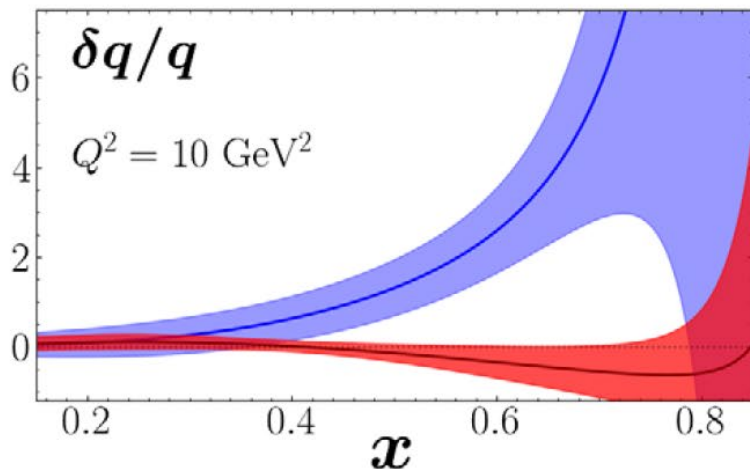


- W^\pm asymmetry data has reduced the capacity of Marathon to uniquely fix d/u
- However, it CAN provide unique insight into nuclear effects

Evidence for a Non-zero isovector effect

Parametrize off-shell effects respecting isospin symmetry in terms of q interacting with spectator nucleons

e.g. $\delta u_{p/D} = \delta d_{n/D}, \quad \delta d_{p/D} = \delta u_{n/D}, \quad \delta u_{p/^3\text{He}} = \delta d_{n/^3\text{H}}, \quad \delta d_{p/^3\text{He}} = \delta u_{n/^3\text{H}}$
 $\delta u_{p/^3\text{H}} = \delta d_{n/^3\text{He}}, \quad \delta d_{p/^3\text{H}} = \delta u_{n/^3\text{He}}$

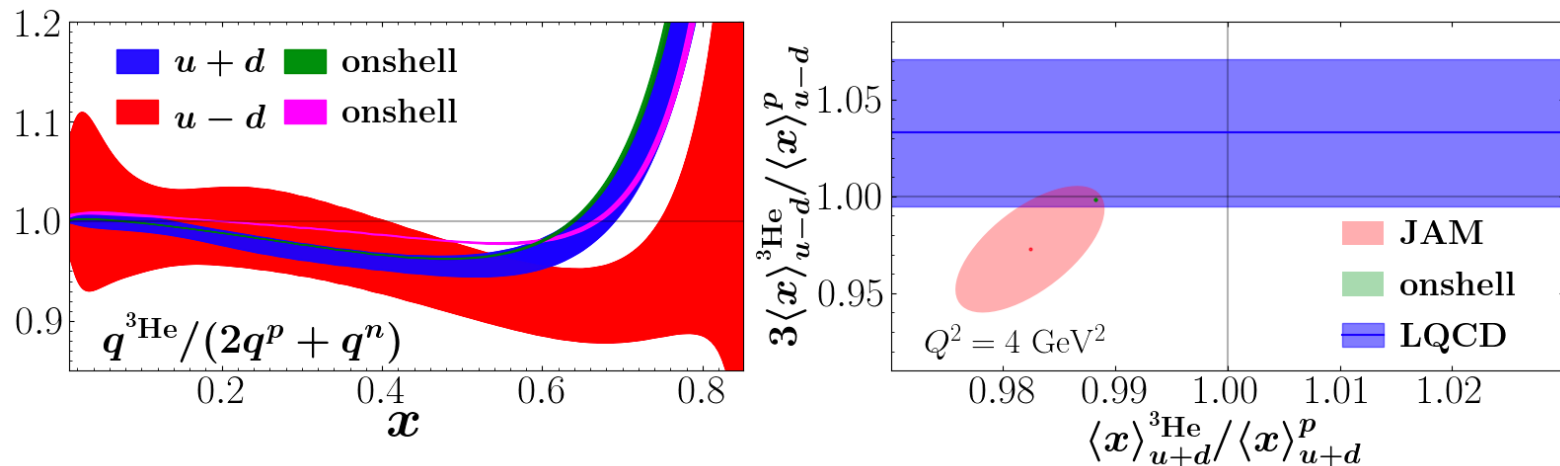


$$\Delta_3^q \equiv \frac{q_{p/^3\text{H}} - q_{p/^3\text{He}}}{q_{p/^3\text{H}} + q_{p/^3\text{He}}}$$

Would be zero without an isovector effect

Preliminary new result

- Exciting proposal to use lattice data to constrain/inform PDF analysis, from Detmold et al., **PRL 126, 202001 (2021)**
- Calculated u-d (connected contribution) in ${}^3\text{He}$ at large quark mass ($m_\pi = 800$ MeV)
- Intriguing comparison with analysis of Coccuzza *et al.*:



- ***Strongly suggests further lattice calculations!***

GPD of ${}^4\text{He}$

Incoherent DVCS on ^4He

Physics Letters B 673 (2009) 9–14



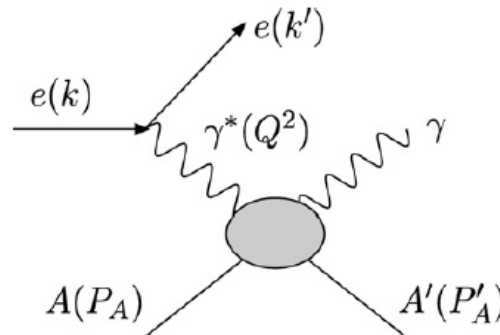
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www.elsevier.com/locate/physletb

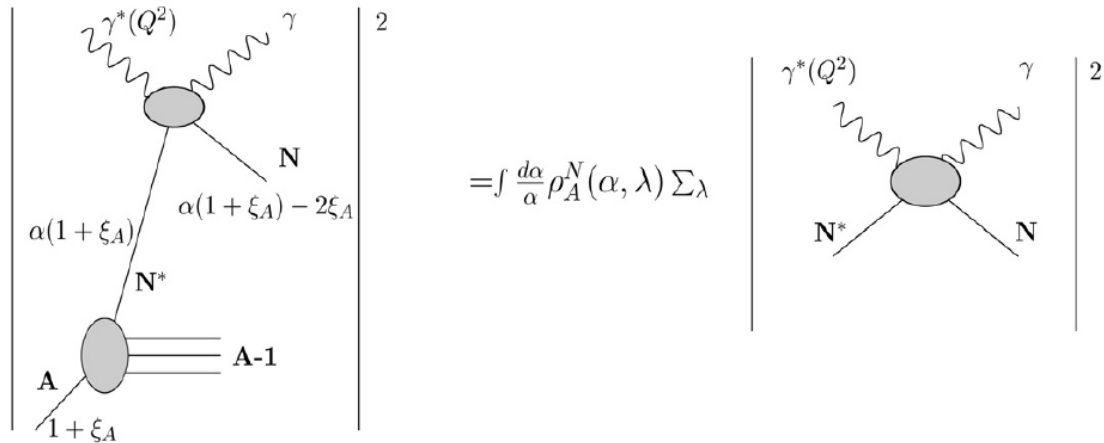
Medium modifications of the bound nucleon GPDs and incoherent DVCS on nuclear targets

V. Guzey^{a,*}, A.W. Thomas^{a,b}, K. Tsushima^c



DVCS on a bound nucleon

- Calculate incoherent DVCS in terms of DVCS from a bound nucleon:



- Assume:

$$H^{q/p^*}(x, \xi, t, Q^2) = \frac{F_1^{p^*}(t)}{F_1^p(t)} H^q(x, \xi, t, Q^2),$$

$$E^{q/p^*}(x, \xi, t, Q^2) = \frac{F_2^{p^*}(t)}{F_2^p(t)} E^q(x, \xi, t, Q^2),$$

$$\tilde{H}^{q/p^*}(x, \xi, t, Q^2) = \frac{G_1^*(t)}{G_1(t)} \tilde{H}^q(x, \xi, t, Q^2),$$

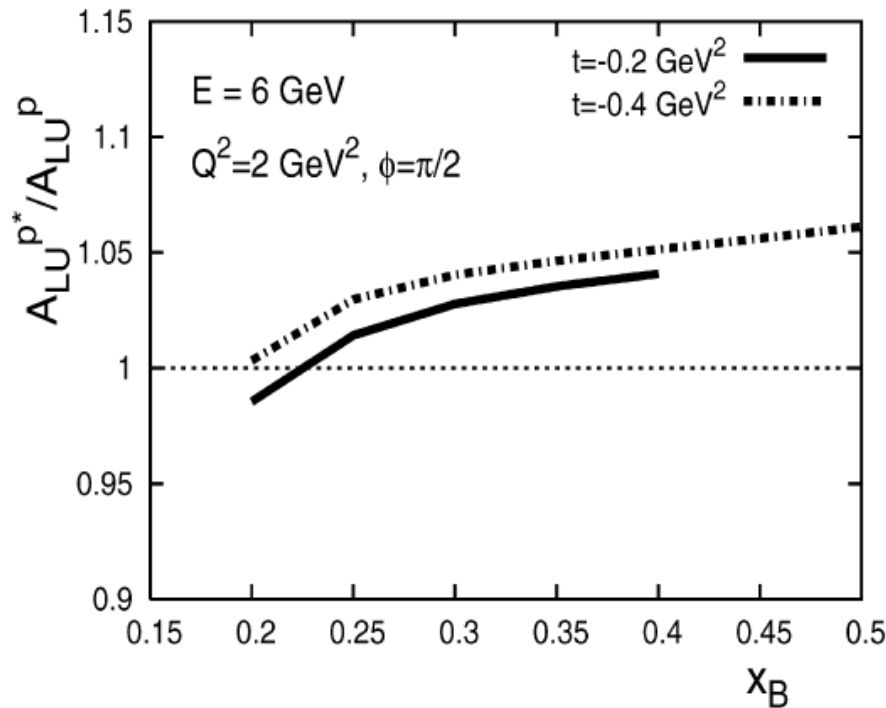
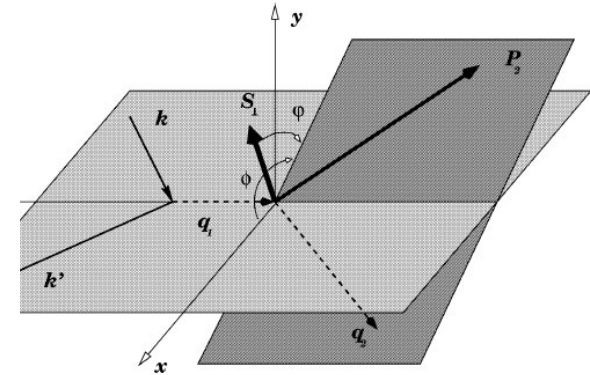
with modification of bound nucleon form factors calculated in the QMC model

(e.g. Lu *et al.*, Phys Lett B417 (1998) 217)

New opportunity to probe medium modifications

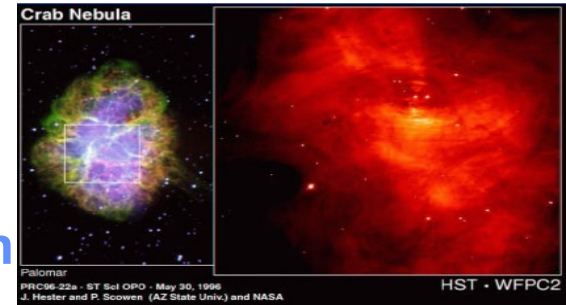
$$A_{\text{LU}}(\phi) \propto \text{Im} \left(F_1^{p*} \mathcal{H}^{p*} + \frac{\chi_B}{2 - \chi_B} (F_1^{p*} + F_2^{p*}) \tilde{\mathcal{H}}^{p*} - \frac{t}{4m_N^2} F_2^{p*} \mathcal{E}^{p*} \right) / f(F_1^{p*}, F_2^{p*}) \sin \phi,$$

A.V. Belitsky et al. / Nuclear Physics B 629 (2002) 323–392



Guzey et al., Phys Lett B673 (2009) 9

Summary



Palomar
PRC66-22a - ST Set OPO - May 30, 1998
J. Hester and P. Scowen (AZ State Univ.) and NASA

HST · WFPC2

- The EMC effect contains fundamental information about the structure of atomic nuclei
- Analysis of the deuteron suggests SRC do not play a dominant role
- Study of recent data for ${}^3\text{H}$ and ${}^3\text{He}$ suggests there is an isovector contribution to the nuclear corrections of PDFs
- Comparison with recent lattice QCD study suggests urgent need for further work
- Studies of GPDs in nuclei may provide insight into changes of structure of bound nucleons



Nuclear DIS Structure Functions : The EMC Effect

The QMC approach is ideal as one **MUST** start with a theory that quantitatively describes nuclear structure and allows calculation of structure functions

– there are no other examples.....

EMC Effect for Finite Nuclei

(There is also a spin dependent EMC effect - as large as unpolarized)

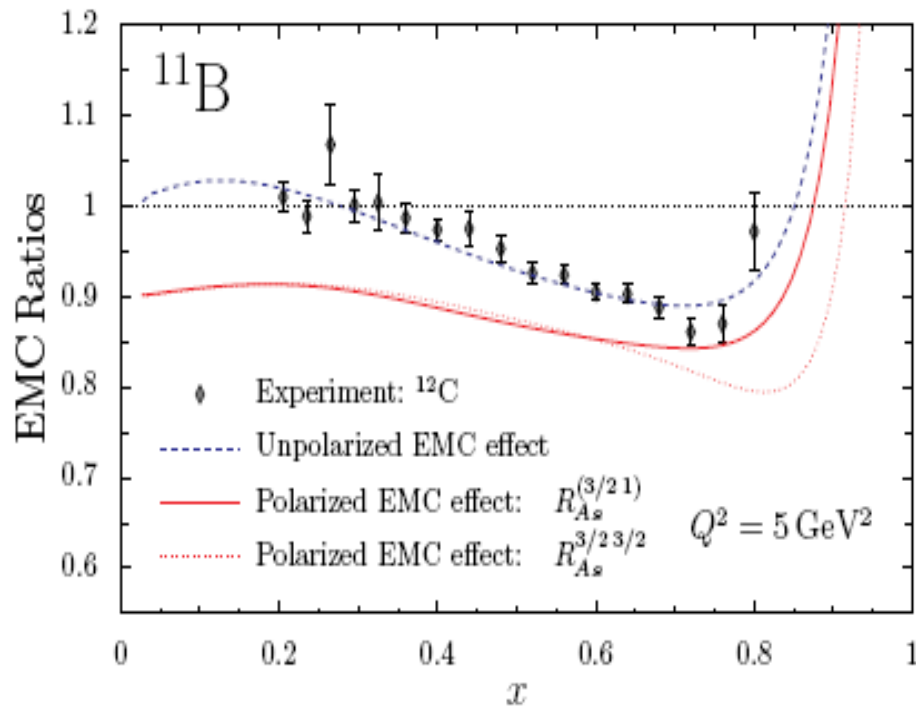


FIG. 7: The EMC and polarized EMC effect in ^{11}B . The empirical data is from Ref. [31].

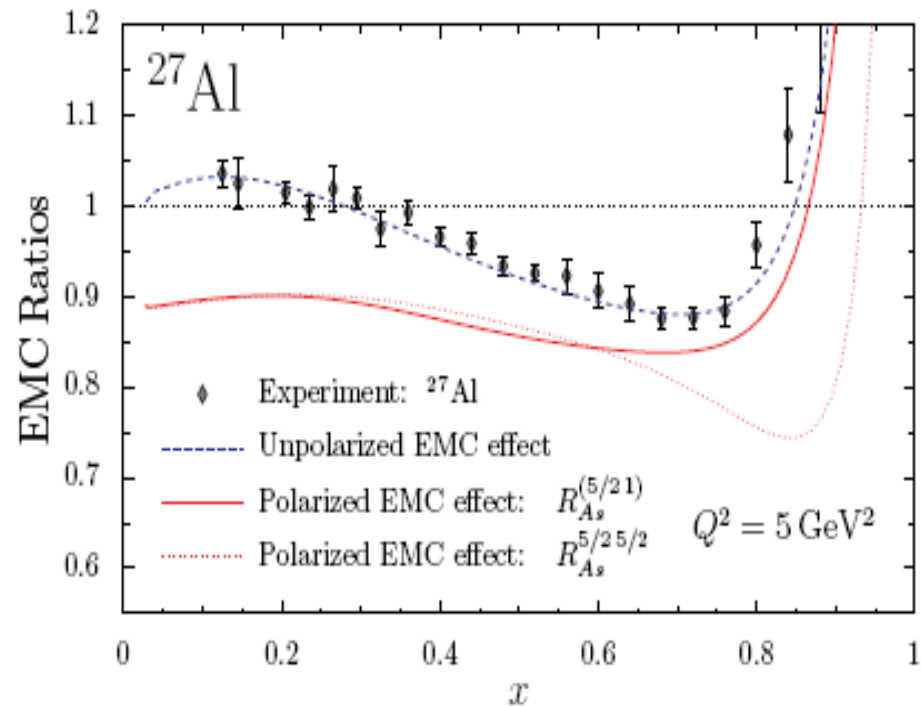


FIG. 9: The EMC and polarized EMC effect in ^{27}Al . The empirical data is from Ref. [31].

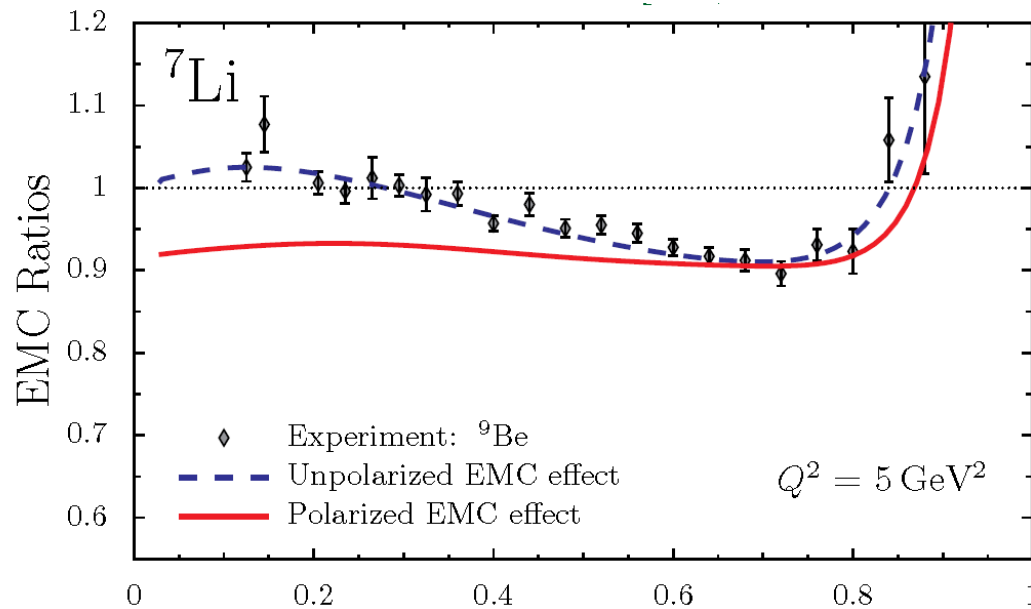
Cloët, Bentz & Thomas, Phys. Lett. B642 (2006) 210
(nucl-th/0605061)

Spin-EMC Effect is a crucial test

- **Tensor correlations leading to high momentum components in nuclear wave function have been proposed as an alternate explanation of the EMC effect**
- **The tensor force scatters 3S_1 pairs almost entirely into 3D_1 at high momentum ($\sim 84\%$ at $p > 400$ MeV/c)**
- **Nucleons in SRC are depolarized – simple Clebsch-Gordan coefficients - and cannot contribute to spin-EMC effect**
- **That is, SRC idea gives essentially NO spin-EMC effect**

Approved JLab Experiment

- Effect in ${}^7\text{Li}$ is slightly suppressed because it is a light nucleus and proton does not carry all the spin (simple WF: $P_p = 13/15$ & $P_n = 2/15$)
- Experiment now approved at JLab [E12-14-001] to measure spin structure functions of ${}^7\text{Li}$ (GFMC: $P_p = 0.86$ & $P_n = 0.04$)
- *Everyone with their favourite explanation for the EMC effect should make a prediction for the polarized EMC effect in ${}^7\text{Li}$*



Other tests (e.g. Isovector EMC effect)

