

proton-deuteron femtoscopy in pp collisions

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proton-deuteron (p-d) interaction

- p-d interaction is well constrained from the **scattering experiments**

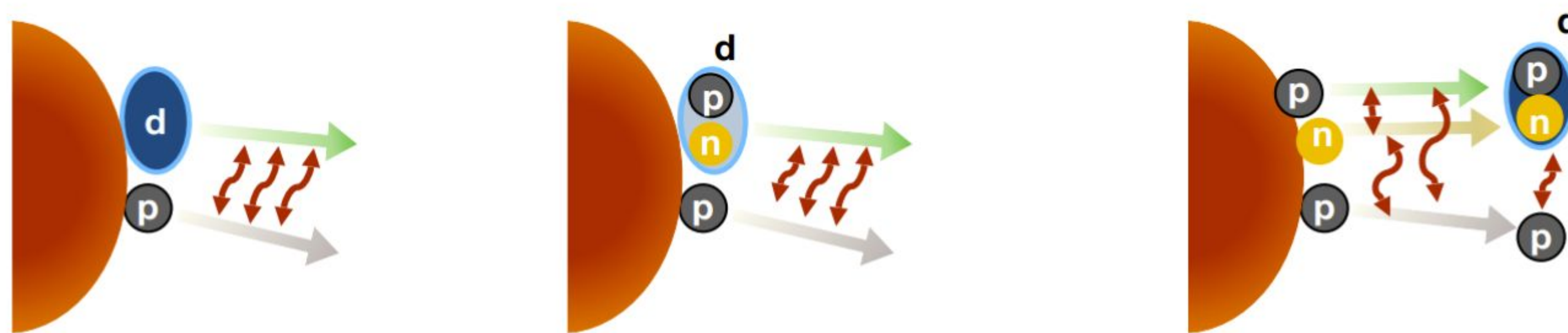
Three body forces

- Fundamental to **explain the nuclear structure**, might become more important at higher densities
- Fundamental **ingredient for the Equation of State (EoS) of dense nuclear matter**
- Theory currently anchored to properties of nuclei, hypernuclei and scattering data

⇒ p-d correlations in pp collisions at the LHC provide a new way to explore the interaction of a three body system at short distances

Production mechanism of light nuclei not understood:

- Models: Thermal emission or Coalescence [Stanislaw Mrowczynski @EXOTICO](#)
- What can final-state interaction studies say about the formation of deuterons (antideuterons)?

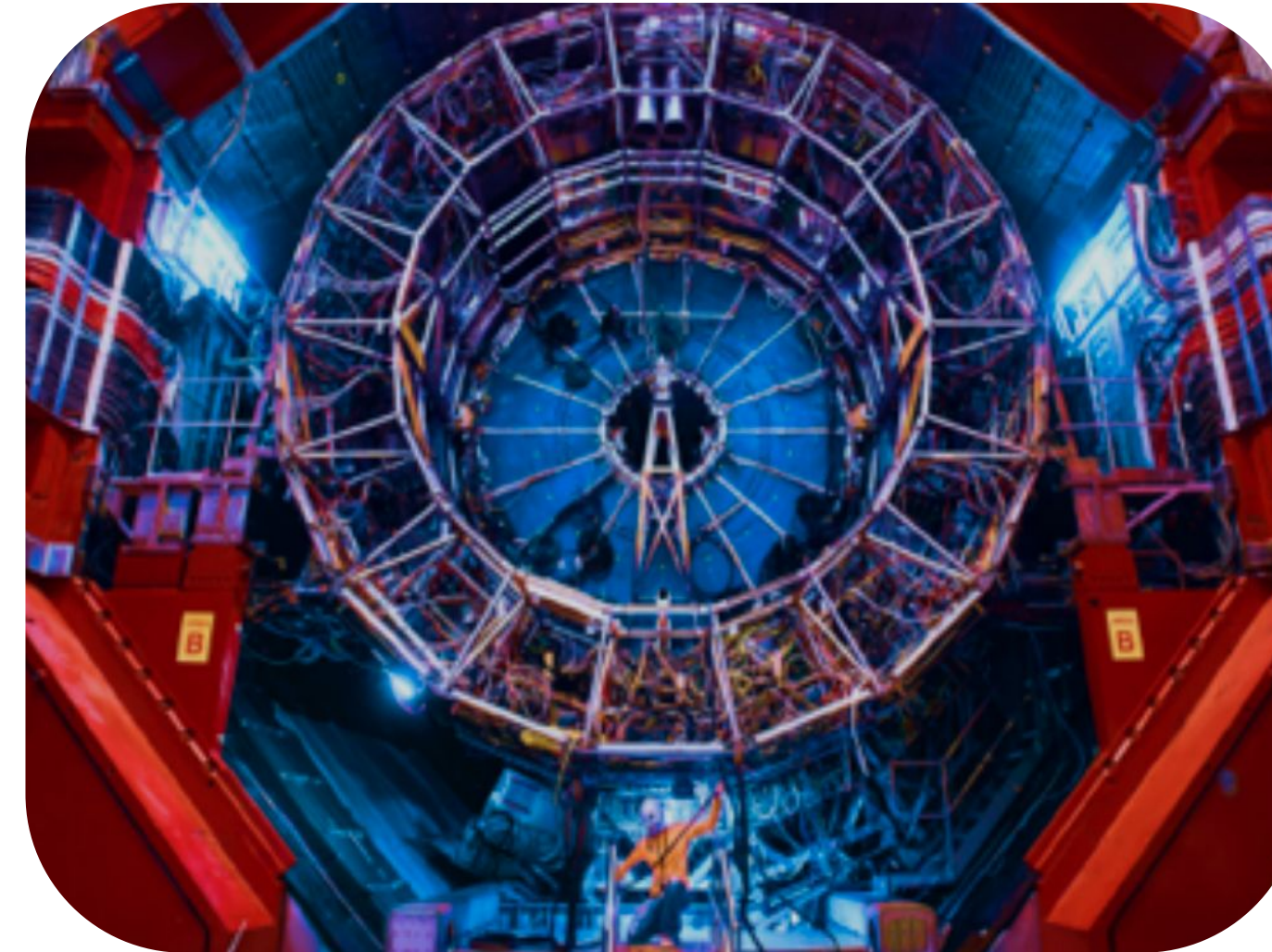


ALICE data

pp collisions @13TeV, High-Multiplicity

- Run 2 High-multiplicity data set with $\sim 1 \times 10^9$ events
- Particles are selected in momentum range:
 - (anti)protons: $0.5 < p_T < 4$ GeV/c
 - (anti)deuterons: $0.4 < p_T < 2.3$ GeV/c

$p-d \oplus p^-d^-$ correlation



⇒ All particles tracked and identified by TPC+TOF

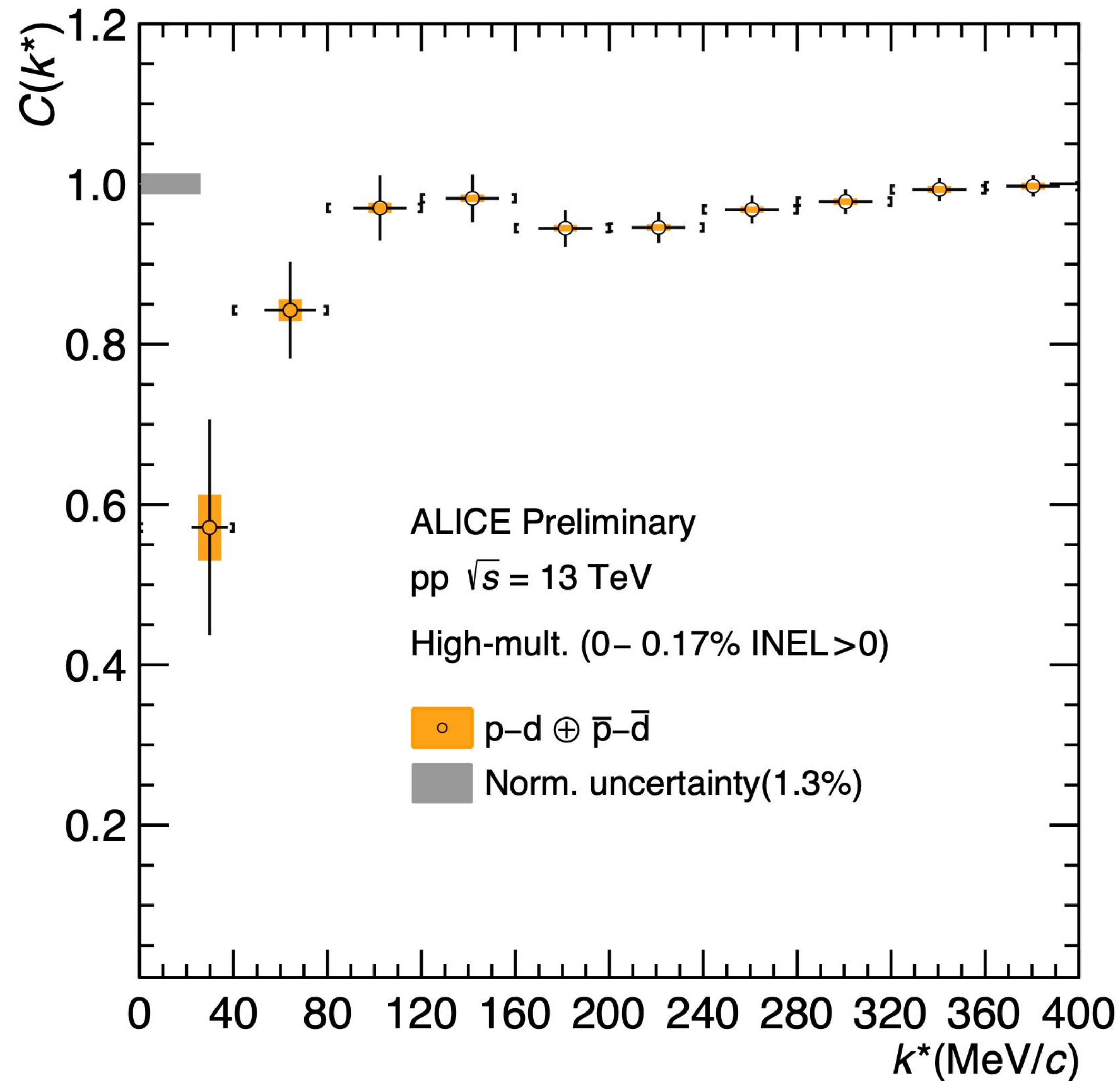
purities >98%

⇒ High-Multiplicity sample enhances number of pairs

$p-d \oplus p^-d^-$ pairs $k^* < 200$ MeV/c = 3851

p-d experimental correlation function

p-d \oplus p $^-$ -d $^-$ correlation



Data corrected for:

- Finite resolution
 - corrected using resolution matrices from MC

Theoretical correlation function corrected for:

- Feed-down
 - Lambda parameters for genuine interaction: $\lambda_{pd} = 82\%$
 - All contributions including feed-down to protons considered as $C(k^*) = 1$.
- Non-Femtoscropy effects
 - Baseline fitted with pol-2 (flat at $k^*=0$)

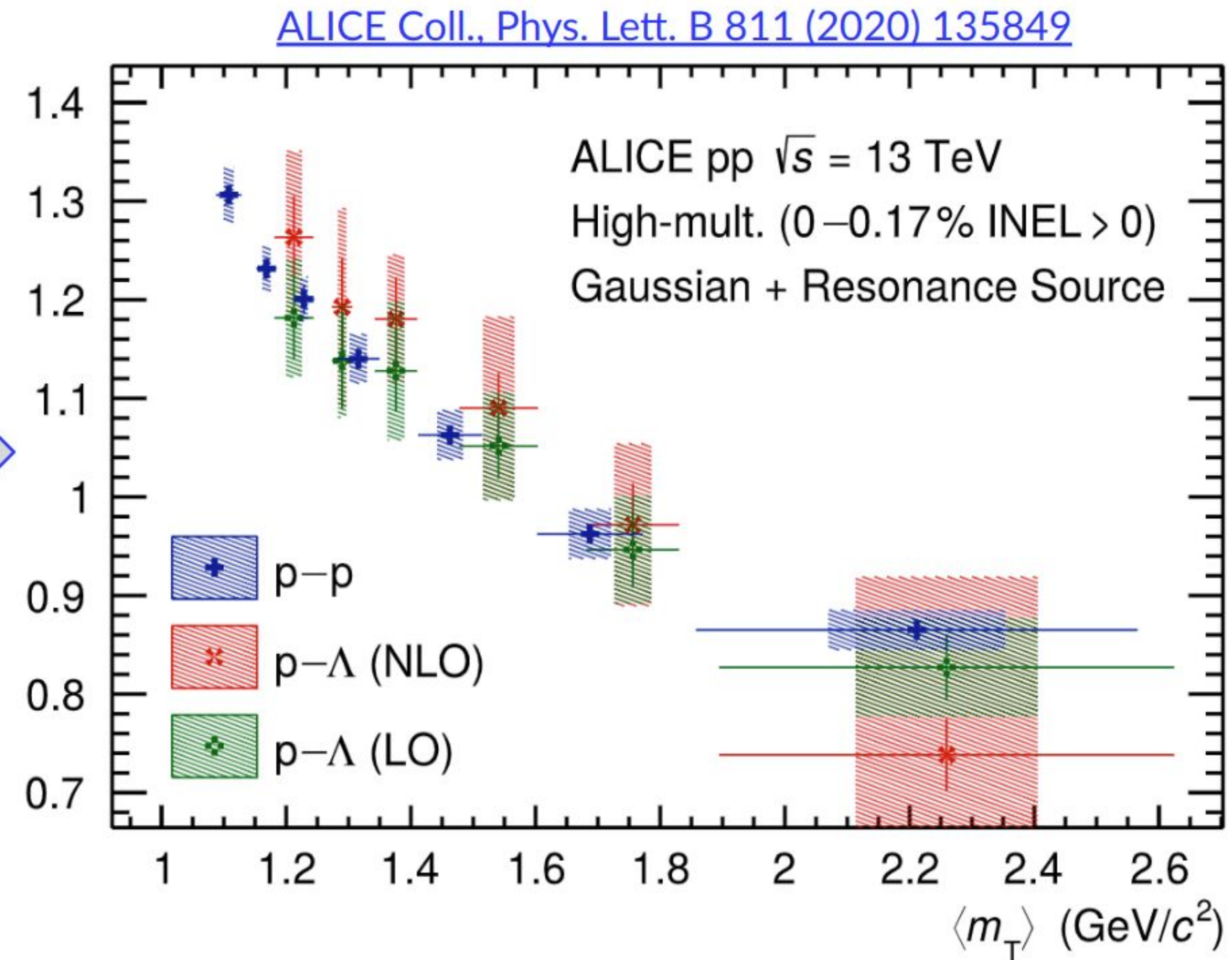
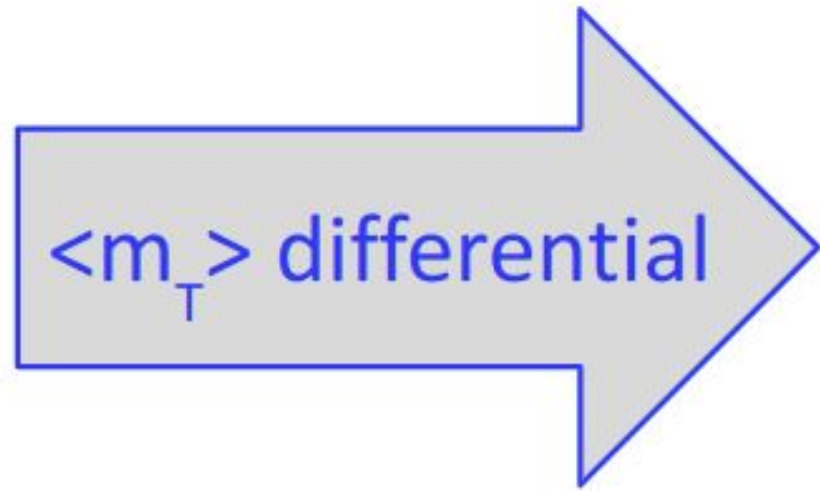
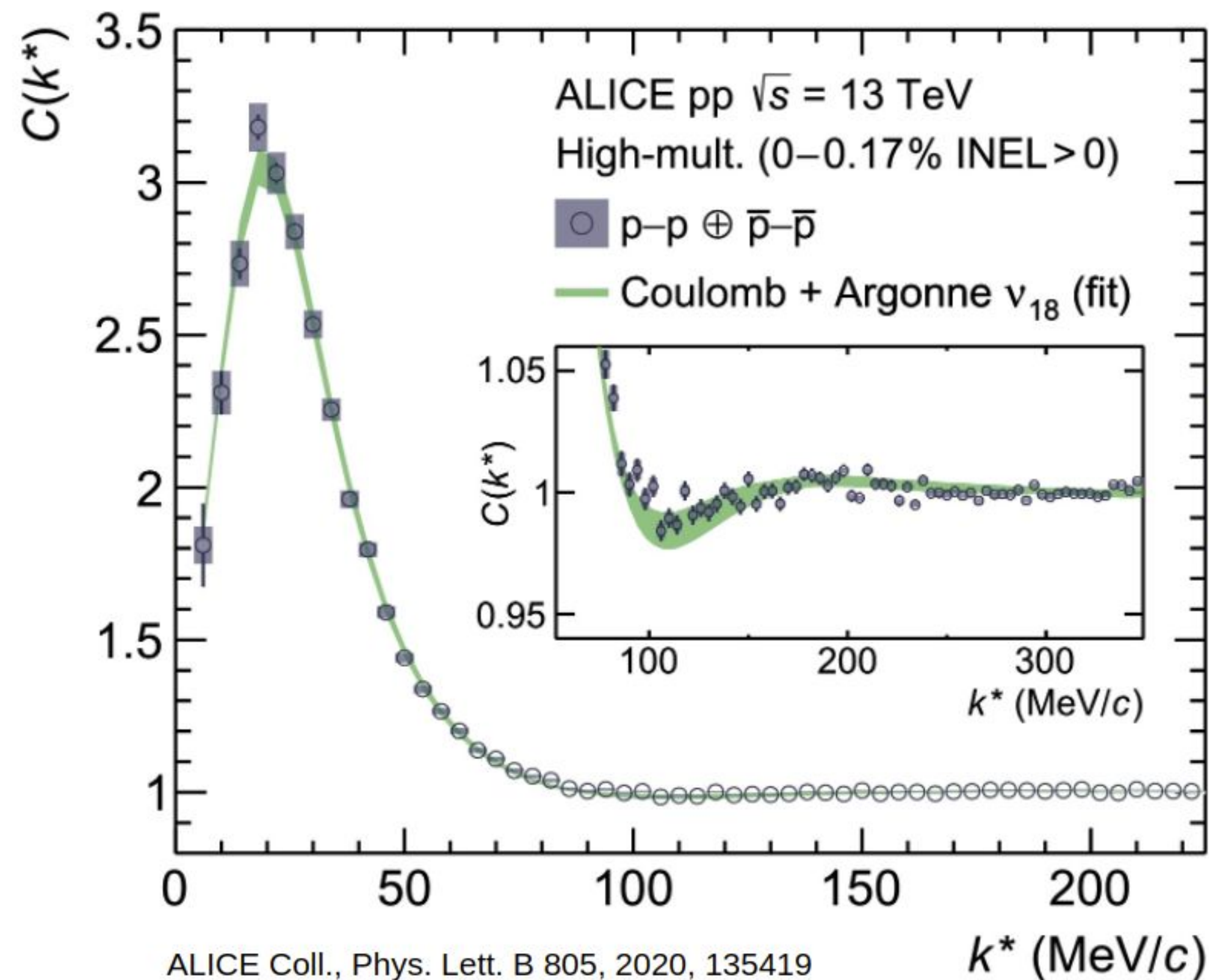
Determination of the source size via m_T scaling + effect of resonances

Common baryon source as a function of $\langle m_T \rangle$



Source size is determined via traditional femtoscopy analysis (known interaction)

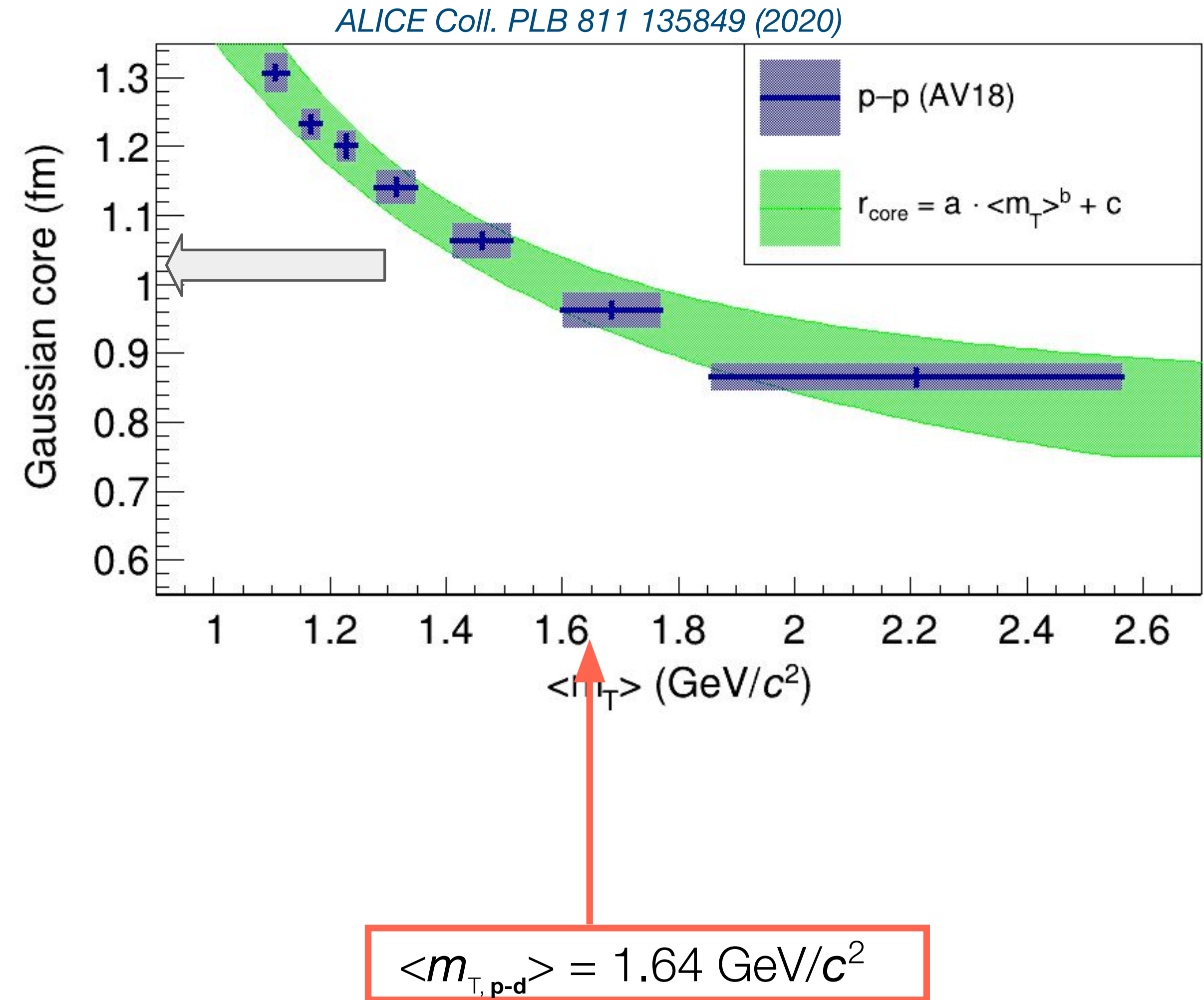
- **fit p-p correlation function** \Rightarrow **extract gaussian source radius**
- differential $\langle m_T \rangle$ fit \Rightarrow **“map” of source size**
- take into account effect of strong decaying resonances



Source size for pd via m_T scaling + resonances

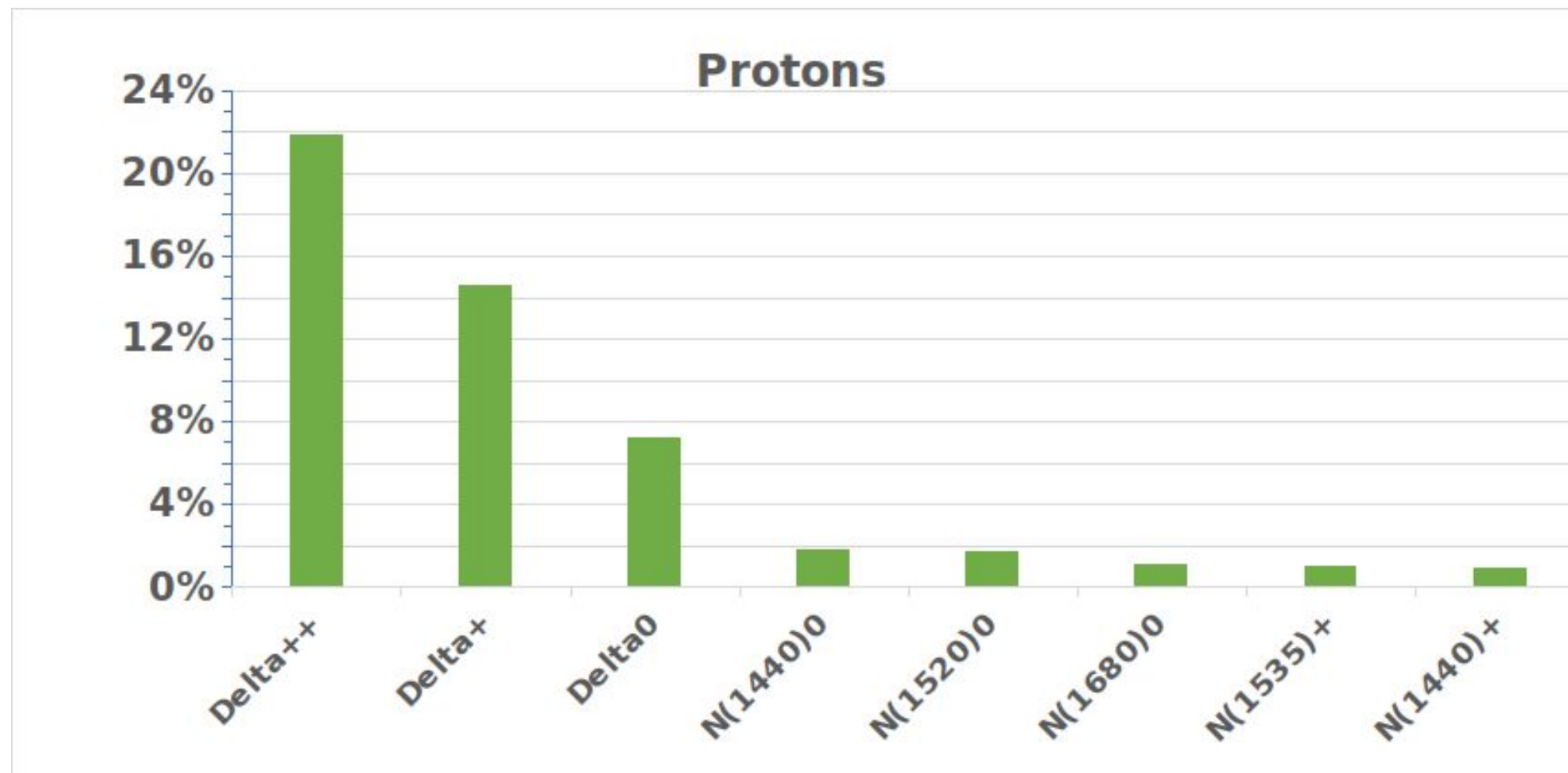
- Assume for pd the universal m_T scaling
- “Core” radius:

Source size	pd
r_{core}	0.99 ± 0.05 fm



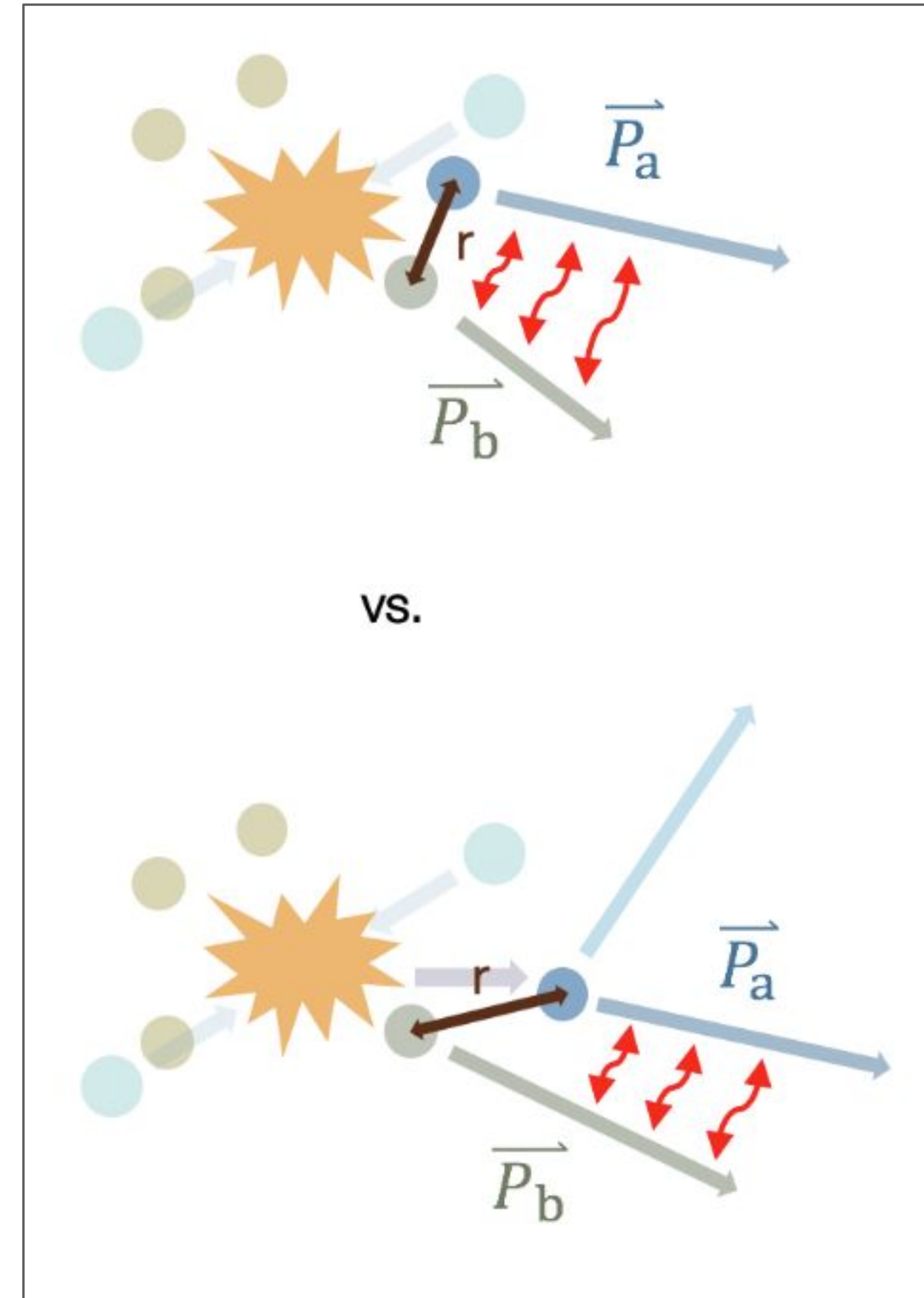
Source size for pd via m_T scaling + resonances

- The source radius is effectively increased by **short-lived strongly decaying resonances** ($\tau \approx r_{\text{core}}$)



- Increase of the source size (long distance tails)

Source size	pd
r_{core}	0.99 ± 0.05 fm
r_{eff}	1.08 ± 0.06 fm



(1)

Theoretical model comparison

Lednicky model: pointlike deuterons

- **For distinguishable particles**

- starting from the scattering parameters \Rightarrow define the s-wave two-particle relative wave function
- considers Coulomb effects

- Coulomb-corrected wave function for final-state interactions (Lednicky): arxiv.org/abs/nucl-th/0501065

$$\psi_{-k^*}(r^*) = e^{i\delta_c} \sqrt{A_c(\eta)} \left[e^{-ik^*r^*} F(-i\eta, 1, i\zeta) + f_c(k^*) \frac{\tilde{G}(\rho, \eta)}{r^*} \right]$$

- f_c : Coulomb normalised scattering amplitude for strong interaction
- $F(-i\eta, 1, i\zeta)$: confluent hypergeometric function
- $\tilde{G}(\rho, \eta)$: combination of singular and regular Coulomb function, describes asymptotic behaviour of wavefunction

\Rightarrow to obtain two-particle correlation we can use Koonin-Pratt formula

Lednicky model: How accurate is it? 🤔



ALICE

Lednicky model: How accurate is it? 🤔

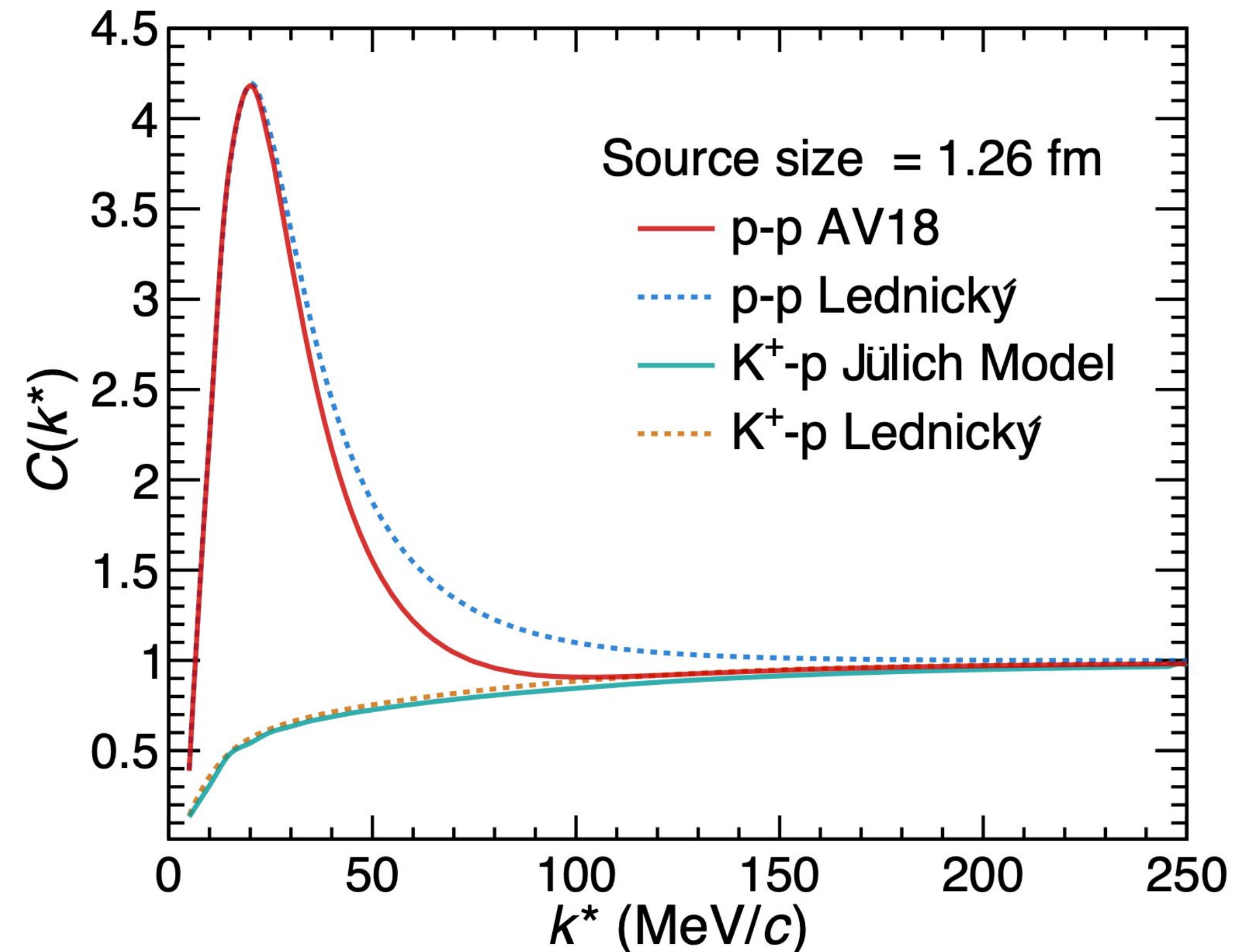
- **Benchmark:** compare correlations with Lednicky model with calculations using

- pp from AV18 potential
- K^+p from Jülich model

System	$f_0(\text{fm})$	$r_0(\text{fm})$	References
pp (S=0)	7.806	2.788	R. Wiringa et al. [6]
K^+p (S=1/2)	-0.316	0.373	M. Hoffmann et al. [7]

- **Correlations are well reproduced by Lednicky approach**

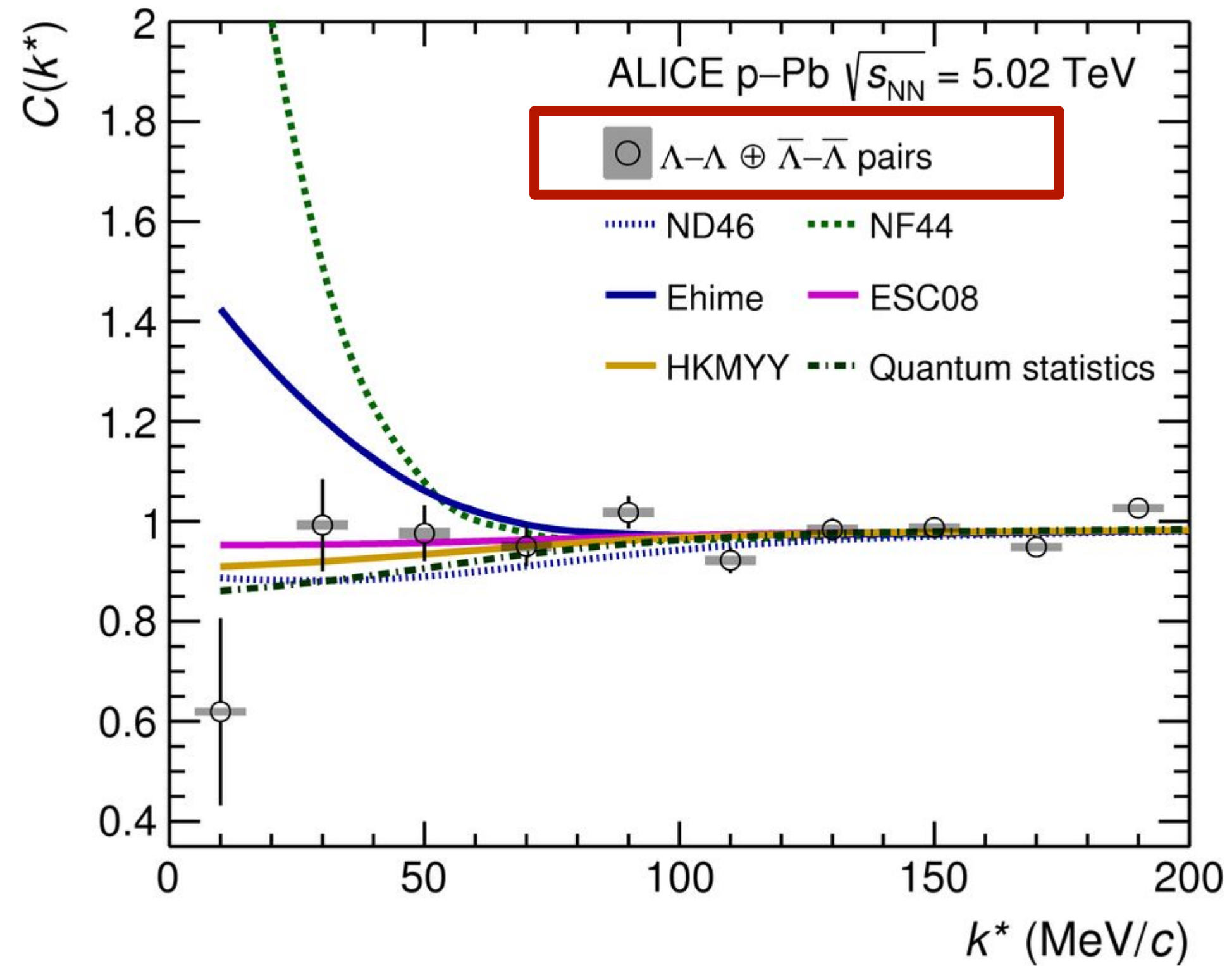
- even with no anti-symmetrization for pp case!



Convention sign: In this presentation positive (negative) f_0 means attractive (repulsive) interaction

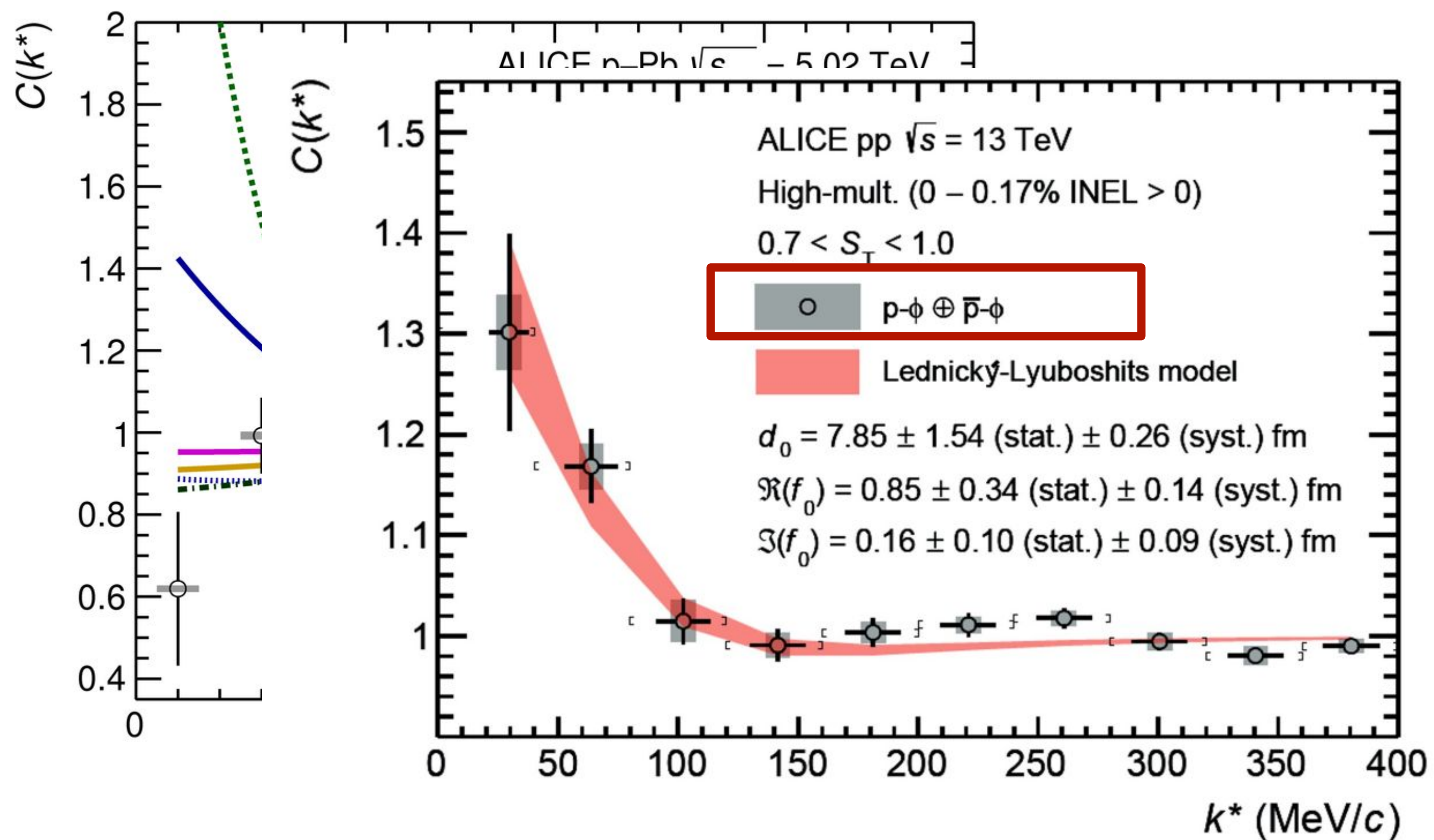
Lednicky model: How accurate is it? 🤔

- Some examples
 - Lednicky-Luboshits approach vs ALICE data



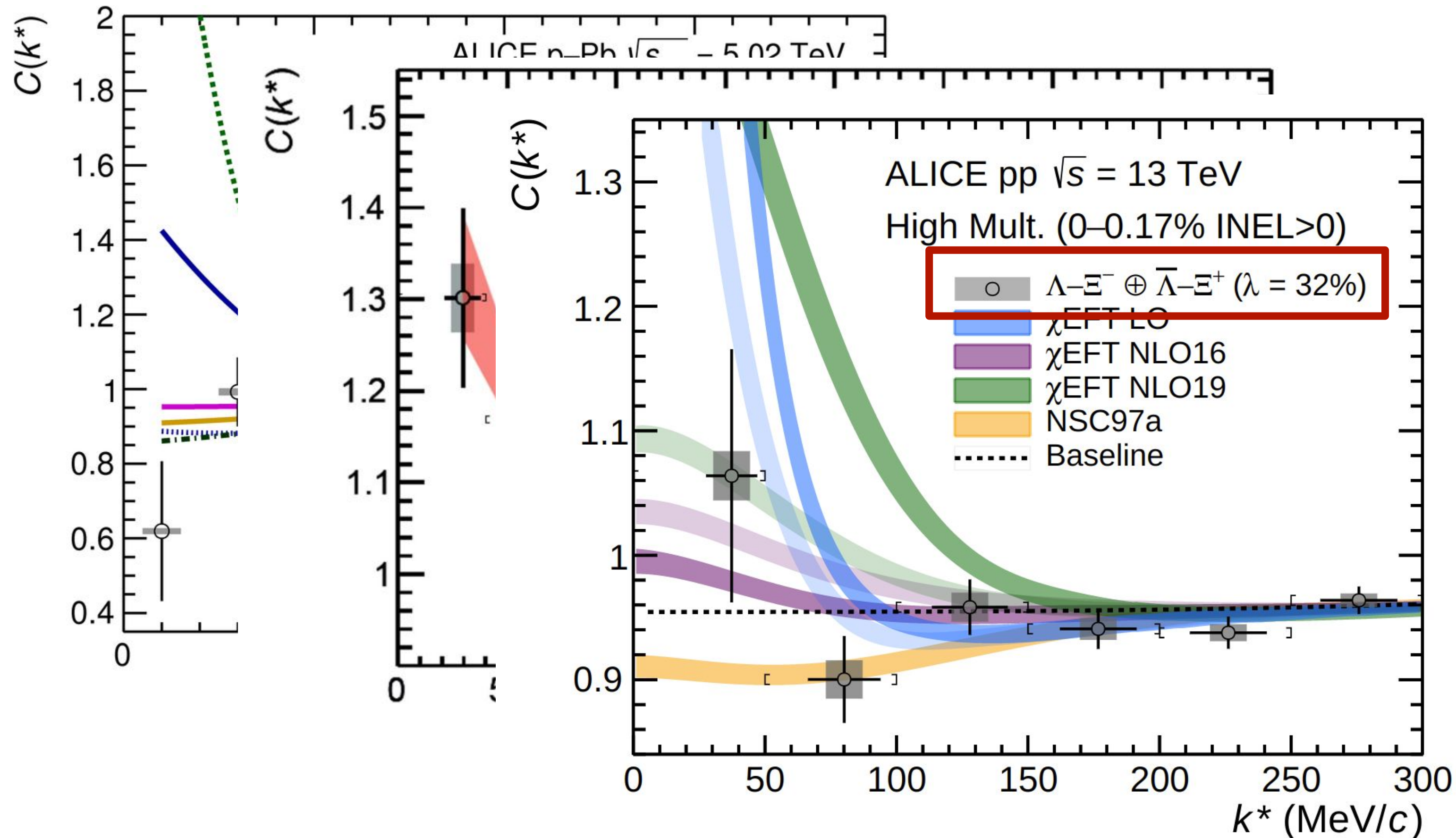
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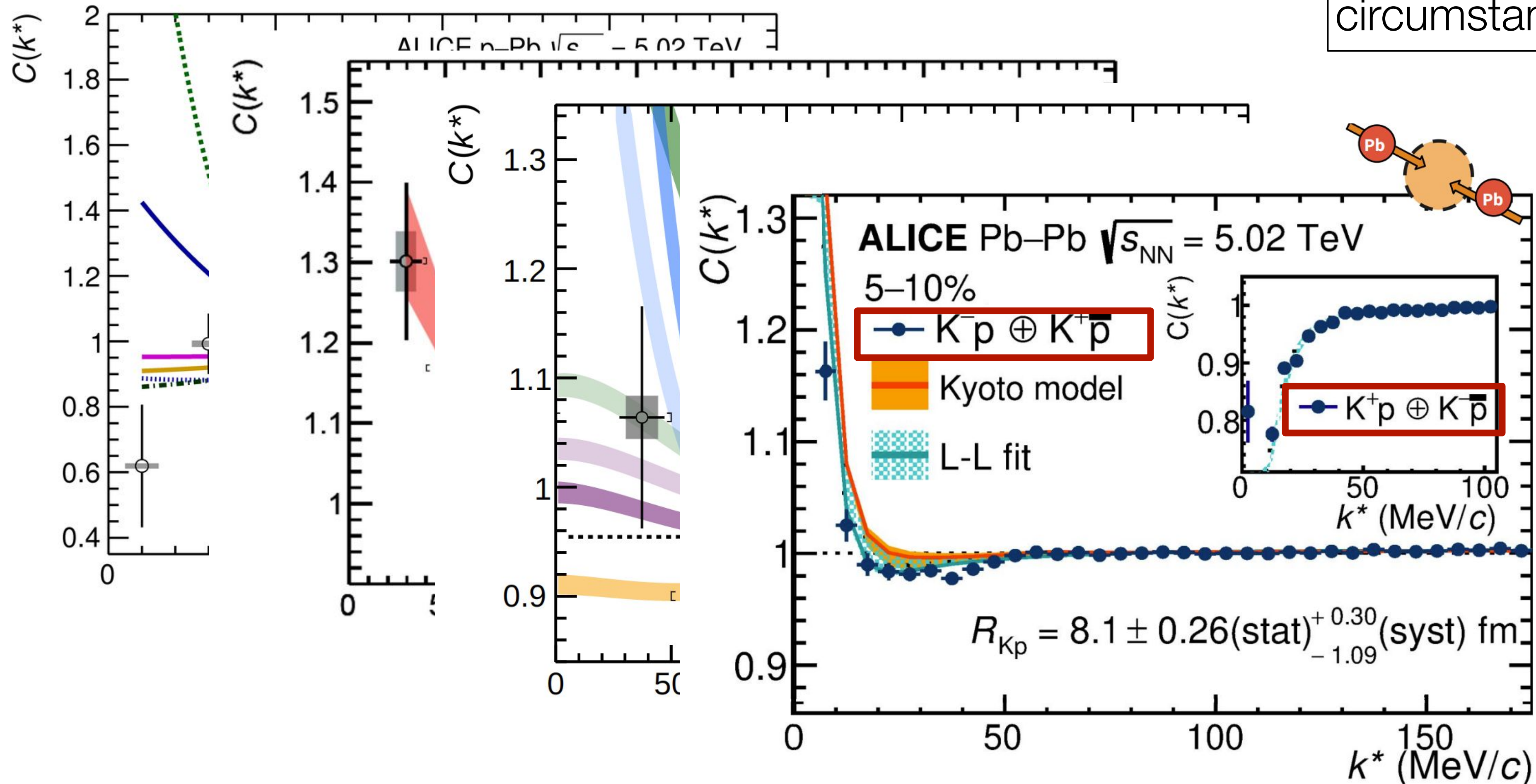
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Lednicky model: How accurate is it? 🤔

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⇒ Useful tool (under the right circumstances)



⇒ **pd scattering parameters** from fits to pd scattering data

$S = 1/2$		$S = 3/2$		
$f_0(\text{fm})$	$r_0(\text{fm})$	$f_0(\text{fm})$	$r_0(\text{fm})$	
$-1.30^{+0.20}_{-0.20}$	—	$-11.40^{+1.80}_{-1.20}$	$2.05^{+0.25}_{-0.25}$	Van Oers et al. Nucl. Phys. A 561 (1967)
$-2.73^{+0.10}_{-0.10}$	$2.27^{+0.12}_{-0.12}$	$-11.88^{+0.40}_{-0.10}$	$2.63^{+0.01}_{-0.02}$	J.Arviex et al. Nucl. Phys. A92 221 (1973)
-4.0	—	-11.1	—	E.Huttel et al. Nucl. Phys. A406 443 (1983)
-0.024	—	-13.7	—	A.Kievsky et al. Phys. Lett, B406 292 (1997)
$0.13^{+0.04}_{-0.04}$	—	$-14.70^{+2.30}_{-2.30}$	—	T. C. Black Phys. Lett, B471 103 (1999)

Assumption: Deuteron as point like particle

Lednicky model: pointlike deuterons

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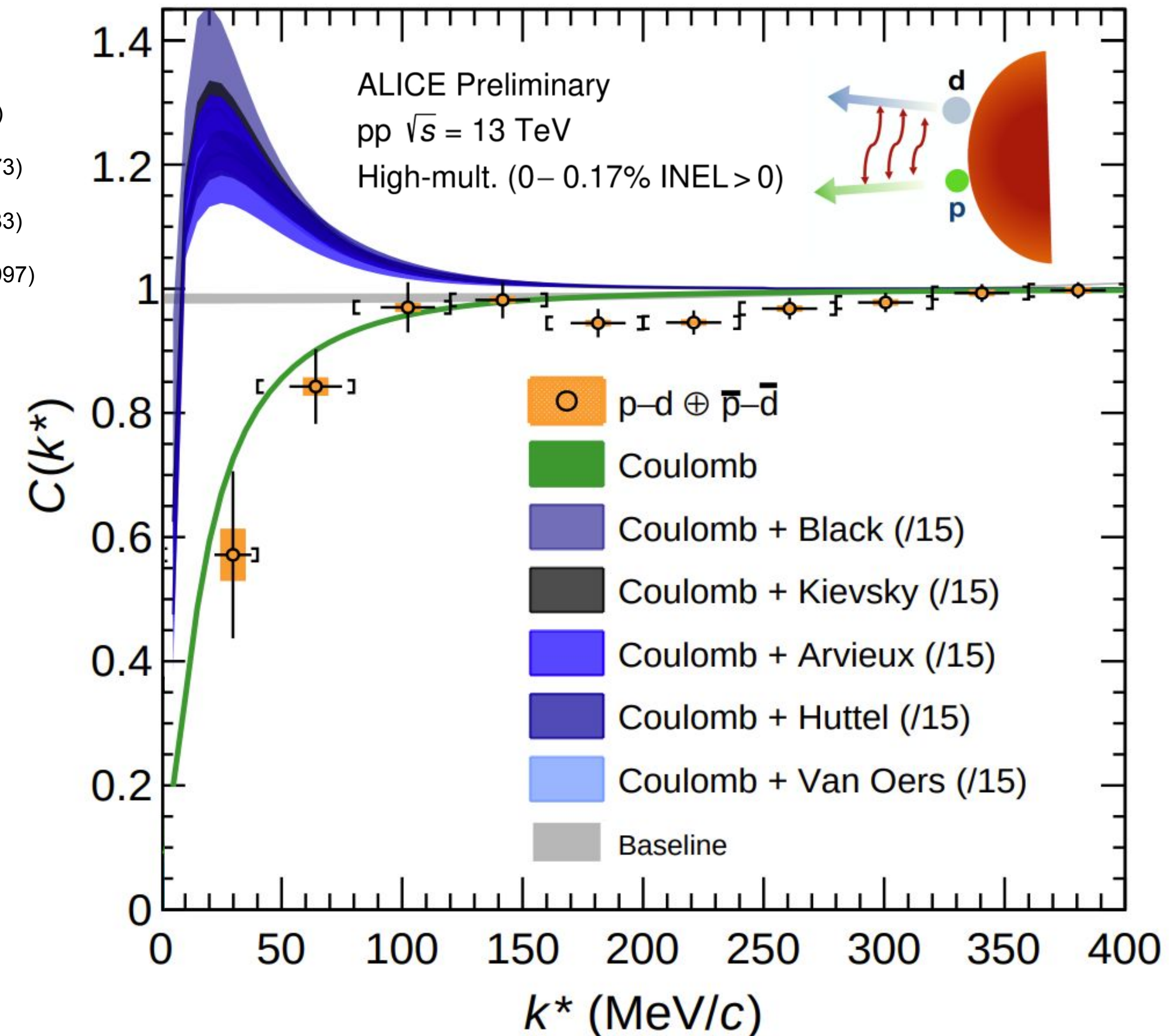
pd data not described

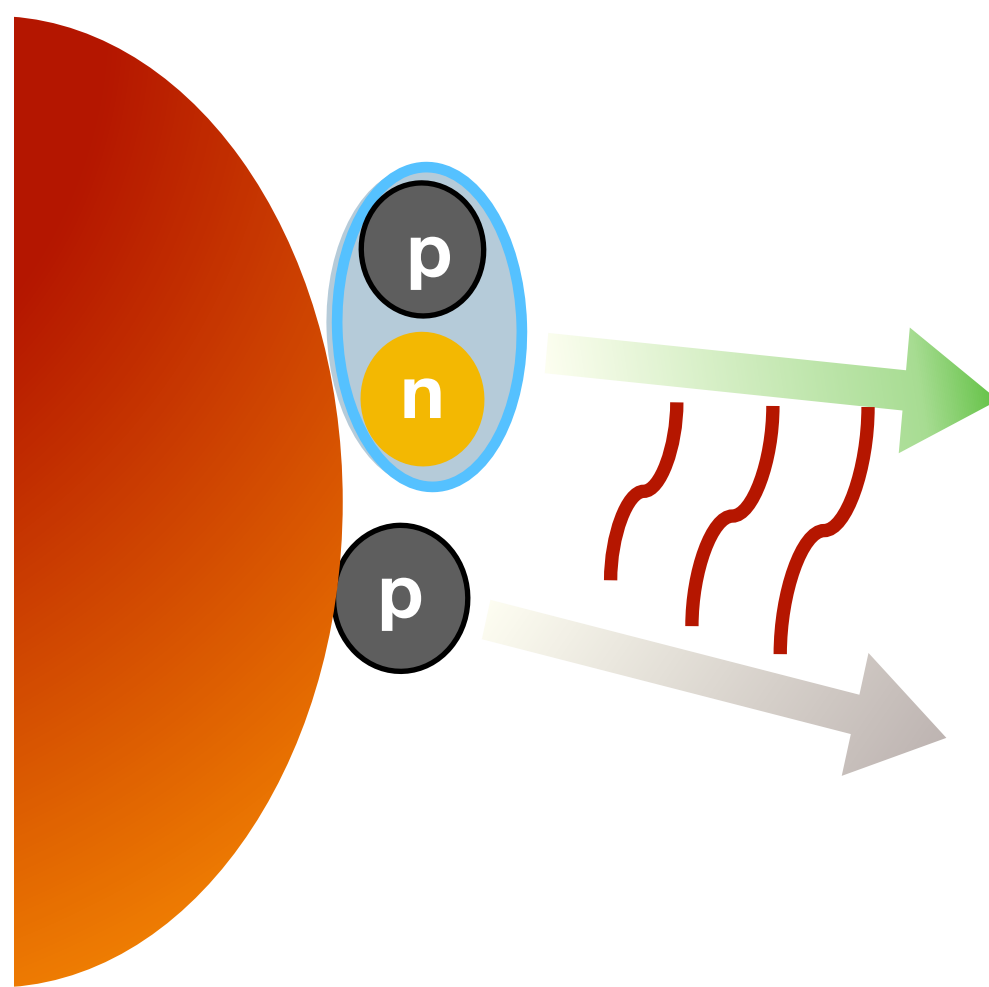
Model and data disagree for source size $r = 1.08$ fm

⇒ Model does not account for p-(p-n) interaction

⇒ **pd can't be treated as effective two-body system**

$r_{pd} = 1.08 \pm 0.06$ fm
 pd model calculations scaled by 1/15



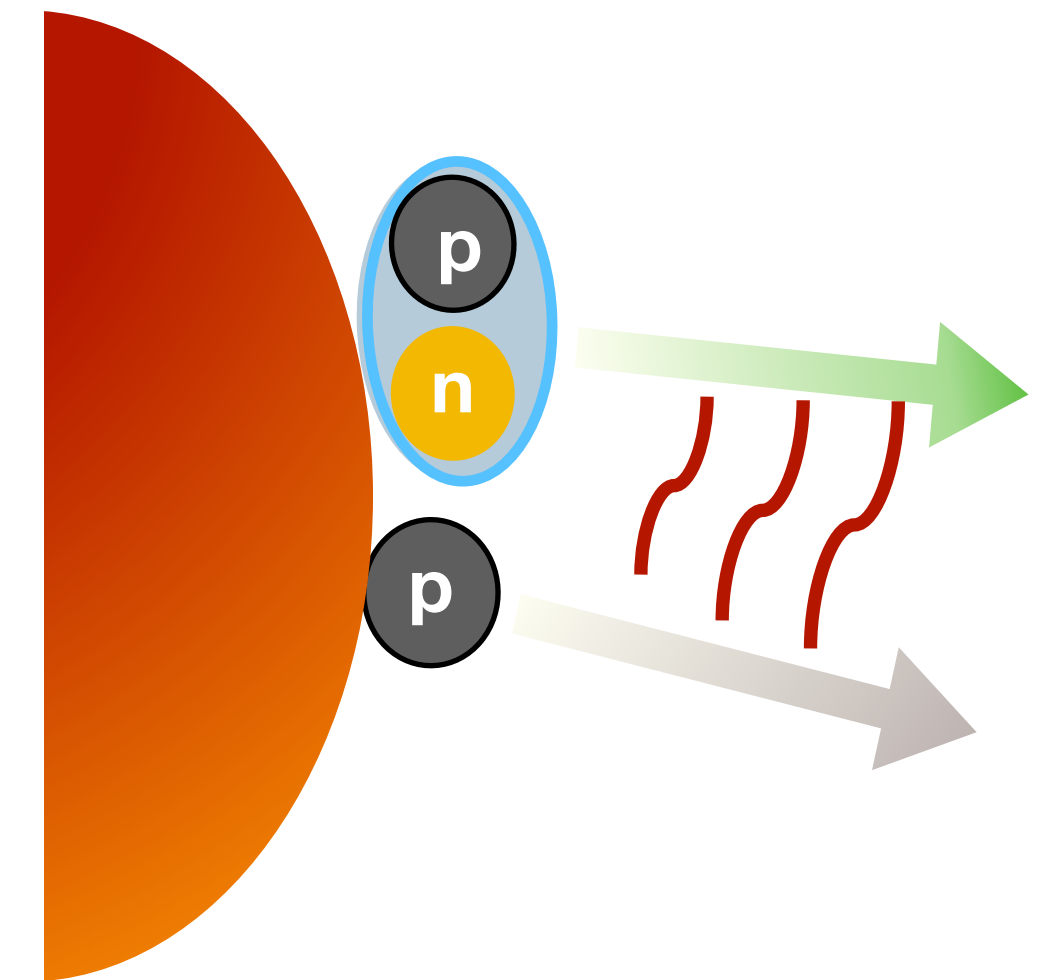


Pisa model: **pd as three-body system**

Full calculation of a three-body p-p-n system projected into the p-d final state

Model under construction: Three-body dynamics calculation by PISA theory group: M. Viviani, A. Kievsky, L. Marcucci

- **Two-body interaction** Argonne V18 potential
- **Three-body interaction** Urbana XI potential
- **Deuteron wave-function** from AV18 NN interaction
- Deuteron is formed at the same time as the proton



- **Three-body full p-d wave function** $\Psi_{m_2, m_1}(\mathbf{x}, \mathbf{y})$ describing three body dynamics, anchored to p-d scattering observables.

- x = distance of p-n system within the deuteron
- y = p-d distance
- m_2 and m_1 deuteron and proton spin

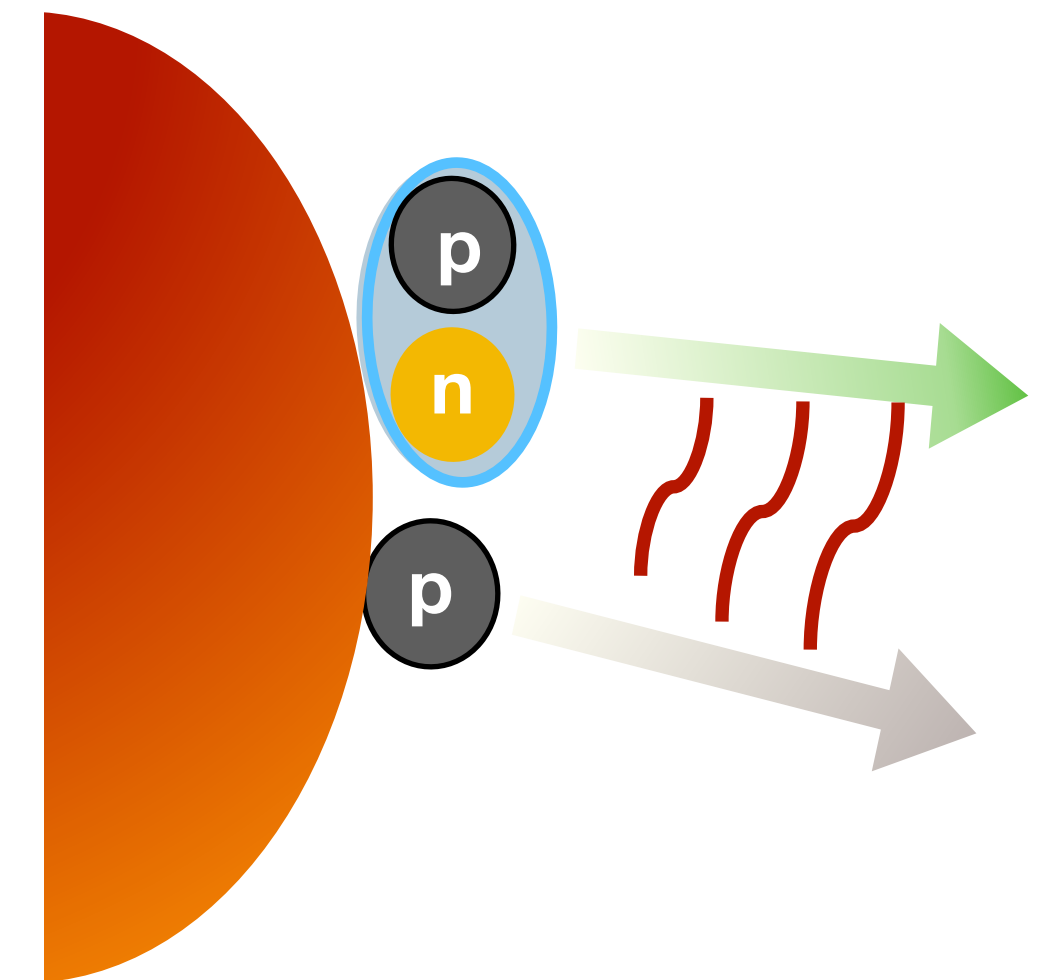
- $\Psi_{m_2, m_1}(\mathbf{x}, \mathbf{y})$ projected to obtain an effective proton-deuteron wave function:

$$\Psi_{m'_2, m'_1, m_2, m_1}(k, \mathbf{y}) = \int d^3x \left[\phi_{m'_2}(1, 2)(\mathbf{x}) \chi_{m'_1}(3) \right]^\dagger \Psi_{m_2, m_1}(\mathbf{x}, \mathbf{y}) .$$

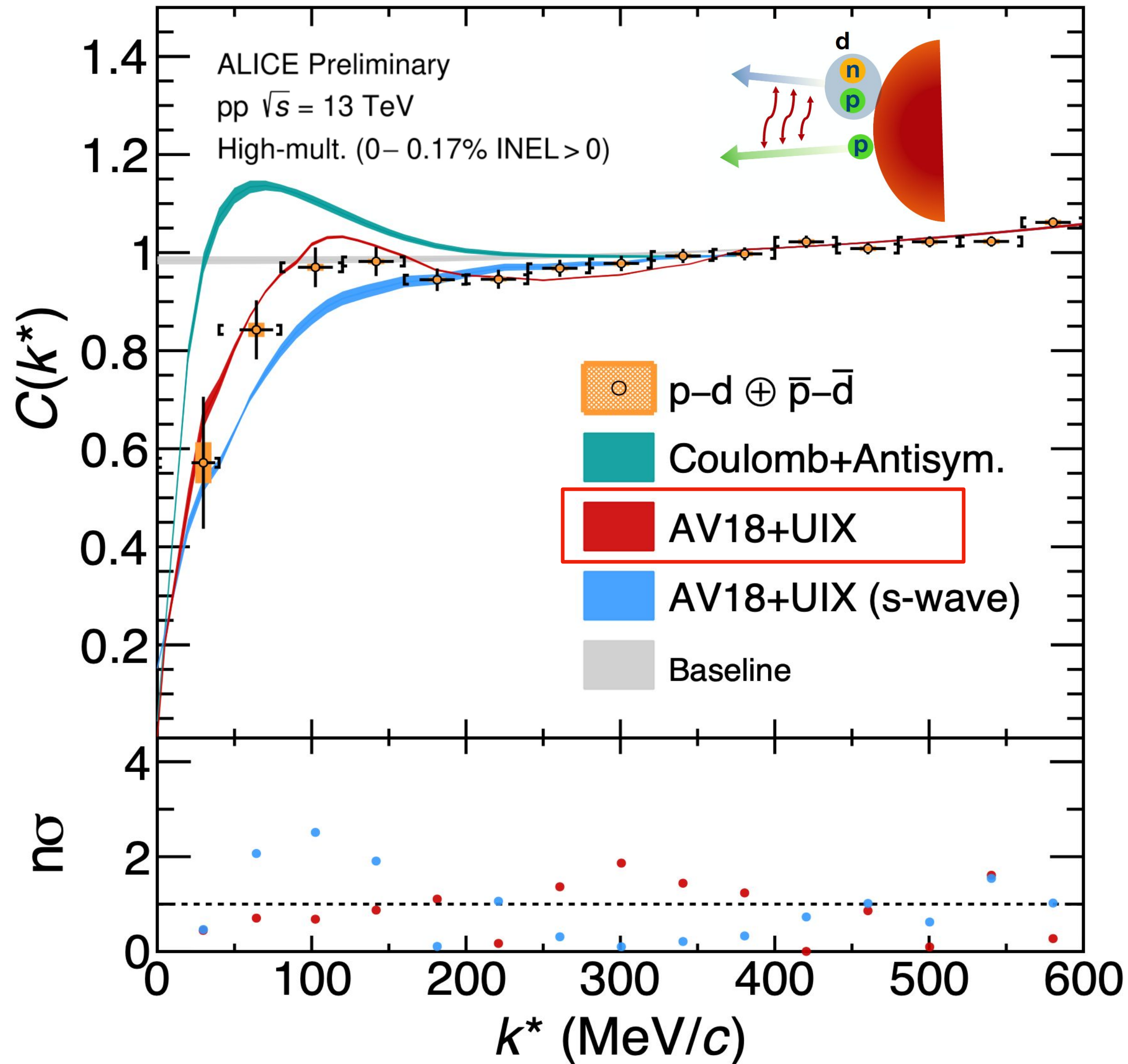
with $\phi_{m'_2}, \chi_{m'_1}$ the deuteron and proton wave-functions

- The correlation function is defined as

$$C_{pd}(k) = 3 \times \frac{1}{6} \sum_{m_2, m_1} \sum_{m'_2, m'_1} \int d^3y S_R(y) |\Psi_{m'_2, m'_1, m_2, m_1}(k, \mathbf{y})|^2 .$$

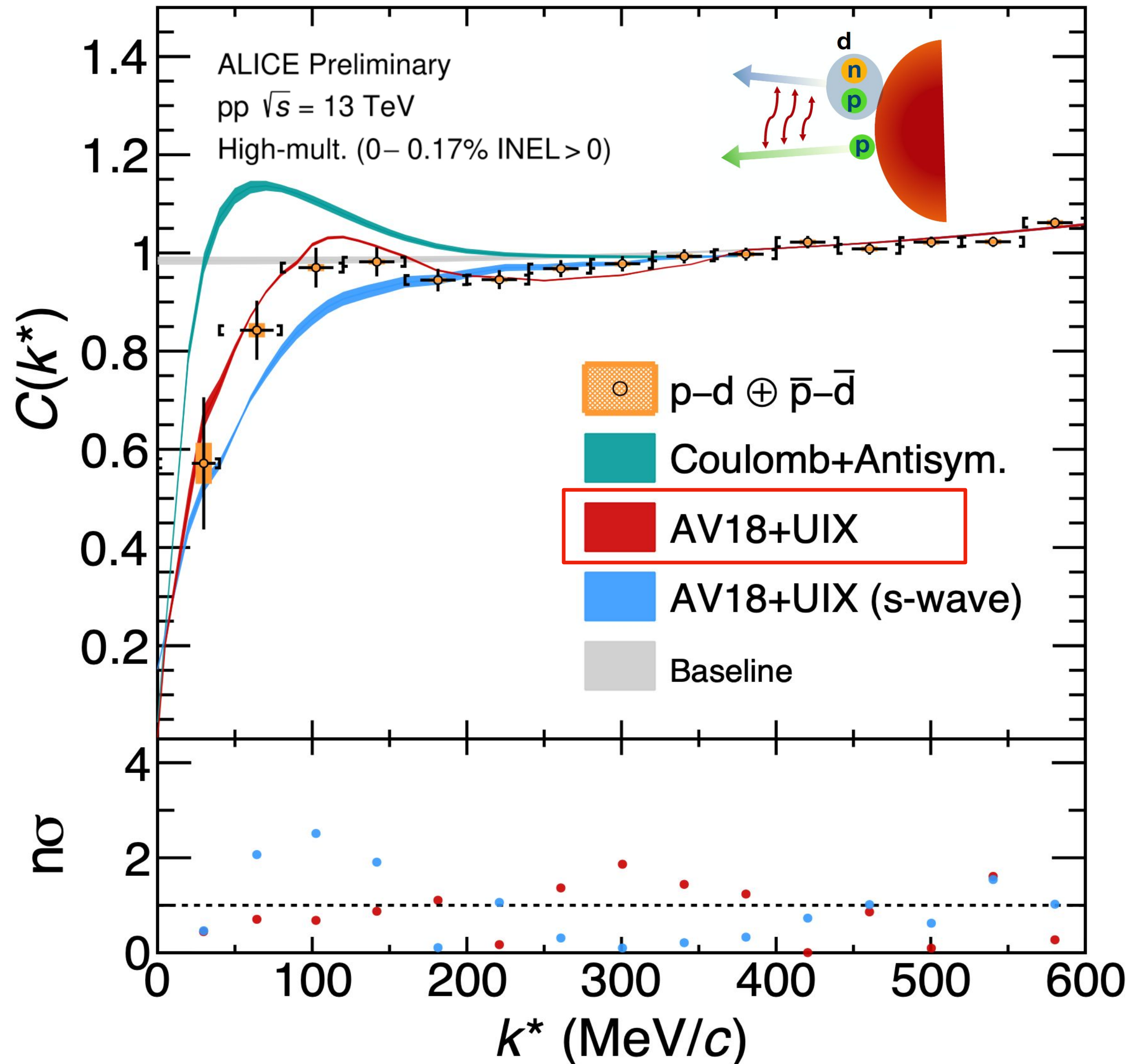


Pisa model vs ALICE data



WORK IN PROGRESS:

Preliminary Model including NN and NNN interactions in s+d-wave agrees much better with data



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Preliminary Model including NN and NNN interactions in s+d-wave agrees much better with data

- ...everything seems to be “back to normal”:
- **Coulomb interaction not strong enough** to describe the data
 - Data **sensitive** to inclusion of **d-wave**
 - Source size = 1.08 ± 0.06 fm \Rightarrow **fully formed deuteron present assuming small source**

Conclusions and outlook

Three-particle systems can be accessed and studied at the LHC in pp collisions with a novel technique

Proton-deuteron femtoscopy

- ➔ **Cannot be treated as effective two-body system:** assumption of pointlike and distinguishable particles does not work
- ➔ **Deuteron described as composite object interacting with a proton:** model considering $p(pn)$ three-body dynamics reproduce the data
 - Source size extracted from the ‘universal’ m_T scaling.
 - Small distance probes short range NNN interaction
 - Measured correlation function sensitive to inclusion of higher partial waves
- **More statistics = more physics:** A m_T dependent study would enable access to shorter distances for the three body system in the near future.