

# Microscopic Structure of the Low-Energy Electric Dipole Response of $^{120}\text{Sn}$

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University of Cologne

ECT\* Workshop on  
**Giant and Soft Modes** of Excitation  
in **Nuclear Structure** and Astrophysics  
Trento, Oct. 2022

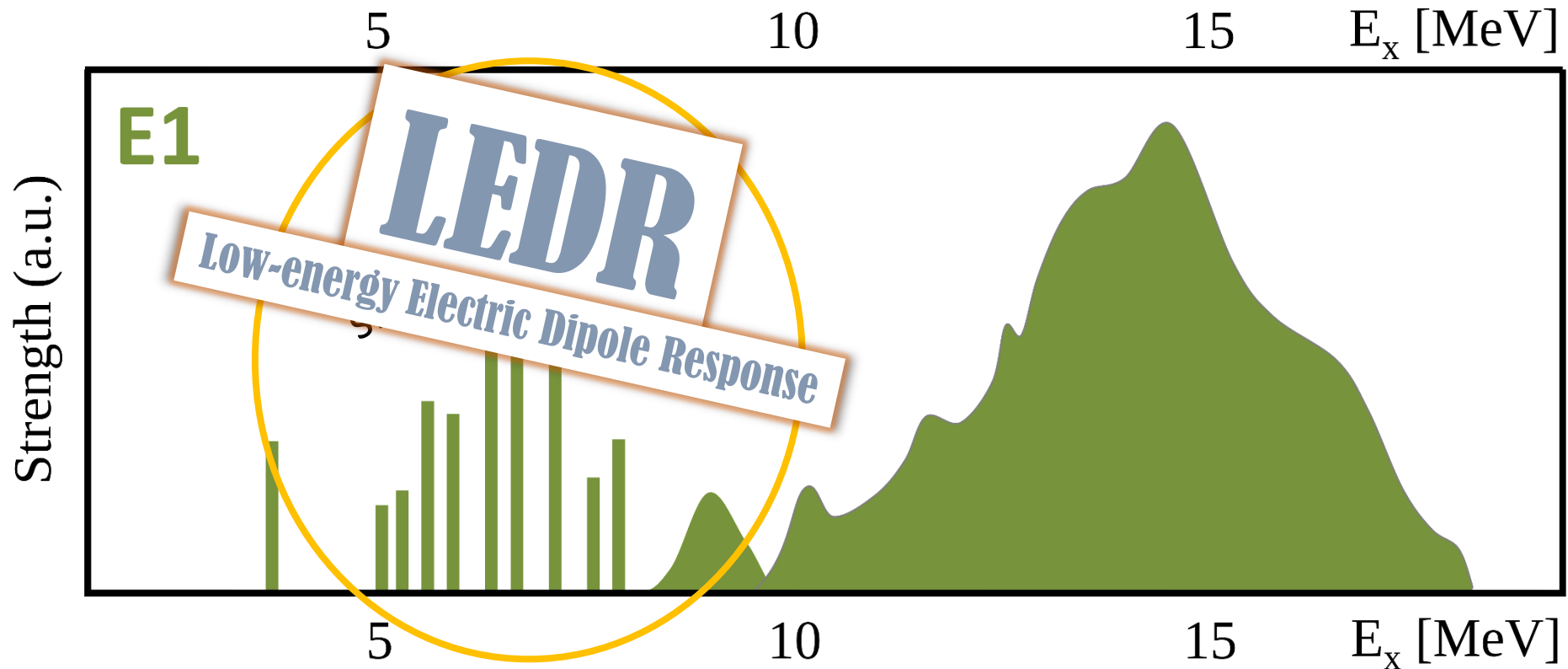
Supported by the DFG (ZI 510/10-1)

Universität  
zu Köln



mweinert@ikp.uni-koeln.de

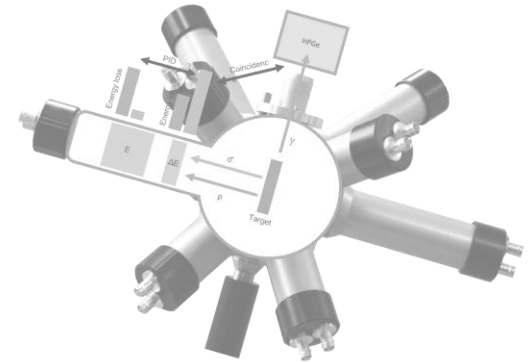
# Typical Dipole-Strength Distribution in Atomic Nuclei



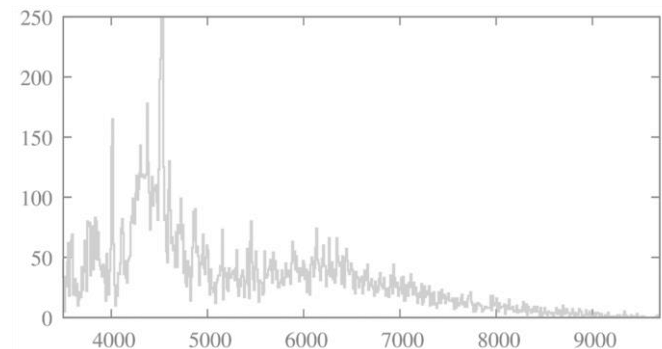
- Part of the photon strength function
  - Used to model  $(\gamma, n)/(n, \gamma)$  reactions during late  $r$  process
- General nuclear structure phenomena
  - How are specific features generated?

# Overview

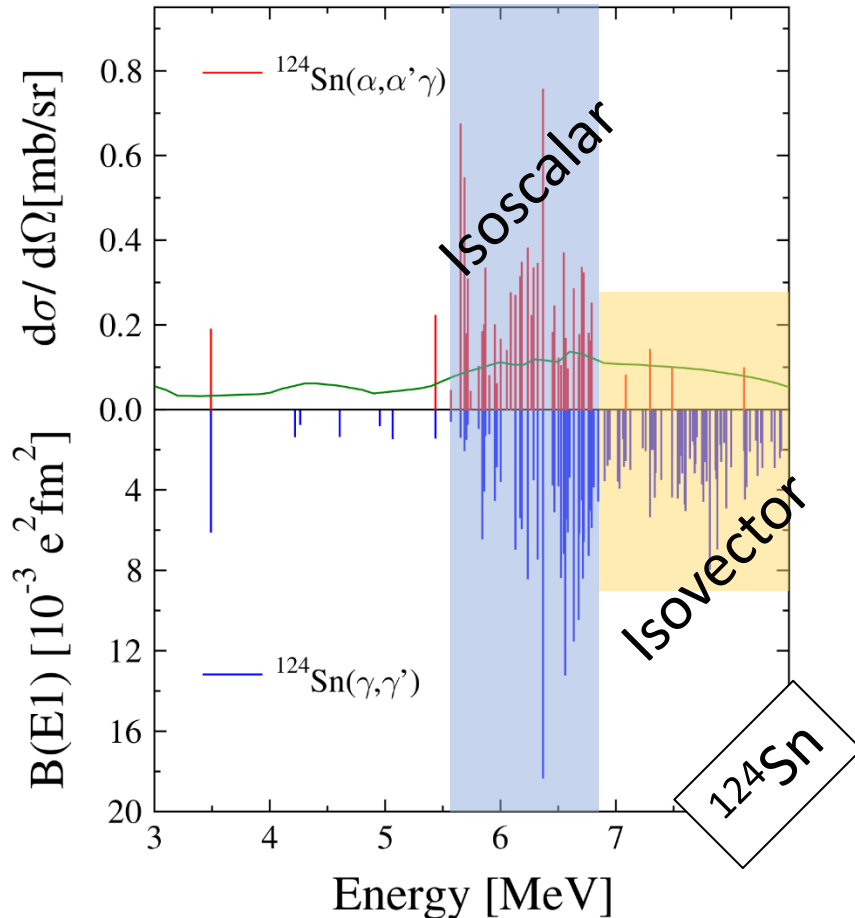
- A short history of complementary experiments on the LEDR
- Microscopic structure:
  - $^{119}\text{Sn}(d,p\gamma)$  and  $^{120}\text{Sn}(\gamma,\gamma')$
  - Quasiparticle-Phonon-Model
  - Comparing apples to apples
- Isoscalar response:
  - $^{120}\text{Sn}(\alpha,\alpha'\gamma)$  at  $E_\alpha = 130$  MeV



$$\Psi_\nu = \left\{ \begin{array}{l} \sum_i R_i(\nu) Q_{1Mi}^+ \\ + \sum_{\substack{\lambda_1 i_1 \\ \lambda_2 i_2}} P_{\lambda_2 i_2}^{\lambda_1 i_1}(\nu) [Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+]_{1M} \\ + \sum_{\substack{\lambda_1 i_1 \lambda_2 i_2 \\ \lambda_3 i_3}} T_{\lambda_3 i_3}^{\lambda_1 i_1 \lambda_2 i_2}(\nu) [ [Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+]_{IK} \\ \times Q_{\lambda_3 \mu_3 i_3}^+]_{1M} \end{array} \right\} \Psi_0$$



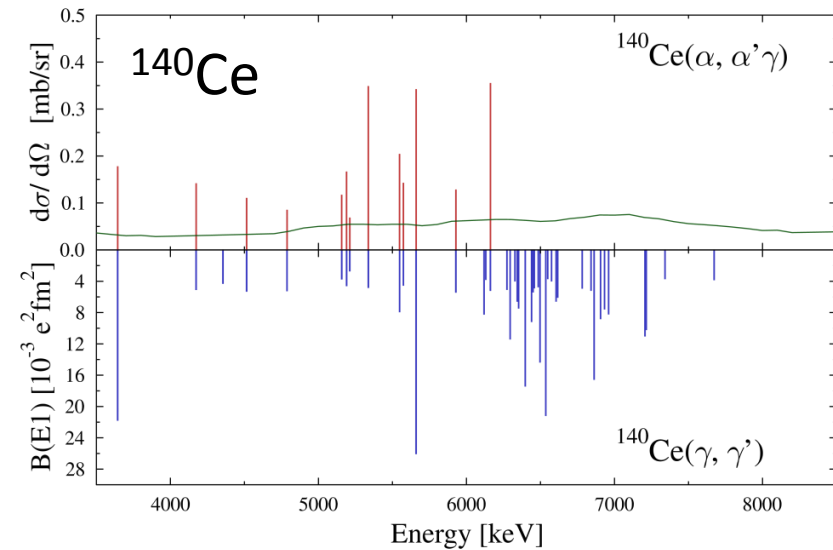
# The Low-Energy Electric Dipole Response



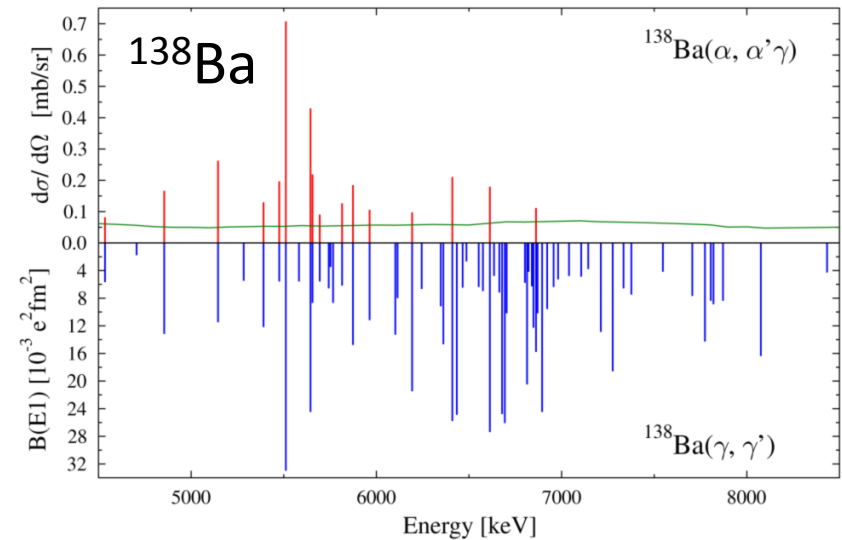
- Photon scattering used to *chart* the LEDR
- Study of total strength and decay behavior
- Comparison to other probes yields deeper insight!
- For example:  
( $\alpha, \alpha'\gamma$ ), ( $p, p'\gamma$ ), ( $^{17}\text{O}, ^{17}\text{O}'\gamma$ )

# Isoscalar E1 response – Isospin *Splitting*

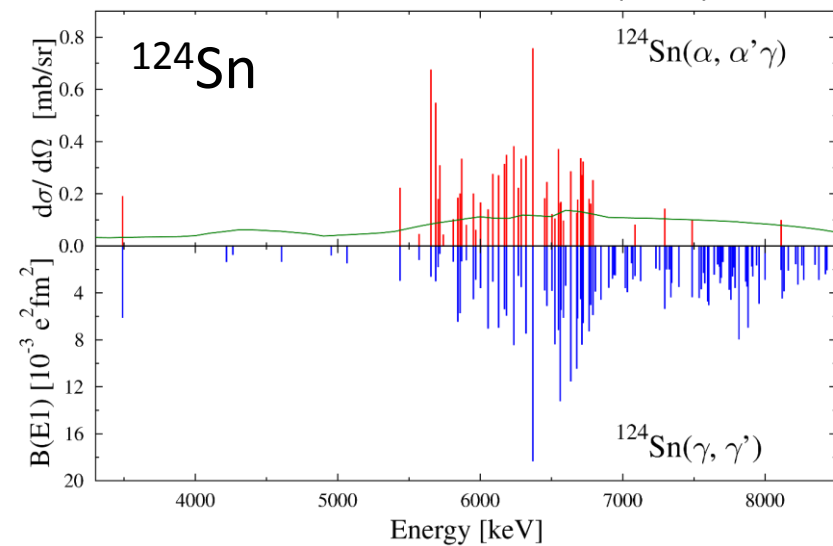
D. Savran *et al.*, PLB **786** (2018) 16



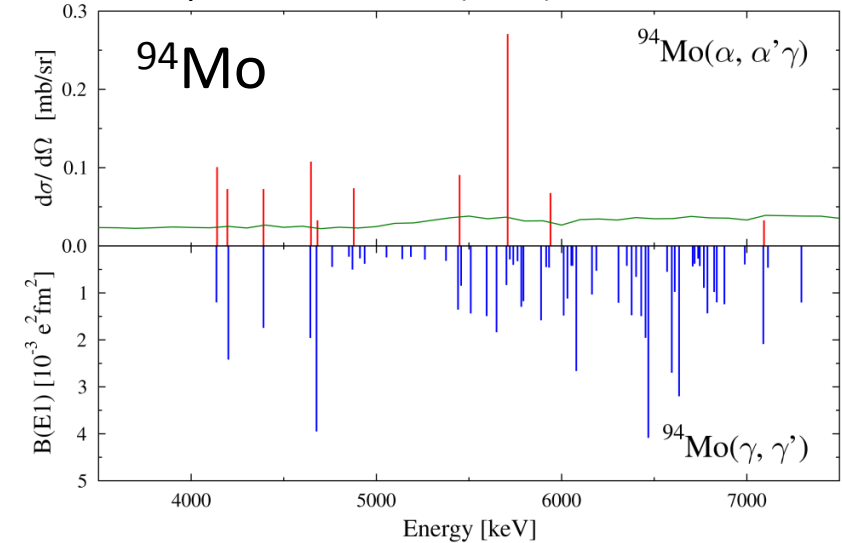
J. Endres *et al.*, PRC **80** (2009) 034302



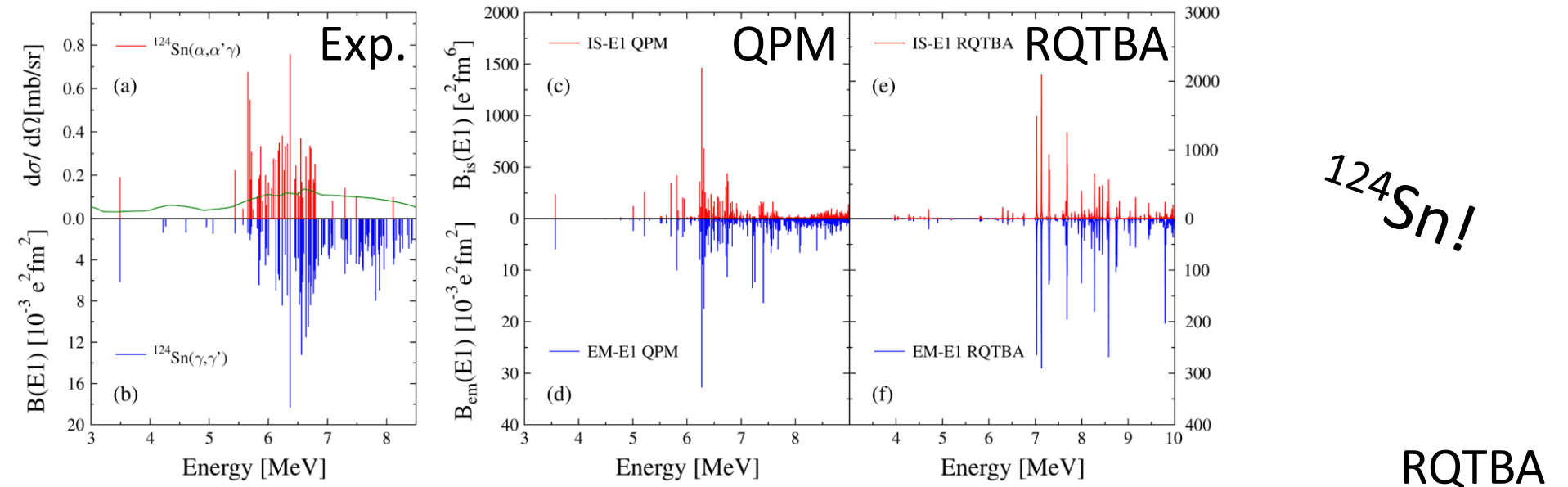
J. Endres, E. Litvinova *et al.*, PRL **105** (2010) 212503



V. Derya *et al.*, NPA **906** (2013) 94



# $^{124}\text{Sn}$ – Experiment and Theory

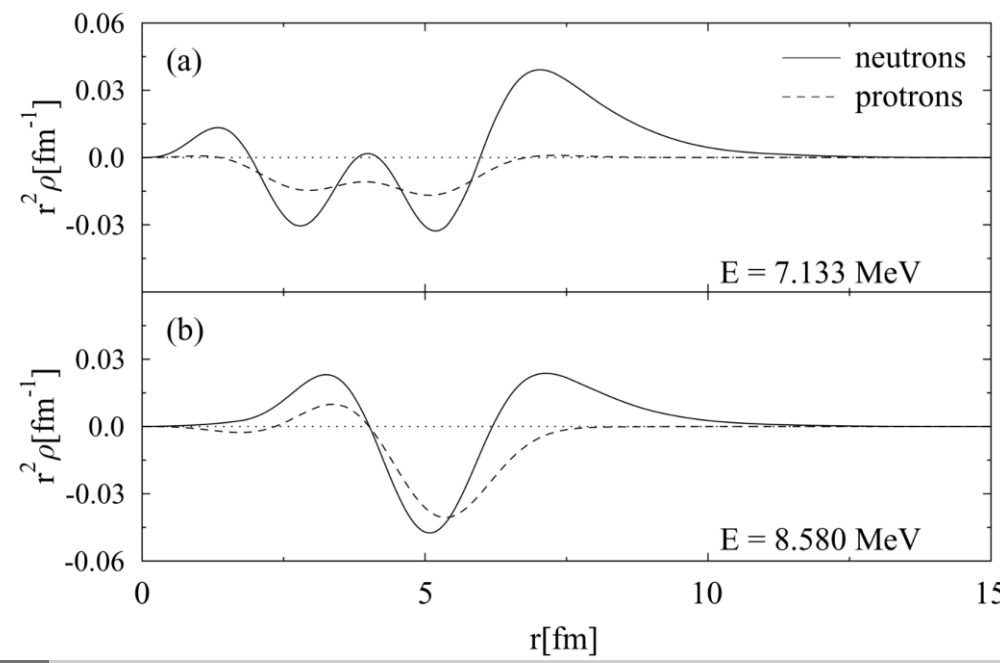


**$^{124}\text{Sn}!$**

**RQTBA**

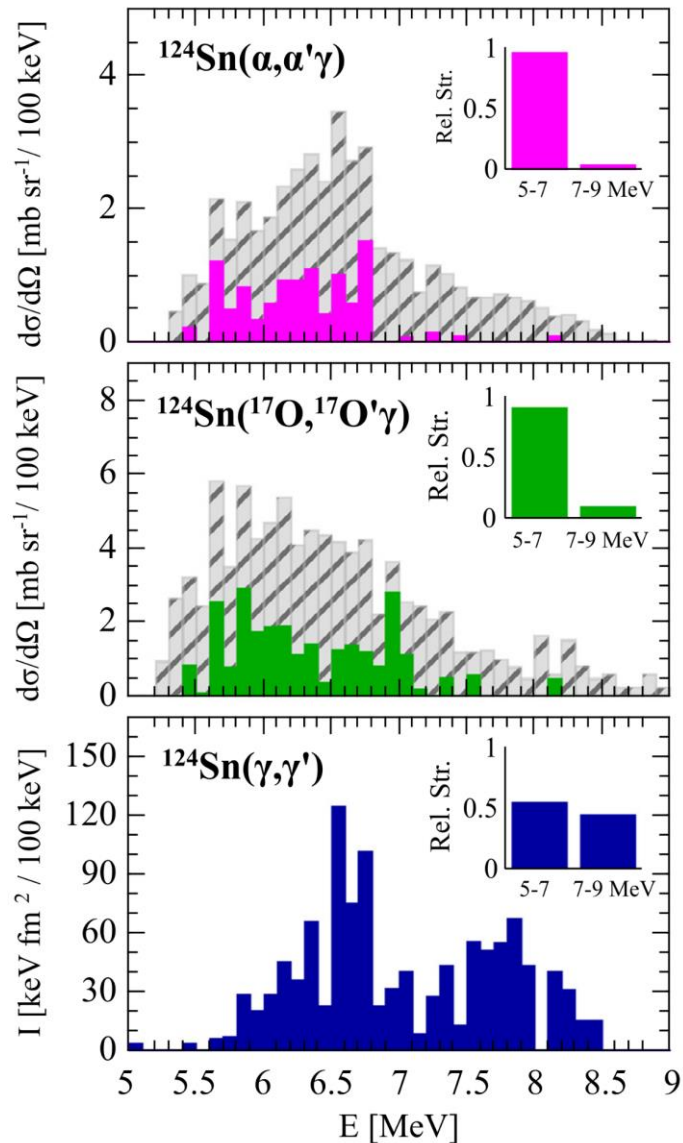
*Splitting* of cross sections reproduced by QPM and RQTBA

Transition densities (TRDs) show *neutron-skin* character in isoscalar part

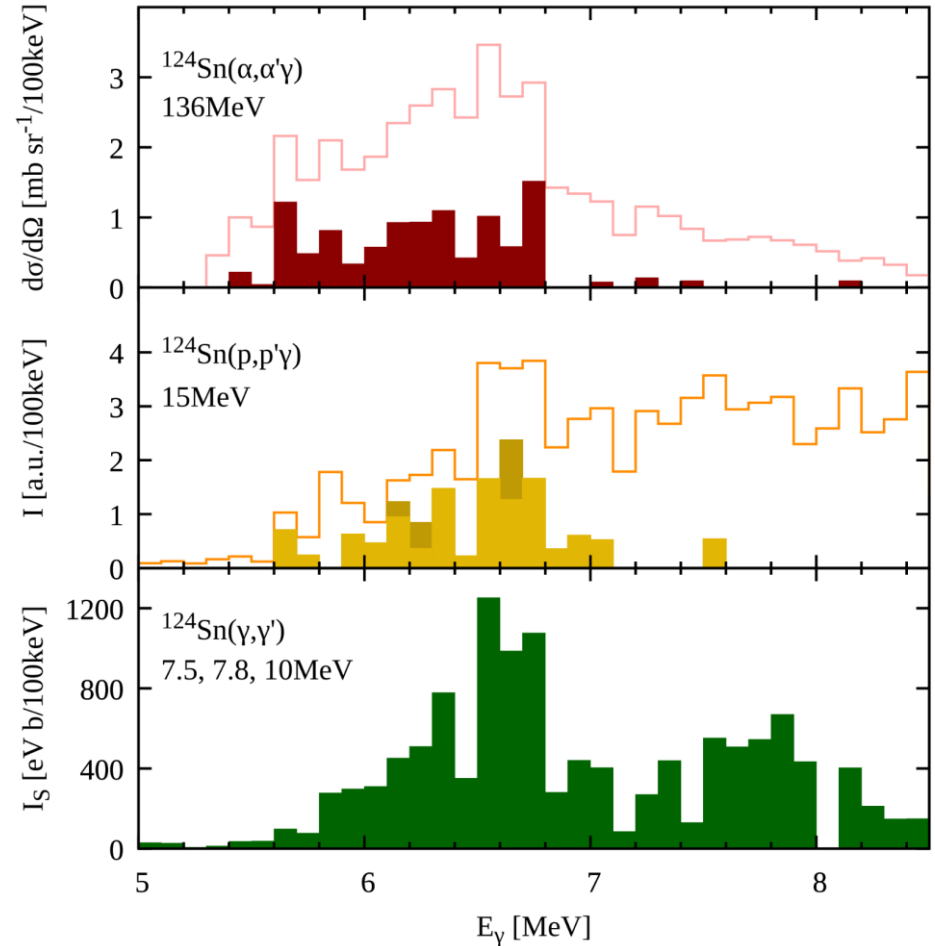


J. Endres, E. Litvinova *et al.*, PRL **105** (2010) 212503  
 J. Endres, D. Savran *et al.*, PRC **85** (2012) 064331

# $^{124}\text{Sn}$ – Other Experiments

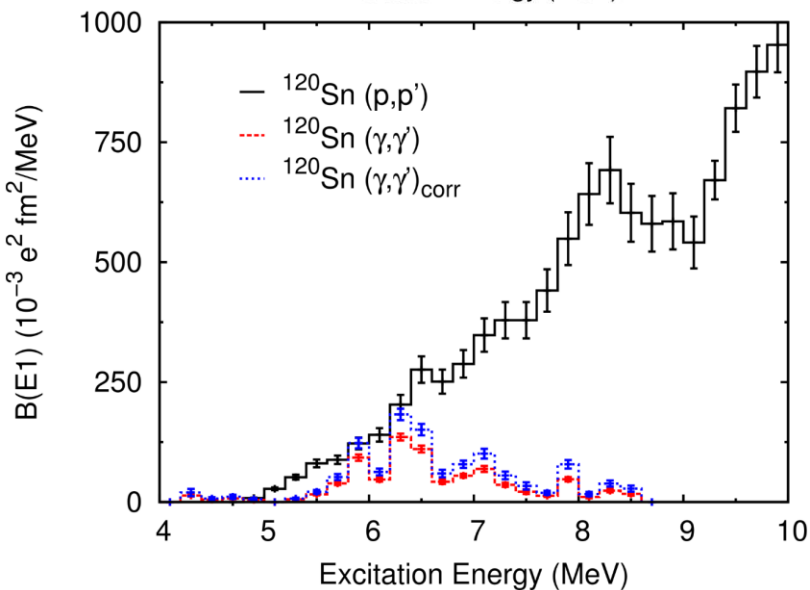
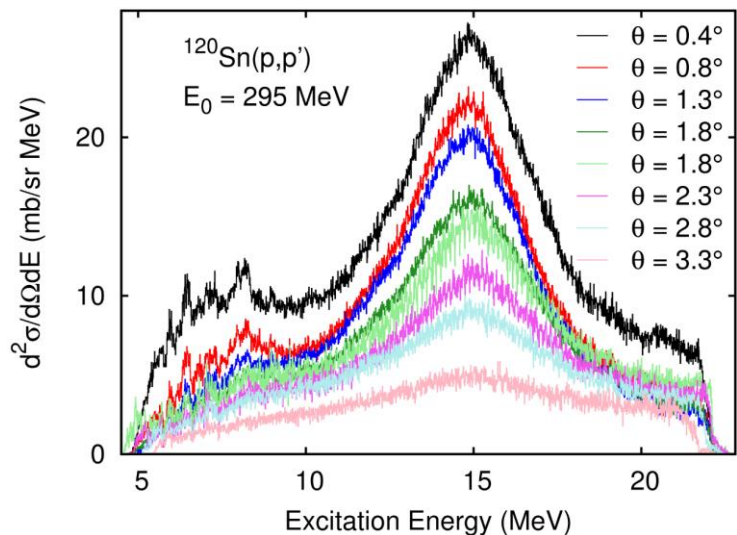


L. Pellegrini *et al.*, PLB **738** (2014) 519

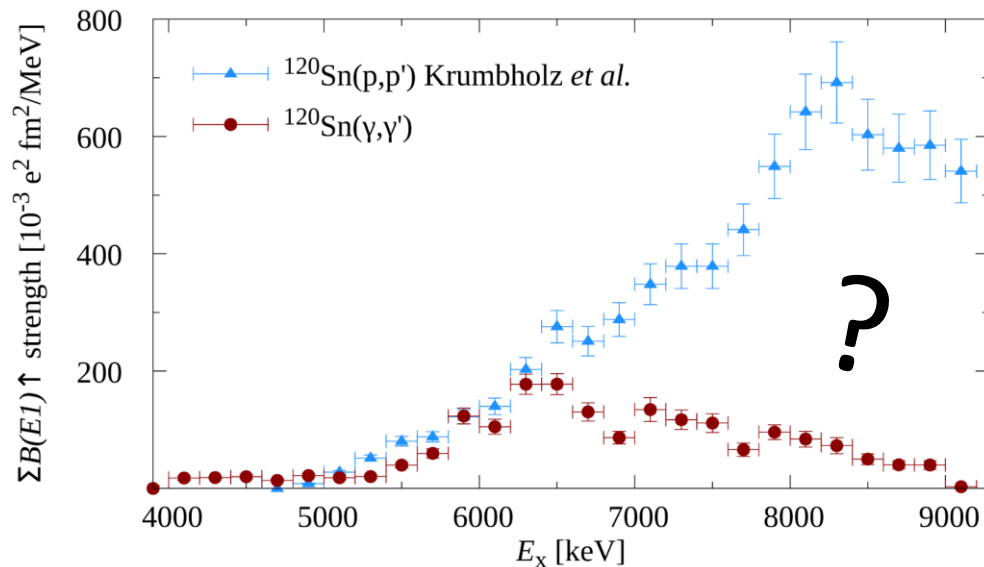


M. Färber, M. Weinert *et al.*, EPJ A **57** (2021) 191

# $^{120}\text{Sn}$ – NRF and CoulEx



A.M. Krumbholz *et al.*, PLB **744** (2015) 7



Recent confirmation of CoulEx data and high sensitivity remeasurement of NRF

→ Discrepancy remains!

→ Caused by nuclear structure?

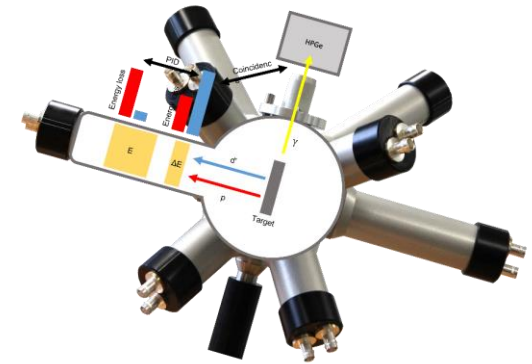
S. Bassauer *et al.*, PRC **102** (2020) 034327

M. Müscher *et al.*, PRC **102** (2020) 014317



# Overview

- A short history of complementary experiments on the LEDR



- Microscopic structure:

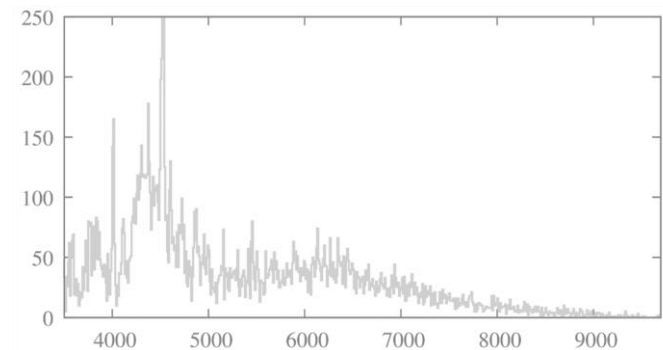
- $^{119}\text{Sn}(d,p\gamma)$  and  $^{120}\text{Sn}(\gamma,\gamma')$
- Quasiparticle-Phonon-Model
- Comparing apples to apples

$$\Psi_\nu = \left\{ \begin{array}{l} \sum_i R_i(\nu) Q_{1Mi}^+ \\ + \sum_{\substack{\lambda_1 i_1 \\ \lambda_2 i_2}} P_{\lambda_2 i_2}^{\lambda_1 i_1}(\nu) [Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+]_{1M} \\ + \sum_{\substack{\lambda_1 i_1 \lambda_2 i_2 \\ \lambda_3 i_3}} T_{\lambda_3 i_3}^{\lambda_1 i_1 \lambda_2 i_2}(\nu) [ [Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+]_{IK} \\ \times Q_{\lambda_3 \mu_3 i_3}^+ ]_{1M} \end{array} \right\} \Psi_0$$

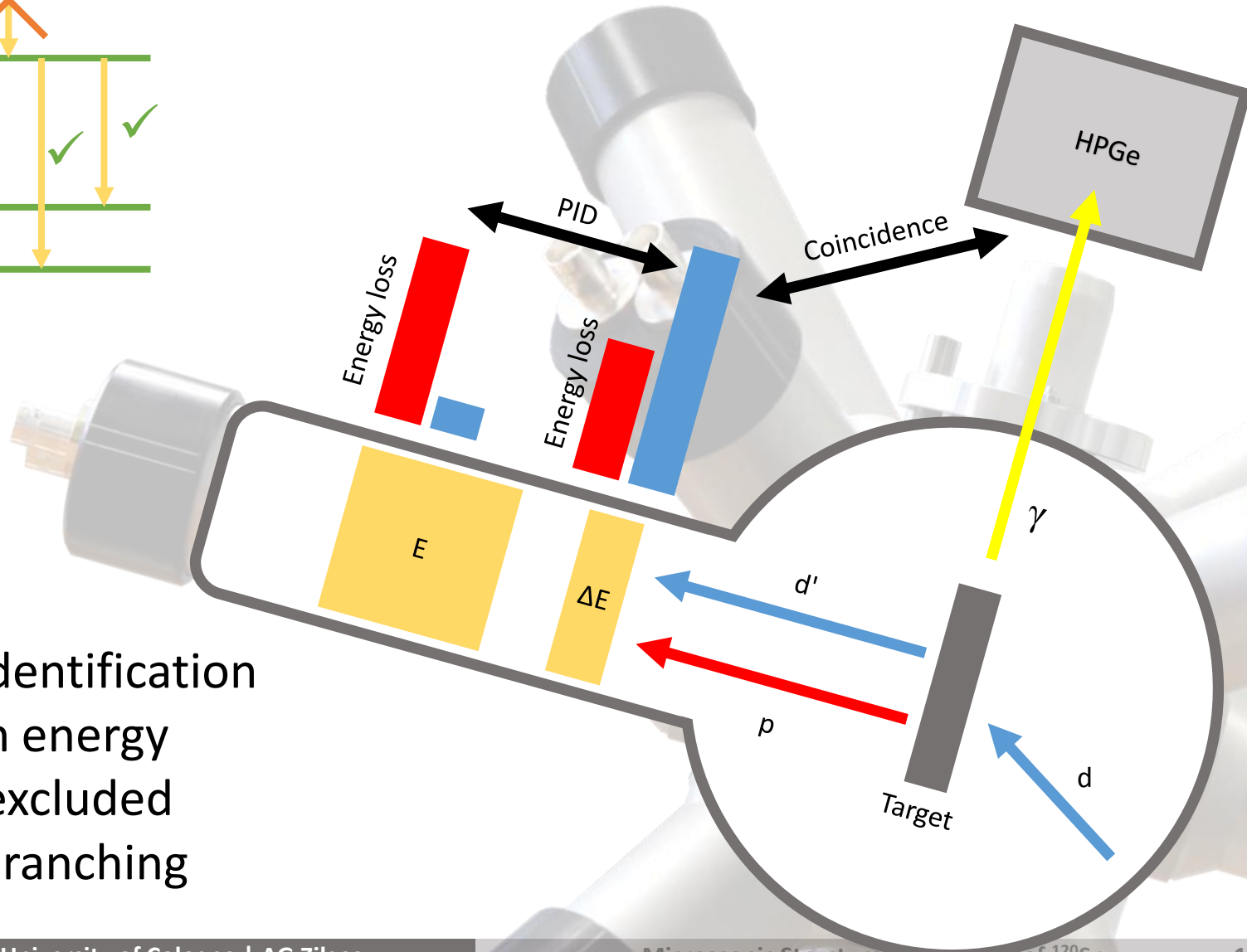
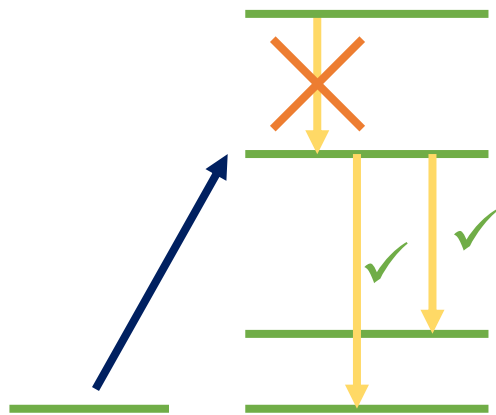


- Isoscalar response:

- $^{120}\text{Sn}(\alpha,\alpha'\gamma)$  at  $E_\alpha = 130$  MeV

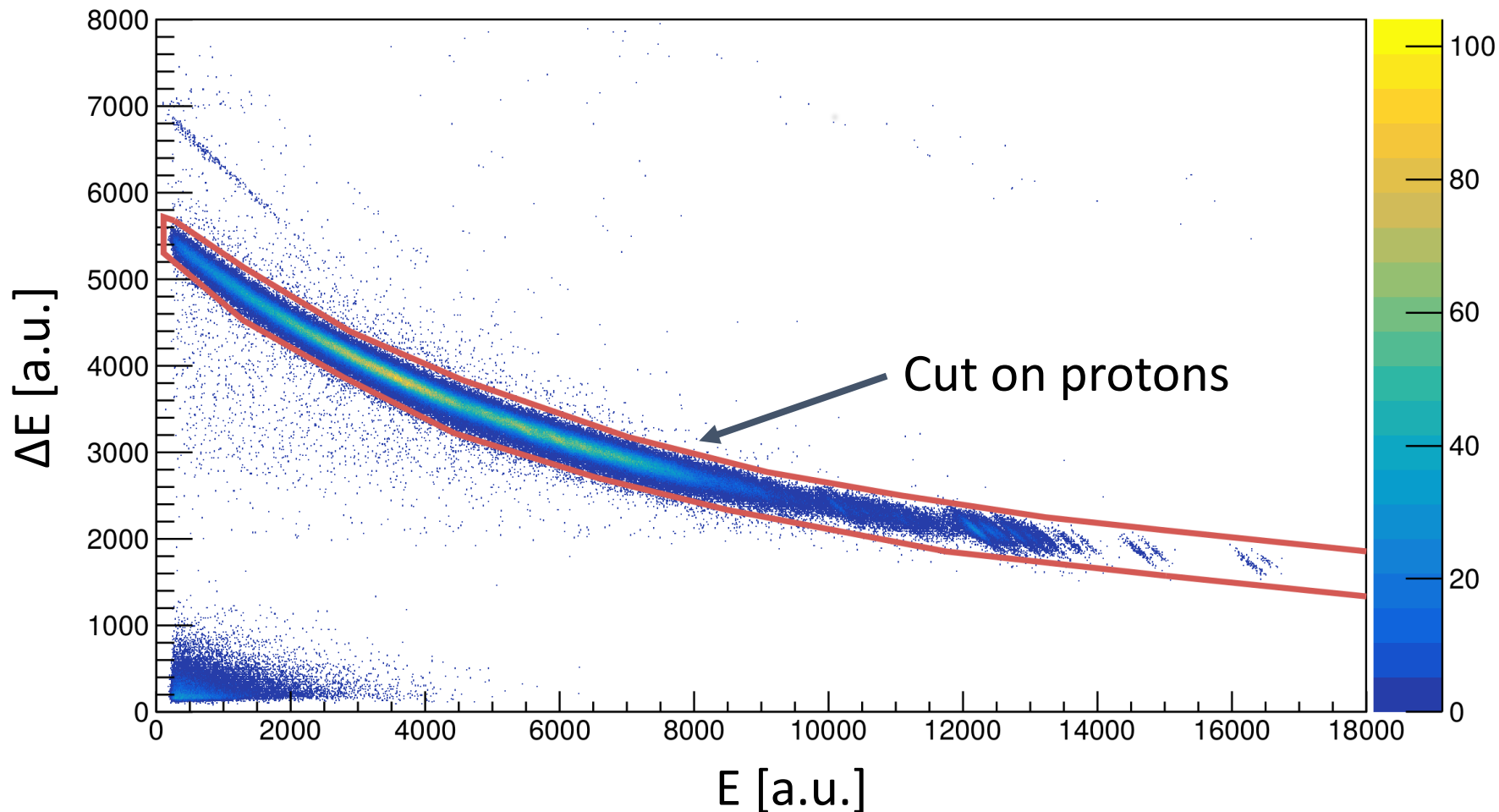


# $^{119}\text{Sn}(d,p\gamma)$ @8.5MeV – SONIC@HORUS



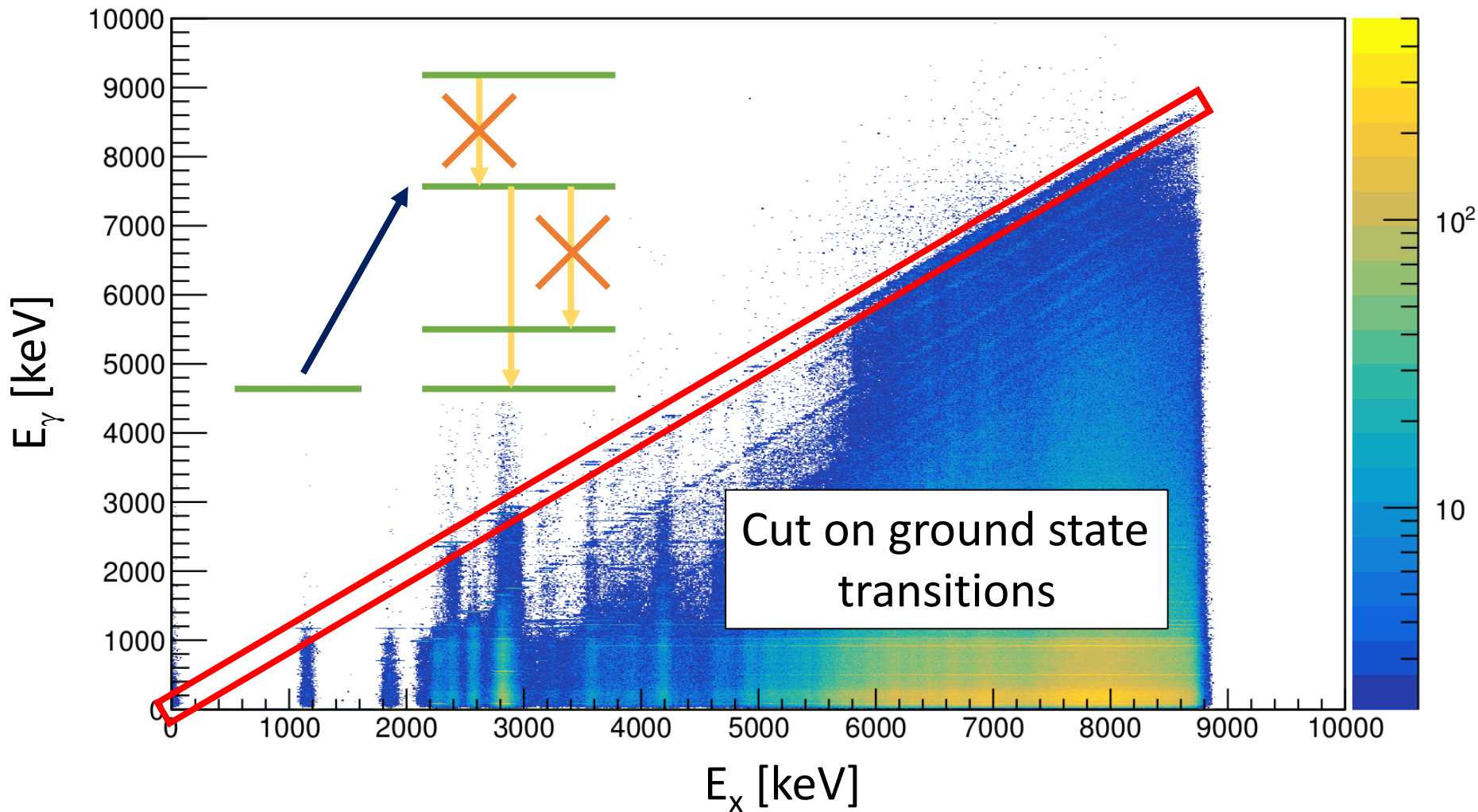
- ✓ Particle identification
- ✓ Excitation energy
- ✓ Feeding excluded
- ✓  $\gamma$ -decay branching

# $^{119}\text{Sn}(d,p\gamma)$ @8.5MeV – SONIC@HORUS



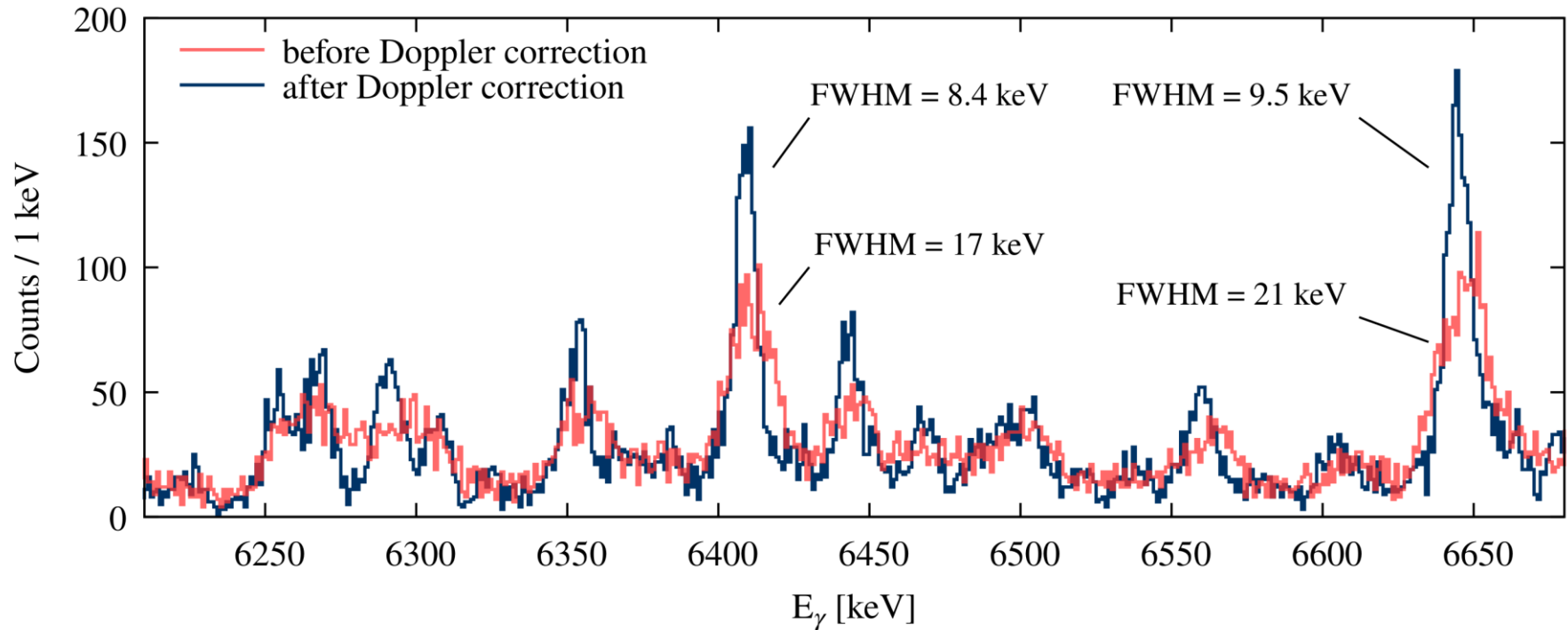
Select protons in  $\Delta E$ - $E$  to distinguish  $(d,p)$  from  $(d,d')$

# $^{119}\text{Sn}(d,p\gamma)$ @8.5MeV – SONIC@HORUS



Select direct excitation and decay into specific state in  $^{120}\text{Sn}$

# $^{119}\text{Sn}(d,p\gamma)$ @8.5MeV – SONIC@HORUS

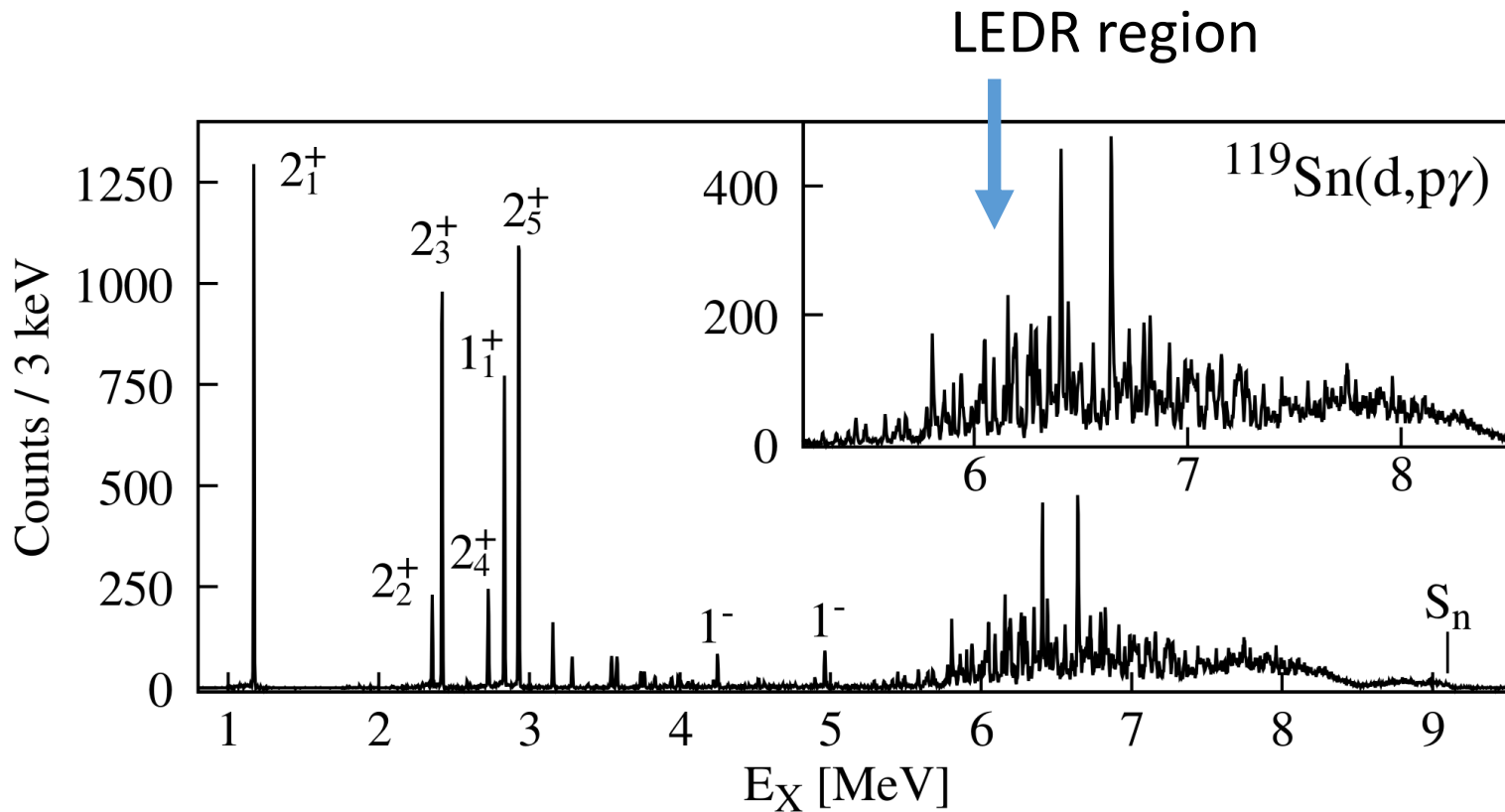


Doppler shift due to recoiling target nuclei ( $\beta=0.0025$ )

Correction assuming very short lifetime and in-flight decay

Nominal HPGe resolution restored in summed spectrum!

# $^{119}\text{Sn}(d,p\gamma)$ @8.5MeV – SONIC@HORUS



Ground state  $\gamma$ -decay spectrum after Doppler correction and gating on  $E_X = E_\gamma$  shows only J=1,2 states

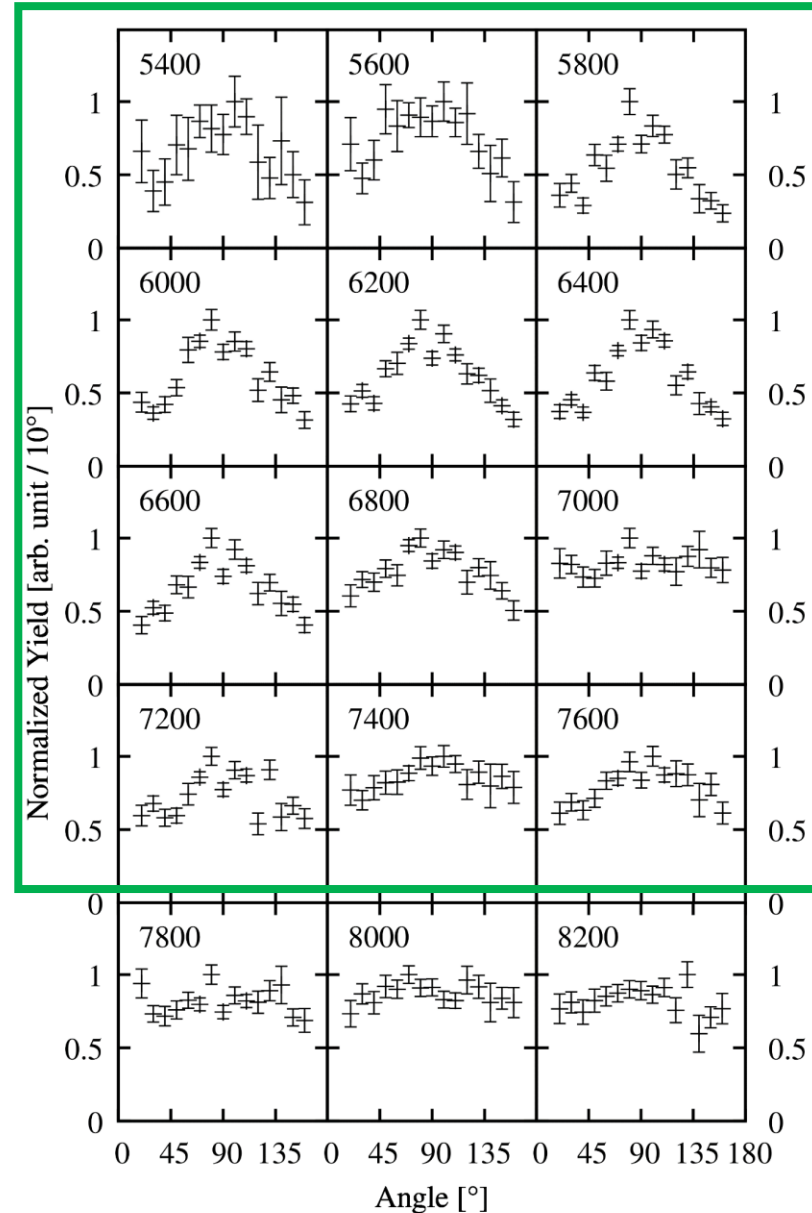
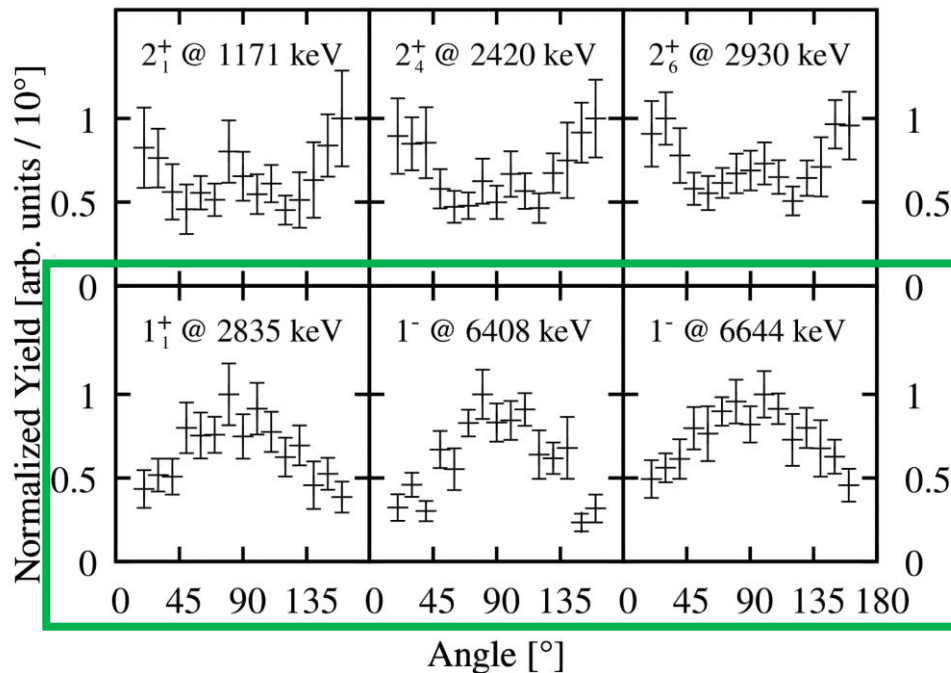
# $^{119}\text{Sn}(d,p\gamma)$ @8.5MeV – SONIC@HORUS

$\gamma$ -ray angular distributions  
relative to recoil nucleus,  
a.k.a. the Doppler-angle

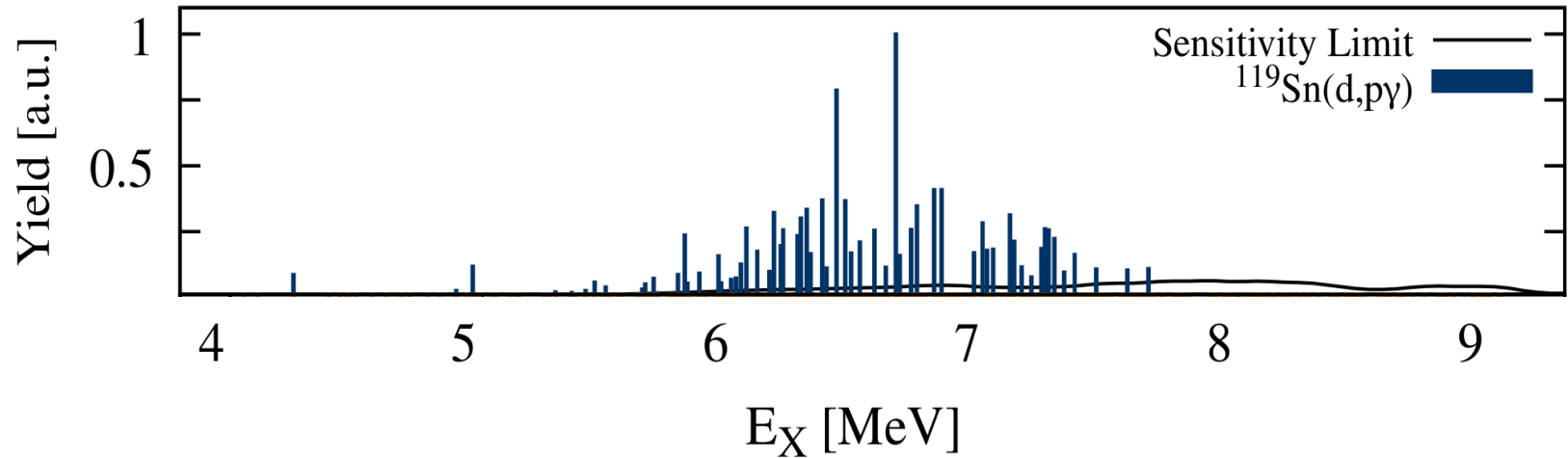
Continuous



Discrete transitions



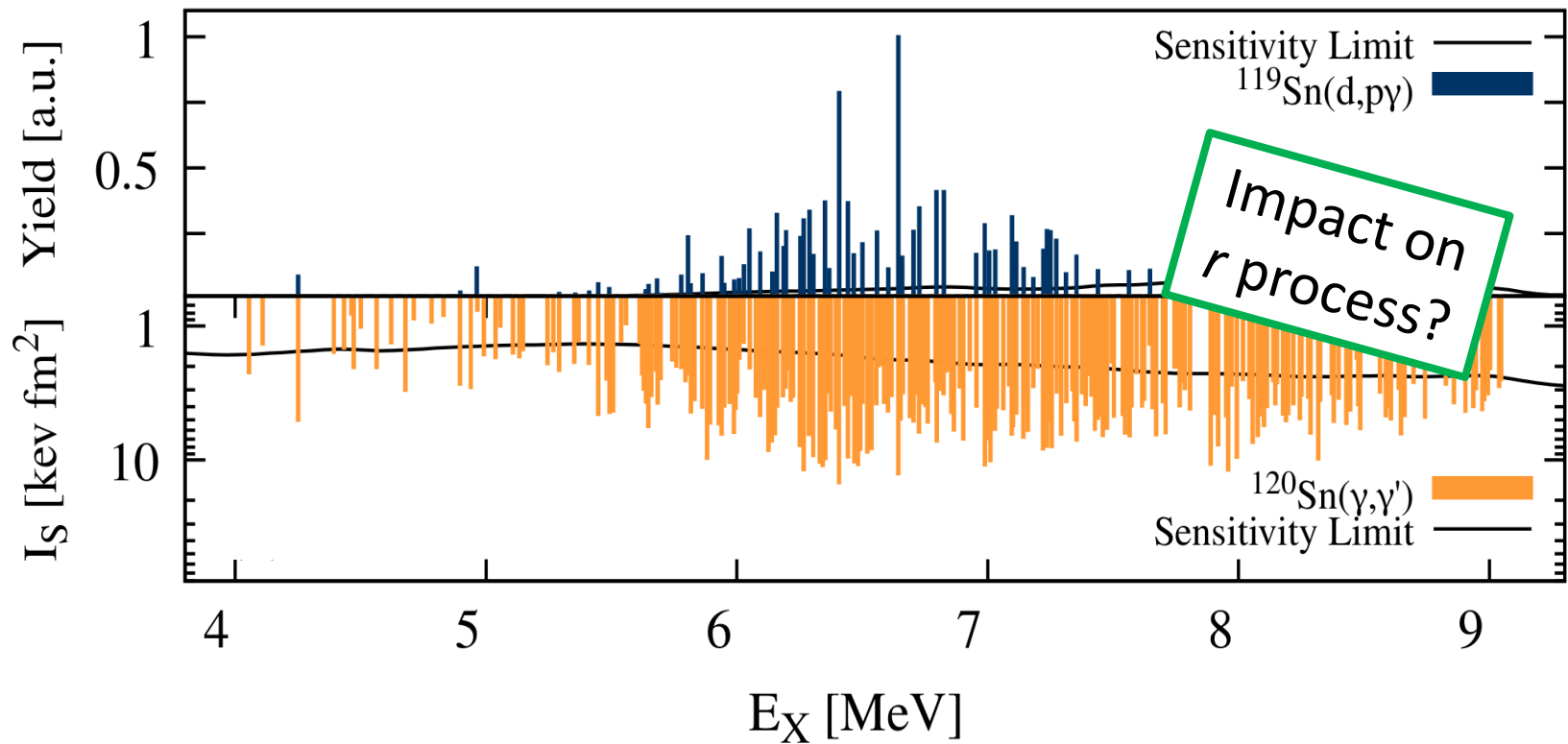
# $^{119}\text{Sn}(d,p\gamma)$



- 64 of 80 observed lines have matching energy to  $(\gamma, \gamma')$
- Angular distributions confirm  $\Delta L=1$  dominant up to 7.5 MeV
- From CoulEx: M1 contribution likely negligible
  - All discretely observed lines are  $J^\pi = 1^-$  states !



# $^{119}\text{Sn}(d,p\gamma)$ vs $^{120}\text{Sn}(\gamma,\gamma')$

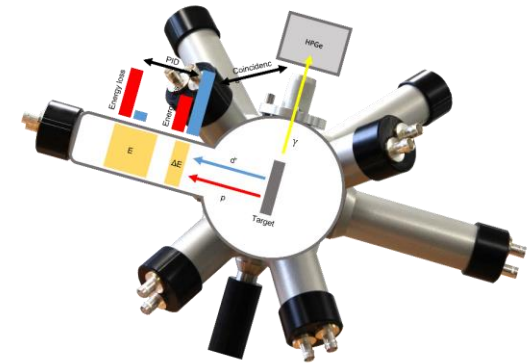


- Strong state-to-state difference between  $(d,p\gamma)$  and  $(\gamma,\gamma')$
- Missing strength above 7.5 MeV intriguing...  
→ Structure reasons?

NRF data from: M. M $\ddot{u}$ scher *et al.*, PRC **102**, 014317 (2020)

# Overview

- A short history of complementary experiments on the LEDR

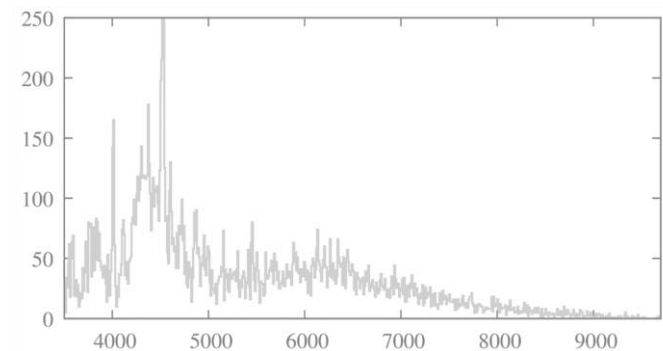


- Microscopic structure:
  - $^{119}\text{Sn}(d,p\gamma)$  and  $^{120}\text{Sn}(\gamma,\gamma')$
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- Isoscalar response:
  - $^{120}\text{Sn}(\alpha,\alpha'\gamma)$  at  $E_\alpha = 130$  MeV



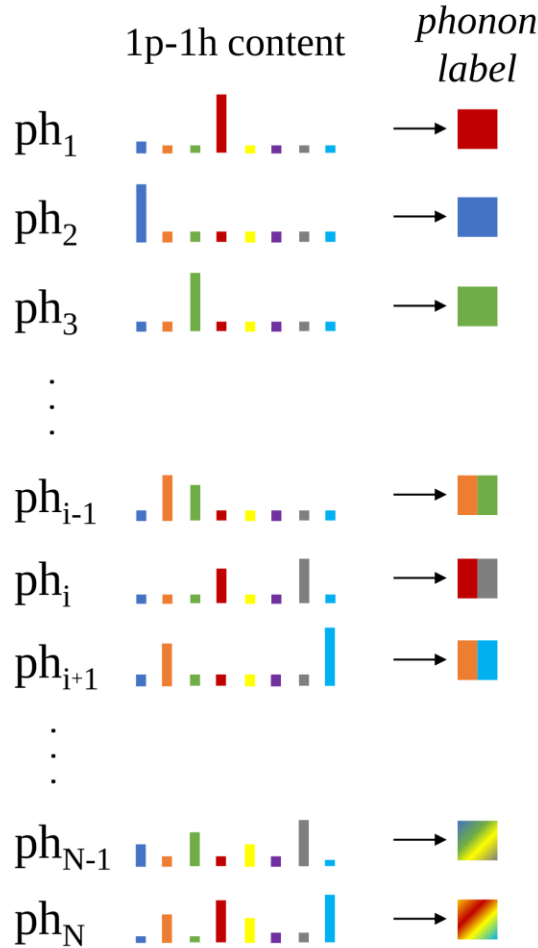
# $^{119}\text{Sn}(d,p\gamma)$ – Quasiparticle-Phonon-Model

Single-Particle configurations

- $\nu()^1()^{-1}$  ●
- $\nu()^1()^{-1}$  ●
- $\nu()^1()^{-1}$  ●
- $\nu()^1()^{-1}$  ●
- $\vdots$
- $\pi()^1()^{-1}$  ●
- $\pi()^1()^{-1}$  ●
- $\pi()^1()^{-1}$  ●
- $\pi()^1()^{-1}$  ●

EDF+QRPA

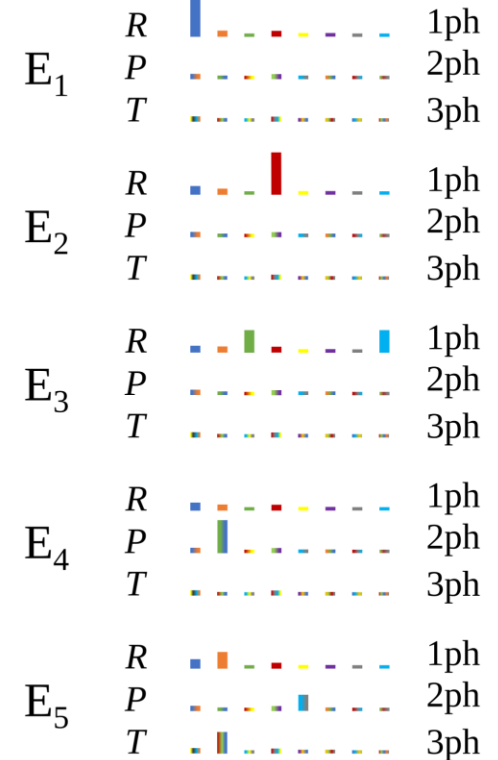
QRPA Phonons



1+2+3 ph QPM

QPM States

phonon content



R<sub>i</sub>: ph<sub>i</sub>

P<sub>i</sub>: ph<sub>j</sub> ⊗ ph<sub>k</sub>

T<sub>i</sub>: ph<sub>j</sub> ⊗ ph<sub>k</sub> ⊗ ph<sub>l</sub>

# $^{119}\text{Sn}(d, p\gamma) - \text{Quasiparticle-Phonon-Model}$

$$\Psi_\nu = \left\{ \begin{aligned} & \sum_i R_i(\nu) Q_{1Mi}^+ \\ & + \sum_{\substack{\lambda_1 i_1 \\ \lambda_2 i_2}} P_{\lambda_2 i_2}^{\lambda_1 i_1}(\nu) \left[ Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+ \right]_{1M} \\ & + \sum_{\substack{\lambda_1 i_1 \lambda_2 i_2 \\ \lambda_3 i_3 I}} T_{\lambda_3 i_3}^{\lambda_1 i_1 \lambda_2 i_2 I}(\nu) \left[ \left[ Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+ \right]_{IK} \right. \\ & \quad \left. \times Q_{\lambda_3 \mu_3 i_3}^+ \right]_{1M} \end{aligned} \right\} \Psi_0$$

Each QPM state is built from contributions that represent

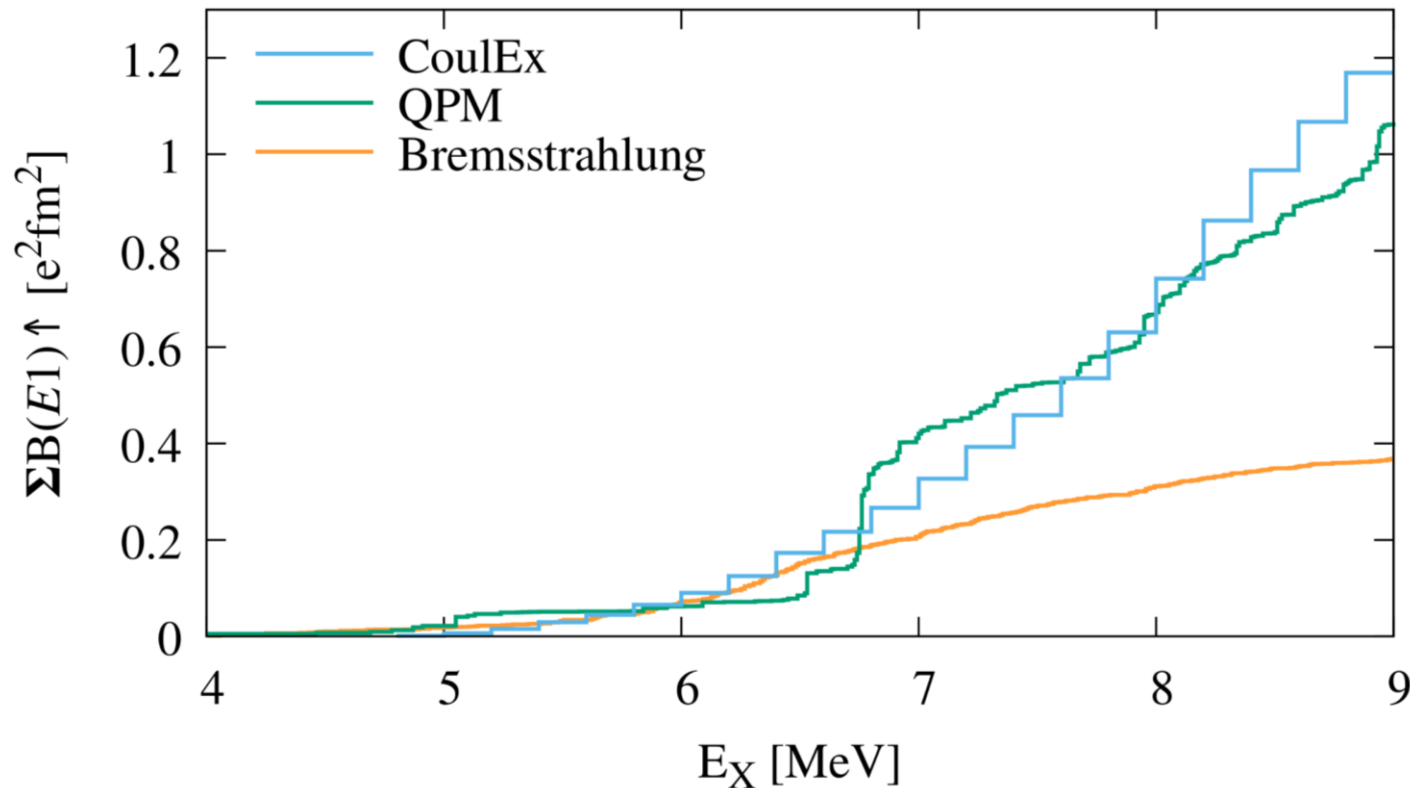
one phonon

two phonons

three phonons

# $^{120}\text{Sn}$ QPM – Electromagnetic Response

$B(E1)\uparrow$  running sums from  $(\gamma,\gamma')$  and  $(p,p')$ -CoulEx



1.169(12)  $e^2\text{fm}^2$   
1.066  $e^2\text{fm}^2$

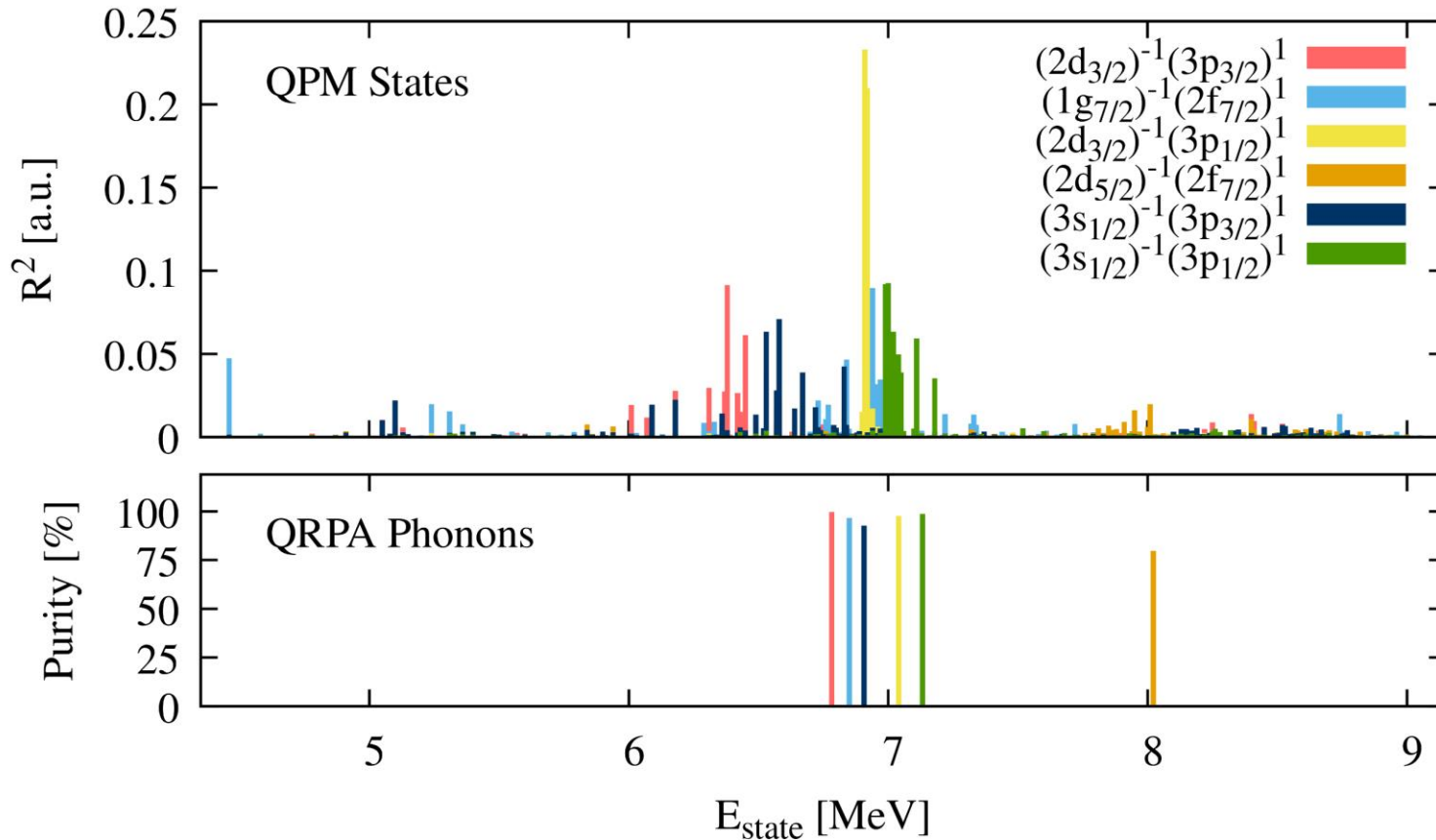
0.369(49)  $e^2\text{fm}^2$

QPM reproduces CoulEx data nicely!

CoulEx: A.M. Krumbholz *et al.*, PLB **744** (2015) 7

Bremsstrahlung: M. Müscher *et al.*, PRC **102**, 014317 (2020)

# $^{120}\text{Sn}$ – QPM One-Phonon Distribution



Distribution of only the dominant 1ph contributions to QPM states

Concentrated around 6-7 MeV

# $^{119}\text{Sn}(d,p\gamma) - \text{QPM} + \text{Reaction Theory}$

$$\Psi_\nu = \left\{ \begin{aligned} & \sum_i R_i(\nu) Q_{1Mi}^+ \\ & + \sum_{\substack{\lambda_1 i_1 \\ \lambda_2 i_2}} P_{\lambda_2 i_2}^{\lambda_1 i_1}(\nu) \left[ Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+ \right]_{1M} \\ & + \sum_{\substack{\lambda_1 i_1 \lambda_2 i_2 \\ \lambda_3 i_3 I}} T_{\lambda_3 i_3}^{\lambda_1 i_1 \lambda_2 i_2 I}(\nu) \left[ \left[ Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+ \right]_{IK} \right. \\ & \quad \left. \times Q_{\lambda_3 \mu_3 i_3}^+ \right]_{1M} \end{aligned} \right\} \Psi_0$$

(d,p) reaction selects only **one phonon** contributions that are accessible from the **ground state of  $^{119}\text{Sn}$** !

Each QPM state is built from contributions that represent

one phonon

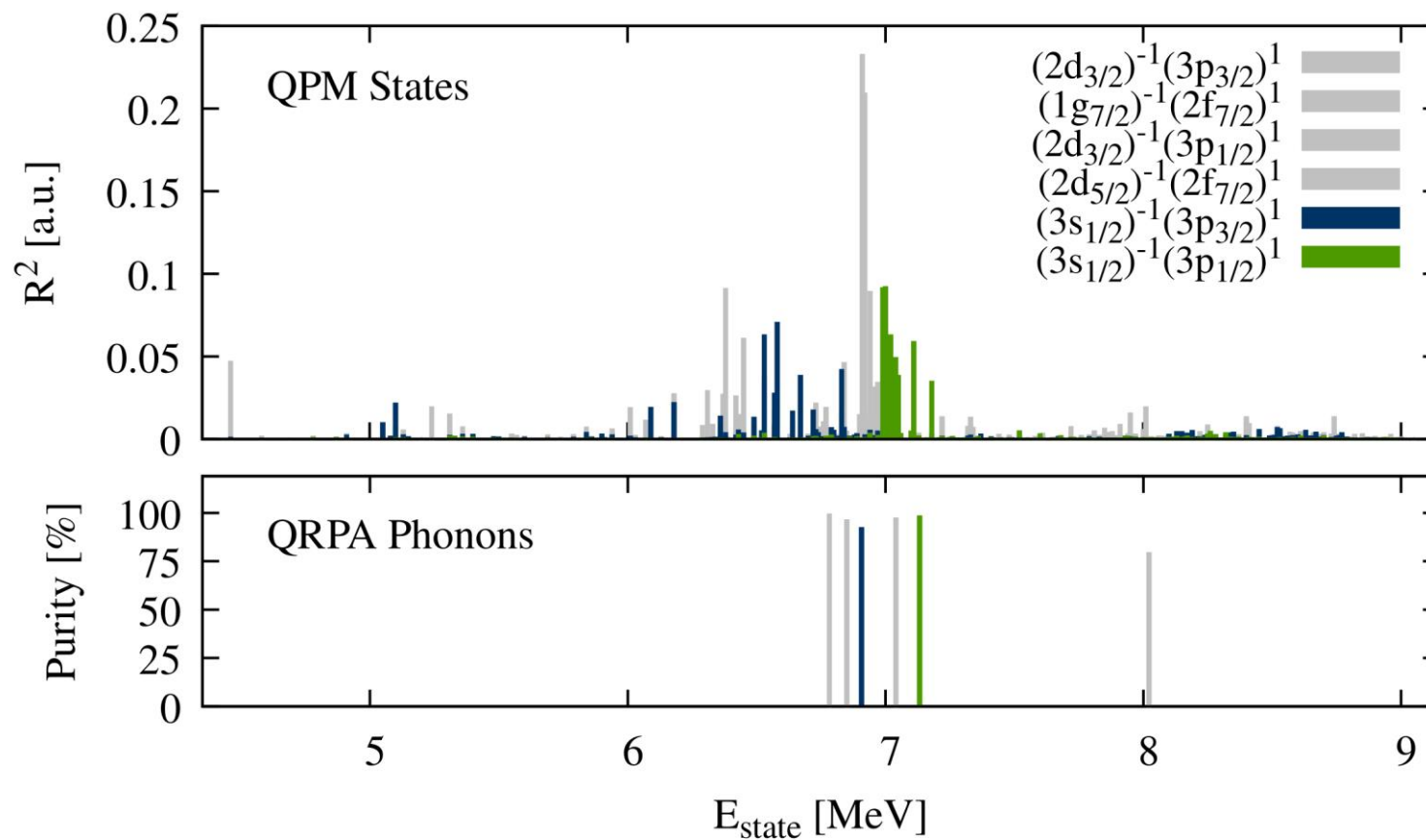
two phonons

three phonons

$$\frac{d\sigma_\nu}{d\Omega}(\theta) = \frac{\mu_i \mu_f}{(2\pi \hbar^2)^2} \frac{k_f}{k_i} \times \left| \begin{aligned} & u_{3p_{1/2}} R_{3p_{1/2}}(\nu) \psi_{\frac{1}{2} \frac{1}{2}}^{3p_{1/2}} \mathcal{T}_{p_{1/2}}(\theta) \\ & + u_{3p_{3/2}} R_{3p_{3/2}}(\nu) \psi_{\frac{1}{2} \frac{3}{2}}^{3p_{3/2}} \mathcal{T}_{p_{3/2}}(\theta) \end{aligned} \right|^2$$

# $^{120}\text{Sn}$ – QPM One-Phonon Distribution

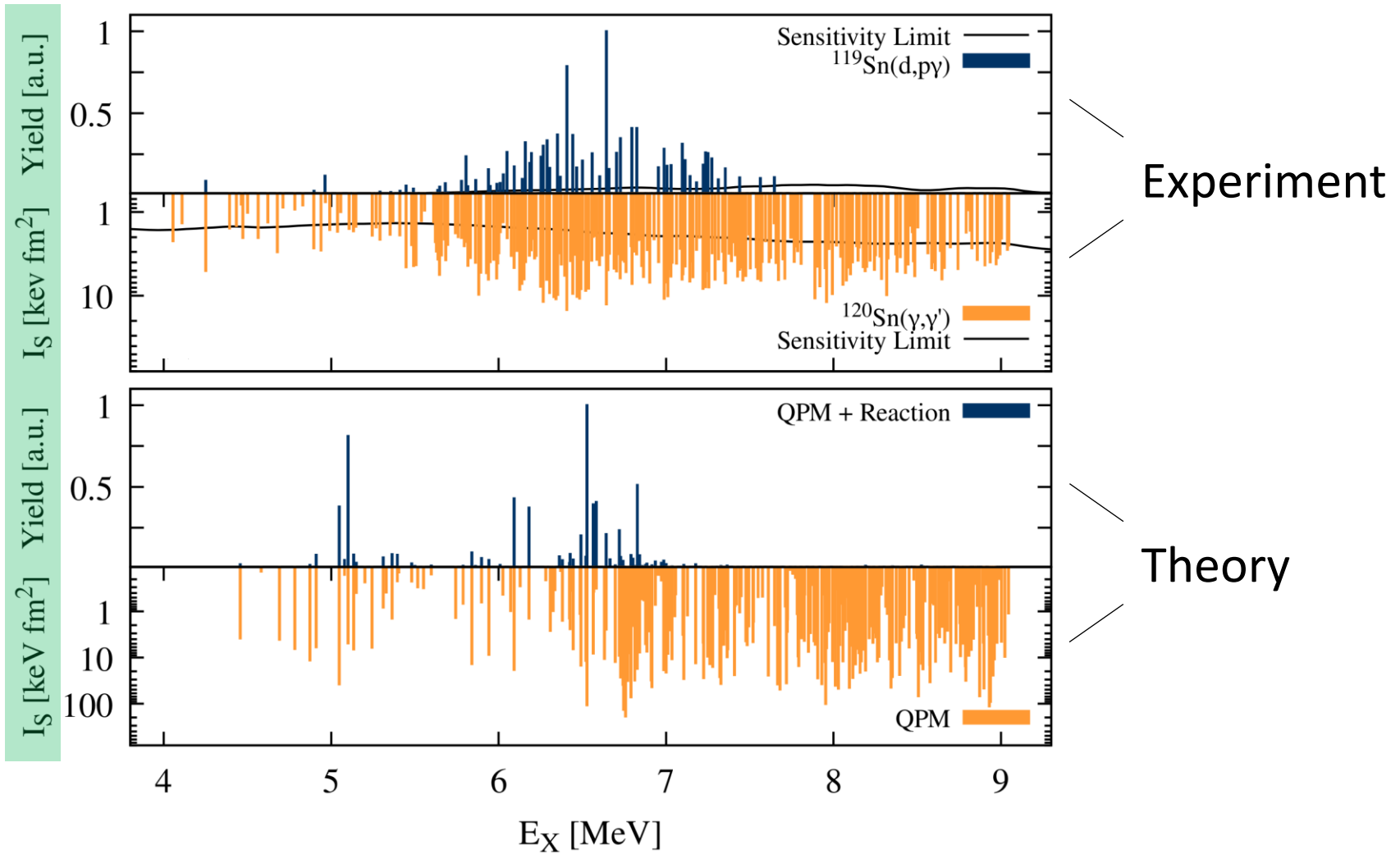
QPM 1ph contributions relevant for  $^{119}\text{Sn}(d,p)$



Theory provided by N. Tsoneva



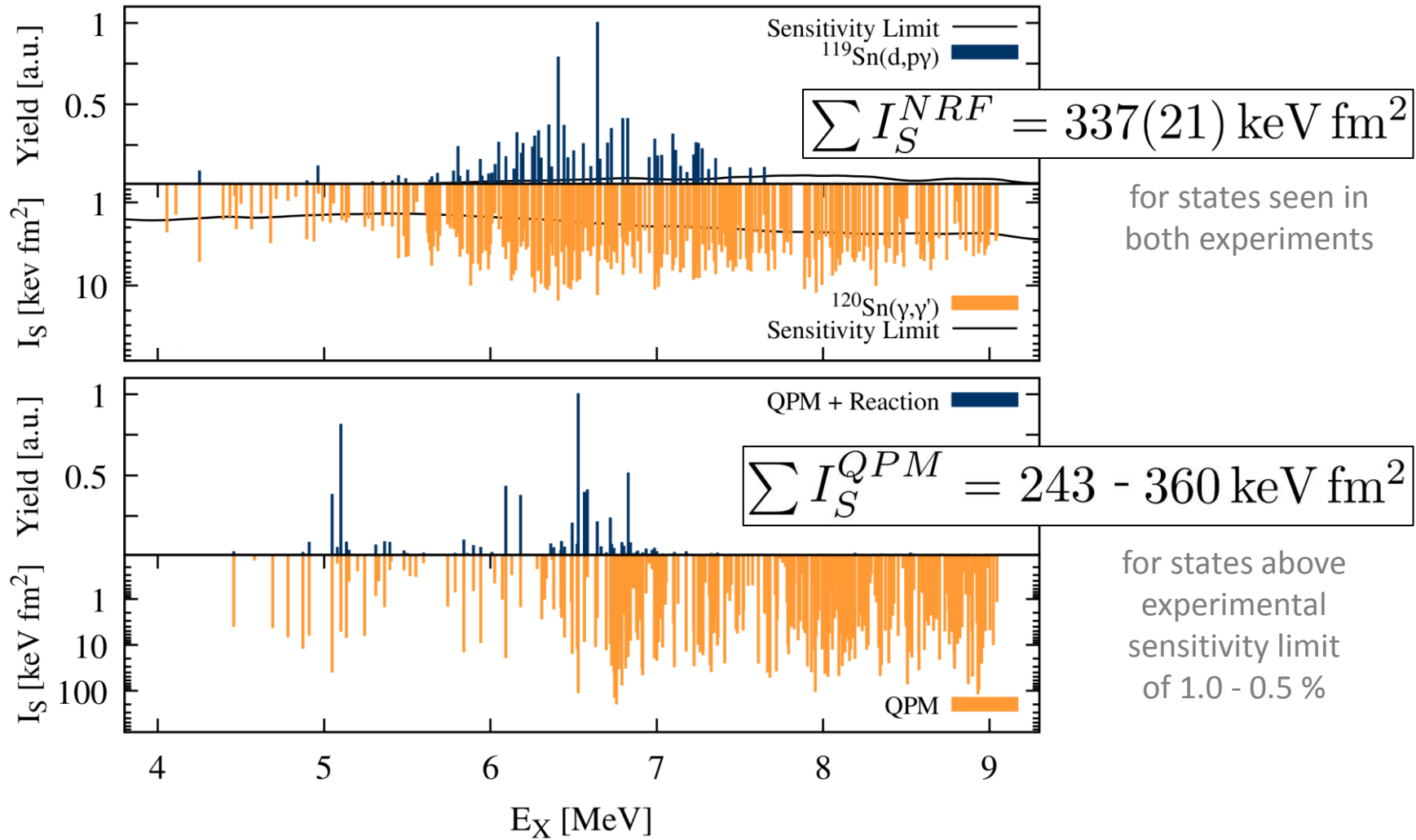
# Experiment and Theory – Apples and Apples



Theory provided by N. Tsoneva and G. Potel

M. Weinert *et al.*, Phys. Rev. Lett. **127** (2021) 242501

# Experiment and Theory – Apples and Apples



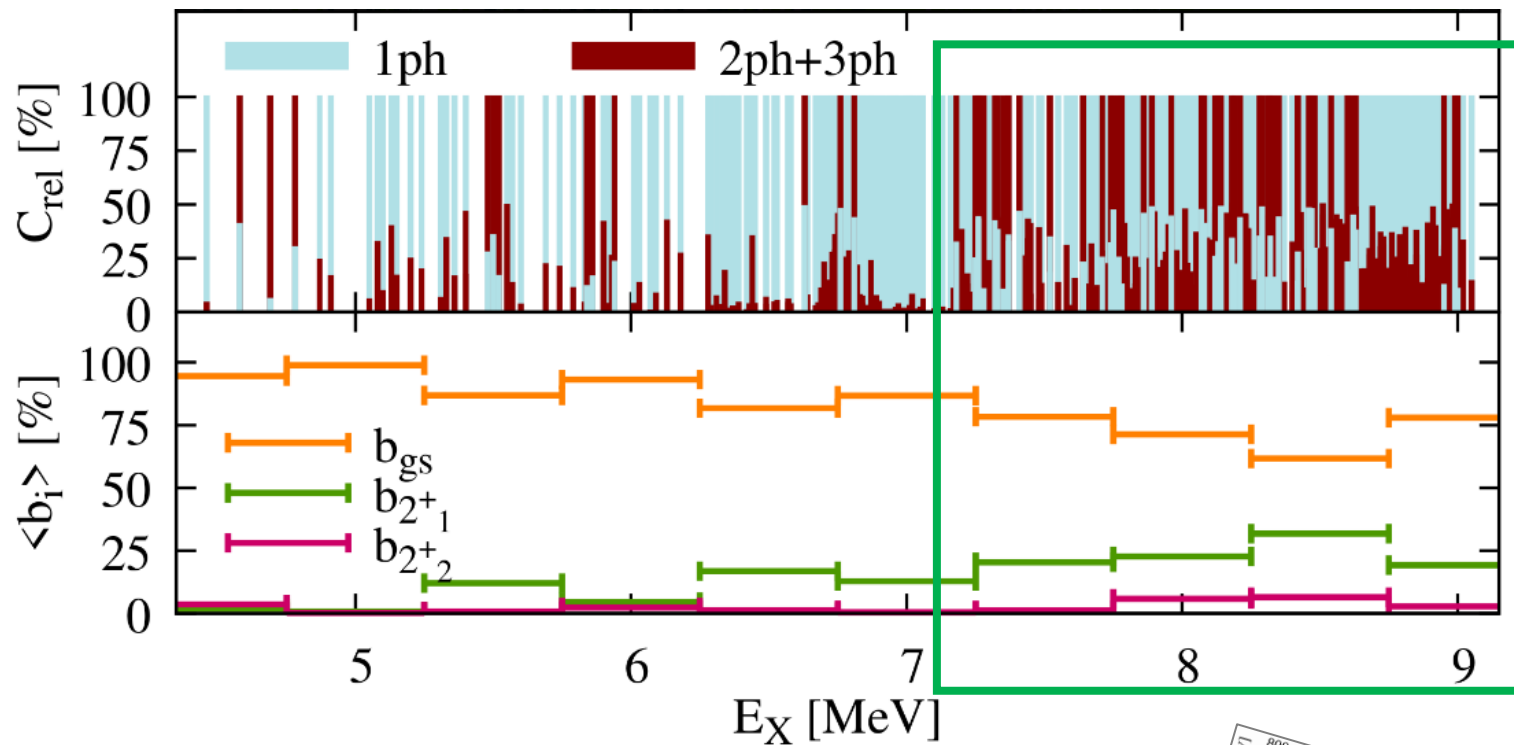
Theory provided by N. Tsoneva and G. Potel

M. Weinert *et al.*, Phys. Rev. Lett. **127** (2021) 242501

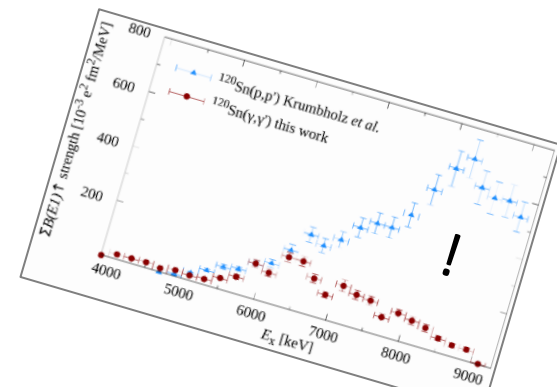
# QPM – Detailed Access to Wave Functions

$$C_{rel}^{1ph} = \sum R^2 / \sum (R^2 + P^2 + T^2)$$

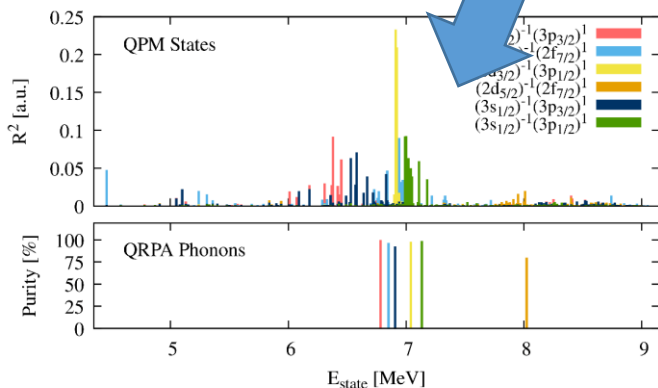
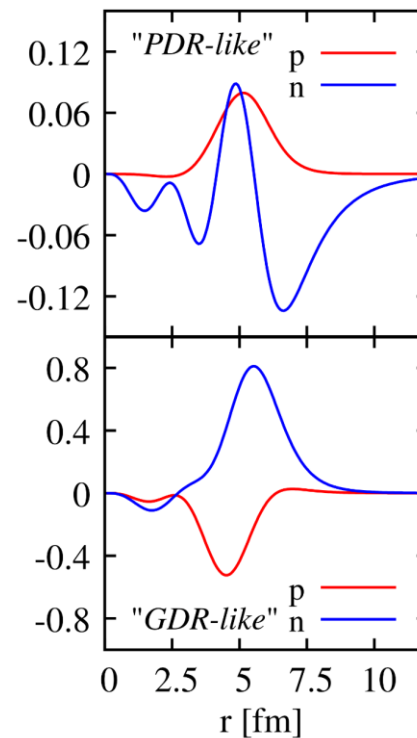
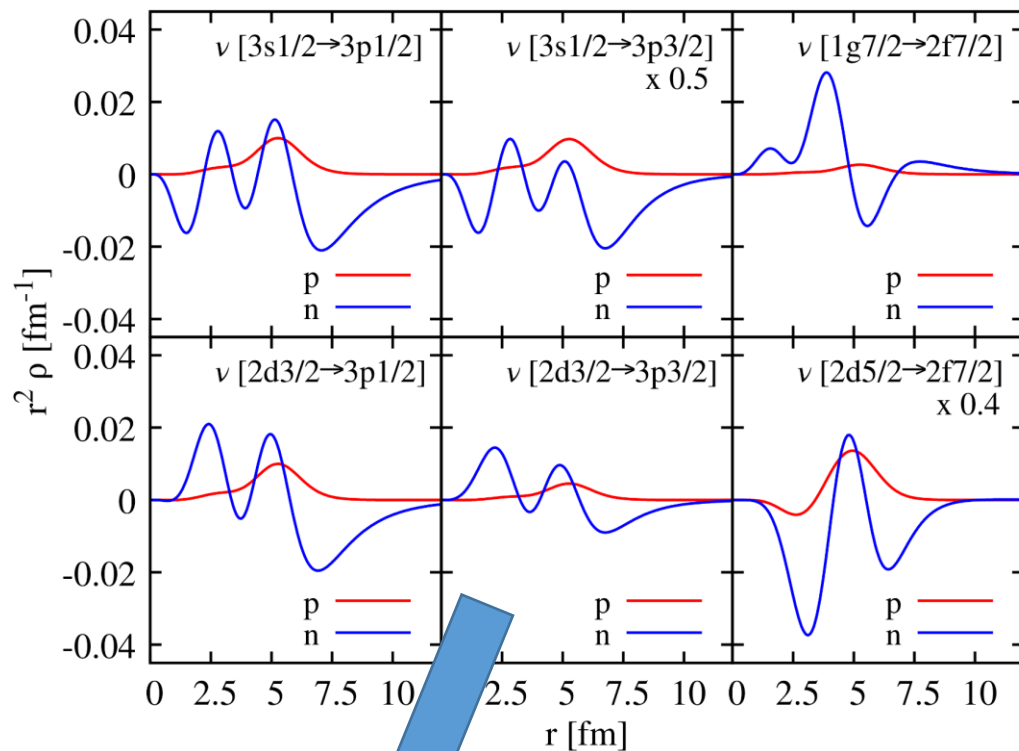
$$C_{rel}^{2ph+3ph} = \sum (P^2 + T^2) / \sum (R^2 + P^2 + T^2)$$



Single-particle character and increasing complexity at the right excitation energies predicted by the QPM!



# QPM Transition Densities

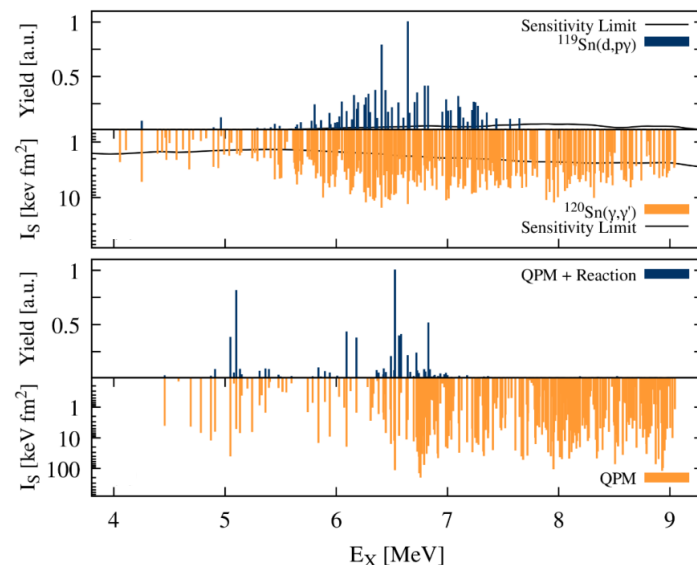


1ph TRD show characteristic behavior

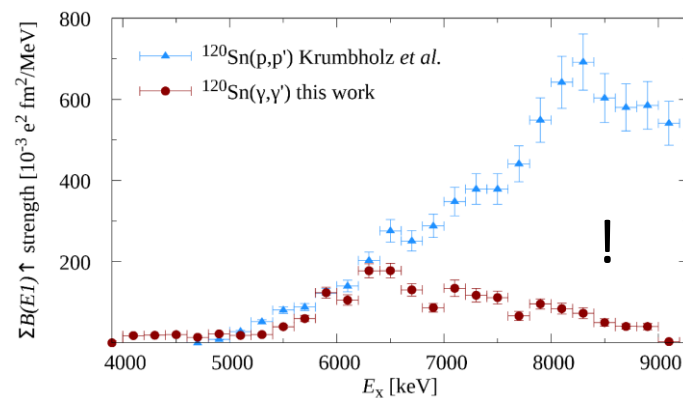
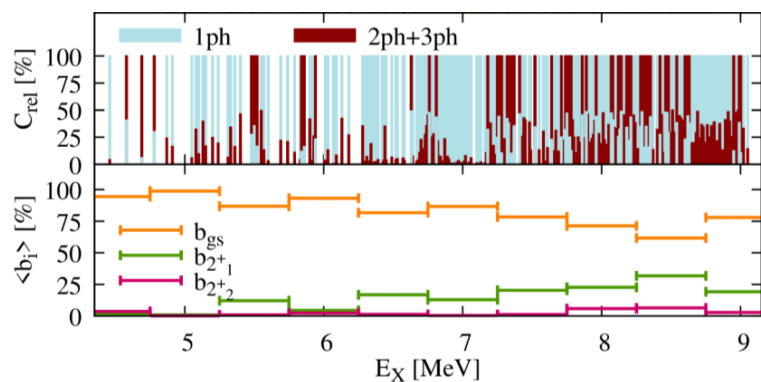
Connection between 1p-1h structure and *neutron skin* oscillation?

# What have we learned so far?

$$\Psi_\nu = \left\{ \begin{aligned} & \sum_i R_i(\nu) Q_{1Mi}^+ \\ & + \sum_{\substack{\lambda_1 i_1 \\ \lambda_2 i_2}} P_{\lambda_2 i_2}^{\lambda_q i_1}(\nu) \left[ Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+ \right]_{1M} \\ & + \sum_{\substack{\lambda_1 i_1 \lambda_2 i_2 \\ \lambda_3 i_3 I}} T_{\lambda_3 i_3}^{\lambda_1 i_1 \lambda_2 i_2 I}(\nu) \left[ \left[ Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+ \right]_{IK} \right. \\ & \quad \left. \times Q_{\lambda_3 \mu_3 i_3}^+ \right]_{1M} \end{aligned} \right\} \Psi_0$$



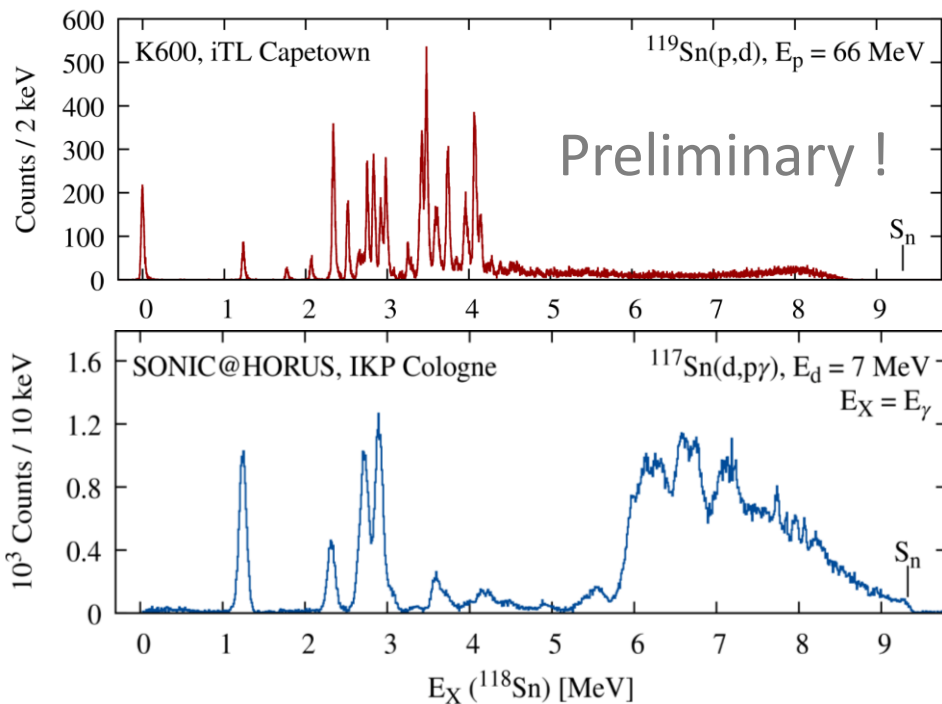
## SONI@HORUS



# What's next?

Further (d,p $\gamma$ ) studies:

- $^{115,117}\text{Sn}(d,p\gamma)$  SONIC@HORUS
- $^{118}\text{Sn}(\gamma,\gamma')$  NRF at  $\gamma$ -ELBE
- $^{61}\text{Ni}(d,p\gamma)$  at ROSPHERE, IFIN-HH

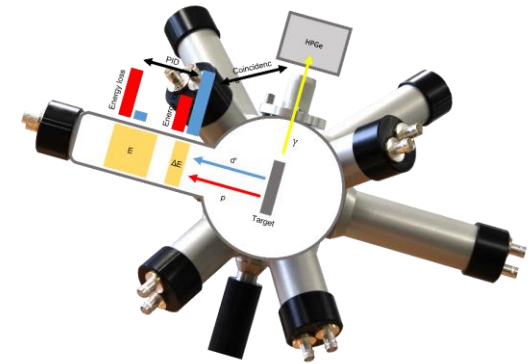


Let's try this:

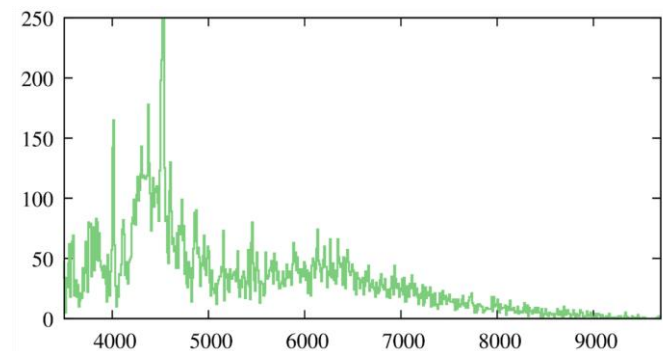
$^{119}\text{Sn}(p,d\gamma)^{118}\text{Sn}$  with  
BaGeL+K600 at iThemba Labs,  
Capetown

# Overview

- A short history of complementary experiments on the LEDR
- Microscopic structure:
  - $^{119}\text{Sn}(d,p\gamma)$  and  $^{120}\text{Sn}(\gamma,\gamma')$
  - Quasiparticle-Phonon-Model
  - Comparing apples to apples
- Isoscalar response:
  - $^{120}\text{Sn}(\alpha,\alpha'\gamma)$  at  $E_\alpha = 130$  MeV



$$\Psi_\nu = \left\{ \begin{array}{l} \sum_i R_i(\nu) Q_{1Mi}^+ \\ + \sum_{\substack{\lambda_1 i_1 \\ \lambda_2 i_2}} P_{\lambda_2 i_2}^{\lambda_1 i_1}(\nu) [Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+]_{1M} \\ + \sum_{\substack{\lambda_1 i_1 \lambda_2 i_2 \\ \lambda_3 i_3}} T_{\lambda_3 i_3}^{\lambda_1 i_1 \lambda_2 i_2}(\nu) [ [Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+]_{IK} \\ \times Q_{\lambda_3 \mu_3 i_3}^+]_{1M} \end{array} \right\} \Psi_0$$



# CAGRA+GR Campaign @ RCNP, Osaka

## GrandRaiden Spectrometer

- High energy resolution under **forward angles** incl.  $0^\circ$

## CAGRA Clover array

- 12 clover type detectors + BGO shields
- 4 large volume  $\text{LaBr}_3$  detectors

$$\begin{aligned} &^{120}\text{Sn}(\alpha, \alpha'\gamma) \\ E_\alpha &= 130 \text{ MeV} \\ \theta_\alpha &= 4.5^\circ \end{aligned}$$

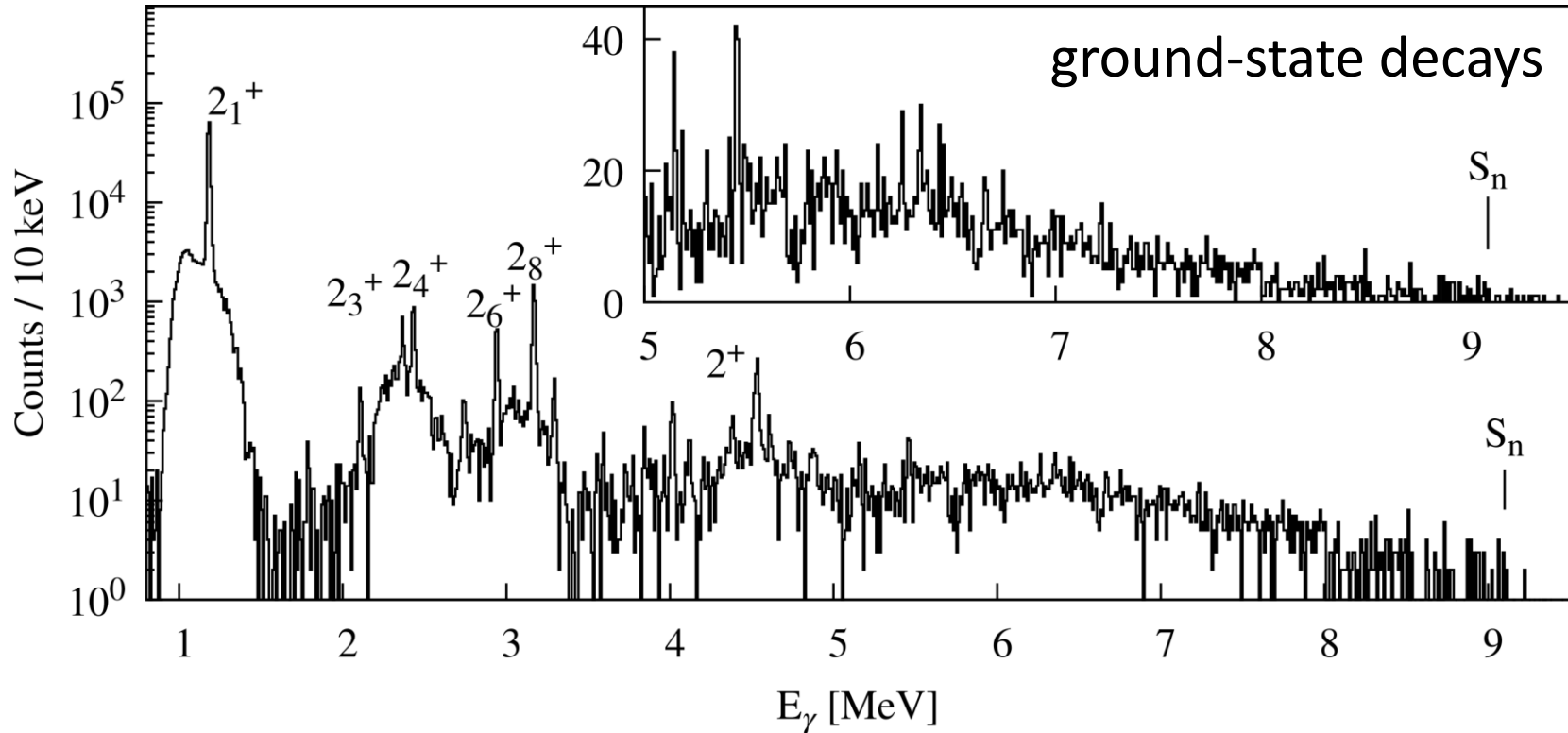
Over **1100 hours** of beam time!





# $^{120}\text{Sn}(\alpha, \alpha' \gamma) - \text{Ground-State Decay Spectrum}$

$^{120}\text{Sn}(\alpha, \alpha' \gamma)$  at  $E_\alpha = 130 \text{ MeV}$ ,  $\theta_\alpha = 4.5^\circ$



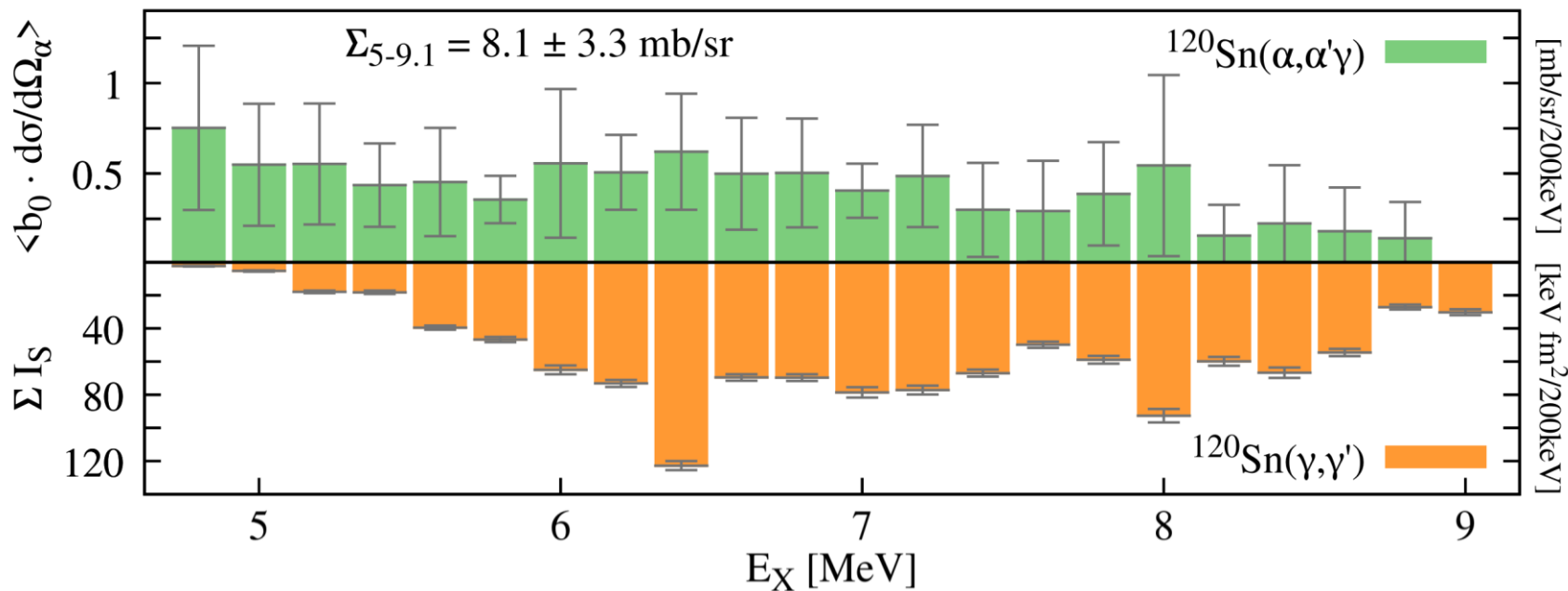
Low statistics above 5 MeV, but above background



Isoscalar response evident!

# $^{120}\text{Sn}(\alpha, \alpha'\gamma)$ vs $^{120}\text{Sn}(\gamma, \gamma')$

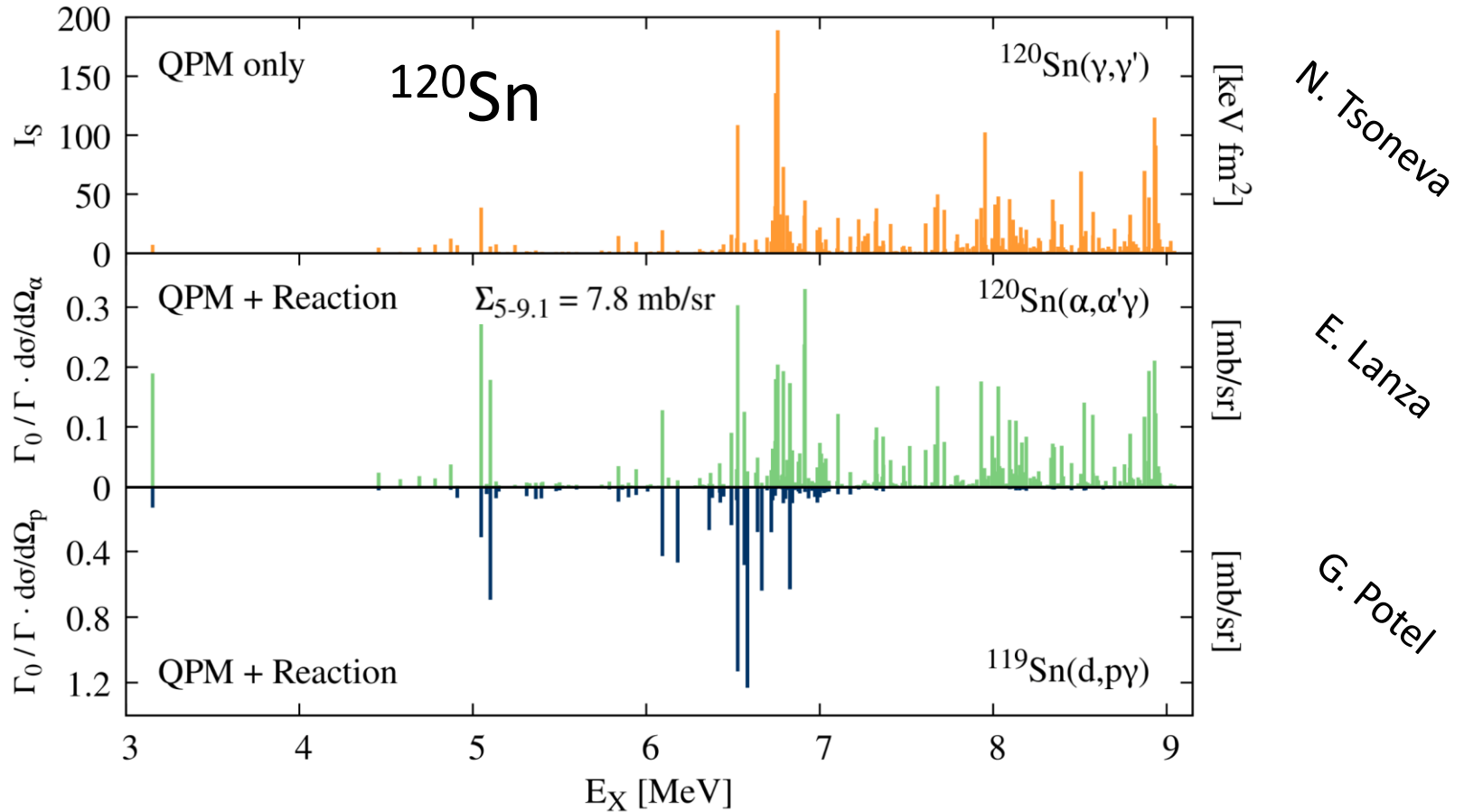
Integrated cross sections for excitation and ground-state decay



Mostly flat isoscalar response, large uncertainties

Summed cross section approx. 5 times lower than  $^{124}\text{Sn}(\alpha, \alpha'\gamma)$ !

# State-to-State QPM+Reaction Predictions

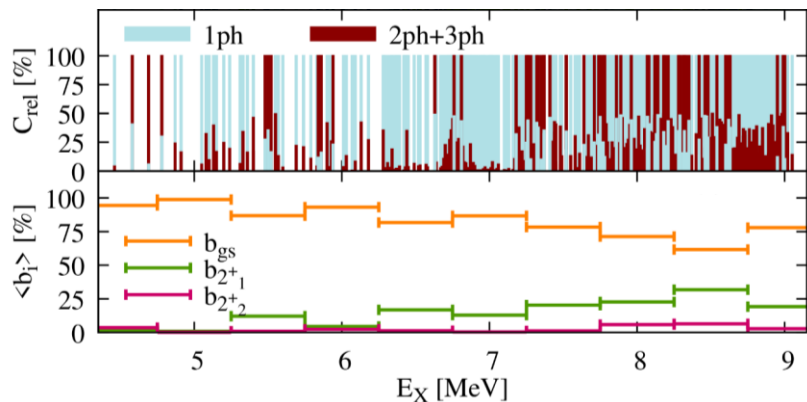


No pronounced difference between  $(\alpha, \alpha' \gamma)$  and  $(\gamma, \gamma')$  suggested  
 Total isoscalar response reproduced from only the 1ph TRDs!

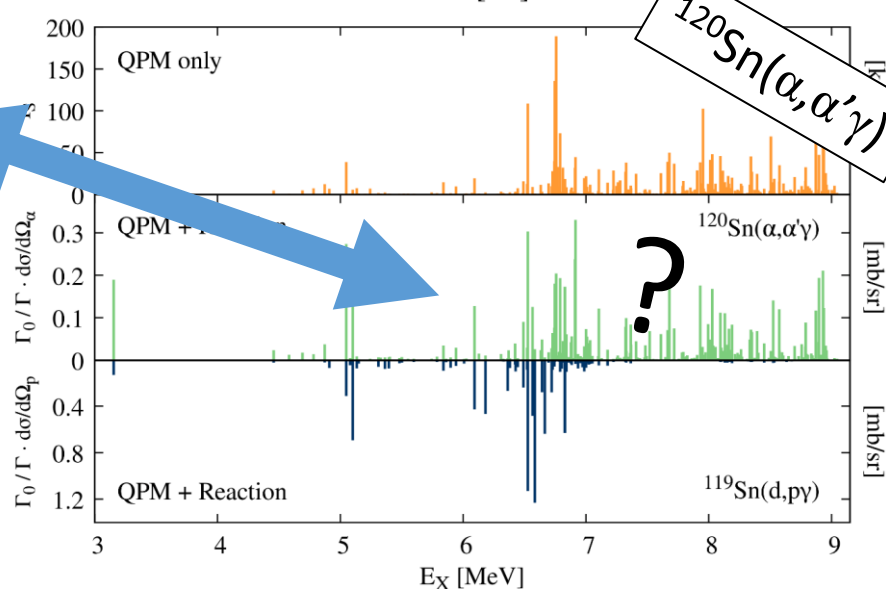
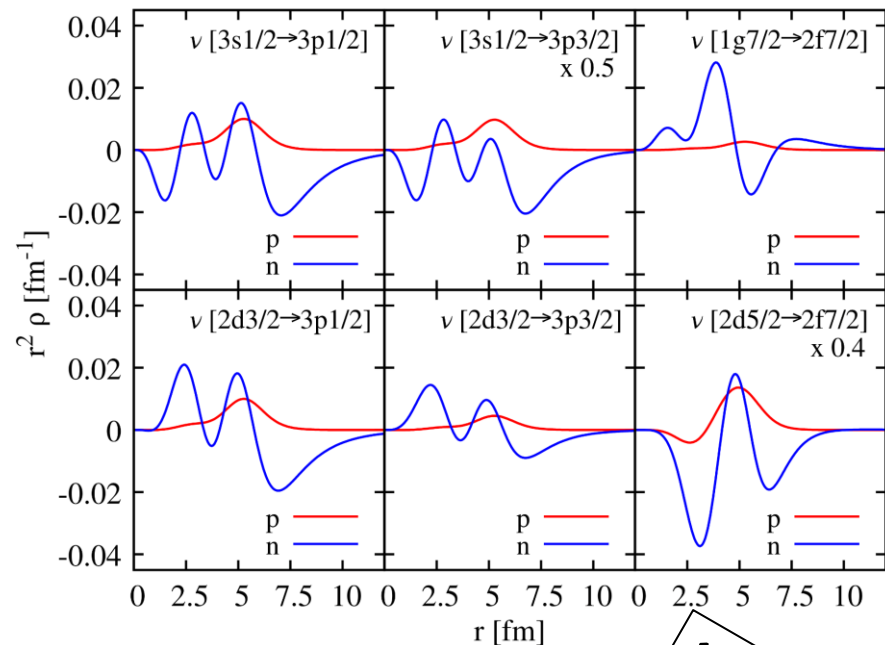
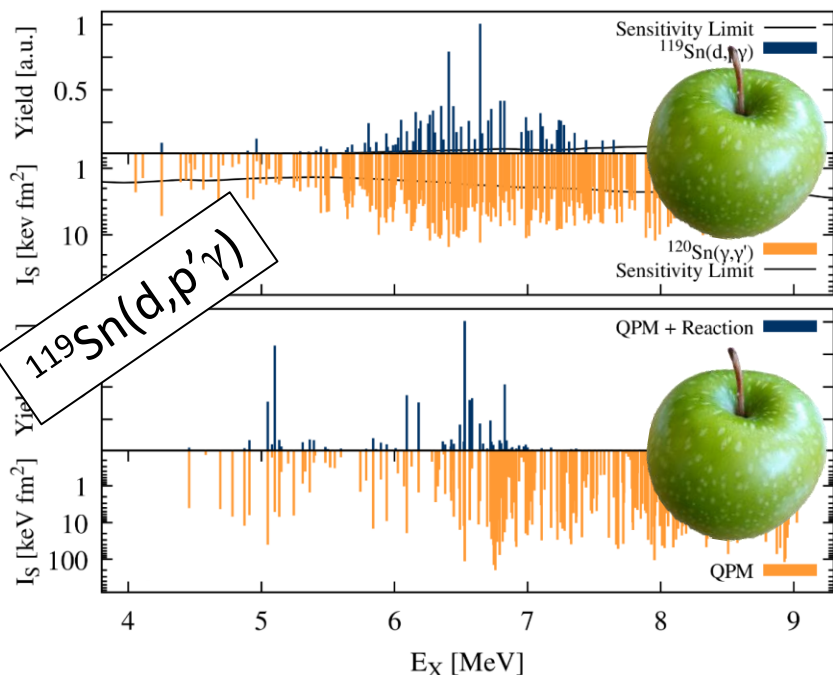


How does the (this) QPM render  $^{124}\text{Sn}(\alpha, \alpha' \gamma)$ ?

# Summary



**SONI@HORUS**



M. Weinert *et al.*, Phys. Rev. Lett. **127** (2021) 242501