

Welcome to **RDMFT2022**

**International workshop on  
Reduced Density Matrix Functional Theory:  
Improving its Foundations and  
Extending its Scope**

Carlos L. Benavides-Riveros, Hardy Gross & Christian Schilling

The one-body reduced density matrix

$$\gamma(\vec{x}, \vec{y}) = \int \Psi(\vec{x}, \vec{x}_2, \dots, \vec{x}_N) \Psi^*(\vec{y}, \vec{x}_2, \dots, \vec{x}_N) d\vec{x}_2 \cdots d\vec{x}_N$$

contains the density  $\rho(\vec{x}) = \gamma(\vec{x}, \vec{x})$

but also coherence and entanglement

$$\gamma(\vec{x}, \vec{y}) = \sum_i n_i \phi_i(\vec{x}) \phi_i^*(\vec{y})$$

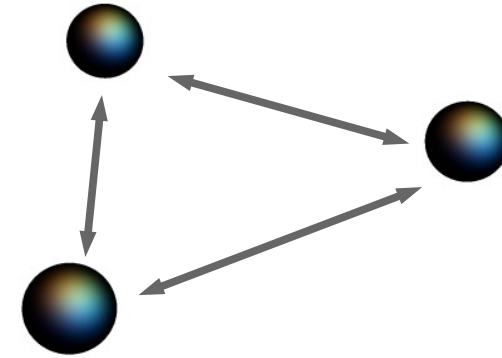
$$\hat{H} = \hat{h} + \hat{W}$$

$$\hat{h} = \sum_i \hat{h}_i$$

1-particle operators

$$\hat{W} = \sum_{i < j} \hat{W}_{ij}$$

2-particle operator



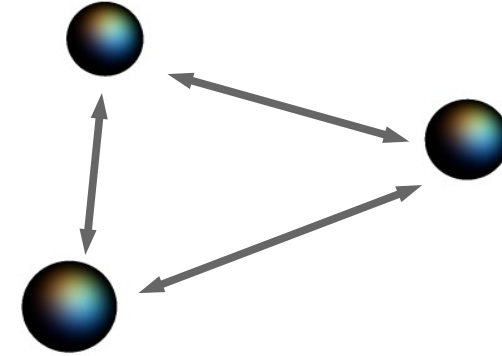
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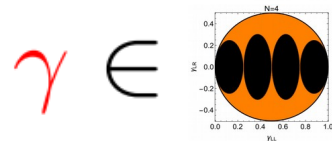
1-particle operators

$$\hat{W} = \sum_{i < j} \hat{W}_{ij}$$

2-particle operator



$$E(\hat{h}) = \min_{\gamma} [\langle \hat{h}, \gamma \rangle + \mathcal{F}(\gamma)]$$



$$\mathcal{F}(\gamma) = \min_{|\Psi\rangle \rightarrow \gamma} \langle \Psi | \hat{W} | \Psi \rangle$$

# RDMFT

fermions (1975)

$T > 0$  (2015)

bosons, ultracold gases (2020)

machine learning (2021)

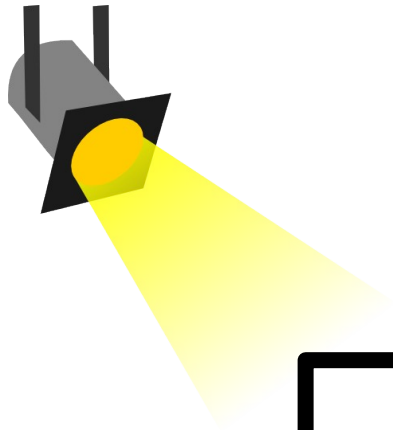
time-dependent RDMFT (2008)

superconductors (2019)

excited states (2021)

relativistic fermionic systems (2022)

# (original) motivation of RDMFT2022



improve the foundations of RDMFT  
extend the scope of RDMFT  
in an intensive & informal meeting



ECT\*  
EUROPEAN CENTRE  
FOR THEORETICAL STUDIES  
IN NUCLEAR PHYSICS AND RELATED AREAS



Hybrid workshop

## Reduced Density-Matrix Functional Theory: Improving its Foundation and Extending its Scope

**Trento (Italy), October 3-14, 2022**

The aim of this international workshop is to discuss and explore new aspects and challenges in Reduced Density Matrix Functional Theory (RDMFT).

This in-person workshop will be complemented by five mini-symposia (hybrid format), open to a broad international audience:

### Symposia

Symposium 1 - October 3, 14:30-18:00 CEST

*Exact results in RDMFT: properties of universal functionals, role of N-representability, etc.*

Symposium 2 - October 5, 9:30-13:00 CEST

*RDMFT & quantum chemistry: Computational and theoretical state-of-the-art, open challenges*

Symposium 3 - October 7, 9:30-13:00 CEST

*Extending the scope of RDMFT: ultracold gases, superconductors, relativistic Quantum Mechanics, etc.*

Symposium 4 - October 10, 9:30-13:00 CEST

*RDMFT for excited states and time-evolution*

Symposium 5 - October 12, 9:30-13:00 CEST

*RDMFT for translational invariant systems*

### Organizers

Carlos Benavides-Riveros (Max Planck Institute for the Physics of Complex Systems, Dresden)

Eberhard Gross (The Hebrew University of Jerusalem)

Christian Schilling (Ludwig-Maximilians-Universität München)

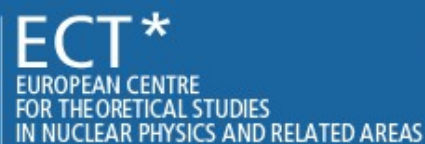


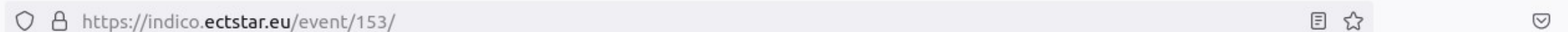
### Director of the ECT\*: Professor Gert Aarts

The ECT\* is part of the Fondazione Bruno Kessler. The Centre is funded by the Autonomous Province of Trento, funding agencies of EU Member and Associated states, and by INFN-TIFPA and has the support of the Department of Physics of the University of Trento. For the organization please contact: Susan Driessen - ECT\* Secretariat - Villa Tambosi - Strada delle Tabarelle 286 | 38123 Villazzano (Trento) - Italy | Tel.: (+39-0461) 314722, E-mail: [driessen@ectstar.eu](mailto:driessen@ectstar.eu) or visit <http://www.ectstar.eu>

[www.ectstar.eu](http://www.ectstar.eu)



# [indico.ectstar.eu/event/153](https://indico.ectstar.eu/event/153)



## Reduced Density-Matrix Functional Theory: Improving its foundation

Oct 3 – 14, 2022  
ECT\*  
Europe/Rome timezone

Overview

Timetable

Registration

Contribution List

Participant List

Videoconference

Speakers

Susan Driessen

 [driessen@ectstar.eu](mailto:driessen@ectstar.eu)

### Please note that in presence attendance is by invitation only

The aim of this international workshop is to discuss and explore new aspects and challenges in Reduced Density Matrix Functional Theory (RDMFT). For this, we invite up to 25 experts in RDMFT to Trento for an intensive and informal meeting.

This in-person workshop during 3-14 October will be complemented by five mini-symposia (hybrid format), open to a broad international audience:

Symposium 1 - October 3, 14:30-18:00 CEST

Exact results in RDMFT: properties of universal functionals, role of N-representability, etc.

Symposium 2 - October 5, 9:30-13:00 CEST

RDMFT for quantum chemistry: Computational and theoretical state-of-the-art and open challenges

Symposium 3 - October 7, 9:30-13:00 CEST

Extending the scope of RDMFT: bosons, ultracold gases, superconductors, relativistic QM, polarons,



 [driessen@ecistar.eu](mailto:driessen@ecistar.eu)

### Session legend

10:00	<b>Registration</b> <i>Half Rustico</i>	10:00 - 10:30
	<b>Introduction</b> <i>Sala Leonardi, ECT*</i>	10:30 - 11:00
11:00	<b>Coffee break</b>	11:00 - 11:30
	<b>Welcome</b> <i>Christian Schilling &amp; Carlos Benavides-Riveros</i>	
12:00		
	<i>Sala Leonardi, ECT*</i>	11:30 - 12:00
13:00	<b>Lunch</b>	
14:00		13:00 - 14:25
	<b>Symposium 1: Exact results in RDMFT</b> <i>Carlos Benavides-Riveros</i>	
	<b>DFT, RDMFT, and the challenge of strong correlations</b> <i>Sala Leonardi, ECT*</i>	Eberhard Gross 14:30 - 15:00
15:00	<b>Density Functional Theory Transformed into a One-electron Reduced Density Matrix Functional Theory for the Capture of Static Correlation</b> <i>David Mazzotti</i>	
	<b>One-body Reduced Density-matrix Functional Theory for the Canonical Ensemble</b> <i>Sala Leonardi, ECT*</i>	Sarina Sutter 15:30 - 16:00
16:00	<b>Coffee break</b>	16:00 - 16:30
	<b>Convex N-Representability</b> <i>Sala Leonardi, ECT*</i>	Federico Castillo 16:30 - 17:00
17:00	<b>Relating the pure and ensemble density matrix functional</b> <i>Sala Leonardi, ECT*</i>	Christian Schilling 17:00 - 17:30
	<b>Implications of pinned occupation numbers for natural orbital expansions</b> <i>Sala Leonardi, ECT*</i>	Tomasz Maciazek 17:30 - 18:00
18:00		

# 5 Symposia

- |  |       |
|--|-------|
| <b>Symposium 1:</b> exact results in RDMFT                   | (Mon) |
| <b>Symposium 2:</b> RDMFT for quantum chemistry              | (Wed) |
| <b>Symposium 3:</b> bosons, ultracold gases, superconductors | (Fri) |
| <b>Symposium 4:</b> conceptual aspects of RDMFT              | (Mon) |
| <b>Symposium 5:</b> excited states, time evolution, and more | (Wed) |

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**Symposium 2:** RDMFT for quantum chemistry (Wed)

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20min + 10min Q&A (mixed audience!)

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20min + 10min Q&A (mixed audience!) **open challenges and ideas**

## During the next 2 weeks

**11:00 - 11:30:** coffee break

**13:00 - 14:30:** lunch

**16:00 - 16:30:** coffee break

**Wednesdays nights:** dinner (Ristorante Ca dei Gobj and tba)

questions & technical difficulties ?

➡ talk to Susan,

Carlos, Hardy & Christian

Enjoy

**RDMFT2022!**