

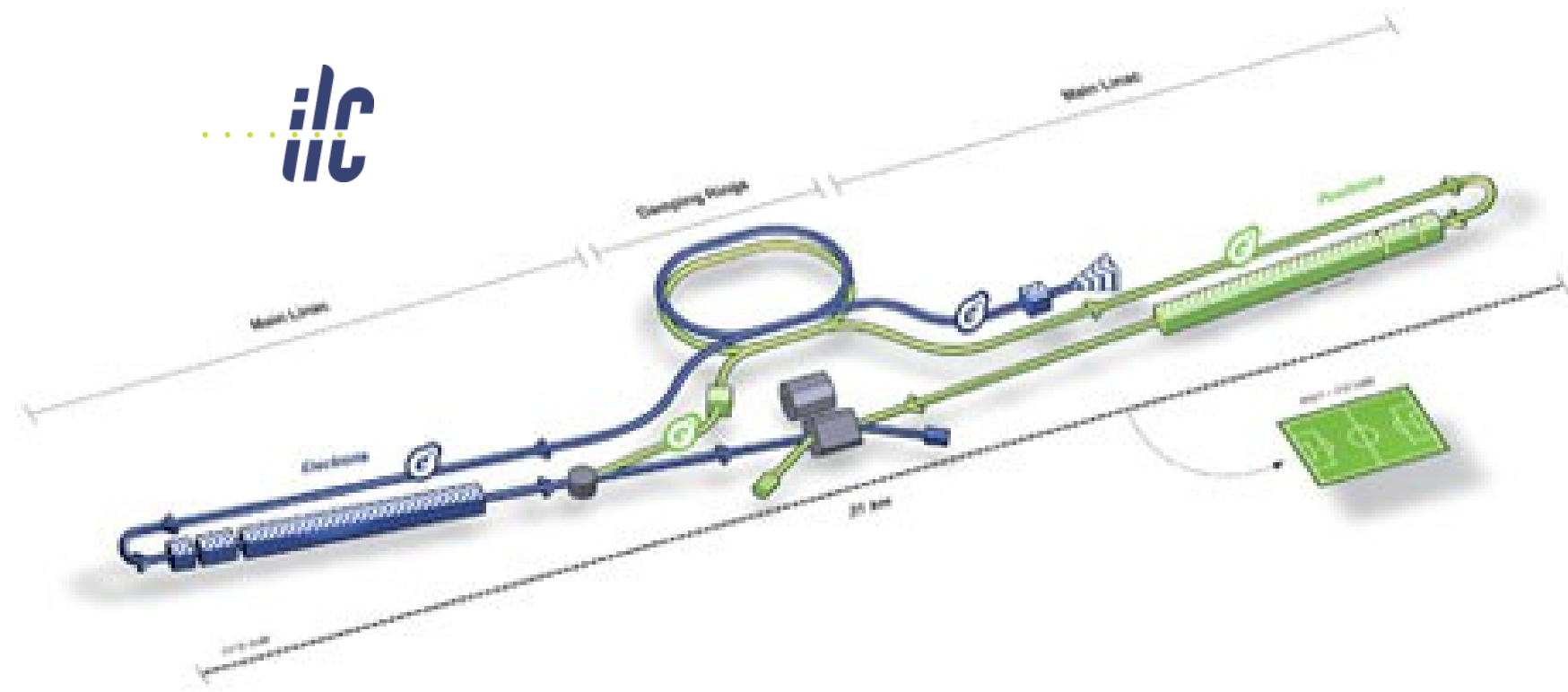
# Top and Heavy Quark Studies at Future High-Energy Electron-Positron Colliders

Roman Pöschl

Based on the results of a number of distinguished colleagues  
A plethora of results have been produced for the Snowmass Community Study



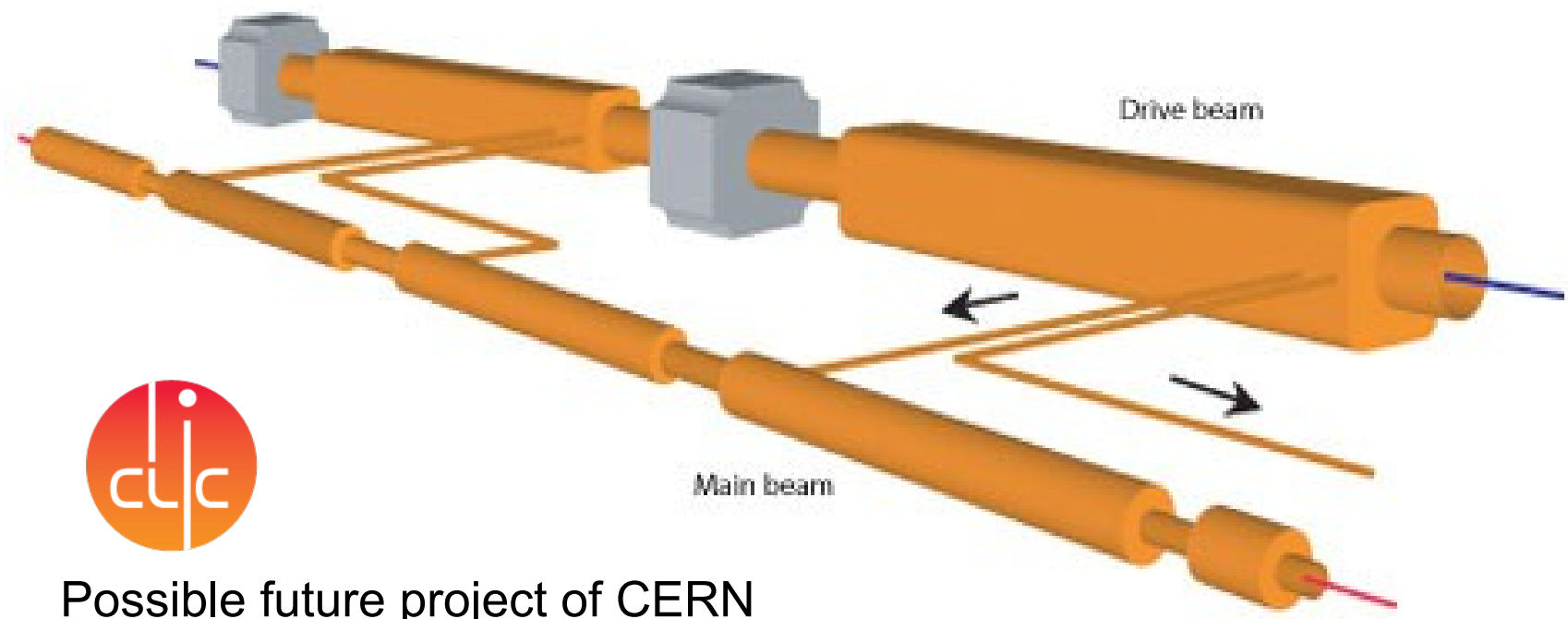
LFC22: STRONG INTERACTIONS FROM QCD TO NEW  
STRONG DYNAMICS AT LHC AND FUTURE COLLIDERS  
ECT\*, Trento, August/September 2022



**Energy: 0.1 - 1 TeV**  
**Electron (and positron) polarisation**  
**TDR in 2013**  
**+ DBD for detectors**  
 Footprint 31 km

Initial Energy 250 GeV – Footprint ~20km

Under discussion in Japanese Government and international community



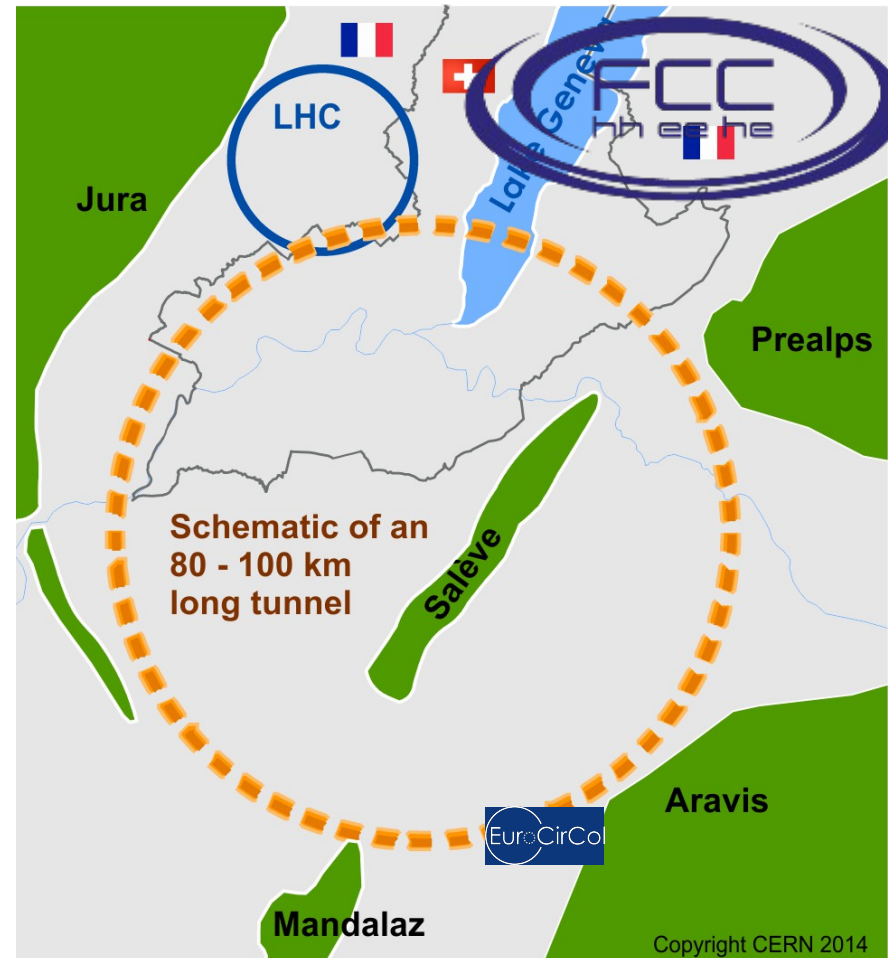
Possible future project of CERN

**Energy: 0.4 - 3 TeV**

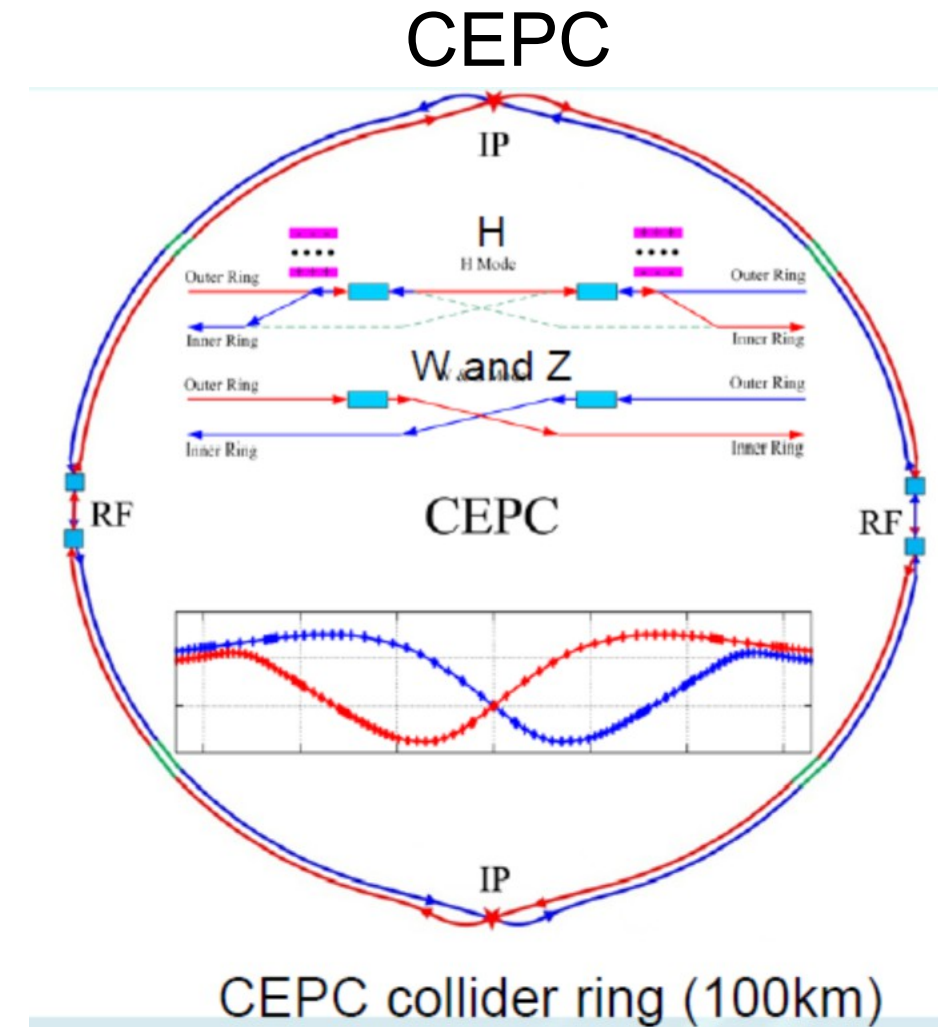
**CDR in 2012**  
**Update 2016**

Footprint 48km

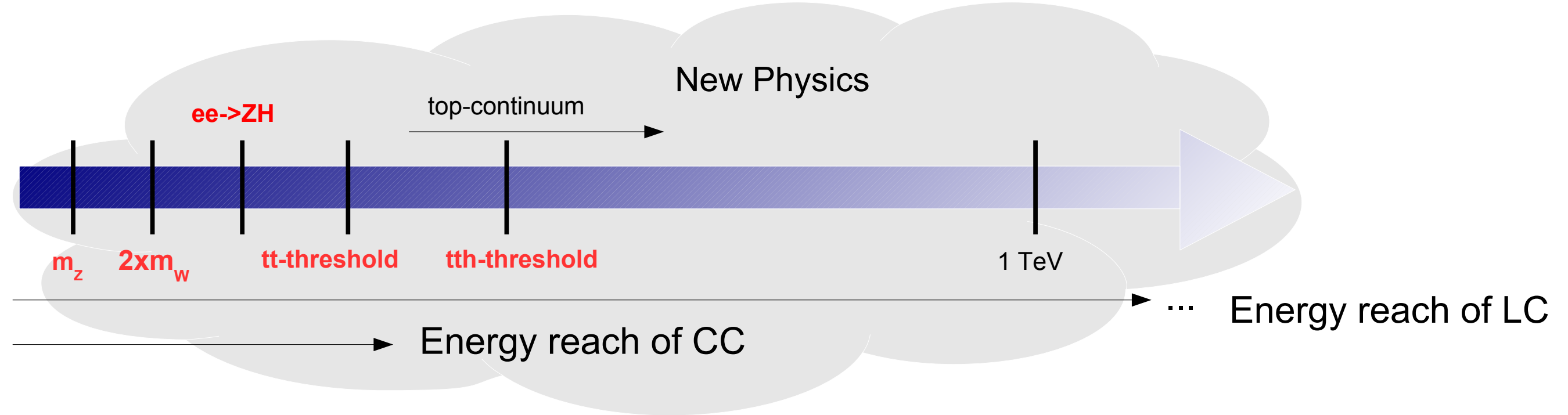
Initial Energy 380 GeV



~100 km storage rings  
 90 – 350 GeV cms energy  
 No long. beam polarisation  
 CDR completed January 2019  
<http://fcc-cdr.web.cern.ch>  
 Feasibility study 2021 - 2025



~100 km storage rings  
 Coupled to hadron collider proposal  
 90 – 240 GeV cms energy  
 No long. beam polarisation  
 CDR completed September 2018  
 Arxiv:1809.00285



All Standard Model particles within reach of planned  $e^+e^-$  colliders

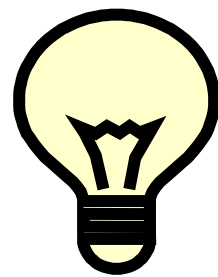
High precision tests of Standard Model over wide range to detect onset of New Physics

Machine settings can be “tailored” for specific processes

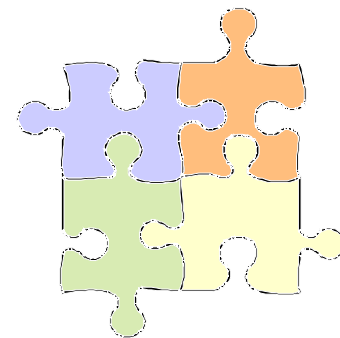
- Centre-of-Mass energy
- Beam polarisation (straightforward at linear colliders)

$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

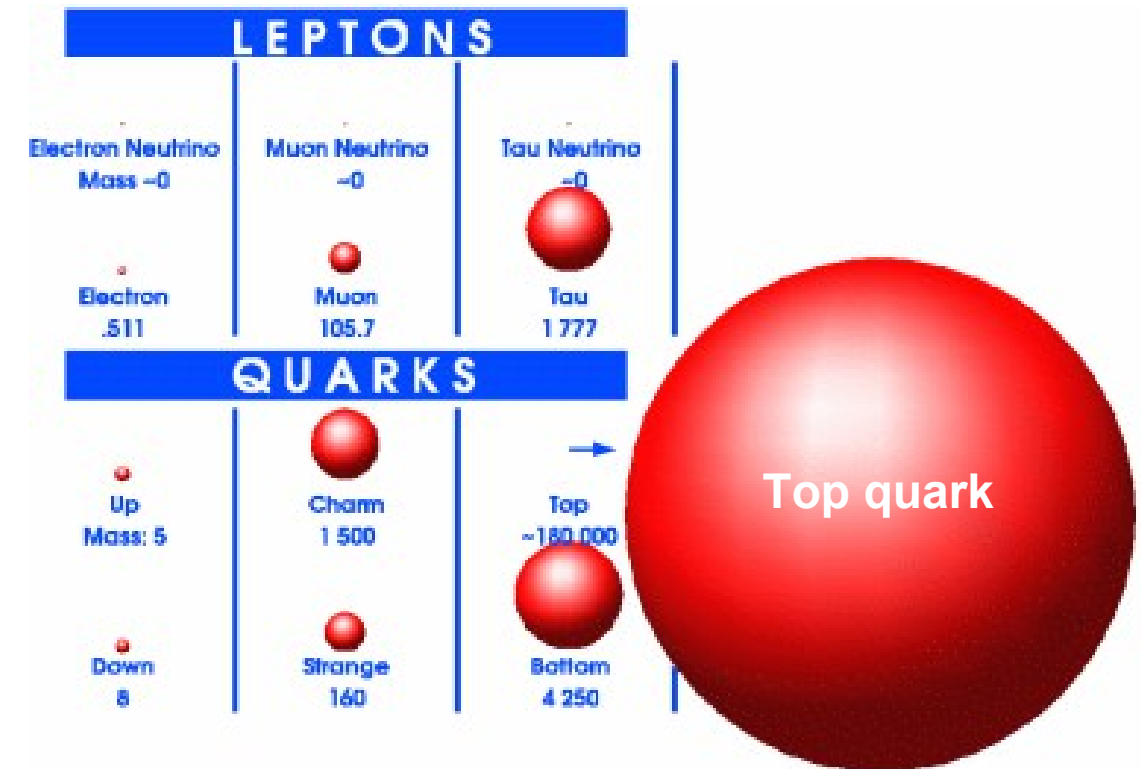
**Background free** searches for BSM through beam polarisation



Elementary Scalar?



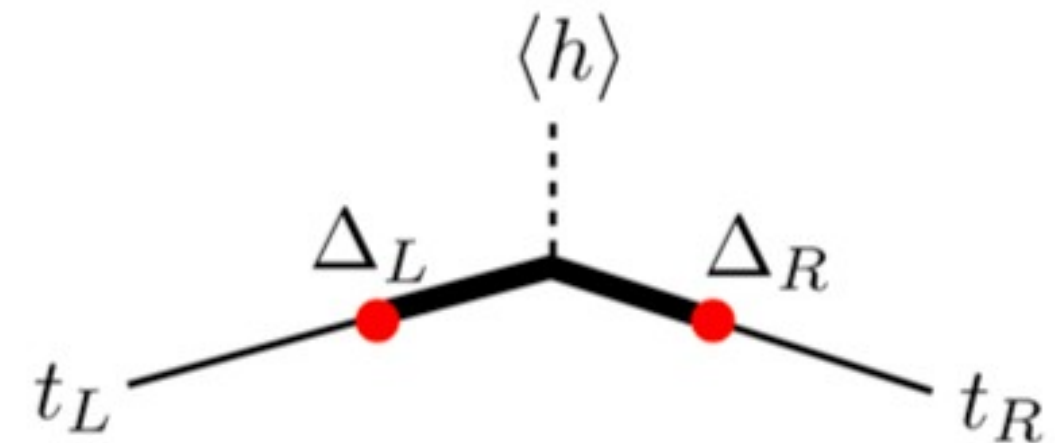
Composite object?



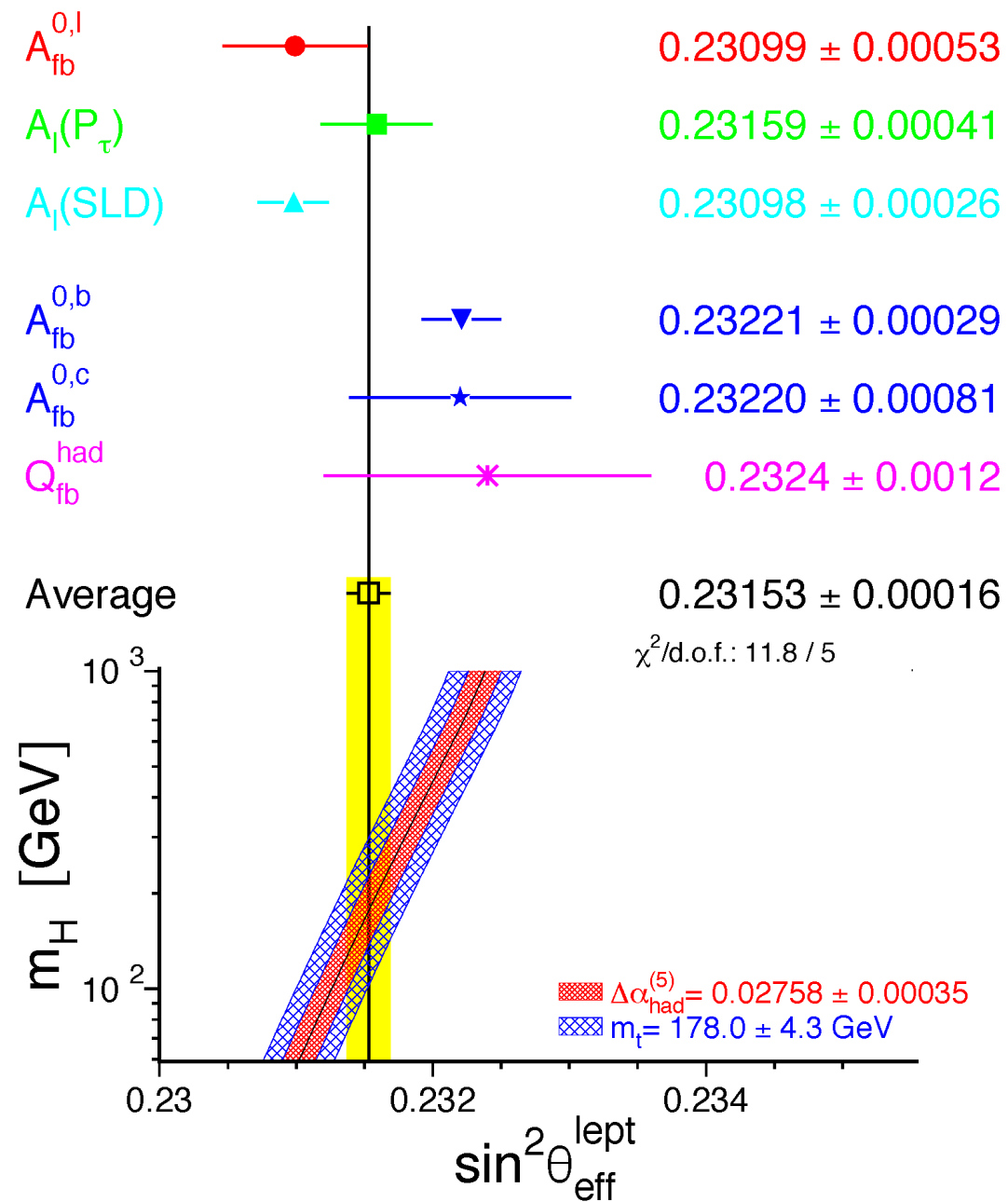
- Higgs and top quark are intimately coupled!  
Top Yukawa coupling  $O(1)$ !  
=> Top mass important SM Parameter

- New physics by compositeness?  
Higgs and top composite objects?

- **e+e- collider perfectly suited to decipher both particles**



Courtesy of S. Rychkov



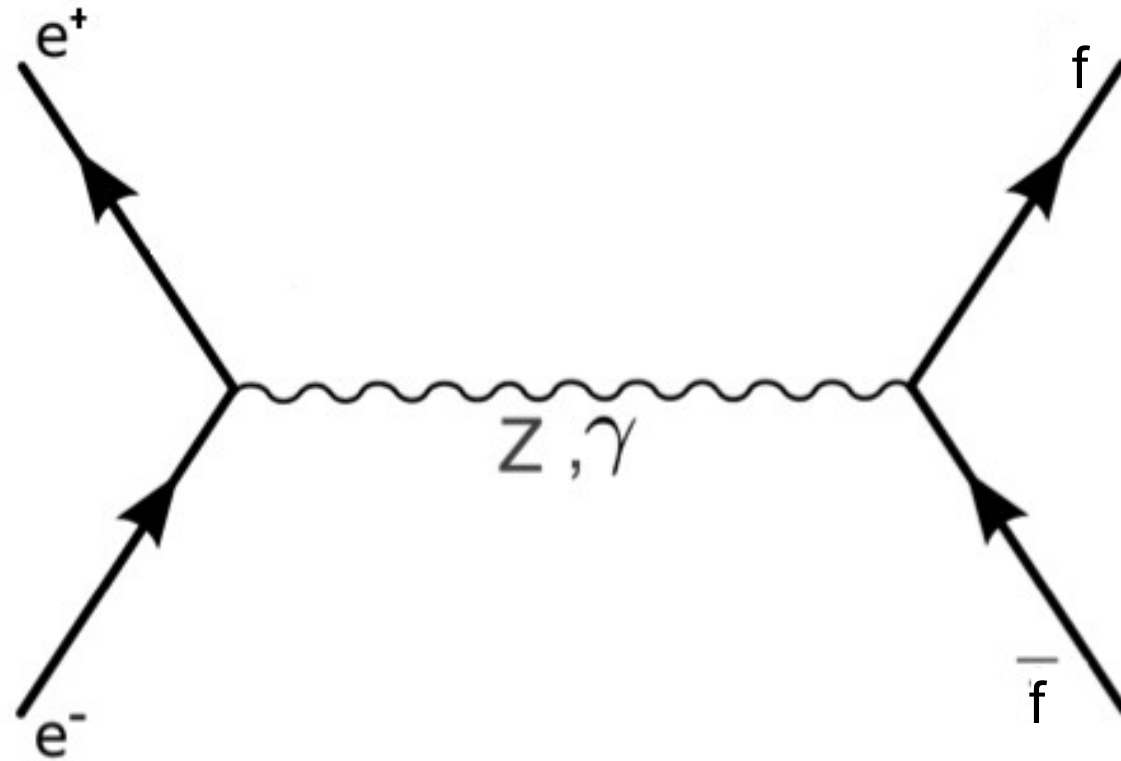
Most precise single Individual determination of  $\sin^2 \theta_{\text{eff}}^{\ell}$  from SLC

- Left-right asymmetry of leptons

- Most precise measurement of  $\sin^2 \theta_{\text{eff}}^{\ell}$  from forward backward asymmetry  $A_{FB}^b$  in  $ee \rightarrow bb$  at LEP

:

- Most precise determinations of  $\sin^2 \theta_{\text{eff}}^{\ell}$  differ significantly
  - Requires verification
  - **Heavy quark effect, effect on all quarks/fermions, no effect at all?**



Differential cross sections for (relativistic) di-fermion production\*:

$$\frac{d\sigma}{d\cos\theta}(e_L^- e_R^+ \rightarrow f \bar{f}) = \Sigma_{LL}(1 + \cos\theta)^2 + \Sigma_{LR}(1 - \cos\theta)^2$$

$$\frac{d\sigma}{d\cos\theta}(e_R^- e_L^+ \rightarrow f \bar{f}) = \Sigma_{RL}(1 + \cos\theta)^2 + \Sigma_{RR}(1 - \cos\theta)^2$$

\*add term  $\sim \sin^2\theta$  in case of non-relativistic fermions e.g. top close to threshold

$\Sigma_{IJ}$  are helicity amplitudes that contain couplings  $g_L, g_R$  (or  $F_V, F_A$ )

$\Sigma_{IJ} \neq \Sigma_{I'J'} \Rightarrow$  (characteristic) asymmetries for each fermion

Forward-backward in angle, general left-right in cross section

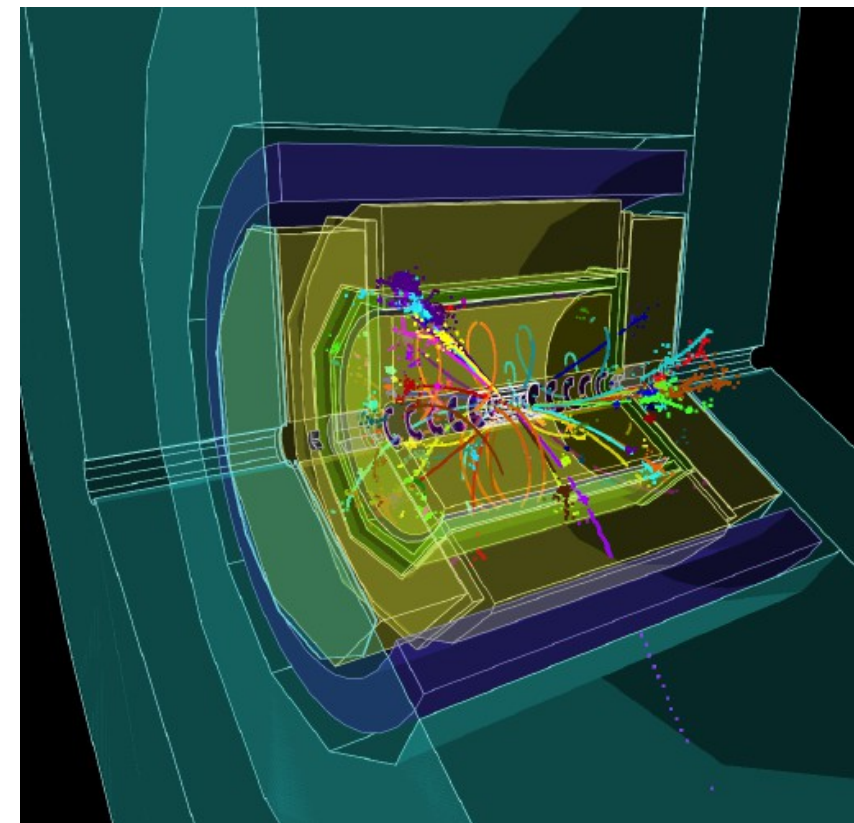
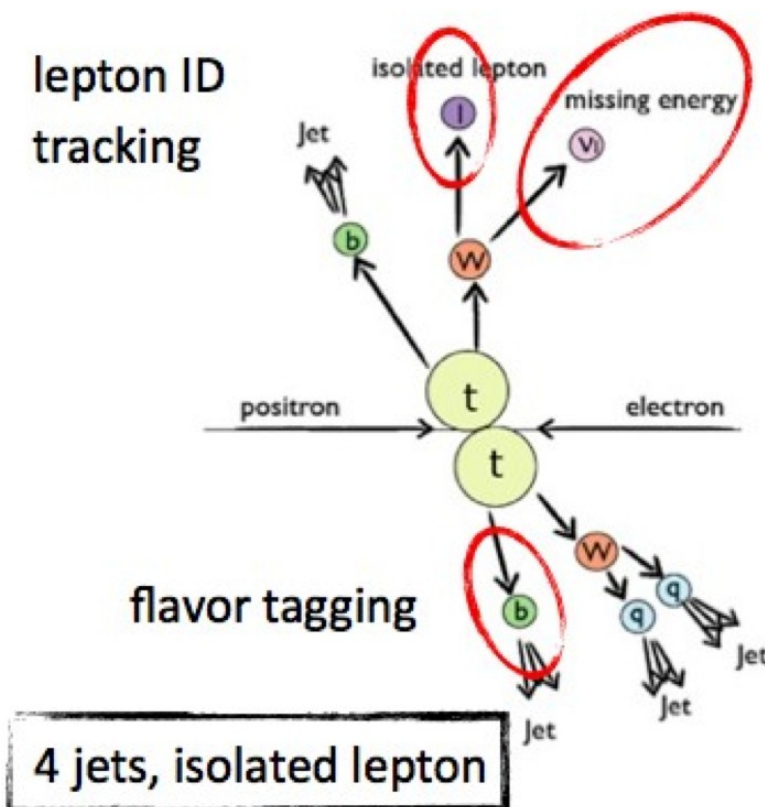
**All four helicity amplitudes for all fermions only available with polarised beams**

**Here we focus on tt, bb and cc pair production**

Three different final states:

- 1) Fully hadronic (46.2%) → 6 jets
- 2) Semi leptonic (43.5%) → 4 jets + 1 charged lepton and a neutrino
- 3) Fully leptonic (10.3%) → 2 jets + 4 leptons

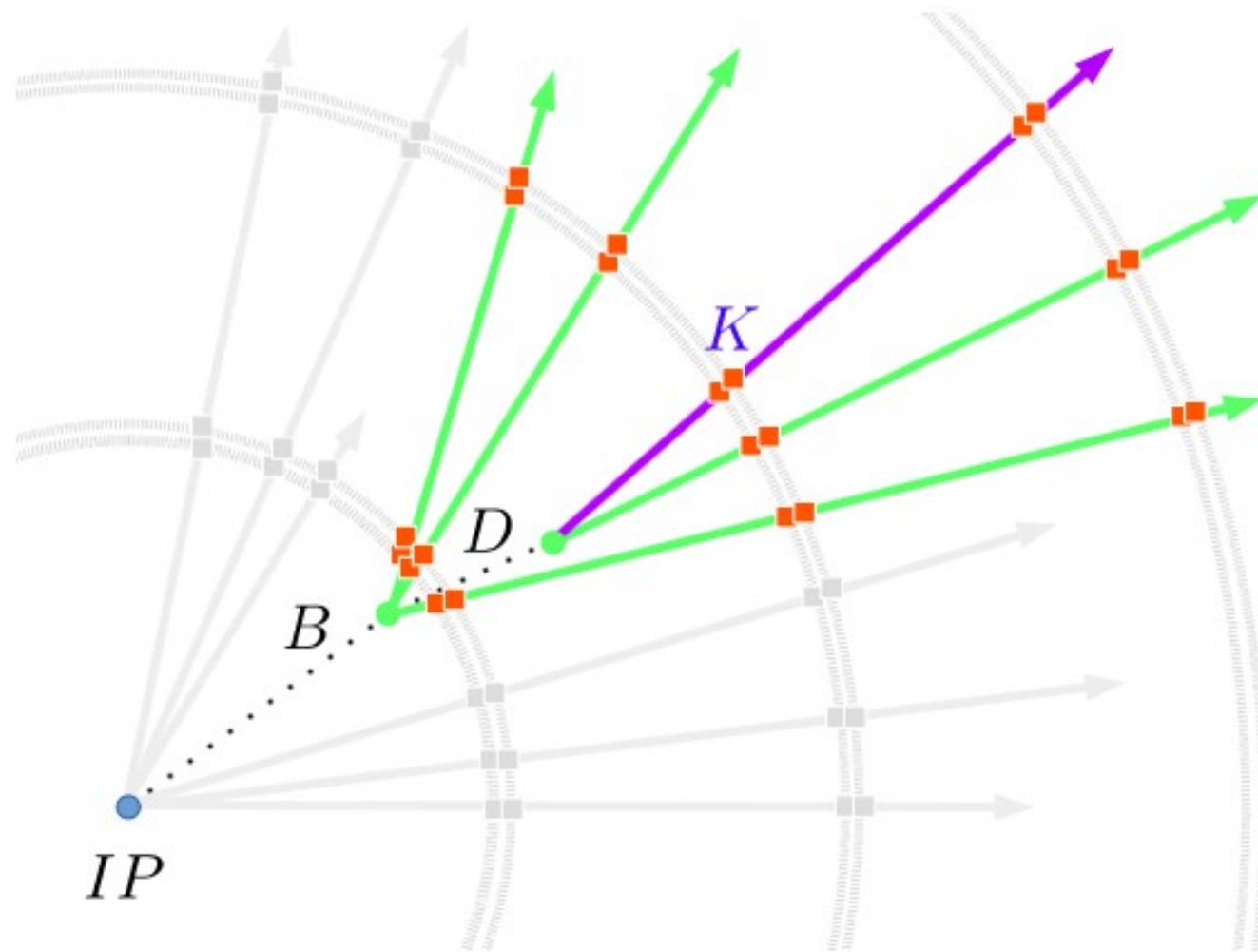
$$t\bar{t} \rightarrow (bW)(bW) \rightarrow (bqq')(bl\nu)$$



Final state reconstruction uses all detector aspects

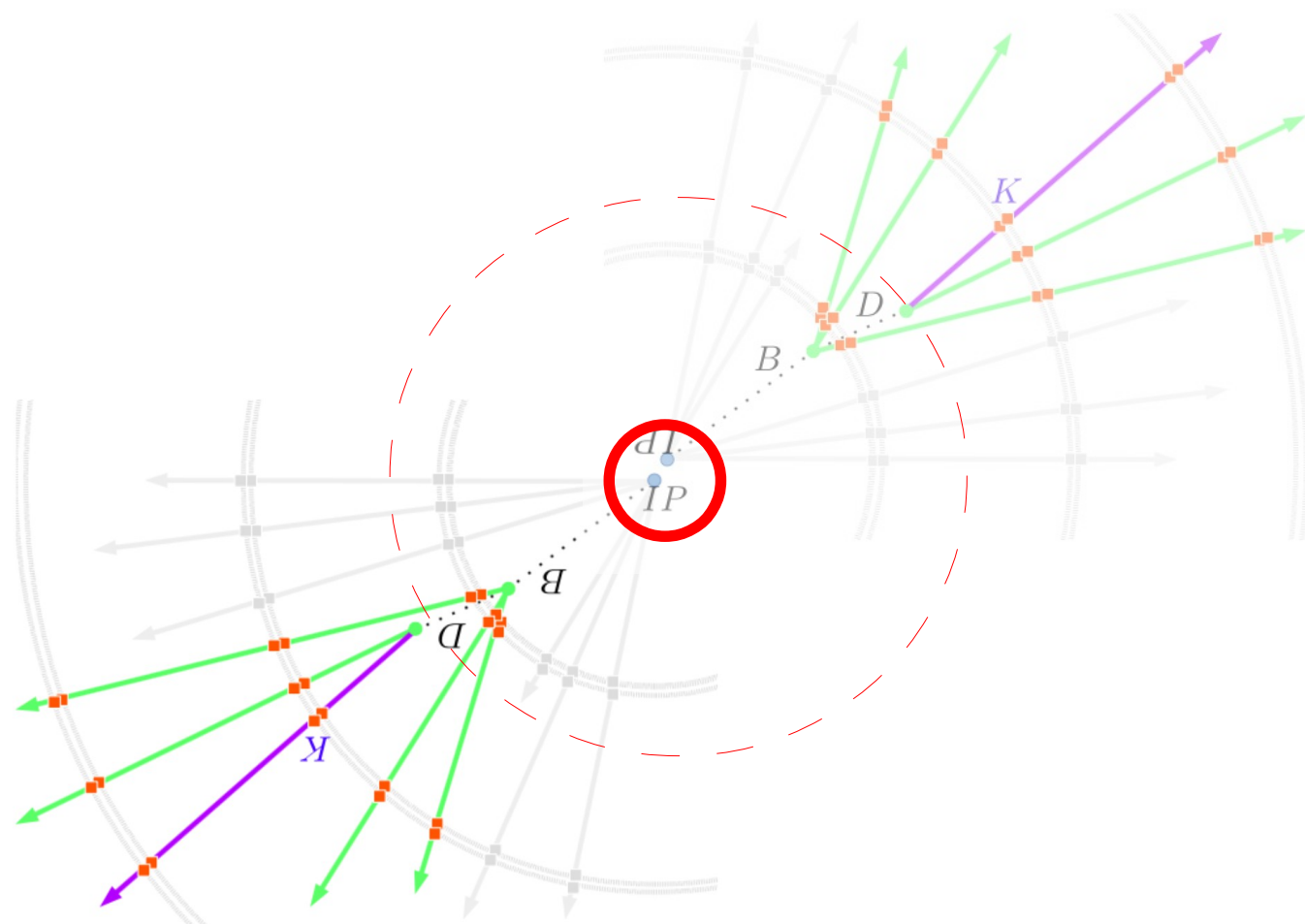
Results shown in the following are based on full simulation of LC Detectors





- Flavor tagging
  - Indispensable for analyses with final state quarks
- Quark charge measurement
  - Important for top quark studies,
  - indispensable for  $ee \rightarrow bb, cc, ss, \dots$
- Control of migrations:
  - Correct measurement of vertex charge
  - Kaon identification by  $dE/dx$  (and more)
- Future detectors can base the entire measurements on double Tagging and vertex charge
  - LEP/SLC had to include single tags and Semi-leptonic events

PhD thesis: S. Bilokin  
A. Irles



Important systematic error is knowledge of tagging efficiency  $\epsilon_q$

Can be derived from data if tagging is independent in two hemispheres, i.e. if

$$C_q = \frac{\epsilon_{double}}{\epsilon_q^2} \approx 1$$

If  $C_q \neq 1 \Rightarrow$  Hemisphere correlations  $\Rightarrow$  systematic error

For example:

LEP (large beam spot):  $C_q - 1 \approx 3\% \Rightarrow \Delta R_b \approx 0.2\%$

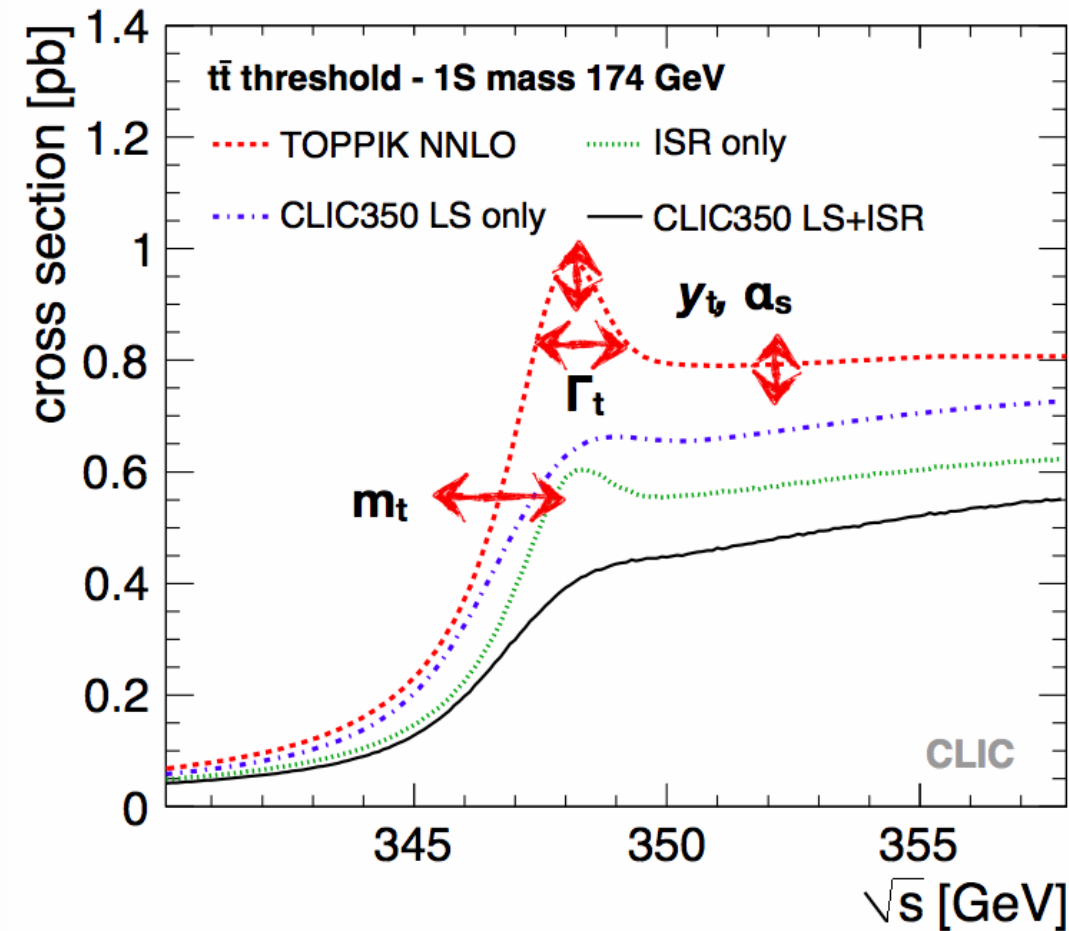
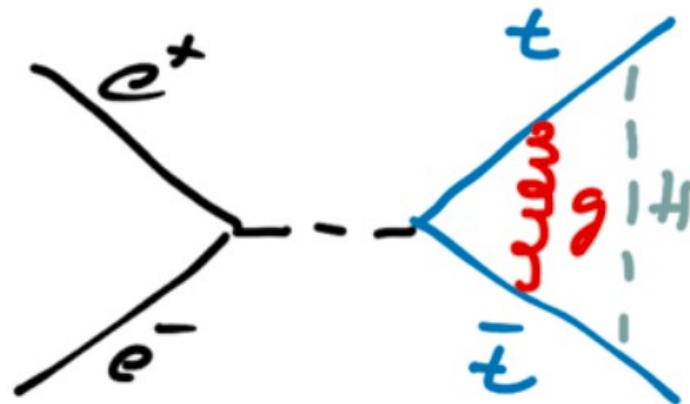
SLC (smaller beam spot):  $C_q - 1 < 1\% \Rightarrow \Delta R_b \approx 0.07\%$

Future (small/tiny beam spot): Expect  $C_q - 1 = 0 \Rightarrow \Delta R_b \approx 0$   
to be verified however

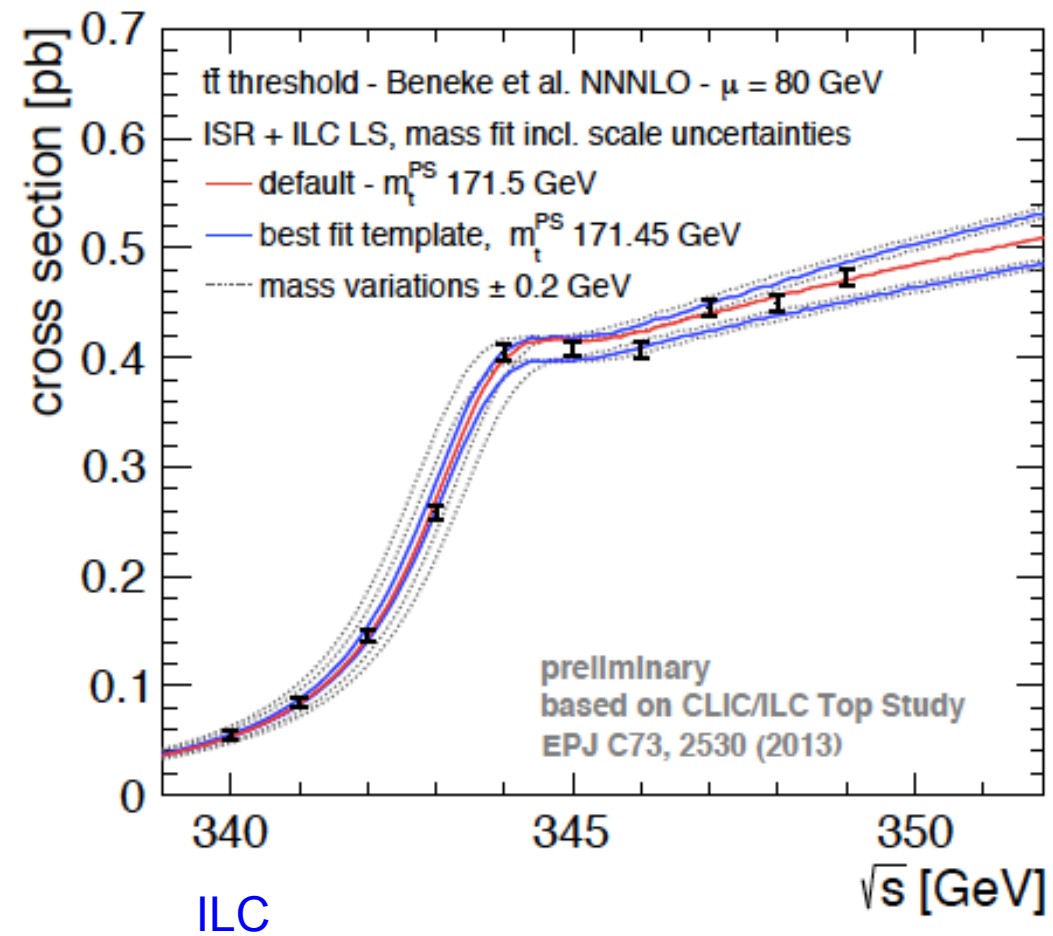
Small size of  $t\bar{t}$  “bound state” at threshold ideal premise for precision physics

Cross section around threshold is affected by several properties of the top quark and by QCD

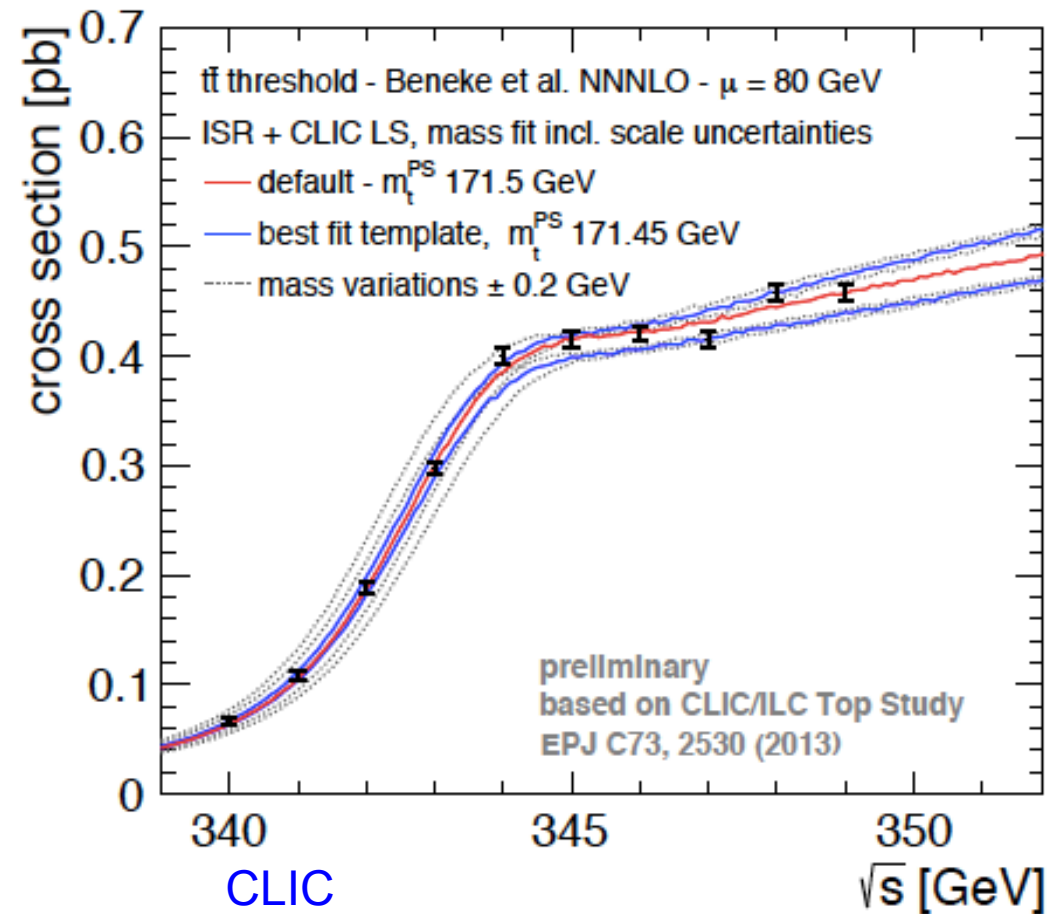
- Top mass, width Yukawa coupling
- Strong coupling constant



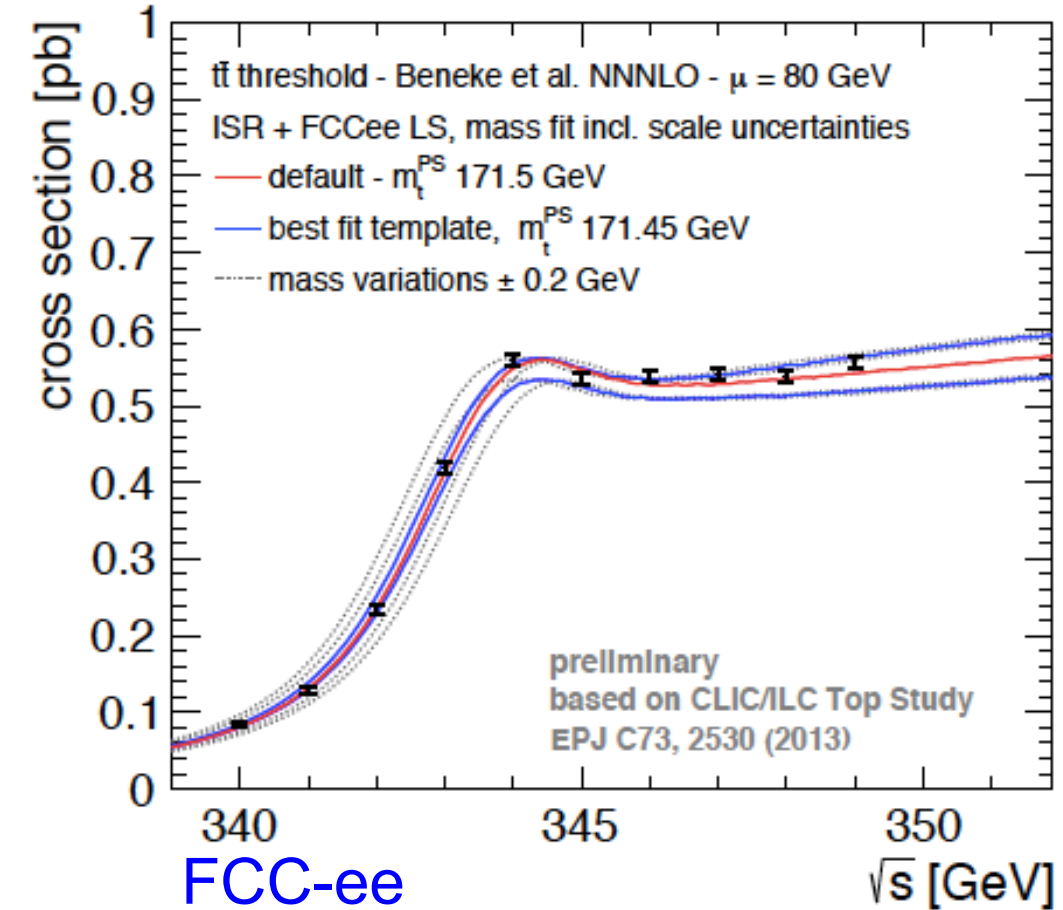
- Effects of some parameters are correlated:
- Dependence on Yukawa coupling rather weak,
- Precise external  $\alpha_s$  helps



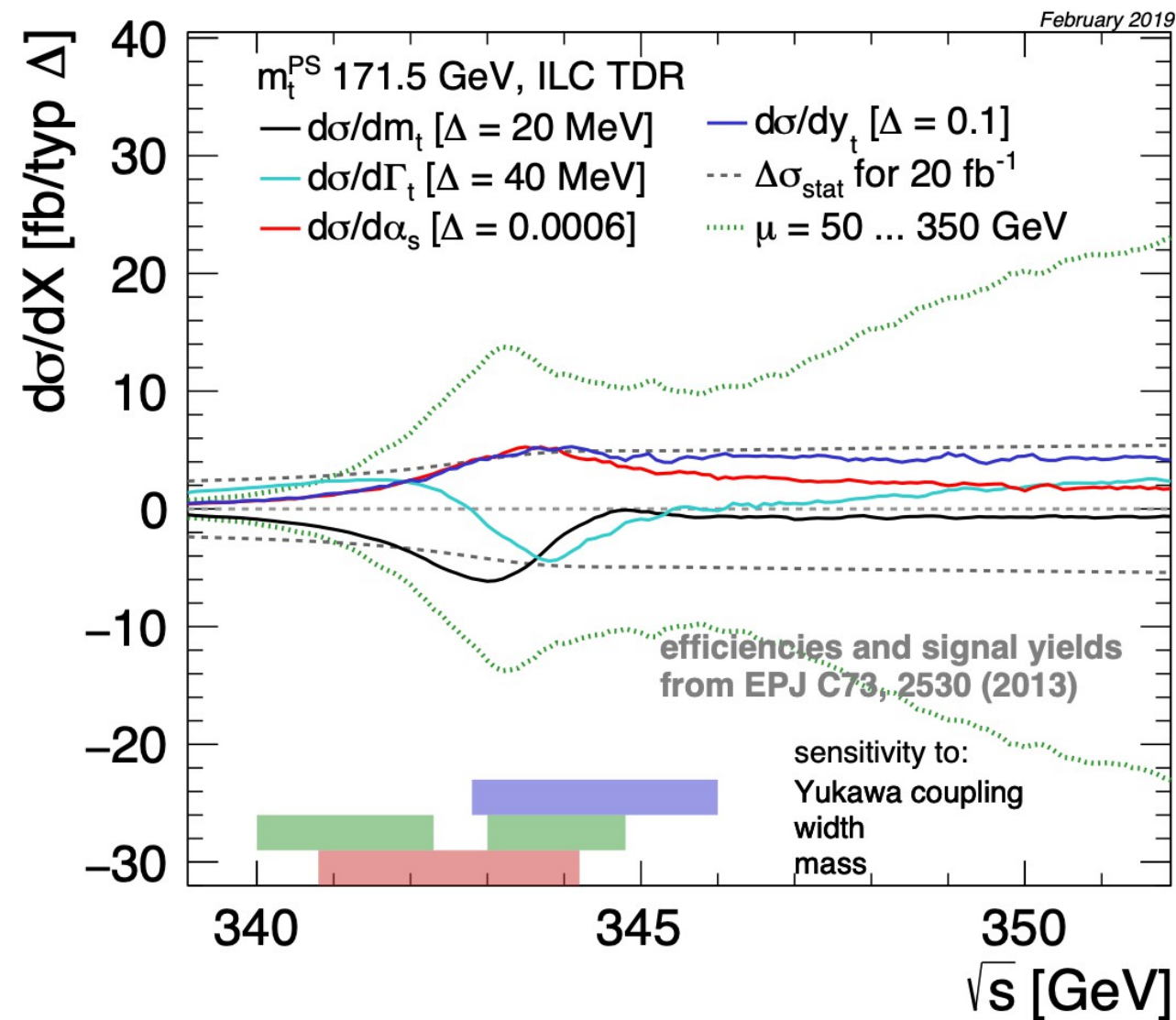
Fit uncertainty:  
 28.5 MeV (18 MeV stat)



Fit uncertainty:  
 31 MeV (21 MeV stat)

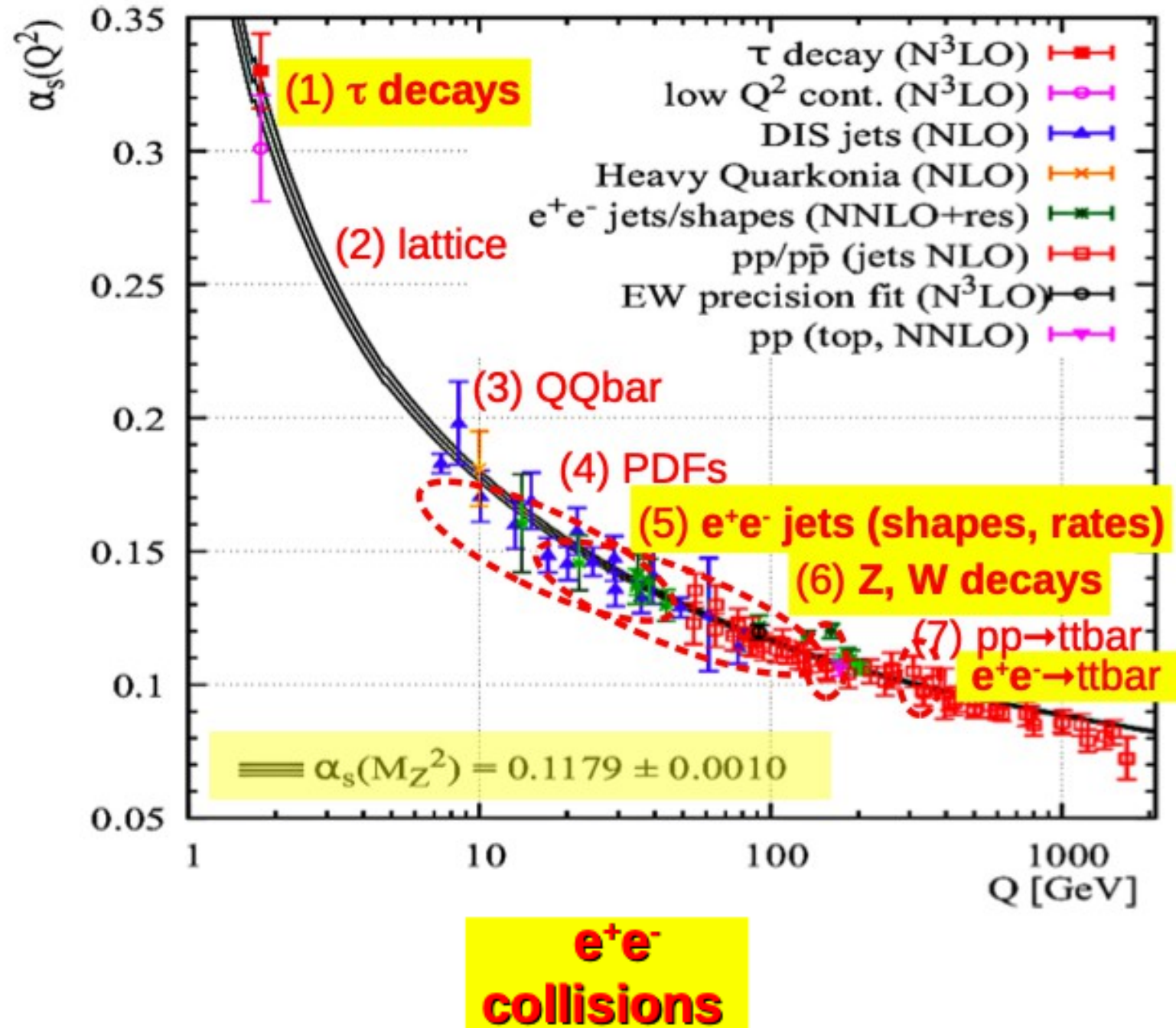


Fit uncertainty:  
 27 MeV (15 MeV stat)



error source	$\Delta m_t^{\text{PS}}$ [MeV]
stat. error ( $200 \text{ fb}^{-1}$ )	13
theory (NNNLO scale variations, PS scheme)	40
parametric ( $\alpha_s$ , current WA)	35
non-resonant contributions (such as single top)	< 40
residual background / selection efficiency	10 – 20
luminosity spectrum uncertainty	< 10
beam energy uncertainty	< 17
combined theory & parametric	30 – 50
combined experimental & backgrounds	25 – 50
total (stat. + syst.)	40 – 75

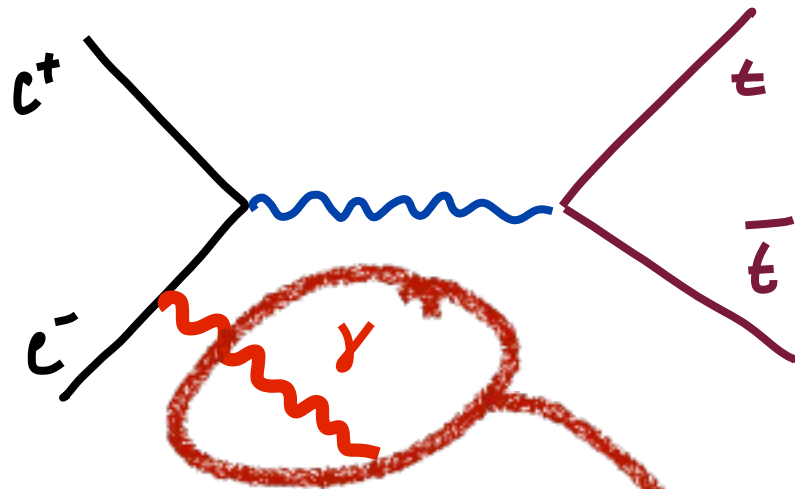
- Numbers for ILC/CLIC, some numbers get better for FCCee
  - e.g. Beam energy uncertainty < 3 [MeV]
- Uncertainty driver  $\alpha_s$ 
  - $\Delta m \sim 2.6 \text{ per } 10^{-4} \text{ in } \alpha_s$



- See talk by Francesco Giuli yesterday
  - [https://indico.ectstar.eu/event/149/contributions/3058/attachments/1919/2513/FCC\\_LFC\\_FGiuli\\_2022.pdf](https://indico.ectstar.eu/event/149/contributions/3058/attachments/1919/2513/FCC_LFC_FGiuli_2022.pdf)
- Best prospects from e<sup>+</sup>e<sup>-</sup> collisions
  - $\Delta\alpha/\alpha \sim 0.1\%$  for FCCee hadronic Z-decays
    - Comparable with QCD Lattice Results
  - Status for ILC  $\Delta\alpha/\alpha \sim 0.6\%$  (arXiv:1512.05194)
    - Worth another look ?!

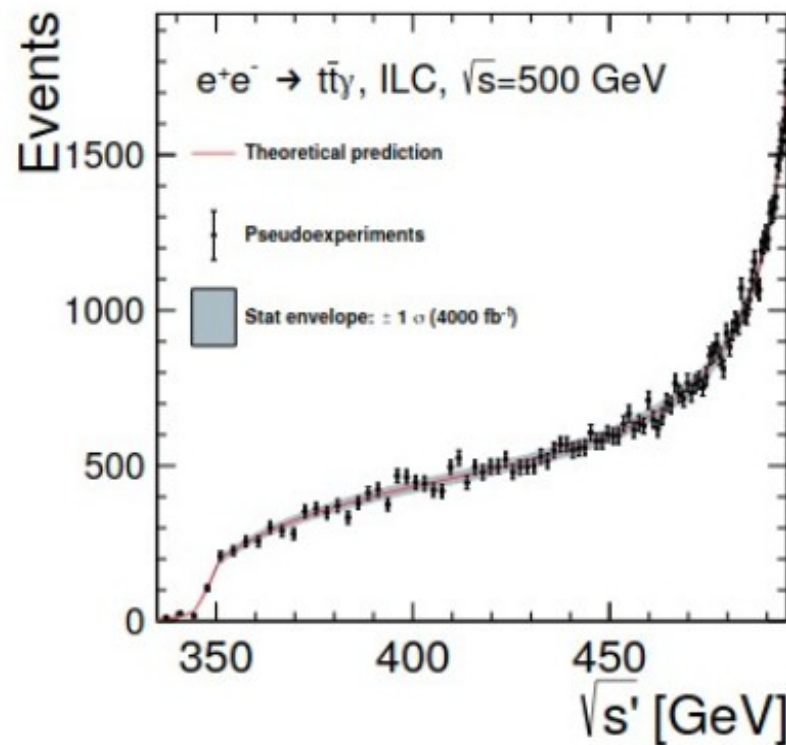
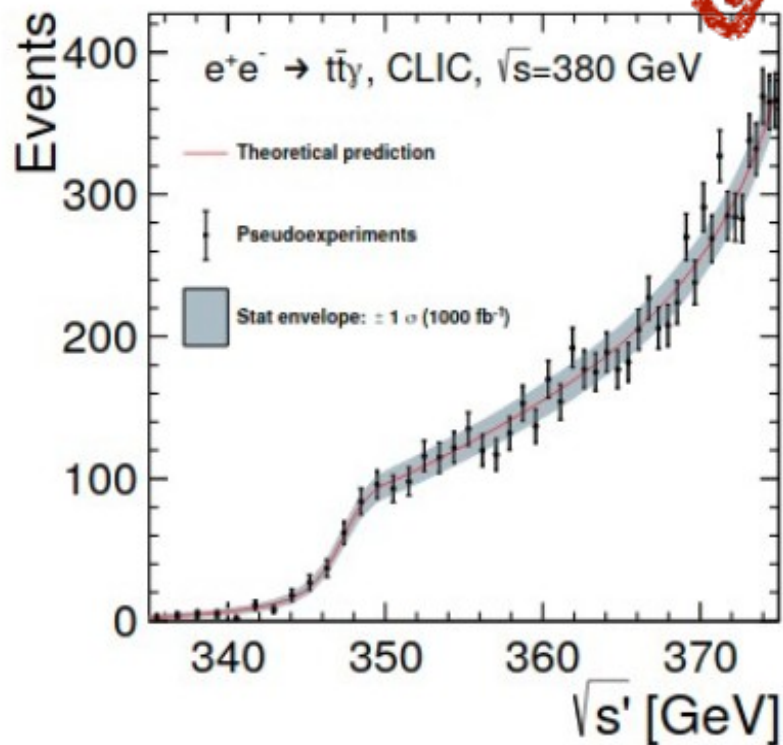
# Running top mass

- A new(er) idea to measure the top mass in a theoretically well-defined scheme in high-energy running above the threshold

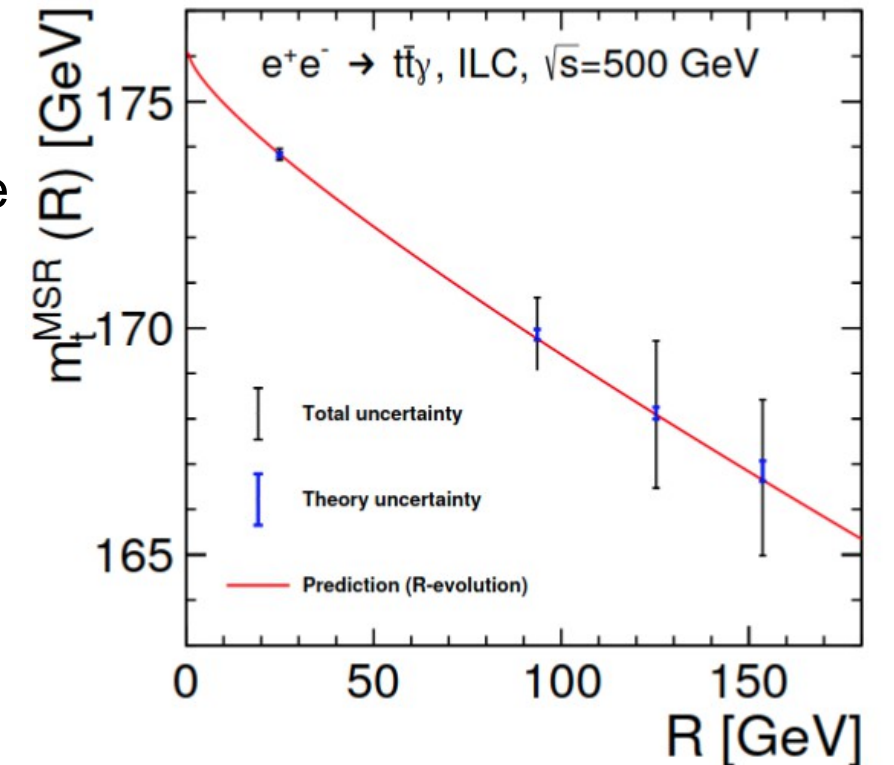


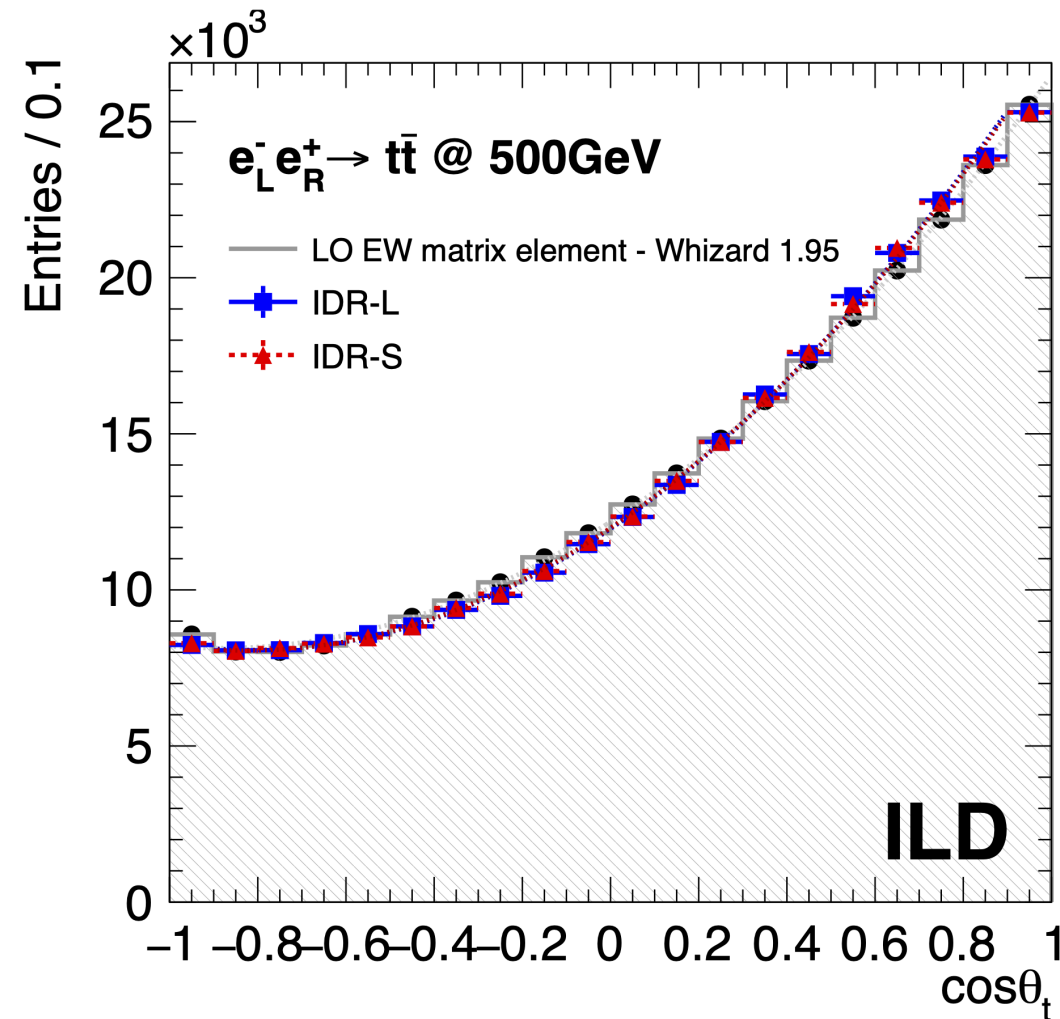
matched NNLO + NNLL calculation, luminosity spectrum folded in explicitly;  
 Extraction of short distance MSR mass

cms energy	CLIC, $\sqrt{s} = 380$ GeV		ILC, $\sqrt{s} = 500$ GeV	
luminosity [ $\text{fb}^{-1}$ ]	500	1000	500	4000
statistical	140 MeV	90 MeV	350 MeV	110 MeV
theory	46 MeV		55 MeV	
lum. spectrum	20 MeV		20 MeV	
photon response	16 MeV		85 MeV	
total	150 MeV	110 MeV	360 MeV	150 MeV

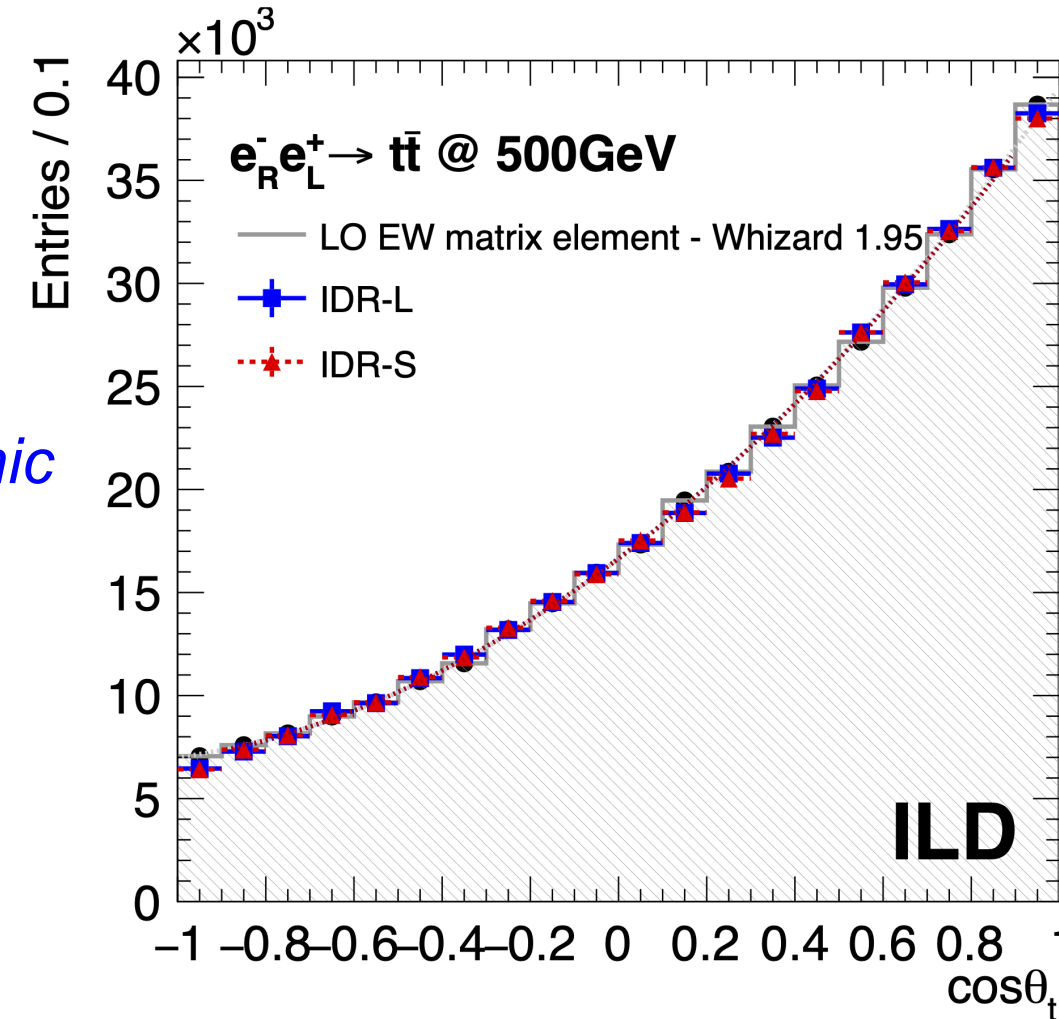


can provide  $5\sigma$  evidence for scale evolution (“running”) of the top quark MSR mass from ILC500 data alone





*Semi-leptonic channel*

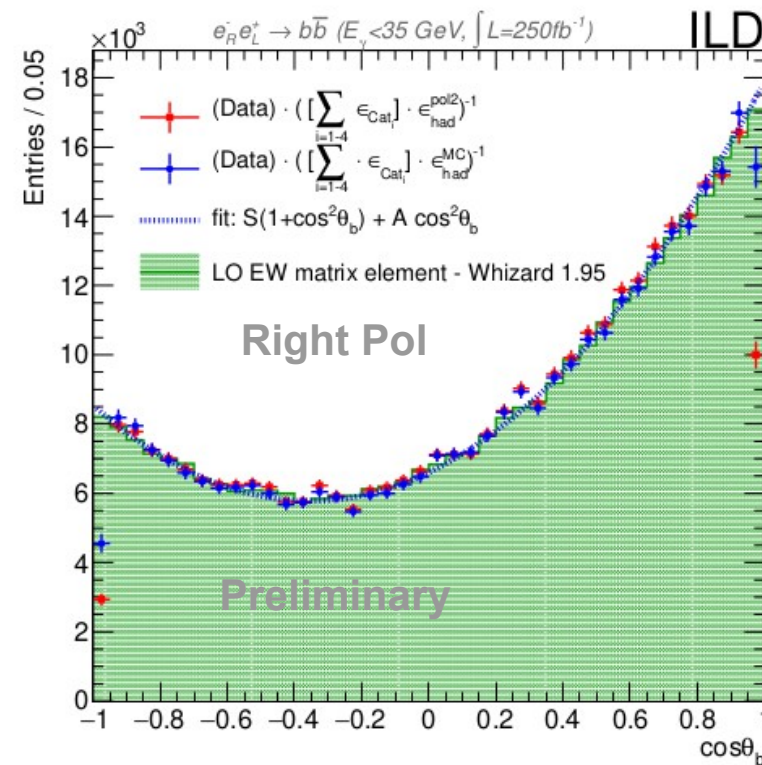
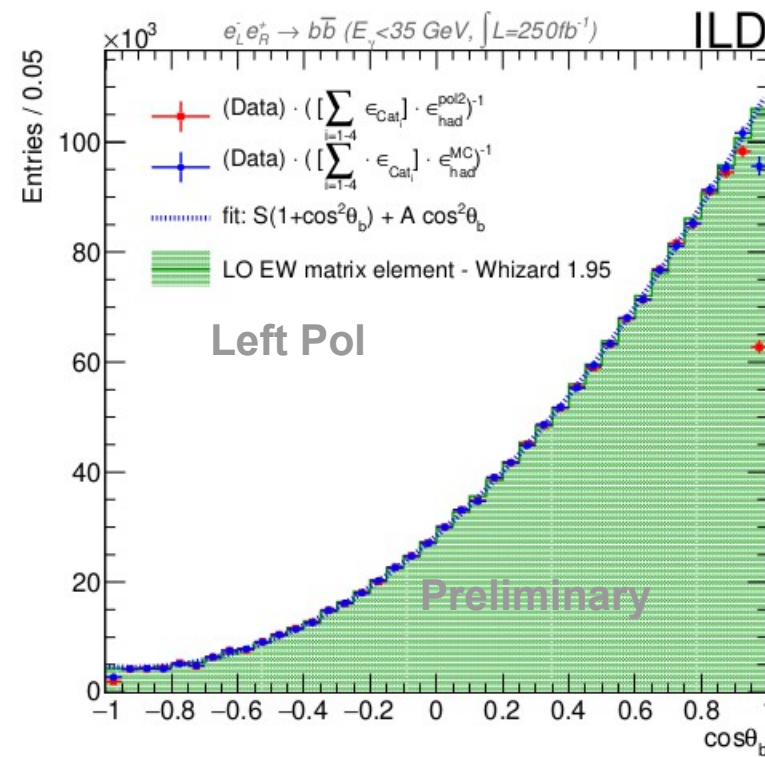


ILD-Note-2019-007

- Integrated Luminosity  $4 \text{ fb}^{-1}$
- Exact reproduction of generated spectra
- Statistical precision on cross section:  $\sim 0.1\%$
- Statistical precision on  $A_{FB}$ :  $\sim 0.5\%$ 
  - Can expect that systematic errors will match statistical precision (but needs to be shown)



Full simulation study within ILD Concept allows for educated guess on uncertainties on Z-Pole



Arxiv:1709.04289, ILD Paper in progress  
 A. Irlès, SUSY2021

## Excellent agreement between predicted and reconstructed distributions

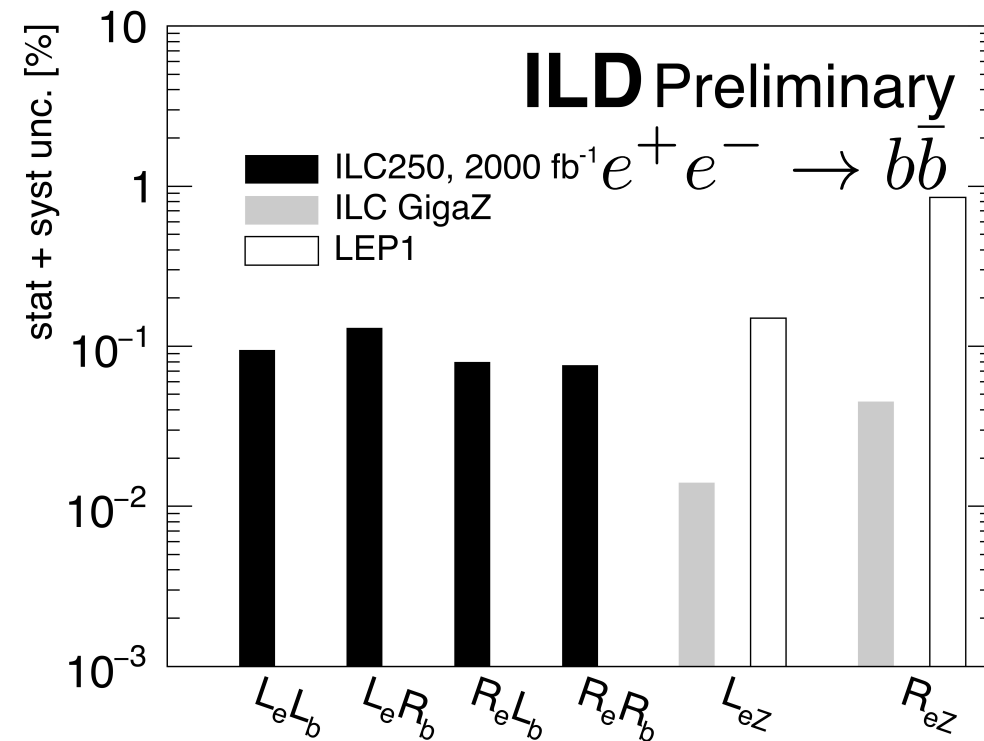
- Gap between red dots and green histogram = acceptance drop.
- Blue dots = corrected acceptance
- The fit is restricted to  $|\cos\theta_b| < 0.8$ 
  - *Minimal impact of the corrections*

## Systematic uncertainties under scrutiny:

- Selection and background rejection
- quark tagging/mistagging (modélisation, QCD, correlations)
- Luminosity
- Polarisation

Additional complication in continuum: Rejection of ISR events – Uncertainty  $\sim 5 \times 10^{-4}$  (doesn't apply on Z-pole)

Arxiv:1709.04289, ILD Paper in progress

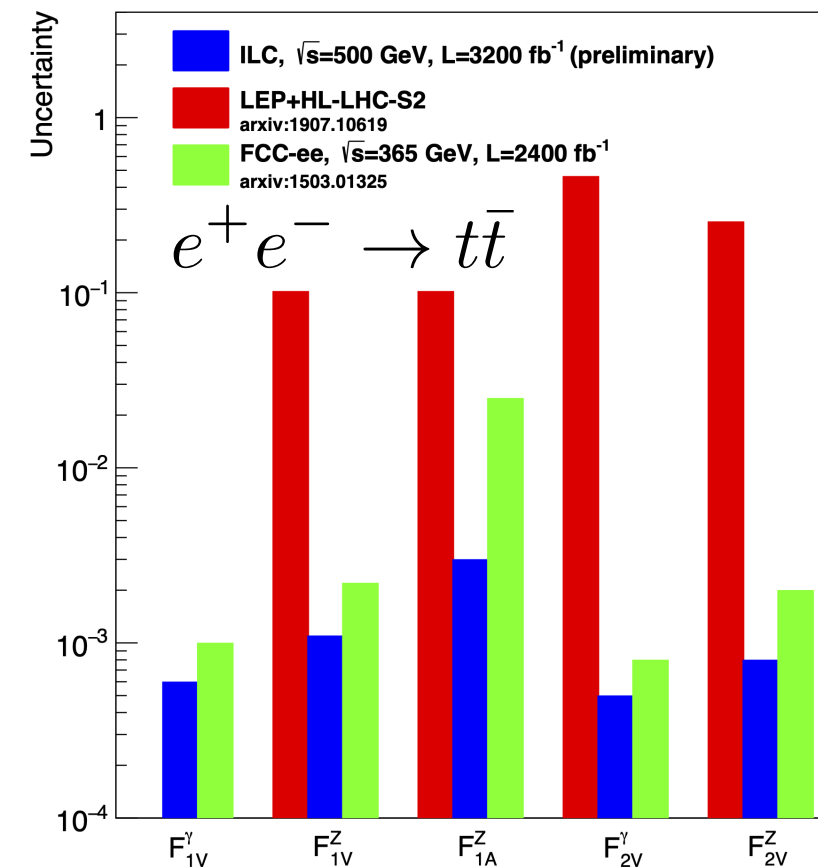


Couplings are order of magnitude better than at LEP

$$LeLb = Q_e Q_b + \frac{LeZLbZ}{s^2 w c^2 w} BWZ + \sum_{Z'} \frac{LeZ'LbZ'}{s^2 w c^2 w} BWZ'$$

Arrows point from the terms to:
 

- ILC250 (from  $Q_e Q_b$ )
- SM (from  $Q_e Q_b$ )
- GigaZ (from  $\frac{LeZLbZ}{s^2 w c^2 w} BWZ$ )
- New resonances (from  $\sum_{Z'} \frac{LeZ'LbZ'}{s^2 w c^2 w} BWZ'$ )

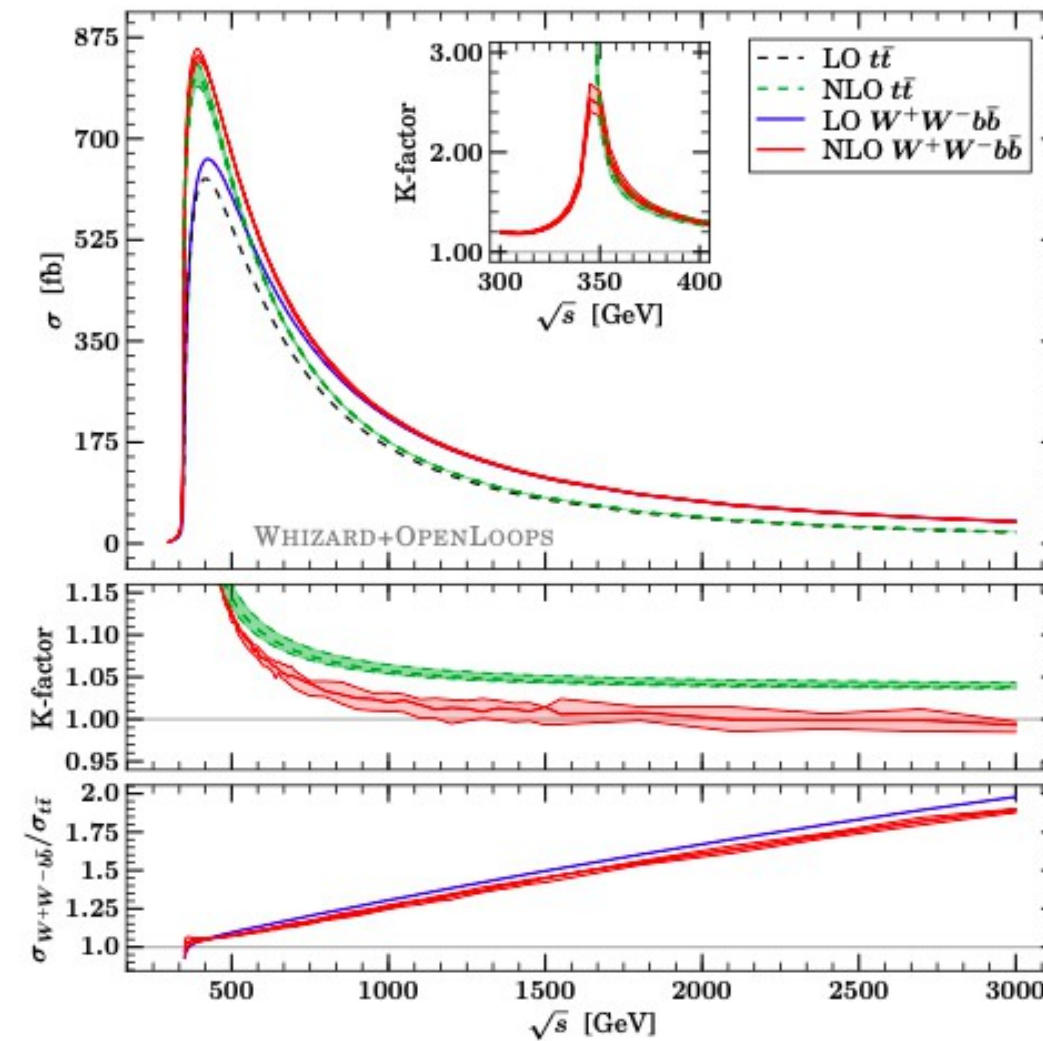
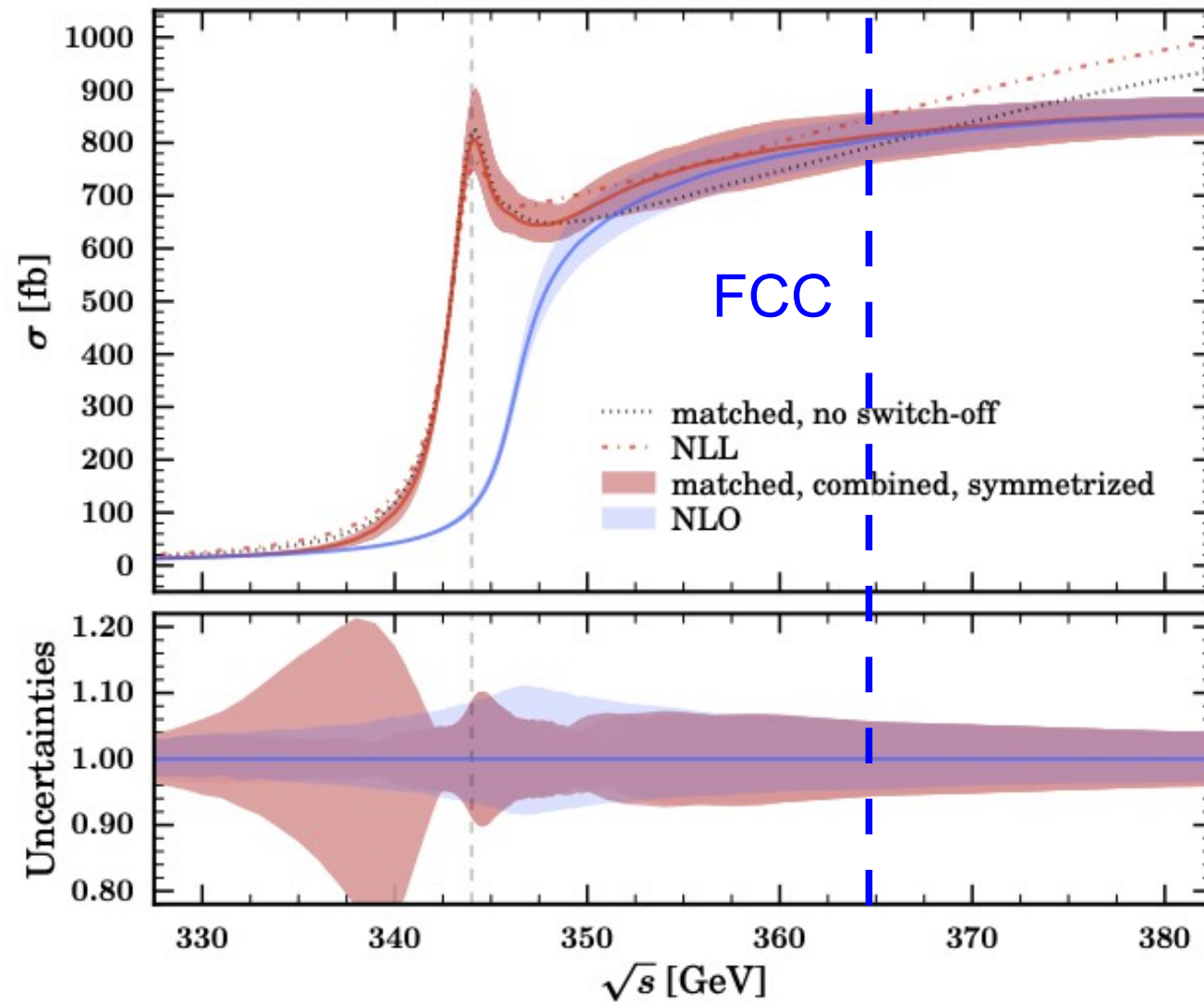


- e<sup>+</sup>e<sup>-</sup> collider way superior to LHC (√s = 14 TeV)
- Final state analysis at FCCee
  - Also possible at LC => Redundancy
- Two remarks:
  - 500 GeV is nicely away from QCD Matching regime
  - Less systematic uncertainties
  - Axial form factors are ~β and benefit therefore from higher energies

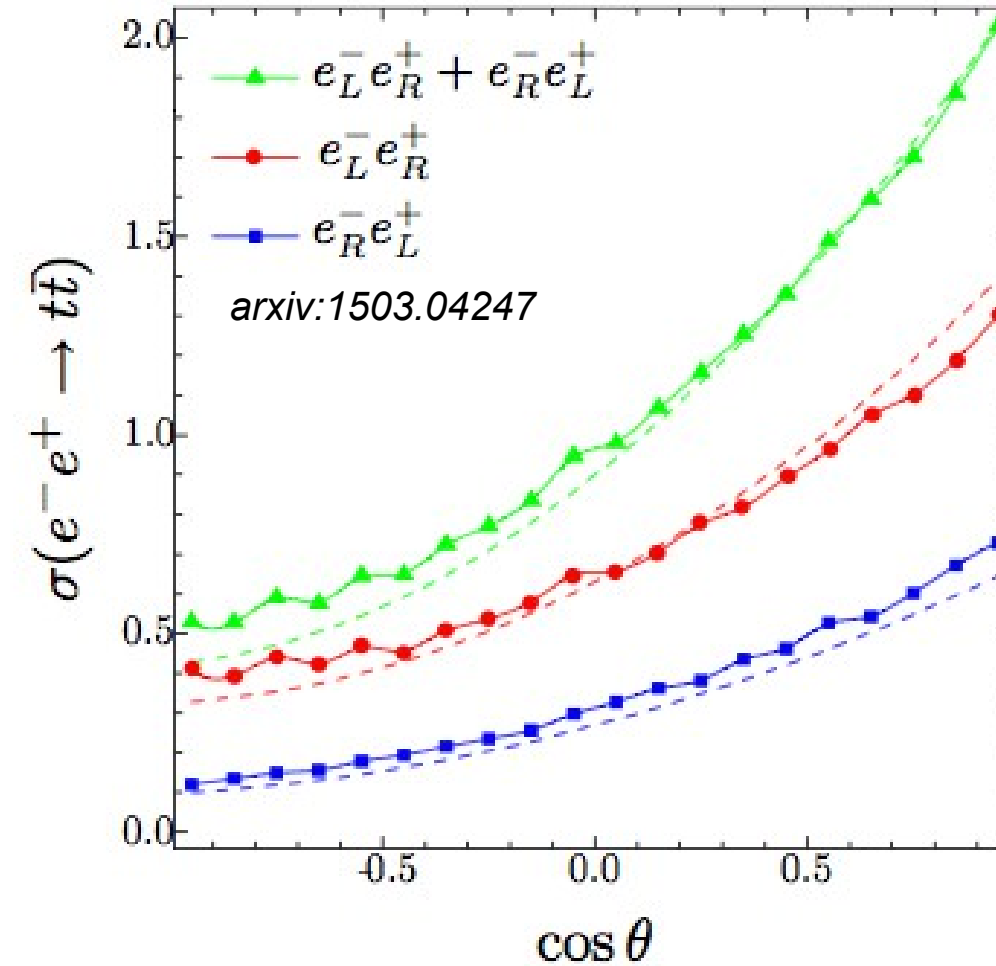
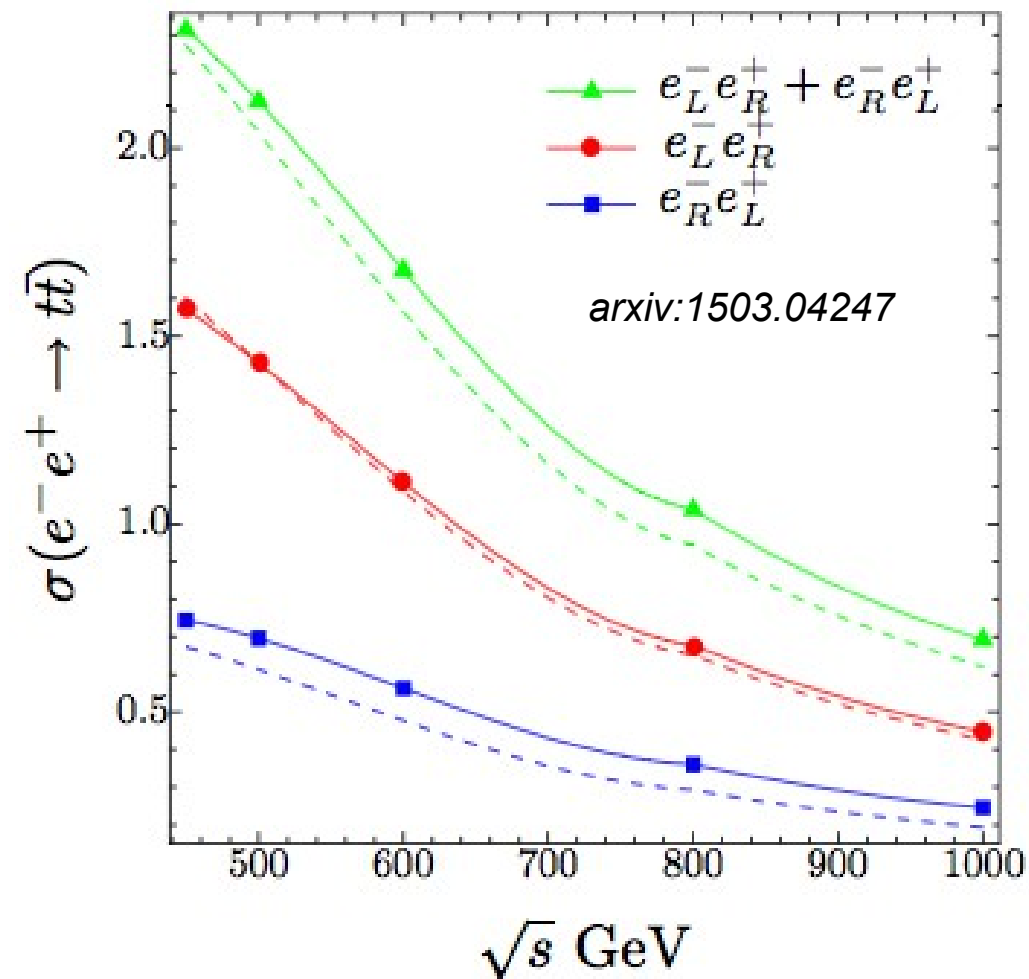
Full disentangling of helicity structure for all fermions only possible with polarised beams!!

$$e^+e^- \rightarrow W^+bW^-\bar{b}$$

Linear Colliders  $\rightarrow$



- Marching non-relativistic calculations in threshold region with  $tt$ -continuum is theoretical challenge
- QCD uncertainties shrink as energy increases
- Non resonant contributions are important (i.e.  $ee \rightarrow tt \rightarrow ee \rightarrow WbWb$ )

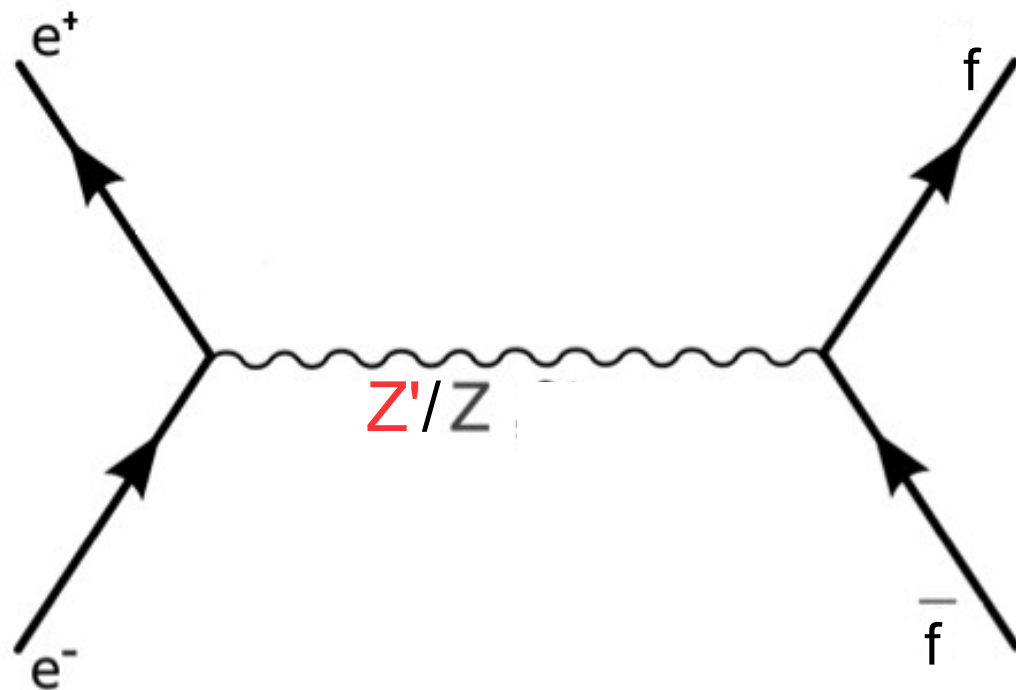


- Electroweak corrections manifest themselves differently for different beam polarisations

**Beam polarisation important asset to disentangle SM and effects of new physics**

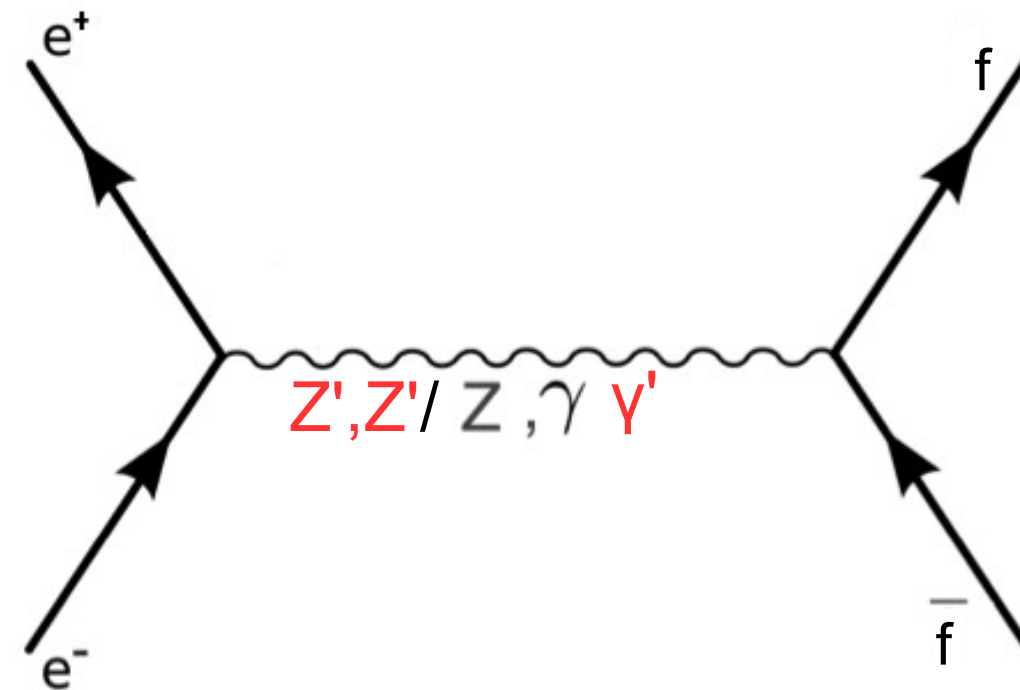
Configuration  $e_R^-e_L^+$  seems to lead to “simpler” corrections

## On the Z-pole

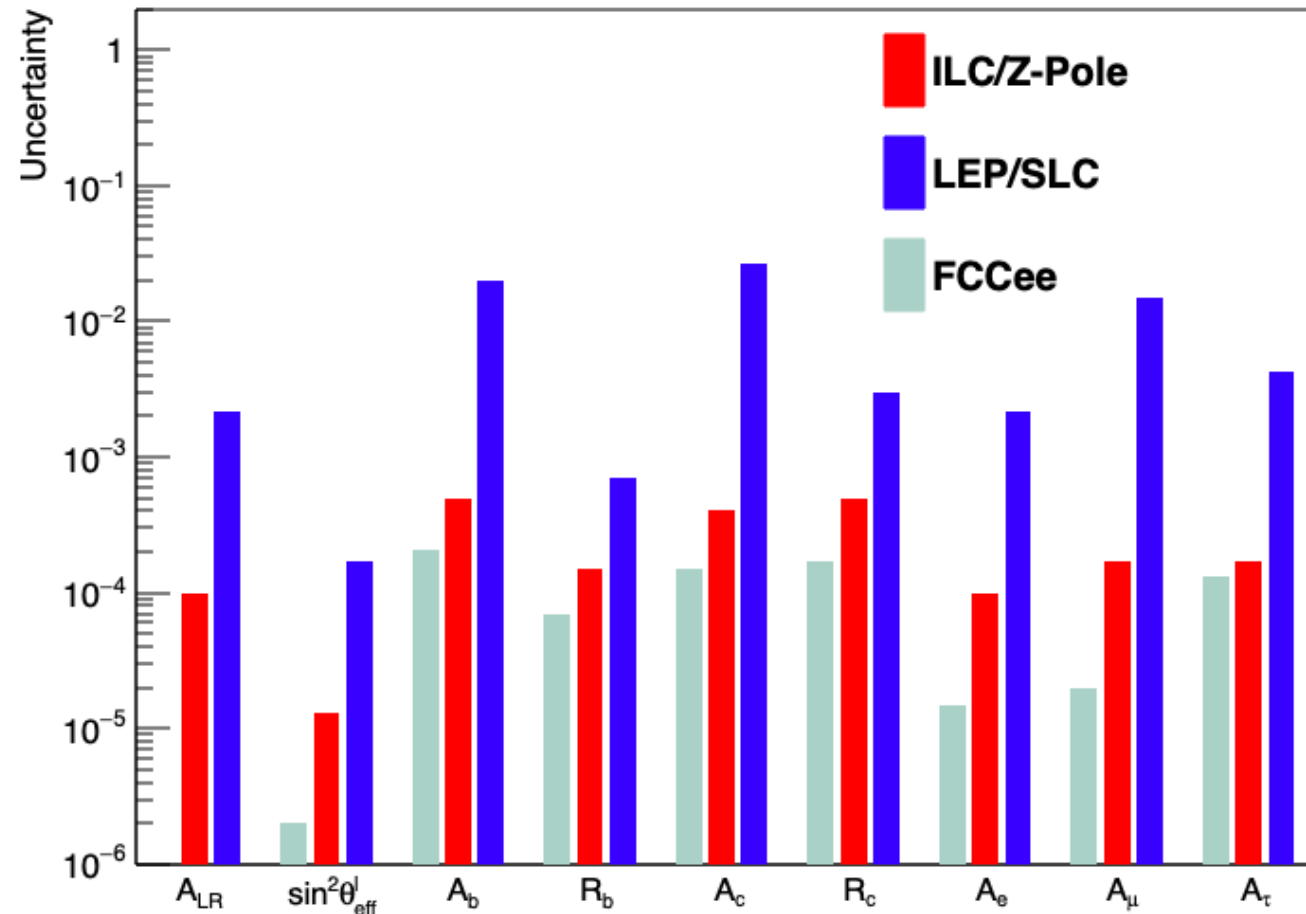


Sensitivity to  $Z/Z'$  mixing  
 Sensitivity to vector (and tensor)  
 couplings of the  $Z$   
 •the photon does not “disturb”

## Above the Z-pole



Sensitivity to interference effects of  $Z$  and photon!!  
 Measured couplings of photon and  $Z$  can be influenced  
 by new physics effects  
 Interpretation of result is greatly supported by precise input  
 from  $Z$  pole



- All future colliders will improve significantly precision compared with LEP/SLC
- Comparable precisions despite differences in luminosity
  - Systematics will play a major role
- Main error sources for heavy quarks
  - Beam polarisation (Linear Collider)
  - QCD corrections that dilute forward-backward asymmetries (arXiv:2010.06604) (all colliders)
    - not considered for ILC here but needs to be looked at once more

Numbers FCCee: “Mixture” of FCC CDR and  
 P. Janot at Precision Workshop/CERN  
<https://indico.cern.ch/event/1140580/timetable/>

Numbers ILC: arxiv: 2203.07622 (ILC Snowmass report)

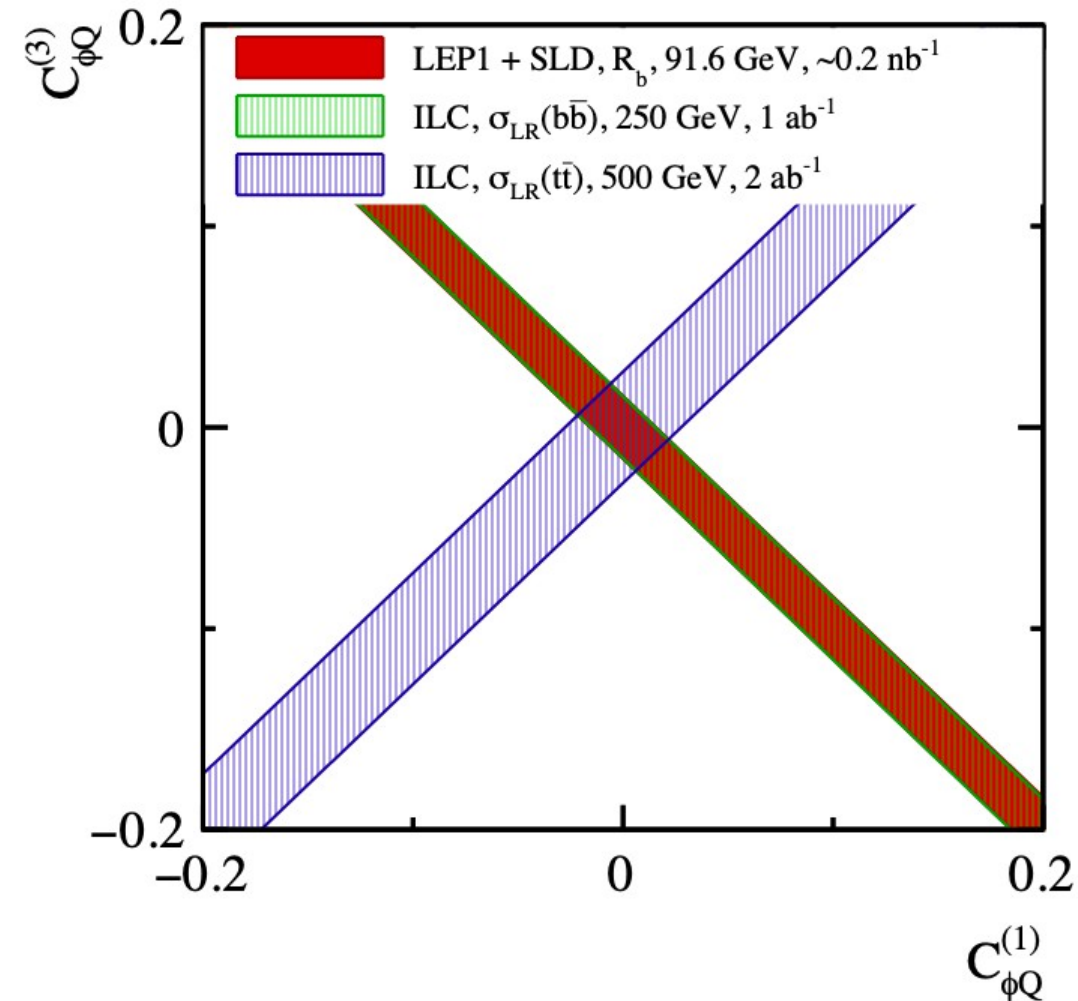
## Summary: Theory inputs for asymmetries

Observables	Present value ( $\times 10^4$ )	TeraZ / GigaZ stat.	TeraZ / GigaZ current syst.	Theory input (not exhaustive)
$A_e$ from $P_\tau$ (FCC-ee)	$1514 \pm 19$	<b>0.07</b>	<b>0.20</b>	SM relation to measured quantities
$A_e$ from $A_{LR}$ (ILC)		<b>0.15</b>	<b>0.80</b>	
$A_\mu$ from $A_{FB}$ (FCC-ee)	$1456 \pm 91$	<b>0.23</b>	<b>0.22</b>	Accurate QED (ISR, IFI, FSR)
$A_\mu$ from $A_{FB}^{pol}$ (ILC)		<b>0.30</b>	<b>0.80</b>	
$A_\tau$ from $P_\tau$ (FCC-ee)	$1449 \pm 40$	<b>0.05</b>	<b>2.00</b>	Prediction for non- $\tau$ backgrounds
$A_\tau$ from $A_{FB}$ (FCC-ee)		<b>0.23</b>	<b>1.30</b>	
$A_\tau$ from $A_{FB}^{pol}$ (ILC)		<b>0.30</b>	<b>0.80</b>	
$A_b$ from $A_{FB}$ (FCC-ee)	$8990 \pm 130$	<b>0.24</b>	<b>2.10</b>	QCD calculations
$A_b$ from $A_{FB}^{pol}$ (ILC)		<b>0.90</b>	<b>5.00</b>	
$A_c$ from $A_{FB}$ (FCC-ee)	$65400 \pm 210$	<b>2.00</b>	<b>1.50</b>	
$A_c$ from $A_{FB}^{pol}$ (ILC)		<b>2.00</b>	<b>3.70</b>	

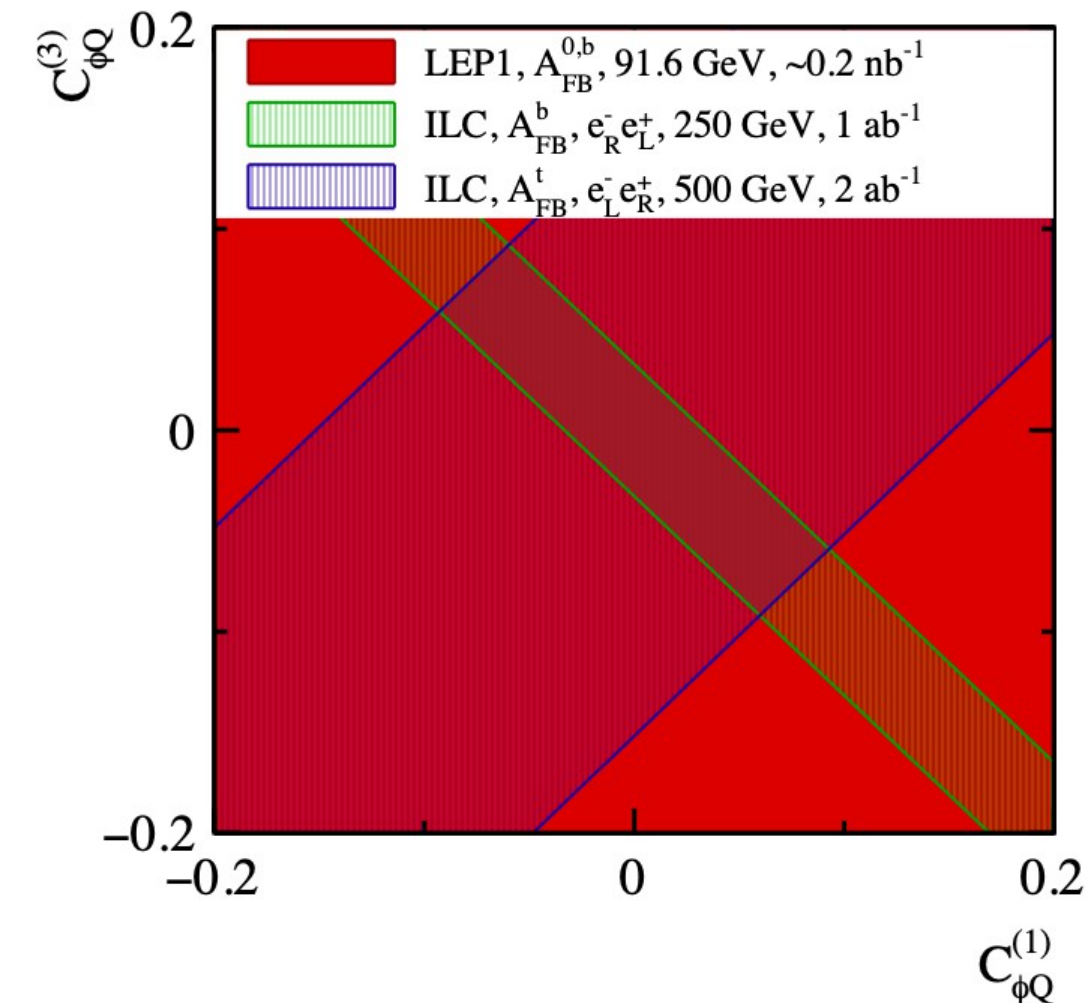
- ◆ **And also sophisticated and state of the art MC generators (signal and backgrounds)**
  - **Plus, maybe, redefined EW Precision Parameters (EWPP) and extraction procedures ?**

Projections from <https://www.overleaf.com/read/xnfpvbdgfgpr>

From cross section



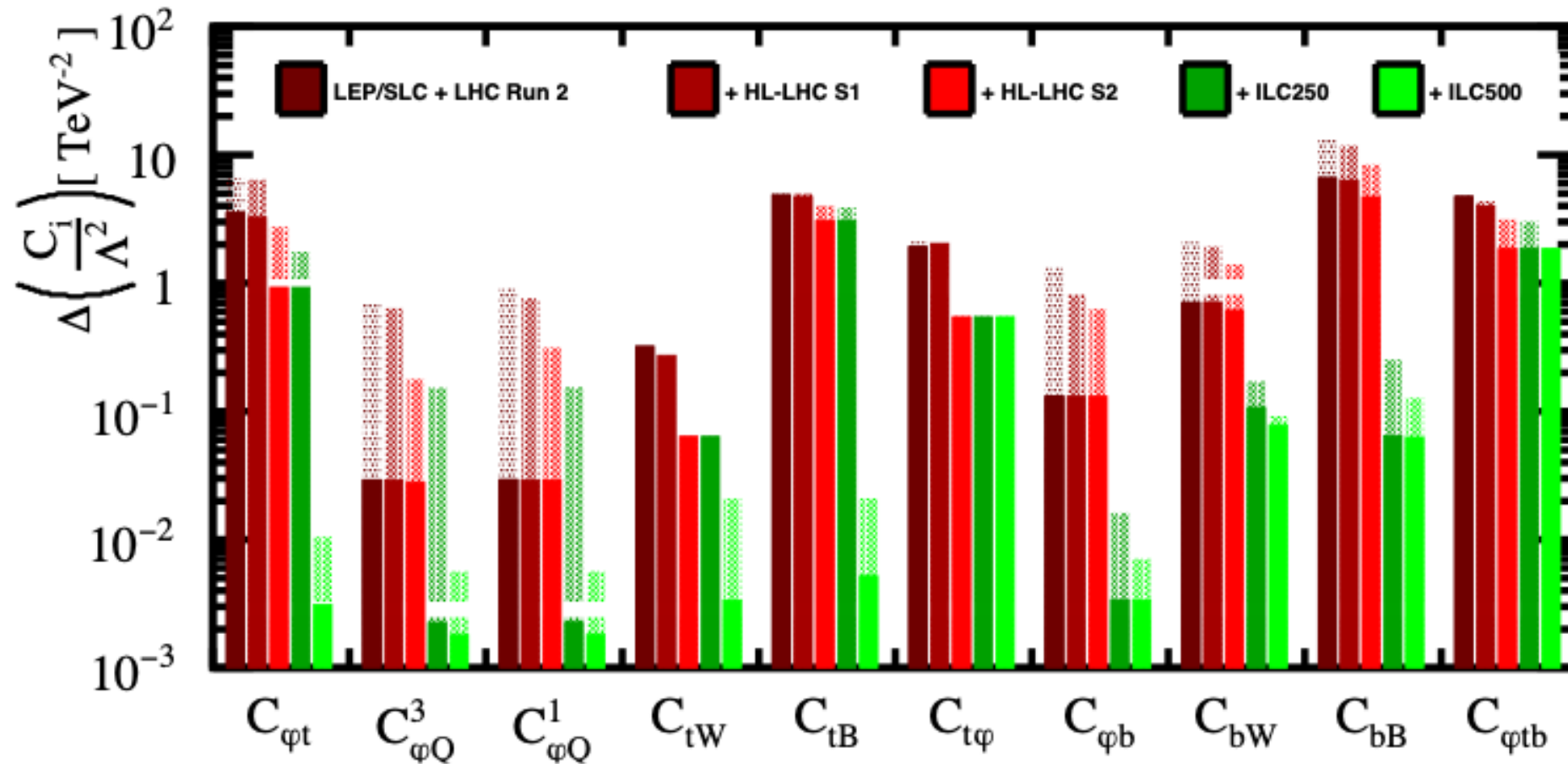
From forward-backward asymmetry



- Measurement of bottom and top observables delivers complementary information for EFT operators
- **ILC@250** GeV comparable to LEP in terms of cross section => Constrain on  $g_{Lb}$
- **ILC@250** GeV drastically better than LEP in terms of AFB => Constrain on  $g_{Rb}$
- How would the picture look with GigaZ precisions?



*arxiv:1907.10619*



## Mapping between FF and EFT Coefficients

$$F_{1V}^Z = \frac{\frac{1}{4} - \frac{2}{3}s_W^2}{s_W c_W} - \frac{m_t^2}{\Lambda^2} \frac{1}{2s_W c_W} \left[ C_{\varphi q}^V = C_{\varphi u}^{(33)} + (C_{\varphi q}^{1(33)} - C_{\varphi q}^{3(33)}) \right],$$

$$F_{1A}^Z = \frac{-\frac{1}{4}}{s_W c_W} - \frac{m_t^2}{\Lambda^2} \frac{1}{2s_W c_W} \left[ C_{\varphi q}^A = C_{\varphi u}^{(33)} - (C_{\varphi q}^{1(33)} - C_{\varphi q}^{3(33)}) \right],$$

$$F_{2V}^Z = 4 \frac{m_t^2}{\Lambda^2} \left[ C_{uZ}^R = \text{Re}\{c_W^2 C_{uW}^{(33)} - s_W^2 C_{uB}^{(33)}\} / s_W c_W \right],$$

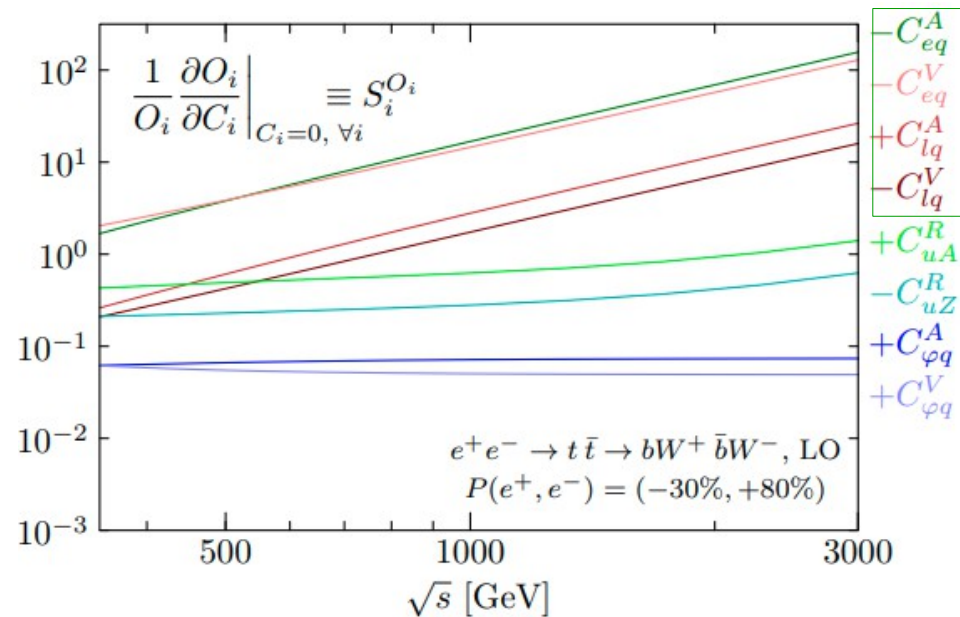
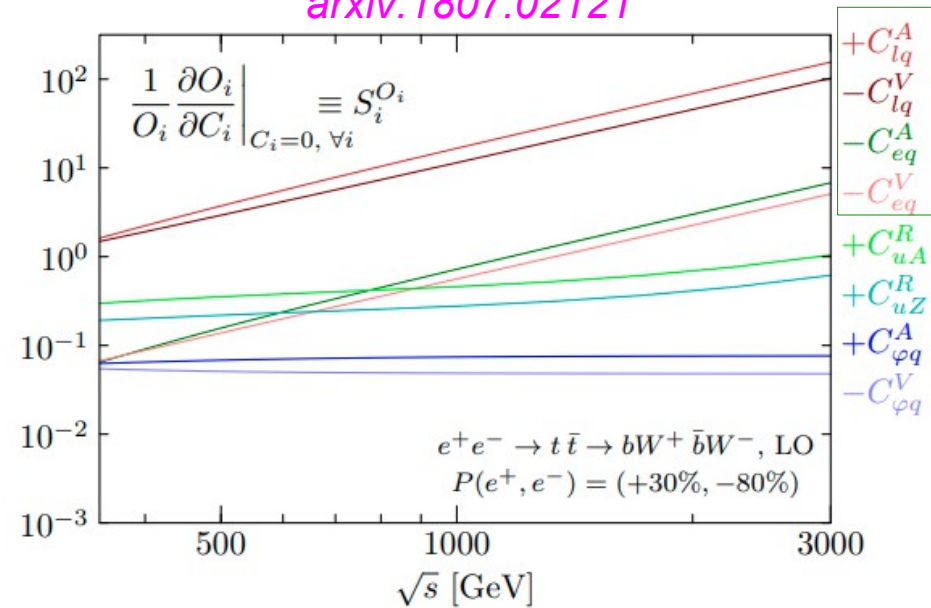
$$F_{2A}^Z = 4 \frac{m_t^2}{\Lambda^2} i \left[ C_{uZ}^I = \text{Im}\{c_W^2 C_{uW}^{(33)} - s_W^2 C_{uB}^{(33)}\} / s_W c_W \right],$$

*arxiv:1807.02121*

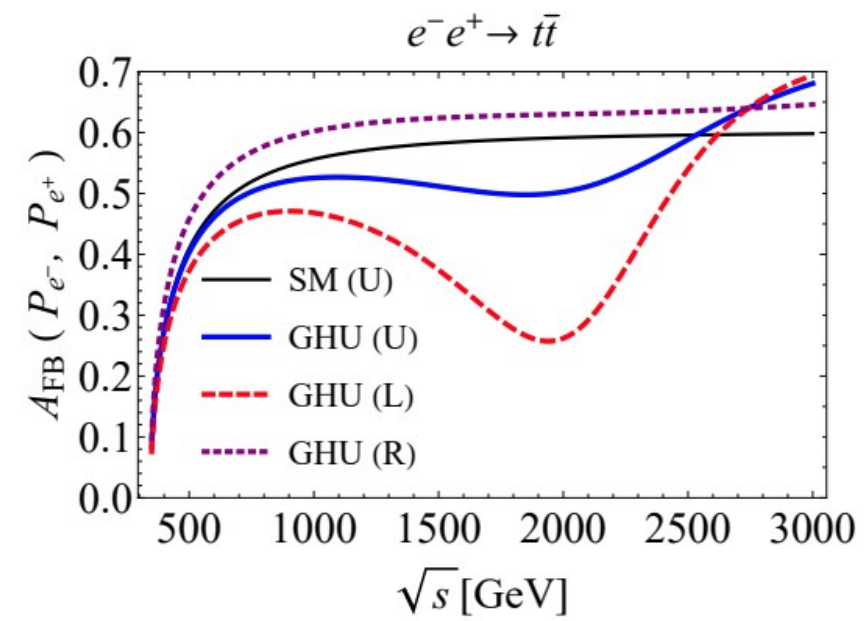
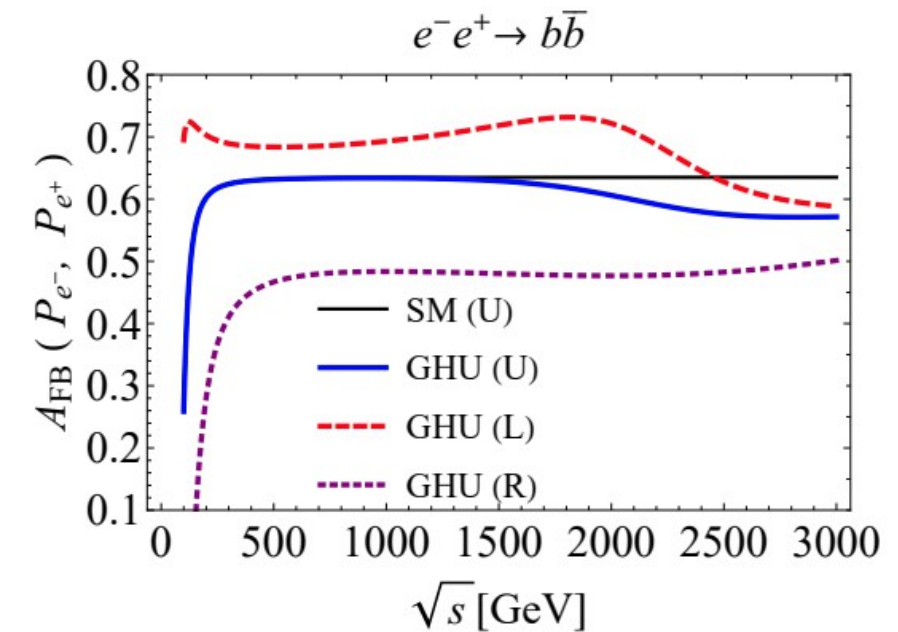
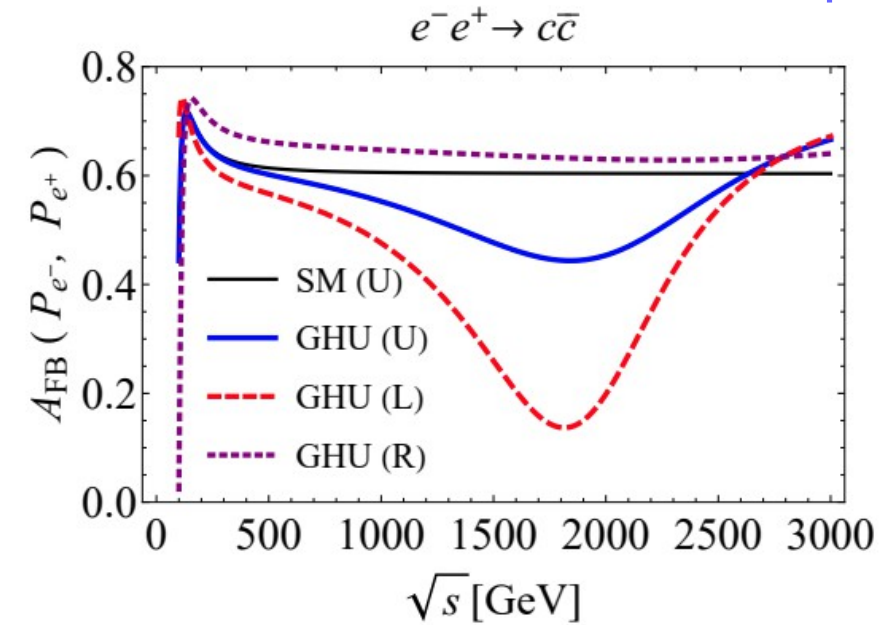
- Translation of results into EFT language confirm superiority of e<sup>+</sup>e<sup>-</sup> w.r.t. LHC
- Several operators benefit already from 250 GeV running
- Top specific operators constrained by running at 500 GeV

## Development of EFT Operators

arxiv:1807.02121



## GUT Inspired GHU Model



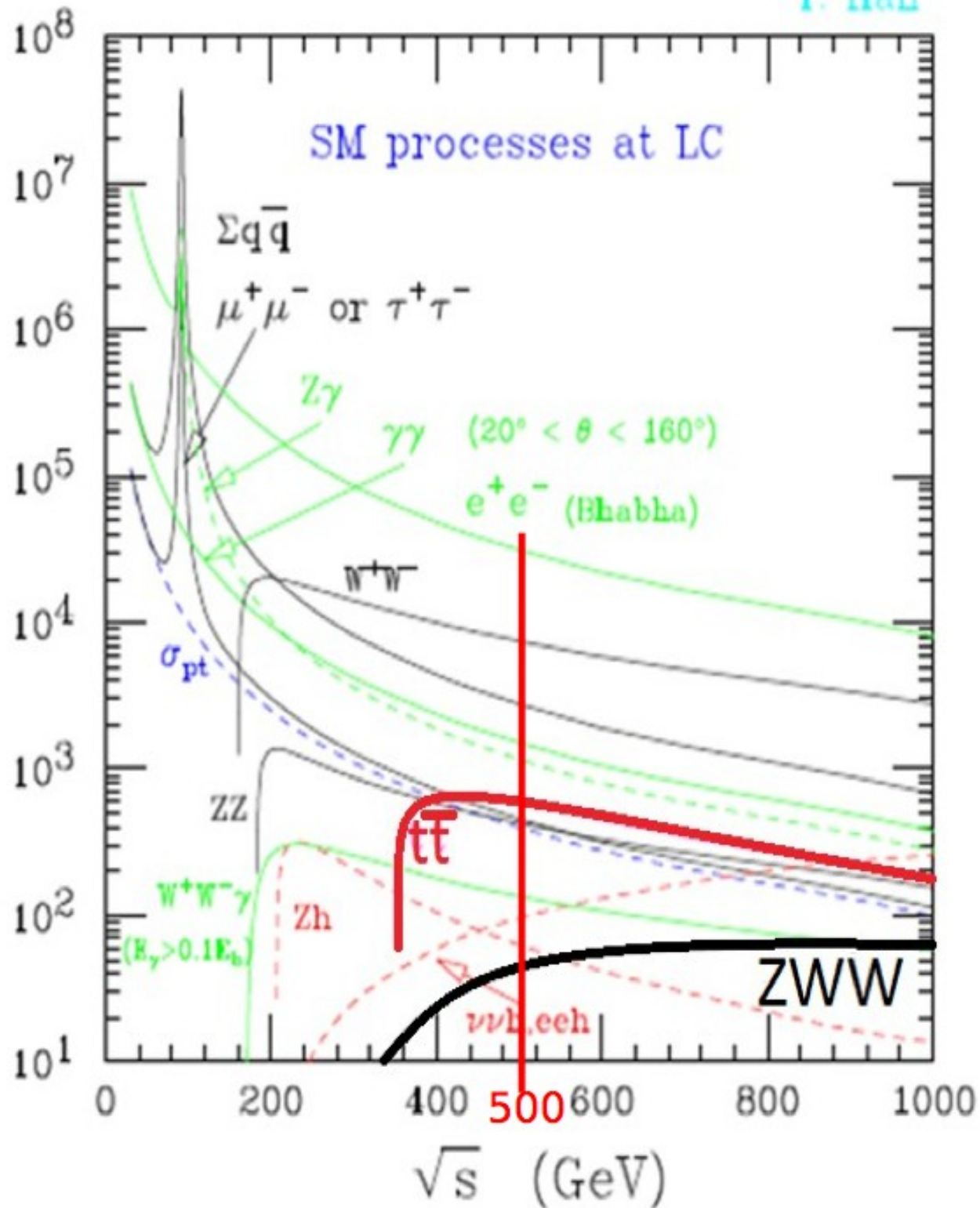
- Effects amplified at higher energies
- Different patterns for different beam polarisations (L, U, R)
- Different patterns for different fermions

Increased sensitivity to operators representing **four-fermion interactions**

- Lepton colliders are ideally suited for precision measurements of two-fermion final states
- Measurement of top mass to a precision of  $\sim 50$  MeV in clean environment
  - Flexibility in energy allow for complementary methods
  - Threshold scan and radiative events
- Linear colliders will have the answer whether new physics acts on heavy doublet (t,b) only or on all fermions
- Will/would probe helicity structure of electroweak fermion couplings over at least one order of magnitude in energy (Z-Pole  $\rightarrow \sim 1$  TeV)
  - Achievable experimental precisions  $\sim 0.1 - 1\%$
  - Effects may become already visible at 250 GeV stage for b quark and c quarks (and other light fermions)
  - Amplification of effects at higher energies
  - Clear and unique pattern thanks to polarised beams
- Active phenomenological studies in terms of global analyses (EFT) and concrete models
- Main challenge at future machines will be the control of systematic errors
  - Experimentally
    - Vertex charge and particle ID
    - PFO for final state jets
  - Theoretically
    - QCD in many aspects
    - Need at least NLO electroweak predictions (and MC programs) for correct interpretation of results

Backup

T. Han



$$e^+e^- \rightarrow t\bar{t} : 500 \text{ GeV}$$

Channel	$\sigma_{unpol.}$ [fb]	$\sigma_{-,+}$ [fb]	$\sigma_{+,-}$ [fb]
$t\bar{t}$	572	1564	724
$\mu^+\mu^-$	456	969	854
$\sum_{q=u,d,s,c} q\bar{q}$	2208	6032	2793
$b\bar{b}$	372	1212	276
$\gamma Z^0$	11185	25500	19126
$W^+W^-$	6603	26000	150
$Z^0Z^0$	422	1106	582
$Z^0W^+W^-$	40	151	8.7
$Z^0Z^0Z^0$	1.1	3.2	1.22
Single $t$ for $e^+e^- \rightarrow e^- \bar{\nu}_e t\bar{b}$ [11]	3.1	10.0	1.7

352 GeV (unpol)

450 fb

25.2 pb

11.5 pb

865 fb

$$e^+e^- \rightarrow b\bar{b} : 250 \text{ GeV}$$

Channel	$\sigma_{unpol}$ fb	$\sigma_L$ fb	$\sigma_R$ fb
$b\bar{b}$	1756	5629	1394
$\gamma b\bar{b}$ (Z return)	7860	18928	12512
ZZ hadronic with $b\bar{b}$	196	549	236
HZ hadronic with $b\bar{b}$	98	241	152

$$e^+e^- \rightarrow c\bar{c} : 250 \text{ GeV}$$

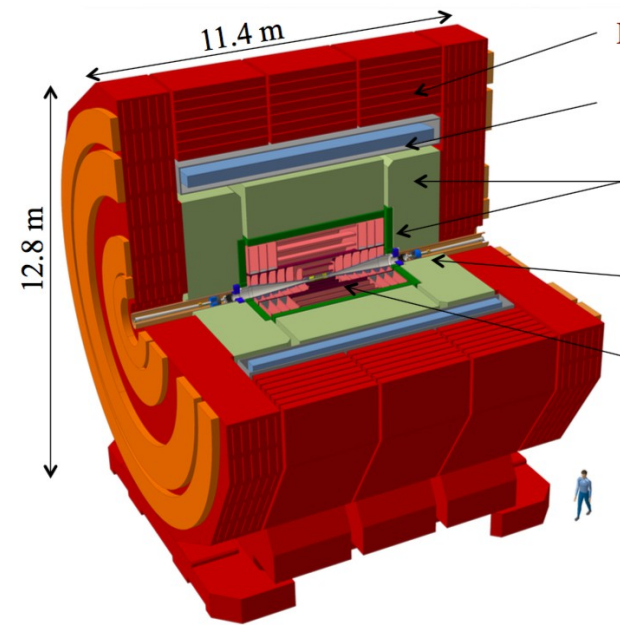
$$\sigma(P_{e^-} = -1, P_{e^+} = +1) \approx 8518 \text{ fb}$$

$$\sigma(P_{e^-} = +1, P_{e^+} = -1) \approx 3565 \text{ fb}$$

$$\sigma_{unpol.} \approx 3020 \text{ fb}$$

e+e- detector concepts for linear colliders  
 Preferred solution Particle Flow Detectors

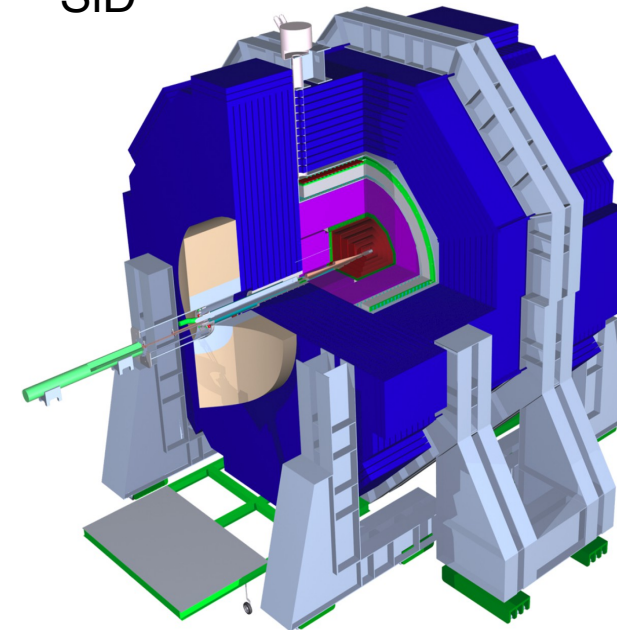
CLIC Detector



B= 4T

Central tracking with silicon

SiD

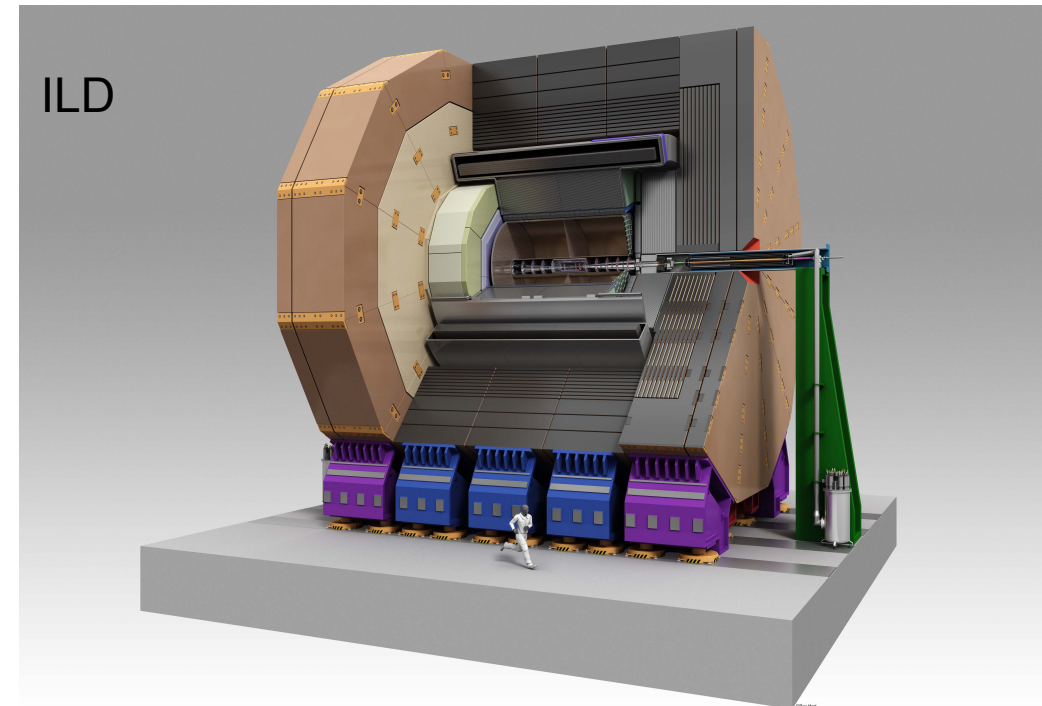


B= 5T

Highly granular calorimeters

Inner tracking with silicon

ILD



B= 3.5T

Central tracking with TPC

Track momentum:  $\sigma_{1/p} < 5 \times 10^{-5}/\text{GeV}$  (1/10 x LEP)

(e.g. Measurement of Z boson mass in Higgs Recoil)

Impact parameter:  $\sigma_{d_0} < [5 \oplus 10/(p[\text{GeV}]\sin^{3/2}\theta)] \mu\text{m}$  (1/3 x SLD)

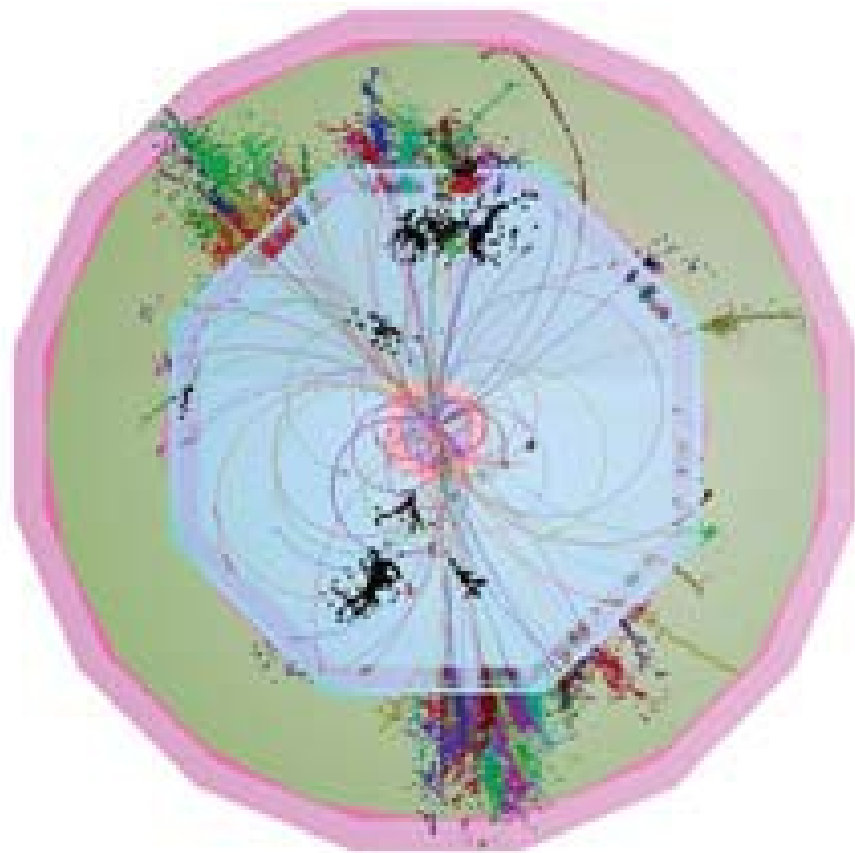
(Quark tagging c/b)

Jet energy resolution :  $dE/E = 0.3/(E(\text{GeV}))^{1/2}$  (1/2 x LEP)

(W/Z masses with jets)

Hermeticity :  $\theta_{\min} = 5 \text{ mrad}$

(for events with missing energy e.g. SUSY)

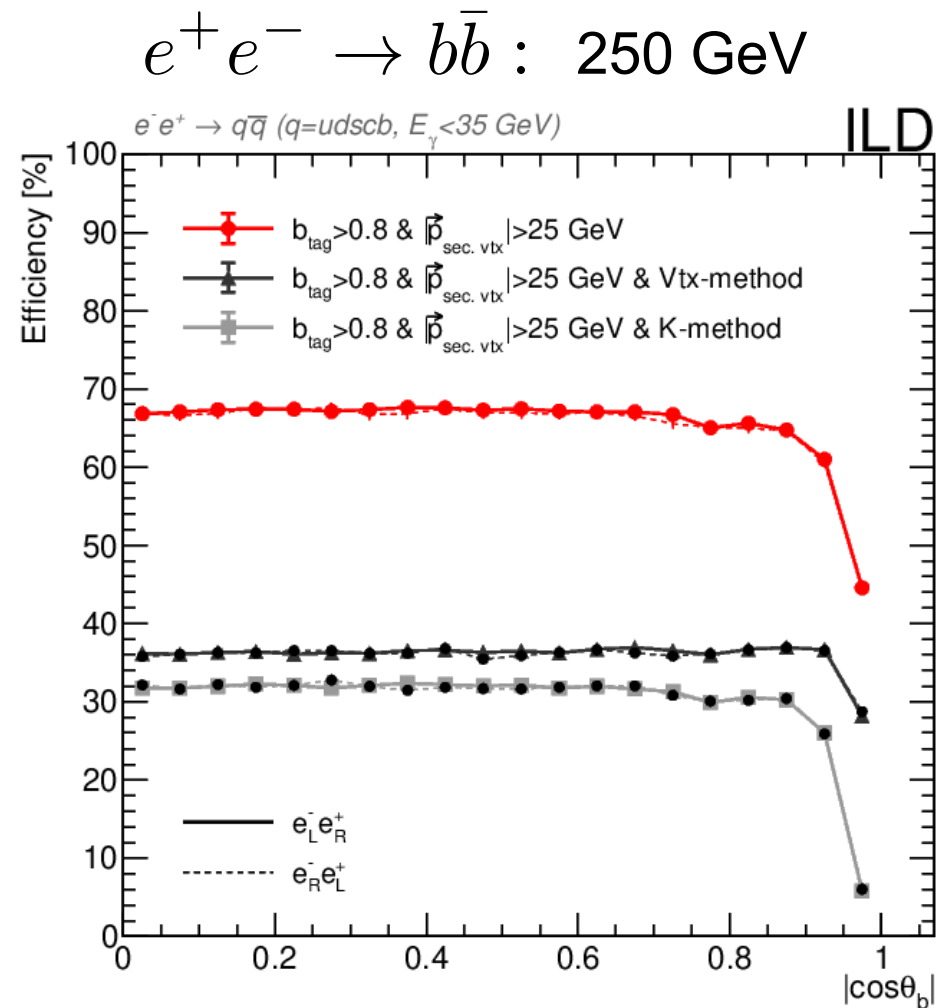


Final state will comprise events with a large number of charged tracks and jets(6+)

- High granularity
- Excellent momentum measurement
- High separation power for particles

Particle Flow Detectors

Detector Concepts: ILD, SiD and CLICdp



- Individual efficiency for correct b-tag and charge measurements using Vtx and Kaon charge
- Final efficiency ~20% from combination of Vtx and Kaon charge in different/same jets

$e_L^- e_R^+ \rightarrow t\bar{t}$  at 500 GeV

General selection cuts	IDR-L	IDR-S
Isolated Lepton	92.1%	92.1%
$b_{tag_1} > 0.8$ or $b_{tag_2} > 0.3$	81.2%	81.1%
Thrust < 0.9	81.2%	81.1%
Hadronic mass	78.2%	78.2%
Reconstructed $m_W$ and $m_t$	73.4%	73.4%
<i>t</i> quark polar angle spectrum		
$\gamma_t^{had.} + \gamma_t^\ell > 2.4$	62.2%	61.8%
$ p_{B, had}  > 15 \text{ GeV}$	34.5%	33.9%
“ <i>t</i> $\bar{t}$ identification”	30.6%	30.2%
<i>b</i> quark polar angle spectrum		
No additional cuts		

- Total cross section
- Typical efficiency 75%
  - Independent of beam polarisation

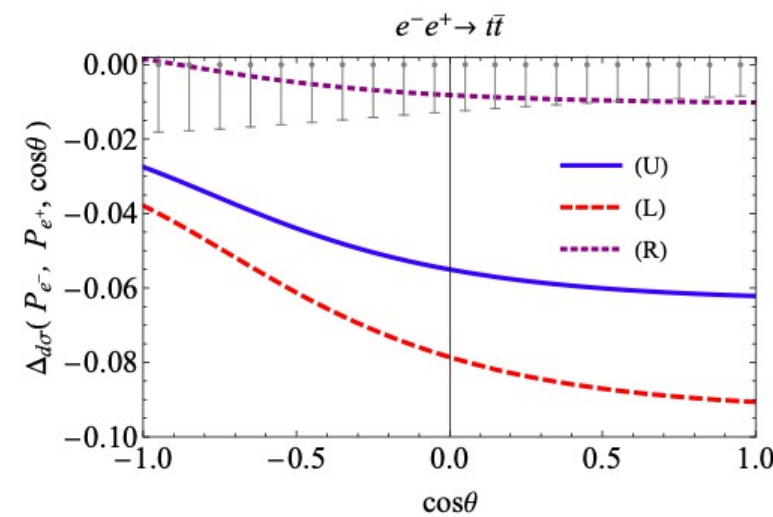
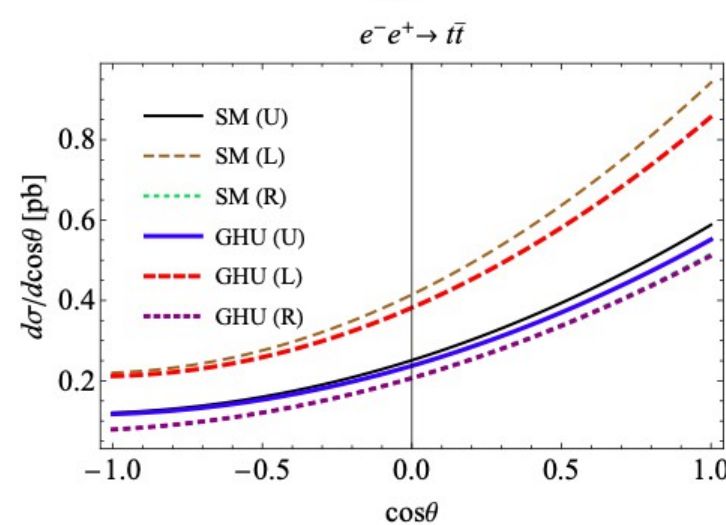
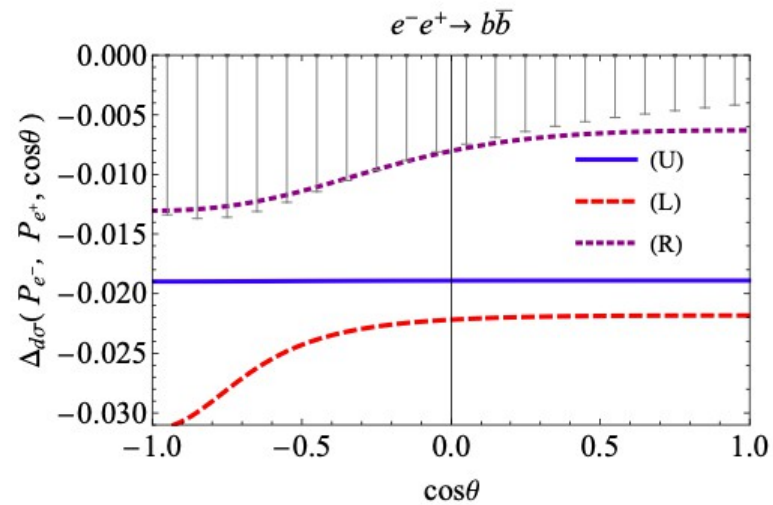
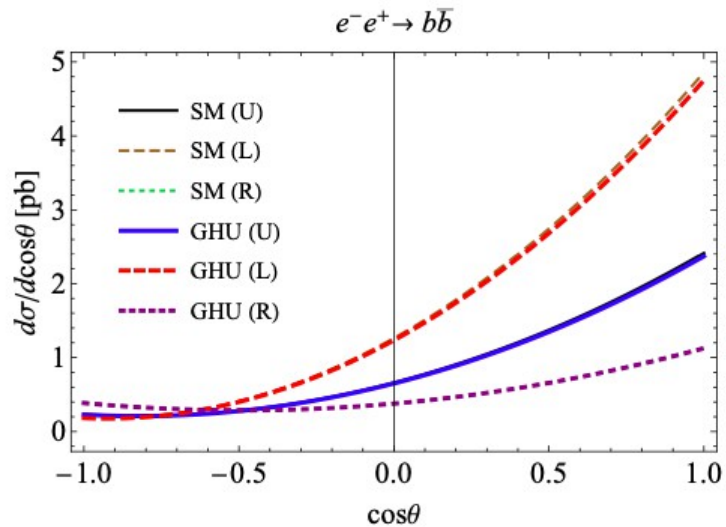
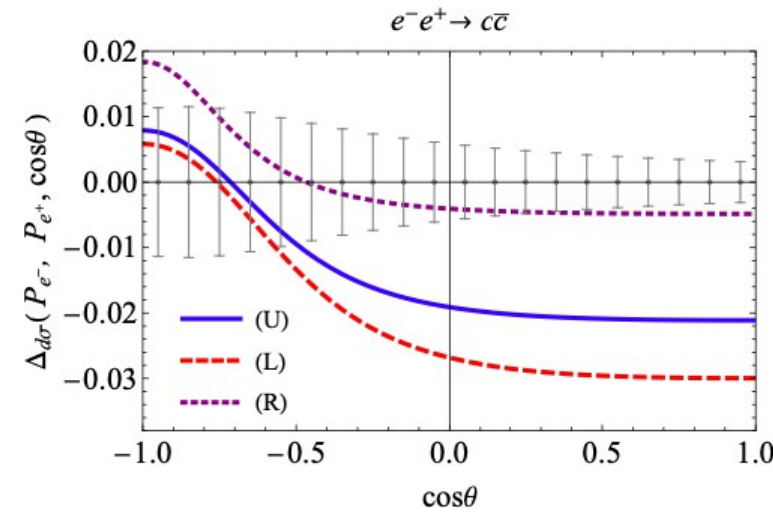
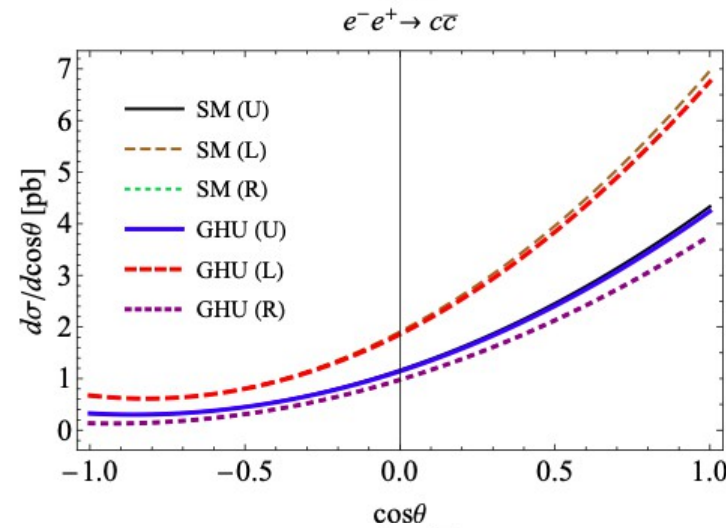
$e_R^- e_L^+ \rightarrow t\bar{t}$  at 500 GeV

General selection cuts	IDR-L	IDR-S
Isolated Lepton	94.1%	94.0%
$b_{tag_1} > 0.8$ or $b_{tag_2} > 0.3$	84.9%	84.8%
Thrust < 0.9	84.9%	84.8%
Hadronic mass	82.2%	82.3%
Reconstructed $m_W$ and $m_t$	77.6%	77.5%
<i>t</i> quark polar angle spectrum		
$\gamma_t^{had.} + \gamma_t^\ell > 2.4$	64.1%	64.1%
<i>b</i> quark polar angle spectrum		
Vtx+Vtx	10.8%	10.3%

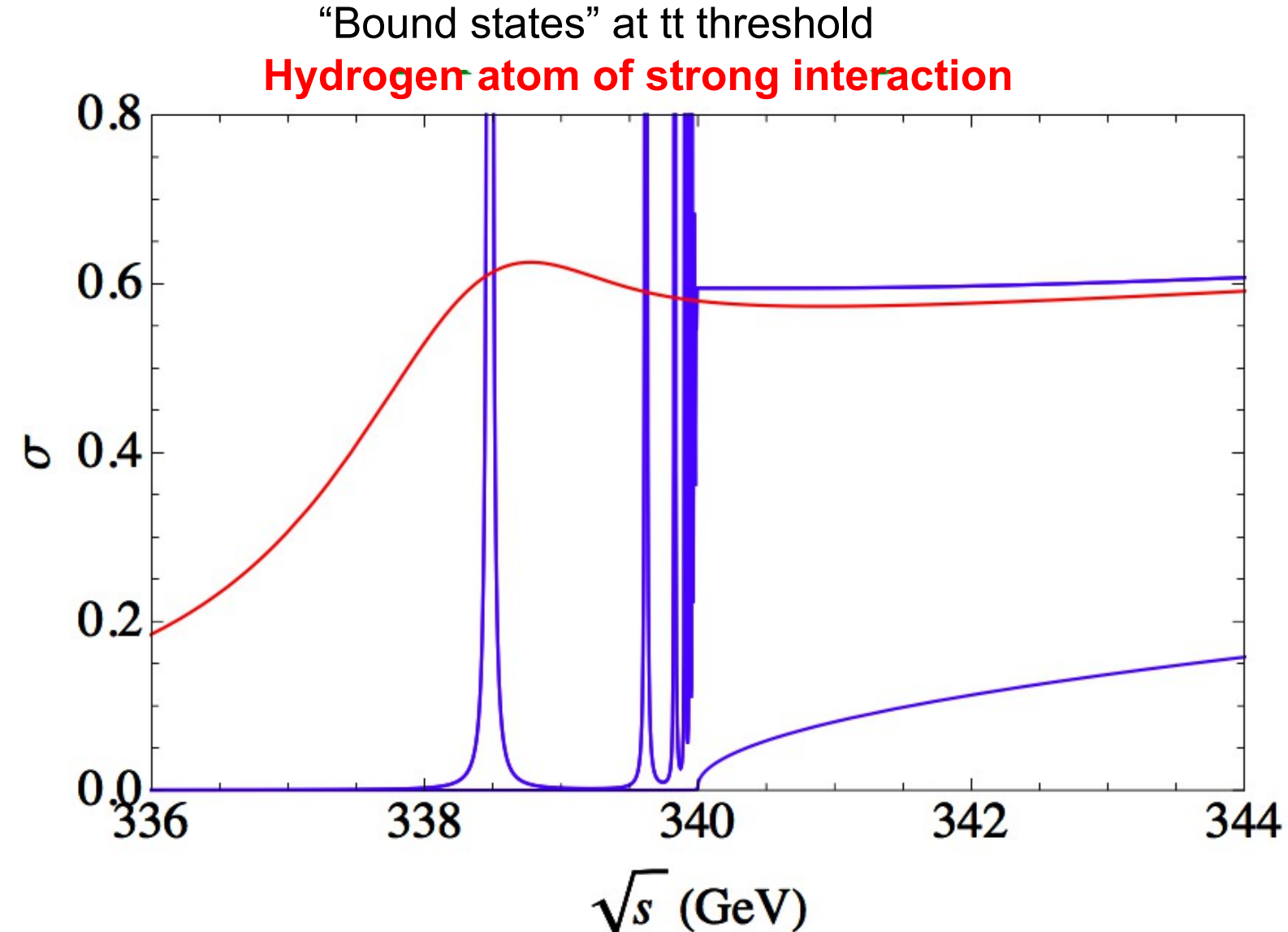
- Differential cross section
- Note, difference for different beam polarisations
  - Left hand polarisation more vulnerable to migrations
  - Requires information from hadronic final state
  - Vtx, Kaon as in bb-case



arxiv:2006.02157

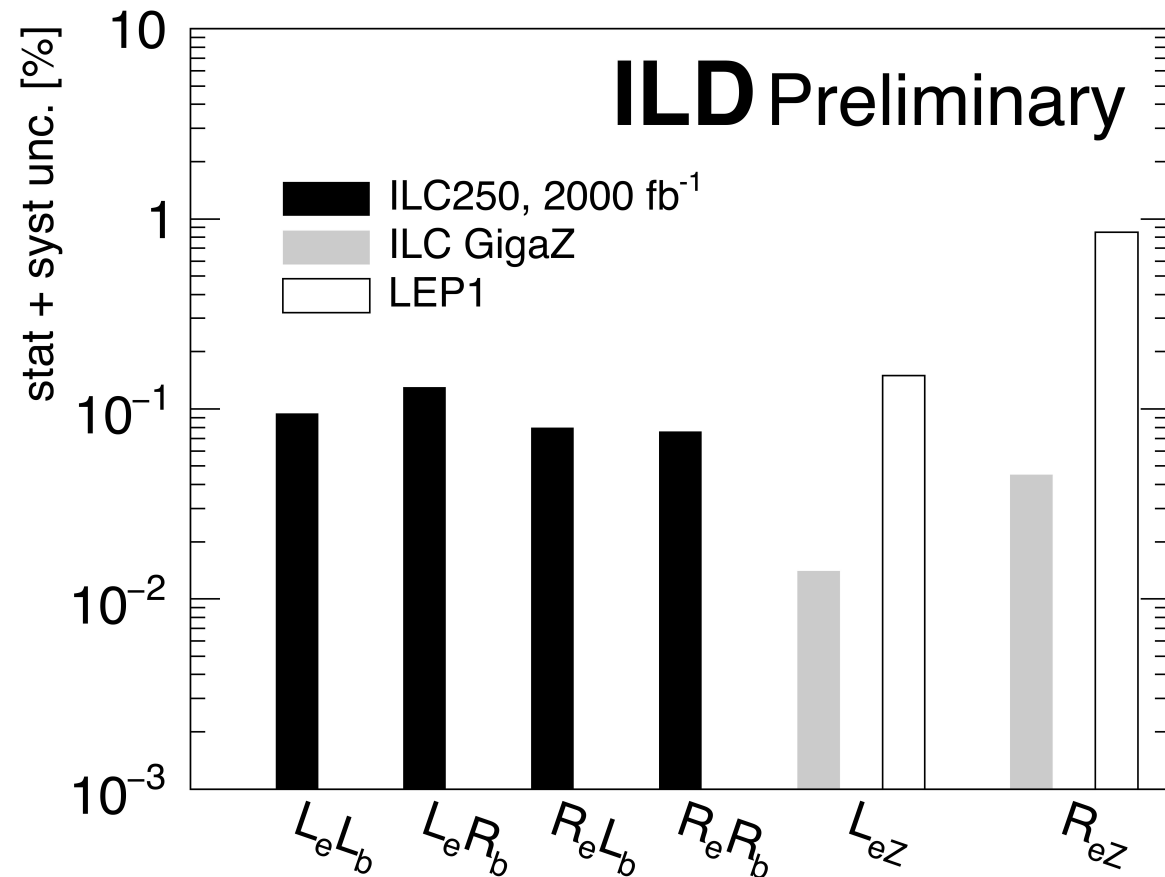


- Model parameter is Hosotani angle  $\theta_H$  yielding the Higgs-Potential as consequence of Aharonov-Bohm Phase in 5<sup>th</sup> dimension
- Model defined in Randall-Sundrum warped extra dimensions
  - KK excitations of gauge bosons and new bosons modify fermion couplings
- Predictions for ILC
  - $m_{KK} = 13$  TeV and  $\theta_H = 0.1$
- Deviations from SM of the order of a few %
  - Effects measurable already at 250 GeV
  - Effects amplified by beam polarisations
  - Effects for tt, bb and cc (and other light fermions)
- One concrete example for importance to measure full pattern of fermion couplings
  - Full pattern only available with beam polarisation



- Size  $O(10^{-17}\text{m})$ , **smallest non-elementary object known in particle physics**  
 Small scale => Free of confinement effects => Ideal premise for precision calculations  
 Measurement of (a hypothetical)  $1^3S_1$  State
- Decay of top quark smears out resonances in a well defined way

## Example b-couplings (same observation for c-couplings, arxiv:2002.05805)



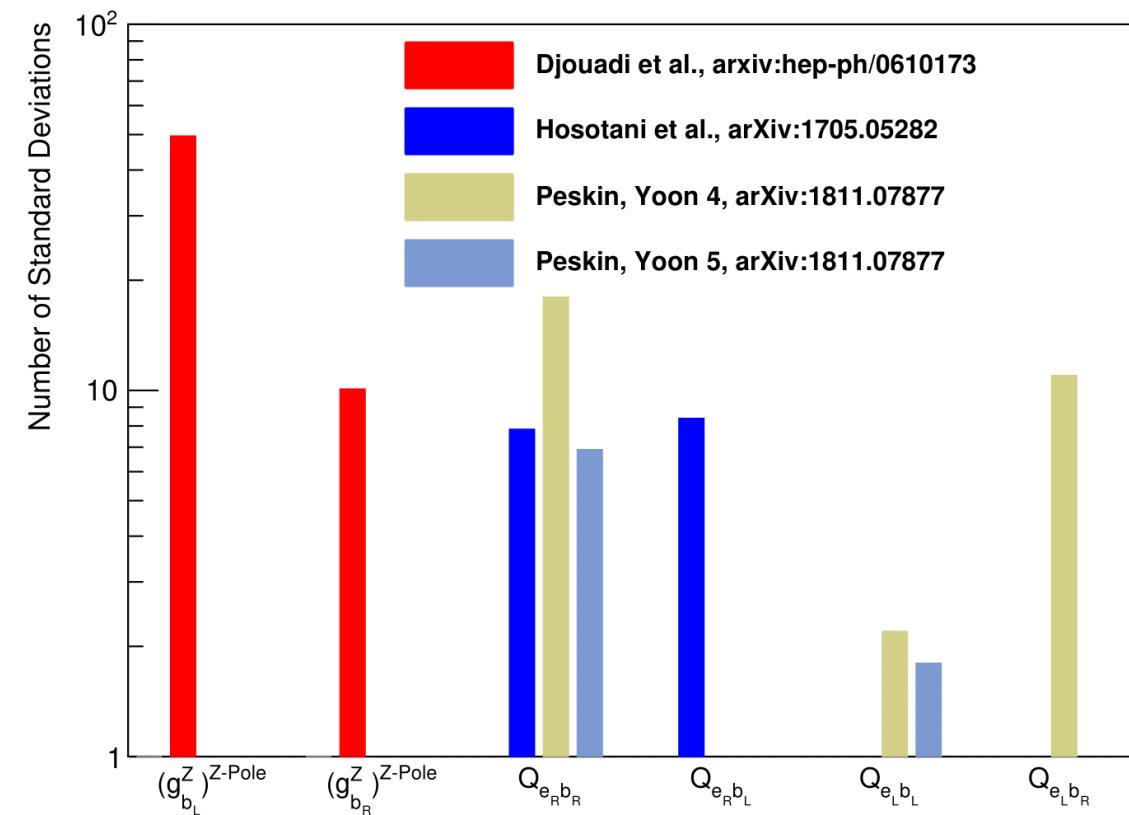
Couplings are order of magnitude better than at LEP

- In particular right handed couplings are much better constrained

New physics can also influence the Zee vertex

- in 'non top-philic' models

Full disentangling of helicity structure for all fermions only possible with polarised beams!!



Impressive sensitivity to new physics in Randall Sundrum Models with warped extra dimensions

- **Complete tests only possible at LC**
- **Discovery reach O(10 TeV)@250 GeV and O(20 TeV)@500 GeV**

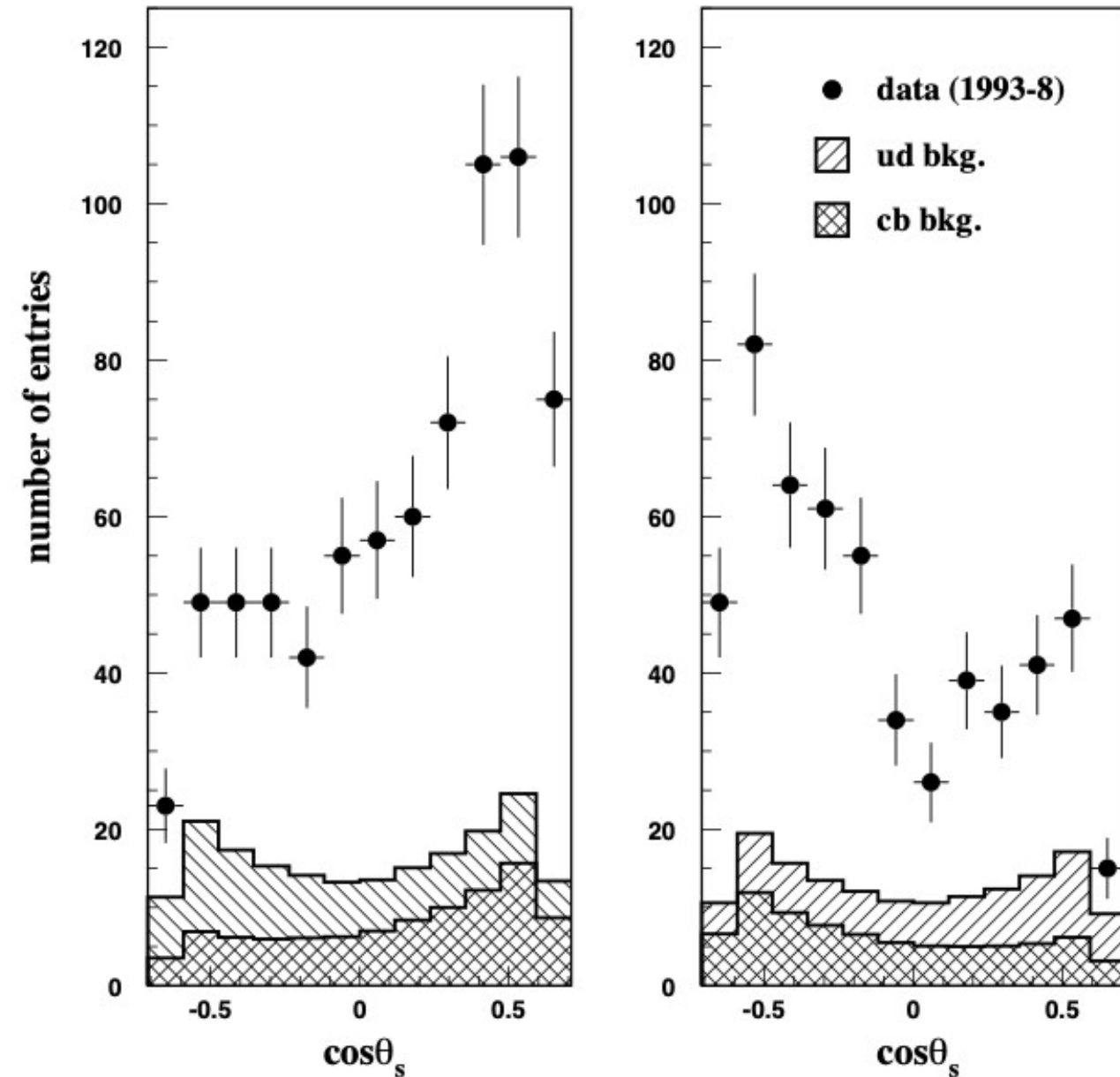
Pole measurements critical input

- Only poorly constrained by LEP

## ee -->ss: SLD Analysis at Z Pole

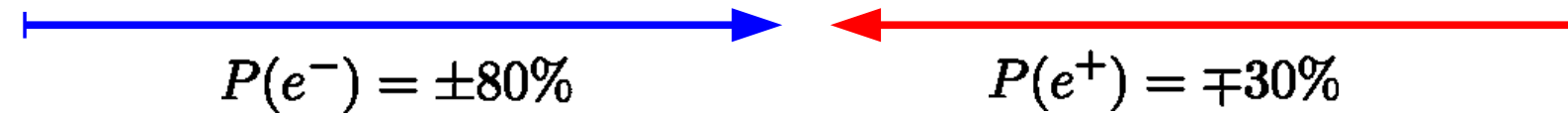
neg. polarization

pos. polarization



- Extend the heavy quark analyses to light quarks to get full picture
- Optimise vertexing and particle ID (i.e .Kaon ID with full simulation studies)

## With two beam polarisation configurations



There exist a number of observables sensitive to chiral structure, e.g.

$\sigma_I$	$A_{FB,I}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$	$(F_R)_I = \frac{(\sigma_{tR})_I}{\sigma_I}$
x-section	Forward backward asymmetry	Fraction of right handed top quarks



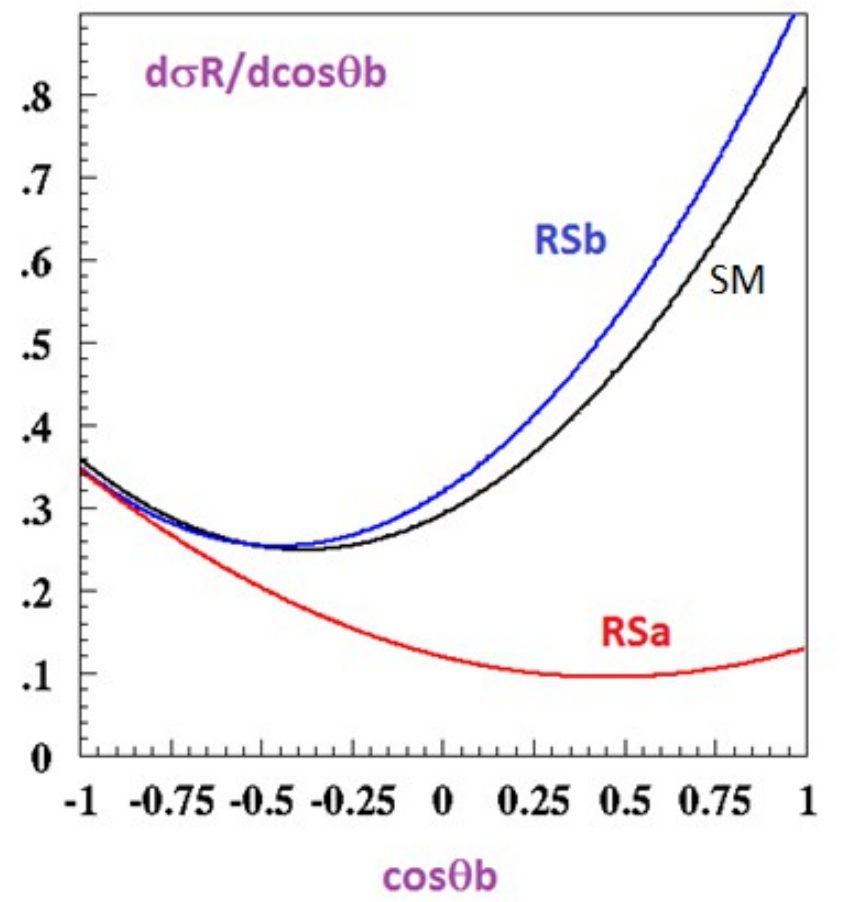
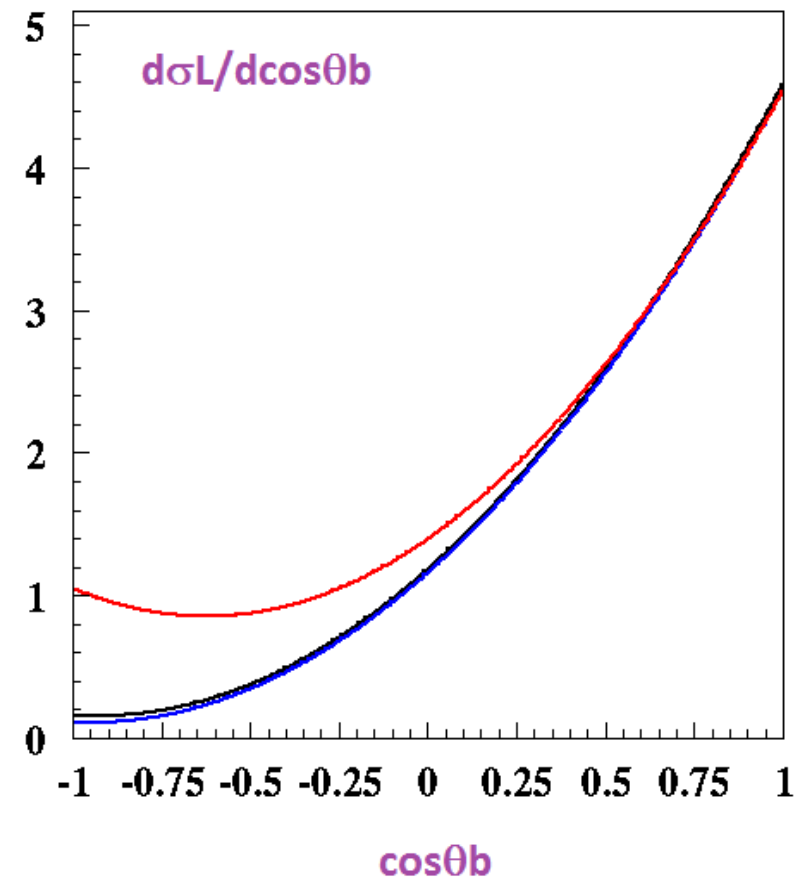
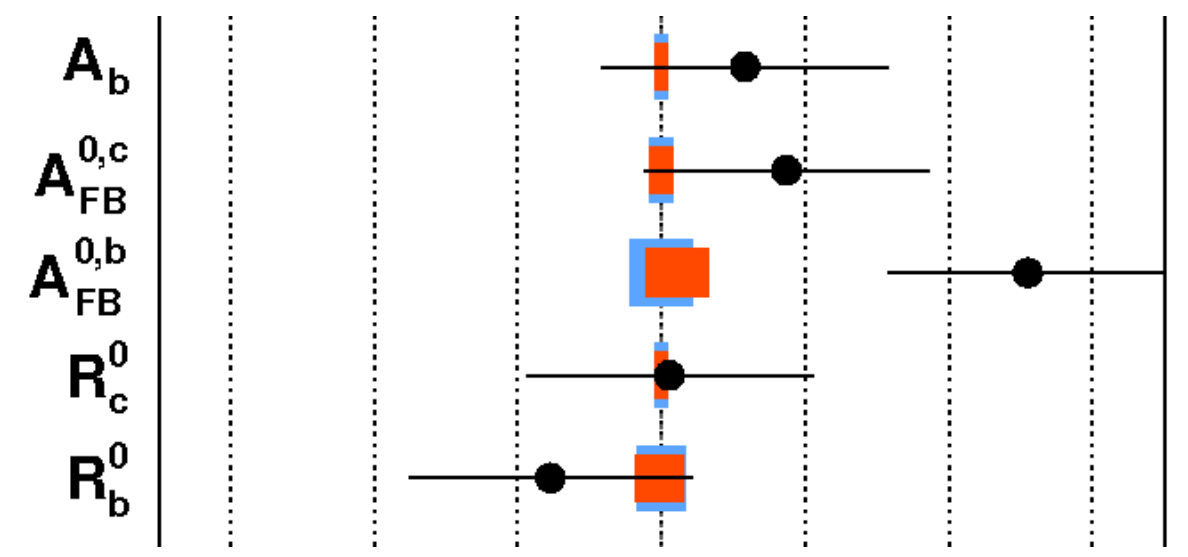
### Extraction of relevant unknowns

$$F_{1V}^\gamma, F_{1V}^Z, F_{1A}^\gamma = 0, F_{1A}^Z \quad \text{or equivalently} \quad g_L^\gamma, g_R^\gamma, g_L^Z, g_R^Z$$

$$F_{2V}^\gamma, F_{2V}^Z$$

~3σ in heavy quark observable  $A_{FB}^b$

ee->bb@250 GeV



- Is tension due to underestimation of errors or due to new physics?

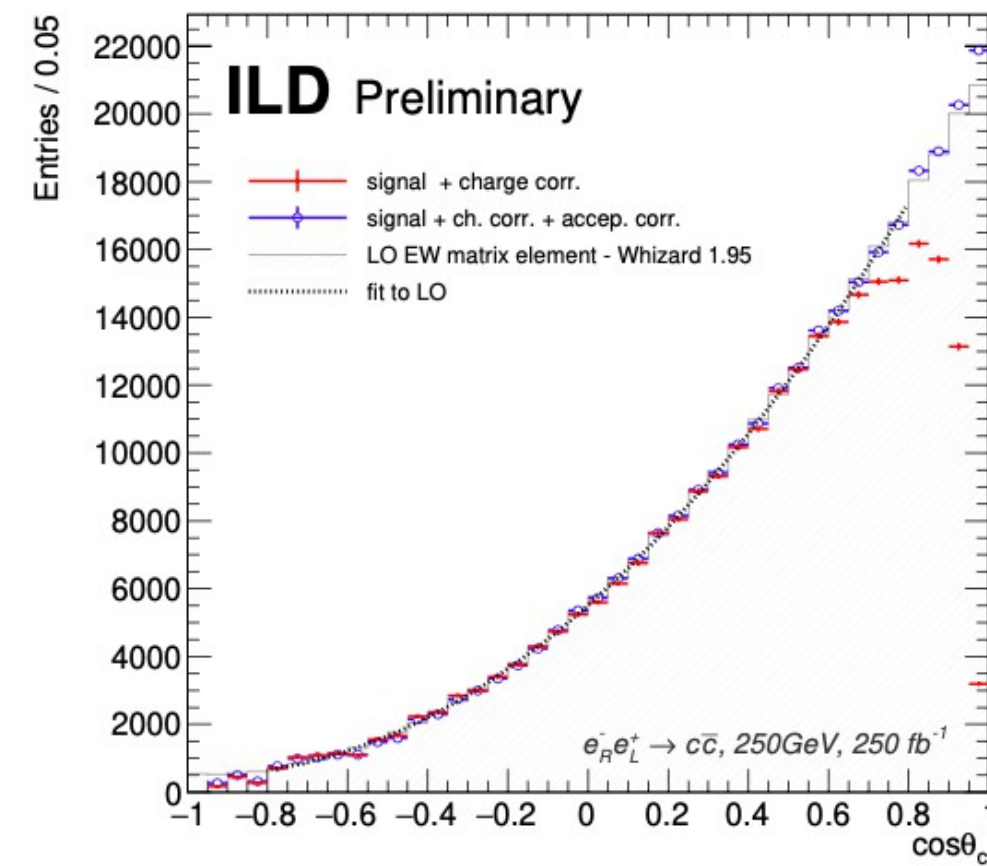
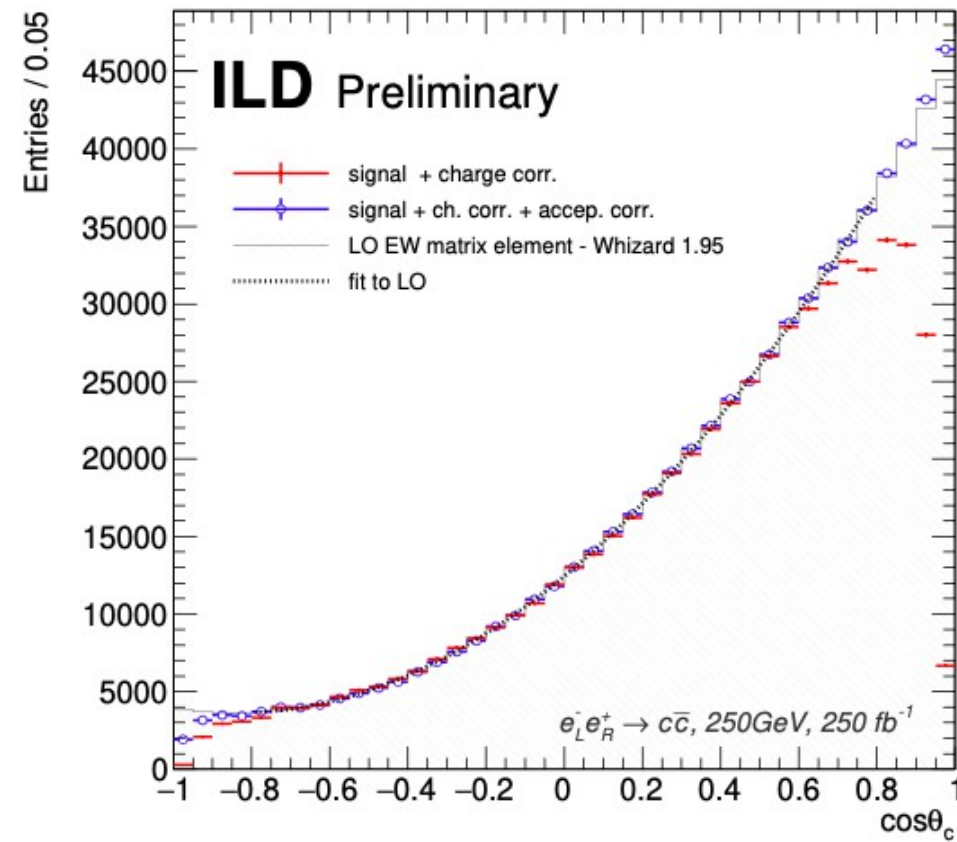
- High precision e+e- collider will give final word on anomaly

Randall Sundrum Models Djouadi/Richard '06

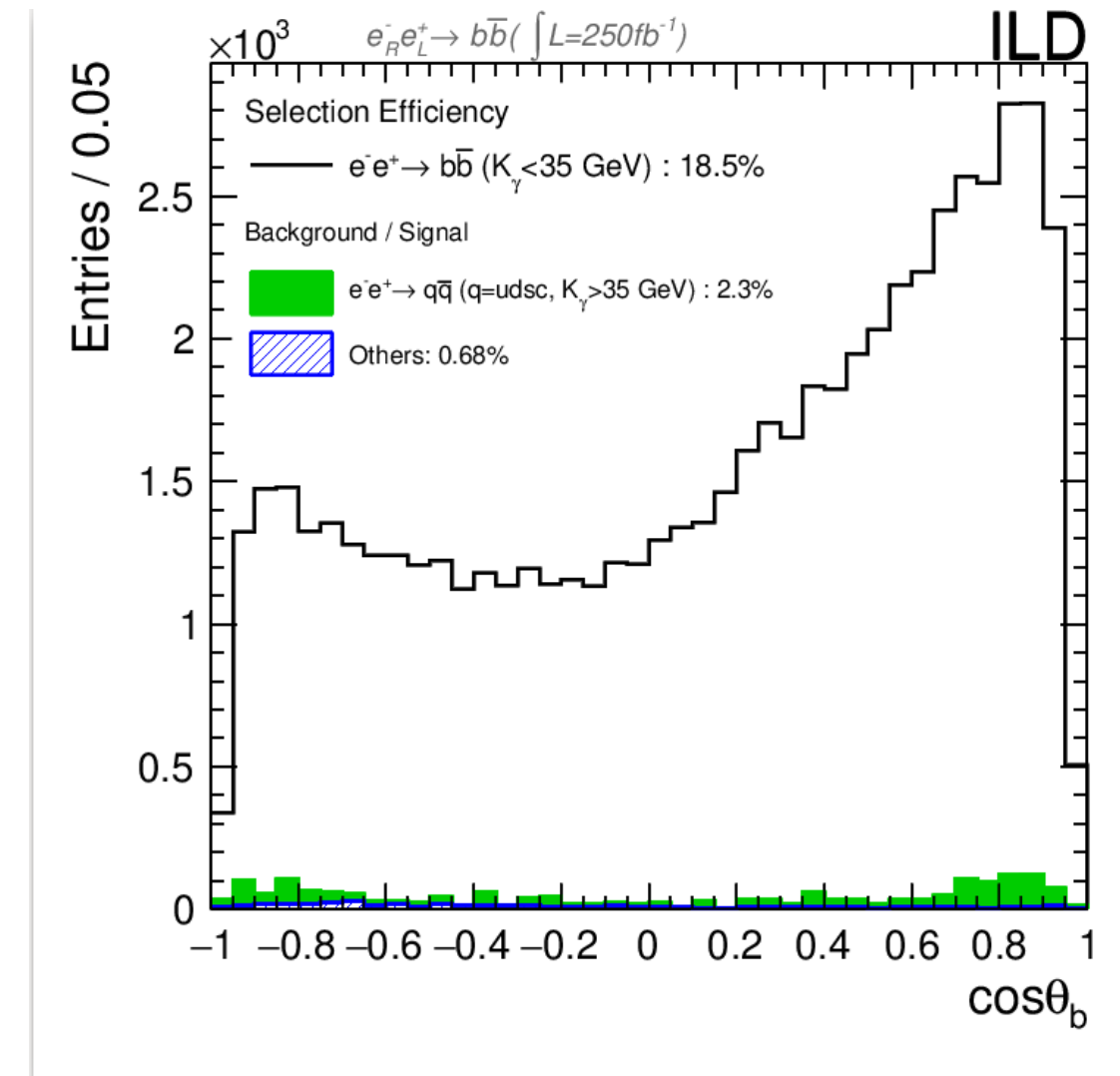
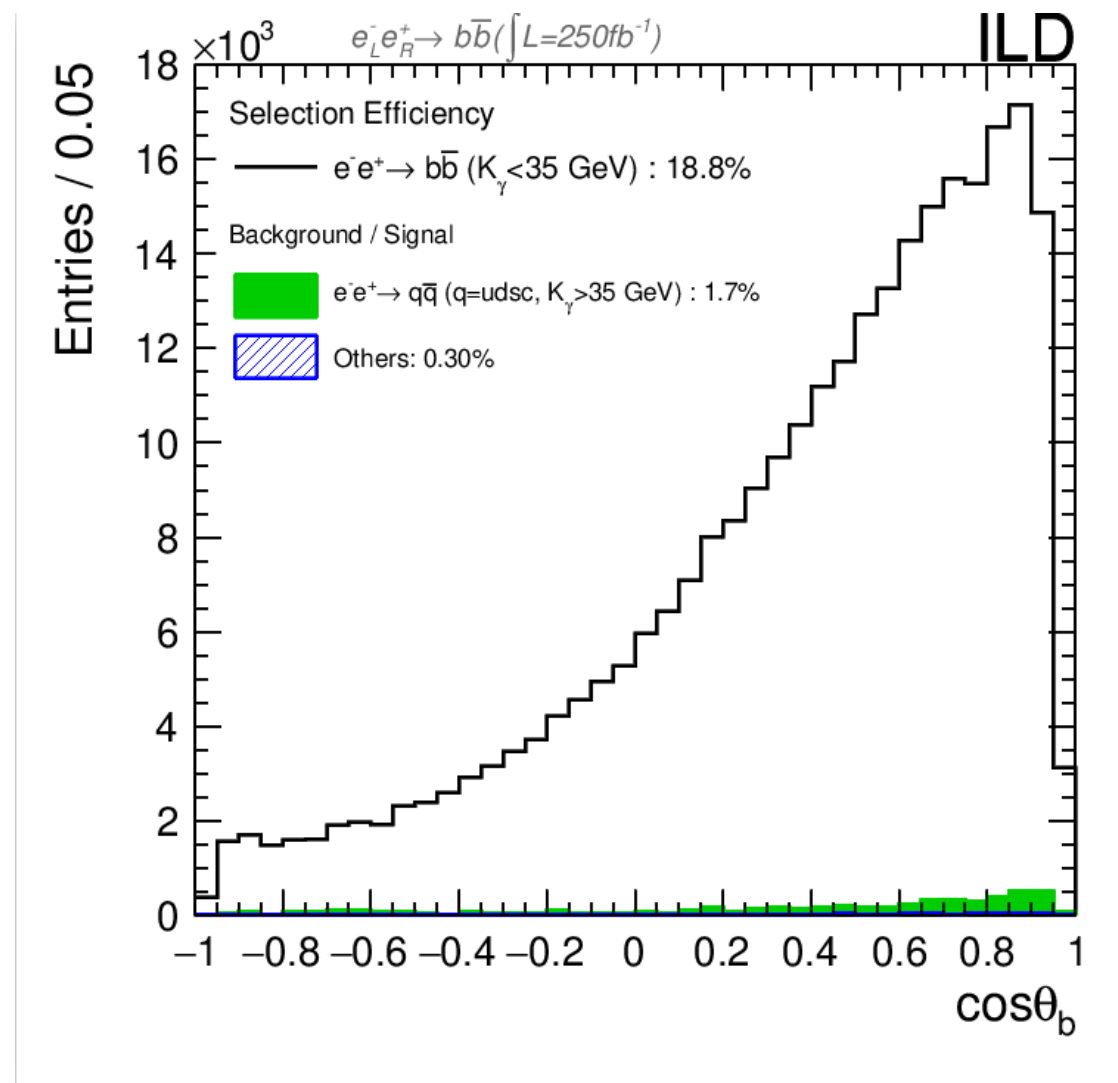
- In case it will persist polarised beams will allow for discrimination between effects on left and right handed couplings (Remember  $Zb_l b_l$  is protected by cross section)

- Note that also B-Factories report on anomalies LFC 22

arxiv:2002.05805



Full simulation study (with ILD concept)  
 Long lever arm in  $\cos \theta_c$  to extract form factors or couplings



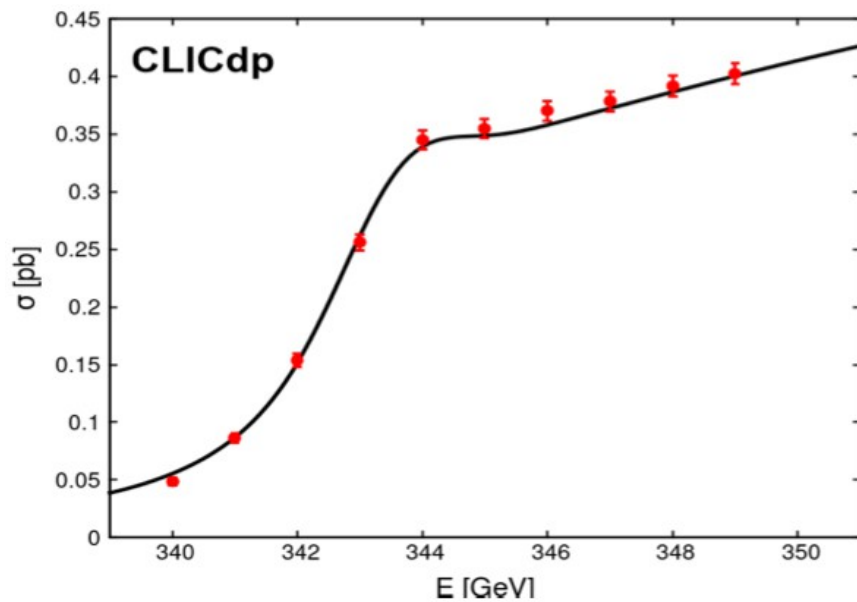
- Background levels can be kept at very small level
- However, these type of analyses seek per-mille level precision



Optimisation of threshold scan using “Non dominated sorting genetic algorithm”

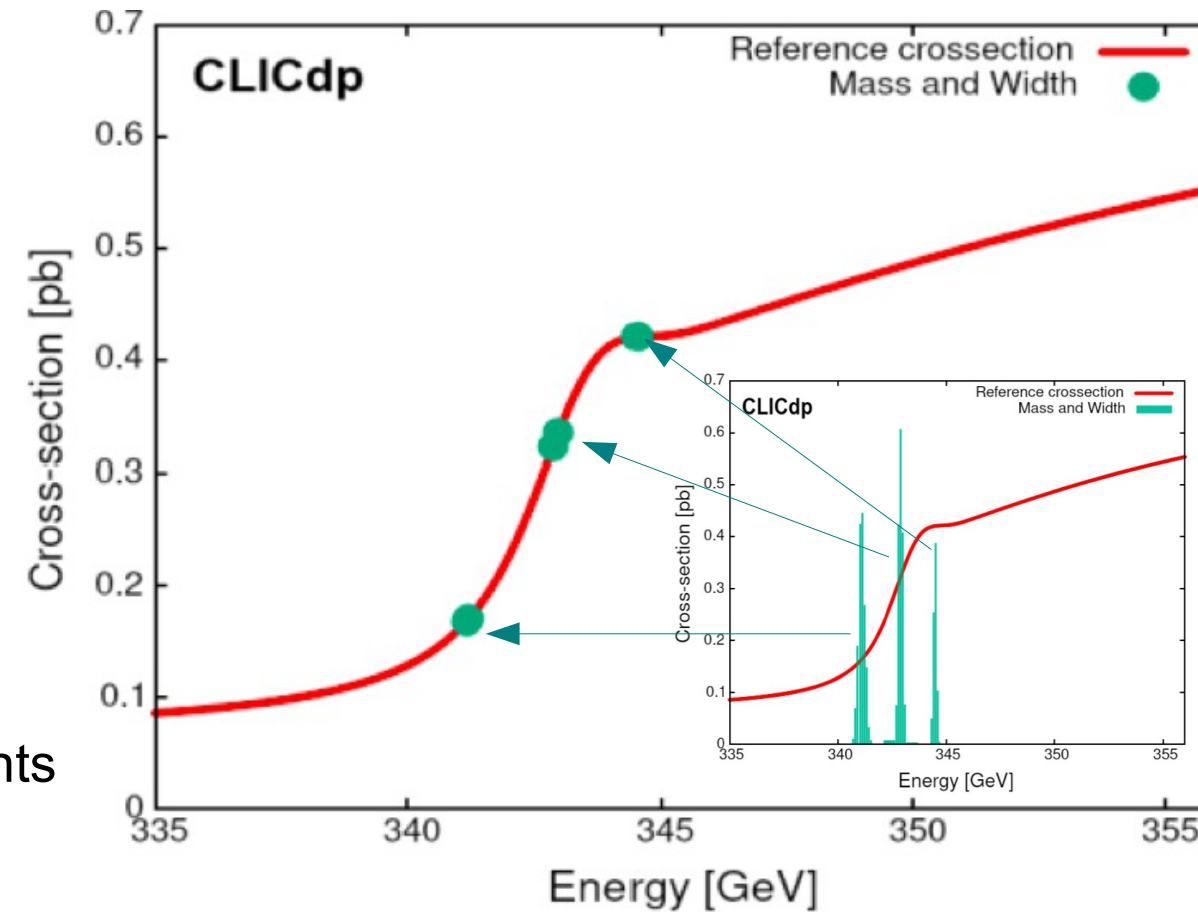
*arxiv: 2103.00522*

Standard scan scenario

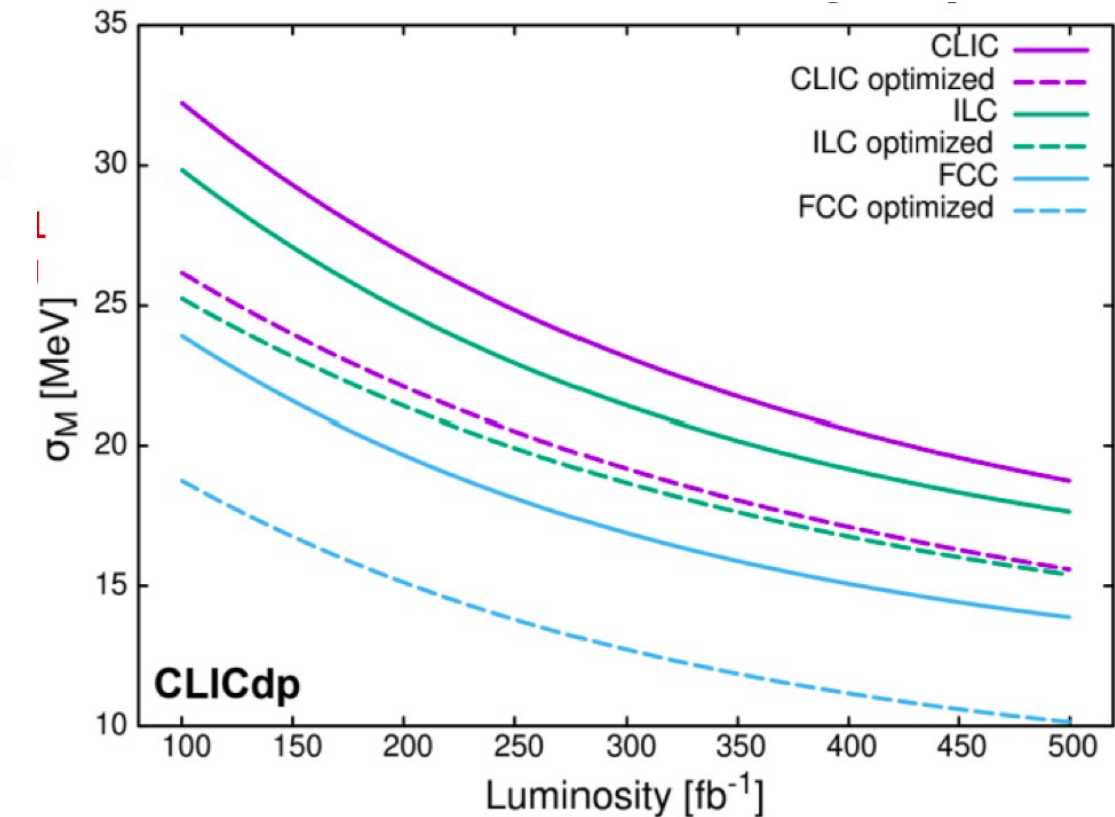


100 fb<sup>-1</sup> for 10 equally distributed points

Optimised scenario for mass a width



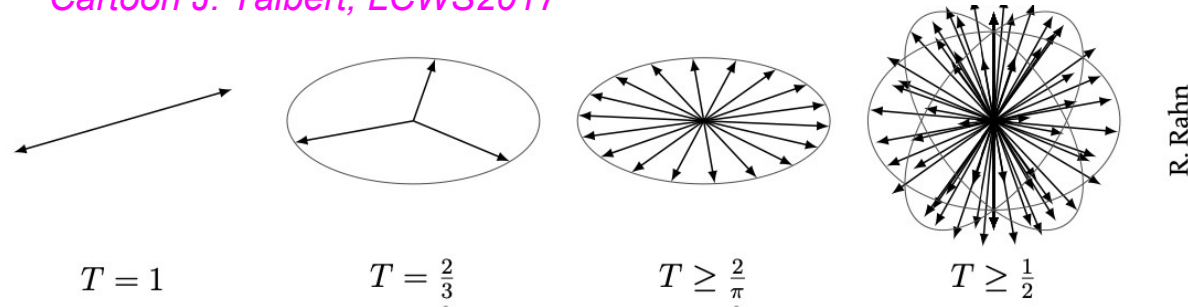
Precision on top mass ...



... taking luminosity spectrum into account

- Optimisation of threshold scan yield 25% statistical precision of top mass compared with scan using equally distributed scan points
  - Choice of measurement points with optimal sensitivity to desired quantity
- For breakdown of systematic errors see backup

Cartoon J. Talbert, LCWS2017



Here brief summary see upcoming ILC Snowmass White Paper for more details

Significant discrepancy between  $\alpha_s$  from lattice calculations (most precise) and QCD event shape variables

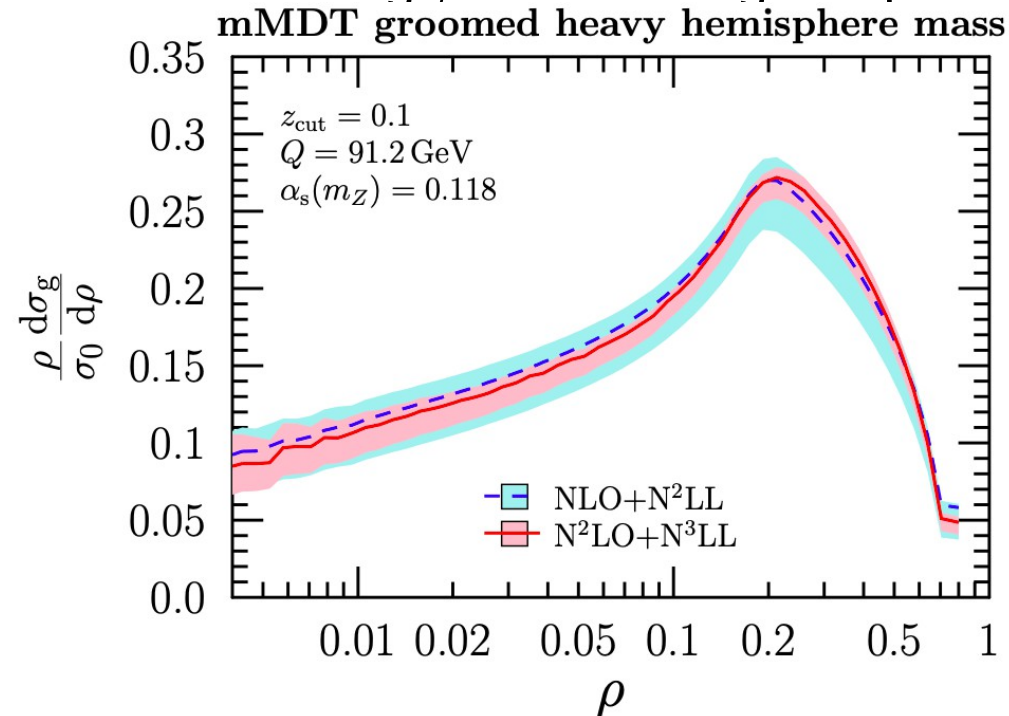
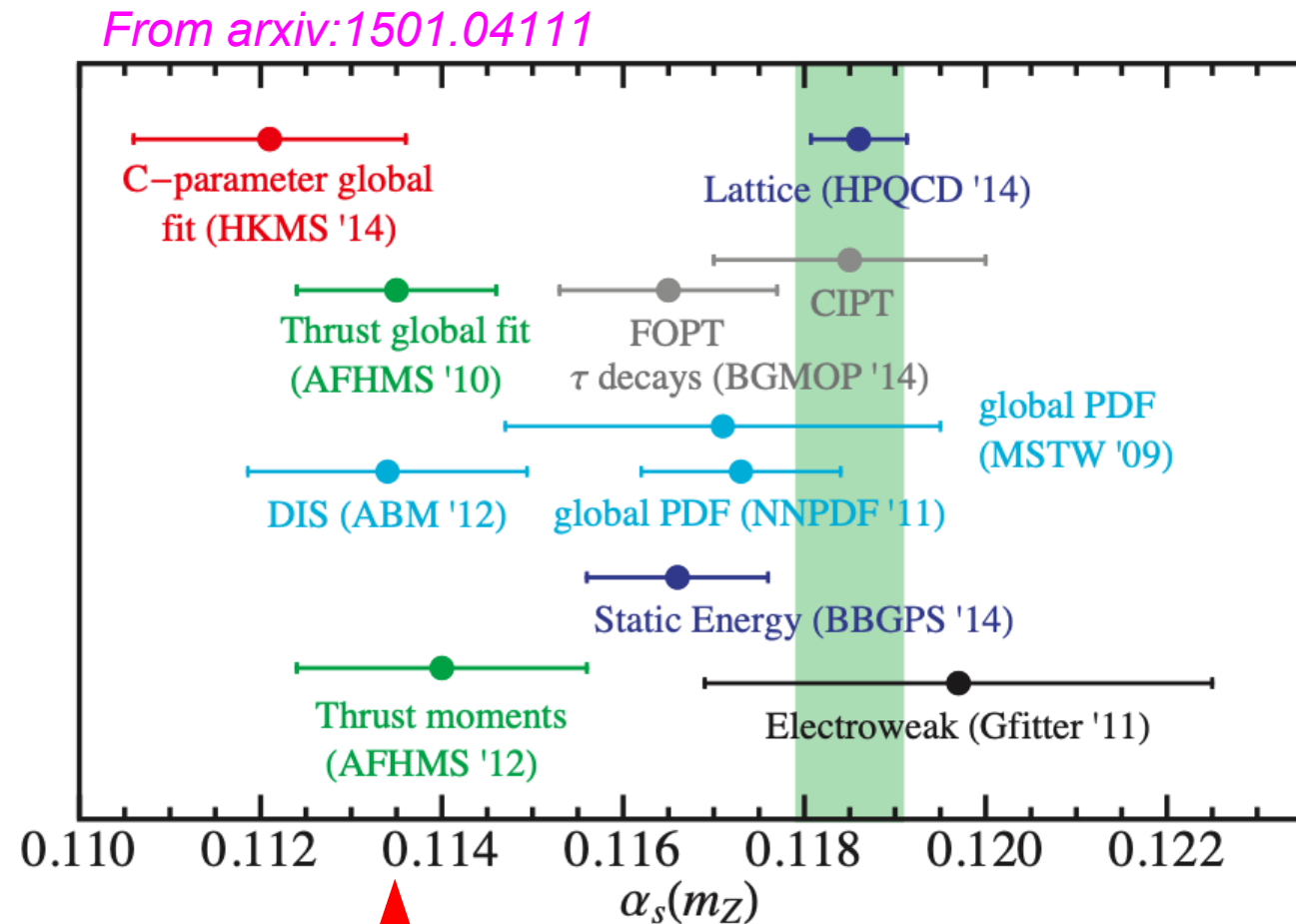
- Most “recent” e+e- input from LEP

Event shape variables are subject to non-perturbative effects

- “Power corrections” caused by soft radiation within a jet

How to take handle effects into account?

- Handling with Soft Collinear Effective Theories and/or
- “Jet Grooming”, i.e. removing soft parts from jet



Stable perturbative series after grooming  
Excellent premise for extracting  $\alpha_s$