

# Radiative Corrections from Medium to High Energy Experiments

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Thank YOU



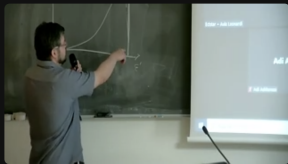
# Dinner



# A Global Workshop

- From Detroit to Tohoku - separated in time by 13 hours
- Covering  $ep$ ,  $\nu p$ ,  $\mu p$ ,  $e^+e^-$ ,  $\gamma\pi$ , and meson decays
- LO to NNLO, 10 MeV to 10 GeV, elastic to (PV)DIS, theory to experiment
- Some pseudo-randomly selected highlights

# Impromptu Classes



Ethan Cline

Mikhail Gorshteyn



Ectstar ~ Aula Leon...



Clément Legris (Toh...

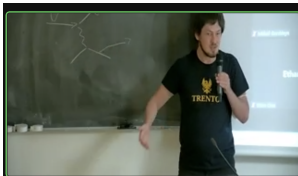


Adi Ashkenazi



vgplekhanov@gmail...

# Impromptu Classes



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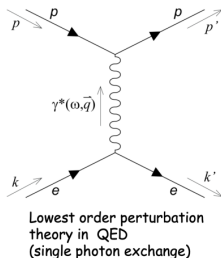


Clément Legris (Tohoku Uni...



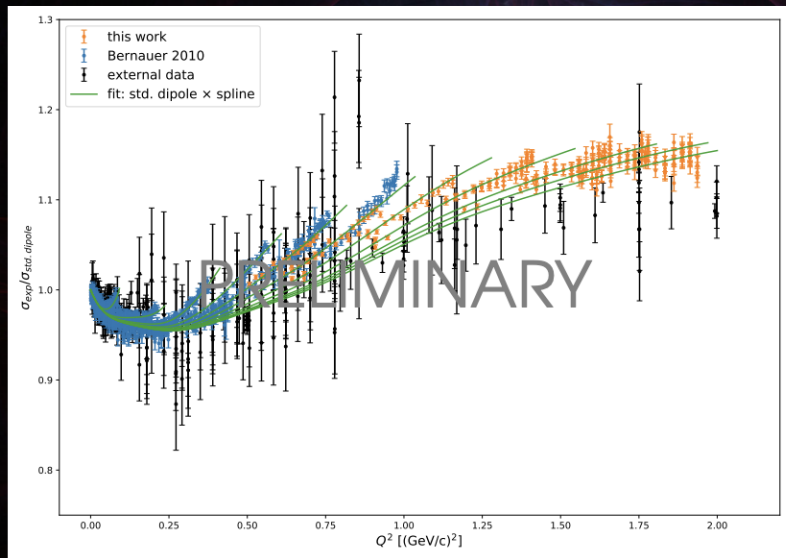
## Background 1

- I grew up in pion scattering, etc., then moved to electromagnetic scattering as a postdoc
- I learned that electron scattering was well understood, with some small, well-understood, “radiative correction” hardly worth discussing



## Results from our speakers - Bernauer

Mainz large  $Q^2$  ff (PhD. thesis Julian Mueller)





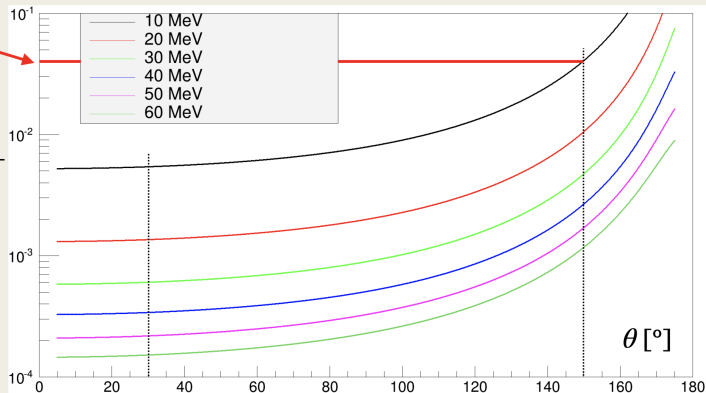
# Results from our speakers - Legris

## Electron mass

Up to 4 % at 10 MeV!

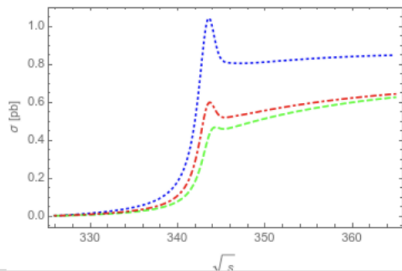
$$\frac{\left| \left( \frac{d\sigma}{d\Omega} \right)_{real} - \left( \frac{d\sigma}{d\Omega} \right)_{URL} \right|}{\left( \frac{d\sigma}{d\Omega} \right)_{real}}$$

(with PWBA and  
standard-dipole  
form factors)



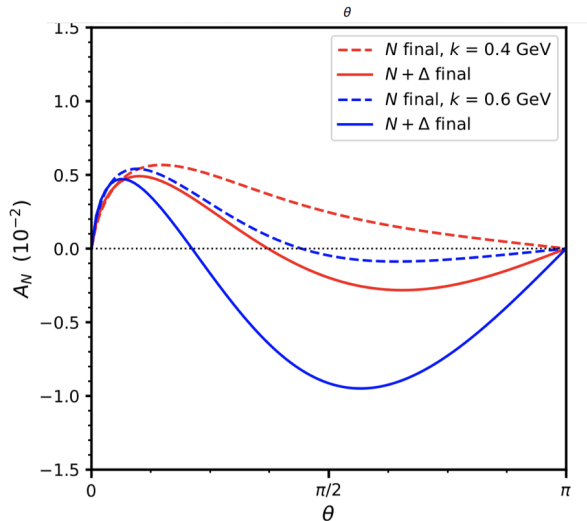
## Conclusions

- We calculated the ISR corrections to the process  $e^+e^- \rightarrow \gamma^*/Z^*$  up to  $O(\alpha^6 L^5)$ .
- This includes the first (up to) three logarithmic terms at lower orders.
- We calculated the leading logarithmic ISR corrections to the forward-backward asymmetry up to  $O(\alpha^6 L^6)$ .
- The corrections can become important at future  $e^+e^-$  machines running at high luminosities.
- The radiators can be used for various processes like  $e^+e^- \rightarrow t\bar{t}$  and  $e^+e^- \rightarrow ZH$ .



blue:  $O(\alpha^0)$ , obtained with QQbarThreshold  
[Beneke, Kiyo, Maier, Piclum (Comp. Phys. Com. (2009))];  
green:  $O(\alpha^1)$ ; red:  $O(\alpha^2)$

## Results from our speakers - Goity

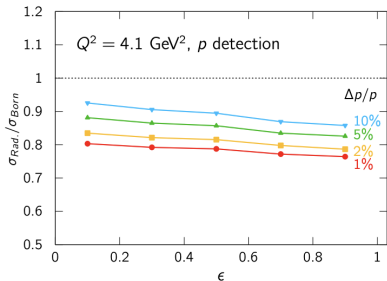


Goity, Weiss, Willemyns arXiv:2207.07588

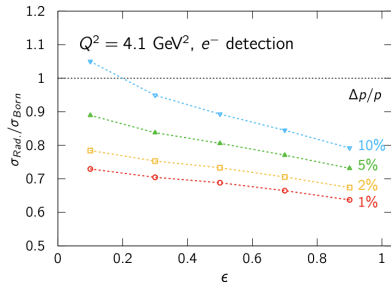
transverse target SSA- approach based on the  $1/N_c$  expansion

# Results from our speakers - Schmidt

$\epsilon$ -dependence of the radiative correction



$\epsilon$ -dependence of the radiative correction



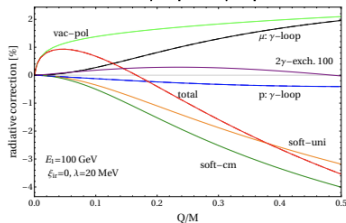
“Finally, radiative corrections (mainly electron bremsstrahlung) . . . have smaller  $\epsilon$ -dependence when the proton is detected.”

“Credit to A. Afanasev for already solving this back in 2001 (and thank you for sending me the paper!).”

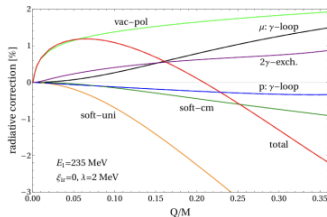
# Results from our speakers - Kaiser

## Pattern of radiative corrections for AMBER and MUSE

- Individual radiative corrections to  $\mu^- p \rightarrow \mu^- p$  including proton structure



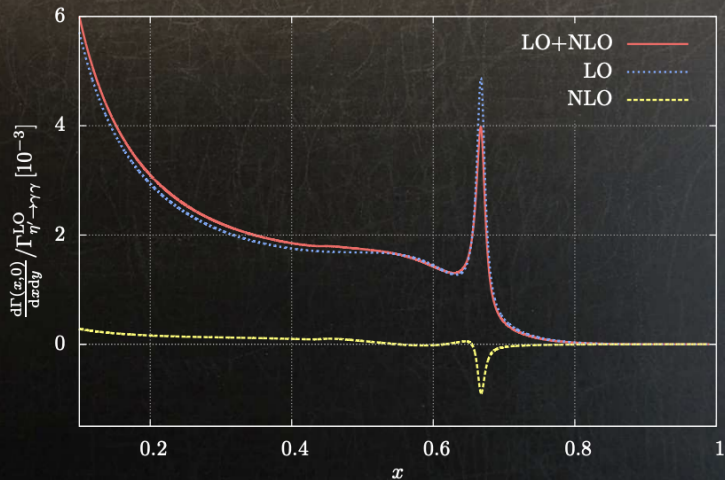
- Photon-loop around proton and  $2\gamma$ -exchange are suppressed
- Major role played by vacuum polarization and soft photon radiation
- Requires calculation of (hard) bremsstrahlung incl. detector acceptance



# Results from our speakers - Husek

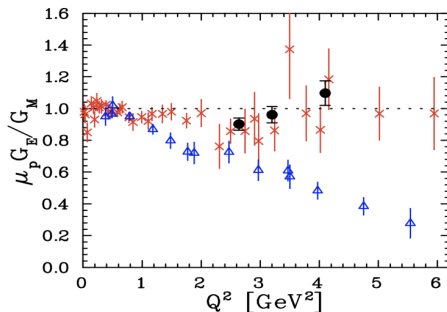
Radiative corrections for  $\eta' \rightarrow e^+e^-\gamma$  decays

The two-fold differential decay width  $d\Gamma(x,0)$  at NLO

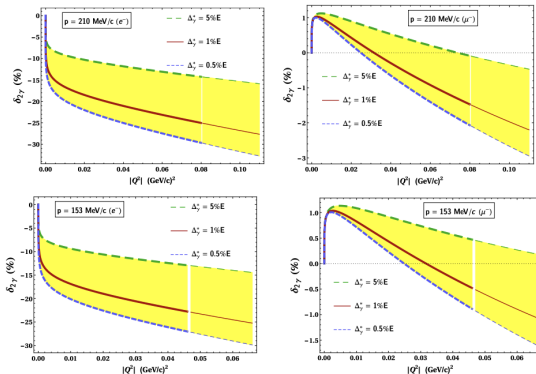


## Discrepancy Reconfirmed

- (Skipping a little forward in time...) I. Qattan et al., PRL 94 (2005) 142301  
Rosenbluth separation measuring recoil protons rather than scattered electrons



# Results from our speakers - Myrher



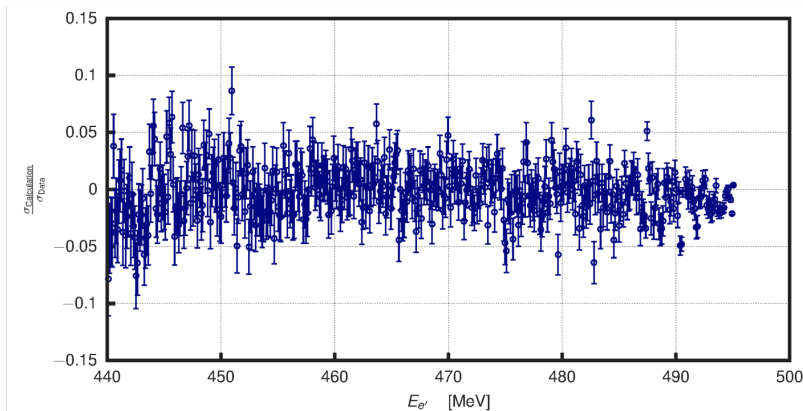
The lower limit of the photon energy detection  $\sim \Delta_{\gamma}^*$ .

Results are found in the soft photon approximation.

The (yellow) bands are the variation of the *lab*-frame detector resolution when  $0.5\% < \Delta_{\gamma}^* < 5\%$  of the incident lepton energy  $E$ .



## Experimental study of external corrections



- **The experiment confirmed the theoretical predictions.**
- The external radiative and collisional corrections impact the shape of the radiative tail.

## SIDIS event generator on radiative corrections

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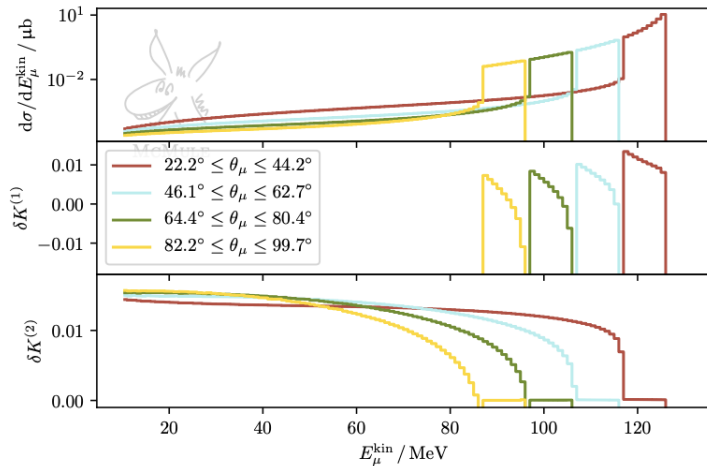
A Monte Carlo event generator created by Duane Byer from Duke University, based on the SIDIS RC paper: <https://github.com/duanebyer/sidis>

- ➔ Generates events for SIDIS six-fold cross sections computation
- ➔ All eighteen SIDIS structure functions implemented in Gaussian and Wandzura-Wilczek type approximations: S. Bastami et. al., JHEP06, 007 (2019)
- ➔ More fine tuning on the generator should be done for running it in the SoLID experiment's framework, including the neutron target
- ➔ In the meantime, the generator can be used for other experiments from medium to high energies, which also measure the SIDIS processes (CIAS12, COMPASS, etc.)

# Results from our speakers - Ulrich

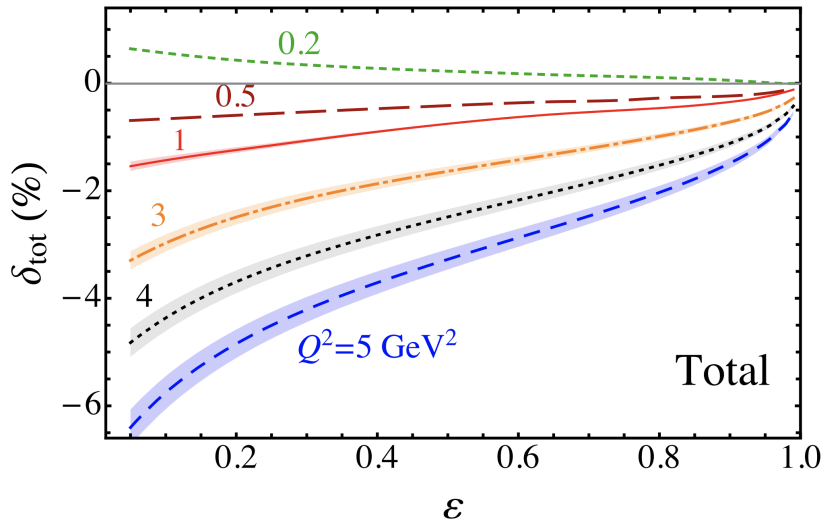
$$p_{\mu}^{\text{in}} = 210 \text{ MeV}, 20^{\circ} < \theta_{\mu} < 100^{\circ}$$

mall mule-tools.gitlab.io/user-library/l-p-scattering/muse-legacy



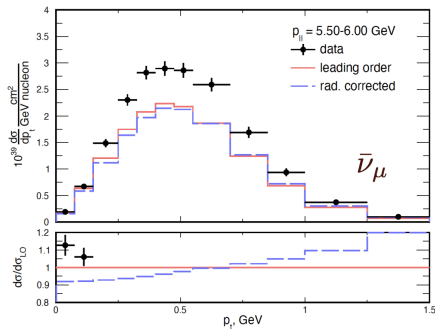
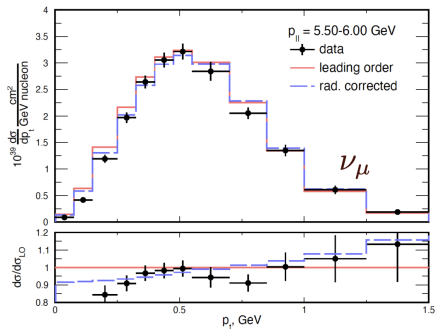
## Results from our speakers - Blunden

### TPE corrections to cross section (CLAS resonances)



## Comparison to data

- medium-energy flux data from MINERvA@FERMILAB



## Lessons Learned

- Experimentalists must make it clear what corrections were applied!
- Theorists should provide equations experimentalists can understand (ratios and asymmetries are nice)!
- There are many excellent calculations, generators, and experiments out there!
- Radiative corrections are *important* for nuclear physics

# Thoughts During the Workshop(revisited)

- Should we write a whitepaper?
  - NSAC charged the American DOE and NSF with recommending a new Long Range Plan by October 2023
  - EIC is on the distant horizon

# Future Work

- Write something up on this workshop
  - At a minimum a list of relevant generators should be compiled and posted
  - Conveners for each subject?
  - Mailing list?
  - arXiv or journal?
- A database of cross sections would be very useful, along with details of radiative corrections that were applied
  - Give user ability to apply some prescription with minimal overhead
- Write a universal translator to interface generators and simulations
- Future workshop? ECT\* or CFNS?



fin.

THANK **YOU!**