

11–15 July, 2022

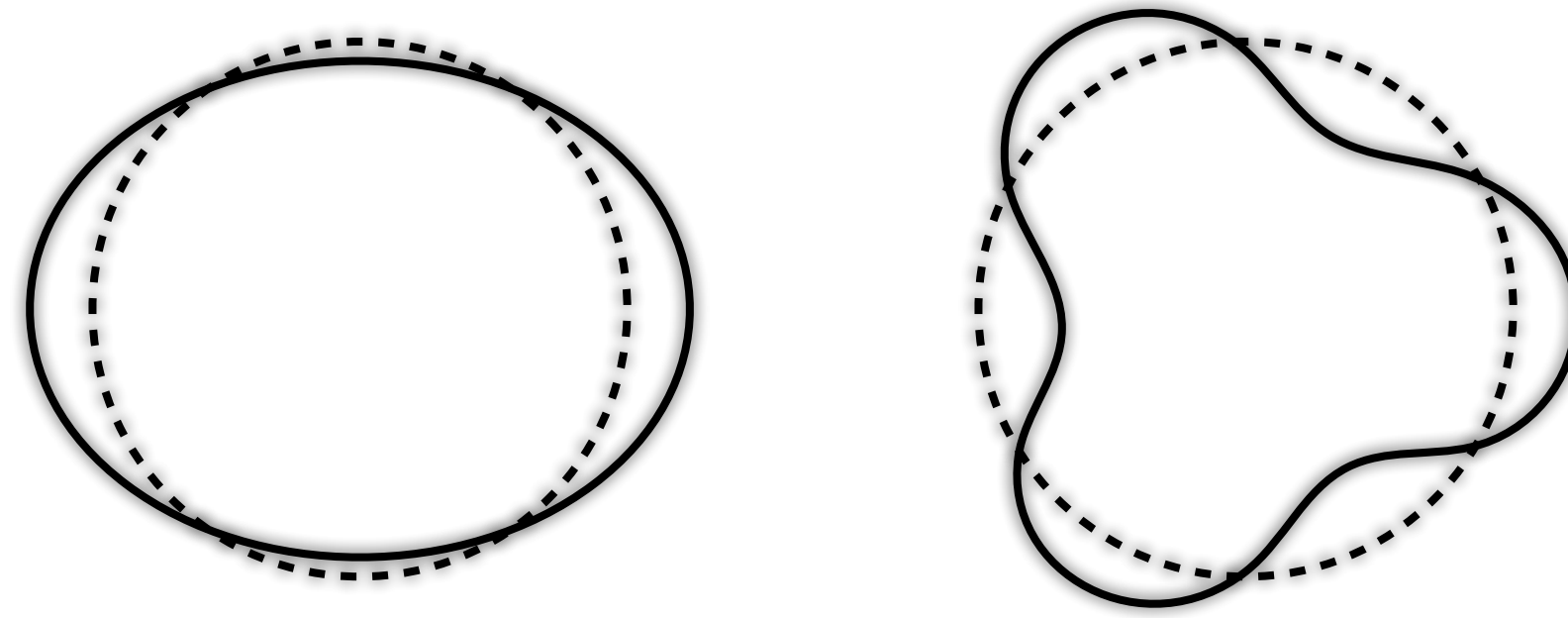
Skyrme-QRPA for monopole modes of excitation

A role of nuclear deformation

K. Yoshida (Kyoto U.)

Giant resonances: collective modes of surface vibration

classical and intuitive picture



$L=2$: Giant Quadrupole Resonance (GQR)

$L=3$: High Energy Octupole Resonance (HEOR)

strongly excited by a one-body operator, exhaust a sum-rule value

$$\hat{O} = \sum_{\sigma\sigma'} \sum_{\tau\tau'} \int_{\text{space}} \vec{r} r^L Y_L(\hat{r}) \hat{\psi}^\dagger(\vec{r}\sigma\tau) \langle \sigma | \left\{ \begin{matrix} 1 \\ \vec{\sigma} \end{matrix} \right\} | \sigma' \rangle \langle \tau | \left\{ \begin{matrix} 1 \\ \vec{\tau} \end{matrix} \right\} | \tau' \rangle \hat{\psi}(\vec{r}\sigma'\tau')$$

rich variety of modes depending on ΔL , ΔS , ΔT , and ΔN .

affected by many-body correlations (deformation and superfluidity)

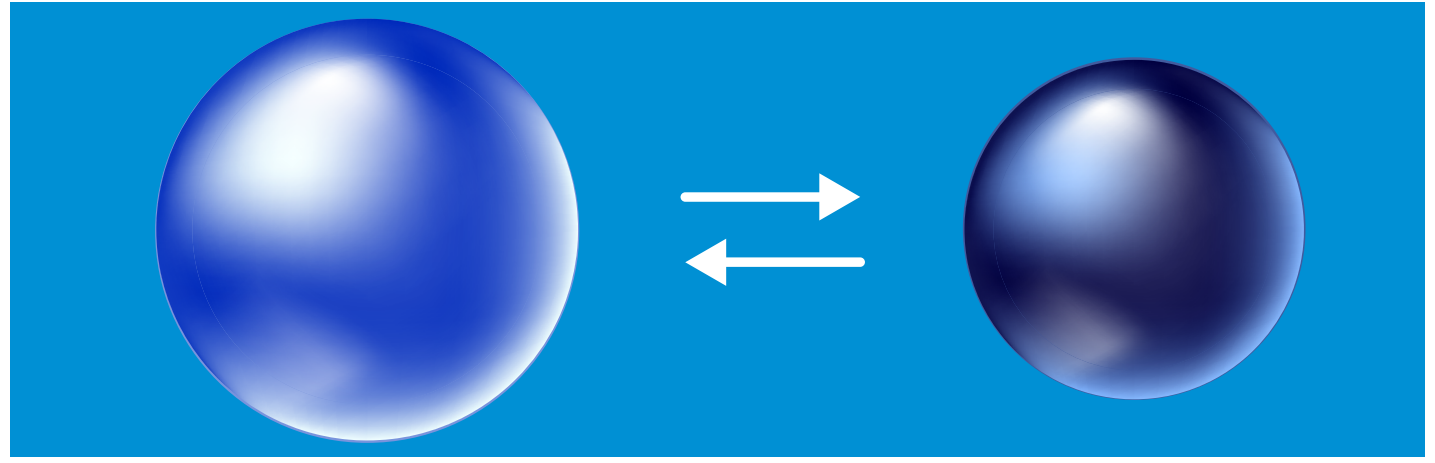
Giant Monopole Resonance (GMR)

$$\hat{O} = \sum_{\sigma\tau} \int d\vec{r} r^2 \psi^\dagger(\vec{r}\sigma\tau) \psi(\vec{r}\sigma\tau)$$

volume change \longleftrightarrow

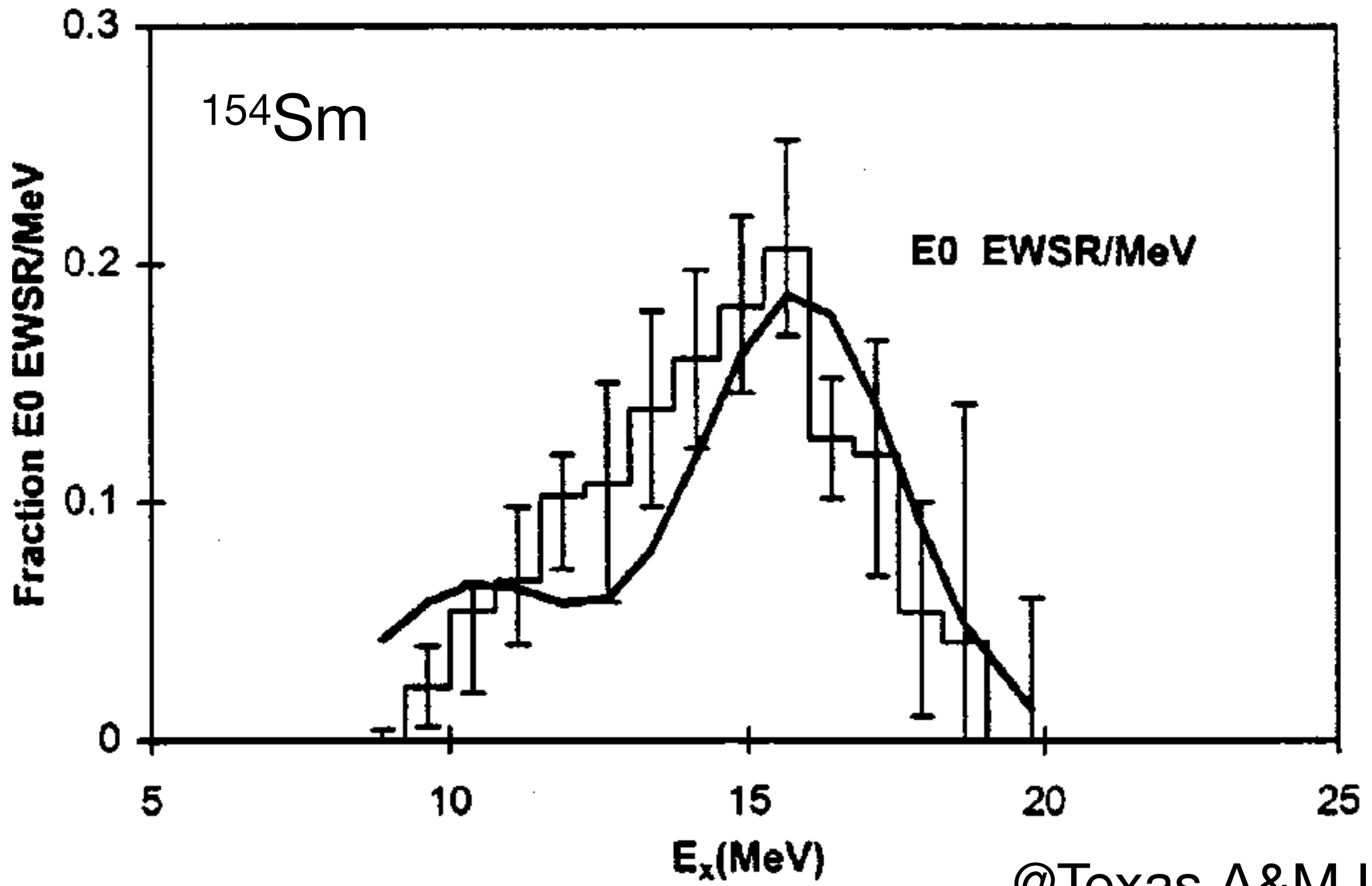
incompressibility of nuclear matter

Blaizot ('80)



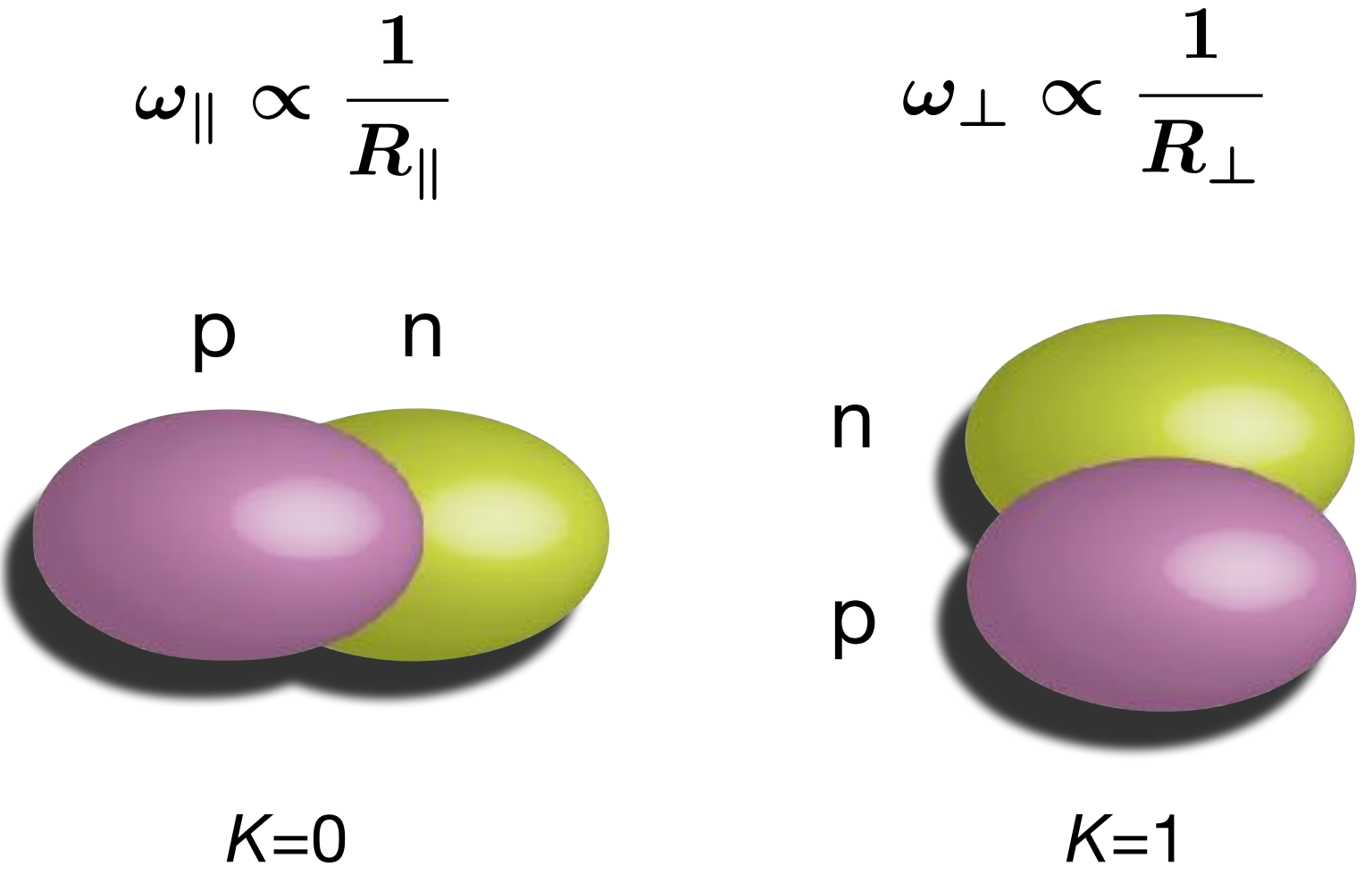
deformation splitting?

Garg+ ('80)
Youngblood+ ('99)

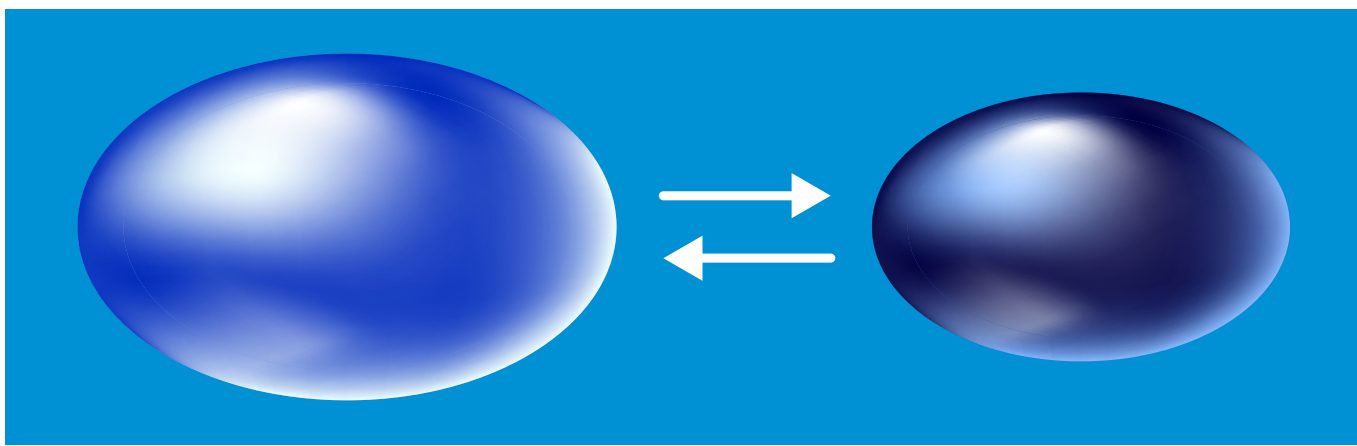


Deformation splitting?

IVGDR

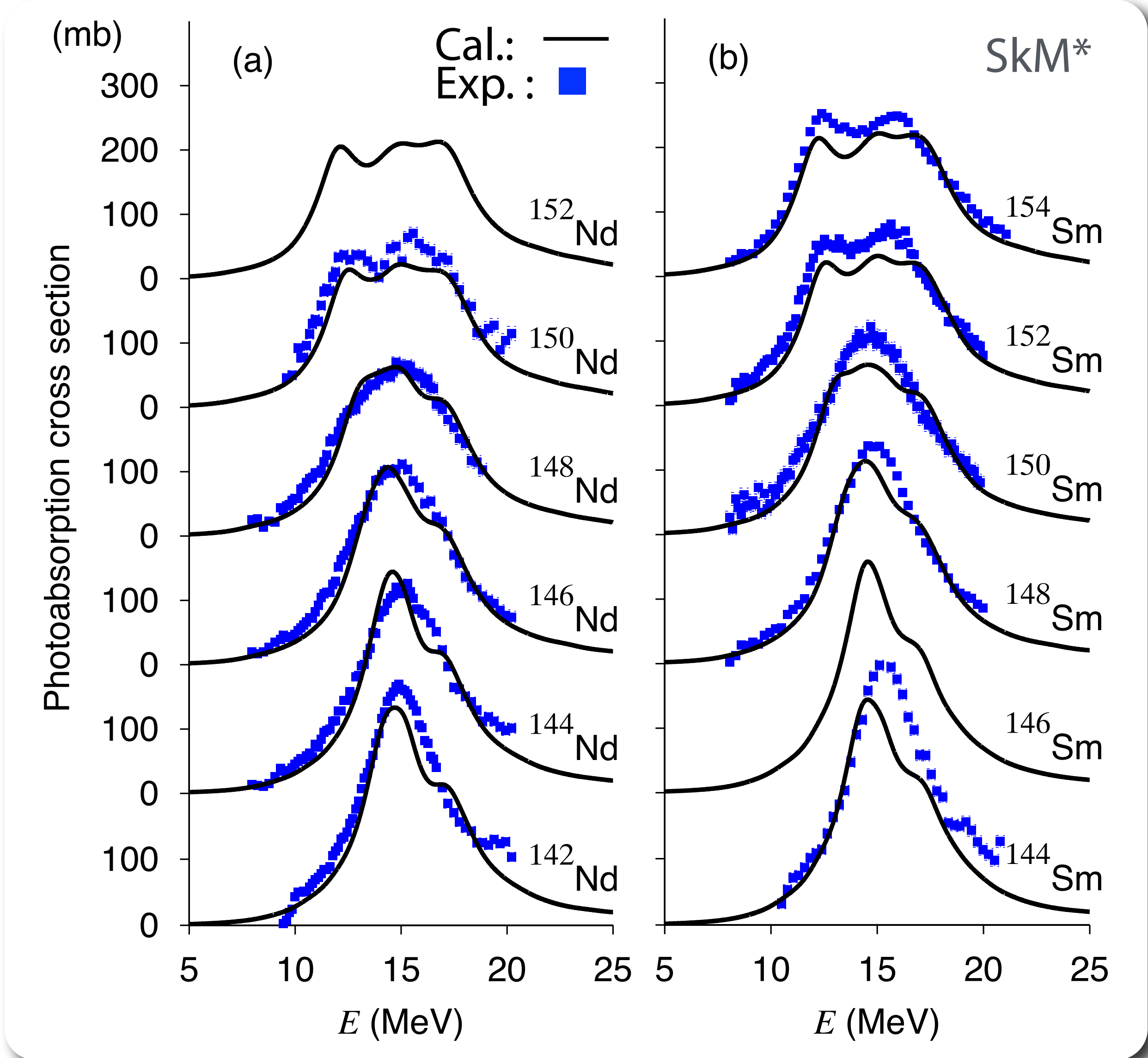


GMR



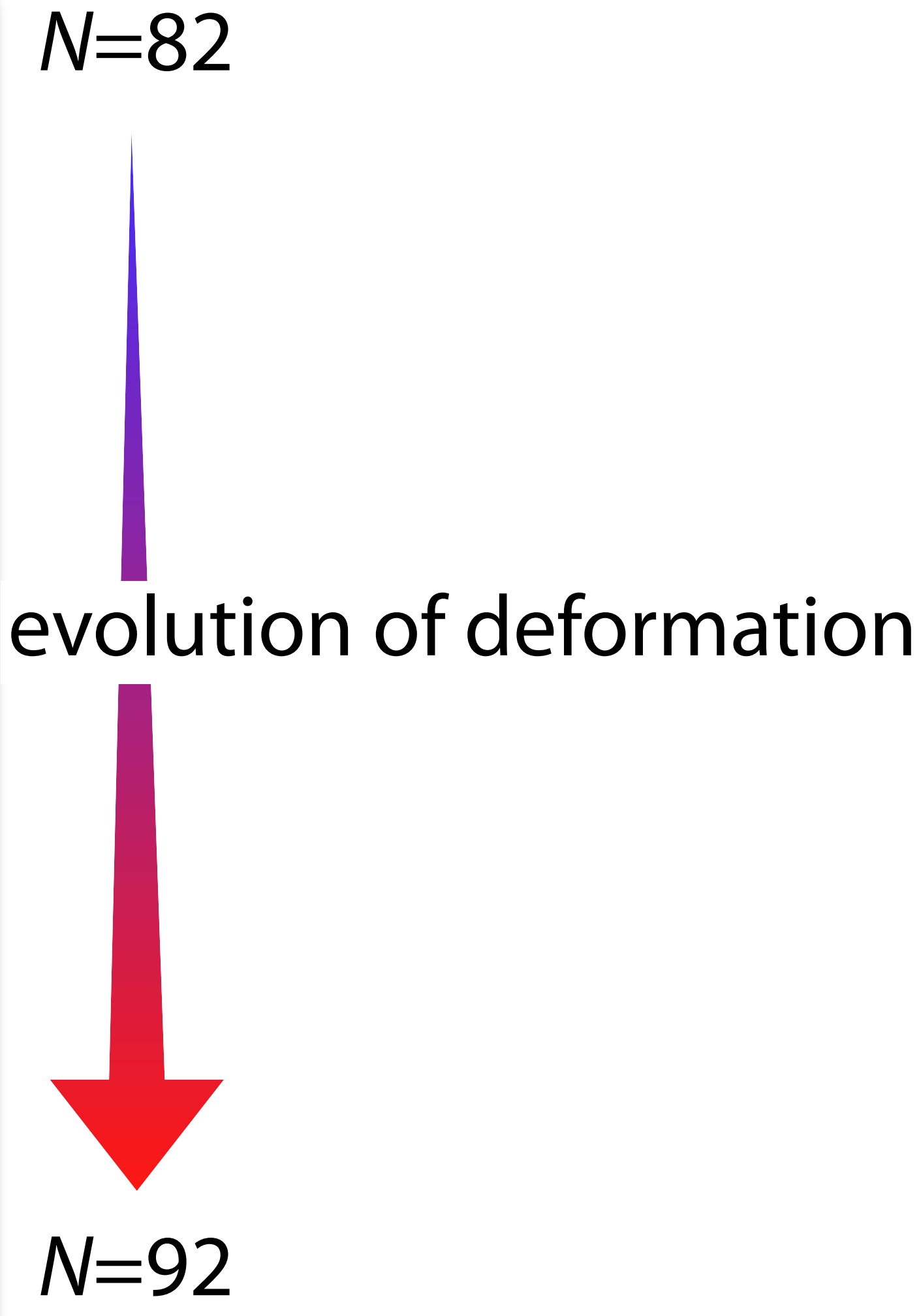
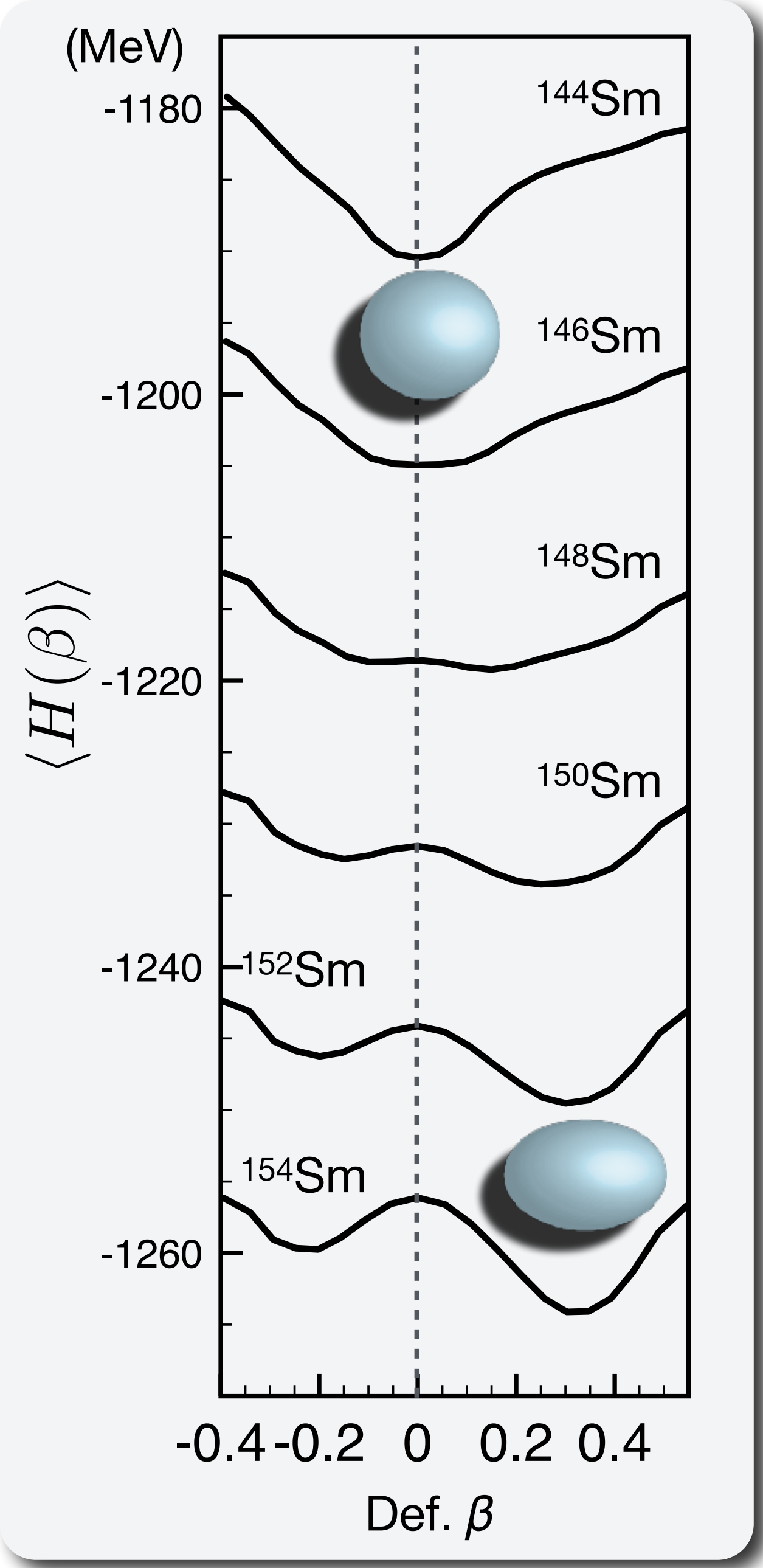
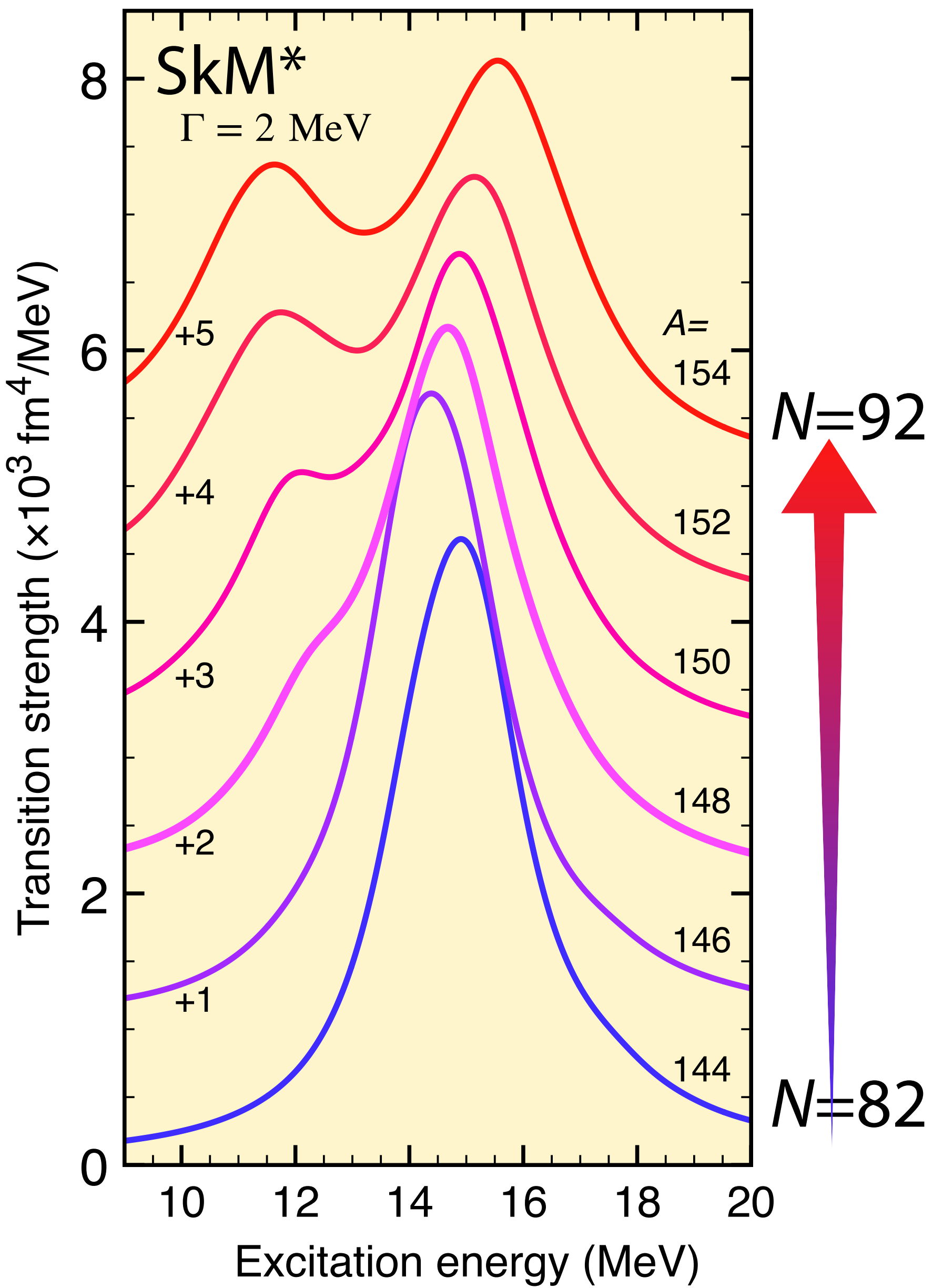
no angle dependence contrary to GDR
 $Y_0(\hat{r})$ $Y_{1K}(\hat{r})$

Yoshida–Nakatsukasa ('11)



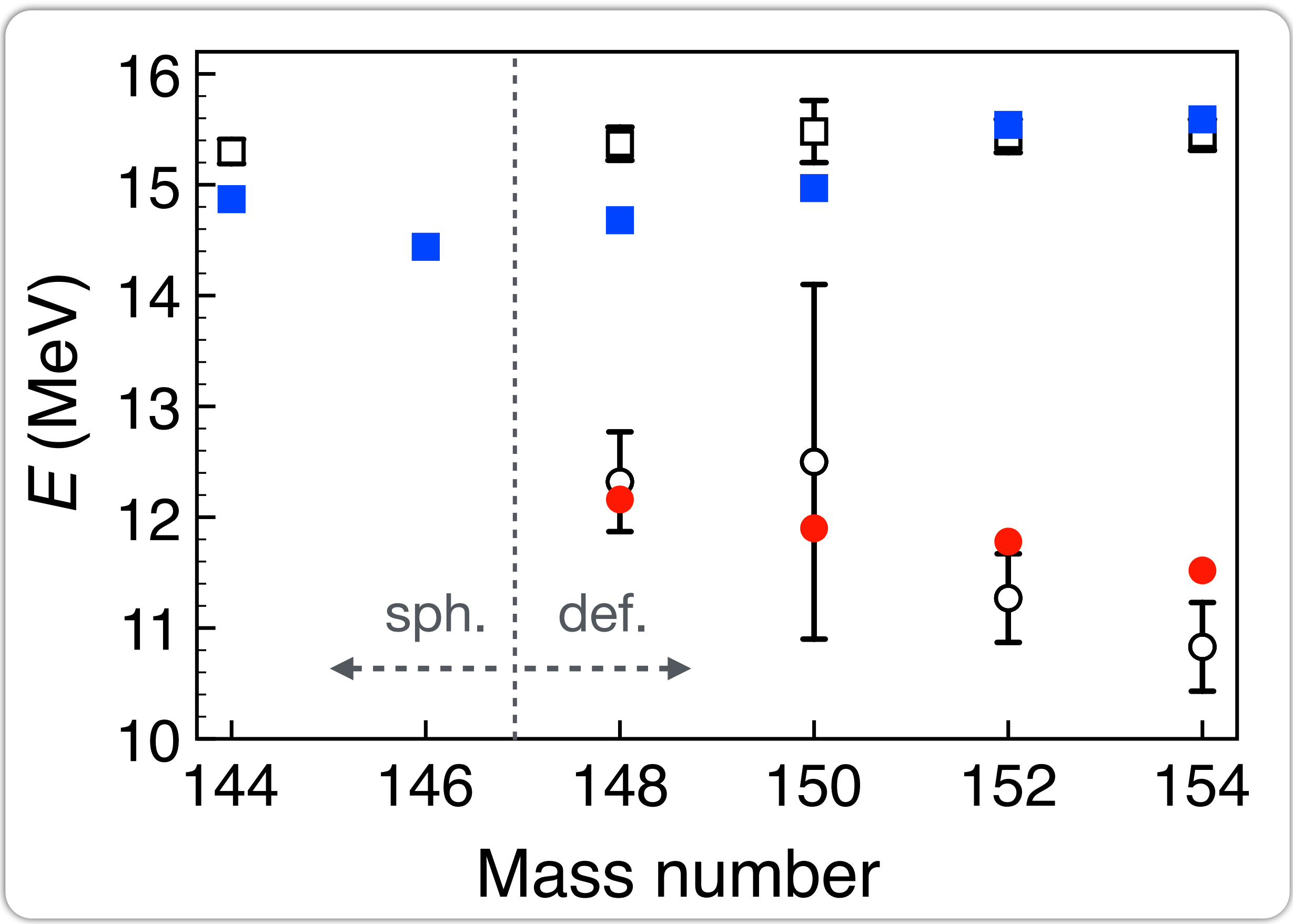
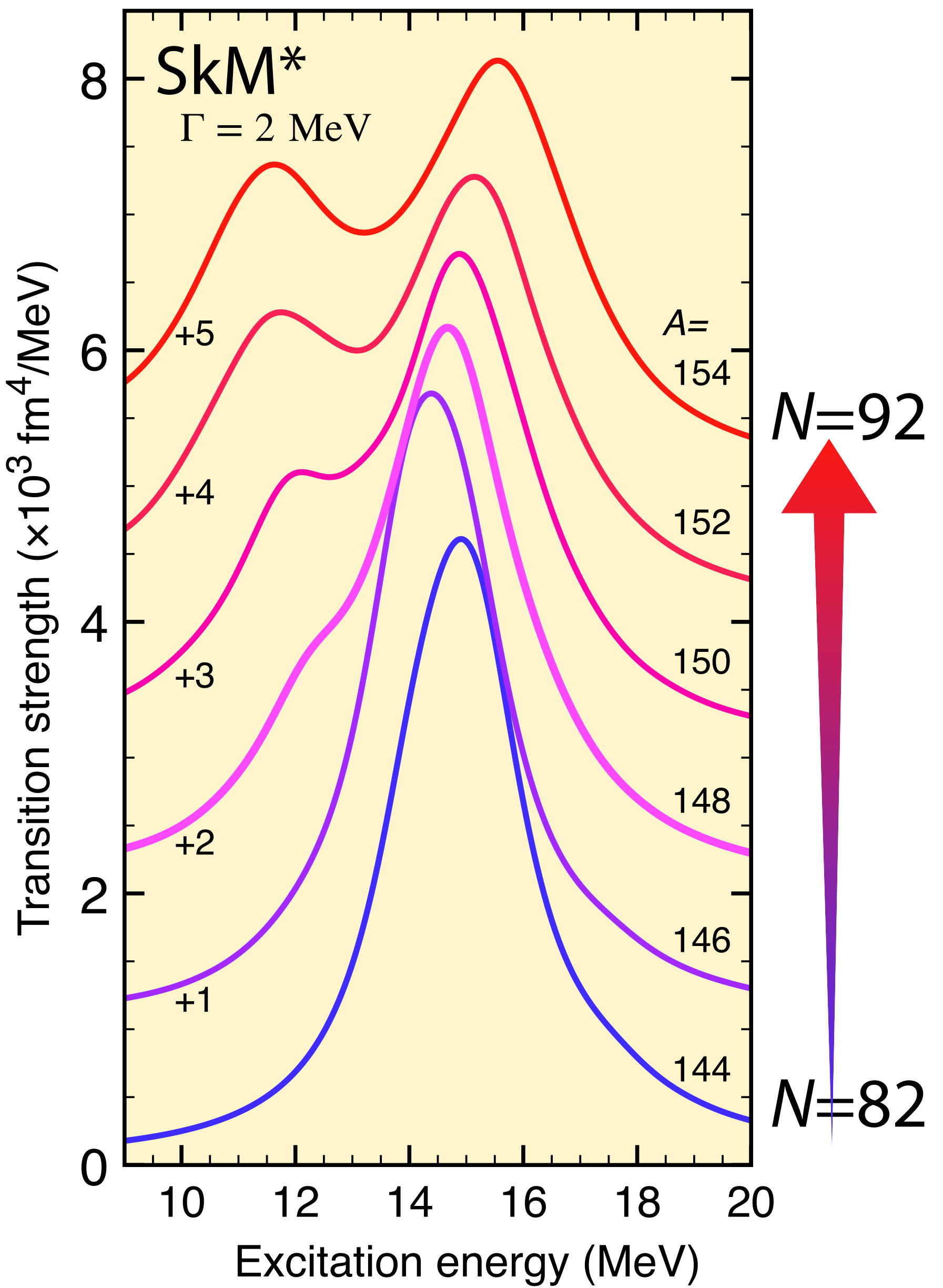
GMR in the Sm isotopes

Yoshida–Nakatsukasa ('13)



GMR in the Sm isotopes

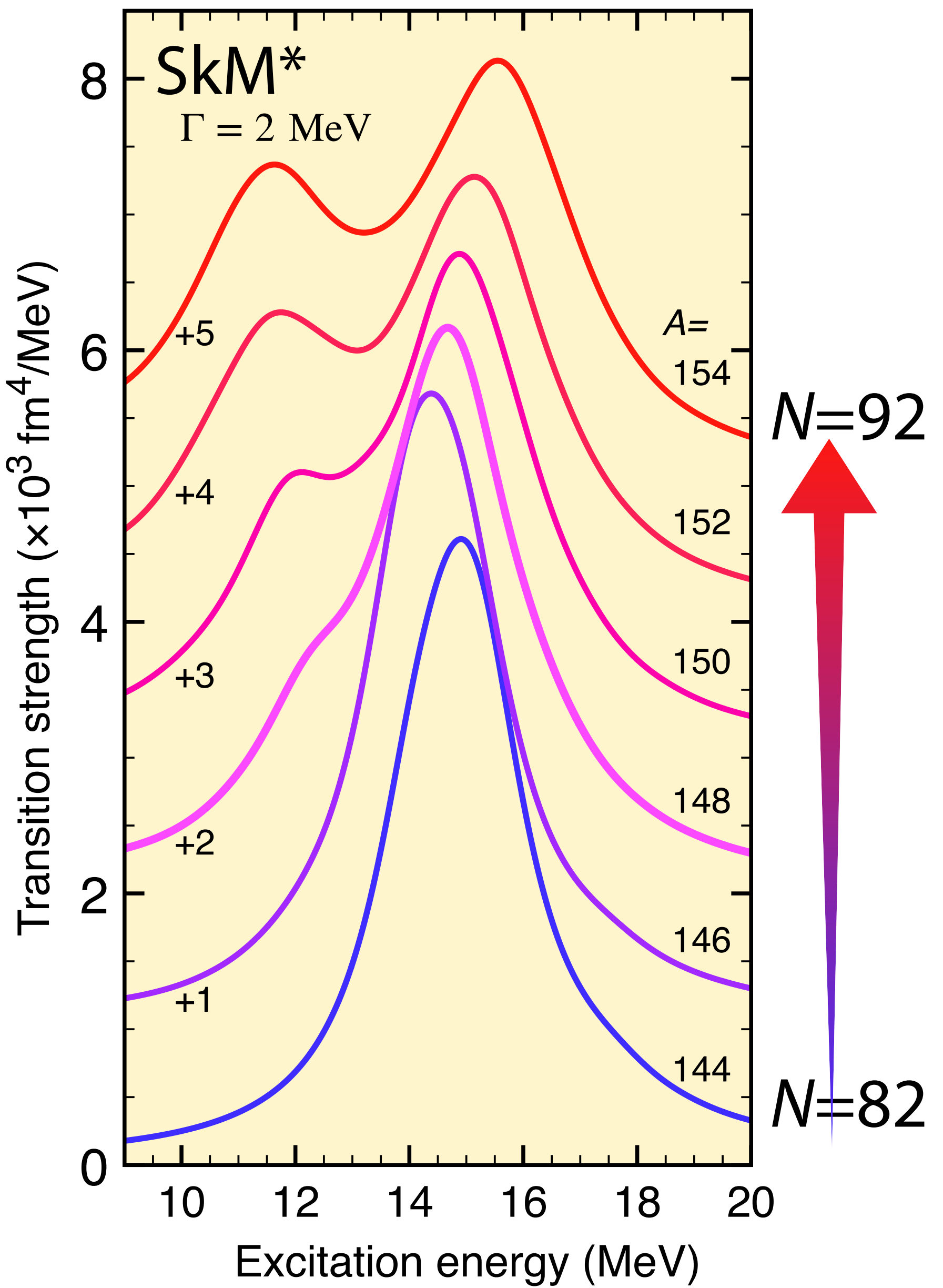
Yoshida–Nakatsukasa ('13)



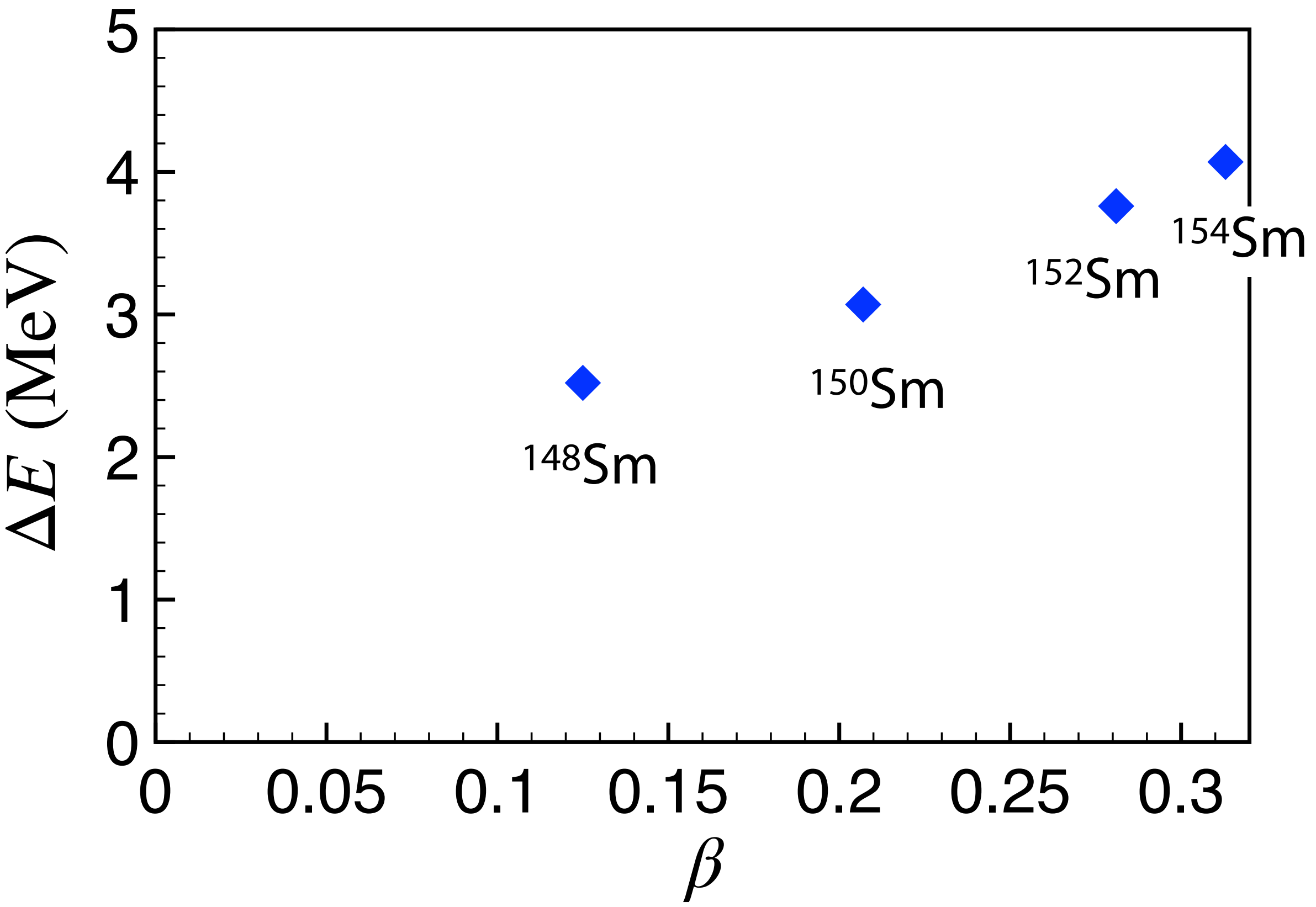
Exp.: Itoh+ ('03)

GMR in the Sm isotopes

Yoshida–Nakatsukasa ('13)

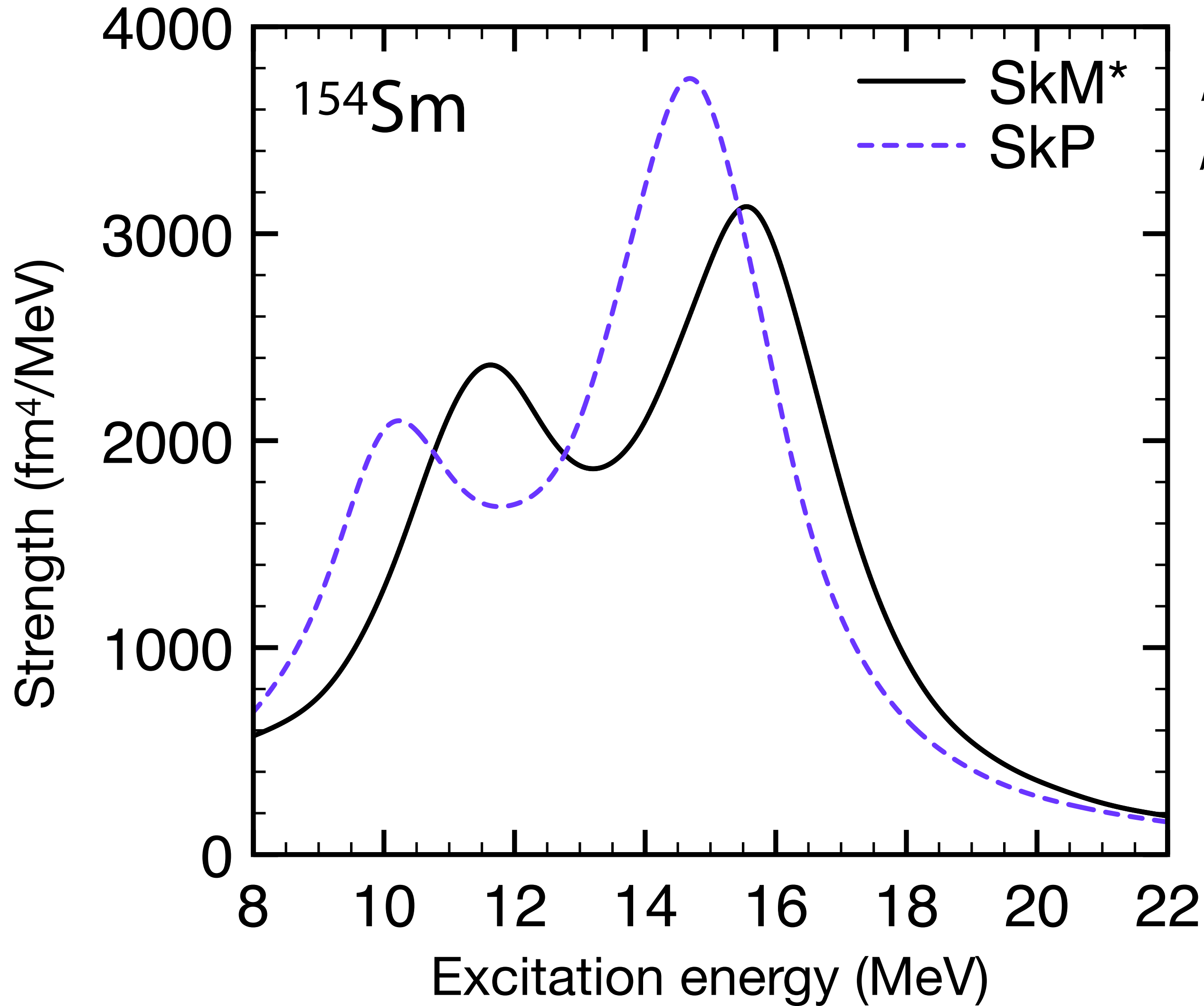


deformation splitting



GMR in the Sm isotopes

Yoshida–Nakatsukasa ('13)



$\beta = 0.31$

$\beta = 0.29$

Ratio of EWS
higher/lower

1.9

3.2

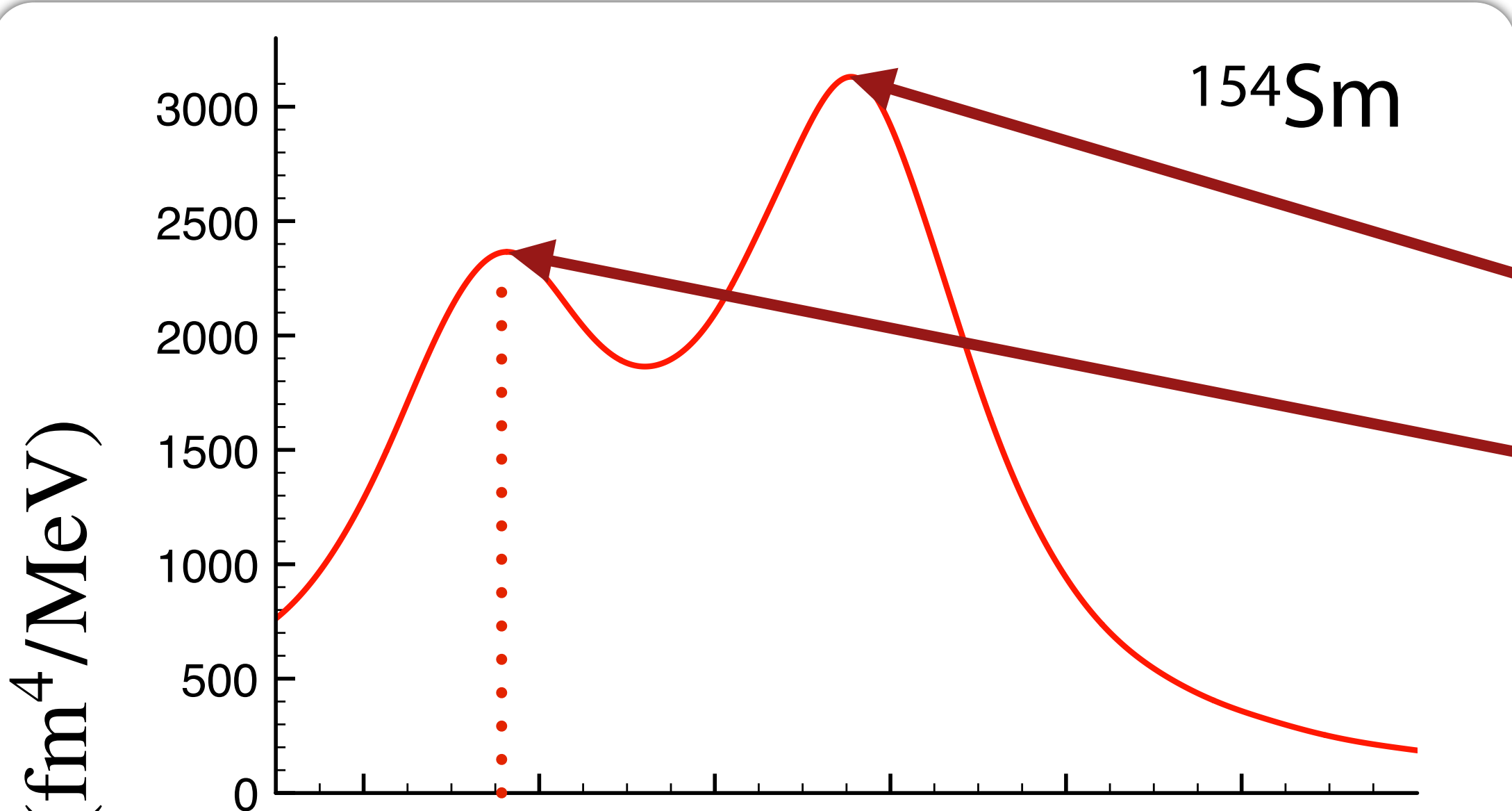
larger strengths in the lower peak
in a strongly-deformed nucleus

stronger coupling between GMR and GQR
as deformation increases

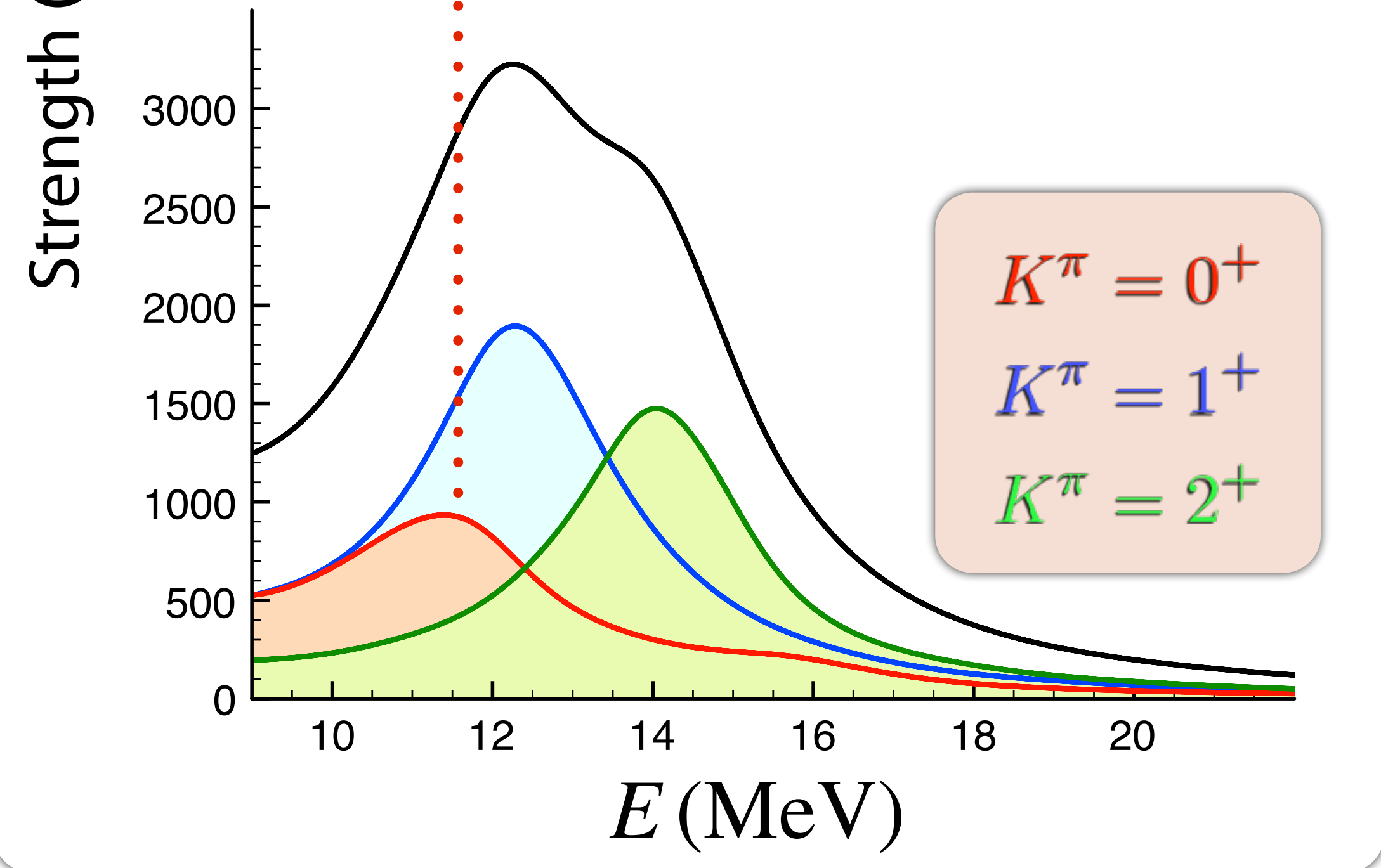
splitting energy
ratio of strengths

Coupling between GMR and GQR

monopole

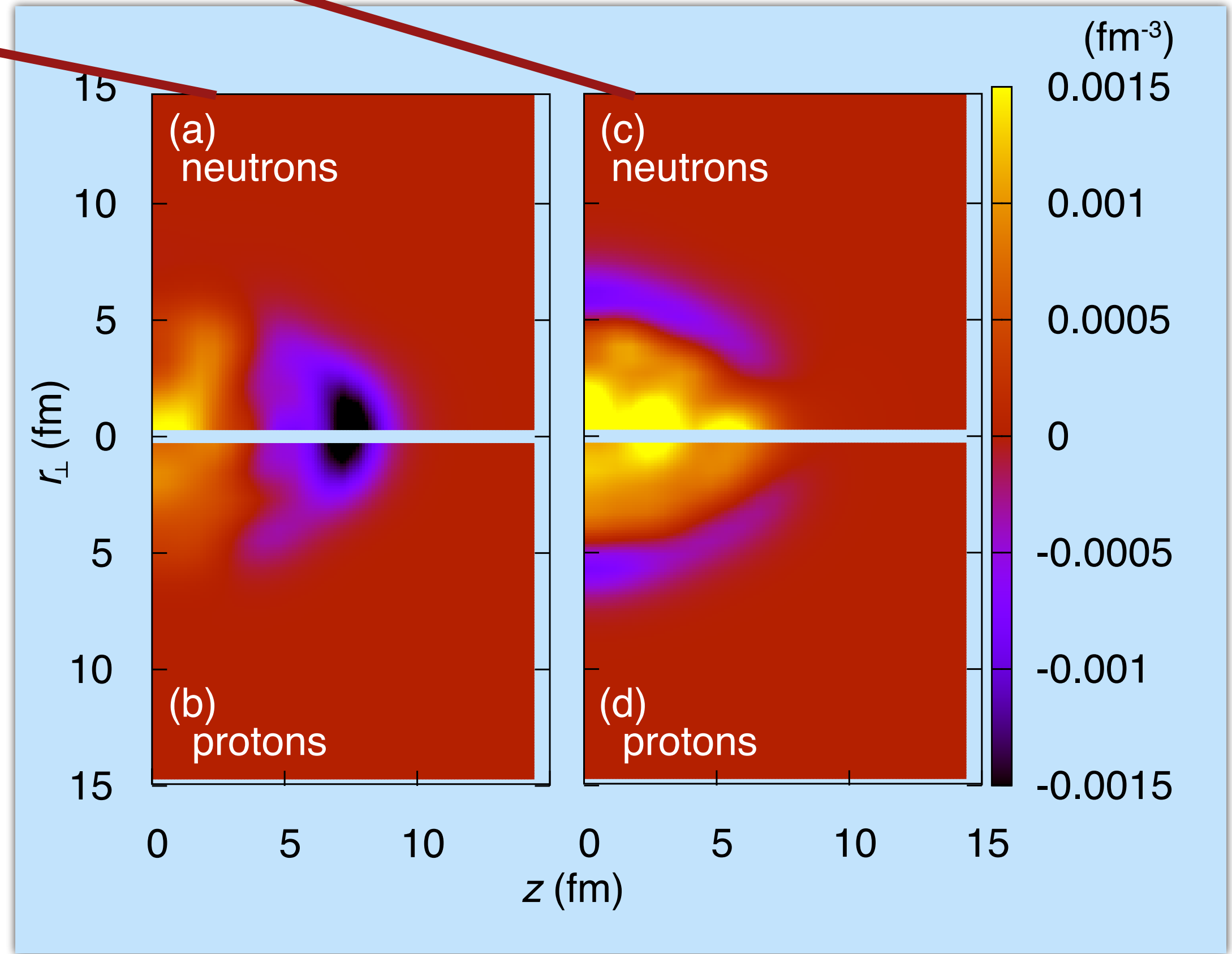


quadrupole

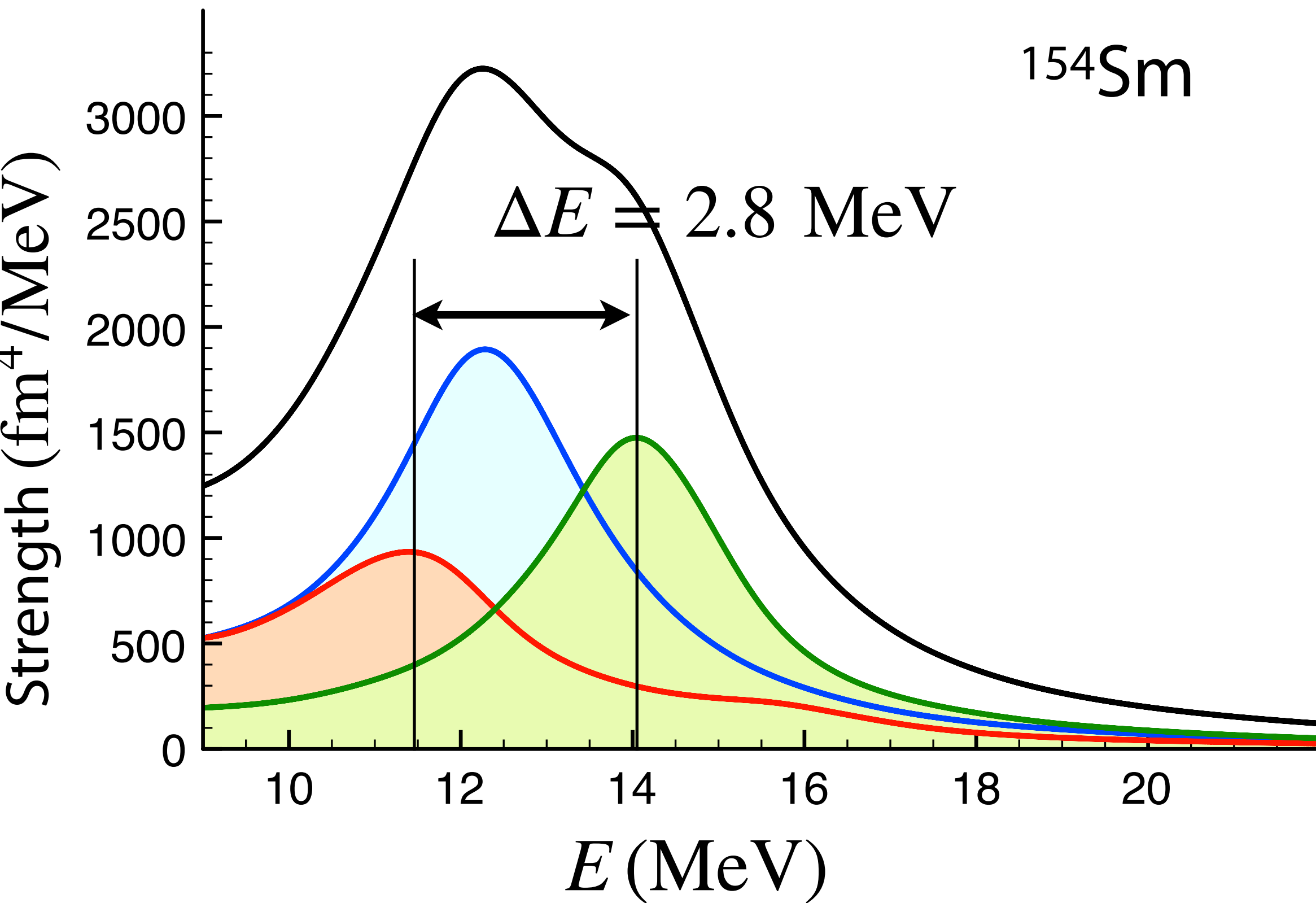


transition density

$$\delta\rho_\lambda(\vec{r}) = \langle \Psi_\lambda | \psi^\dagger(\vec{r})\psi(\vec{r}) | \Psi_0 \rangle$$

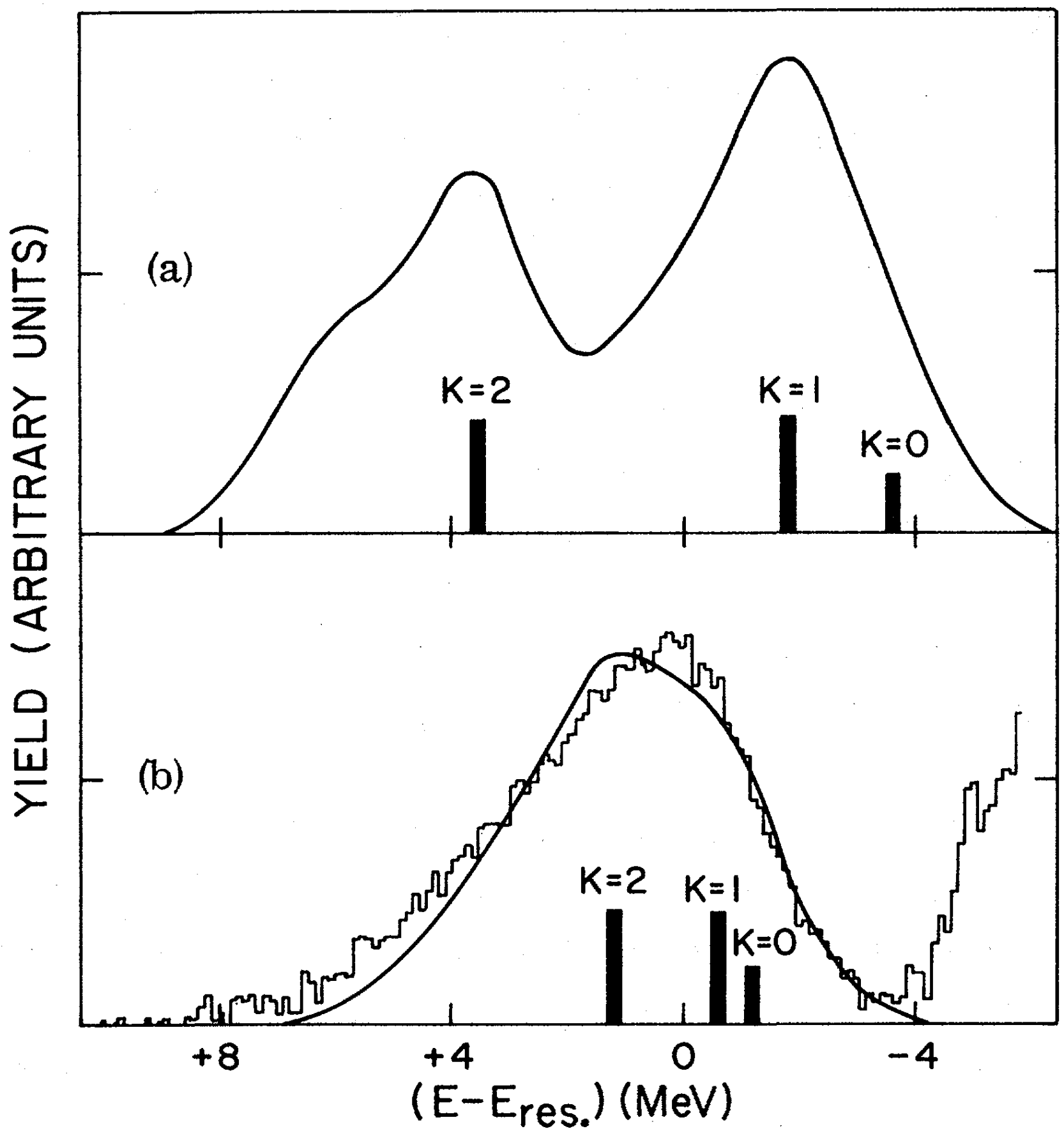


Deformation splitting of the GQR



P+Q model

Kishimoto+('75)



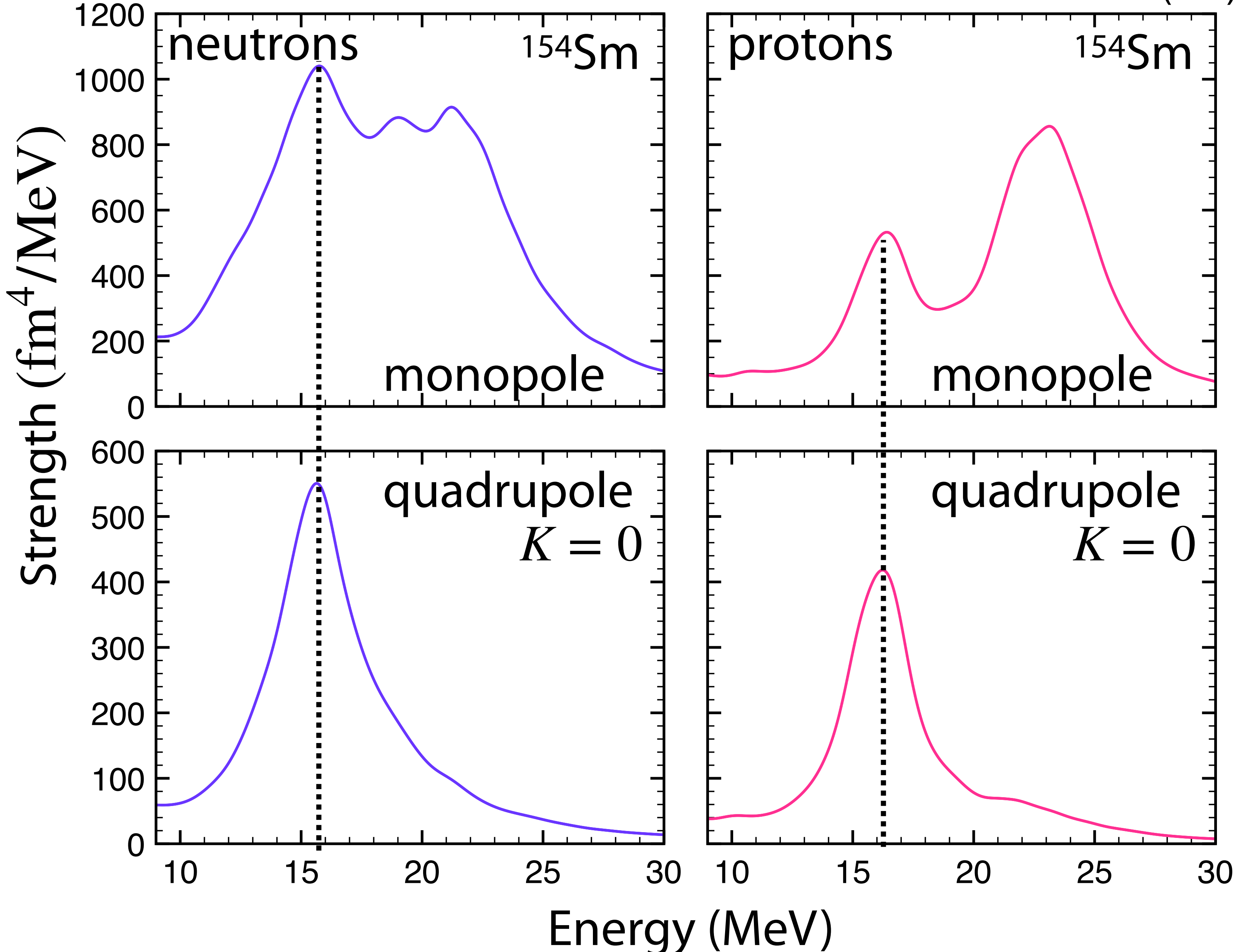
$\Delta E \sim 6 \text{ MeV}$
ordinal coordinate

$\Delta E \sim 2 \text{ MeV}$
doubly-stretched coordinate

EDF-based QRPA satisfies the nuclear self-consistency
shape (density distribution) and potential

Coupling at the static level

Yoshida ('21)



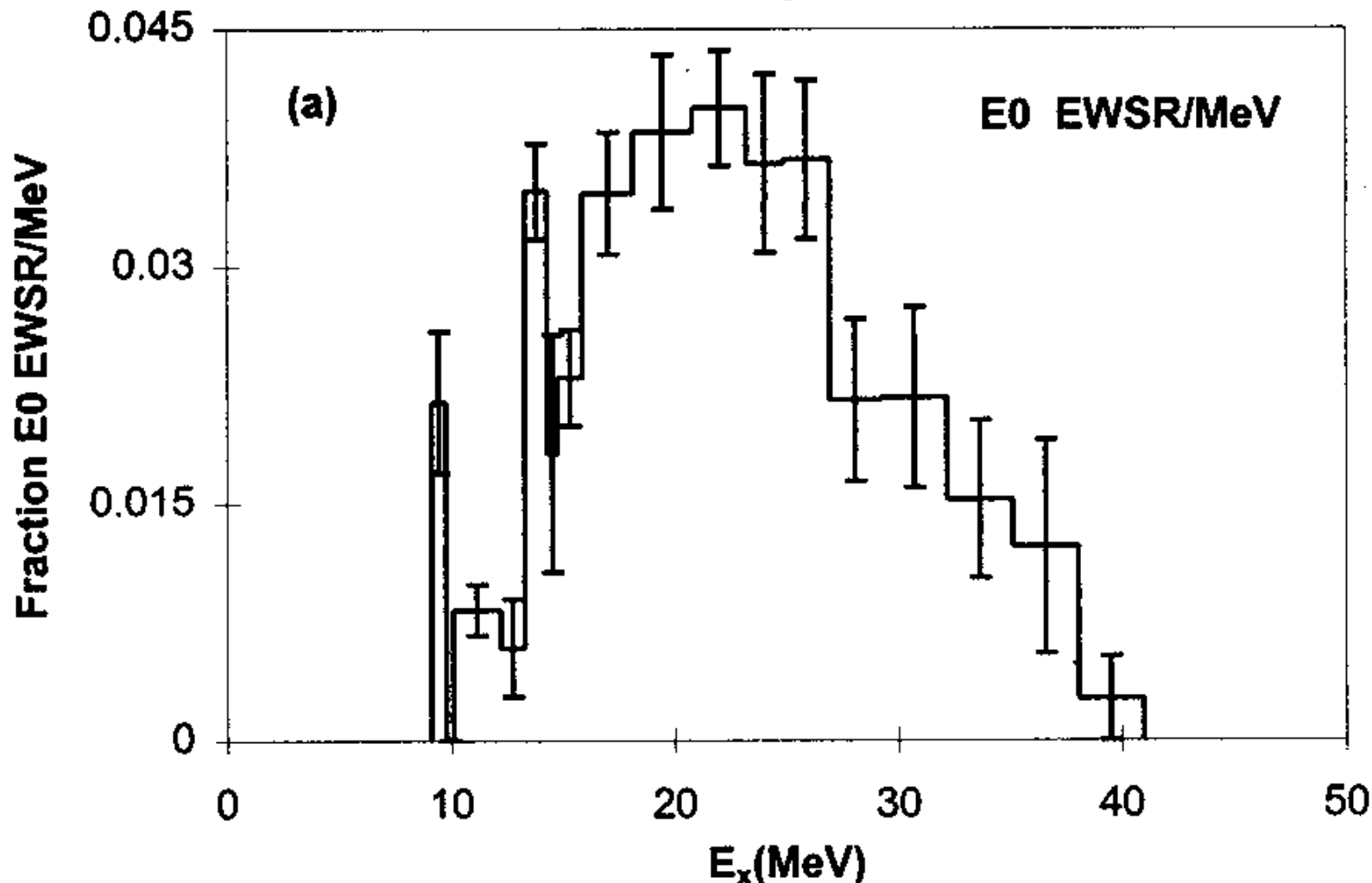
Unperturbed strengths
w/o the RPA (dynamic) correlations
deformation-induced coupling

Peaks
↓
monopole and $K=0$ quadrupole
coincide in energy
residual interactions
↓
Coexistence persists

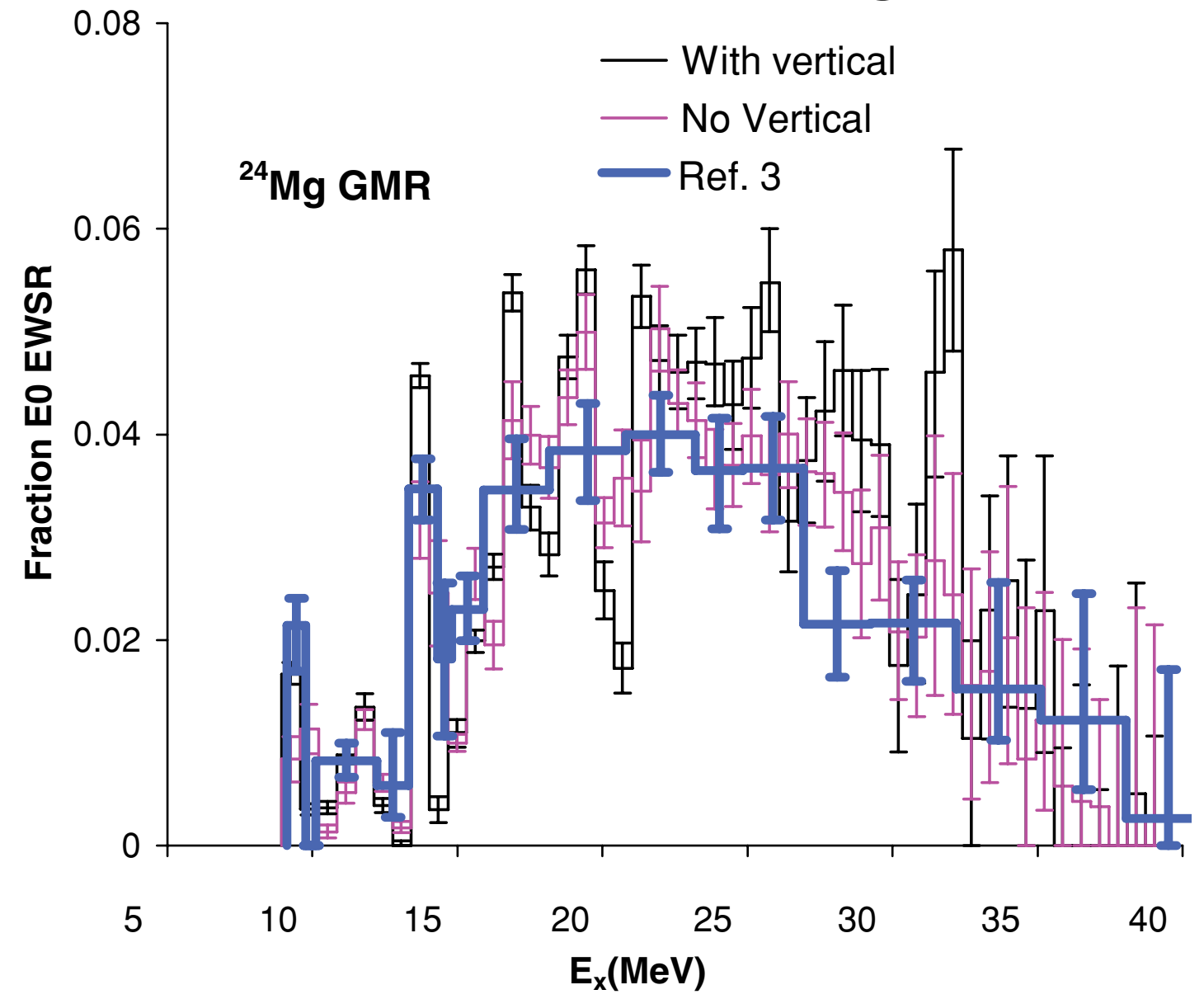
Deformation effect on GMR in light nuclei: universality

^{24}Mg @ TAMU

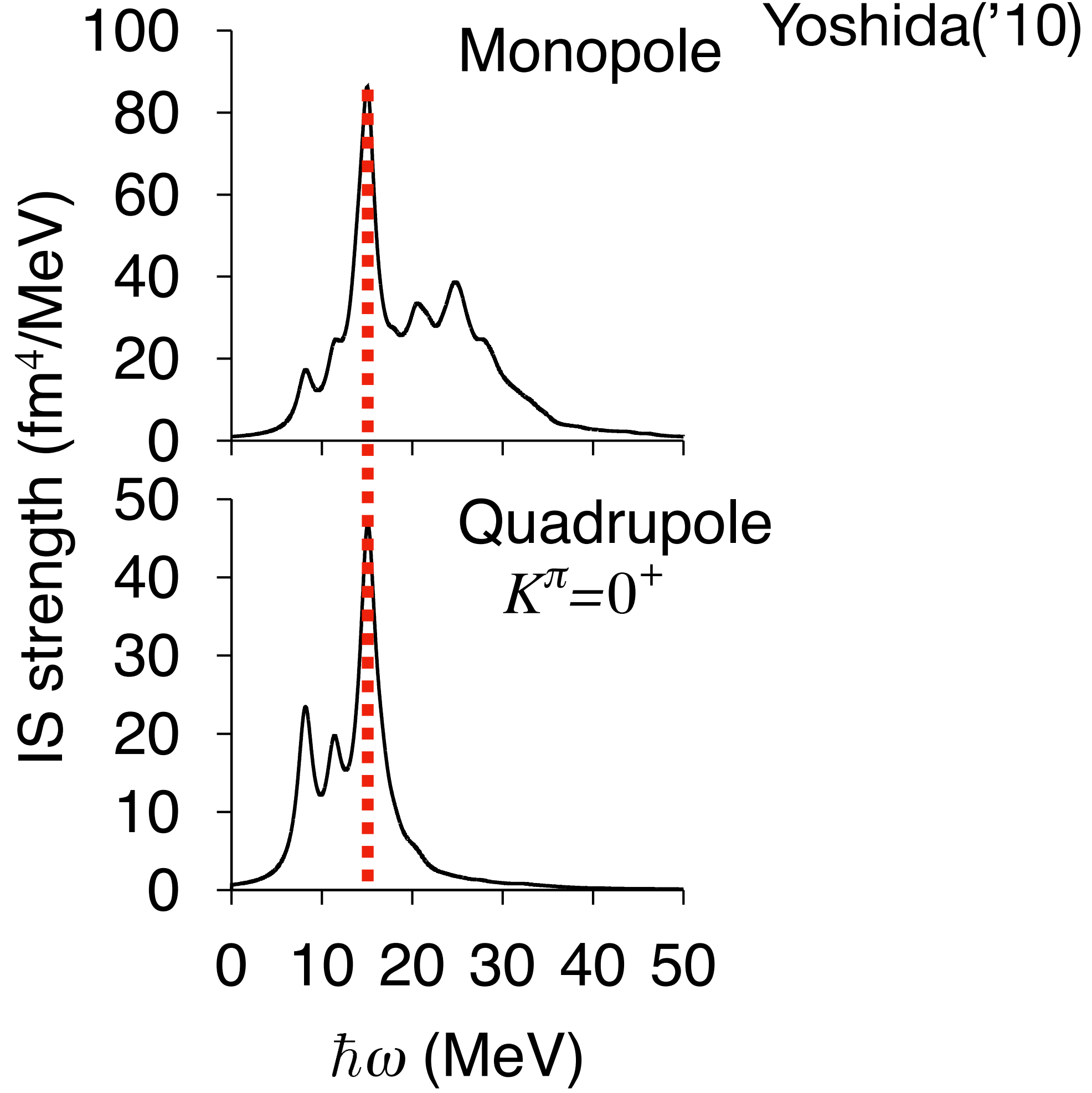
Youngblood+('99)



Youngblood+('09)



Yoshida('10)



occurrence of the "lower-energy (~ 15 MeV)" peak due to coupling to the $K=0$ of GQR

Deformation splitting in a light nucleus

Physics Letters B 748 (2015) 343–346



ELSEVIER

Contents lists available at ScienceDirect

Physics Letters B

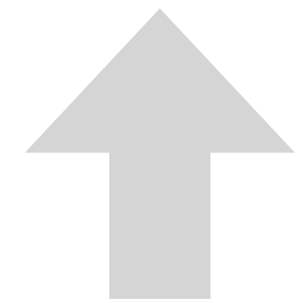
www.elsevier.com/locate/physletb

Splitting of ISGMR strength in the light-mass nucleus ^{24}Mg due to ground-state deformation

Y.K. Gupta^{a,1}, U. Garg^a, J.T. Matta^a, D. Patel^a, T. Peach^a, J. Hoffman^{a,2}, K. Yoshida^{b,c}, M. Itoh^{d,3}, M. Fujiwara^d, K. Hara^d, H. Hashimoto^d, K. Nakanishi^d, M. Yosoi^d, H. Sakaguchi^e, S. Terashima^e, S. Kishi^e, T. Murakami^e, M. Uchida^{e,4}, Y. Yasuda^e, H. Akimune^f, T. Kawabata^{g,5}, M.N. Harakeh^h

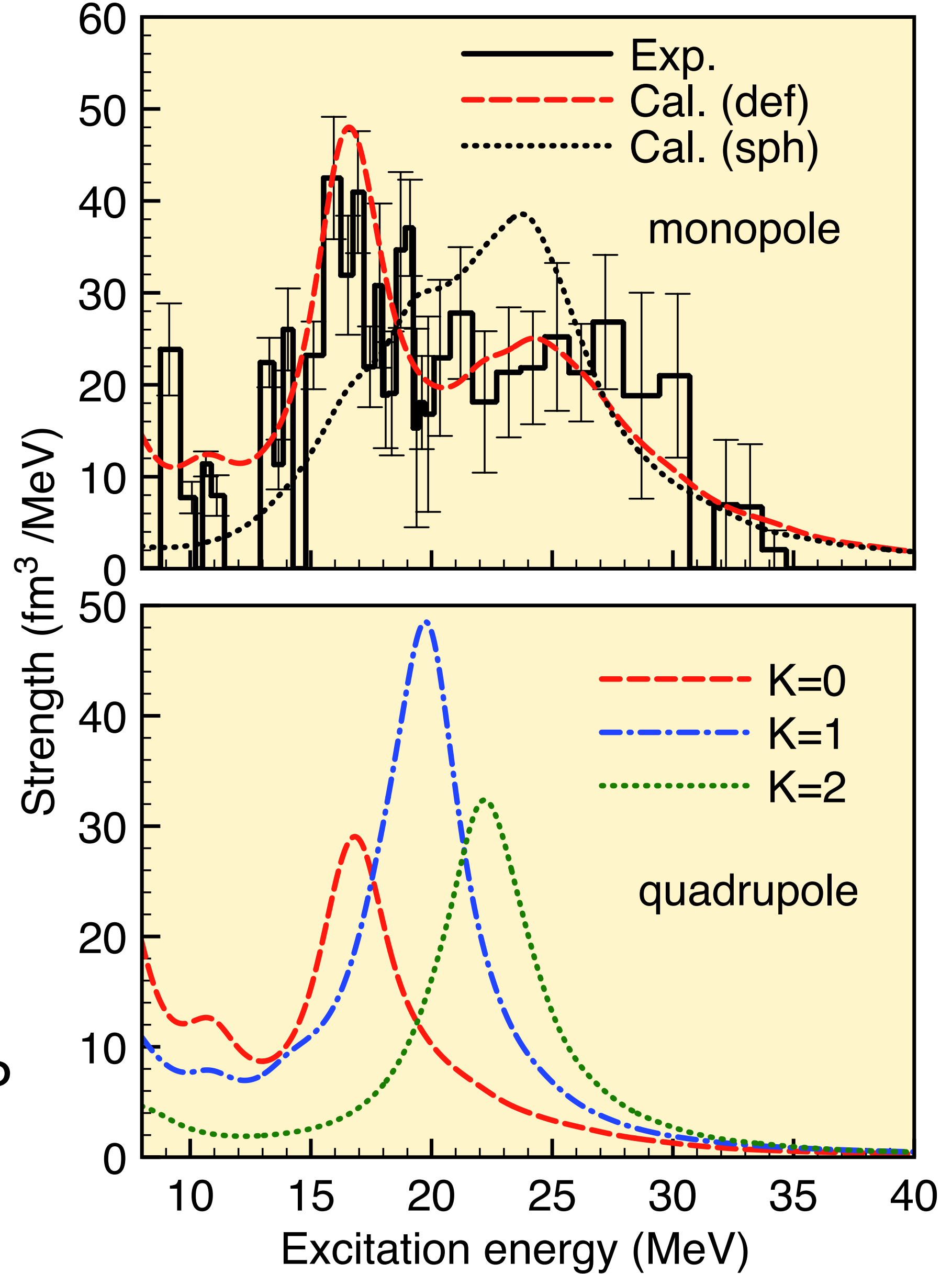
First observation of the splitting of GMR strengths in a light system

universal feature in deformed nuclei

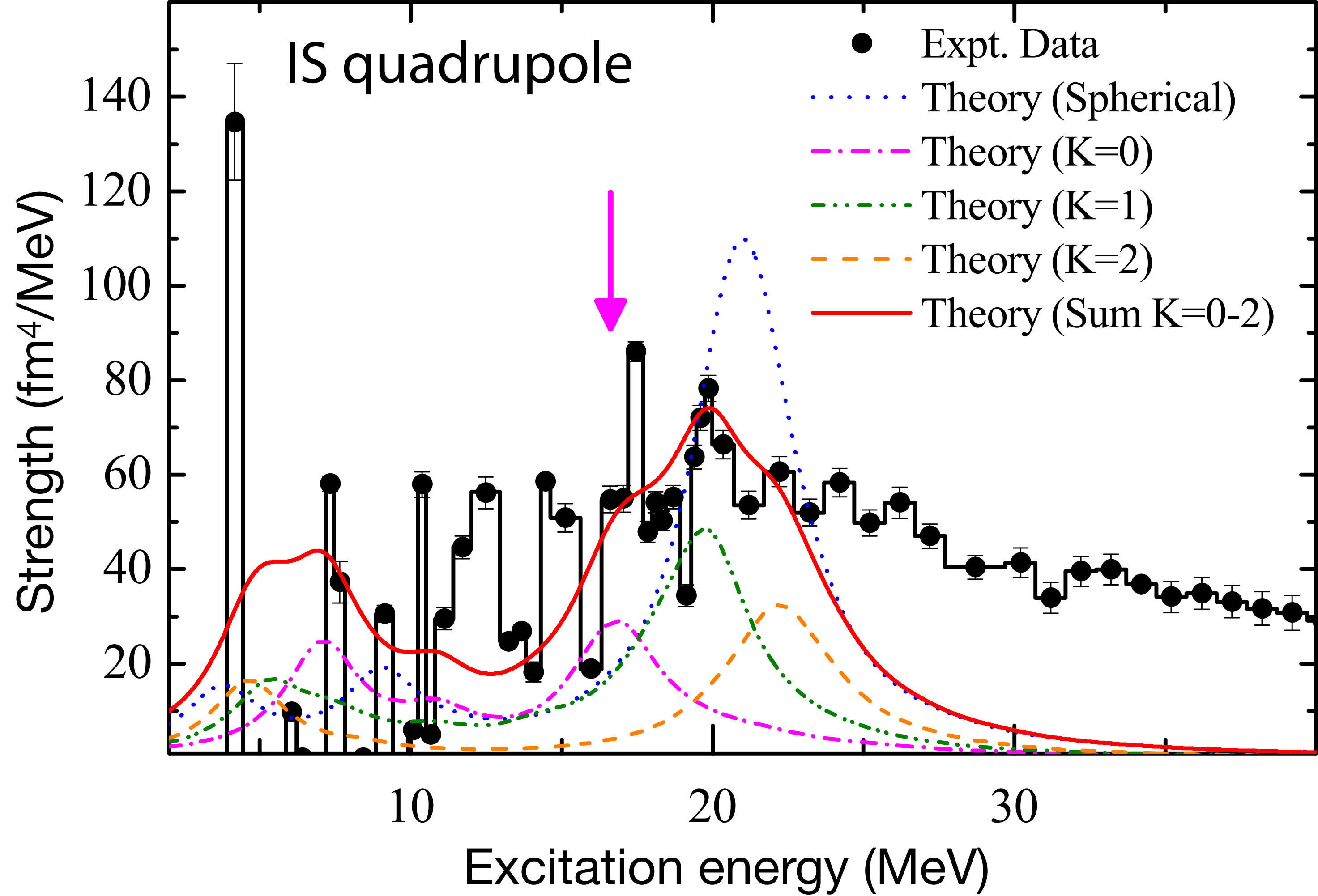


background-free high-resolution experiment @RCNP

parameter-free nuclear DFT calculation



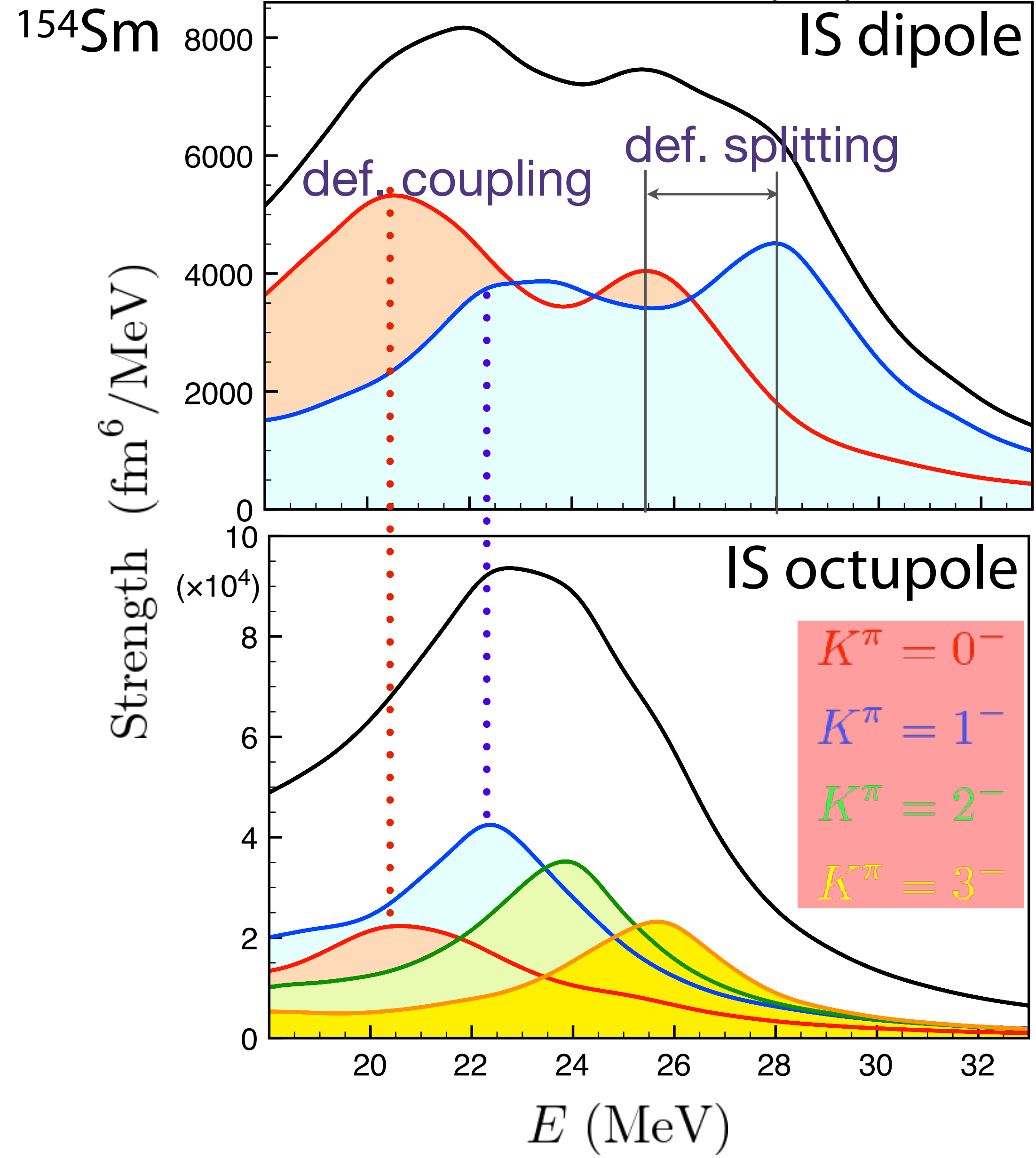
Strengths: missing in the QRPA



QRPA misses some states around 10–15 MeV
beyond QRPA? clustering degree of freedom?

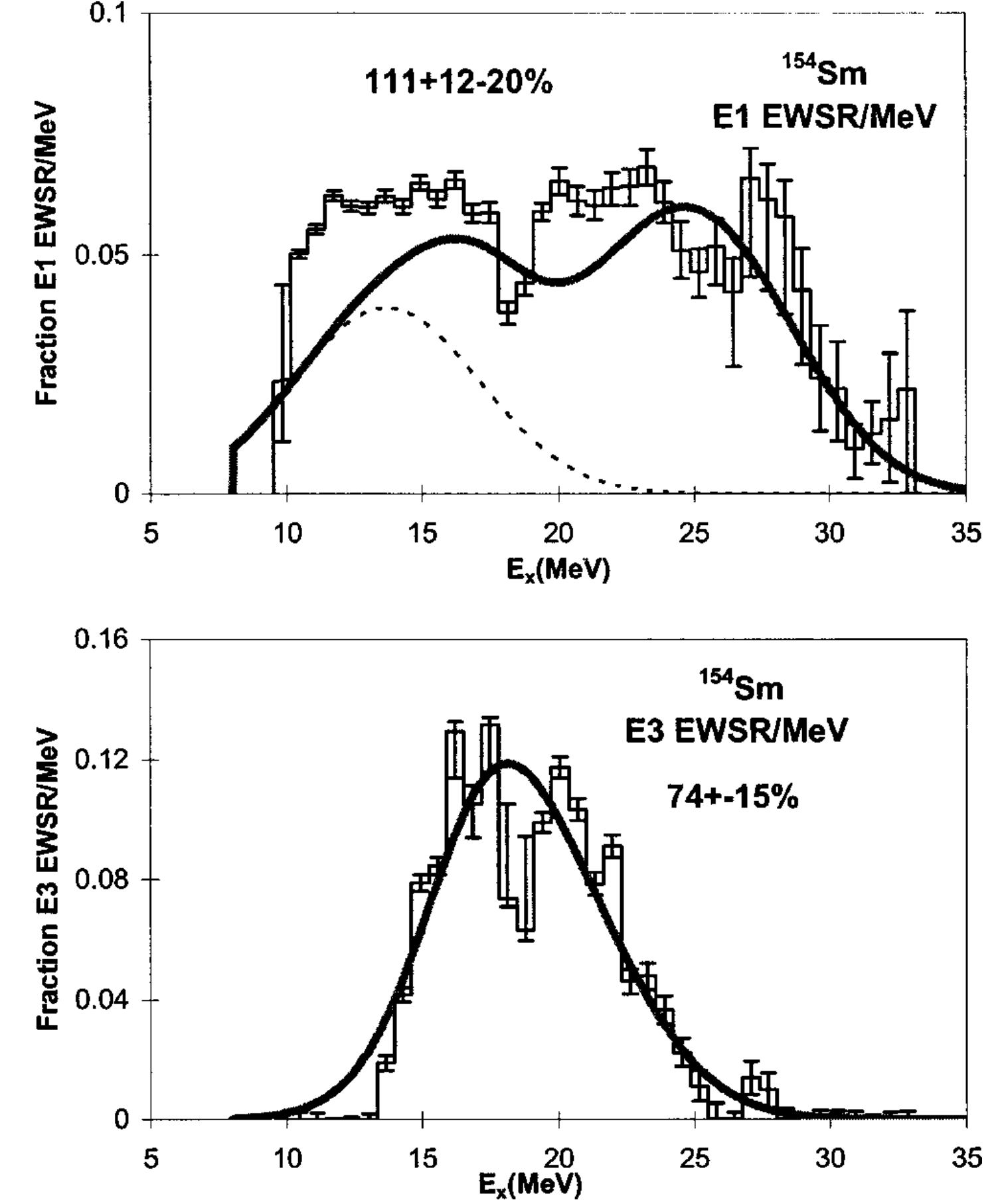
Coupling between $\Delta L = 2$

Yoshida–Nakatsukasa ('13)

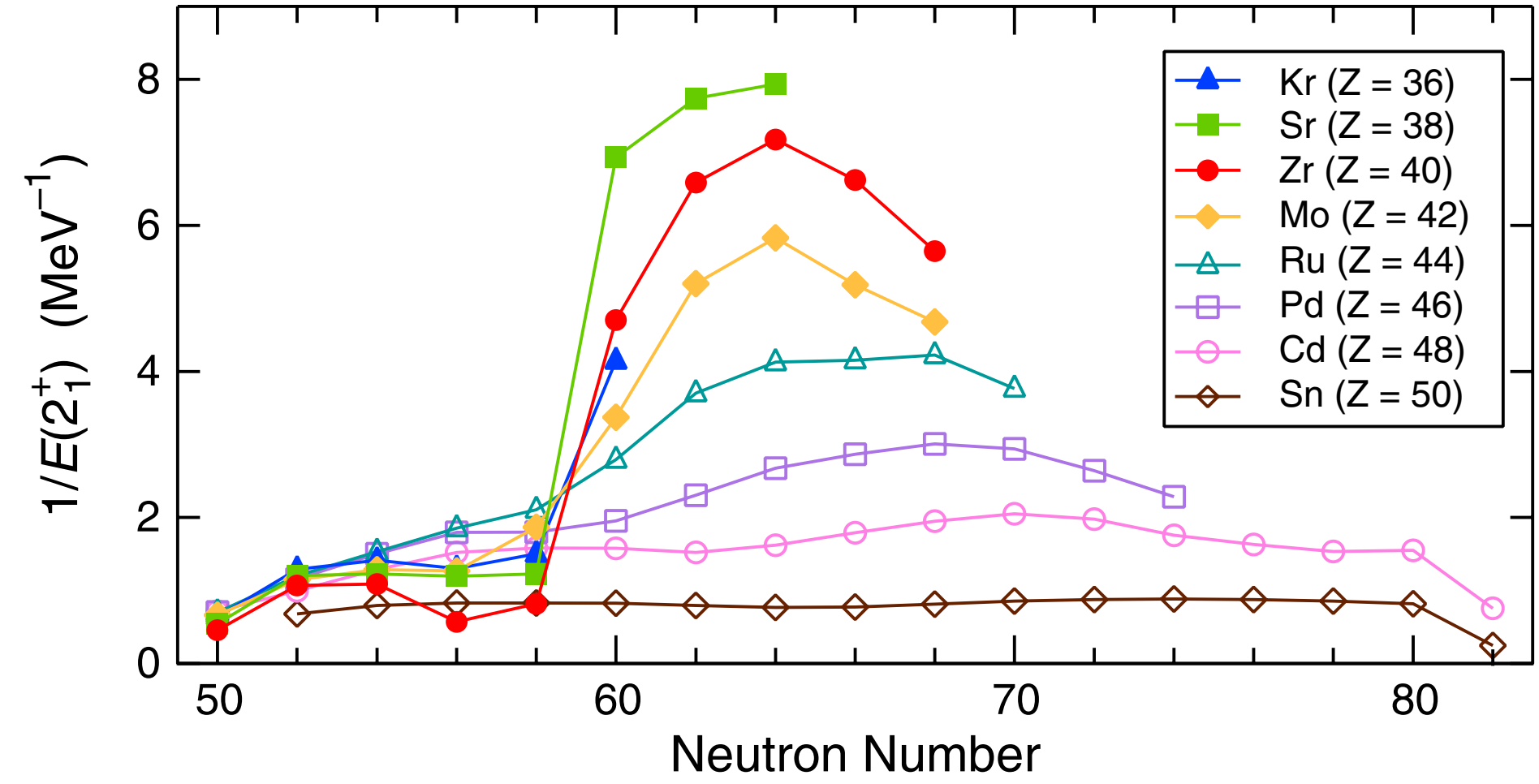
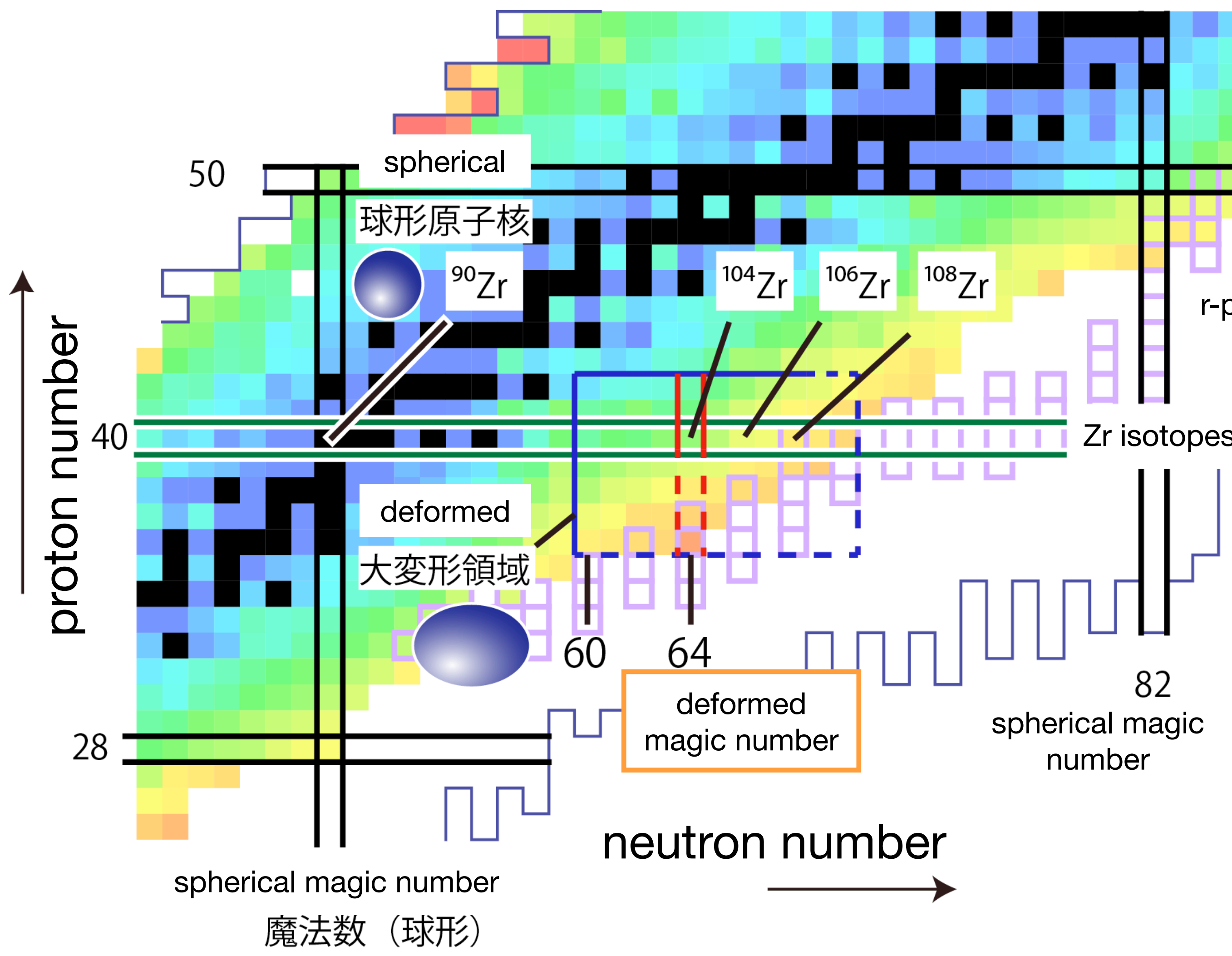


leading to a large width of the ISGDR

Youngblood+ ('04)

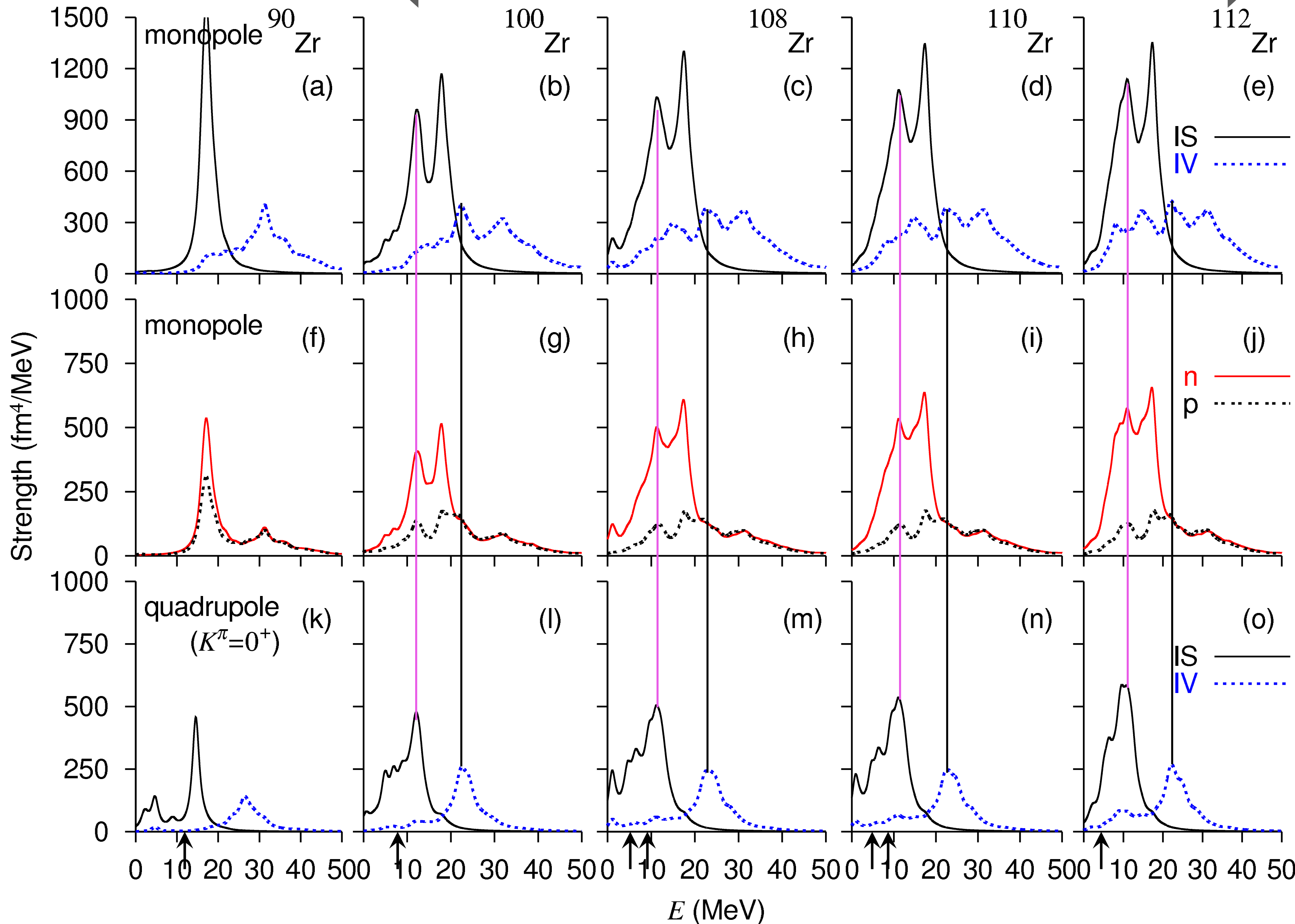


Large deformation of neutron-rich Zr isotopes



Sumikama+ ('11)
 Figure taken from RIDAI-RIKEN press release 16

GMR in deformed neutron-rich nuclei



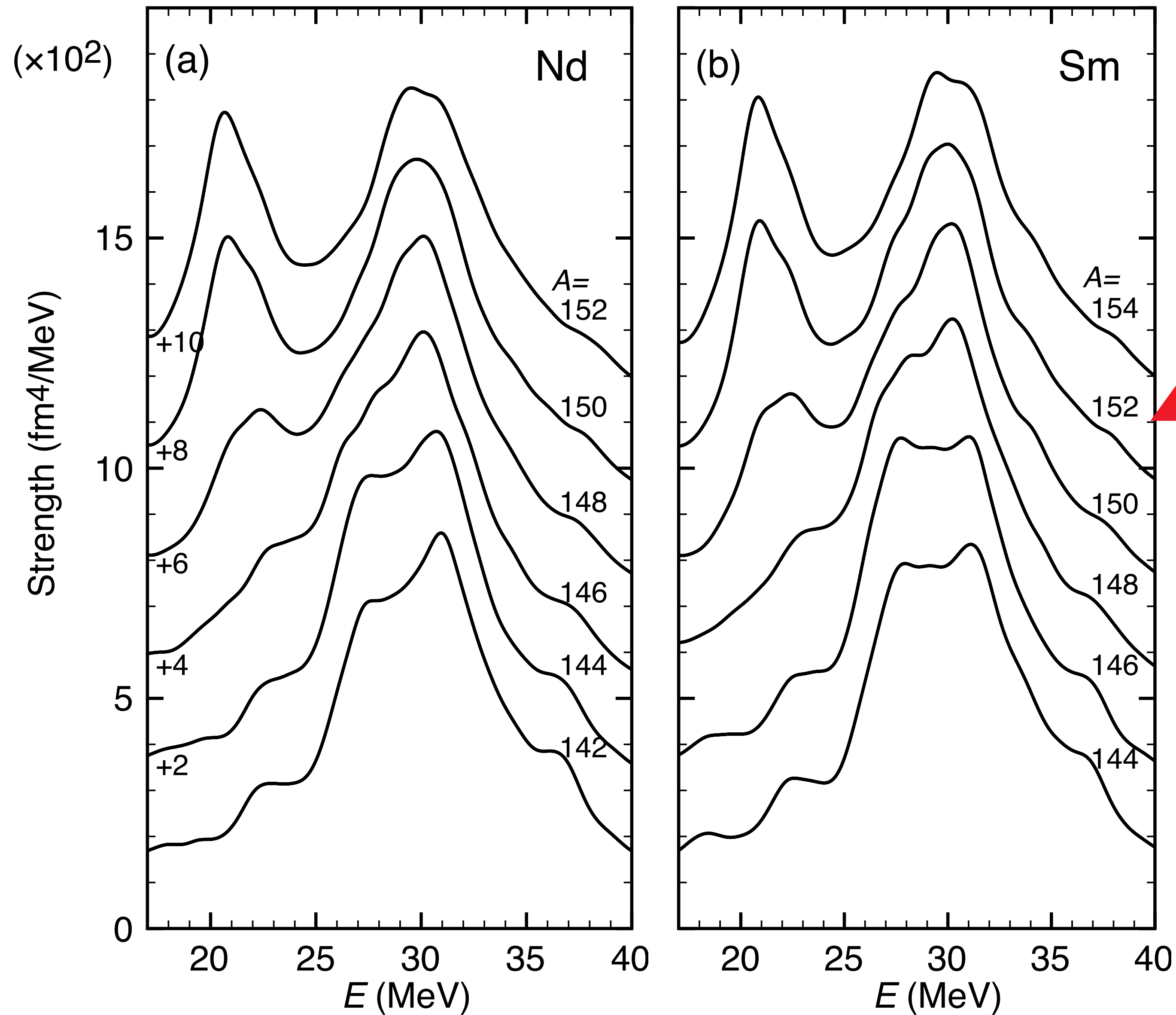
SkM* $\Gamma = 2$ MeV
 Yoshida('10)

IV strengths in low energy excitation of neutrons
 deformation splitting in IVGMR

Isovector (IV)-GMR in deformed nuclei

$$O = \int d\vec{r} r^2 \psi^\dagger(\vec{r}\tau) \langle \tau | \tau_3 | \tau' \rangle \psi(\vec{r}\tau')$$

Yoshida–Nakatsukasa ('13)

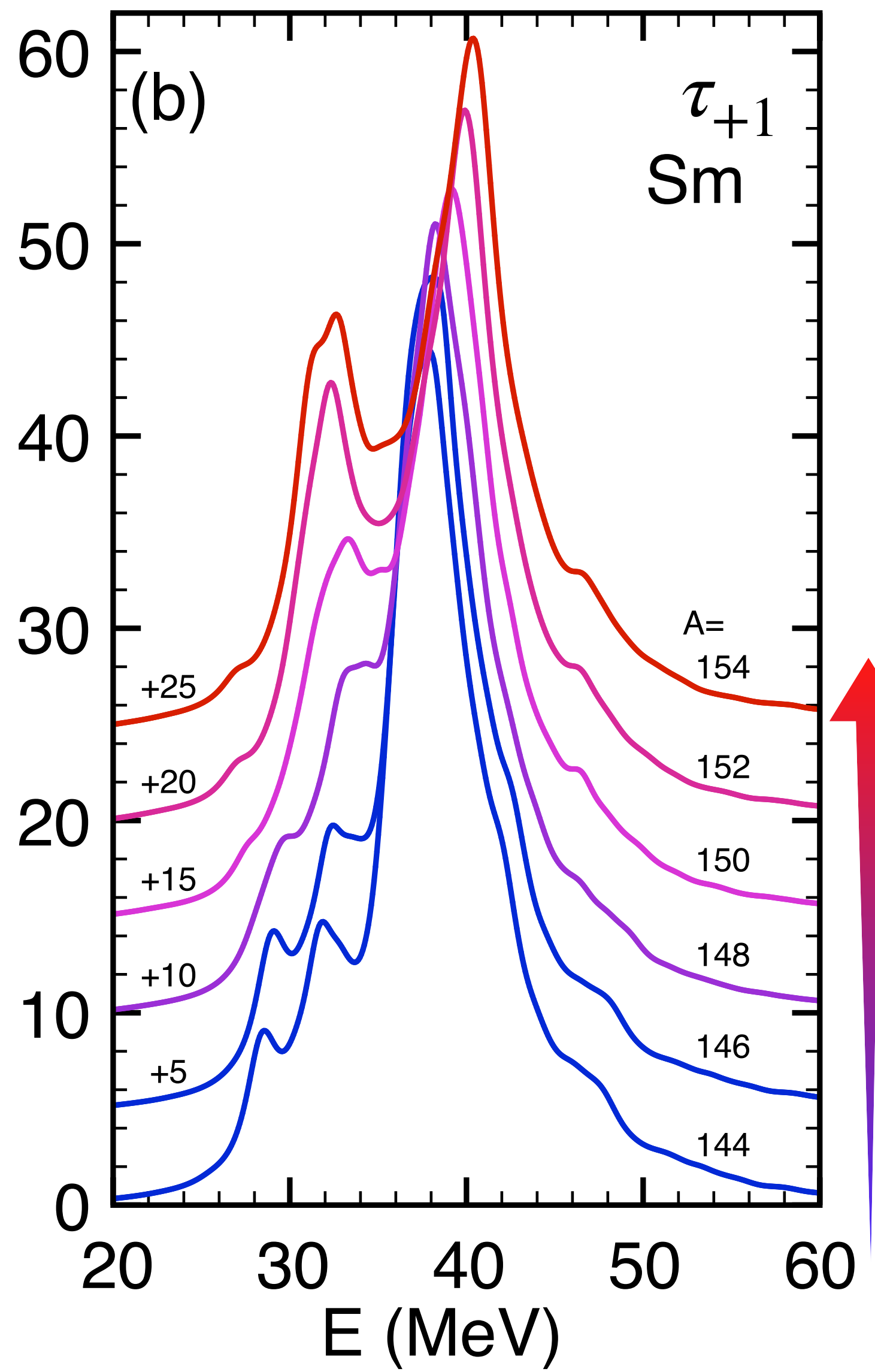
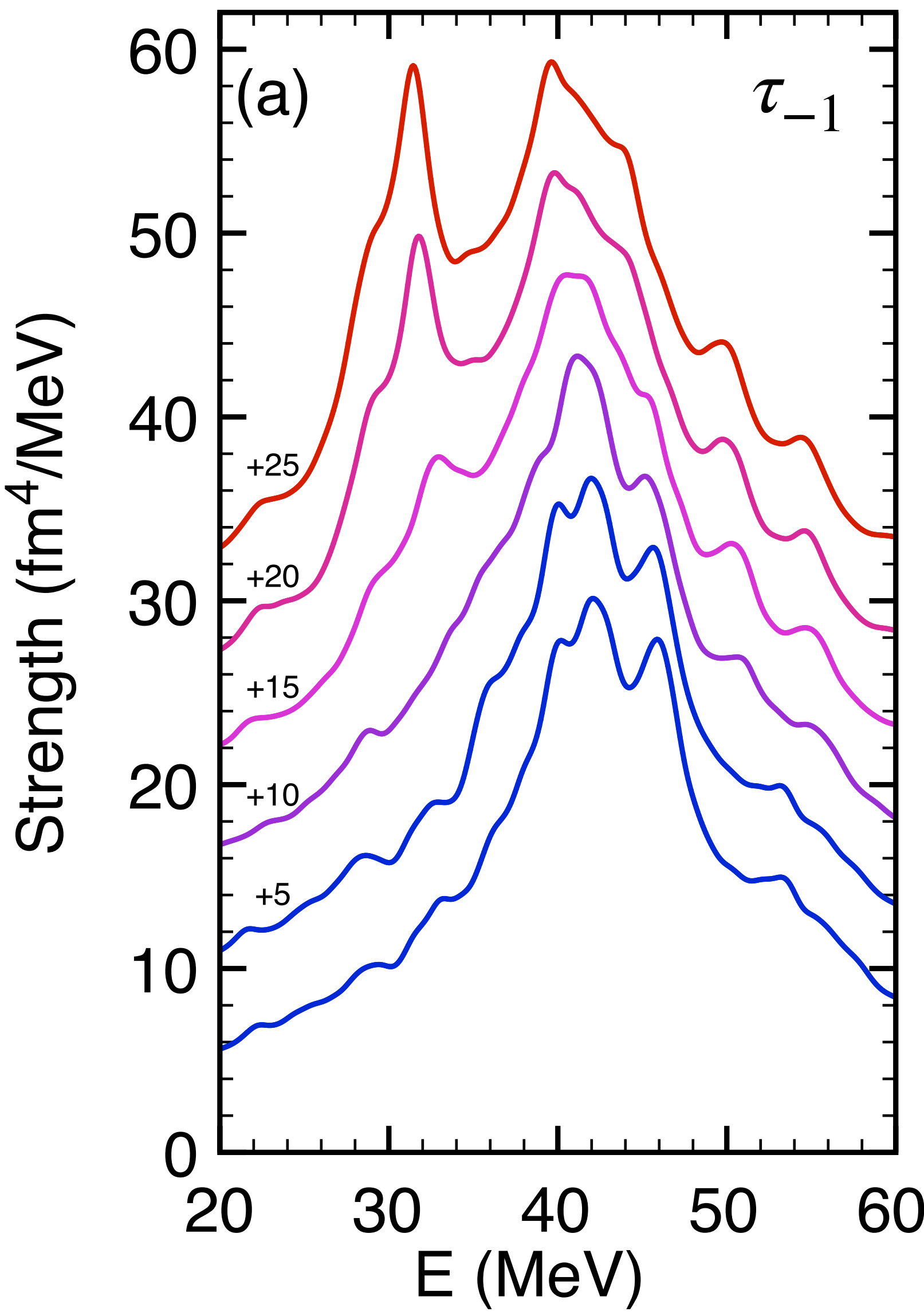


emergence of deformation "splitting"
 $\Delta E \sim 10 \text{ MeV} @ ^{154}\text{Sm}$
 $\sim 2 \times \Delta E(\text{ISGMR})$
 due to the coupling to the $K = 0$ of IV-GQR

Isvector (IV)-GMR in deformed nuclei

Yoshida ('21)

$$O = \int d\vec{r} r^2 Y_0(\hat{r}) \psi^\dagger(\vec{r}\tau) \langle \tau | \tau_{\pm 1} | \tau' \rangle \psi(\vec{r}\tau')$$



emergence of deformation "splitting"
 $\Delta E \sim 10 \text{ MeV} @ ^{154}\text{Sm}$
 universal in IV excitations
 $\mu_\tau = -1, 0, +1$

development of deformation

Summary

Deformation effect in GMR studied by nuclear DFT

appearance of the **deformation splitting**

coupling to the $K=0$ component of the GQR

deformation splitting of the GQR ($K=0,1,2$)

taking place at the mean-field level

stronger coupling in well-deformed nuclei

universal in medium-mass and light nuclei, as well as in n-rich nuclei

universal in IS and IV excitations

Coupling between the $K=0$ component of the dip. and oct. giant resonances

(if the parity is a good quantum number)

References

Yoshida ('10): Mod. Phys. Lett. A 25 (2010), 1783

Yoshida ('10): Phys. Rev. C 82 (2010), 034324

Yoshida–Nakatsukasa ('11): Phys. Rev. C 83 (2011), 021304(R)

Yoshida–Nakatsukasa ('13): Phys. Rev. C 88 (2013), 034309

Yoshida ('21): Phys. Rev. C 104 (2021), 044309