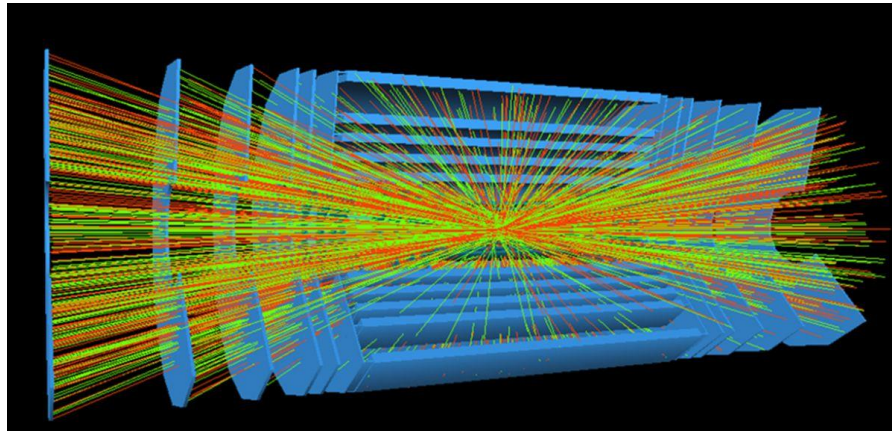


# Multi particle production in proton-nucleus collisions at high-energy

Yair Mulian / CEA Saclay  
Together with E. Iancu, “To appear”



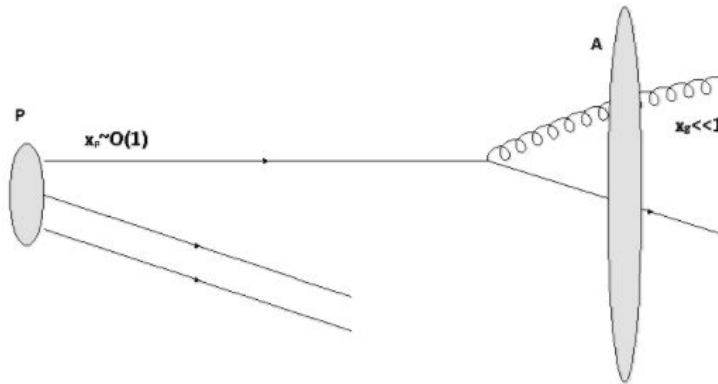
# Talk Outline

- 1) Forward particle production -- general formulation.
- 2) A strategy to find the trijet outgoing state.
- 3) The leading order forward trijet cross section.
- 4) The next-to-leading order forward dijet production.

# Forward Particle Production

By using the formalism of the light-cone wave function in perturbative QCD, together with the hybrid factorization, the derivation of the forward LO dijet cross-section was done in hep-ph/0708.0231 (C. Marquet).

The basic setup: a large- $x$  parton from the proton scatters off the small- $x$  gluon distribution in the target nucleus. Large- $x$  parton is most likely a quark.



Quark fragmentation in the presence of a shockwave.

The time evolution of the initial (bare) quark state is given by:

$$|q_\lambda^\alpha(q^+, \mathbf{q})\rangle_{\text{in}} \equiv U(0, -\infty) |q_\lambda^\alpha(q^+, \mathbf{q})\rangle$$

Where U denotes a unitary operator:

$$U(t, t_0) = \text{T exp} \left\{ -i \int_{t_0}^t dt_1 H_I(t_1) \right\}$$

The information both on the time evolution and interaction of the bare quark with the target nucleus is given by the “outgoing state”:

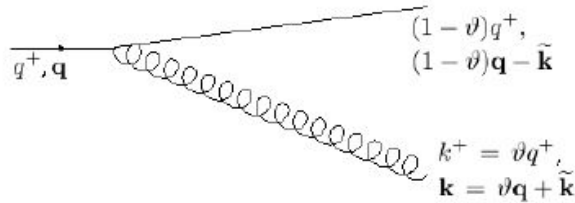
$$|q_\lambda^\alpha(q^+, \mathbf{w})\rangle_{\text{out}} \equiv U(\infty, 0) \hat{S} U(0, -\infty) |q_\lambda^\alpha(q^+, \mathbf{w})\rangle$$

This state will be shown to generate all the possible insertions of the shockwave. More importantly, the outgoing state is directly related to expectation values:

$$\langle \hat{\mathcal{O}} \rangle = \left\langle \langle q | U^\dagger \hat{S} U \hat{\mathcal{O}} U^\dagger \hat{S} U | q \rangle \right\rangle_{cgc}$$

# From the Wave Function to the Outgoing State

The leading-order quark wave function contain two additional contributions with respect to the bare quark state:



(a)



(b)

The real vs virtual contributions.

The expansion for the leading order quark wave-function:

$$|q_{\lambda_1}^\alpha(q)\rangle_{\text{in}} = \mathcal{Z}_{\text{LO}} |q_{\lambda_1}^\alpha(q)\rangle - \frac{\langle q_{\lambda_2}^\beta(s) g_i^a(k) | H_{gqq} | q_{\lambda_1}^\alpha(q) \rangle}{\Delta(q; s, k)} |q_{\lambda_2}^\beta(s) g_i^a(k)\rangle$$

The  $H_{gqq}$  is the part of the QCD Hamiltonian which generates the transition from the bare quark state to a bare quark and gluon state.

More explicitly:

$$H_{q \rightarrow qg} \equiv -g \int dx^- d^2x \left( 2(\partial_i A_i^a) \frac{1}{\partial^+} (\psi_+^\dagger t^a \psi_+) + \psi_+^\dagger t^a (\sigma_i \partial_i) \frac{1}{\partial^+} (\sigma_j A_j^a \psi_+) + \psi_+^\dagger t^a (\sigma_i A_i^a) \frac{1}{\partial^+} (\sigma_j \partial_j \psi_+) \right)$$

The energy denominator can be simplified by introducing new variables:

$$\Delta(q; k, q-k) = \frac{k^2}{2k^+} + \frac{(q-k)^2}{2(q^+ - k^+)} - \frac{q^2}{2q^+} = \frac{(k - \vartheta q)^2}{2\vartheta(1-\vartheta)q^+} = \frac{\tilde{k}^2}{2\vartheta(1-\vartheta)q^+} \quad \begin{aligned} \vartheta &\equiv \frac{k^+}{q^+}, \\ \tilde{k} &\equiv k - \vartheta q \end{aligned}$$

After inserting the relevant matrix element:

$$\begin{aligned} |q_{\lambda_1}^\alpha(q^+, q)\rangle_{\text{in}} &= \mathcal{Z}_{\text{LO}} |q_{\lambda_1}^\alpha(q^+, q)\rangle \\ &- \int_0^1 d\vartheta \int d^2\tilde{k} \frac{gt_{\beta\alpha}^a \phi_{\lambda_2\lambda_1}^{ij}(\vartheta) \tilde{k}^j}{4\pi^{3/2} \sqrt{\vartheta q^+ \tilde{k}^2}} |q_{\lambda_2}^\beta((1-\vartheta)q^+, (1-\vartheta)q - \tilde{k}) g_i^a(\vartheta q^+, \vartheta q + \tilde{k})\rangle \end{aligned}$$

After Fourier transformation:

$$\begin{aligned} |q_{\lambda_1}^\alpha(q^+, w)\rangle_{\text{in}} &= \mathcal{Z}_{\text{LO}} |q_{\lambda_1}^\alpha(q^+, w)\rangle \\ &+ \int_{x,z} \int_0^1 d\vartheta \frac{igt_{\beta\alpha}^a \phi_{\lambda_2\lambda_1}^{ij}(\vartheta) X^j}{4\pi^{3/2} \sqrt{\vartheta q^+ X^2}} \delta^{(2)}(w - (1-\vartheta)x - \vartheta z) |q_{\lambda_2}^\beta((1-\vartheta)q^+, x) g_i^a(\vartheta q^+, z)\rangle \end{aligned}$$

# The LO Outgoing State

The production state at leading order is given by

$$|q_\lambda^\alpha(q^+, \mathbf{w})\rangle_{out}^{(g)} \equiv U(\infty, 0) \hat{S} U(0, -\infty) |q_\lambda^\alpha(q^+, \mathbf{w})\rangle = |\psi_\lambda^\alpha(q^+, \mathbf{w})\rangle_{qg} + |q_\lambda^\alpha(q^+, \mathbf{w})\rangle$$

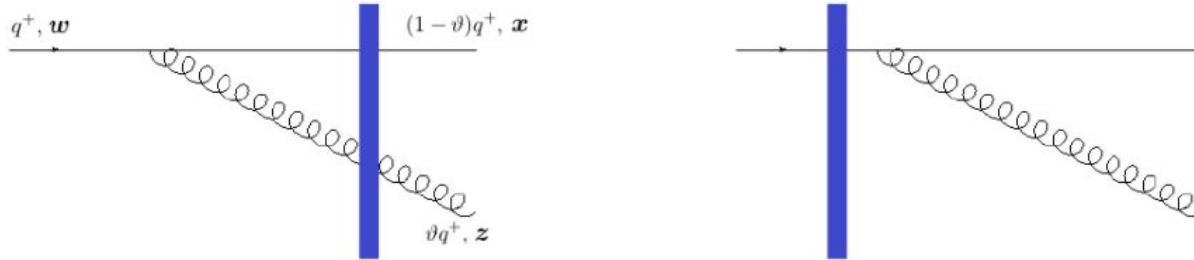
$$|\psi_\lambda^\alpha\rangle_{qg} = |q^\gamma g^b\rangle \left( -\langle q^\gamma g^b | \hat{S} | q^\beta g^a \rangle \frac{\langle q^\beta g^a | H_{q \rightarrow qg} | q^\alpha \rangle}{E_{qg} - E_q} + \frac{\langle q^\gamma g^b | H_{q \rightarrow qg} | q^\beta \rangle}{E_{qg} - E_q} \langle q^\beta | \hat{S} | q^\alpha \rangle \right)$$

Where only terms of order  $g$  were kept. The following result is obtained for the  $|qg\rangle$  contribution:

$$|\psi_\lambda^\alpha(q^+, \mathbf{w})\rangle_{qg} = \int_{\mathbf{x}, \mathbf{z}} \int_0^1 d\vartheta \frac{ig\phi_{\lambda_1\lambda}^{ij}(\vartheta)\sqrt{q^+} \mathbf{X}^j}{4\pi^{3/2}\sqrt{\vartheta} \mathbf{X}^2} \delta^{(2)}(\mathbf{w} - (1-\vartheta)\mathbf{x} - \vartheta\mathbf{z})$$

$$\times \left[ V^{\gamma\beta}(\mathbf{x}) U^{ba}(z) t_{\beta\alpha}^a - t_{\gamma\beta}^b V^{\beta\alpha}(\mathbf{w}) \right] |q_{\lambda_1}^\gamma((1-\vartheta)q^+, \mathbf{x}) g_i^b(\vartheta q^+, \mathbf{z})\rangle$$

Diagrammatically (blue bar denotes a shockwave = interaction with the target):



One gluon production at leading order with shockwave before and after the emission.

# The LO forward dijet cross-section

From the production state we can pass easily to the quark-gluon dijet cross section:

$$\begin{aligned} \frac{d\sigma_{\text{LO}}^{qA \rightarrow qg+X}}{d^3k d^3p} &\equiv \frac{1}{2N_c L} \stackrel{(g)}{out} \langle q_\lambda^\alpha(q^+, \mathbf{q}) | \hat{N}_q(p) \hat{N}_g(k) | q_\lambda^\alpha(q^+, \mathbf{q}) \rangle_{out}^{(g)} \\ &= \frac{1}{2N_c L} \int_{\mathbf{w}, \bar{\mathbf{w}}} e^{i(\mathbf{w} - \bar{\mathbf{w}}) \cdot \mathbf{q}} \stackrel{qg}{\langle} \psi_\lambda^\alpha(q^+, \bar{\mathbf{w}}) | \hat{N}_q(p) \hat{N}_g(k) | \psi_\lambda^\alpha(q^+, \mathbf{w}) \rangle_{qg} \end{aligned}$$

The following number density operators were introduced:

$$\hat{N}_q(p) \equiv \frac{1}{(2\pi)^3} b_\lambda^{\alpha\dagger}(p) b_\lambda^\alpha(p) \qquad \hat{N}_g(k) \equiv \frac{1}{(2\pi)^3} a_i^{a\dagger}(k) a_i^a(k)$$

Then the result for the leading-order dijet cross section is given by:

$$\begin{aligned} \frac{d\sigma_{\text{LO}}^{qA \rightarrow qg+X}}{dk^+ d^2k dp^+ d^2p} &= \frac{\alpha_s C_F (1 + (1 - \vartheta)^2)}{4\pi^3 \vartheta q^+} \delta(q^+ - k^+ - p^+) \\ &\times \int_{x, \bar{x}, z, \bar{z}} \frac{\mathbf{X} \cdot \bar{\mathbf{X}}}{X^2 \bar{X}^2} e^{-ip \cdot (x - \bar{x}) - ik \cdot (z - \bar{z})} \\ &\times \left[ S_{q\bar{q}gg}^{(1)}(\bar{x}, \bar{z}, x, z) - S_{q\bar{q}g}(\bar{w}, x, z) - S_{q\bar{q}g}(\bar{x}, w, \bar{z}) + \mathcal{S}(\bar{w}, w) \right] \end{aligned}$$

with  $\mathbf{X} \equiv x - z$ ,  $\bar{\mathbf{X}} \equiv \bar{x} - \bar{z}$ ,  $w = (1 - \vartheta)x + \vartheta z$  and  $\bar{w} = (1 - \vartheta)\bar{x} + \vartheta \bar{z}$ .



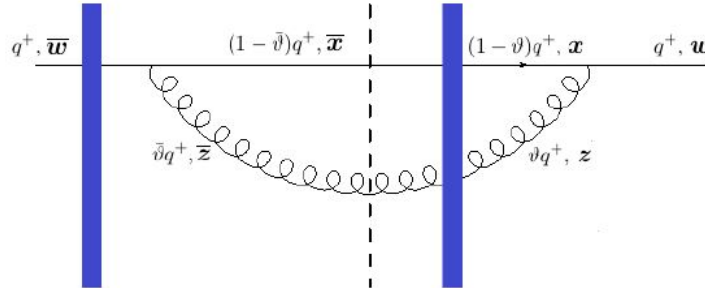
Where the following combinations of Wilson lines were introduced (in the large  $N_c$  limit these combinations represent the quadropole-dipole and dipole-dipole interactions):

$$\begin{aligned}
 S_{q\bar{q}gg}^{(1)}(\bar{x}, \bar{z}, x, z) &\equiv \frac{1}{C_F N_c} \text{tr} \left( V^\dagger(\bar{x}) V(x) t^a t^c \right) \left[ U^\dagger(\bar{z}) U(z) \right]^{ca} \\
 &= \frac{1}{2C_F N_c} (N_c^2 \mathcal{Q}(\bar{x}, x, z, \bar{z}) \mathcal{S}(\bar{z}, z) - \mathcal{S}(\bar{x}, x)) \simeq \mathcal{Q}(\bar{x}, x, z, \bar{z}) \mathcal{S}(\bar{z}, z) \\
 S_{q\bar{q}g}(\bar{w}, x, z) &\equiv \frac{1}{C_F N_c} \text{tr} \left( V^\dagger(\bar{w}) t^b V(x) t^a \right) U^{ba}(z) \\
 &= \frac{1}{2C_F N_c} (N_c^2 \mathcal{S}(\bar{w}, z) \mathcal{S}(z, x) - \mathcal{S}(\bar{w}, x)) \simeq \mathcal{S}(\bar{w}, z) \mathcal{S}(z, x)
 \end{aligned}$$

The dipole and quadropole are defined by:

$$\begin{aligned}
 \mathcal{S}(\bar{w}, w) &\equiv \frac{1}{N_c} \text{tr} \left[ V^\dagger(\bar{w}) V(w) \right] \\
 \mathcal{Q}(\bar{x}, x, z, \bar{z}) &\equiv \frac{1}{N_c} \text{tr} \left[ V^\dagger(\bar{x}) V(x) V^\dagger(z) V(\bar{z}) \right] \\
 U(x) &= \text{T exp} \left\{ ig \int dx^+ T^a A_a^-(x^+, x) \right\}, \quad V(x) = \text{T exp} \left\{ ig \int dx^+ t^a A_a^-(x^+, x) \right\}
 \end{aligned}$$

In total there are four different insertions of Wilson lines (each diagram corresponds to a different term in the rectangular brackets). For example, below is the relevant diagram which corresponds to  $S_{q\bar{q}g}(\bar{w}, x, z)$  (the location of the measurement is denoted by a dashed line).

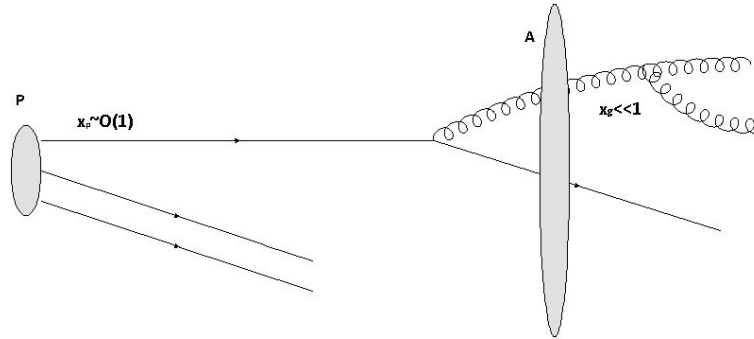


# The Trijet Setup

In the new setup, we have to produce three particles in the final state. There are two configurations of particles:

- a) Quark, quark and anti-quark
- b) Quark together with two gluons.

Due to the fact that we are using the light-cone gauge, the production of these configurations can happen both instantaneously (via one emission), or in the regular way, via two successive emissions or one emission followed by splitting process.



An example for a contribution with three particles in the final state

# The Trijet Outgoing State

The perturbative expression for the outgoing state is:

$$|out\rangle = |in\rangle + |out\rangle^{(1)} + |out\rangle^{(2)} + \dots$$

with:

$$|out\rangle^{(1)} = - \sum_{f,j} |f\rangle \langle f|S|j\rangle \frac{\langle j|H_{\text{int}}|in\rangle}{E_j - E_{in}} + \sum_{f,j} |f\rangle \frac{\langle f|H_{\text{int}}|j\rangle}{E_f - E_j} \langle j|S|in\rangle$$

$$|out\rangle^{(2)} = \sum_{f,j,i} |f\rangle \langle f|S|j\rangle \frac{\langle j|H_{\text{int}}|i\rangle \langle i|H_{\text{int}}|in\rangle}{(E_j - E_{in})(E_i - E_{in})} + \sum_{f,j,i} |f\rangle \frac{\langle f|H_{\text{int}}|j\rangle \langle j|H_{\text{int}}|i\rangle}{(E_f - E_j)(E_f - E_i)} \langle i|S|in\rangle$$

$$- \sum_{f,j,i} |f\rangle \frac{\langle f|H_{\text{int}}|j\rangle}{E_f - E_j} \langle j|S|i\rangle \frac{\langle i|H_{\text{int}}|in\rangle}{E_i - E_{in}}$$

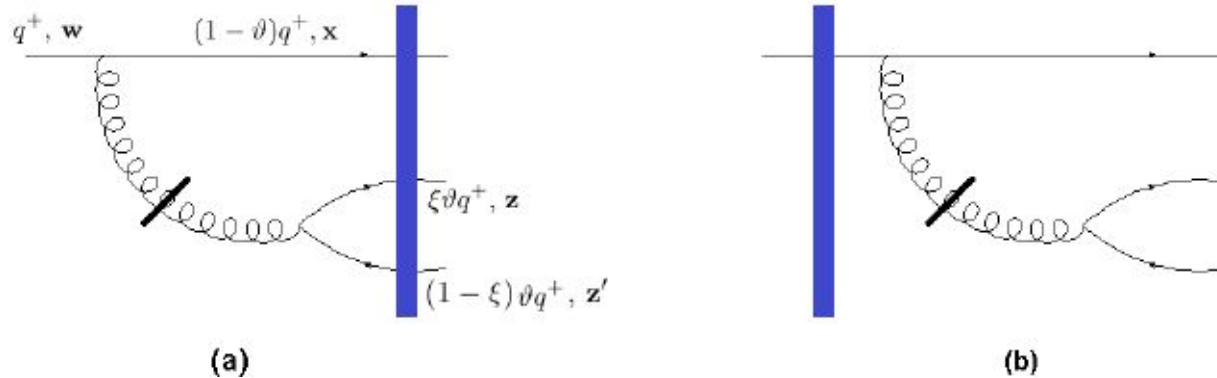
Where i, j and k runs over the relevant bare states, and Hint represent the interaction part of the QCD Hamiltonian. In the following we will focus only on the contribution to the outgoing states from the quark, quark, anti-quark configuration:

$$|\psi^\alpha\rangle_{qq\bar{q}}^{inst} \equiv |\bar{q}^\rho q^e q^\sigma\rangle \left( \frac{\langle \bar{q}^\rho q^e q^\sigma | H_{q \rightarrow qq\bar{q}} | q^\beta \rangle \langle q^\beta | \hat{S} | q^\alpha \rangle}{E_{qq\bar{q}} - E_q} - \frac{\langle \bar{q}^\rho q^e q^\sigma | \hat{S} | \bar{q}^\epsilon q^\delta q^\beta \rangle \langle \bar{q}^\epsilon q^\delta q^\beta | H_{q \rightarrow qq\bar{q}} | q^\alpha \rangle}{E_{qq\bar{q}} - E_q} \right)$$

$$|\psi^\alpha\rangle_{qq\bar{q}}^{reg} \equiv |\bar{q}^\rho q^e q^\sigma\rangle \left( \frac{\langle \bar{q}^\rho q^e q^\sigma | \hat{S} | \bar{q}^\delta q^\epsilon q^\kappa \rangle \langle \bar{q}^\delta q^\epsilon q^\kappa | H_{g \rightarrow q\bar{q}} | q^\beta g^i \rangle \langle q^\beta g^i | H_{q \rightarrow qg} | q^\alpha \rangle}{(E_{qq\bar{q}} - E_q)(E_{qg} - E_q)} \right.$$

$$+ \frac{\langle \bar{q}^\rho q^e q^\sigma | H_{g \rightarrow q\bar{q}} | q^\gamma g^i \rangle \langle q^\gamma g^i | H_{q \rightarrow qg} | q^\beta \rangle \langle q^\beta | \hat{S} | q^\alpha \rangle}{(E_{qq\bar{q}} - E_{qg})(E_{qq\bar{q}} - E_q)} - \frac{\langle \bar{q}^\rho q^e q^\sigma | H_{g \rightarrow q\bar{q}} | q^\gamma g^j \rangle \langle q^\gamma g^j | \hat{S} | q^\beta g^i \rangle \langle q^\beta g^i | H_{q \rightarrow qg} | q^\alpha \rangle}{(E_{qq\bar{q}} - E_{qg})(E_{qg} - E_q)} \Bigg)$$

# The Results for the Quark Anti-quark Outgoing State (Instantaneous Emission)

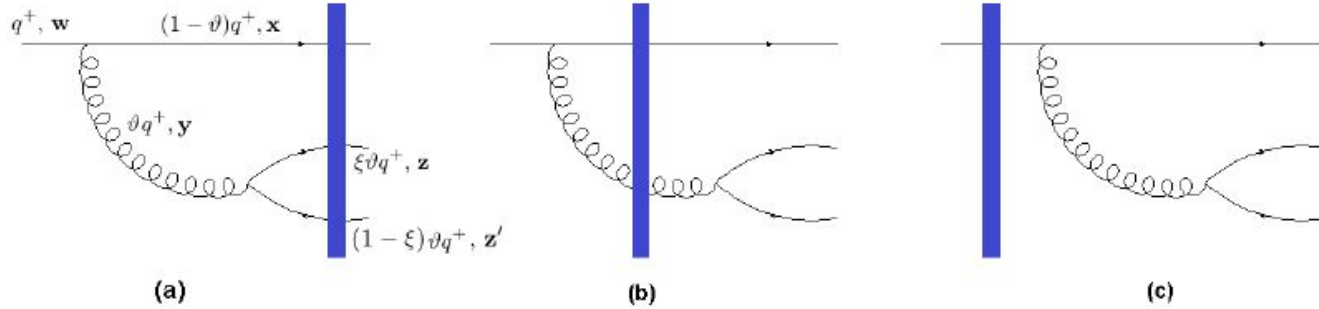


$$\begin{aligned}
 |\psi_{\lambda}^{\alpha}(q^{+}, \mathbf{w})\rangle_{qq\bar{q}}^{inst} = & - \int_{\mathbf{x}, \mathbf{z}, \mathbf{z}'} \int_0^1 d\vartheta d\xi \frac{g^2 (1-\vartheta)\xi(1-\xi)q^{+}}{4\pi^3 \left( \xi(1-\xi)Z^2 + (1-\vartheta)(X + \xi Z)^2 \right)} \\
 & \times \left[ V^{\varrho\delta}(\mathbf{z}') t_{\delta\epsilon}^a V^{\dagger\epsilon\rho}(\mathbf{z}) V^{\sigma\beta}(\mathbf{x}) t_{\beta\alpha}^a - t_{\varrho\rho}^a t_{\sigma\beta}^a V^{\beta\alpha}(\mathbf{w}) \right] \\
 & \times \delta^{(2)}(\mathbf{w} - \mathbf{C}) \left| \bar{q}_{\lambda_1}^{\rho}((1-\xi)\vartheta q^{+}, \mathbf{z}) q_{\lambda_1}^{\varrho}(\xi\vartheta q^{+}, \mathbf{z}') q_{\lambda}^{\sigma}((1-\vartheta)q^{+}, \mathbf{x}) \right\rangle
 \end{aligned}$$

$\mathbf{C}$  denotes the c.o.m for of the three produced particles:

$$\mathbf{C} \equiv (1-\vartheta)\mathbf{x} + \xi\vartheta\mathbf{z} + (1-\xi)\vartheta\mathbf{z}'.$$

# Regular Emission



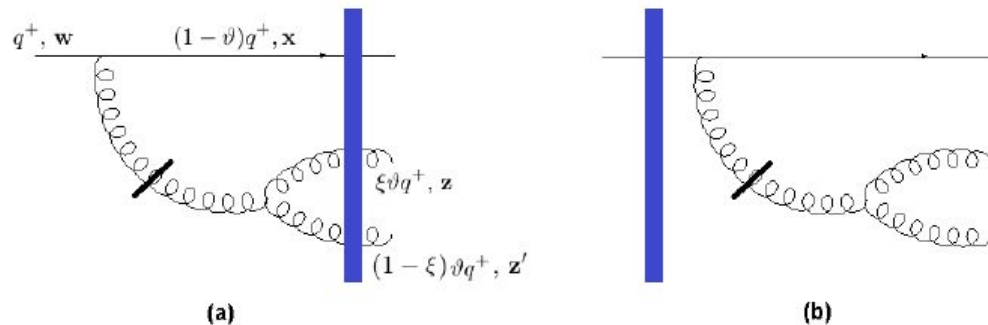
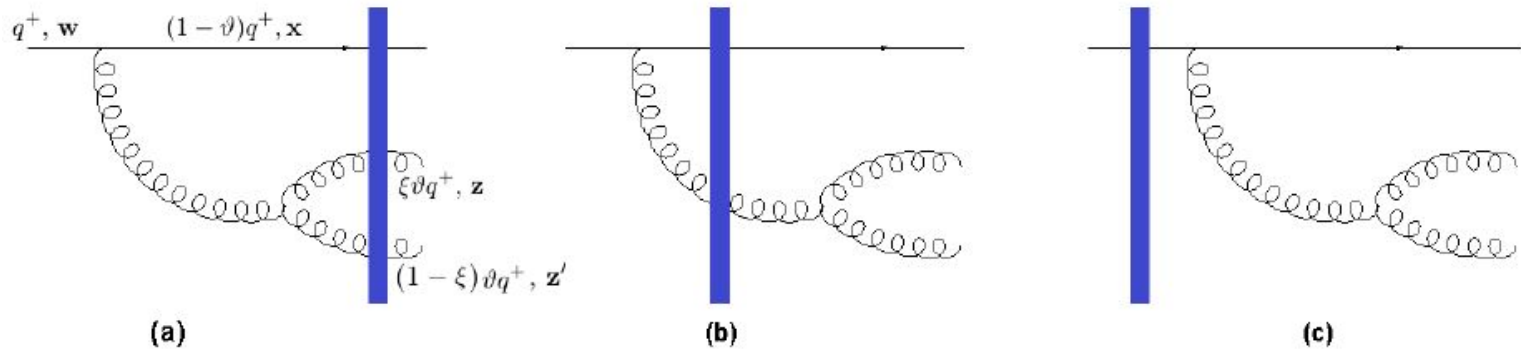
$$\begin{aligned}
 |\psi_{\lambda}^{\alpha}(q^+, w)\rangle_{qq\bar{q}}^{reg} = & - \int_{x, z, z'} \int_0^1 d\vartheta d\xi \frac{g^2 \varphi_{\lambda_2 \lambda_3}^{il}(\xi) \phi_{\lambda_1 \lambda}^{ij}(\vartheta) Z^l (X^j + \xi Z^j) q^+}{8\pi^3 (X + \xi Z)^2 Z^2} \\
 & \times \left[ \Theta_1(x, z, z') V^{\varrho\delta}(z') t_{\delta\epsilon}^a V^{\dagger\epsilon\rho}(z) V^{\sigma\beta}(x) t_{\beta\alpha}^a + \Theta_2(x, z, z') t_{\varrho\rho}^a t_{\sigma\beta}^a V^{\beta\alpha}(w) \right. \\
 & \left. - t_{\varrho\rho}^b V^{\sigma\beta}(x) U^{ba}(y) t_{\beta\alpha}^a \right] \delta^{(2)}(w - C) \left| \bar{q}_{\lambda_3}^{\rho}((1-\xi)\vartheta q^+, z) q_{\lambda_2}^{\varrho}(\xi\vartheta q^+, z') q_{\lambda_1}^{\sigma}((1-\vartheta)q^+, x) \right\rangle
 \end{aligned}$$

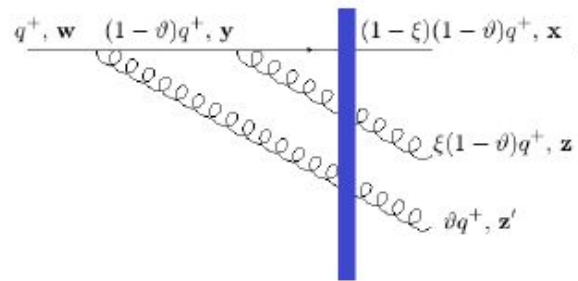
With the following definitions:

$$y \equiv \xi z' + (1-\xi)z \quad \Theta_1(x, z, z') \equiv \frac{(1-\vartheta)(X + \xi Z)^2}{(1-\vartheta)(X + \xi Z)^2 + \xi(1-\xi)Z^2} \quad \Theta_2(x, z, z') \equiv \frac{\xi(1-\xi)Z^2}{(1-\vartheta)(X + \xi Z)^2 + \xi(1-\xi)Z^2}$$

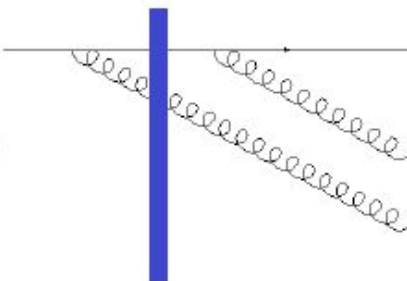
Note that both the result above and in the previous slide vanishes under the limit  $S \rightarrow 1$ . This property of the results has to be expected since the new particles are produced by the shockwave.

# The Diagrams for the Quark and Two Gluons Outgoing States

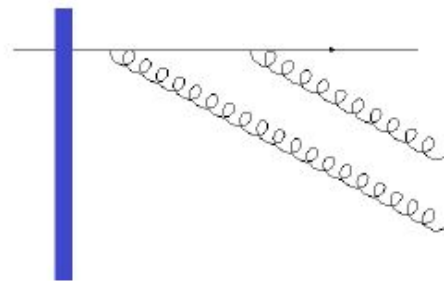




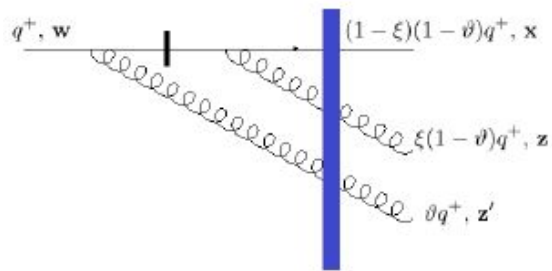
(a)



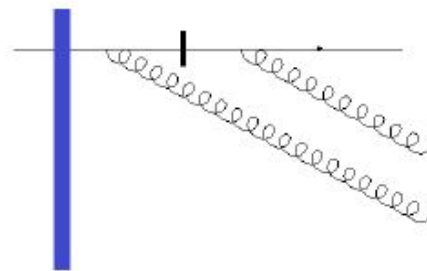
(b)



(c)



(a)



(b)

# The results for the forward trijet cross section

The expression for the forward trijet cross section is composed by two contributions:

$$\frac{d\sigma^{pA \rightarrow 3jet+X}}{d^3q_1 d^3q_2 d^3q_3} = \int dx_p q(x_p, \mu^2) \left( \frac{d\sigma^{qA \rightarrow qgg+X}}{d^3q_1 d^3q_2 d^3q_3} + \frac{d\sigma^{qA \rightarrow qq\bar{q}+X}}{d^3q_1 d^3q_2 d^3q_3} \right)$$

The two contributions to the two final partonic state:

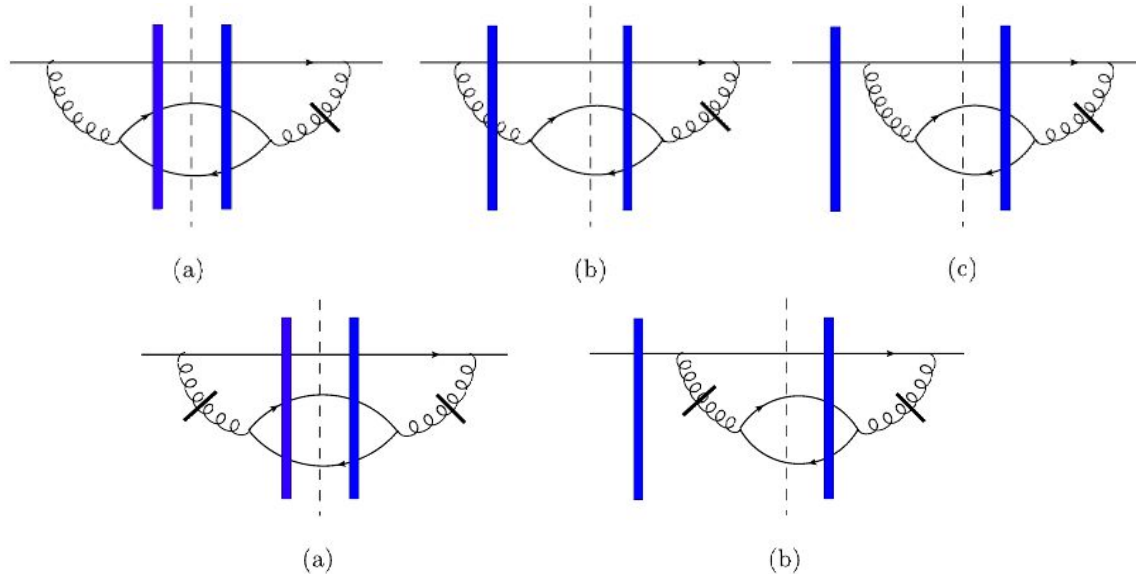
$$\begin{aligned} \frac{d\sigma^{qA \rightarrow qq\bar{q}+X}}{d^3q_1 d^3q_2 d^3q_3} &\equiv \frac{1}{2N_c L} \langle q_\lambda^\alpha(q^+, \mathbf{q} = 0_\perp) | \hat{N}_q(q_1) \hat{N}_q(q_2) \hat{N}_{\bar{q}}(q_3) | q_\lambda^\alpha(q^+, \mathbf{q} = 0_\perp) \rangle_{out}^{(g^2)} \\ &= \frac{1}{2N_c L} \int_{\mathbf{w}, \bar{\mathbf{w}}} \langle \psi_\lambda^\alpha(q^+, \bar{\mathbf{w}}) | \hat{N}_q(q_1) \hat{N}_q(q_2) \hat{N}_{\bar{q}}(q_3) | \psi_\lambda^\alpha(q^+, \mathbf{w}) \rangle_{qq\bar{q}} \end{aligned}$$

$$\begin{aligned} \frac{d\sigma^{qA \rightarrow qgg+X}}{d^3q_1 d^3q_2 d^3q_3} &\equiv \frac{1}{2N_c L} \langle q_\lambda^\alpha(q^+, \mathbf{q} = 0_\perp) | \hat{N}_q(q_1) \hat{N}_g(q_2) \hat{N}_g(q_3) | q_\lambda^\alpha(q^+, \mathbf{q} = 0_\perp) \rangle_{out}^{(g^2)} \\ &= \frac{1}{2N_c L} \int_{\mathbf{w}, \bar{\mathbf{w}}} \langle \psi_\lambda^\alpha(q^+, \bar{\mathbf{w}}) | \hat{N}_q(q_1) \hat{N}_g(q_2) \hat{N}_g(q_3) | \psi_\lambda^\alpha(q^+, \mathbf{w}) \rangle_{qgg} \end{aligned}$$



## The results for the cross section (quark contribution)

The contribution of the quarks to the cross section is given in terms of four blocks which represent two direct (regular / instantaneous gluon both in the amplitude and its conjugate) and two interference (regular - inst.) contributions.



The result is given by:

$$\begin{aligned}
\frac{d\sigma^{qA \rightarrow qq\bar{q}+X}}{d^3q_1 d^3q_2 d^3q_3} &\equiv \frac{\alpha_s^2 C_F N_f}{32\pi^5 (q^+)^2} \delta(q^+ - q_1^+ - q_2^+ - q_3^+) \int_{\bar{x}, \bar{z}, \bar{z}', x, z, z'} e^{-i\mathbf{q}_1 \cdot (\mathbf{x} - \bar{\mathbf{x}}) - i\mathbf{q}_2 \cdot (\mathbf{z} - \bar{\mathbf{z}}) - i\mathbf{q}_3 \cdot (\mathbf{z}' - \bar{\mathbf{z}}')} \\
&\times \left\{ K_{qq\bar{q}}^1 (\bar{x}, \bar{z}, \bar{z}', x, z, z') \left[ \bar{\Theta}_1 \Theta_1 S_{q\bar{q}q\bar{q}q\bar{q}} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - \bar{\Theta}_1 S_{q\bar{q}q\bar{q}g}^{(1)} (\bar{x}, \bar{z}, \bar{z}', x, y) \right. \right. \\
&- \Theta_1 S_{q\bar{q}q\bar{q}g}^{(2)} (\bar{x}, \bar{y}, x, z, z') + \bar{\Theta}_2 \Theta_1 S_{q\bar{q}q\bar{q}} (\bar{w}, x, z, z') + \bar{\Theta}_1 \Theta_2 S_{q\bar{q}q\bar{q}} (\bar{x}, w, \bar{z}', \bar{z}) \\
&+ S_{q\bar{q}gg} (\bar{x}, \bar{y}, x, y) - \bar{\Theta}_2 S_{q\bar{q}g} (\bar{w}, y, x) - \Theta_2 S_{q\bar{q}g} (\bar{x}, w, \bar{y}) + \bar{\Theta}_2 \Theta_2 \mathcal{S} (\bar{w}, w) \Big] \\
&+ K_{qq\bar{q}}^2 (\bar{x}, \bar{z}, \bar{z}', x, z, z') \left[ \Theta_1 S_{q\bar{q}q\bar{q}q\bar{q}} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - S_{q\bar{q}q\bar{q}g}^{(1)} (\bar{x}, \bar{z}, \bar{z}', x, y) \right. \\
&- \Theta_1 S_{q\bar{q}q\bar{q}} (\bar{w}, x, z, z') + \Theta_2 S_{q\bar{q}q\bar{q}} (\bar{x}, w, \bar{z}', \bar{z}) + S_{q\bar{q}g} (\bar{w}, y, x) - \Theta_2 \mathcal{S} (\bar{w}, w) \Big] \\
&+ K_{qq\bar{q}}^2 (x, z, z', \bar{x}, \bar{z}, \bar{z}') \left[ \bar{\Theta}_1 S_{q\bar{q}q\bar{q}q\bar{q}} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - S_{q\bar{q}q\bar{q}g}^{(2)} (\bar{x}, \bar{y}, x, z, z') \right. \\
&+ \bar{\Theta}_2 S_{q\bar{q}q\bar{q}} (\bar{w}, x, z, z') - \bar{\Theta}_1 S_{q\bar{q}q\bar{q}} (\bar{x}, w, \bar{z}', \bar{z}) + S_{q\bar{q}g} (\bar{x}, w, \bar{y}) - \bar{\Theta}_2 \mathcal{S} (\bar{w}, w) \Big] \\
&+ K_{qq\bar{q}}^3 (\bar{x}, \bar{z}, \bar{z}', x, z, z') \left[ S_{q\bar{q}q\bar{q}q\bar{q}} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - S_{q\bar{q}q\bar{q}} (\bar{w}, x, z, z') \right. \\
&- S_{q\bar{q}q\bar{q}} (\bar{x}, w, \bar{z}', \bar{z}) + \mathcal{S} (\bar{w}, w) \Big] \Big\} + (q_1^+ \leftrightarrow q_2^+, q_1 \leftrightarrow q_2) .
\end{aligned}$$

$$\begin{aligned}
S_{q\bar{q}q\bar{q}q\bar{q}}(\bar{x}, \bar{z}, \bar{z}', x, z, z') &\equiv \frac{2}{C_F N_c} \text{tr} \left( V^\dagger(\bar{x}) V(x) t^a t^b \right) \text{tr} \left( V(\bar{z}') t^b V^\dagger(\bar{z}) V(z) t^a V^\dagger(z') \right) \\
&= \frac{1}{2C_F N_c} \left( N_c^2 Q(\bar{x}, x, z', \bar{z}') \mathcal{S}(\bar{z}, z) - \mathcal{H}(\bar{x}, x, z', \bar{z}', \bar{z}, z) - \mathcal{H}(\bar{x}, x, \bar{z}, z, z', \bar{z}') \right. \\
&\quad \left. + \mathcal{S}(\bar{x}, x) Q(\bar{z}, z, z', \bar{z}') \right) \simeq Q(\bar{x}, x, z', \bar{z}') \mathcal{S}(\bar{z}, z),
\end{aligned}$$

$$\begin{aligned}
S_{q\bar{q}q\bar{q}g}^{(1)}(\bar{x}, \bar{z}, \bar{z}', x, y) &\equiv \frac{2}{C_F N_c} \text{tr} \left[ t^a V^\dagger(\bar{x}) V(x) t^d \right] \text{tr} \left[ t^a V^\dagger(\bar{z}) t^c V(\bar{z}') \right] U^{cd}(y) = \frac{1}{2C_F N_c} \\
&\times \left( N_c^2 Q(\bar{x}, x, y, \bar{z}') \mathcal{S}(\bar{z}, y) - \mathcal{H}(\bar{x}, x, y, \bar{z}', \bar{z}, y) - Q(\bar{x}, x, \bar{z}, \bar{z}') + \mathcal{S}(\bar{x}, x) \mathcal{S}(\bar{z}, \bar{z}') \right) \\
&\simeq Q(\bar{x}, x, y, \bar{z}') \mathcal{S}(\bar{z}, y).
\end{aligned}$$

$$\begin{aligned}
S_{q\bar{q}q\bar{q}g}^{(2)}(\bar{x}, \bar{y}, x, z, z') &\equiv \frac{2}{C_F N_c} \text{tr} \left[ t^d V^\dagger(\bar{x}) V(x) t^a \right] \text{tr} \left[ t^c V(z) t^a V^\dagger(z') \right] U^{cd}(\bar{y}) = \frac{1}{2C_F N_c} \\
&\times \left( N_c^2 Q(\bar{x}, x, z', \bar{y}) \mathcal{S}(\bar{y}, z) - \mathcal{H}(\bar{x}, x, \bar{y}, z, z', \bar{y}) - Q(\bar{x}, x, z', z) + \mathcal{S}(\bar{x}, x) \mathcal{S}(z', z) \right) \\
&\simeq Q(\bar{x}, x, z', \bar{y}) \mathcal{S}(\bar{y}, z),
\end{aligned}$$

$$\begin{aligned}
S_{q\bar{q}q\bar{q}}(\bar{w}, x, z, z') &= \frac{2}{C_F N_c} \text{tr} \left[ V^\dagger(\bar{w}) t^b V(x) t^a \right] \text{tr} \left[ V(z) t^a V^\dagger(z') t^b \right] = \frac{1}{2C_F N_c} \\
&\times \left( N_c^2 \mathcal{S}(\bar{w}, z) \mathcal{S}(z', x) - Q(\bar{w}, x, z', z) - Q(\bar{w}, z, z', x) + \mathcal{S}(\bar{w}, x) \mathcal{S}(z', z) \right) \simeq \mathcal{S}(\bar{w}, z) \mathcal{S}(z', x)
\end{aligned}$$

$$K_{qq\bar{q}}^1(\bar{x}, \bar{z}, \bar{z}', x, z, z') \equiv \frac{2\bar{Z}^n (\bar{X}^p + \xi\bar{Z}^p) Z^l (X^j + \xi Z^j)}{\bar{Z}^2 (\bar{X} + \xi\bar{Z})^2 Z^2 (X + \xi Z)^2} \\ \times \left( ((2\xi - 1)^2(\vartheta - 2)^2 + \vartheta^2) \delta^{np} \delta^{lj} + ((\vartheta - 2)^2 + 2\vartheta^2) \delta^{pj} \delta^{nl} - ((2\xi - 1)^2 \vartheta^2 + (\vartheta - 2)^2) \delta^{lp} \delta^{nj} \right)$$

$$K_{qq\bar{q}}^2(\bar{x}, \bar{z}, \bar{z}', x, z, z') \equiv -\frac{4(2 - \vartheta)(1 - \vartheta)(2 - \xi)\xi(1 - \xi) (X \cdot Z + \xi Z^2)}{\left( \xi(1 - \xi)\bar{Z}^2 + (1 - \vartheta) (\bar{X} + \xi\bar{Z})^2 \right) Z^2 (X + \xi Z)^2}$$

$$K_{qq\bar{q}}^3(\bar{x}, \bar{z}, \bar{z}', x, z, z') \equiv \frac{(1 - \vartheta)^2 \xi^2 (1 - \xi)^2}{\left( \xi(1 - \xi)\bar{Z}^2 + (1 - \vartheta) (\bar{X} + \xi\bar{Z})^2 \right) \left( \xi(1 - \xi)Z^2 + (1 - \vartheta) (X + \xi Z)^2 \right)}$$

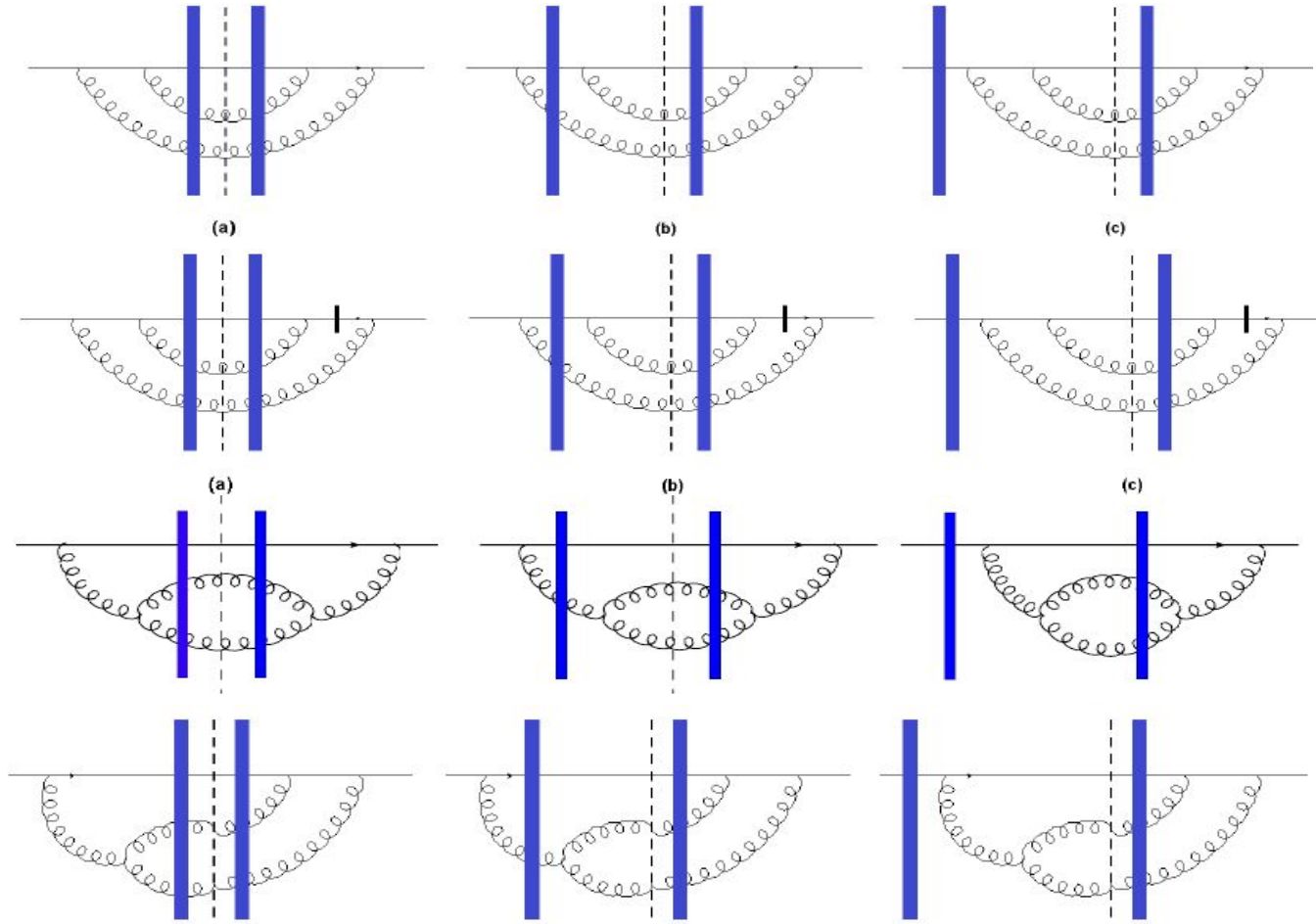
$$\vartheta = \frac{q_2^+ + q_3^+}{q^+}, \quad \xi = \frac{q_3^+}{q_2^+ + q_3^+}$$

At the large  $N_c$  limit:

$$\begin{aligned}
\frac{d\sigma^{qA \rightarrow qq\bar{q}+X}}{d^3q_1 d^3q_2 d^3q_3} &\equiv \frac{\alpha_s^2 N_c N_f}{64\pi^5 (q^+)^2} \delta(q^+ - q_1^+ - q_2^+ - q_3^+) \int_{\bar{x}, \bar{z}, \bar{z}', x, z, z'} e^{-i\mathbf{q}_1 \cdot (\mathbf{x} - \bar{\mathbf{x}}) - i\mathbf{q}_2 \cdot (\mathbf{z} - \bar{\mathbf{z}}) - i\mathbf{q}_3 \cdot (\mathbf{z}' - \bar{\mathbf{z}}')} \\
&\times \{ K_{qq\bar{q}}^1(\bar{x}, \bar{z}, \bar{z}', x, z, z') [\bar{\Theta}_1 \Theta_1 \mathcal{Q}(\bar{x}, x, z', \bar{z}') \mathcal{S}(\bar{z}, z) - \bar{\Theta}_1 \mathcal{Q}(\bar{x}, x, y, \bar{z}') \mathcal{S}(\bar{z}, y) \\
&- \Theta_1 \mathcal{Q}(\bar{x}, x, z', \bar{y}) \mathcal{S}(\bar{y}, z) + \bar{\Theta}_2 \Theta_1 \mathcal{S}(\bar{w}, z) \mathcal{S}(z', x) + \bar{\Theta}_1 \Theta_2 \mathcal{S}(\bar{x}, \bar{z}') \mathcal{S}(\bar{z}, w) \\
&+ \mathcal{Q}(\bar{x}, x, y, \bar{y}) \mathcal{S}(\bar{y}, y) - \bar{\Theta}_2 \mathcal{S}(\bar{w}, x) \mathcal{S}(x, y) - \Theta_2 \mathcal{S}(\bar{x}, \bar{y}) \mathcal{S}(\bar{y}, w) + \bar{\Theta}_2 \Theta_2 \mathcal{S}(\bar{w}, w)] \\
&+ K_{qq\bar{q}}^2(\bar{x}, \bar{z}, \bar{z}', x, z, z') [\Theta_1 \mathcal{Q}(\bar{x}, x, z', \bar{z}') \mathcal{S}(\bar{z}, z) - \mathcal{Q}(\bar{x}, x, y, \bar{z}') \mathcal{S}(\bar{z}, y) \\
&- \Theta_1 \mathcal{S}(\bar{w}, z) \mathcal{S}(z', x) + \Theta_2 \mathcal{S}(\bar{x}, \bar{z}') \mathcal{S}(\bar{z}, w) + \mathcal{S}(\bar{w}, x) \mathcal{S}(x, y) - \Theta_2 \mathcal{S}(\bar{w}, w)] \\
&+ K_{qq\bar{q}}^2(x, z, z', \bar{x}, \bar{z}, \bar{z}') [\bar{\Theta}_1 \mathcal{Q}(\bar{x}, x, z', \bar{z}') \mathcal{S}(\bar{z}, z) - \mathcal{Q}(\bar{x}, x, z', \bar{y}) \mathcal{S}(\bar{y}, z) \\
&+ \bar{\Theta}_2 \mathcal{S}(\bar{w}, z) \mathcal{S}(z', x) - \bar{\Theta}_1 \mathcal{S}(\bar{x}, \bar{z}') \mathcal{S}(\bar{z}, w) + \mathcal{S}(\bar{x}, \bar{y}) \mathcal{S}(\bar{y}, w) - \bar{\Theta}_2 \mathcal{S}(\bar{w}, w)] \\
&+ K_{qq\bar{q}}^3(\bar{x}, \bar{z}, \bar{z}', x, z, z') [\mathcal{Q}(\bar{x}, x, z', \bar{z}') \mathcal{S}(\bar{z}, z) - \mathcal{S}(\bar{w}, z) \mathcal{S}(z', x) \\
&- \mathcal{S}(\bar{x}, \bar{z}') \mathcal{S}(\bar{z}, w) + \mathcal{S}(\bar{w}, w)] \} + (q_1^+ \leftrightarrow q_2^+, q_1 \leftrightarrow q_2)
\end{aligned}$$

Note that the result vanishes (each block of terms in the rectangular brackets separately) when taking the limit  $S \rightarrow 1$ .

# Contribution from the Gluons



## The results for the cross section (gluon contribution)

We split the contribution from the gluons to three parts:

$$\frac{d\sigma^{q \rightarrow qgg}}{d^3q_1 d^3q_2 d^3q_3} = \frac{d\sigma_{aa}^{q \rightarrow qgg}}{d^3q_1 d^3q_2 d^3q_3} + \frac{d\sigma_{bb}^{q \rightarrow qgg}}{d^3q_1 d^3q_2 d^3q_3} + \frac{d\sigma_{ab}^{q \rightarrow qgg}}{d^3q_1 d^3q_2 d^3q_3}$$

The direct part is given by:

$$\frac{d\sigma_{aa}^{q \rightarrow qgg}}{d^3q_1 d^3q_2 d^3q_3} \equiv \frac{1}{2N_c L} \int_{w, \bar{w}} {}^{aa}_{qgg} \langle \psi_\lambda^\alpha(q^+, \bar{w}) | \hat{N}_q(q_1) \hat{N}_g(q_2) \hat{N}_g(q_3) | \psi_\lambda^\alpha(q^+, w) \rangle_{qgg}^a$$

The interference part is given by:

$$\frac{d\sigma_{ab}^{q \rightarrow qgg}}{d^3q_1 d^3q_2 d^3q_3} \equiv \frac{1}{N_c L} \text{Re} \int_{w, \bar{w}} {}^{ab}_{qgg} \langle \psi_\lambda^\alpha(q^+, \bar{w}) | \hat{N}_q(q_1) \hat{N}_g(q_2) \hat{N}_g(q_3) | \psi_\lambda^\alpha(q^+, w) \rangle_{qgg}^b$$



$$\begin{aligned}
\frac{d\sigma_{aa}^{qA \rightarrow qgg+X}}{d^3q_1 d^3q_2 d^3q_3} &\equiv \frac{\alpha_s^2 C_F^2}{8\pi^5 (q^+)^2} \delta(q^+ - q_1^+ - q_2^+ - q_3^+) \int_{\bar{x}, \bar{z}, \bar{z}', x, z, z'} e^{-iq_1 \cdot (x - \bar{x}) - iq_2 \cdot (z - \bar{z}) - iq_3 \cdot (z' - \bar{z}')} \\
&\times \left\{ K_{qgg}^1 (\bar{x}, \bar{z}, \bar{z}', x, z, z') \left[ \bar{\Theta}_3 \Theta_3 S_{q\bar{q}gggg}^{(1)} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - \bar{\Theta}_3 S_{q\bar{q}ggg}^{(1)} (\bar{y}, \bar{z}', x, z, z') \right. \right. \\
&- \Theta_3 S_{q\bar{q}ggg}^{(2)} (\bar{x}, \bar{z}, \bar{z}', y, z) + \bar{\Theta}_4 \Theta_3 S_{q\bar{q}gg}^{(1)} (\bar{y}, \bar{z}', y, z') + \bar{\Theta}_3 \Theta_4 S_{q\bar{q}gg}^{(2)} (\bar{w}, x, z, z') \\
&+ S_{q\bar{q}gg}^{(2)} (\bar{x}, w, \bar{z}', \bar{z}) - \bar{\Theta}_4 S_{q\bar{q}g} (\bar{w}, y, z') - \Theta_4 S_{q\bar{q}g} (\bar{y}, w, \bar{z}') + \bar{\Theta}_4 \Theta_4 \mathcal{S} (\bar{w}, w) \Big] \\
&+ K_{qgg}^2 (\bar{x}, \bar{z}, \bar{z}', x, z, z') \left[ \Theta_3 S_{q\bar{q}gggg}^{(1)} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - S_{q\bar{q}ggg}^{(2)} (\bar{x}, \bar{z}, \bar{z}', y, z) \right. \\
&- \Theta_3 S_{q\bar{q}gg}^{(2)} (\bar{w}, x, z, z') + \Theta_4 S_{q\bar{q}gg}^{(2)} (\bar{x}, w, \bar{z}', \bar{z}) + S_{q\bar{q}g} (\bar{w}, y, z') - \Theta_4 \mathcal{S} (\bar{w}, w) \Big] \\
&+ K_{qgg}^2 (x, z, z', \bar{x}, \bar{z}, \bar{z}') \left[ \bar{\Theta}_3 S_{q\bar{q}gggg}^{(1)} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - S_{q\bar{q}ggg}^{(1)} (\bar{y}, \bar{z}', x, z, z') \right. \\
&+ \bar{\Theta}_4 S_{q\bar{q}gg}^{(2)} (\bar{w}, x, z, z') - \bar{\Theta}_3 S_{q\bar{q}gg}^{(2)} (\bar{x}, w, \bar{z}', \bar{z}) + S_{q\bar{q}g} (\bar{y}, w, \bar{z}') - \bar{\Theta}_4 \mathcal{S} (\bar{w}, w) \Big] \\
&+ K_{qgg}^3 (\bar{x}, \bar{z}, \bar{z}', x, z, z') \left[ S_{q\bar{q}gggg}^{(1)} (\bar{x}, \bar{z}, \bar{z}', x, z, z') - S_{q\bar{q}gg}^{(2)} (\bar{w}, x, z, z') \right. \\
&- S_{q\bar{q}gg}^{(2)} (\bar{x}, w, \bar{z}', \bar{z}) + \mathcal{S} (\bar{w}, w) \Big] \Big\} + (q_2^+ \leftrightarrow q_3^+, q_2 \leftrightarrow q_3).
\end{aligned}$$

$$\Theta_3(x, z, z') \equiv \frac{\vartheta(\xi X - X')^2}{\vartheta(\xi X - X')^2 + \xi(1 - \xi)X^2}$$

$$\Theta_4(x, z, z') \equiv \frac{\xi(1 - \xi)X^2}{\vartheta(\xi X - X')^2 + \xi(1 - \xi)X^2}$$



$$K_{qgg}^1(\bar{x}, \bar{z}, \bar{z}', x, z, z') \equiv \frac{2(1-\vartheta) (1+(1-\vartheta)^2) (1+(1-2\xi)^2) \bar{X} \cdot X \left( \xi \bar{X} - \bar{X}' \right) \cdot (\xi X - X')}{\xi \vartheta^2 \bar{X}^2 X^2 \left( \xi \bar{X} - \bar{X}' \right)^2 (\xi X - X')^2},$$

$$K_{qgg}^2(\bar{x}, \bar{z}, \bar{z}', x, z, z') \equiv \frac{\xi(1-\xi) (\xi X^2 - X \cdot X')}{\sqrt{\vartheta} \left( \vartheta \left( \xi \bar{X} - \bar{X}' \right)^2 + \xi(1-\xi) \bar{X}^2 \right) X^2 (\xi X - X')^2},$$

$$K_{qgg}^3(\bar{x}, \bar{z}, \bar{z}', x, z, z') \equiv \frac{\xi \vartheta (1-\xi)^2}{(1-\vartheta) \left( \vartheta \left( \xi \bar{X} - \bar{X}' \right)^2 + \xi(1-\xi) \bar{X}^2 \right) \left( \vartheta (\xi X - X')^2 + \xi(1-\xi) X^2 \right)}.$$

$$\vartheta = \frac{q_2^+}{q^+}, \quad \xi = \frac{q_1^+}{q_1^+ + q_3^+}.$$

$$\begin{aligned}
S_{q\bar{q}g g g}^{(1)}(\bar{x}, \bar{z}, \bar{z}', x, z, z') &\equiv \frac{1}{C_F^2 N_c} \text{tr} \left[ V^\dagger(\bar{x}) V(x) t^b t^a t^f t^e \right] \left[ U^\dagger(\bar{z}') U(z') \right]^{fa} \left[ U^\dagger(\bar{z}) U(z) \right]^{eb} \\
&\simeq \mathcal{Q}(\bar{x}, x, z, \bar{z}) \mathcal{Q}(z', \bar{z}', \bar{z}, z) \mathcal{S}(\bar{z}', z'),
\end{aligned}$$

$$\begin{aligned}
S_{q\bar{q}g g g}^{(1)}(\bar{y}, \bar{z}', x, z, z') &\equiv \frac{1}{C_F^2 N_c} \text{tr} \left[ V^\dagger(\bar{y}) t^d V(x) t^b t^a t^e \right] \left[ U^\dagger(\bar{z}') U(z') \right]^{ea} U^{db}(z) \\
&\simeq \mathcal{Q}(\bar{y}, \bar{z}', z', z) \mathcal{S}(\bar{z}', x) \mathcal{S}(z, z'),
\end{aligned}$$

$$\begin{aligned}
S_{q\bar{q}g g g}^{(2)}(\bar{x}, \bar{z}, \bar{z}', y, z) &\equiv \frac{1}{C_F^2 N_c} \text{tr} \left[ V^\dagger(\bar{x}) t^d V(y) t^a t^f t^e \right] \left[ U^\dagger(\bar{z}') U(z') \right]^{fa} U^{de}(\bar{z}) \\
&\simeq \mathcal{Q}(z', \bar{z}', \bar{z}, y) \mathcal{S}(\bar{z}', z') \mathcal{S}(\bar{x}, z),
\end{aligned}$$

$$\begin{aligned}
S_{q\bar{q}g g}^{(2)}(\bar{w}, x, z, z') &\equiv \frac{1}{C_F^2 N_c} \text{tr} \left[ V^\dagger(\bar{w}) t^c t^d V(x) t^b t^a \right] U^{db}(z) U^{ca}(z') \\
&= \frac{1}{4C_F^2} \left( N_c^2 \mathcal{S}(\bar{w}, z') \mathcal{S}(z', z) \mathcal{S}(z, x) - \mathcal{S}(\bar{w}, z) \mathcal{S}(z, x) - \mathcal{S}(\bar{w}, z') \mathcal{S}(z', x) + \frac{1}{N_c^2} \mathcal{S}(\bar{w}, x) \right) \\
&\simeq \mathcal{S}(\bar{w}, z') \mathcal{S}(z', z) \mathcal{S}(z, x).
\end{aligned}$$

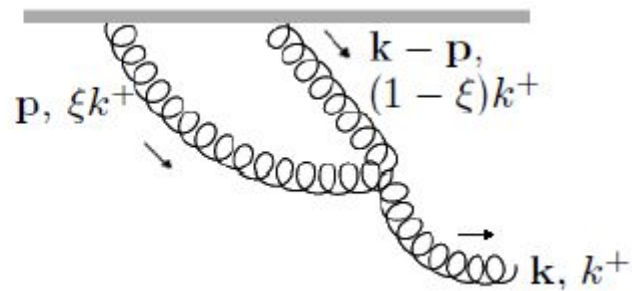
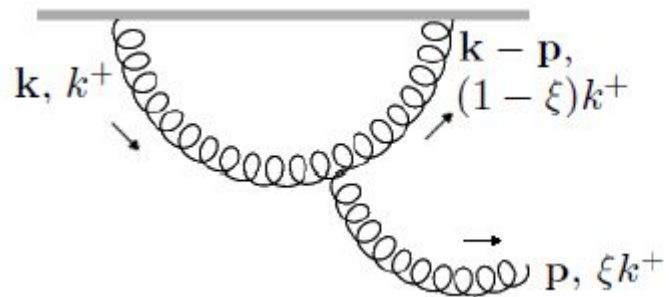
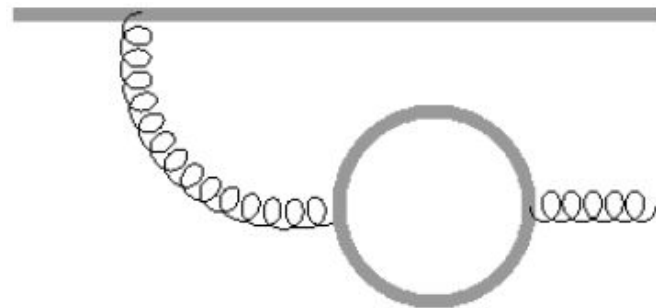
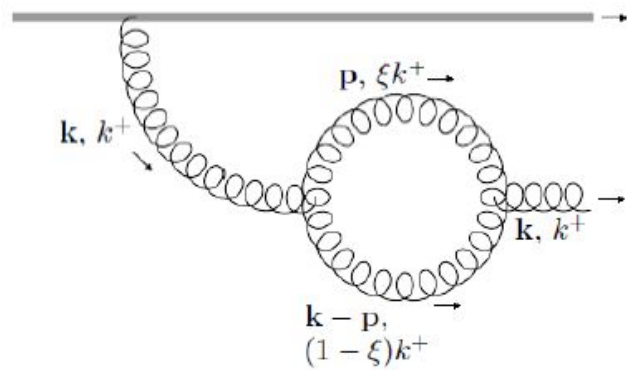
# The forward dijet cross section

In order to allow phenomenology to be reliable, higher order corrections as dictated by pQCD must be included in the result of hep-ph/0708.0231.

The missing part of the new outgoing state (with respect to the trijet calculation) is the part which involves the production of a quark and a gluon together with a loop / virtual correction. In addition, each of the diagrams has a dependence on an IR longitudinal momentum cutoff. This dependence must not be a part of the final result for the cross section.

The NLO outgoing quark state has the following structure:

$$\begin{aligned} |q_\lambda^\alpha(q^+, \mathbf{w})\rangle_{NLO} = & \hat{z}_{NLO} |q_\lambda^\alpha(q^+, \mathbf{w})\rangle + |\Phi_\lambda^\alpha(q^+, \mathbf{w})\rangle_{LO} + |\Phi_\lambda^\alpha(q^+, \mathbf{w})\rangle_{qg} \\ & + |\Phi_\lambda^\alpha(q^+, \mathbf{w})\rangle_{qq\bar{q}} + |\Phi_\lambda^\alpha(q^+, \mathbf{w})\rangle_{qgg}. \end{aligned}$$



The dijet cross section is given by:

$$\frac{d\sigma^{dijet}}{d^3k d^3p} \equiv \frac{1}{2N_c L} \text{NLO} \langle q_\lambda^\alpha(q^+, \mathbf{q} = 0_\perp) | \hat{\mathcal{N}}(k) \hat{\mathcal{N}}(p) | q_\lambda^\alpha(q^+, \mathbf{q} = 0_\perp) \rangle_{\text{NLO}}$$

Which can be written as a sum of five different contributions:

$$\frac{d\sigma^{dijet}}{d^3k d^3p} \equiv \frac{d\sigma^{q \rightarrow qqX}}{d^3k d^3p} + \frac{d\sigma^{q \rightarrow q\bar{q}X}}{d^3k d^3p} + \frac{d\sigma^{q \rightarrow ggX}}{d^3k d^3p} + \frac{d\sigma_1^{q \rightarrow qgX}}{d^3k d^3p} + \frac{d\sigma_2^{q \rightarrow qgX}}{d^3k d^3p}$$

# Summary

- 1) A generalization of the method shown in hep-ph/0708.0231 to all orders is possible by adopting the outgoing state approach.
- 2) We computed the three-parton Fock space components of the light-cone wave function of the incoming quark and its corresponding outgoing state.
- 3) From the above result we managed to deduce the expression for the forward trijet cross section.
- 4) The NLO dijet production cross section calculation is experimentally more important, but its calculation is more tricky since it involves many more contributions, with some of them diverge.