

## Invariant-mass spectrometry

Most of the experimental data I will show come from experiments at NSCL (MSU) using the HiRA apparatus - 14 Si-CsI(TI) E- $\Delta \mathrm{E}$ telescopes. For heavier resonances we the S 800 spectrometer with an annual $\mathrm{Si}-\mathrm{Csi}(\mathrm{TI})$ array instead.


Measured energy and angle of charged decay products to construct invariant-mass spectra

Where is the edge of the chart of Nuclides in this region

Al- 21
Al- 22
91.1 ms


Mg-19 4.0ps

## Na- 18 $1.3 \mathrm{E}-21 \mathrm{~s}$

|  |  |
| :--- | :--- |

Ne- $\mathbf{1 7}$
109.2 ms
$0-12$

FIE-225
F-14
$5.0 \mathrm{E}-225$
$\mathbf{O - 1 3}$
8.58

\section*{| 3.7 |  |
| :---: | :---: |
|  | F |
|  |  |}


| F-15 |  |
| :---: | :---: |
| 4.1 |  |
|  |  |
|  |  |


|  |
| :---: |
| F-15 |
| $1 \mathrm{E}-22 \mathrm{~s}$ |
|  |
| $\mathbf{0 - 1 4}$ |

F-16
$1.1 \mathrm{E}-19$

\section*{| 1.1 |
| :---: |
|  |
|  |
|  |}


$\mathrm{N}-11$
$5.5 \mathrm{E}-22 \mathrm{~s}$
22 s

C
C-1

## 10

| C- |
| :---: |
| 20. |
| E |


| B-9 |
| :---: |
| $8.5 \mathrm{E}-1$ |

## 

| C |
| :---: |
| 126.5 |
| $\mathbf{B}-8$ |
| 770 |
| Be |
| 53.2 |

[-



Al- 23
AI- 24
Al- 2
Al- 26
Al- 27 2.053 s
$* 130.9 \mathrm{~ms}$


The edge of chart of nuclides is diffuse - determined by when the width of resonances become so wide they melt into the continuum.

So what is the maximum width we can consider for an isotope?
In high-energy physics, the W -boson has a decay width of 2 GeV , but this is unrealistic for a nucleus.

Separation of timescales between formation and decay of resonance.
i.e., reaction timescale must be shorter that lifetime of resonance.

Typical reaction time is that in which $100 \mathrm{MeV} / \mathrm{A}$ projectile travels one diameter ( 9 fm ) of target $\sim 7 \times 10^{-23} \mathrm{~s} \quad$ Thus $\Gamma<9 \mathrm{MeV}$.

Decay time cannot be shorter than typical time scale of nuclear motion time for a valence nucleon (Ek $\sim 40 \mathrm{MeV}$ ) to travel a nuclear diameter ( 9 fm ), Thus $\Gamma<6 \mathrm{MeV}$

Experimentally a resonance of width 6 MeV would be hard to find especially if there is some non-resonance background and/or multitude of states which overlap and form a continuum.

Just beyond the proton drip line we find $1 p$ emitters for odd- $Z$ isotopes and $2 p$ emitter for even- $Z$ isotopes


$70 \mathrm{MeV} / \mathrm{A}^{13} \mathrm{O}$ beam
Webb et al PRC 100 (2019) 024306


Correlations in decay can be explained in the time-dependent approach starting with Gamow Coupled Channel wavefunctions. Determined by nuclear structure and final-state interactions. Decay is dominated by the proton $\left(\mathrm{s}_{1 / 2}\right)^{2}$ configuration of the initial wavefunction. Wang et al , J. Phys. G to be published.
${ }^{11} \mathrm{O}->2 \mathrm{p}+{ }^{9} \mathrm{C}$ mirror of ${ }^{11} \mathrm{Li}$


Two-neutron knockout from ${ }^{13} \mathrm{O}$ beam
Webb et al PRL 122 (2019) 122501

Overlapping states:
Decomposition is done with the aid of Gamow Coupled Channels modellots of interesting effects of the continuum here.


Three neutron knockout reactions to resonance states added.
${ }^{17} \mathrm{Ne}->{ }^{16} \mathrm{Ne}_{\text {g.s. }}$
${ }^{13} \mathrm{O} \quad->^{12} \mathrm{O}_{\text {g.s. }}$
${ }^{9} \mathrm{C} \quad->^{8} \mathrm{C}_{\text {g.s. }}$

Nucleon knockout to resonant states is further suppressed compared to the Gade-Tostevin systematics. We suggested that this extra suppression is a result of smaller spectroscopic factors influenced by the continuum coupling - This has been supported with theory calculations including the continuum.
[J. Wylie et al., Phys. Rev. C 104, L061301 (2021)]


Discovery of ${ }^{13} \mathrm{~F}$ formed in a charge-exchange reaction with a ${ }^{13} \mathrm{O}$ beam with the invariant-mass method. Mirror of ${ }^{13} \mathrm{~B}$ discussed by G . Rogachev

Only the $5 / 2^{+}$first excited states was resolved.
Intermediate states in ${ }^{12} \mathrm{O}$ were identified


Charity et al , PRL 1126 (2021) 132501
$4 p$ emitters for even-Z isotopes.


NSCL HiRA experiment PRC 82 041304(R) (2010)

$2 p+\alpha$ subevents from the detected $4 p+\alpha$ events. Six subevents per event. All ${ }^{8} \mathrm{C}_{\text {g.s. }}$ events have a ${ }^{6} \mathrm{Be}_{\text {g.s. }}$ intermediate state.
$2 p+\alpha$ events from a ${ }^{7}$ Be beam following one-neutron knockout
$4 p+\alpha$ events from ${ }^{9} \mathrm{C}$ beam following one neutron knockout

$\frac{0^{+}}{4 \mathrm{p}+\alpha}$

${ }^{8} \mathrm{C}$ excited states?
5 nucleon knockout from a ${ }^{13} \mathrm{O}$ beam


Gamow-Shell-Model predictions J. Wylie, S Wang, W. Nazarewicz

2 protons plus a ${ }^{6} \mathrm{Be}$ core.

Background from ${ }^{12} \mathrm{O}->4 p+2 \alpha$ subtracted
${ }^{18} \mathrm{Mg}$ formed following two-neutron knockout from a ${ }^{20} \mathrm{Mg}$ beam: NSCL PRL 127, 262502 (2021)
${ }^{18} \mathrm{Mg}->4 p+{ }^{14} \mathrm{O} . \quad{ }^{14} \mathrm{O}$ fragment detected in the S 800 spectrometer, protons detected in a Si-CsI(TI) annular counter. Collaboration with Peking University.


Ground and $2^{+}$first excited state identified

Ground-state subevents consistent with decay path consisting of two-steps of prompt $2 p$ decay with a ${ }^{16} \mathrm{Ne}$ intermediate state.

$3 p$ and $4 p$ emitters so far involve sequential steps of $1 p$ and $2 p$ decay. No evidence for prompt $3 p$ and $4 p$ emission.
$5 p$ emitters?


$70 \mathrm{MeV} / \mathrm{A}{ }^{13} \mathrm{O}$ beam - knockout 1 proton and 3 neutrons
$5 p+\alpha$ invariant-mass distribution is quite broad and no clear peaks.

Look for events that $p+{ }^{8} C_{\text {g.s. }}$ decay by gating on the invariant-mass of the $4 p+\alpha$ subevents. (Five subevents for each $5 p+\alpha$ event)


Single peak fit.
Can only fit this as $\mathrm{I}=0$ resonance using a R -matrix lineshape for $p+{ }^{8} \mathrm{C}$.
$\mathrm{Q}_{1 \mathrm{p}}=1.22(6) \mathrm{MeV}$
$\Gamma=2.59(23) \mathrm{MeV}$
$\Gamma>2 \times \mathrm{Q}_{5 \mathrm{p}}$ - subthreshold resonance ( similar to diproton)
More of a final state effect.

Two-peak fit.
Upper peak is at energy of the $1 / 2{ }^{-2}$ state predicted with Gamow Shell Model. (Wyle, Wang, Nazarewicz). As for ${ }^{11} \mathrm{Be}$, we expect an inversion of the $12^{+}$and $1 / 2^{-}$ground and first excited states as the $\mathrm{s}_{1 / 2}$ orbital intrudes in the $p$-shell. Can the lower peak be the $1 / 2+$ state? In the mirror ${ }^{9} \mathrm{He}$, a number of experimental studies report a $12^{+}$ virtual state in the $n+{ }^{8} \mathrm{He}$ system (final-state effect).
The Gamow Shell Model cannot find a real $1 / 2^{+}$resonance. Within the statistical uncertainty we cannot determine if the $1 / 2+$ peak is from a real resonance or a final-state effect.

Do we see a ${ }^{9} \mathrm{~N}$ state?

Option 1) one peak all associated with $\mathrm{s}_{1 / 2}$ strength,
this strength is from a sub-threshold resonance, i.e., final-state interaction

Option 2) two peaks. Upper peak is the $1 / 2^{-}$state in ${ }^{9} \mathrm{~N}$. Within statistics we cannot discriminate if lower peak in fit is from a real resonance or a final-state interaction.

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Gamow Shell Model calculations (J. Wylie, S. Wang, W. Nazarewicz)
1/2 state Q }\mp@subsup{\textrm{Q}}{5\textrm{p}}{}=8.3\textrm{MeV}\quad\Gamma=1.4 Me
Does not predict a 1/2+ ground state
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Have we reached the edge yet?
${ }^{19} \mathrm{Mg} \Gamma=1 \times 10^{-10} \mathrm{MeV}$ (exp.)
${ }^{18} \mathrm{Mg} \Gamma=1.2 \times 10^{-1} \mathrm{MeV}$ (exp.)
Nine orders of magnitude change, extrapolating to ${ }^{17} \mathrm{Mg}$ would give us well over 10 MeV
${ }^{16} \mathrm{Ne} \Gamma=0.8 \times 10^{-3} \mathrm{MeV}$ (prediction by Grigorenko et al.)
${ }^{15} \mathrm{Ne} \Gamma=0.6 \mathrm{MeV}$ (exp.)
Three orders of magnitude change
${ }^{12} \mathrm{O} \Gamma=5 \times 10^{-2} \mathrm{MeV}$ (exp.)
${ }^{11} \mathrm{O} \Gamma=1.3 \mathrm{MeV}$ (exp + theory)
Two orders of magnitude change


Other $5 p$ emitters, or even $6 p$ emitters?


## Summary

Exploration far beyond the proton drip line allows us to explore the role of continuum in nuclear structure.

We have observed 3, 4, and 5-proton emitters at the extreme edge of Chart of Nuclides and more such emitters will be found in heavy isotopes.

The extreme proton-rich edge of the chart of nuclides has been largely found in the region of light nuclei.

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## Backup slides



Fits where $1 / 2^{+}$strength is from the Gamow Coupled Channels time-dependent calculations.

