

Constraining nuclear physics parameters

L_{sym} , K_{sym} and Q_{sat} from astrophysical data

Based on paper: Baillot d'Etivaux, SG, JM et al. 2019

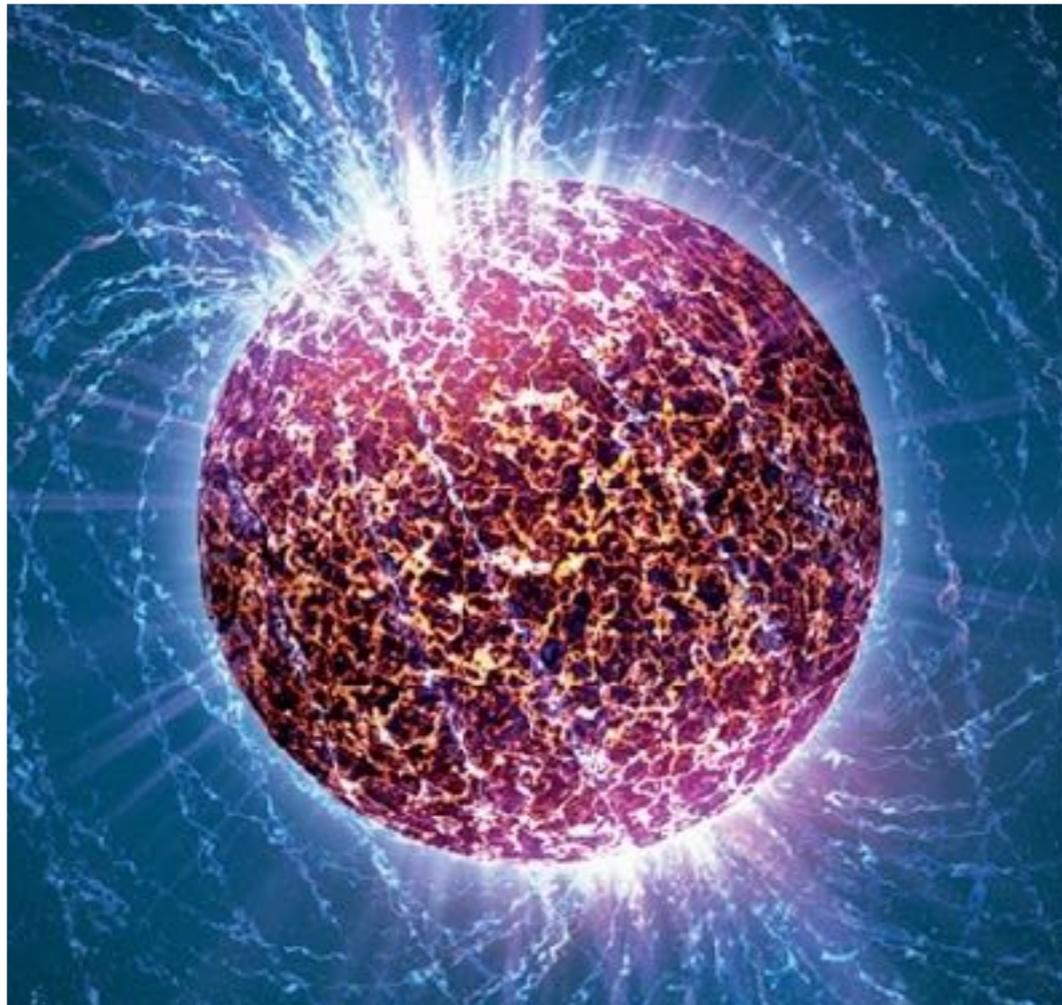
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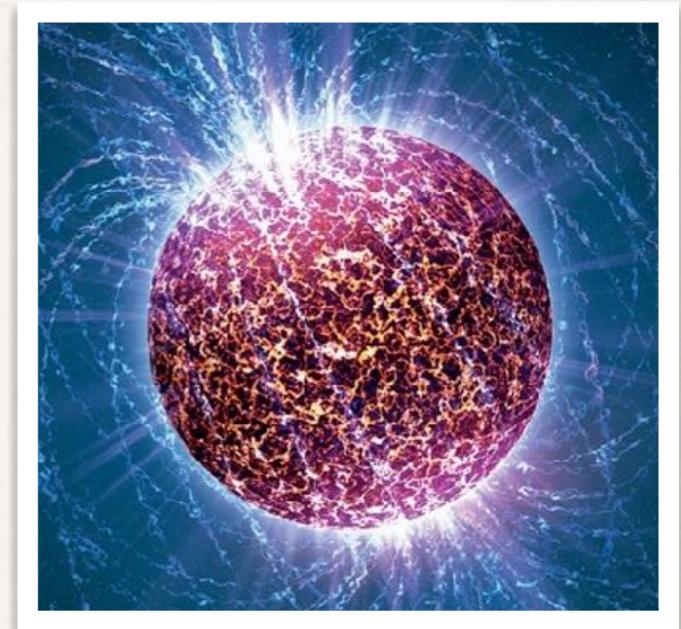


Measuring the radius precisely is rather difficult for neutron stars.

To measure the radius, we need to:

- ♦ observe the surface thermal emission,
- ♦ correctly model this emission,
- ♦ know the distance independently.

$$L = 4\pi R^2 \sigma T_{\text{eff}}^4 \longrightarrow F = \left(\frac{R}{D} \right)^2 \sigma T_{\text{eff}}^4$$

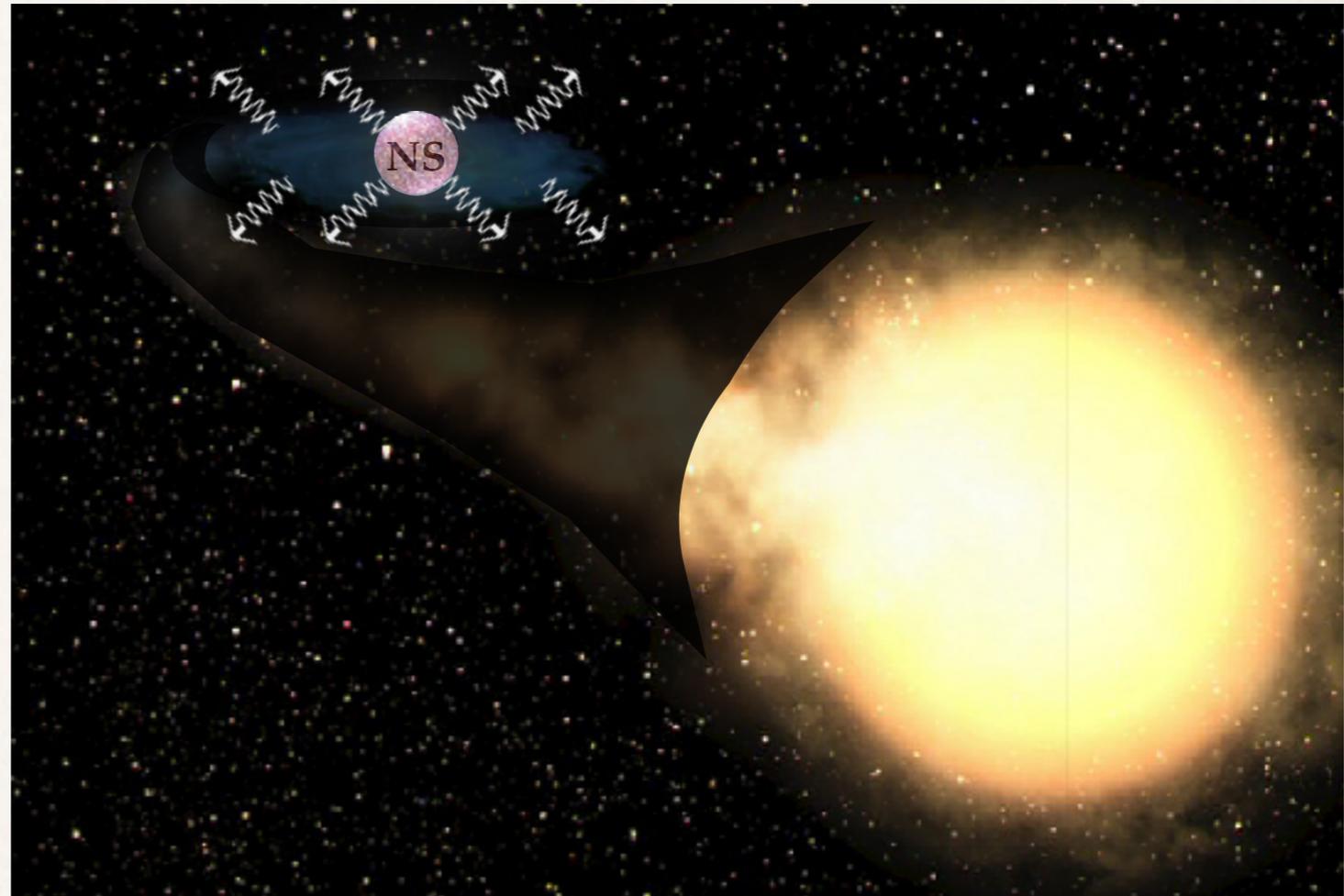


Neutron stars
in quiescent low-mass X-ray
binaries

Quiescent low-mass X-ray binaries are ideal systems for radius measurements.

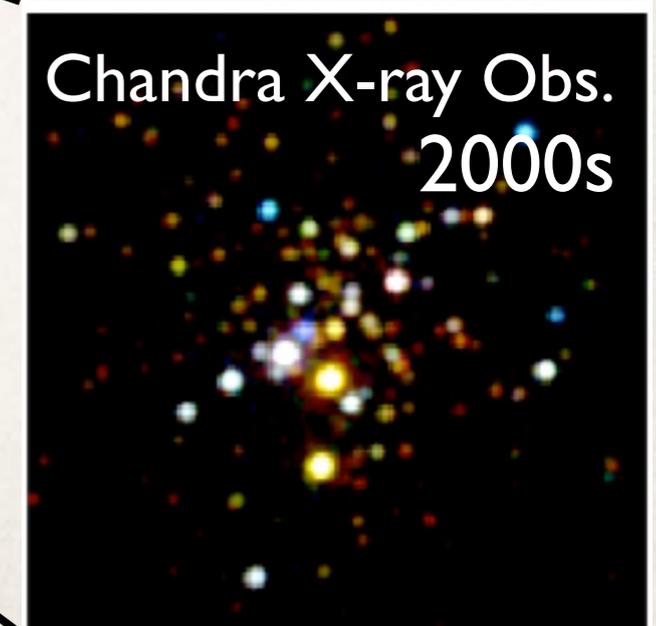
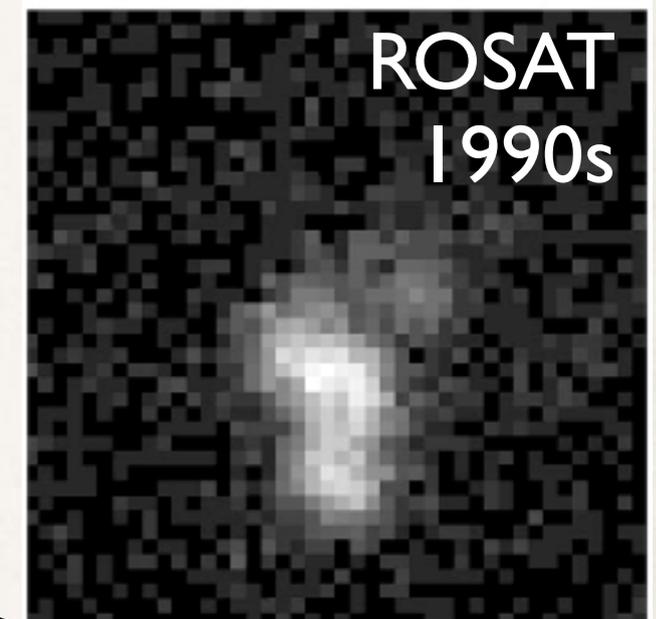
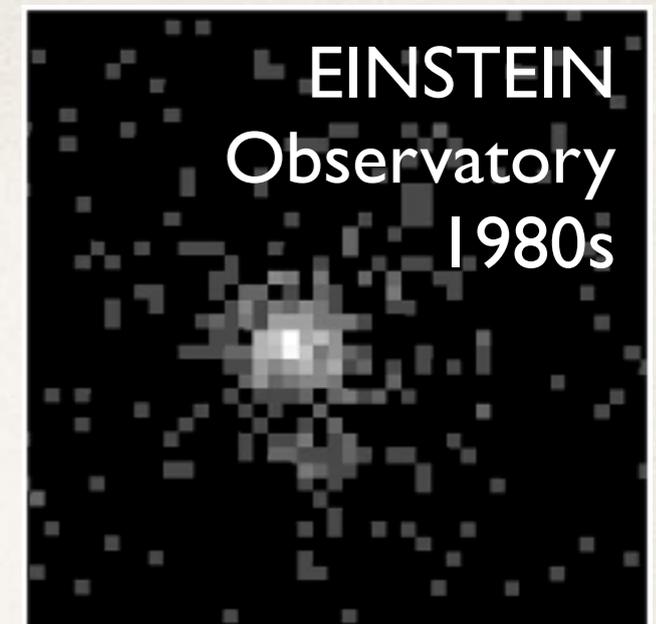
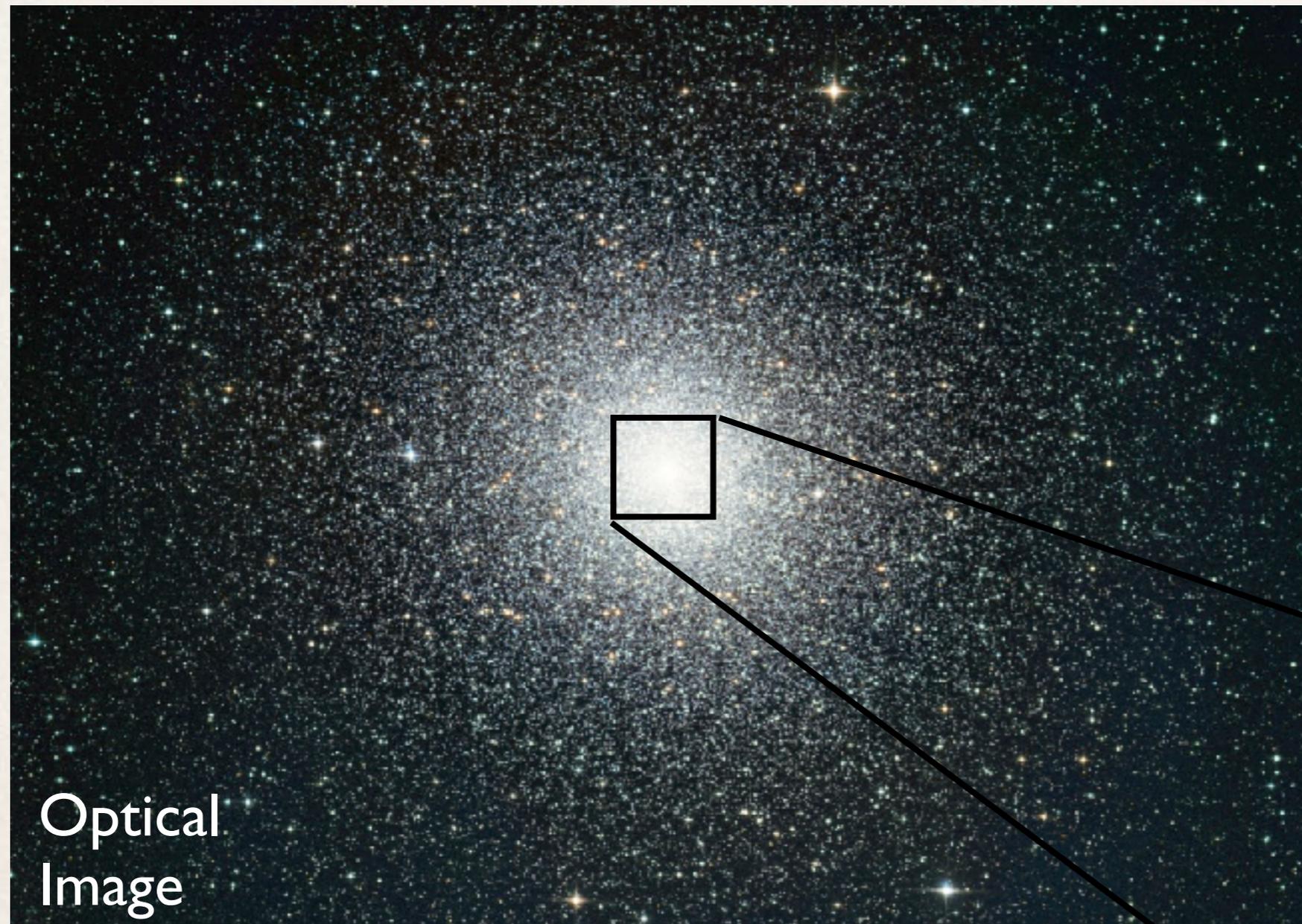
Surface thermal emission at $T_{\text{eff}} \sim 10^6$ K, powered by residual heat from the deep crust radiating outwards through the **atmosphere** with $L_X = 10^{32-33}$ erg/sec

X-ray Spectral fitting of this surface emission gives us T_{eff} and $F_X \propto (R_\infty/D)^2$



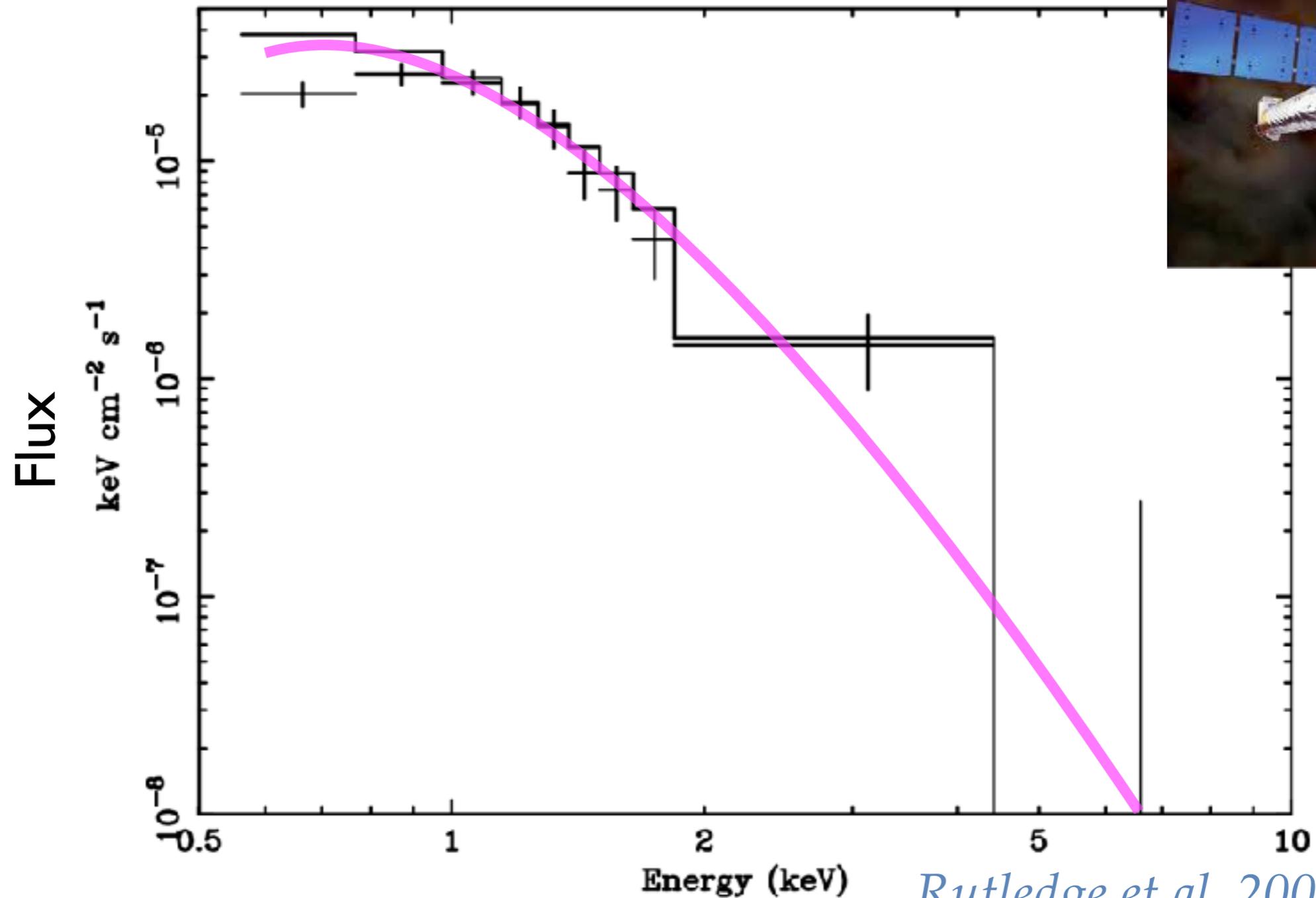
$$R_\infty = R_{\text{NS}} (1 + z) = R_{\text{NS}} \left(1 - \frac{2GM_{\text{NS}}}{R_{\text{NS}} c^2} \right)^{-1/2}$$

Globular clusters host an overabundance of LMXB systems...



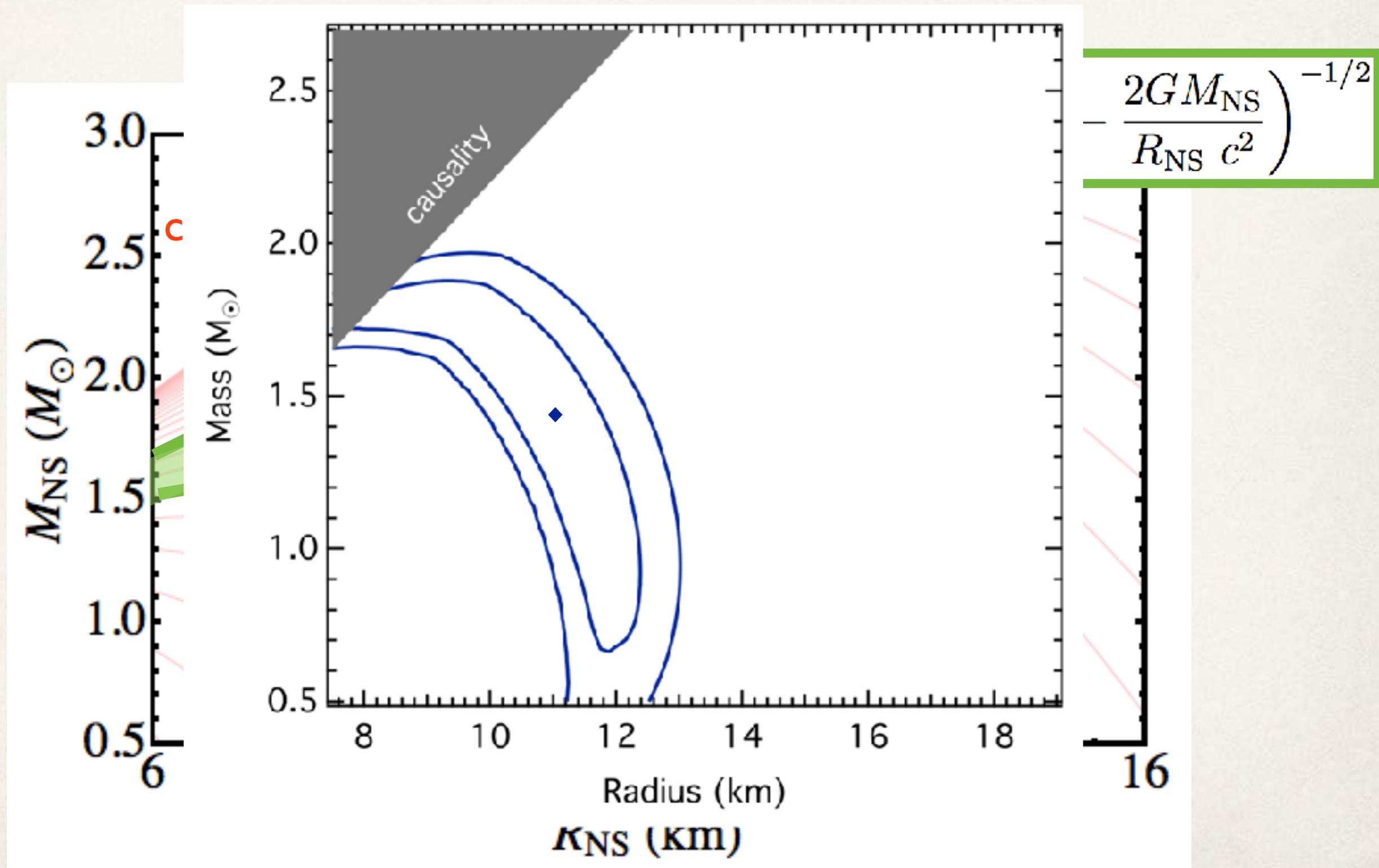
...and they have independently measured distances.

The first globular cluster qLMXB was discovered in Omega Centauri.

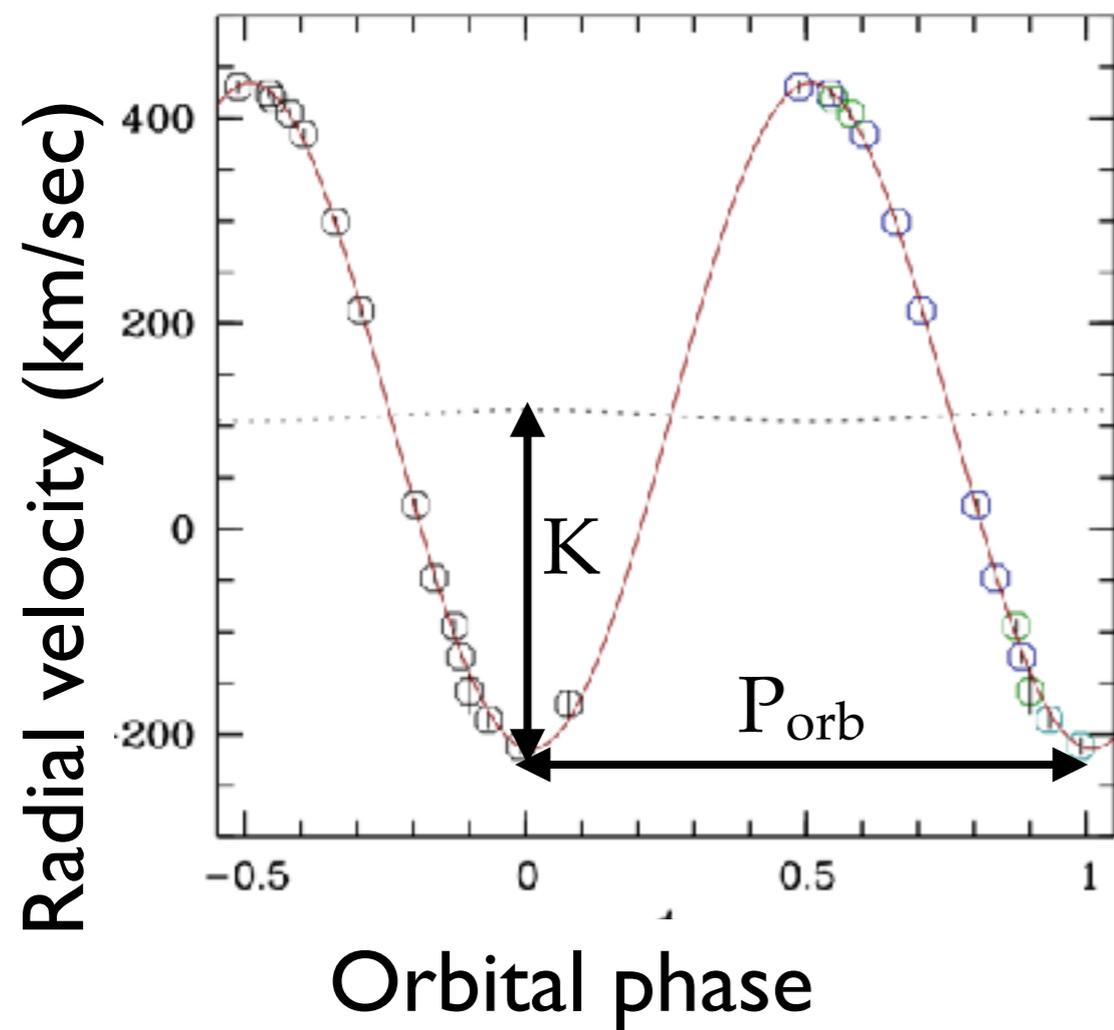


Rutledge et al. 2002

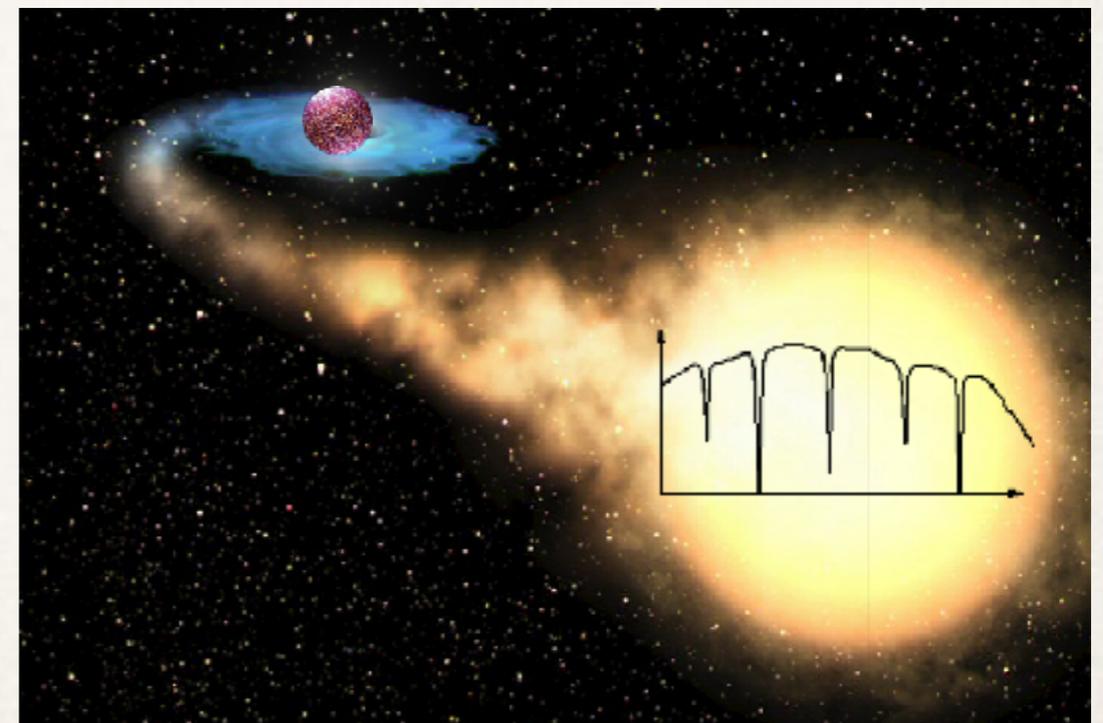
Because of gravitational redshift, the radius is degenerate with the unknown mass.



The degeneracy between M_{NS} and R_{NS} can be broken by measuring M_{NS} independently.

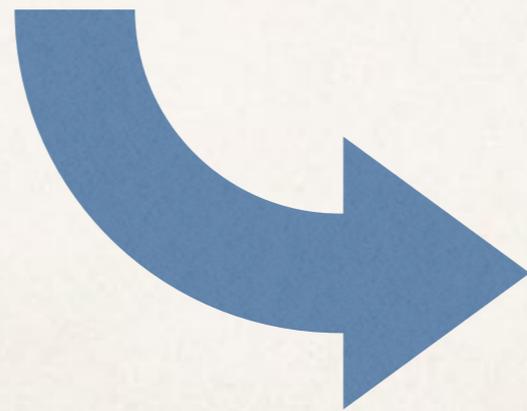
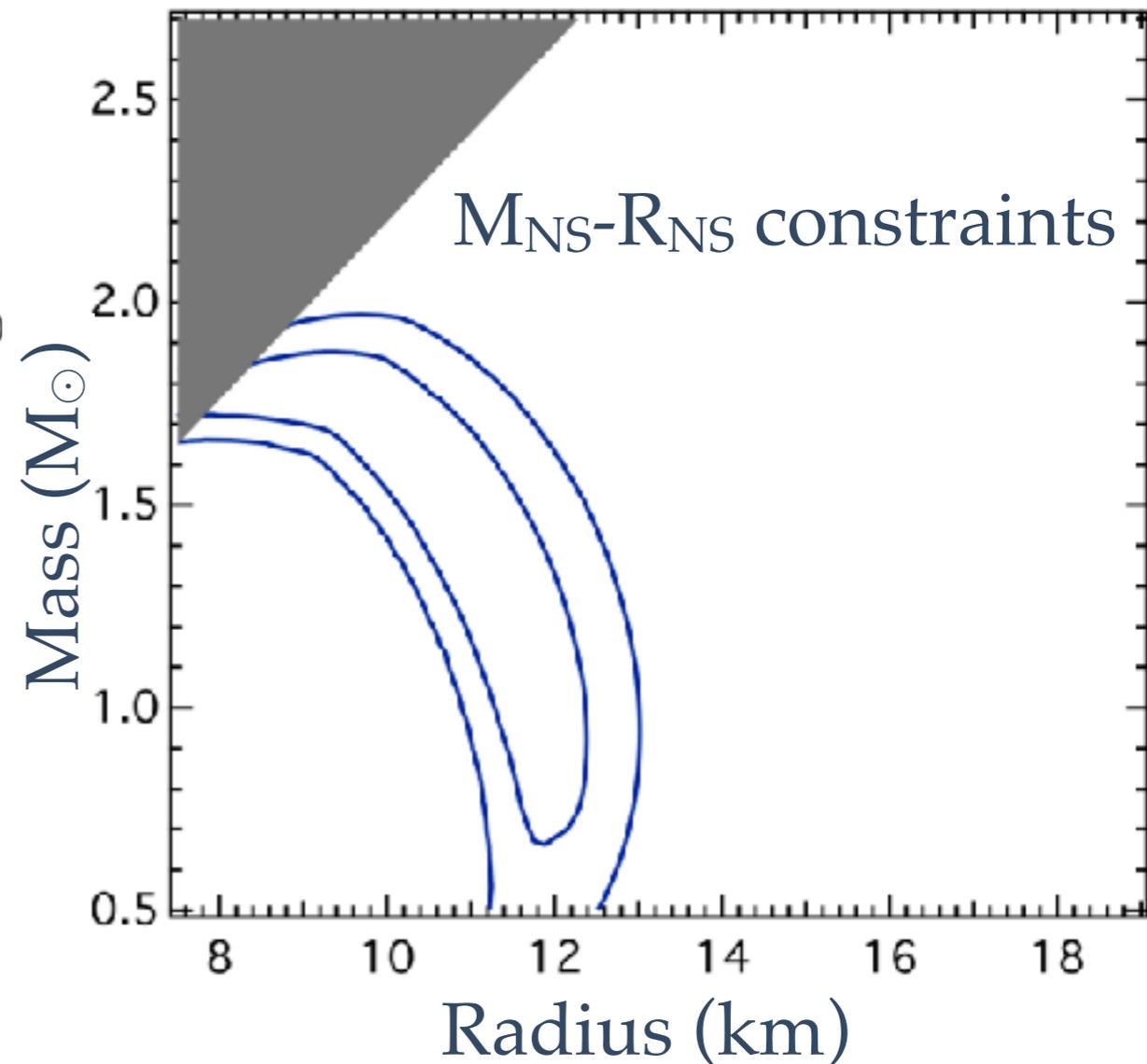
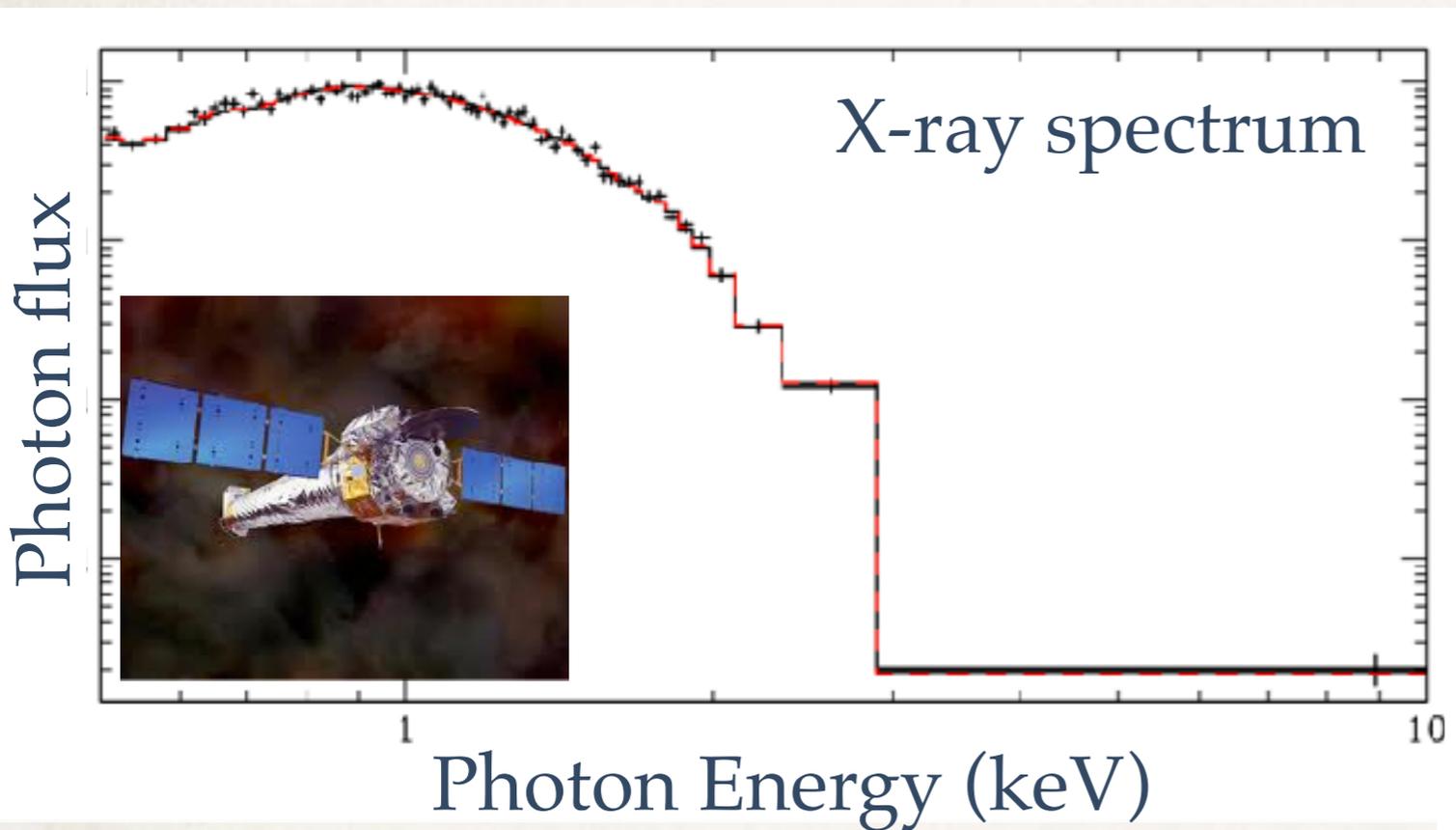


Observing the binary companion to the NS



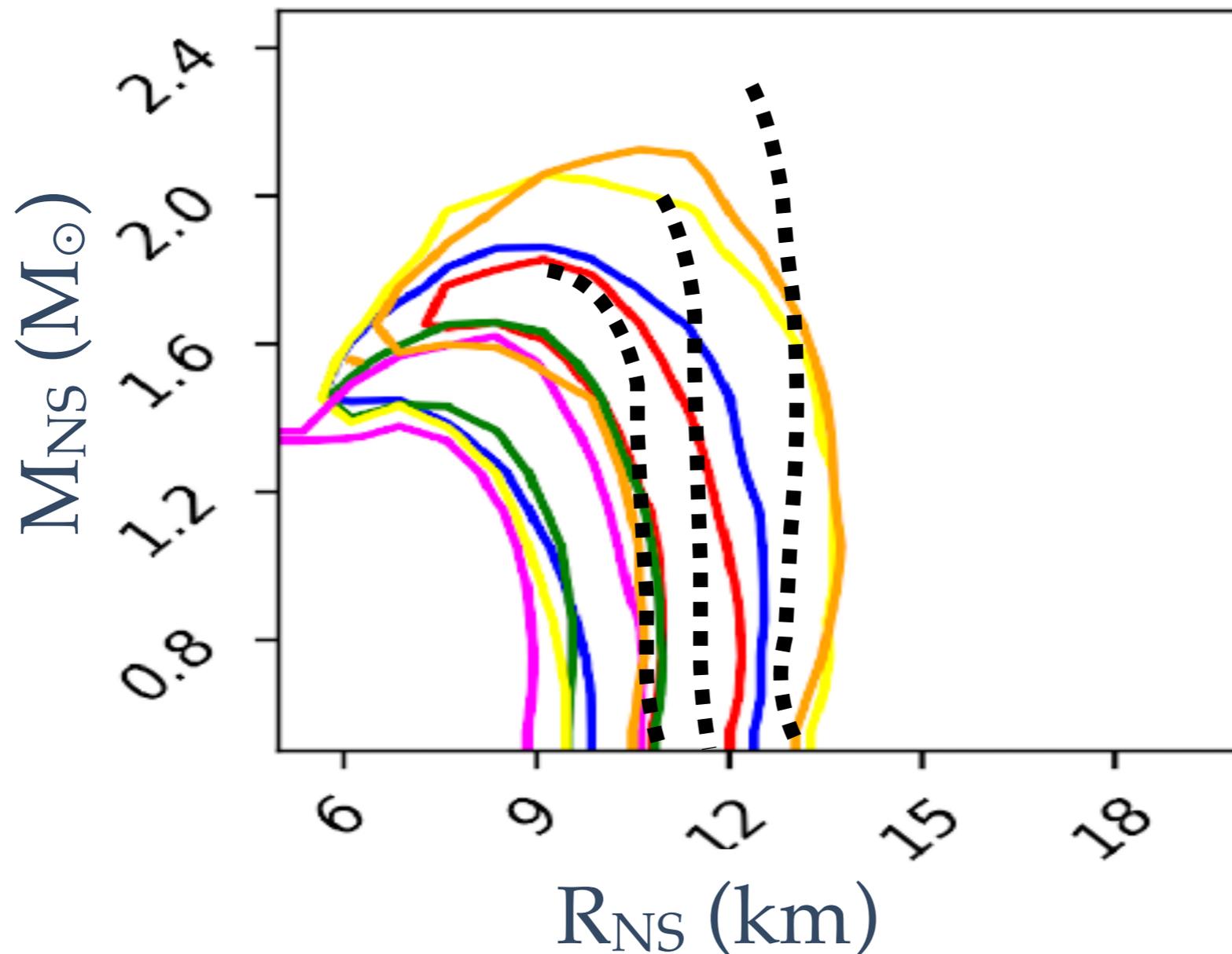
$$\frac{M_{\text{NS}}^3 \sin^3 i}{(M_{\text{NS}} + M_{\text{comp}})^2} = \frac{P_{\text{orb}} K^3}{2\pi G}$$

To sum up, the X-ray spectra of thermally emitting neutron stars is used to extract their M_{NS} and R_{NS} .



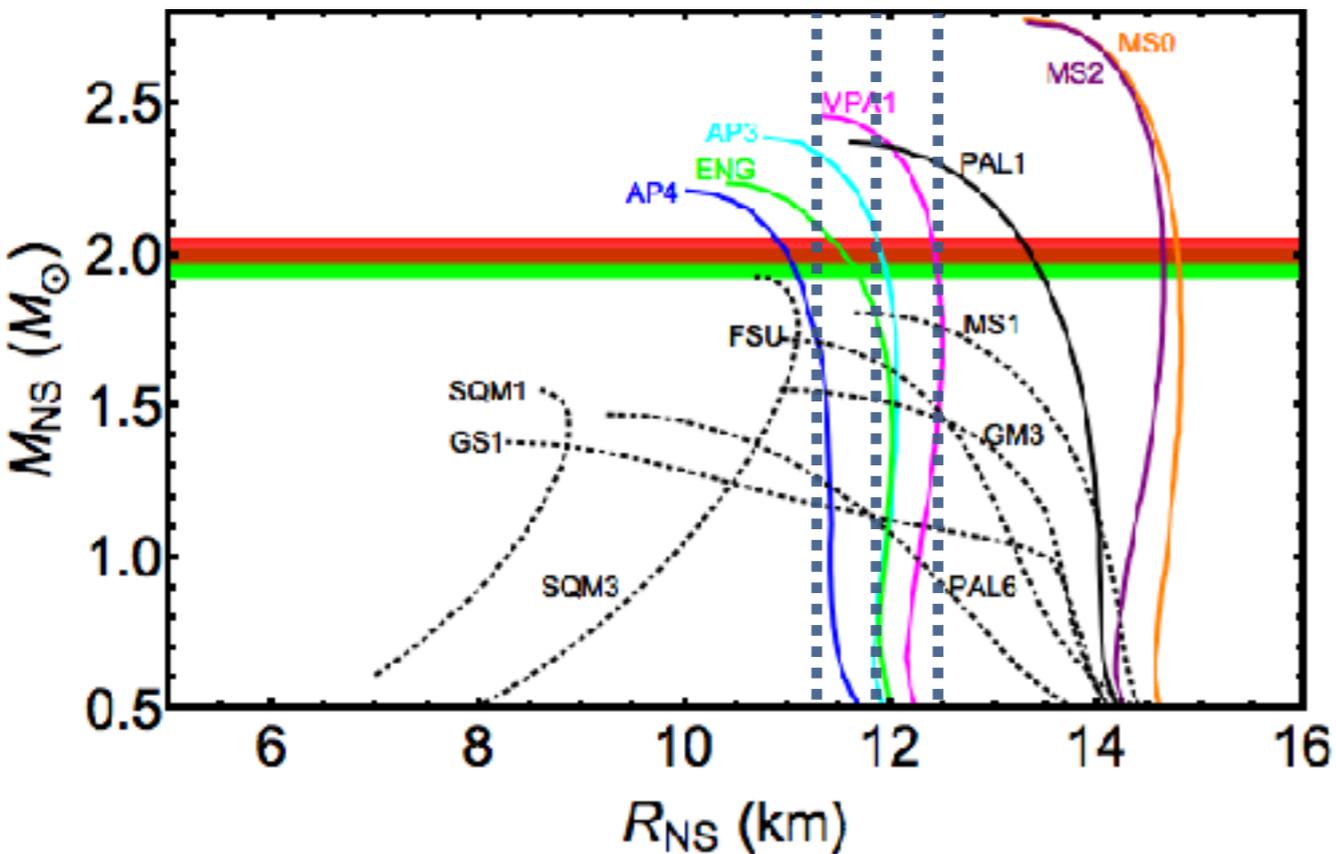
We want to find which equation of state in M-R space is common to all these measurements.

$$R_{\infty} = R_{\text{NS}} (1 + z) = R_{\text{NS}} \left(1 - \frac{2GM_{\text{NS}}}{R_{\text{NS}} c^2} \right)^{-1/2}$$



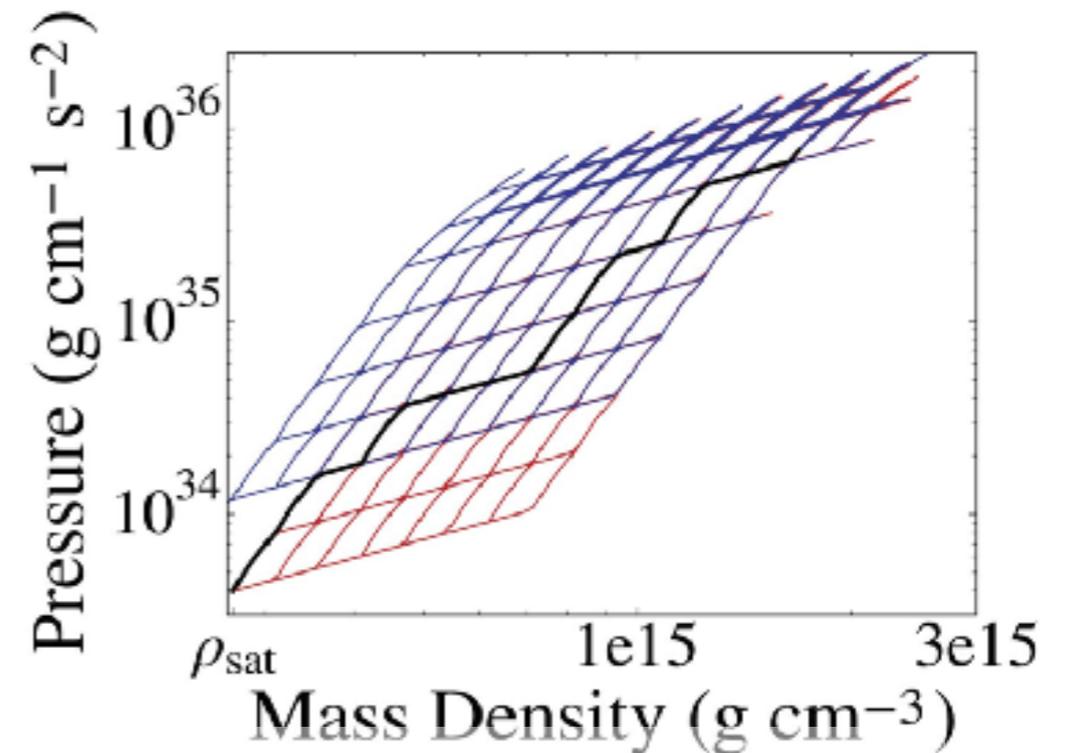
**Seven
sources
with
known
distances.**

A solution consists in combining these observations in a statistical analysis.

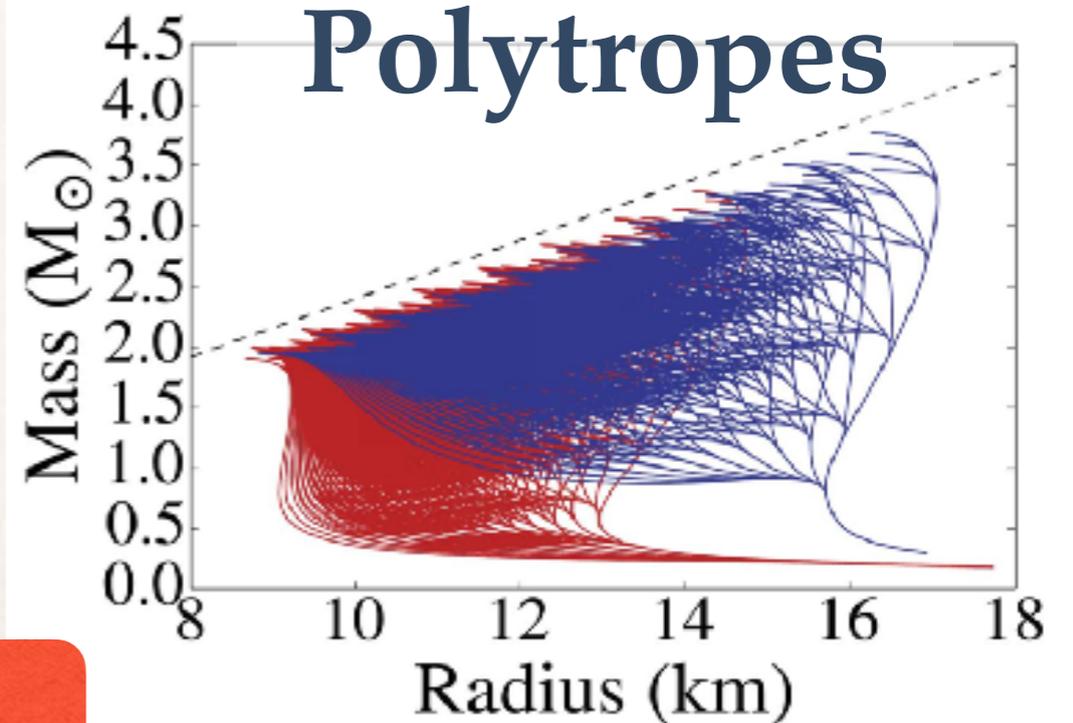


Constant R_{NS}

i.e., the radius is the same for all neutron stars



Polytropes



Analytical
parameterizations

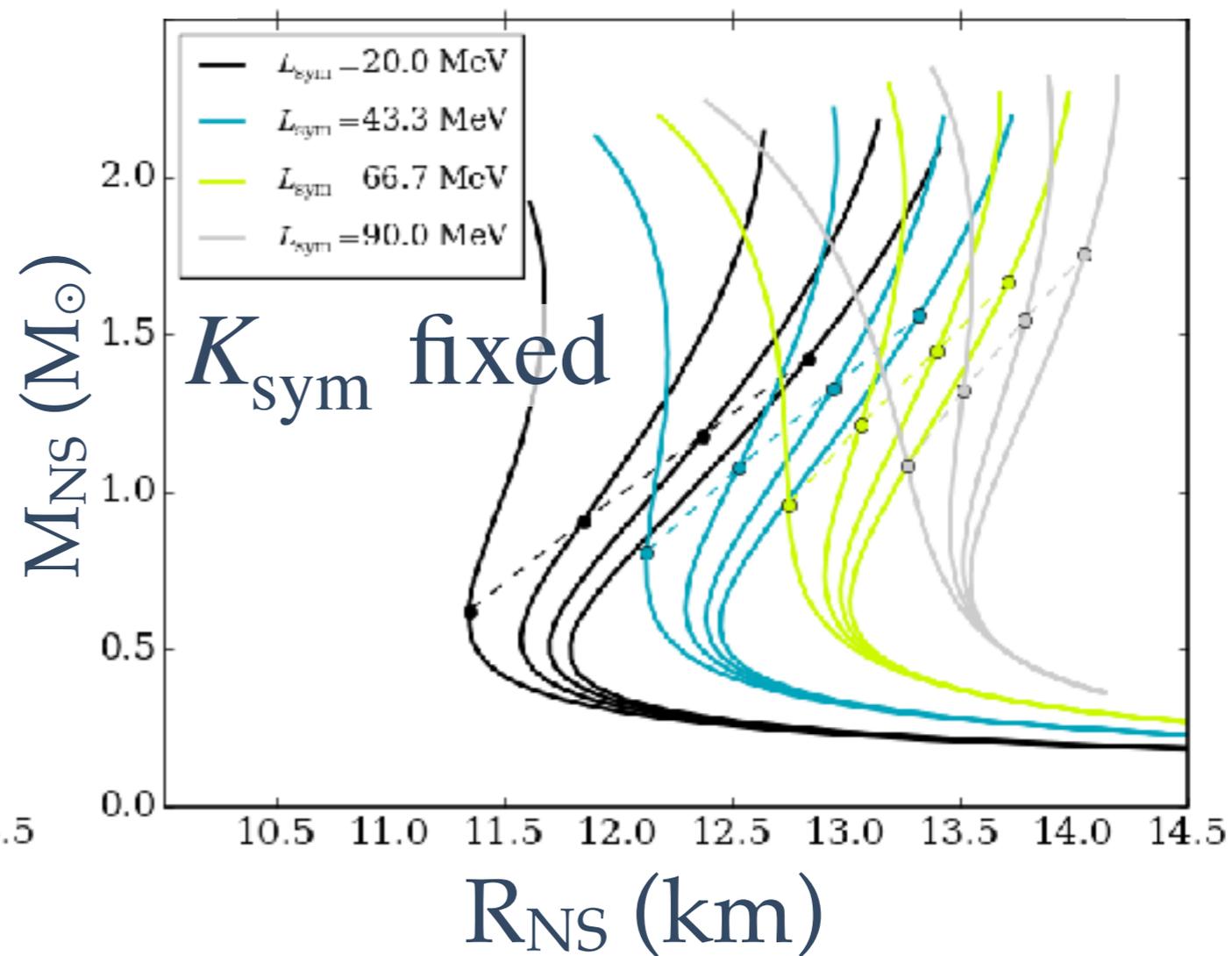
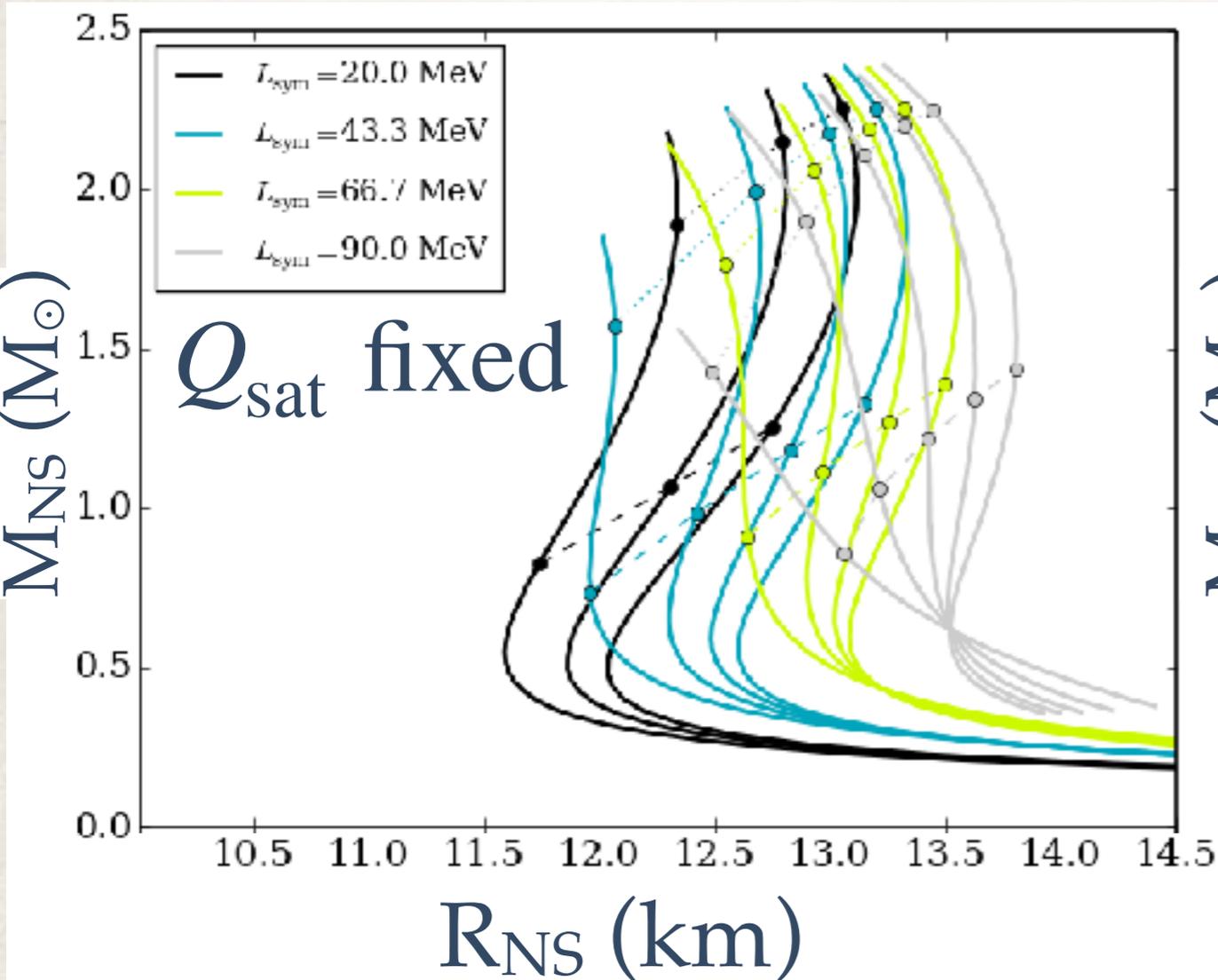
Using a realistic, physically-driven, parameterisation of the equation of state is preferable.

$$e_{\text{sat}} = E_{\text{sat}} + \frac{1}{2}K_{\text{sat}}x^2 + \frac{1}{3!}Q_{\text{sat}}x^3 + \frac{1}{4!}Z_{\text{sat}}x^4 + \dots$$

$$e_{\text{sym}} = E_{\text{sym}} + L_{\text{sym}}x + \frac{1}{2}K_{\text{sym}}x^2 + \frac{1}{3!}Q_{\text{sym}}x^3 + \frac{1}{4!}Z_{\text{sym}}x^4 + \dots$$

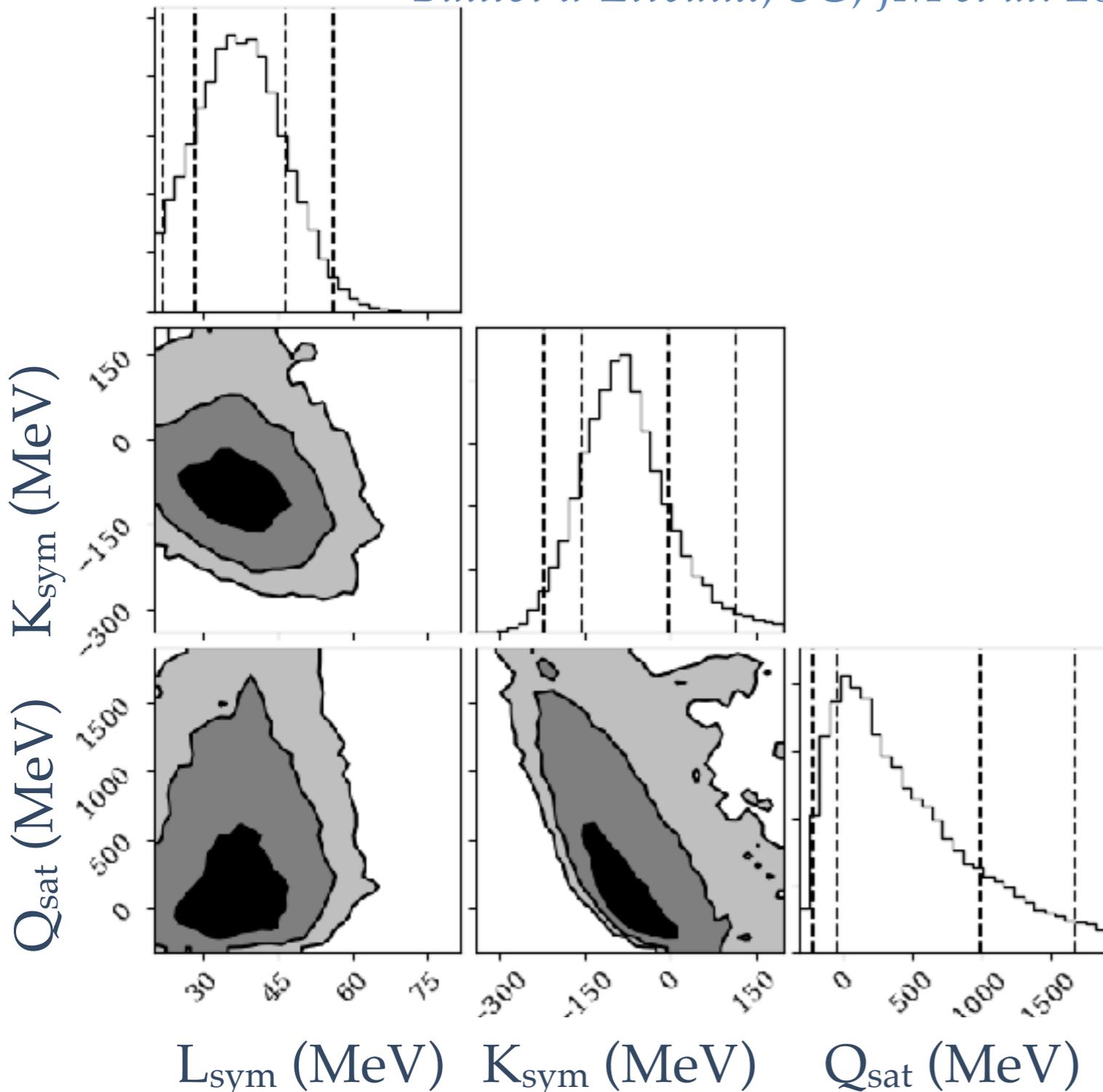
With x

$$x = \frac{n - n_{\text{sat}}}{3n_{\text{sat}}}$$



Our measurements of these three parameters improve on previous estimates.

Baillet d'Etivaux, SG, JM et al. 2019



Our measurements (2σ):

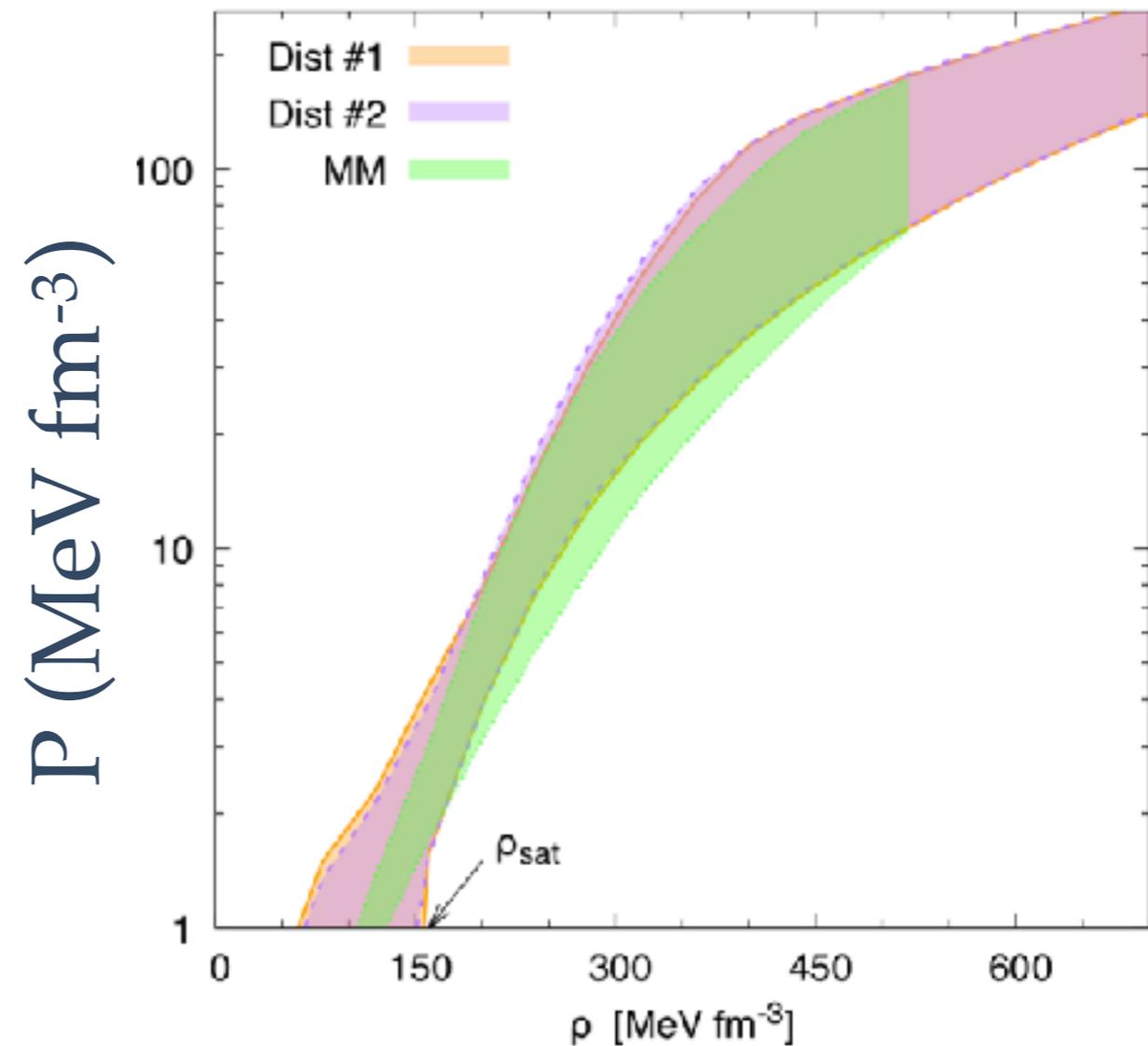
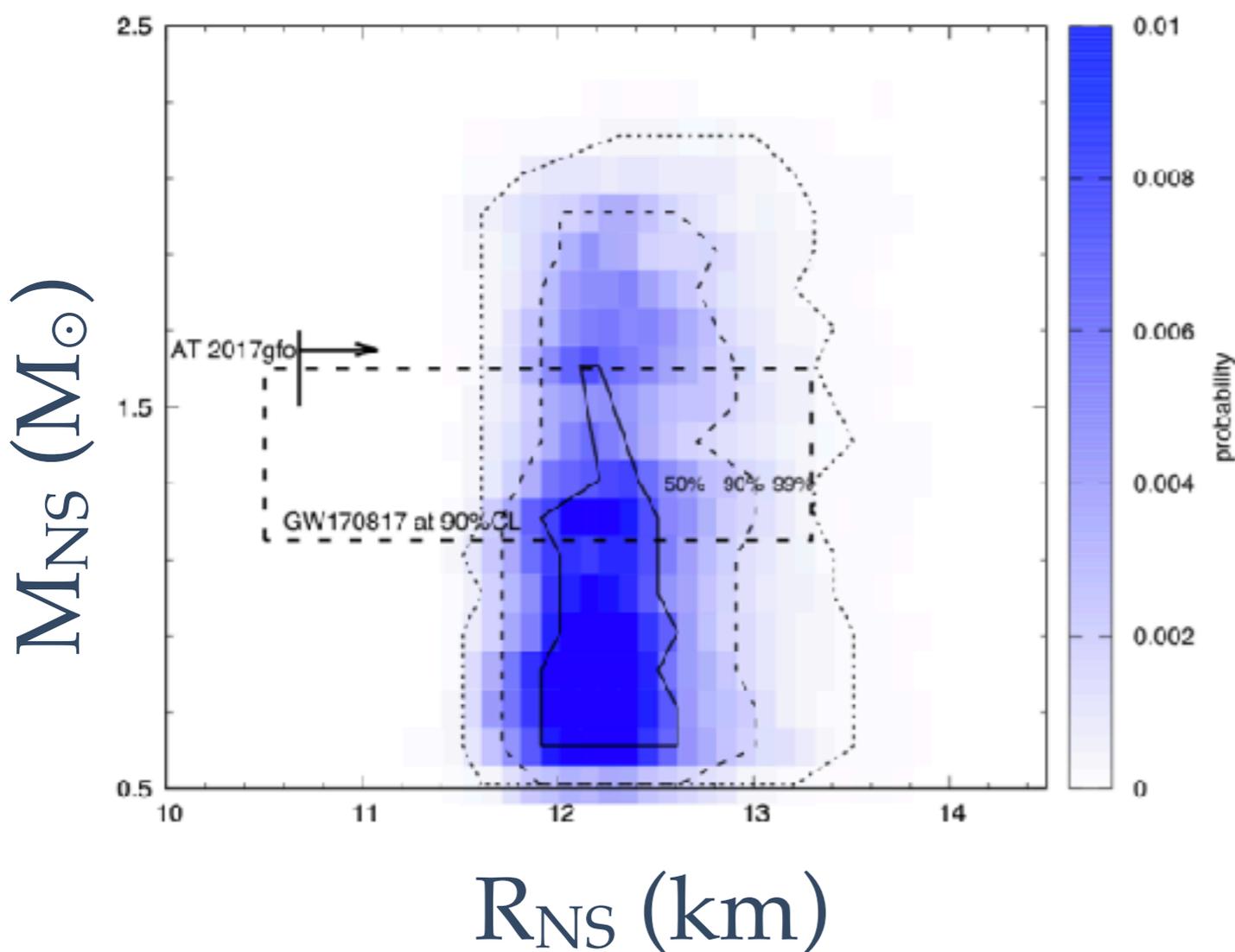
- ◆ $L_{\text{sym}} \sim 25 - 60$ MeV
- ◆ $K_{\text{sym}} \sim -250 - 130$ MeV
- ◆ $Q_{\text{sat}} \sim -200 - 1900$ MeV

For comparison:

Ranges of value from experimental and theoretical estimates

- ◆ $L_{\text{sym}} \sim 20 - 90$ MeV
- ◆ $K_{\text{sym}} \sim -400 - 200$ MeV
- ◆ $Q_{\text{sat}} \sim -1300 - 1900$ MeV

Our analysis results in $M_{\text{NS}}-R_{\text{NS}}$ or in $P-\rho$ space are consistent with other measurements.



Summary

- ◆ By applying the meta-model of Margueron et al. (2018) directly to astrophysical data, we extract measurements of the parameters L_{sym} , K_{sym} and Q_{sat} :

$$L_{\text{sym}} = 37.2^{+9.2}_{-8.9} \text{ MeV}$$

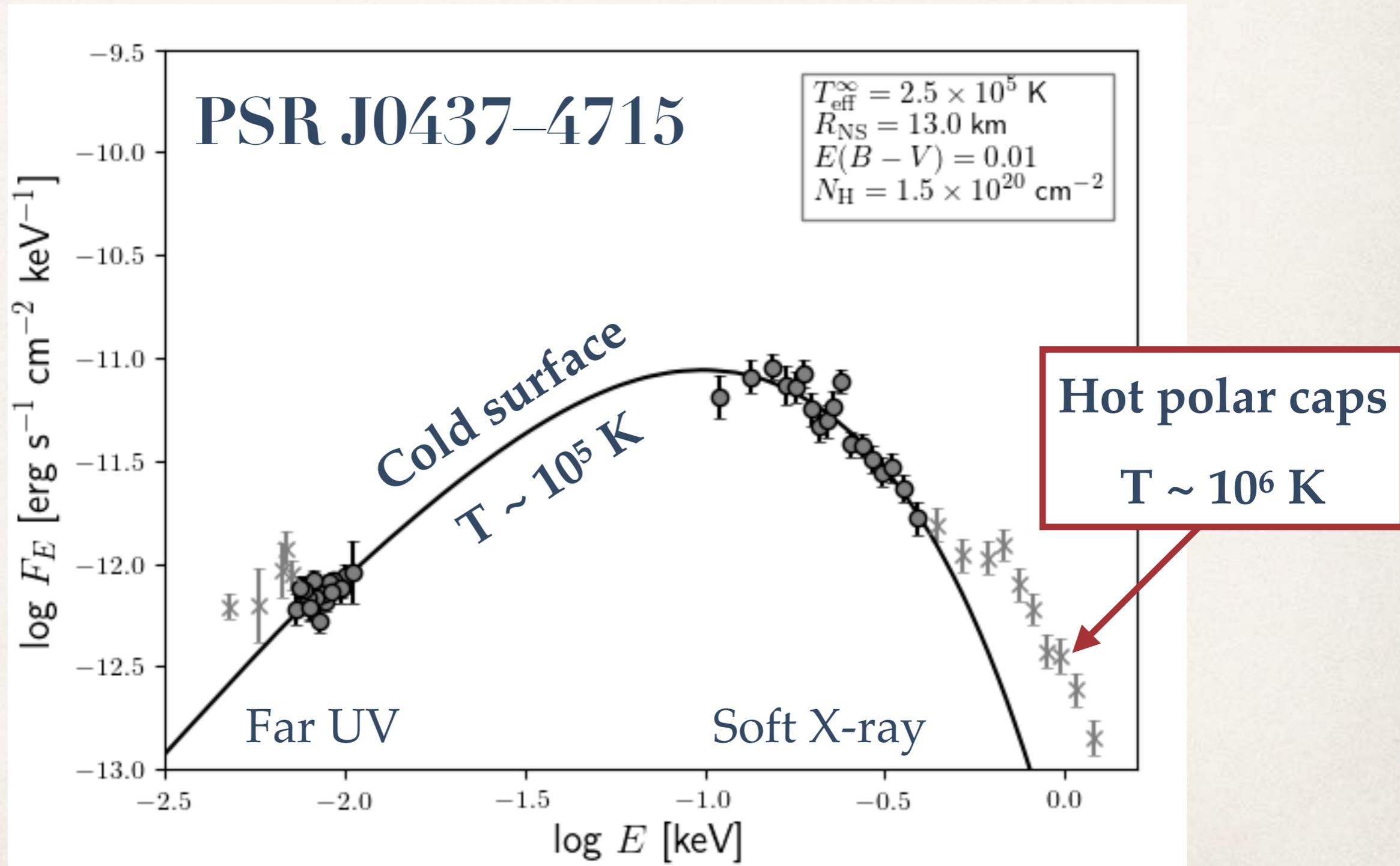
$$K_{\text{sym}} = -85^{+82}_{-70} \text{ MeV} \quad \longrightarrow \quad R_{\text{NS}} = 12.4 \pm 0.4 \text{ km}$$

$$Q_{\text{sat}} = 318^{+673}_{-366} \text{ MeV}$$

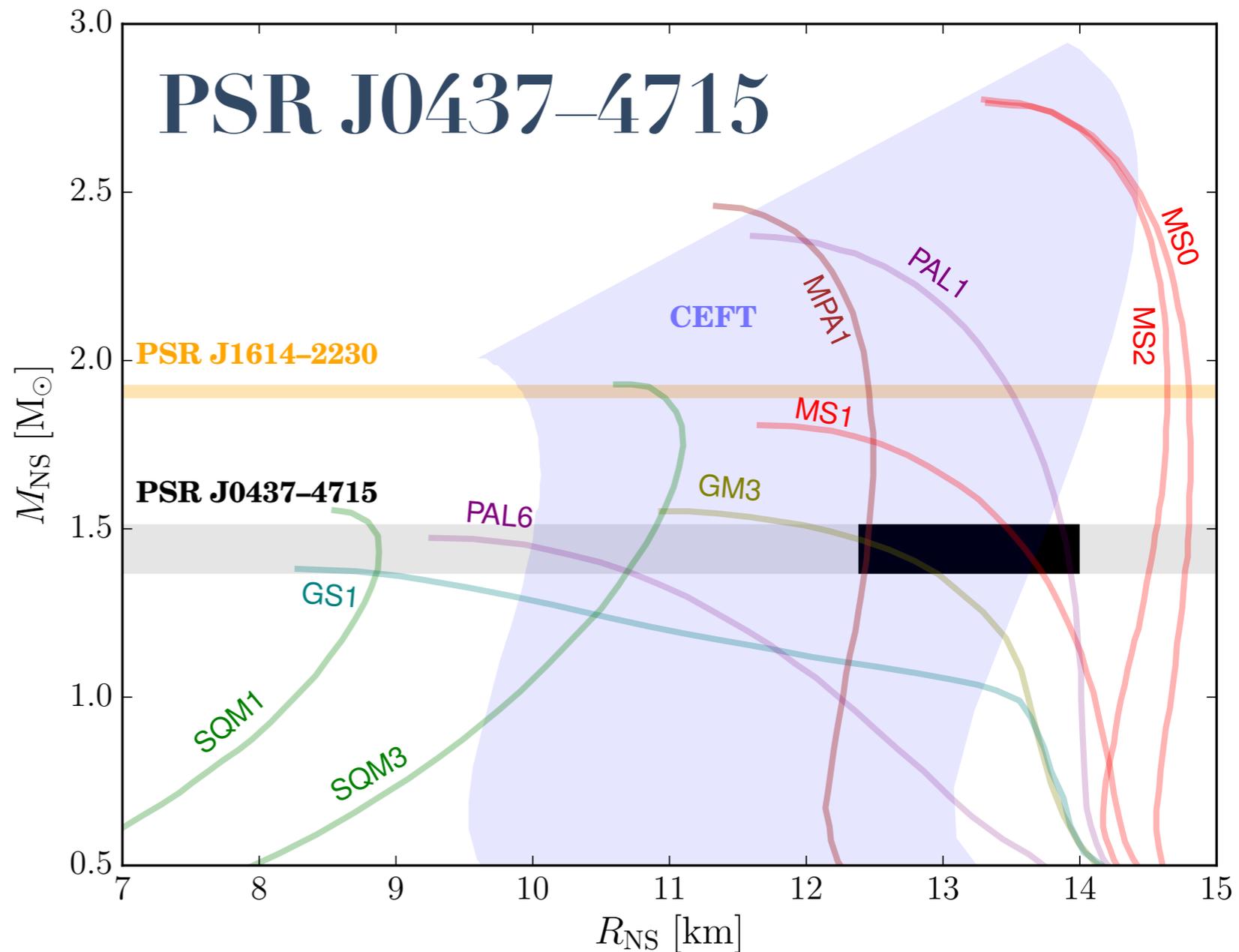
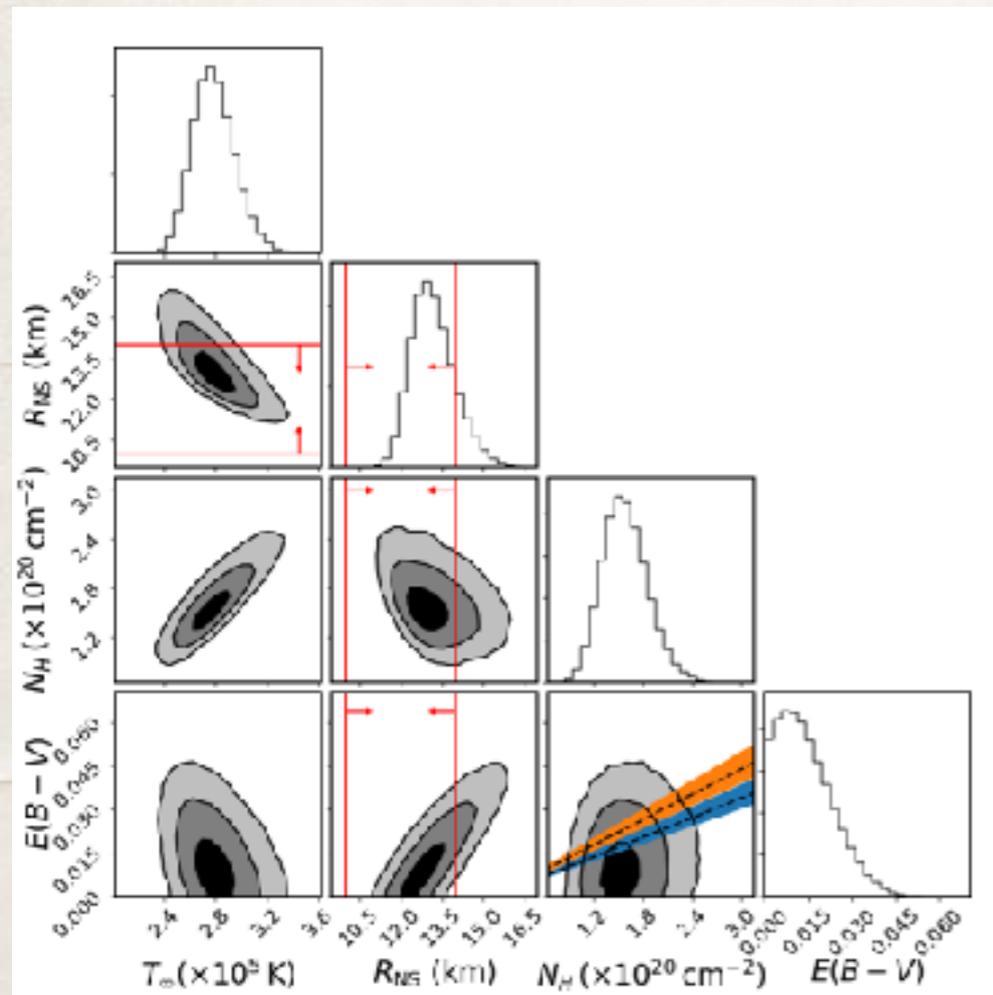
Baillet d'Etivaux, SG, JM et al. 2019

- ◆ This requires assuming that **all neutron stars are described by the same equation of state.**

The cold surface of millisecond pulsars can also be used to measure their radius.

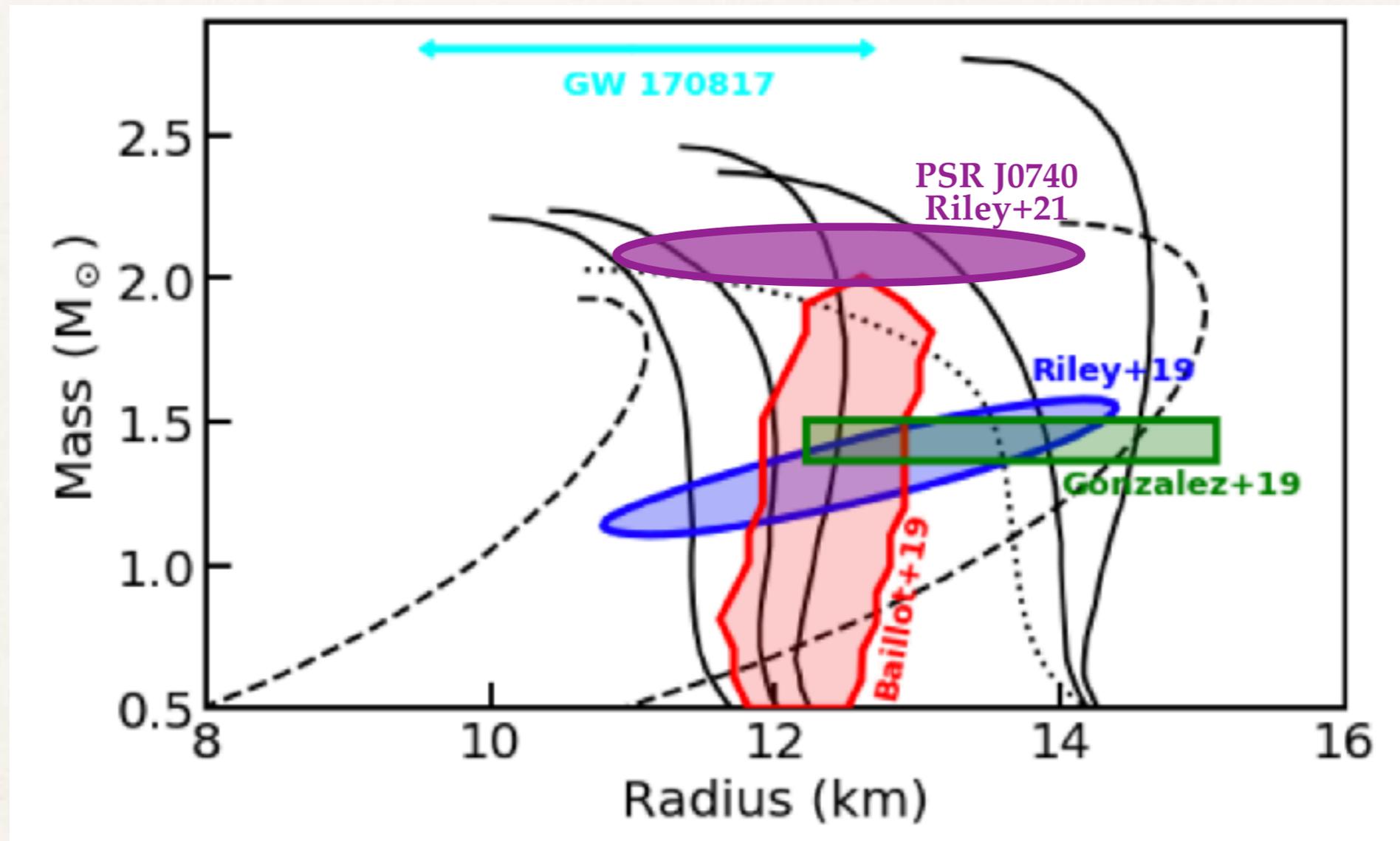


The cold surface of millisecond pulsars can also be used to measure their radius.



Conclusion

So far, results from different approaches are consistent with each other.



Gonzalez-Canuilef, SG et al. 2019

Baillot-d'Etivaux, SG, JM et al. 2019

Riley et al. 2019

Riley et al. 2021

Abbott et al. 2018