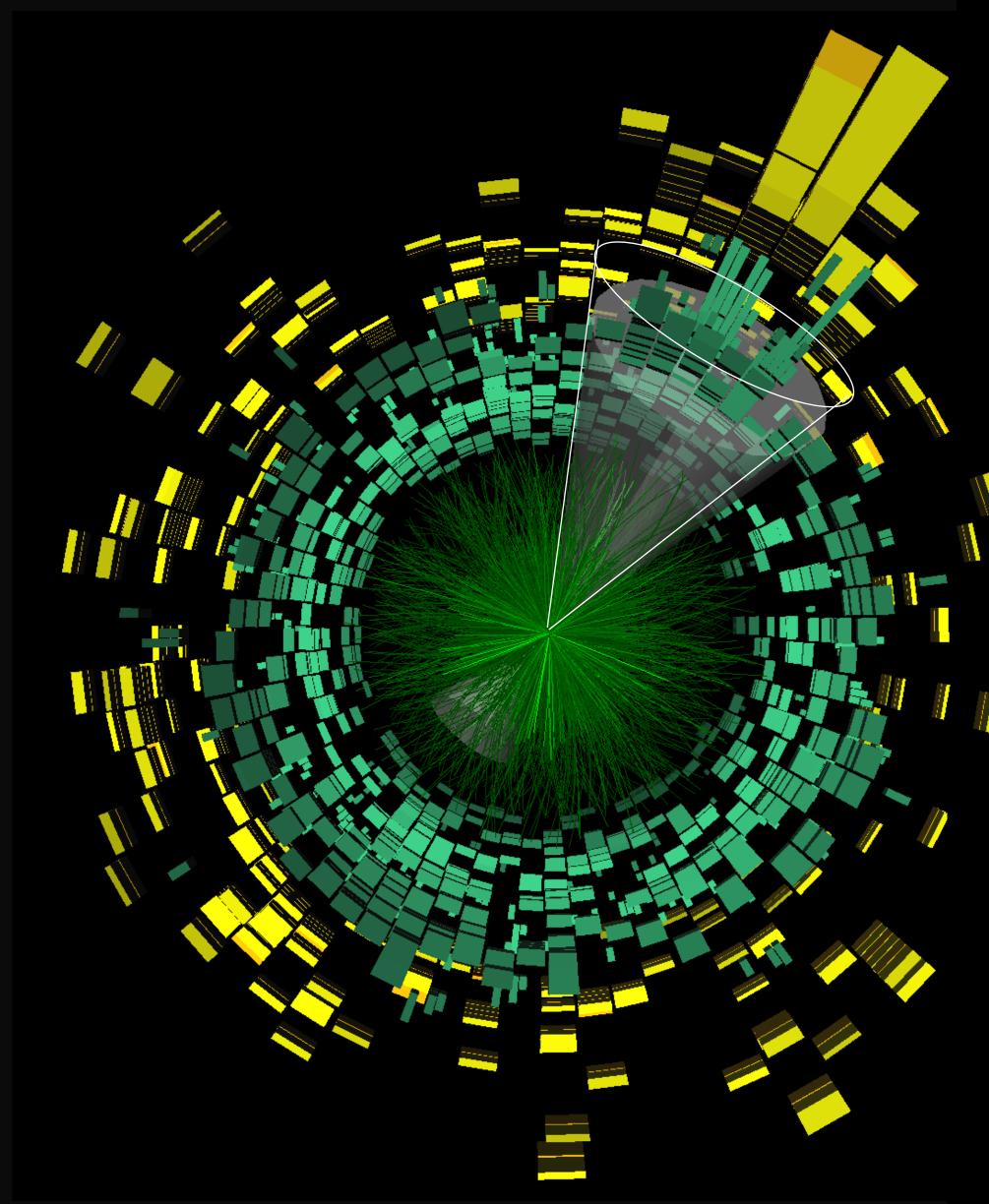
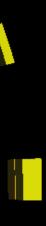
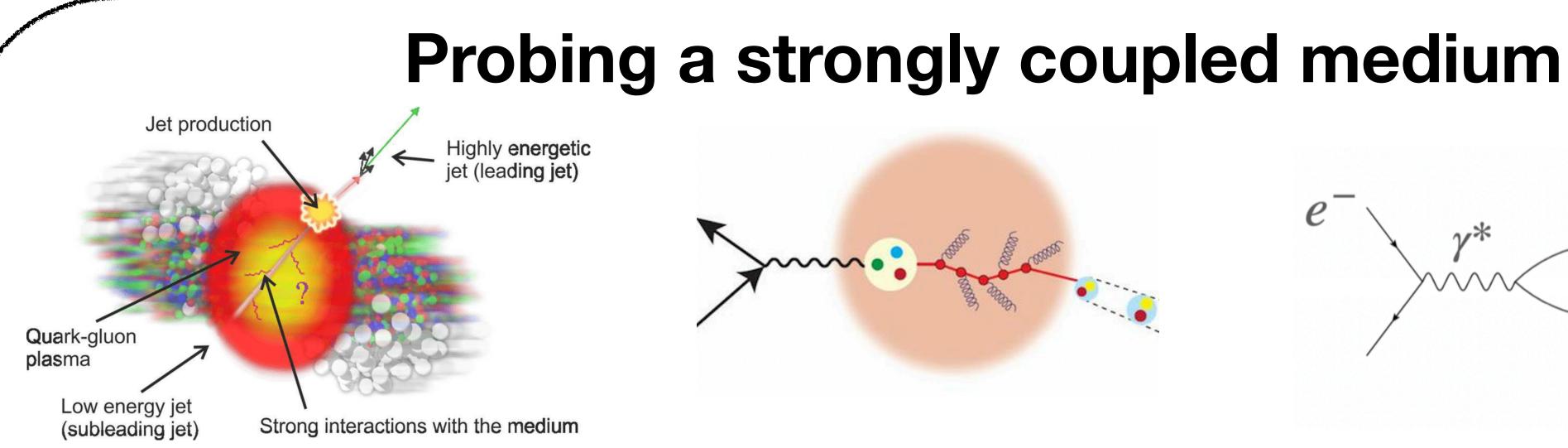
Why we need factorization for jet physics in Heavy Ion collisions

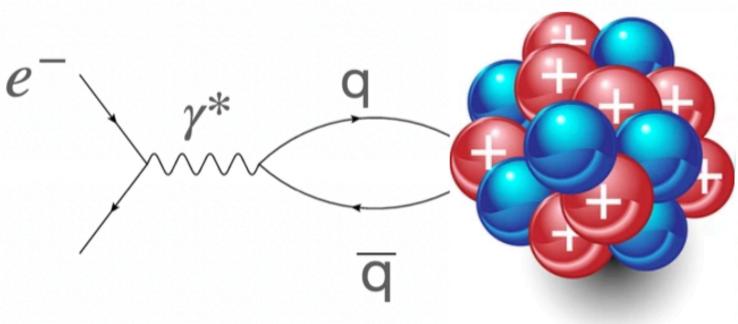
Varun Vaidya, MIT, June 13, 2022







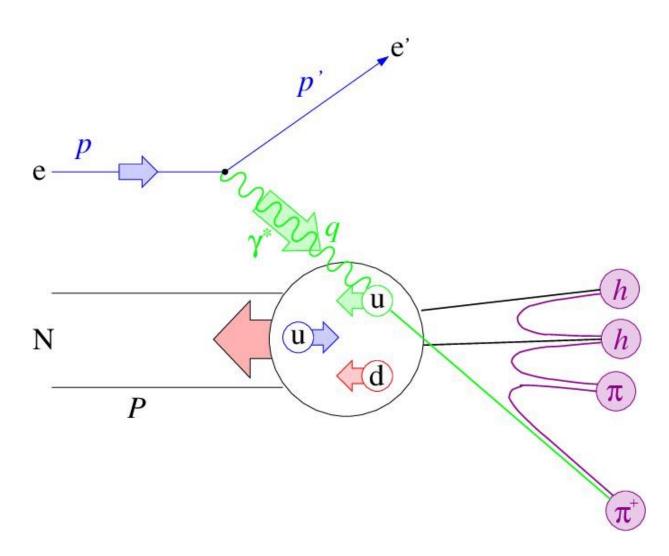
- Quark Gluon Plasma created during HIC is a strongly coupled liquid.
- Perturbation Theory is not reliable to describe the structure of the QGP.
- Hydrodynamic description works at long length scales.
- Not suitable for microscopic structure probed by high energy jets.
- Holographic methods \rightarrow Qualitative results \rightarrow Not systematically improvable



How can we make precise predictions for jet observables in a HIC environment?

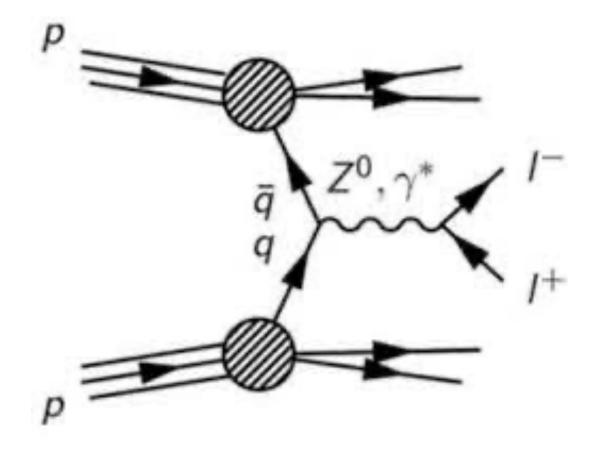


- This is NOT a new problem in nuclear physics
- We are faced with the same issue in hadronic colliders: A strongly coupled initial state that cannot be described by perturbation theory.
- Precision predictions for ep, pp colliders still possible.



• We rely on **Factorization**.

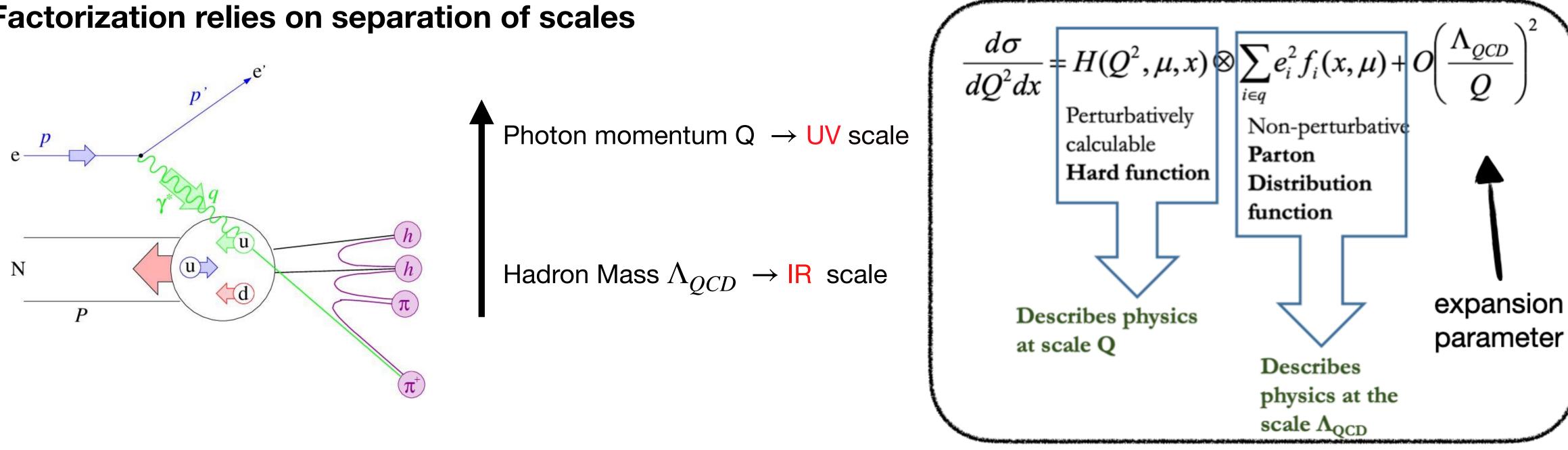
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Familiar examples

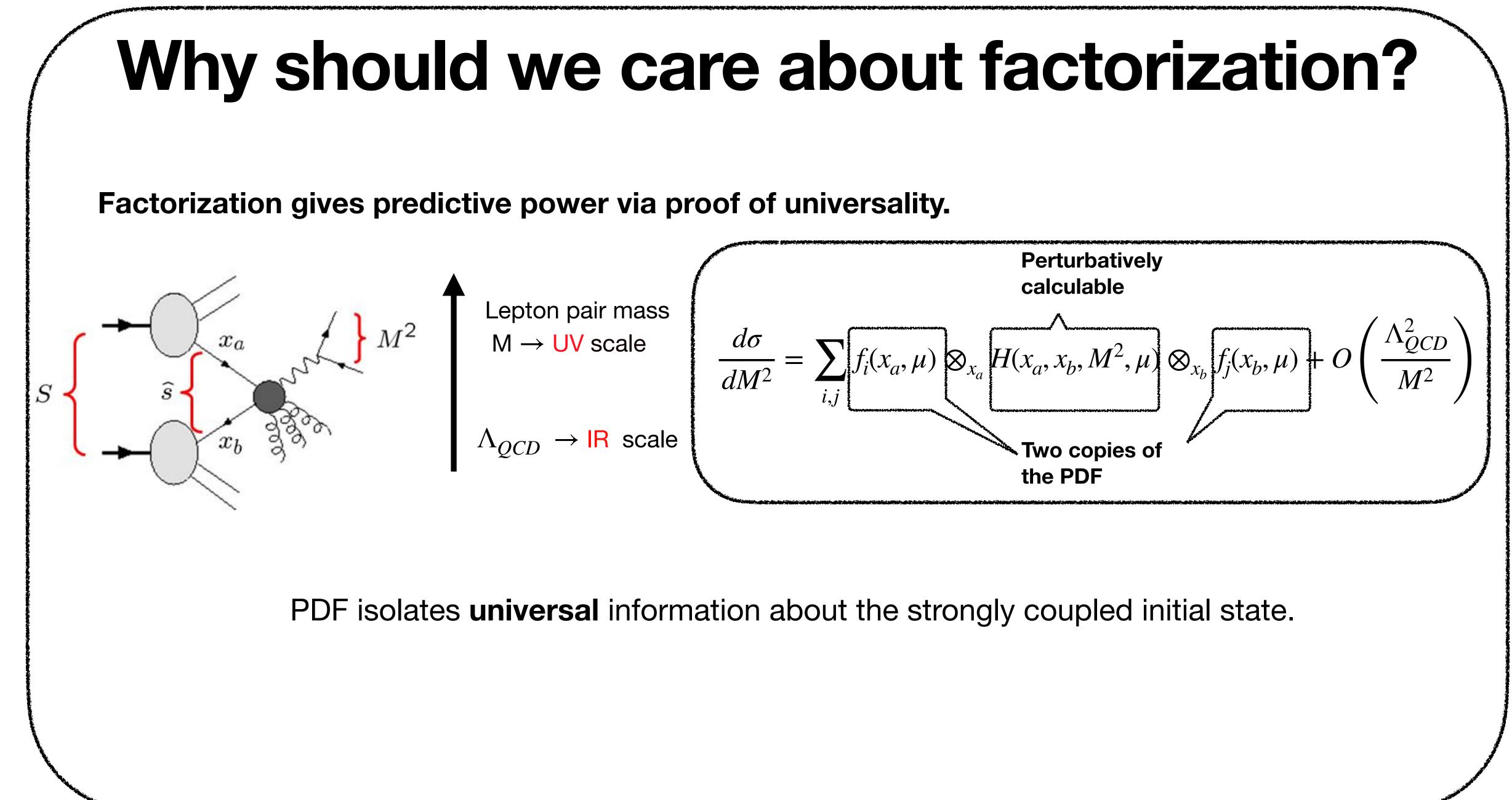
Factorization relies on separation of scales



- to all orders in α_{s} .
- An explicit separation of perturbative and non-perturbative physics.

• The degrees of freedom at Q no longer interact with those at $\Lambda_{OCD} \rightarrow H$ and f can be computed independently





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Why should we care about factorization?

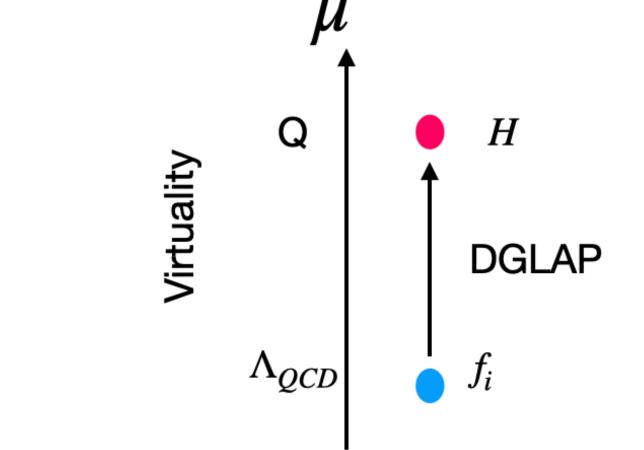
• A precise gauge invariant operator definition of the universal non-perturbative physics.

$$f_q(\xi) = \int \frac{dx^+}{2\pi} e^{-ix^+\xi Q} \operatorname{Tr} \left[\bar{\chi}_q(x^+) W(x^+) \right] dx$$

- A standalone matrix element in a hadron state is much easier to compute numerically (lattice/Quantum computer) than a full simulation.
- Renormalization of the operator(**radiative corrections**) can be done **only once** independent of any specific experiment and independent of any specific hadron :LO \rightarrow DGLAP
- Numerical predictions can be enormously improved by resumming logarithms in the expansion parameters by RG running. $(\alpha_s^n \ln^n \frac{Q}{\Lambda_{oCD}})$
- parameter.

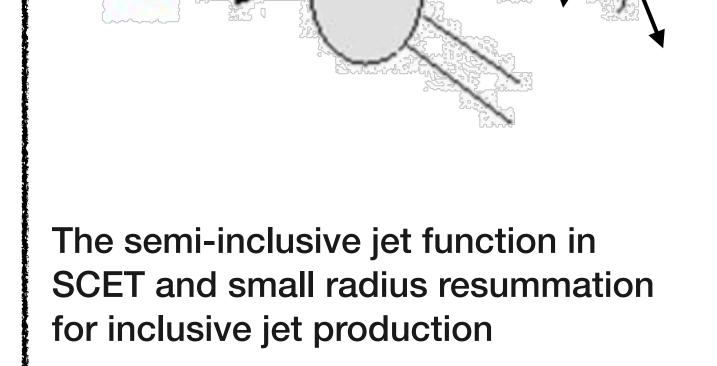
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 $\chi^+,0)\gamma^-\chi_q(0)\rho_H$



• Systematically improvable \rightarrow Computing perturbative functions to higher order, Including higher powers in the expansion



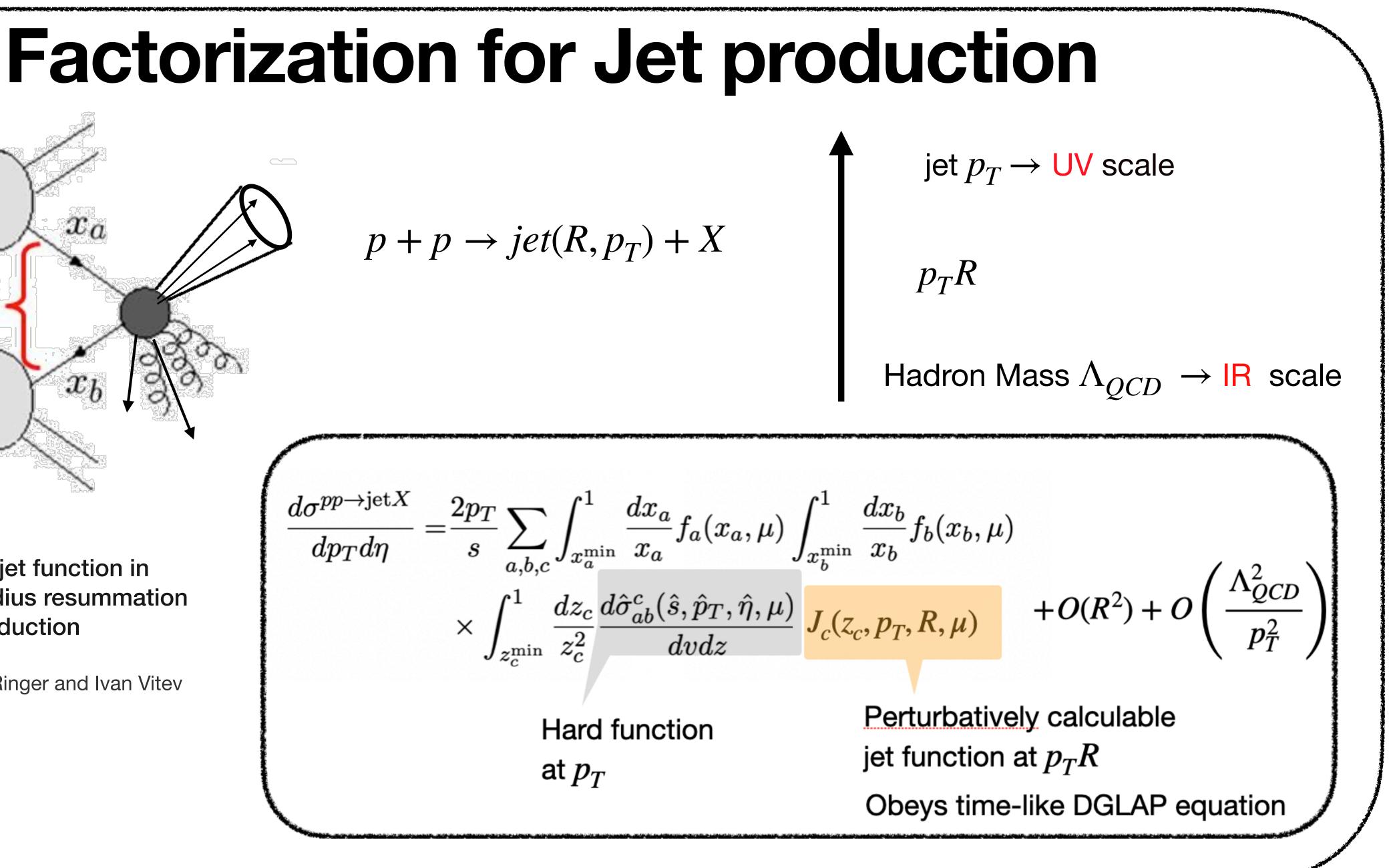


 x_{a}

Zhong-bo Kang, Felix Ringer and Ivan Vitev JHEP 10 (2016) 125

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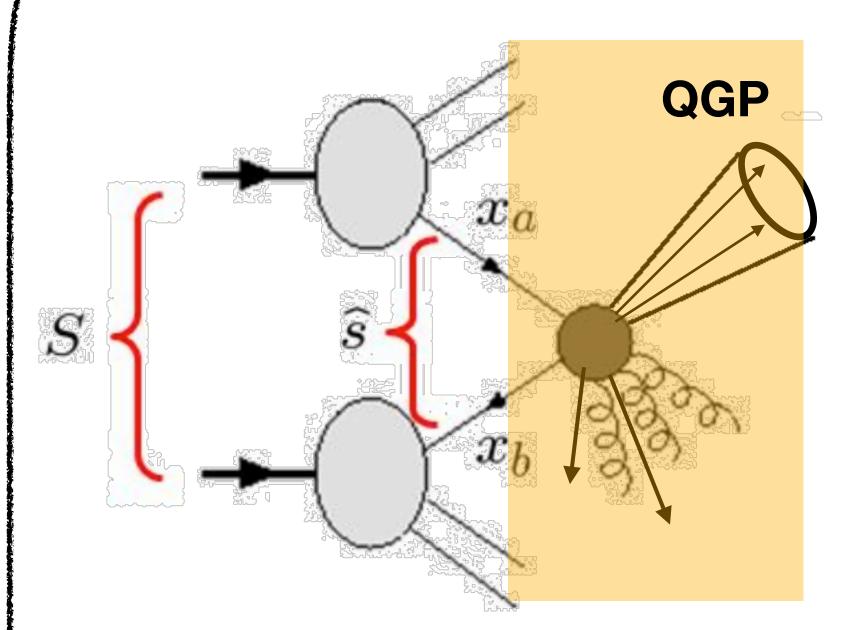
S



Can we do the same for jets in Heavy Ion Collisions?



Semi Inclusive Jet production in HIC



 $A + A \rightarrow jet(R, p_T)$

Emergent Scales

Jet formation time

 $t_F \sim \frac{E}{c^2} \sim$

Mean free path of the probe

 $\lambda_{mfp}(p_T, R)$

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$$t(R, p_T) + X$$

$$\frac{1}{p_T R^2}$$

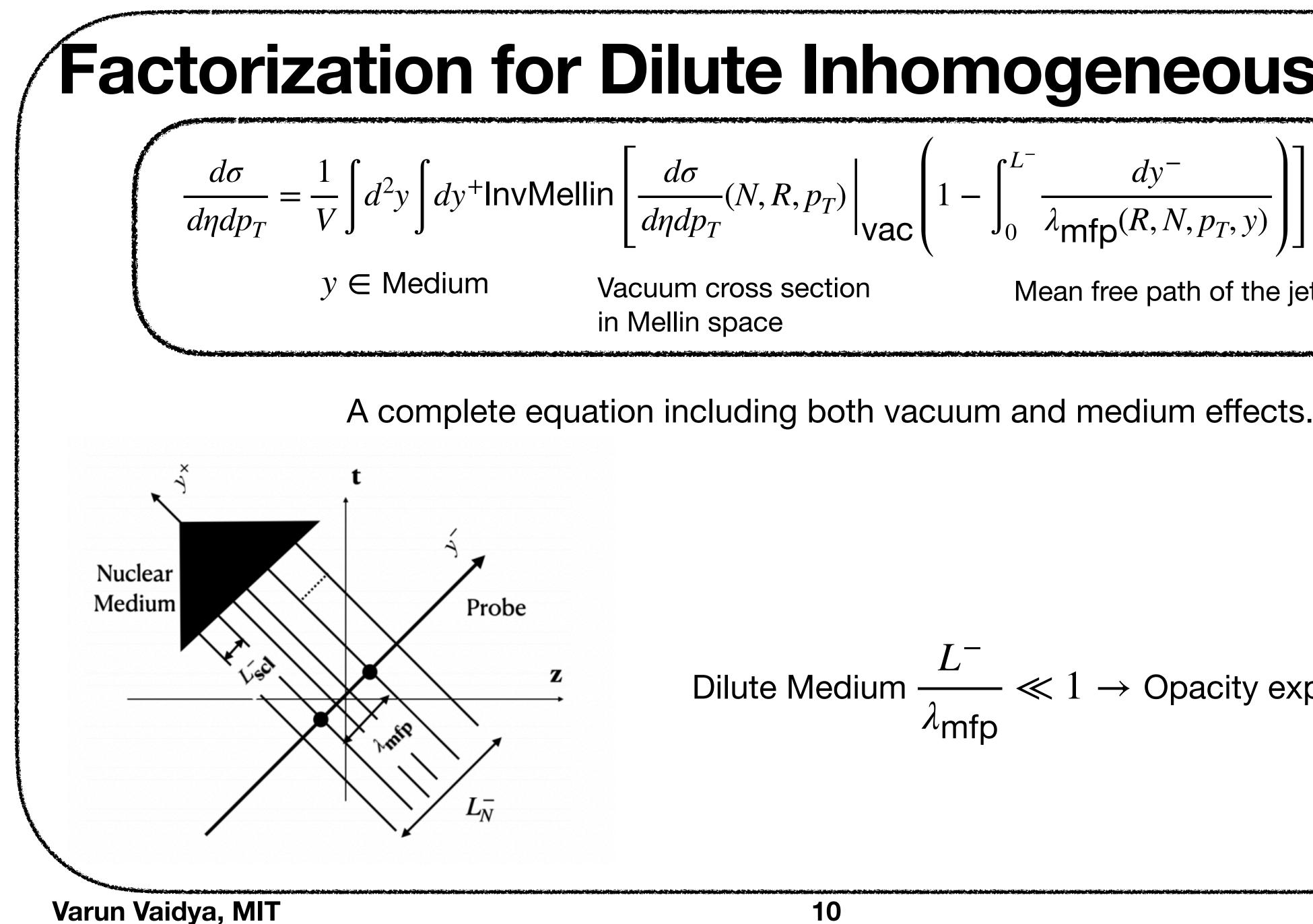
 $p_T R$

Temperature, Debye Mass, $\Lambda_{OCD} \rightarrow IR$ scale

1/ Medium size ~ 1/ L

jet $p_T \rightarrow \mathbf{UV}$ scale





Factorization for Dilute Inhomogeneous Medium Mean free path of the jet,

A complete equation including both vacuum and medium effects.

Medium
$$\frac{L^-}{\lambda_{\rm mfp}} \ll 1 \rightarrow {\rm Opacity\ expansion}$$



Factorization for Dilute Inhomogeneous Medium

$$\lambda_{mfp}^{-1}(R, p_T, y) \equiv \hat{q} = Je$$

The jet transport parameter depends on both the properties of the jet and the properties of the medium and hence

 \hat{q} is not a direct probe of observable independent medium properties.

Therefore we must factorize this object further to separate out the universal physics of the medium from the properties of the jet.

$$\lambda_{mfp}^{-1}(R, N, p_T, y) = H_G(p_T, \mu) \int d^2k_{\perp}S_{r}$$
University independent of the structure of the s

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et transport parameter

 $med^{(k_{\perp}, y, \mu, \nu)}J_c^{med}(R, p_T, N, k_{\perp}) + O(R^2)$

sal observable endent ure function

Medium jet function

V. Vaidya

An Effective Field Theory for jet substructure in Heavy Ion Collisions. JHEP 11, 064 (2021)



Medium Structure function

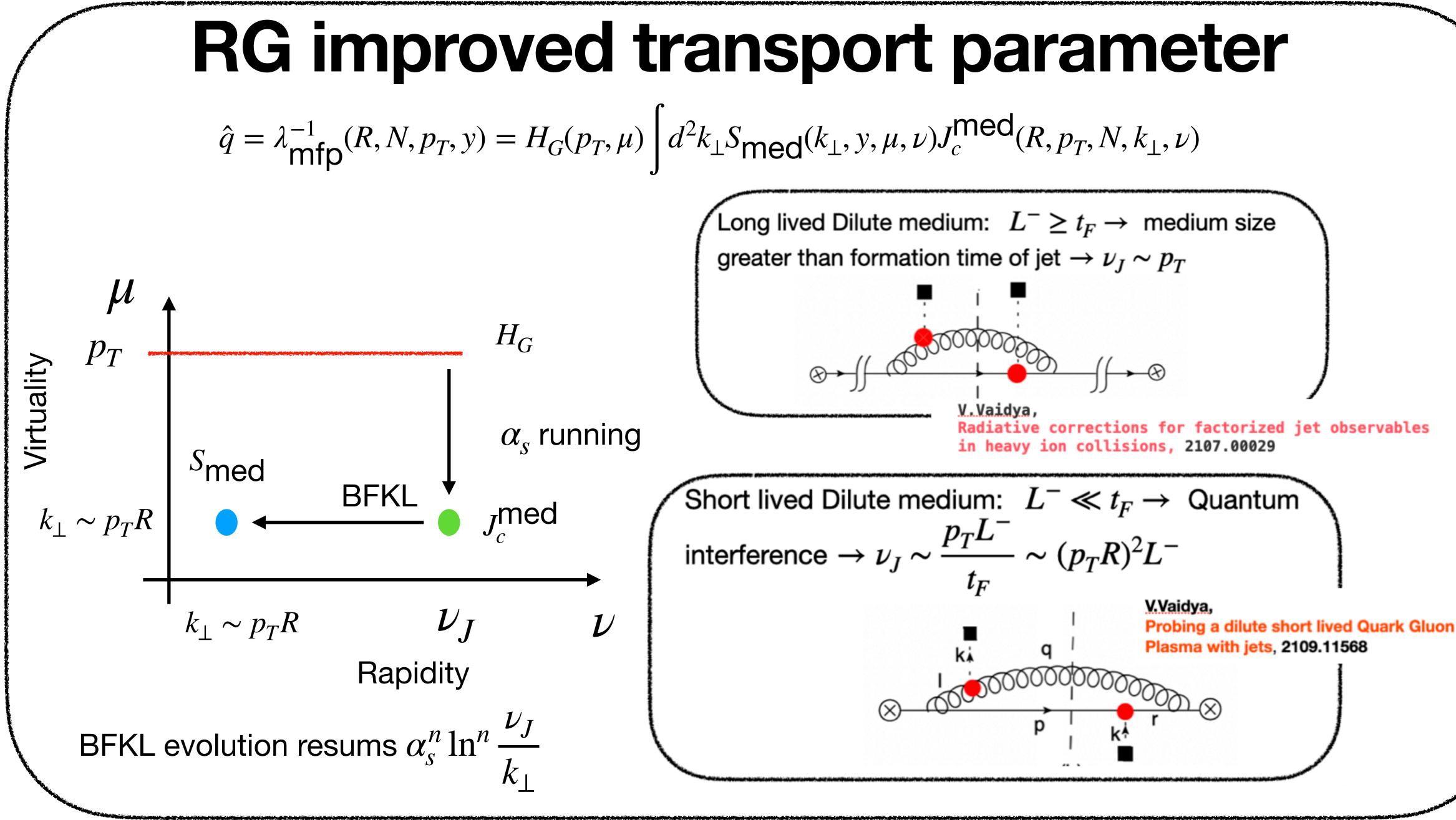
$$S_{\text{med}}(k_{\perp}, y) = \frac{1}{k_{\perp}^2} \int \frac{dk^-}{2\pi} \int d^4 x e^{-ik \cdot x} \text{Tr} \Big[O_S^A(x+y) O_S^A(y) \rho_{\text{Med}} \Big]$$
$$O_S^A = \sum_{i \in q,g} O_S^{A,i} \qquad O_S^{A,q} = \bar{\psi} S_+ T^A \frac{\gamma^+}{2} S_+^{\dagger} \psi$$

- Gauge Invariant operator definition for universal medium physics.
- Depends only on the **local** properties of the medium.
- Renormalization group Equation in rapidity is the **BFKL** equation.

V.Vaidva. Radiative corrections for factorized jet observables in heavy ion collisions, 2107.00029

• The same operator describes the medium in small x DIS and jet propagation in EIC!





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A non-perturbative medium

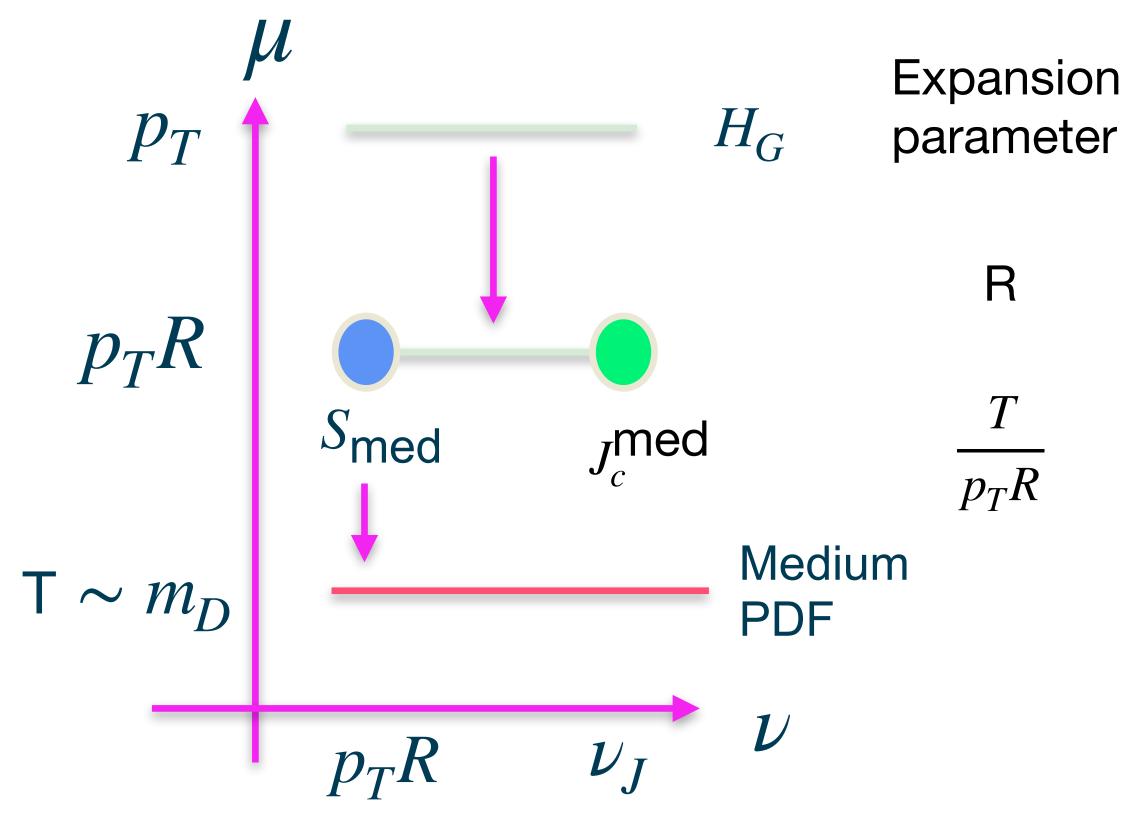
$$\hat{q} = \lambda_{\mathsf{mfp}}^{-1}(R, N, p_T, y) = H_G(p_T, \mu) \int d^2k_{\perp} S$$

 $p_T \gg p_T R \gg T$

• Jet function is perturbative and calculable.

- Medium function $S_{\rm med}$ can be matched onto the medium PDF at T
- Medium PDF: Non perturbative but observable independent!
- Only need to recompute the jet function for different jet substructure observables.

 $S_{med}(k_{\perp}, y, \mu, \nu)J_c^{med}(R, p_T, N, k_{\perp}) + O(R^2)$





Summary

- nonperturbative medium.
- •A general framework to compute **any** jet observable merely by imposing different measurements on the jet function.

Outlook

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• Factorization is crucial if we are to make quantitative predictions for jet propagation in a

•It isolates the universal observable independent properties of a strongly coupled medium.

This type of analysis can also be extended for the case of a Dense Medium where we need to sum multiple jet-medium interaction.



