

**ETC* WORKSHOP: “QUARK-GLUON PLASMA CHARACTERISATION
WITH HEAVY FLAVOUR PROBES”**

15 November 2021 — 18 November 2021

**Charm and Bottom dynamics: nuclear
modification factor R_{AA} and anisotropic flows v_n
in event shape selections**



Maria Lucia Sambataro

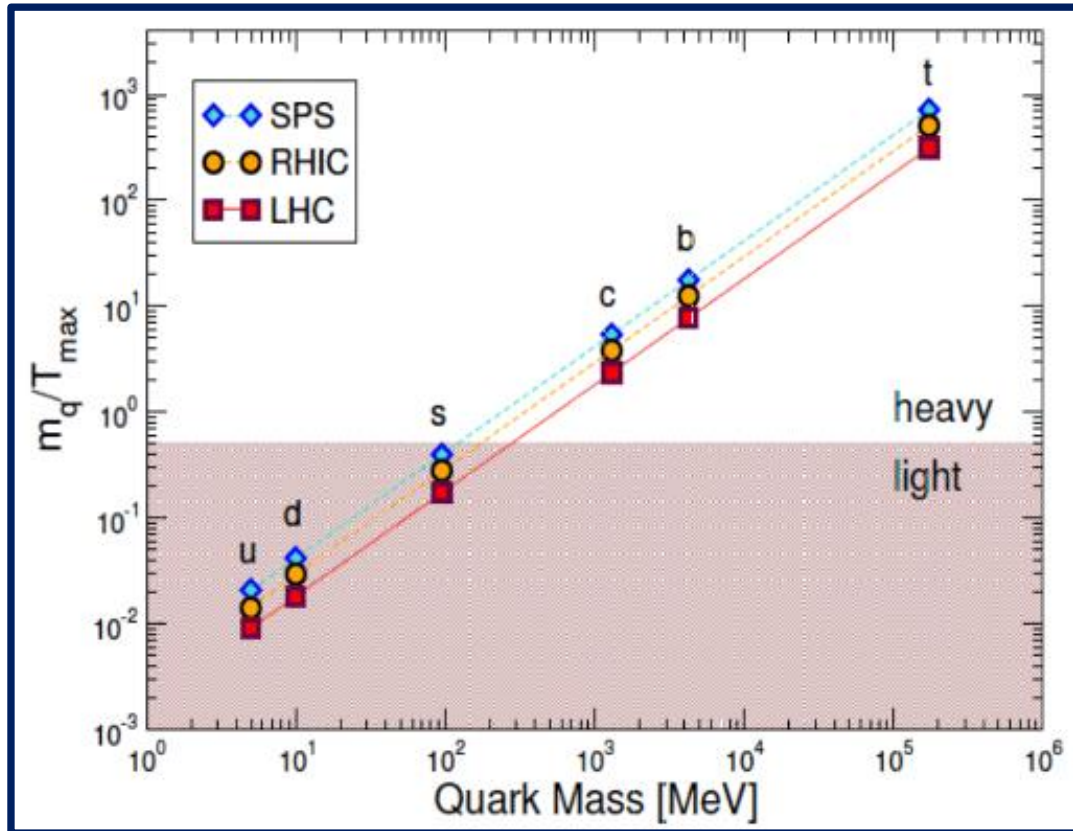
Dipartimento di Fisica e Astronomia 'E. Majorana'
Università degli Studi di Catania, INFN-LNS

In collaboration with: S. Plumari, Y. Sun, V. Minissale, V. Greco

Outline

- QPM Catania approach to charm quark dynamics
 - $R_{AA}, v_2 \rightarrow$ Spatial diffusion coefficient $D_s(T)$ of charm.
- Initial state fluctuations \rightarrow Event-Shape-Engineering
 - Anisotropic flows $v_{n(=2,3,4)}$ and their correlations.
- Predictions for bottom quark
 - R_{AA}, v_2 of electrons from semileptonic B-mesons decays.
 - Spatial diffusion coefficient $D_s(T)$ of bottom.
- Extension to off-shell dynamics
 - Impact on transport properties and FDT validity.
 - Energy loss
- Conclusions and new perspectives.

Basic scales of charm and bottom quarks



- $m_{c,b} \gg \Lambda_{QCD}$
pQCD initial production
- $m_{c,b} \gg T_{RHIC,LHC}$
negligible thermal production
- $\tau_0 < 0,08 \text{ fm}/c \ll \tau_{QGP}$
- $\tau_{th} \approx \tau_{QGP} \gg \tau_{g,q}$

They experience the full evolution of the QGP.

They carry more informations with respect to their light counterparts.

CATANIA MODEL: QPM APPROACH AND TRANSPORT THEORY

QP-Model fitting IQCD

Non perturbative dynamics → M scattering matrices (q,g → Q) evaluated by Quasi-Particle Model fit to **IQCD thermodynamics**

$$m_g^2(T) = \frac{2N_c}{N_c^2 - 1} g^2(T) T^2$$

$$m_q^2(T) = \frac{1}{N_c} g^2(T) T^2$$

g(T) from a fit to ε from IQCD data
→ good reproduction of P, ε-3P, c_S

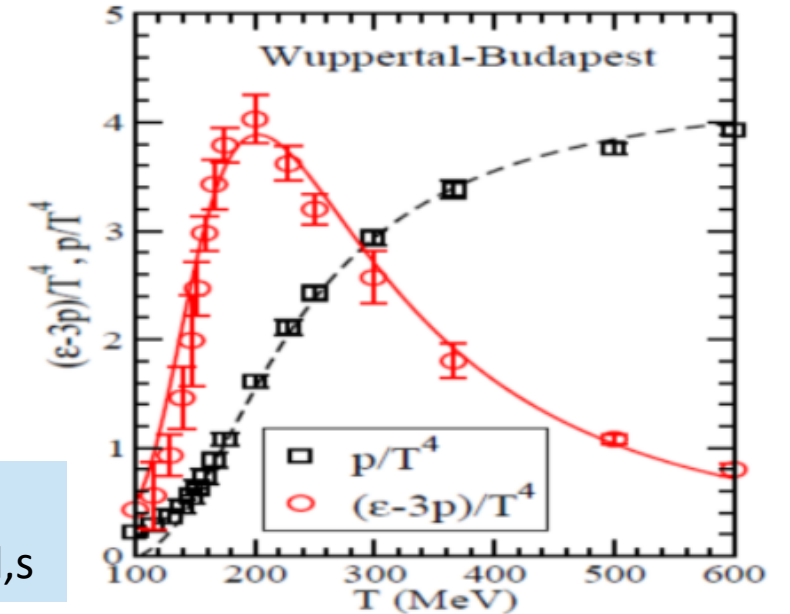
$$g^2(T) = \frac{48\pi^2}{(11N_c - 2N_f) \ln \left[\lambda \left(\frac{T}{T_c} - \frac{T_s}{T_c} \right) \right]^2}$$

$$\lambda = 2.6$$

$$T_s = 0.57 T_c$$

Larger than pQCD especially as T → T_c

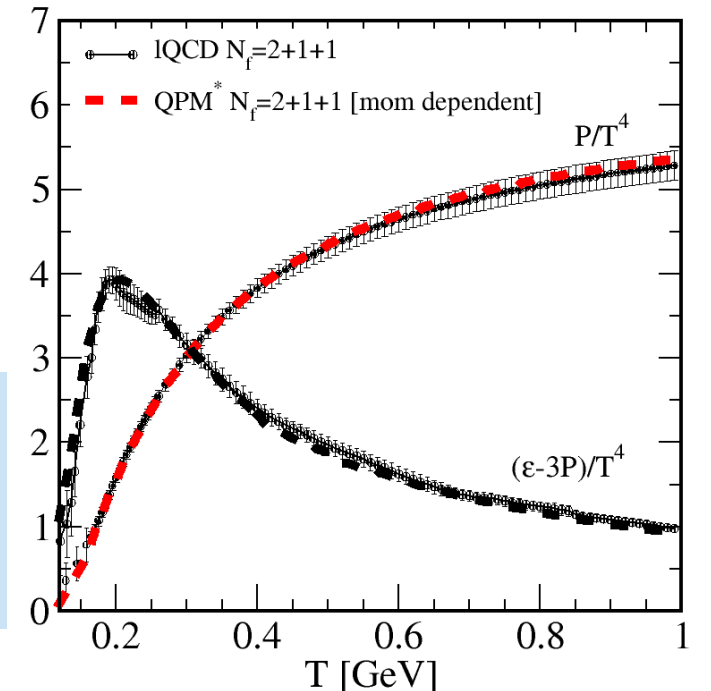
S. Plumari et al, *Phys.Rev.D* 84 (2011) 094004
H. Berrehrah,, *PHYSICAL REVIEW C* 93, 044914 (2016)
M.L. Sambaturo et al. in preparation



$N_f = 2+1$
Bulk: u,d,s

NEW

Including charm!
 $N_f = 2+1+1$
and
mom dependence



Relativistic Boltzmann equation at finite η/s

Bulk evolution

$$p^\mu \partial_\mu f_q(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_q(x, p) = C[f_q, f_g]$$

$$p^\mu \partial_\mu f_g(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_g(x, p) = C[f_q, f_g]$$

Equivalent to viscous hydro
at $\eta/s \approx 0.1$

Free-streaming

field interaction

Collision term

$$\varepsilon - 3p \neq 0$$

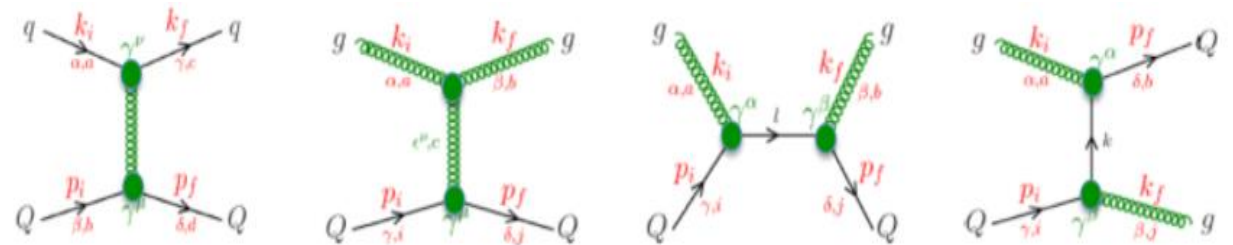
gauged to some $\eta/s \neq 0$

HQ evolution

$$p^\mu \partial_\mu f_Q(x, p) = C[f_q, f_g, f_Q]$$

$$C[f_q, f_g, f_Q] = \frac{1}{2E_1} \int \frac{d^3 p_2}{2E_2 (2\pi)^3} \int \frac{d^3 p_1'}{2E_1' (2\pi)^3} \\ \times [f_Q(p_1') f_{q,g}(p_2') - f_Q(p_1) f_{q,g}(p_2)] \\ \times |M_{(q,g) \rightarrow Q}(p_1 p_2 \rightarrow p_1' p_2')| \\ \times (2\pi)^4 \delta^4(p_1 + p_2 - p_1' - p_2')$$

Feynmann diagrams at first order pQCD for HQs-bulk interaction:



Scattering matrices $M_{g,q}$ by QPM fit to IQCD thermodynamics

Relativistic Boltzmann equation at finite η/s

Bulk evolution

$$p^\mu \partial_\mu f_q(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_q(x, p) = C[f_q, f_g]$$

$$p^\mu \partial_\mu f_g(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_g(x, p) = C[f_q, f_g]$$

Equivalent to viscous hydro
at $\eta/s \approx 0.1$



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Collision term

$$\varepsilon - 3p \neq 0$$

gauged to some $\eta/s \neq 0$

HQ evolution

$$p^\mu \partial_\mu f_Q(x, p) = C[f_q, f_g, f_Q]$$

Coalescence + fragmentation hadronization ($\varepsilon \rightarrow \varepsilon_c$)

For details: S. Plumari talk [17.30]

$$\frac{dN_h}{d^2 p_h} = \sum_f \int dz \frac{dN_f}{d^2 p_f} D_{f \rightarrow h}(z)$$

Peterson fragmentation function

$$\frac{dN_{Hadron}}{d^2 p_T} = g_H \int \prod_{i=1}^n p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3} f_q(x_i, p_i) f_W(x_1, \dots, x_n; p_1, \dots, p_n) \delta(p_T - \sum_i p_{iT})$$

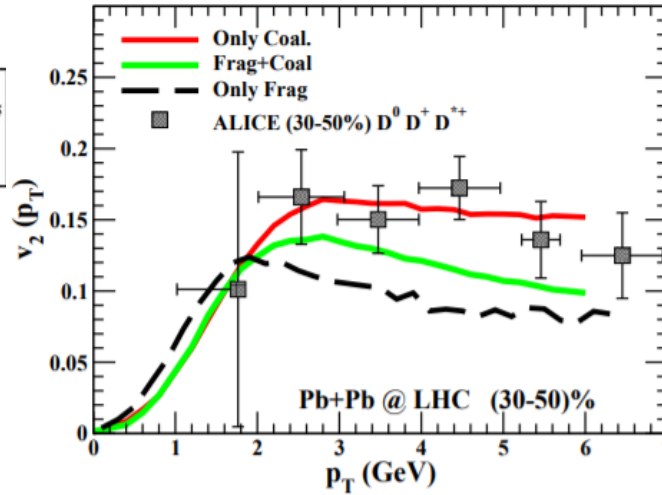
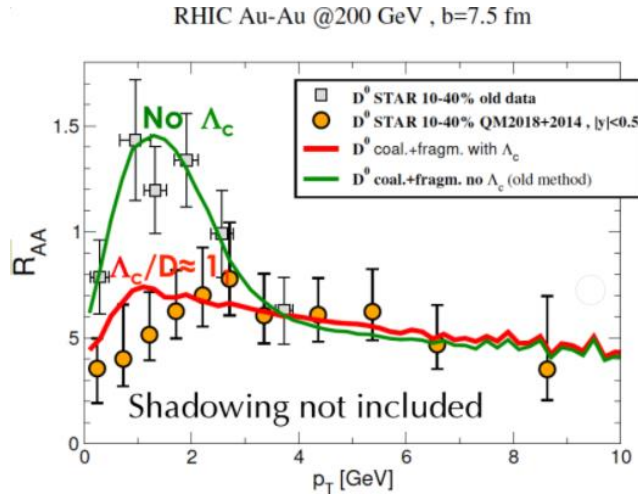
Wigner function

C. Peterson, D. Schalatter, I. Schmitt,
P.M. Zerwas PRD 27 (1983) 105

S. Plumari, et al.,
Eur. Phys. J. C78 no. 4, (2018) 348

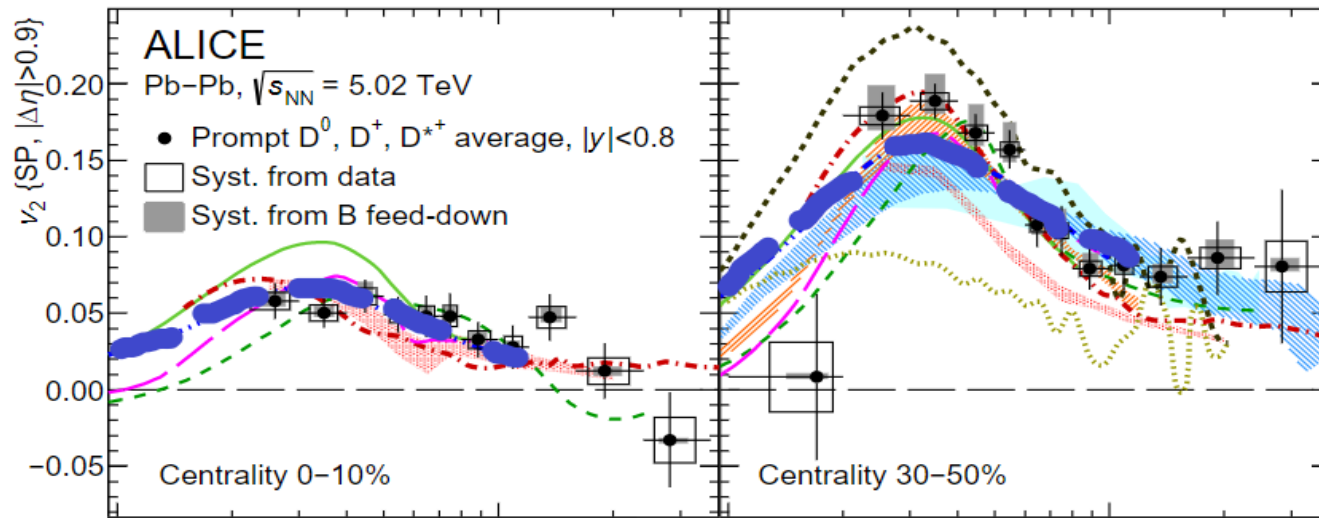
$$P_{coal} = 1 \text{ for } p = 0$$

Catania QPM: some prediction for charm...



Scardina et al., PRC 97(2017)

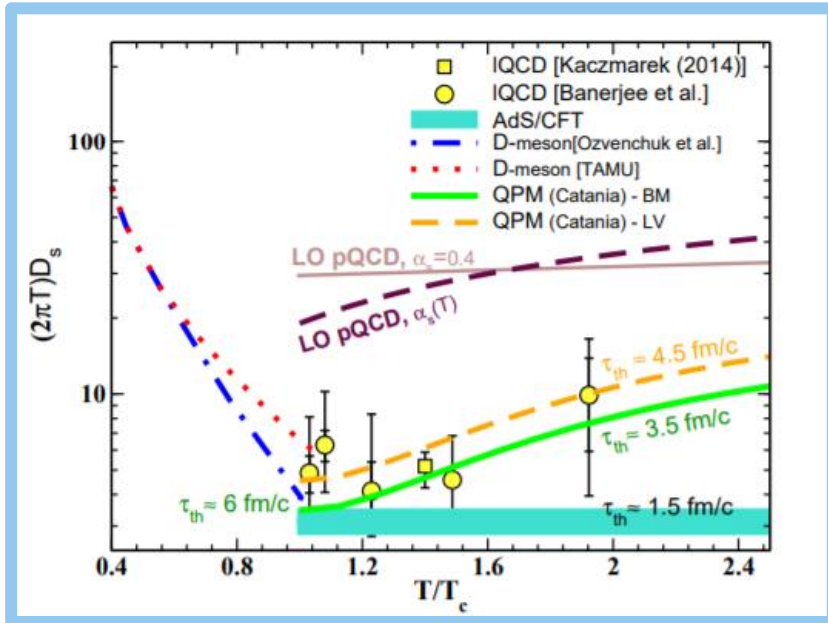
Good description of R_{AA} , v_2 at RHIC & LHC energies within error bars



— Catania Model

ALICE collaboration, *Phys.Lett.B* 813 (2021) 136054

Spatial diffusion coefficient of charm quark



Not a model fit to IQCD data!
Results from $R_{AA}(p_T)$, $v_2(p_T)$

We have a probe with $\tau_{therm} \approx \tau_{QGP}$

$$\tau_{th} = \frac{M}{2\pi T^2} (2\pi T D_s) \cong 1.8 \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

Reviews:

- F. Prino and R. Rapp, JPG(2019)
- X. Dong and V. Greco, Prog.Part.Nucl.Phys. (2019)
- Jiaxing Zhao et al., arXiv:2005.08277

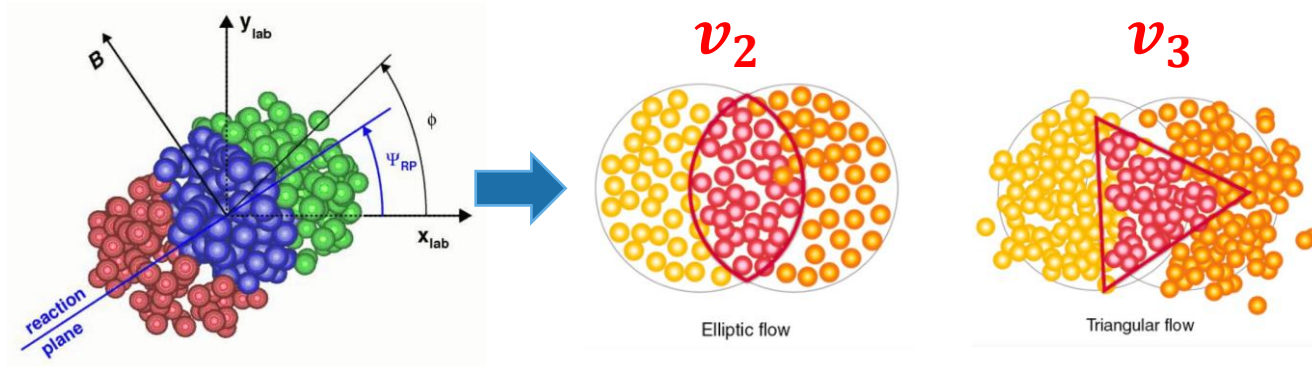
FUTURE:

- Access low p and precision data (detector upgrade);
- Better insight into hadronization;
- New observables;**
- Bottom.**

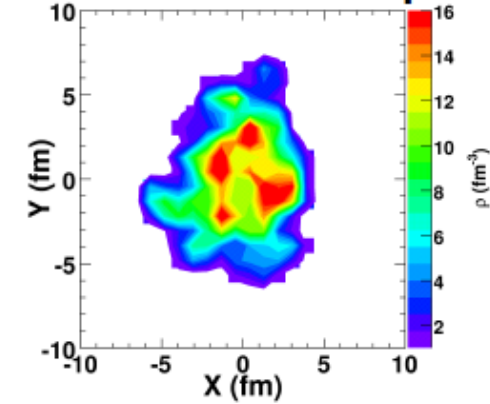
Main focus of this talk

Extension to higher order anisotropic flows $v_n(p_T)$

$$E \frac{d^3N}{dp_T} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left\{ 1 + \sum_{i=1}^{\infty} v_n \cos[n(\varphi - \Psi_n)] \right\}$$



Not almond shape



$$\epsilon_n = \frac{\langle r_{\perp}^n \cos[n(\varphi - \Phi_n)] \rangle}{\langle r_{\perp}^n \rangle} \quad \Phi_n = \frac{1}{n} \arctan \frac{\langle r_{\perp}^n \sin(n\varphi) \rangle}{\langle r_{\perp}^n \cos(n\varphi) \rangle}$$

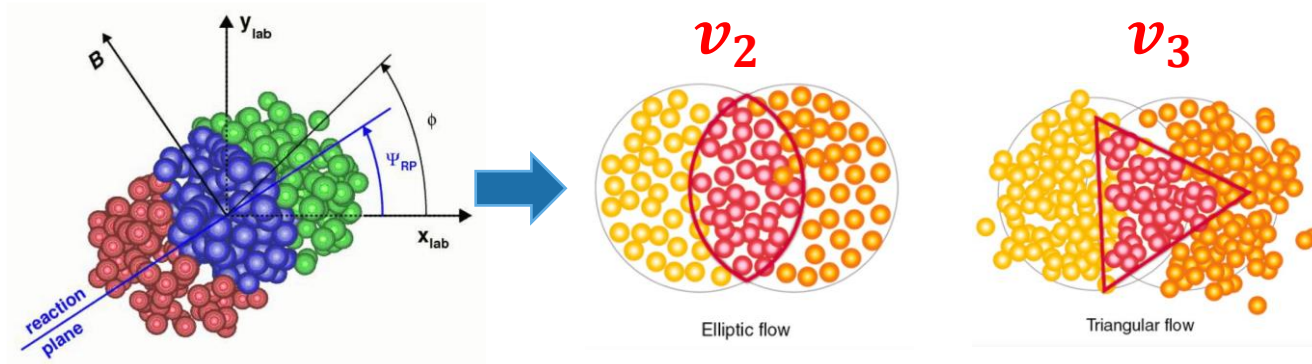
$$r_{\perp} = \sqrt{x^2 + y^2}, \quad \varphi = \arctan(y/x)$$

Monte Carlo Glauber for initial condition of partons

S.Plumari et al, *Phys.Rev.C* 92 (2015) 5

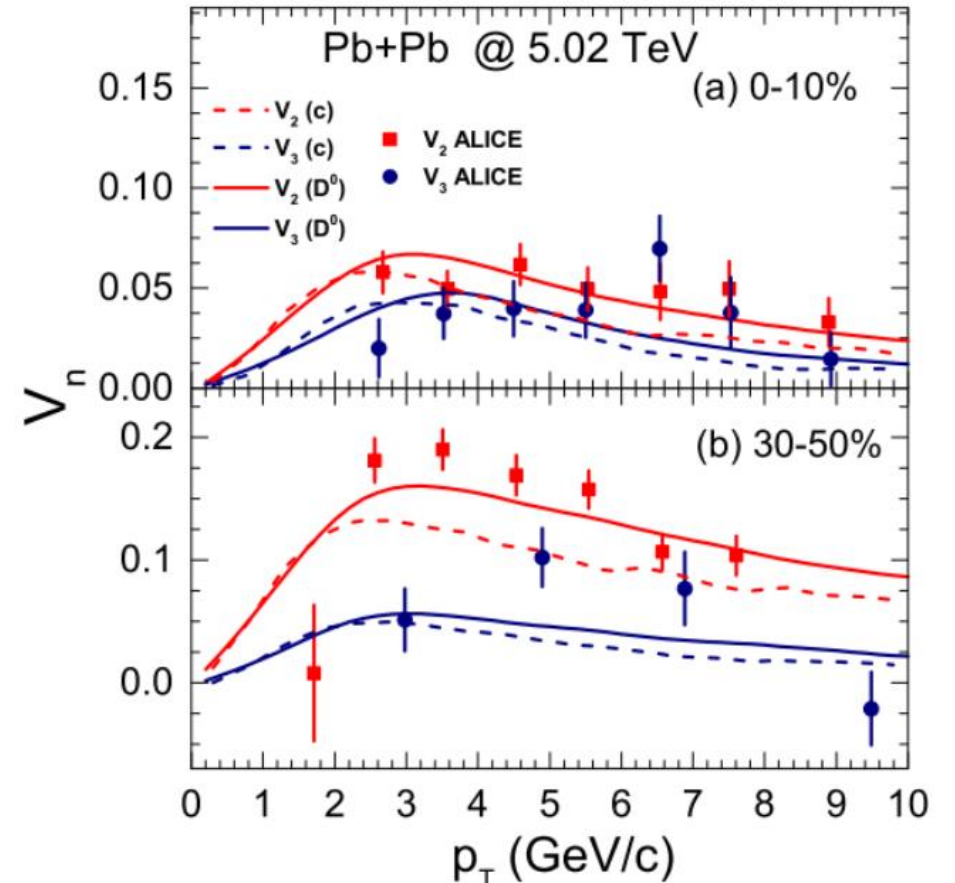
Extension to higher order anisotropic flows $v_n(p_T)$

$$E \frac{d^3N}{dp_T} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left\{ 1 + \sum_{i=1}^{\infty} v_n \cos[n(\varphi - \Psi_n)] \right\}$$



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$$r_{\perp} = \sqrt{x^2 + y^2}, \quad \varphi = \arctan(y/x)$$



Data taken from ALICE collaboration: *Phys.Lett.B* 813 (2021) 136054

- In the more peripheral collision (30-50 % centrality class) \rightarrow larger v_2 and comparable v_3
- \triangleright v_2 mainly generated by the geometry of overlapping region in larger centrality collision
- \triangleright v_3 mainly driven by the fluctuation of the triangularity of overlap region at all centrality

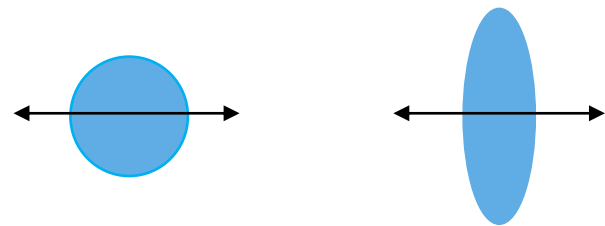
Extension to higher order anisotropic flows $v_n(p_T)$

ESE technique and v_n correlations

Selection of events with the **same centrality** but **different initial geometry** on the basis of the magnitude of the second-order harmonic reduced flow vector q_2 .

$$q_2 = |\vec{Q}_2|/\sqrt{M}$$

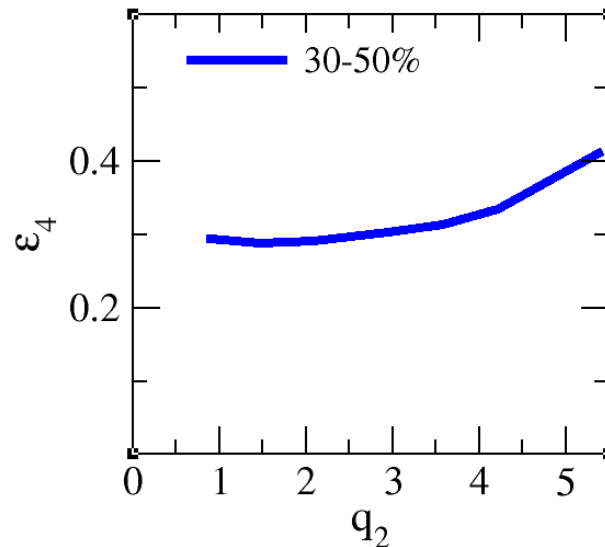
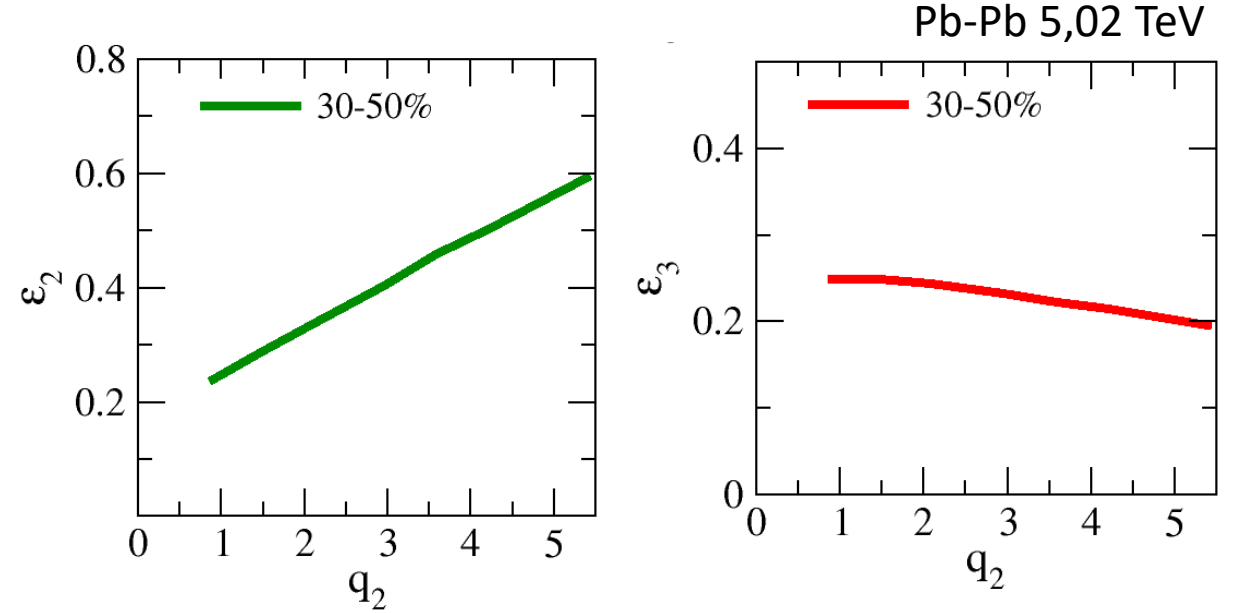
$$\vec{Q}_2 = \sum_{j=1}^M e^{i2\varphi_j}$$



20 % small q_2 20 % large q_2
 Large $q_2 \rightarrow$ large ϵ_2

$$\epsilon_n = \frac{\langle r_{\perp}^n \cos[n(\varphi - \Phi_n)] \rangle}{\langle r_{\perp}^n \rangle} \quad \Phi_n = \frac{1}{n} \arctan \frac{\langle r_{\perp}^n \sin(n\varphi) \rangle}{\langle r_{\perp}^n \cos(n\varphi) \rangle}$$

$$r_{\perp} = \sqrt{x^2 + y^2}, \quad \varphi = \arctan(y/x)$$

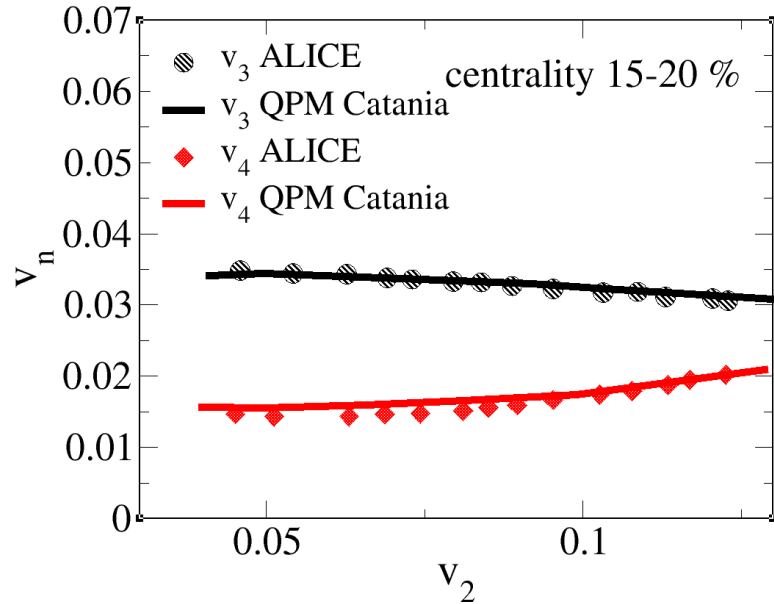


Anti-correlation between ϵ_2 and ϵ_3

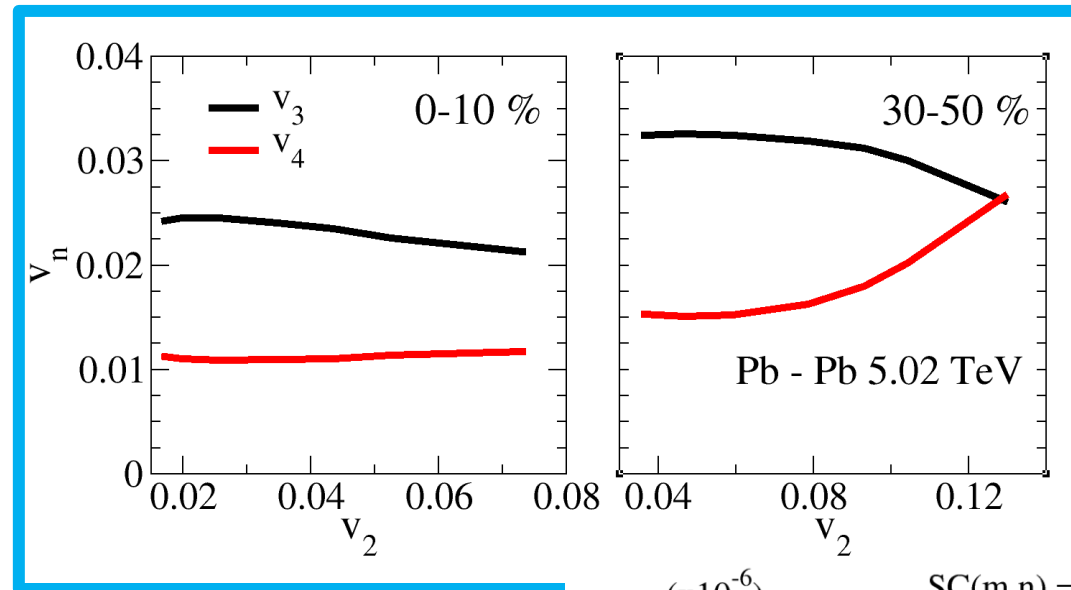
Non-linear correlation between ϵ_2 and ϵ_4

ESE: $v_n - v_m$ correlations

Charged particles



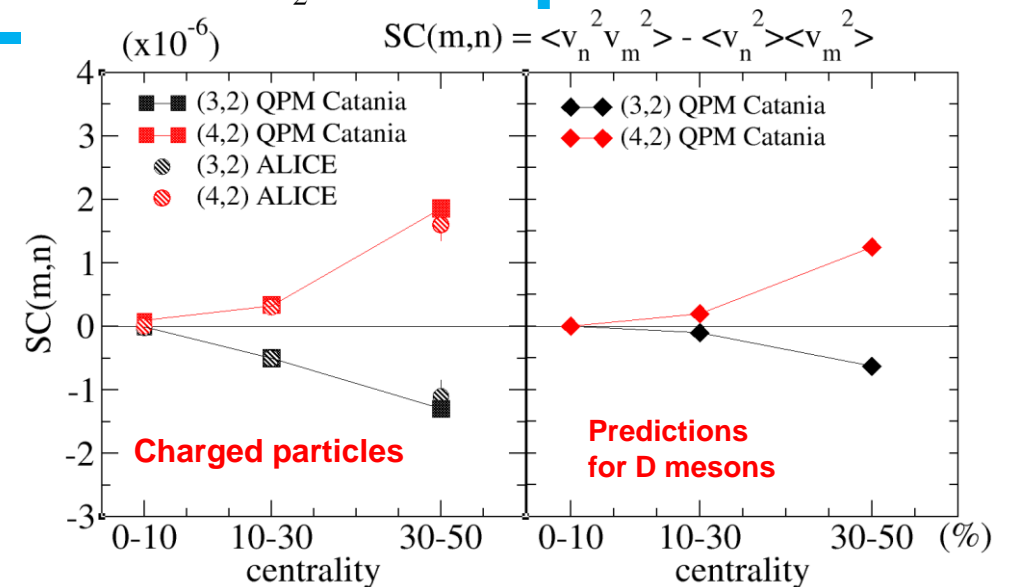
Predictions for D mesons



Correlations between the ε_n and ε_m present in the initial geometry \rightarrow correlations between flow harmonics different orders, i.e. correlations v_n and v_m

- \triangleright Good description of $v_n - v_m$ correlation for bulk
- \triangleright Prediction for similar and weaker correlation between soft and hard particles \rightarrow NSC(m,n)?

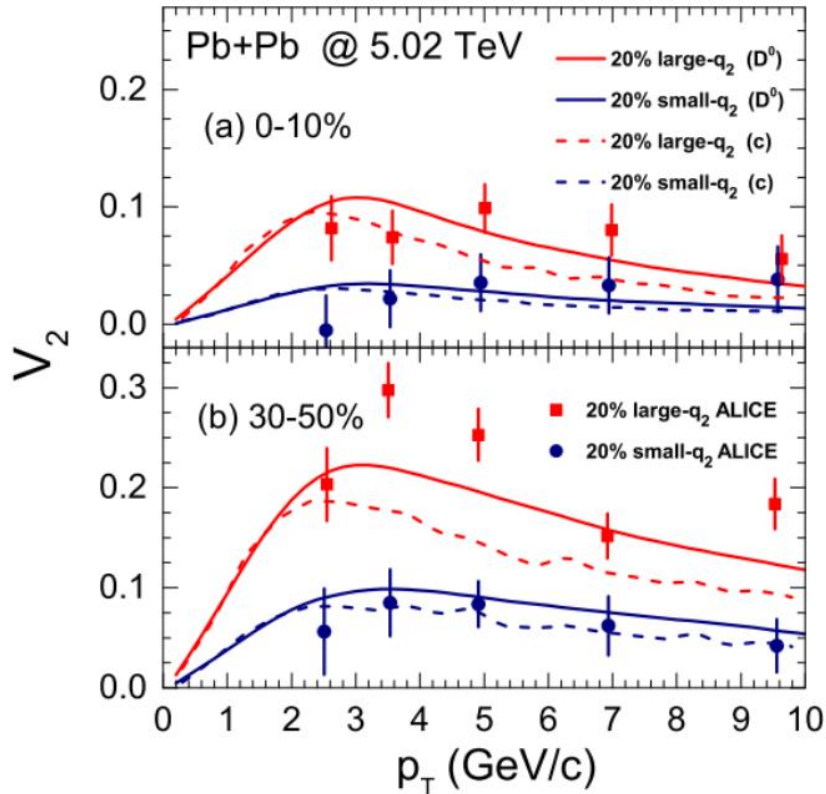
M.L. Sambaturo, Y. Sun et al. in preparation



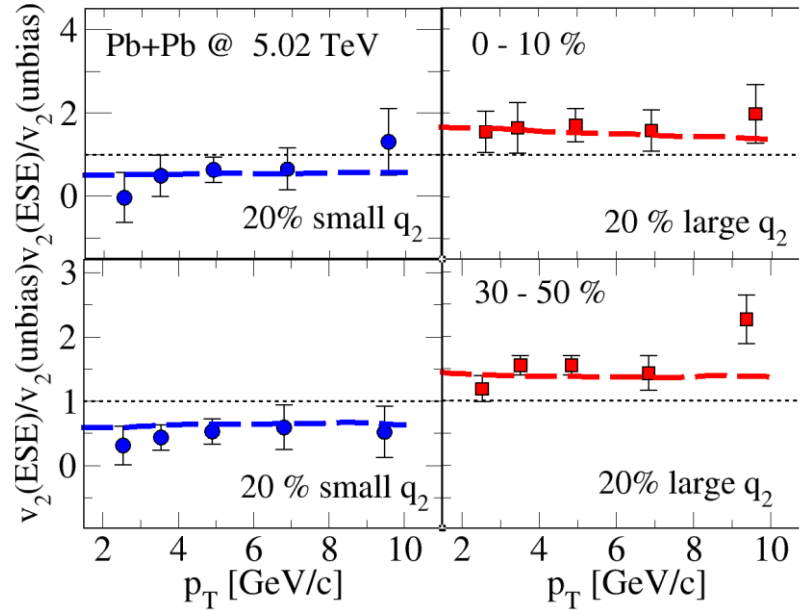
Data taken from: S. Mohapatra *Nucl.Phys.A* 956 (2016) 59-66

ESE: v_2 and spectra (20% small/large q_2)

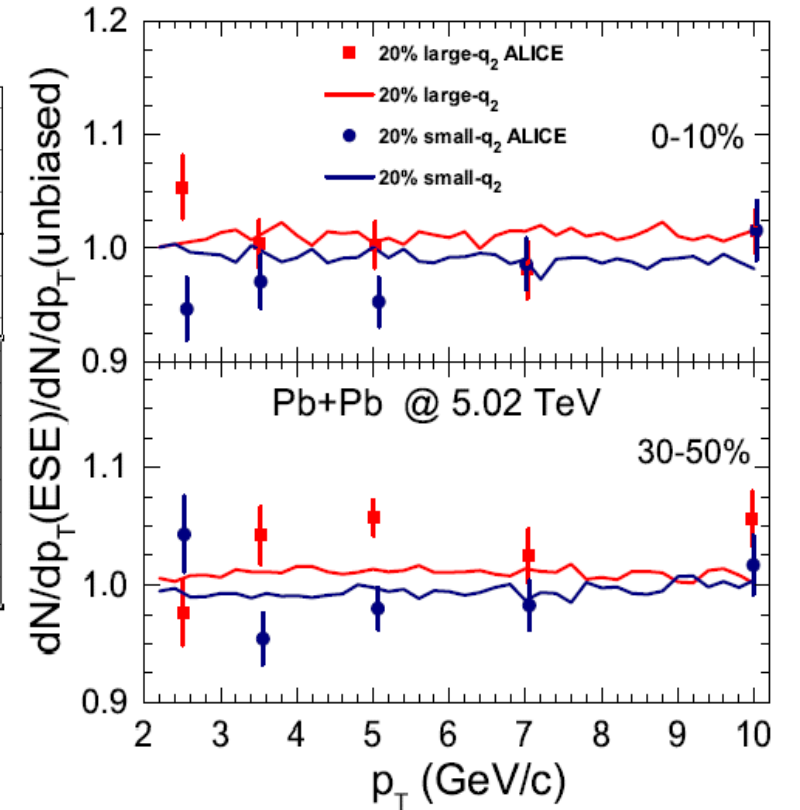
q_2 selected $v_2(p_T)$



q_2 selected $v_2(p_T)$ ratio



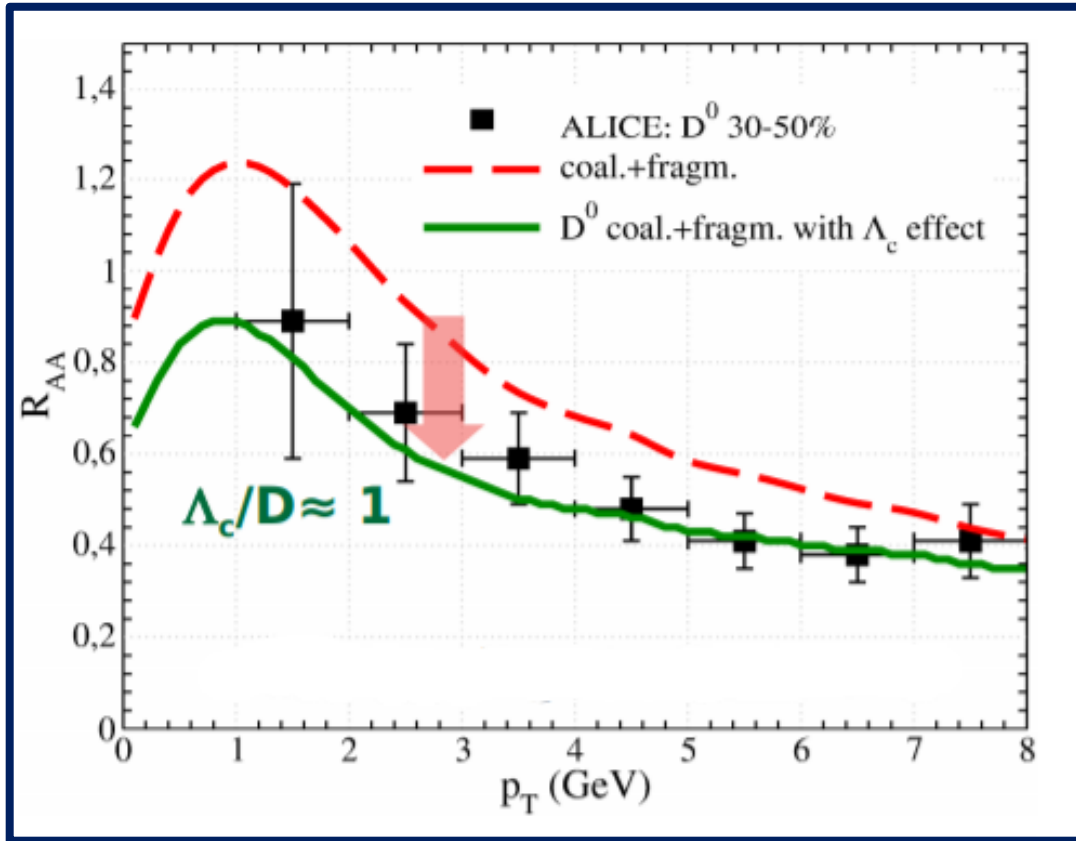
q_2 selected spectra ratio



Data taken from ALICE collaboration: *Phys.Lett.B* 813 (2021) 136054

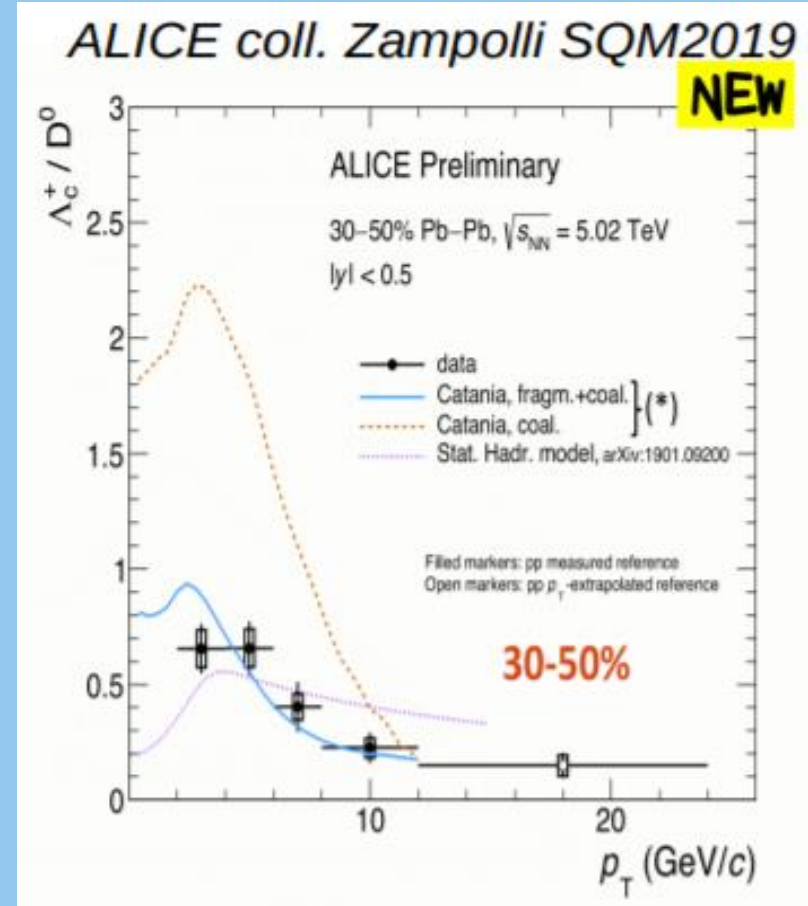
- v_2 (large- q_2 /small- q_2) \cong v_2 (unbiased) of **about 50%** in both 0-10% and 30-50% centrality.
- Spectra ratio of D mesons (ESE selected/unbiased event) \rightarrow close to unity \rightarrow small correlation between the radial flow and the azimuthal anisotropy (still missing ev. by ev. fluctuation for coalescence)

D meson: Impact of large Λ_c production on R_{AA}



$D_s(T)$ of charm quark that reproduces R_{AA} and v_2 gives good description of

- Impact of Λ_c/D^0
- Triangular flow $v_3(p_T)$.
- q_2 selected anisotropic flow and spectra.



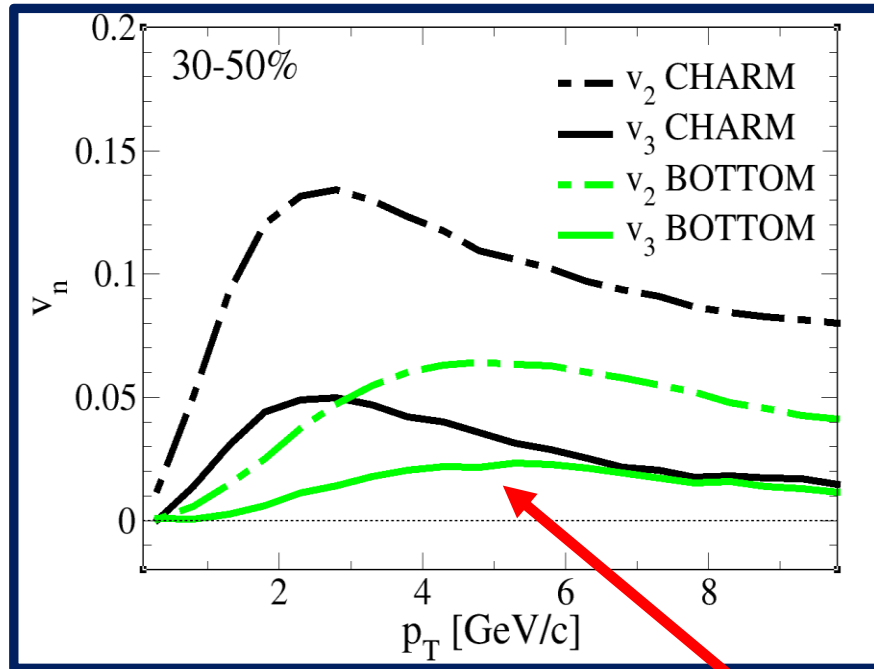
- With the same coalescence plus fragmentation model we describe the Λ_c/D^0

S. Plumari, et al.,
 Eur. Phys. J. C78 no. 4, (2018) 348

Extension to bottom dynamics: R_{AA} and v_n

- Prediction for B meson, electrons from semileptonic B meson decay within a coal + fragm model

Pb + Pb 5,02 TeV



Non-zero v_2, v_3 for bottom quark

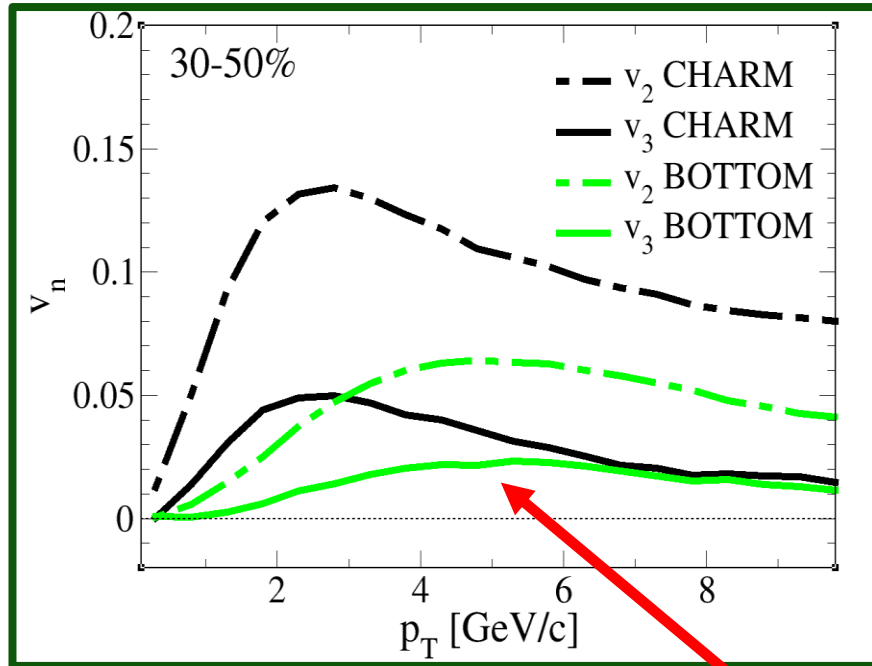
No parameters changed
with respect to charm dynamics

Extension to bottom dynamics: R_{AA} and v_n

Data taken from Arnaldi HP(2020)

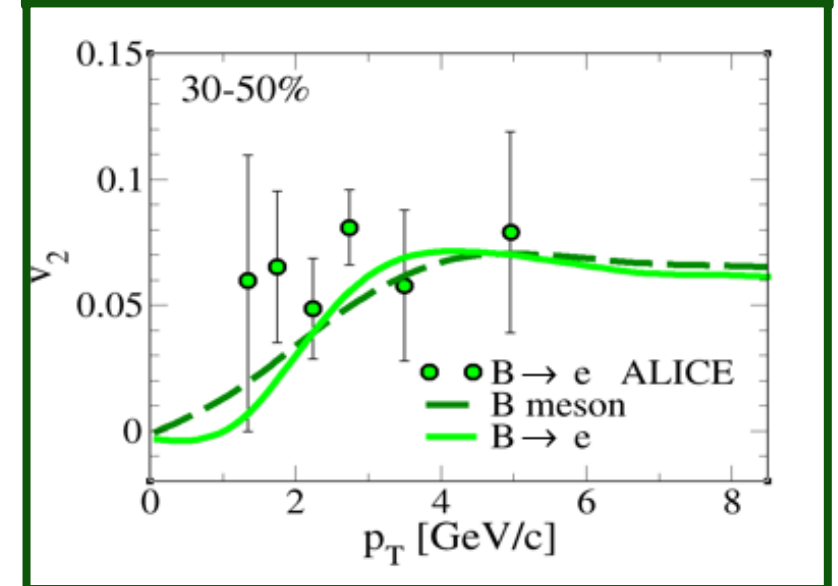
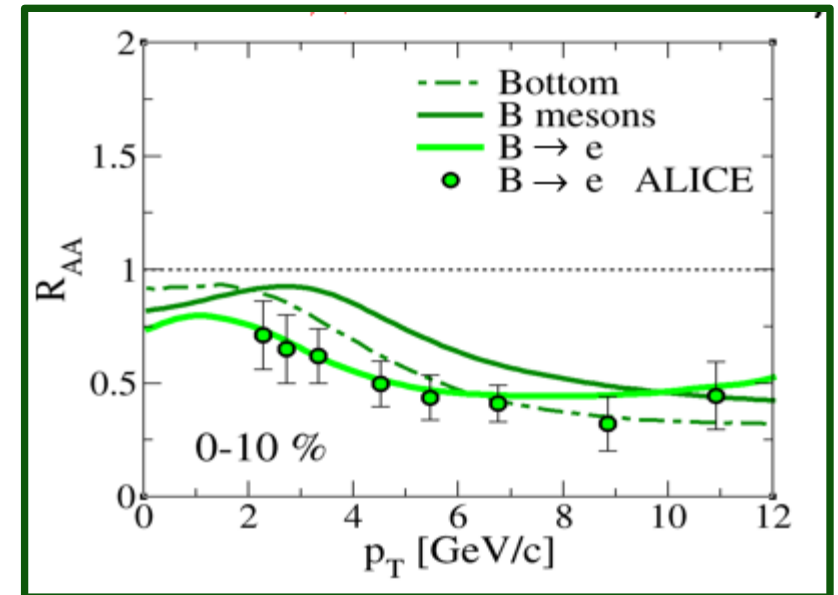
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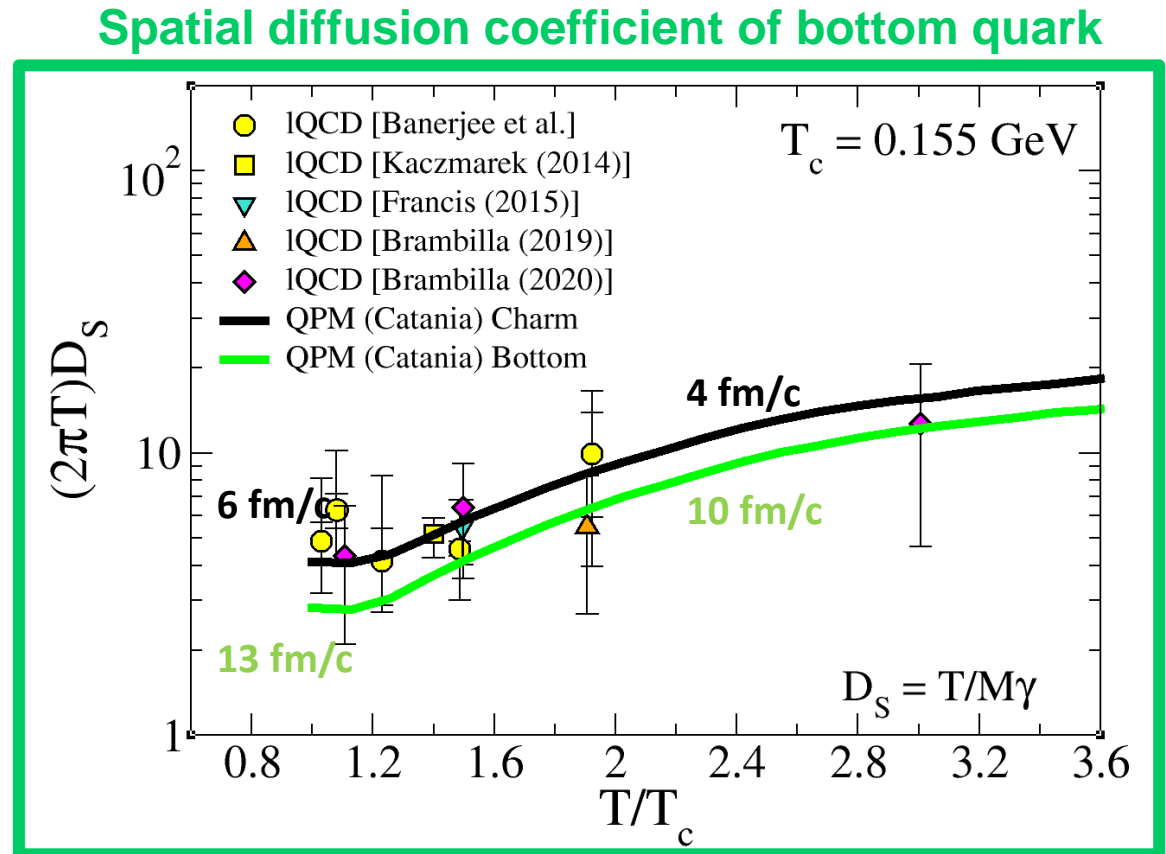
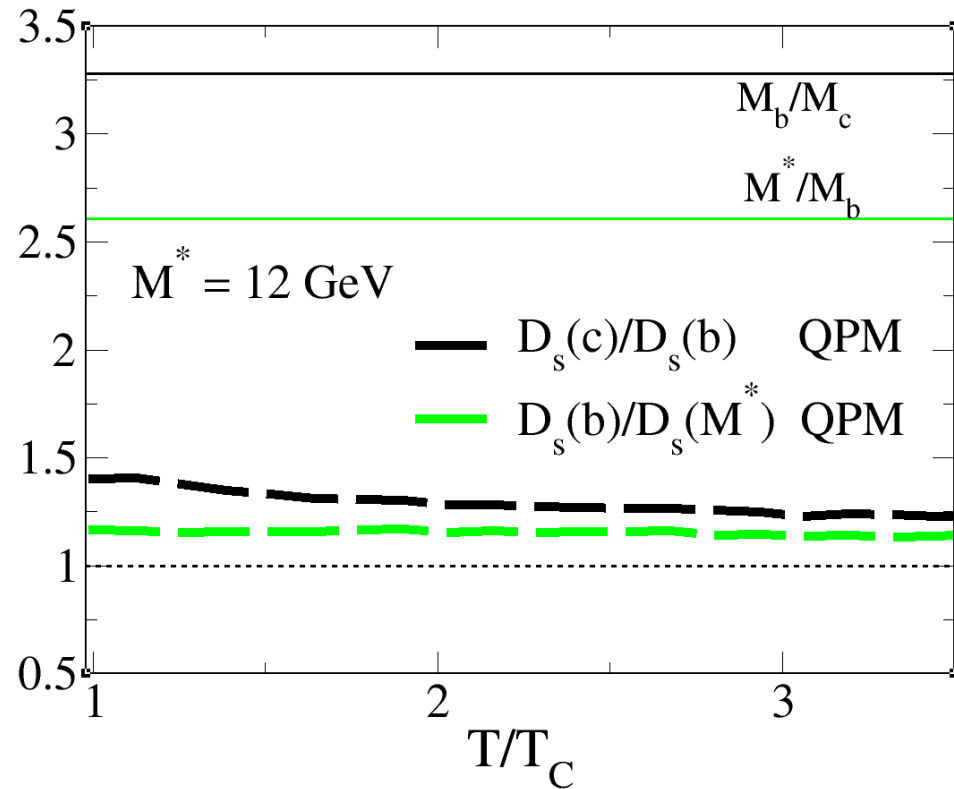


Non-zero v_2, v_3 for bottom quark

- R_{AA} and v_2 indicate a strong coupling for bottom with collectively expanding fireball



Charm quark vs Bottom quark



Kinetic theory: $\tau_{th}(b)/\tau_{th}(c) \approx \gamma_c/\gamma_b \approx M_b/M_c$

$$D_s = \frac{T}{M\gamma} = \frac{T}{M} \tau_{th} \text{ ideally } M \text{ independent } (M \rightarrow \infty)$$

In QPM approach $\rightarrow D_s(c)$ is 30-40% larger than $D_s(b)$
 $M \rightarrow \infty$ limit is not reached for charm

Results from $R_{AA}(p_T)$ and $v_2(p_T)$

FCC \rightarrow Bottom fully thermalized

ON-SHELL VS OFF-SHELL IN A STATIC BOX

Non-perturbative effects: impact of off-shell dynamics

QPM vs. DQPM

- Partons are dressed by non-perturbative spectral functions:

$$A_i^{BW}(m_i) = \frac{2}{\pi} \frac{m_i^2 \gamma_i^*}{(m_i^2 - M_i^2)^2 + (m_i \gamma_i^*)^2}$$

$$C[f] = \int dm_i A(m_i) \int dm_f A(m_f) \times \frac{1}{2E_p} \int \frac{d^3\mathbf{q}}{2E_q(2\pi)^3} \int \frac{d^3\mathbf{q}'}{2E_{q'}(2\pi)^3} \int \frac{d^3\mathbf{p}'}{2E_{p'}(2\pi)^3} \times \frac{1}{\gamma_Q} \sum |\mathcal{M}_Q|^2 (2\pi)^4 \delta^4(p+q-p'-q') \times [f(\mathbf{p}') \hat{f}(\mathbf{q}', m_f) - f(\mathbf{p}) \hat{f}(\mathbf{q}, m_i)]$$

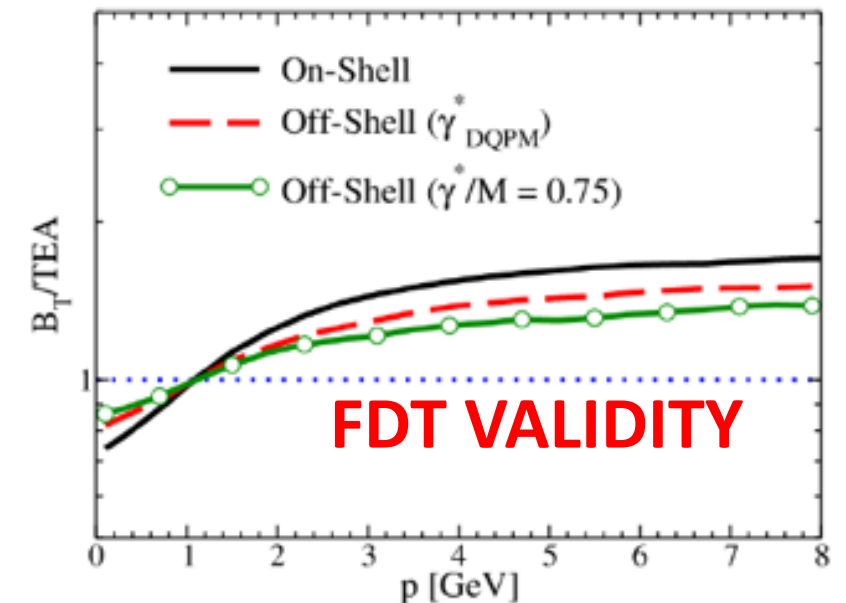
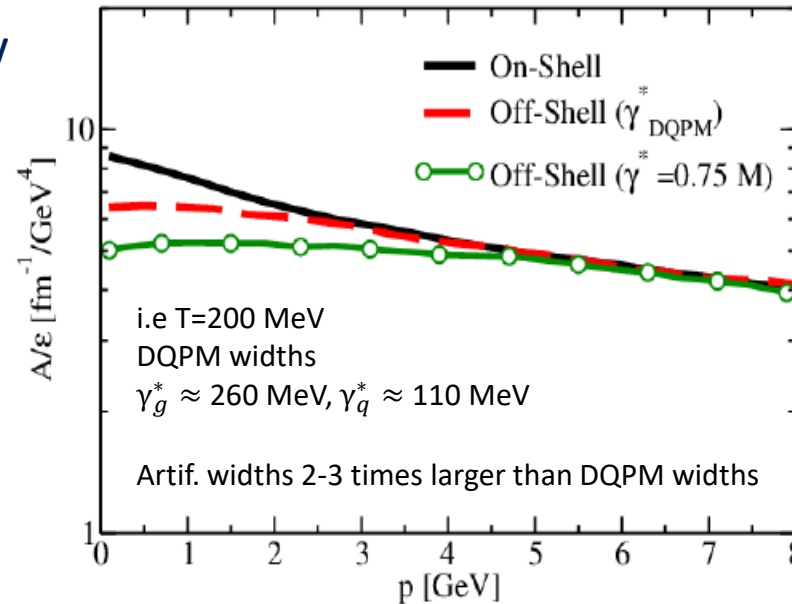
For references: W. Cassing, Nucl.Phys. A831, 215
 E. Bratkovskaya, Nucl.Phys. A856, 162
 H. Berrehrh, Phys. Rev. C 89(5), 054901
 M.L. Sambaturo et al., Eur.Phys.J.C 80 12, 1140

Off-shell \approx PHSD but also larger widths!

BOX CALCULATION [T=200 MeV] FOR CHARM

Bulk is not with the same energy density
The energy density of off-shell case is smaller

- Transport coefficient scales with energy density of the system ϵ
- Larger breaking for low p region ($p \lesssim 2-3$ GeV/c)
 → **larger off-shell effects**
 → 30-40% decreasing drag



On-shell vs Off-shell energy loss

BOX CALCULATION [T=200 MeV] FOR CHARM

➤ Partons are dressed by non-perturbative spectral functions:

$$A_i^{BW}(m_i) = \frac{2}{\pi} \frac{m_i^2 \gamma_i^*}{(m_i^2 - M_i^2)^2 + (m_i \gamma_i^*)^2}$$

Boltzmann equation and off-shell extension

$$p^\mu \partial_\mu f_Q = C[f_Q, f_g, f_q]$$

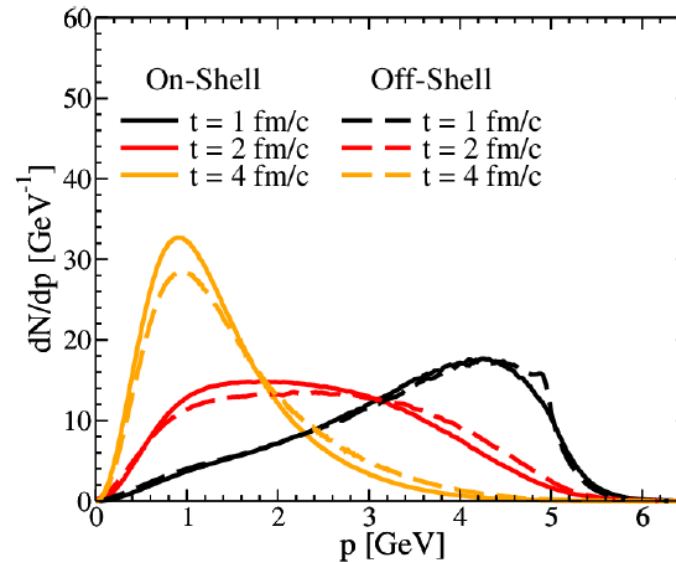
Plasma uniform $\rightarrow p^0 \partial_0 f_Q = C[f_Q, f_g, f_q]$

$$\frac{\partial f_Q}{\partial t} = \frac{1}{E_Q} C[f_q, f_g, f_Q]$$

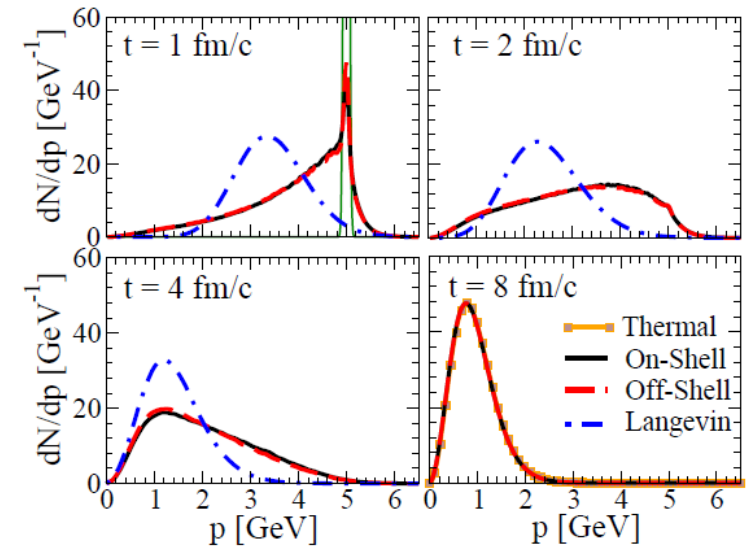
$$f(t + \Delta t, p) = f(t, p) + \frac{1}{E_Q} C[f]$$

$C[f_q, f_g, f_Q]$ Collision integral calc. both in on-shell and off-shell mode

$$\epsilon_{onshell} = \epsilon_{offshell}$$



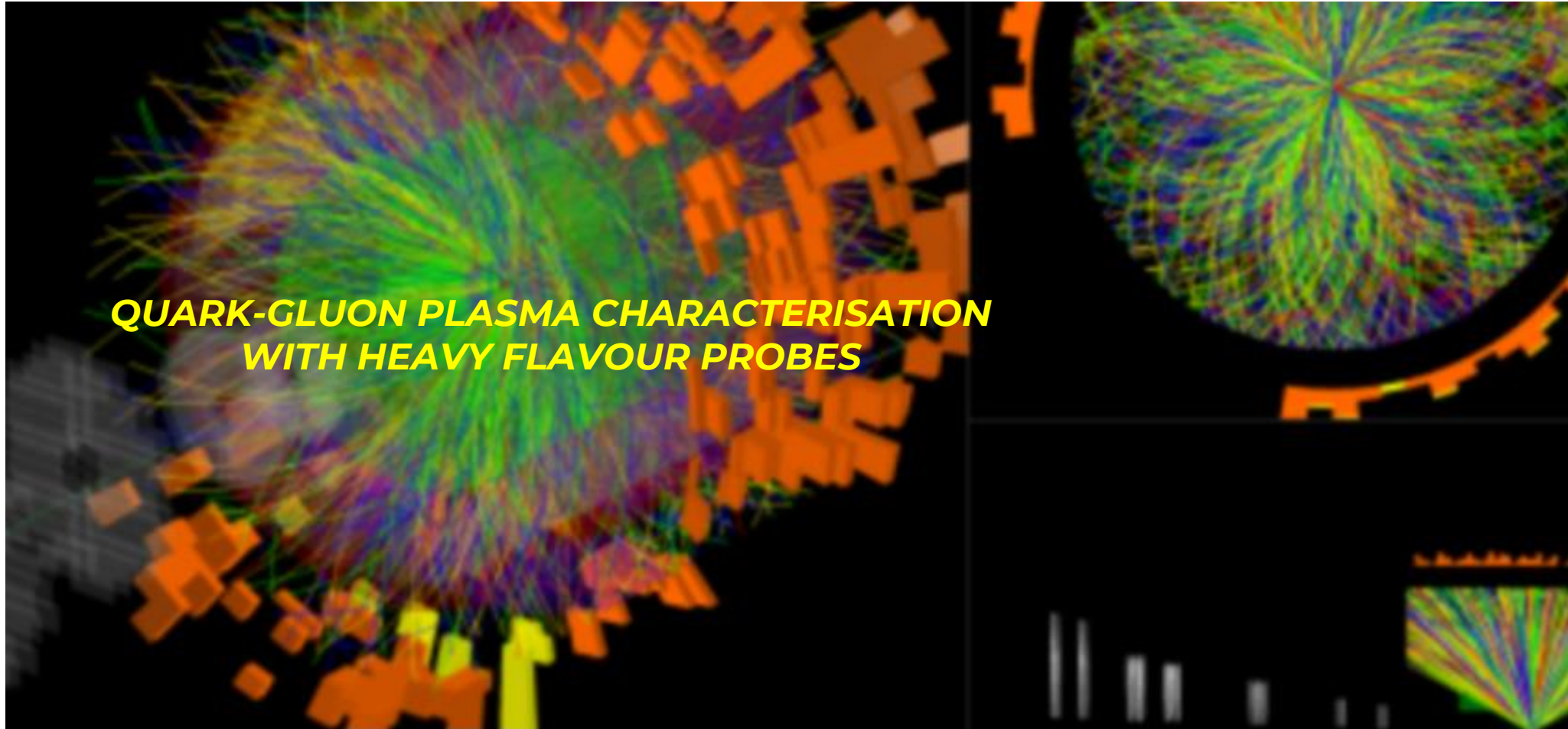
+k(p) making the Drag on-shell=Drag off-shell



The difference between on-shell and off-shell mode can be adsorbed by multiplying scattering matrix for a k factor

Conclusions

- $D_S(T)$ reproduces D meson R_{AA} and v_2
 - correct predictions for v_3 and q_2 selected anisotropic flow/spectra.
- Extension to bottom quark dynamics:
 - good description of R_{AA}, v_2 of electron from semileptonic B meson decay.
 - $D_S(T)$ of bottom in agreement with lattice QCD data within the still significantly large uncertainties.
- Prediction for significant $v_n - v_m$ correlation of hard particles, similar correlation between v_n of soft and hard particles.
- New perspectives: B meson v_3 and impact of Λ_B / B^0 on B meson R_{AA} .

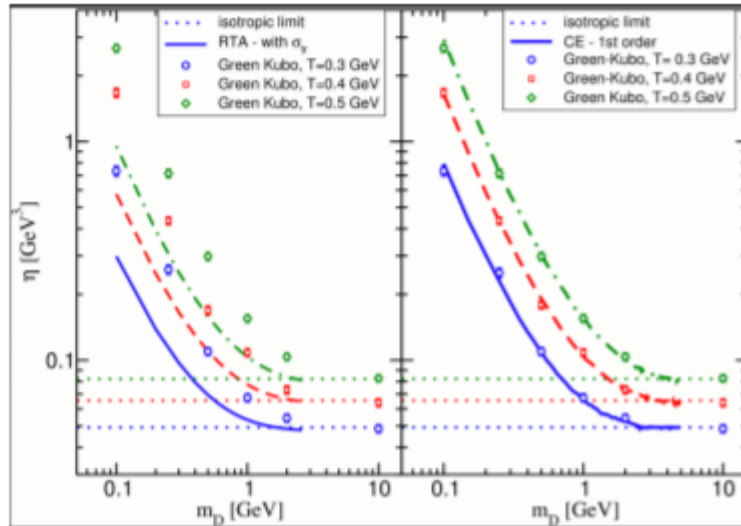


Thanks for your attention!

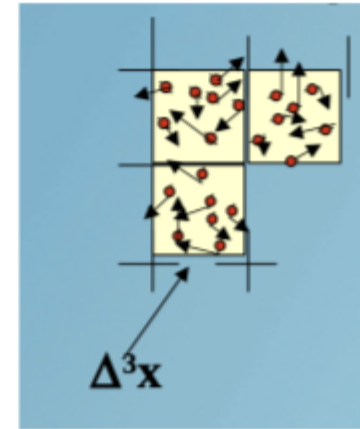
Back-up slides

We evaluate the cross section in each cell α according to the Chapman-Enskog formula in order to have a fluid at the wanted $\eta/s(T_\alpha)$ (S. Plumari et al., *Phys. Rev. C* 86, 054902 (2012)):

$$\sigma_{\text{tot},\alpha} = \frac{1}{15} \frac{\langle p \rangle_\alpha}{g \left(\frac{m_D}{T_\alpha} \right) n_\alpha} \frac{1}{\eta/s}.$$



Comparison between Relaxation Time Approximation, Chapman-Enskog and Green-Kubo. In the non-isotropic case CE works better than RTA.



From that we obtain the probability for a $2 \rightarrow 2$ collision (Z. Xu, C. Greiner, *Phys. Rev. C* 71, 064901 (2005)):

$$P = v_{\text{rel}} \sigma_{\text{tot}} \frac{\Delta t}{\Delta^3 x}.$$

Non-perturbative effects: impact of off-shell dynamics QPM vs. DQPM

- Partons are dressed by non-perturbative spectral functions:

$$A_i^{BW}(m_i) = \frac{2}{\pi} \frac{m_i^2 \gamma_i^*}{(m_i^2 - M_i^2)^2 + (m_i \gamma_i^*)^2}$$

$$\gamma_g(T) = \frac{1}{3} N_C \frac{g^2(T/T_C) T}{8\pi} \ln \left[\frac{2c}{g^2(T/T_C)} + 1 \right]$$

$$\gamma_q(T) = \frac{1}{3} \frac{N_C^2 - 1}{2N_C} \frac{g^2(T/T_C) T}{8\pi} \ln \left[\frac{2c}{g^2(T/T_C)} + 1 \right]$$

$$C[f] = \int dm_i A(m_i) \int dm_f A(m_f) \times \frac{1}{2E_p} \int \frac{d^3\mathbf{q}}{2E_q(2\pi)^3} \int \frac{d^3\mathbf{q}'}{2E_{q'}(2\pi)^3} \int \frac{d^3\mathbf{p}'}{2E_{p'}(2\pi)^3} \times \frac{1}{\gamma_Q} \sum |\mathcal{M}_Q|^2 (2\pi)^4 \delta^4(p+q-p'-q') \times [f(\mathbf{p}') \hat{f}(\mathbf{q}', m_f) - f(\mathbf{p}) \hat{f}(\mathbf{q}, m_i)]$$

Off-shell \approx PHSD

+k(p) making
the Drag off-shell=Drag off-shell

