

# Double Gamow-Teller resonances and their relation to neutrinoless $\beta\beta$ decays

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"Exploring the role of electro-weak currents in Atomic Nuclei"  
ECT\*, Trento, 26<sup>th</sup> April 2018



Graduate School of Science  
University of Tokyo

Center for Nuclear Study (CNS)



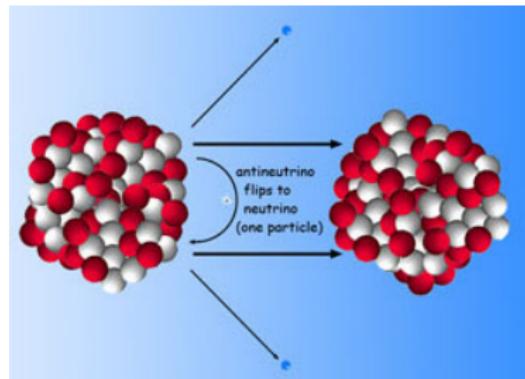
東京大学  
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KAKENHI

# Nuclear matrix elements for fundamental physics

Neutrinos, dark matter studied in experiments using nuclei

Nuclear matrix elements depend on nuclear structure crucial to anticipate reach and fully exploit experiments



$$0\nu\beta\beta \text{ decay: } (T_{1/2}^{0\nu\beta\beta})^{-1} \propto |M^{0\nu\beta\beta}|^2 m_{\beta\beta}^2$$

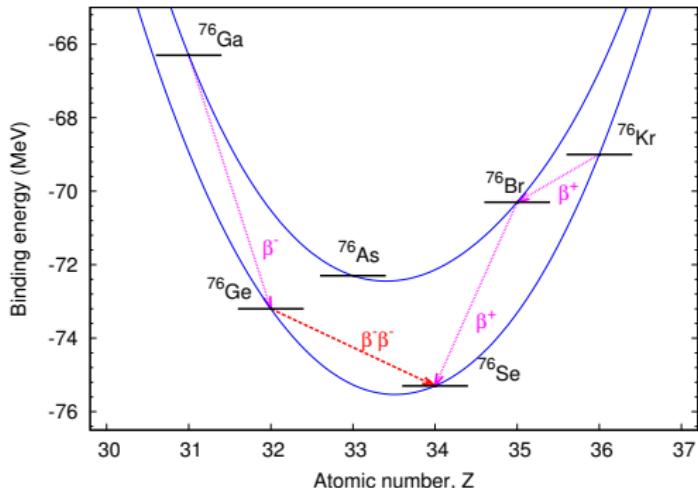
$$\text{Dark matter: } \frac{d\sigma_{\chi N}}{dq^2} \propto \left| \sum_i c_i \zeta_i \mathcal{F}_i \right|^2$$

$M^{0\nu\beta\beta}$ : Nuclear matrix element  
 $\mathcal{F}_i$  : Nuclear structure factor

# Neutrinoless $\beta\beta$ decay

Lepton-number violation, Majorana nature of neutrinos

Second order process only observable in rare cases  
with  $\beta$ -decay energetically forbidden or hindered by  $\Delta J$



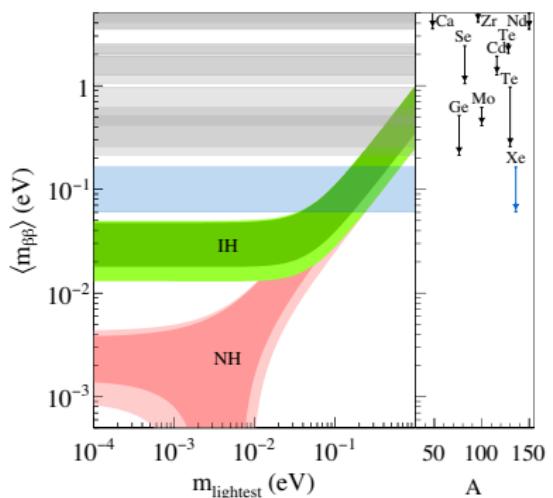
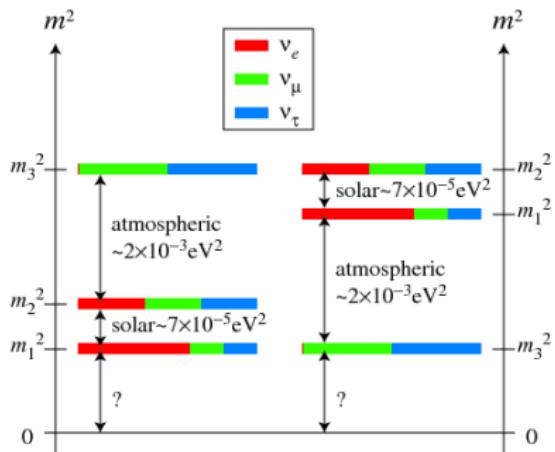
Best limit:  $^{76}\text{Ge}$  (GERDA),  $^{130}\text{Te}$  (CUORE),  $^{136}\text{Xe}$  (EXO, KamLAND-Zen)

# Next generation experiments: inverted hierarchy

The decay lifetime is

$$T_{1/2}^{0\nu\beta\beta} (0^+ \rightarrow 0^+)^{-1} = G_{01} |M^{0\nu\beta\beta}|^2 m_{\beta\beta}^2$$

sensitive to absolute neutrino masses,  $m_{\beta\beta} = |\sum U_{ek}^2 m_k|$ , and hierarchy



Matrix elements needed to make sure next generation ton-scale experiments fully explore "inverted hierarchy"

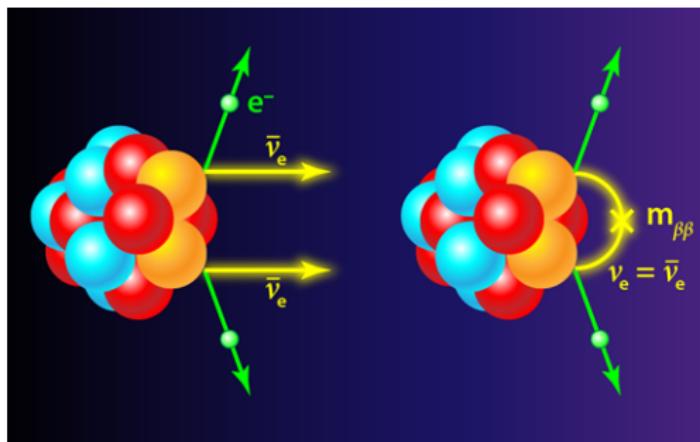
KamLAND-Zen, PRL117 082503(2016)

# Calculating nuclear matrix elements

Nuclear matrix elements needed to study fundamental symmetries

$$\langle \text{Final} | \mathcal{L}_{\text{leptons-nucleons}} | \text{Initial} \rangle = \langle \text{Final} | \int dx j^\mu(x) J_\mu(x) | \text{Initial} \rangle$$

- Nuclear structure calculation of the initial and final states:  
Shell model, QRPA, IBM,  
Energy-density functional  
Ab initio many-body methods  
GFMC, Coupled-cluster, IM-SRG...
- Lepton-nucleus interaction:  
Hadronic current in nucleus:  
phenomenological,  
effective theory of QCD

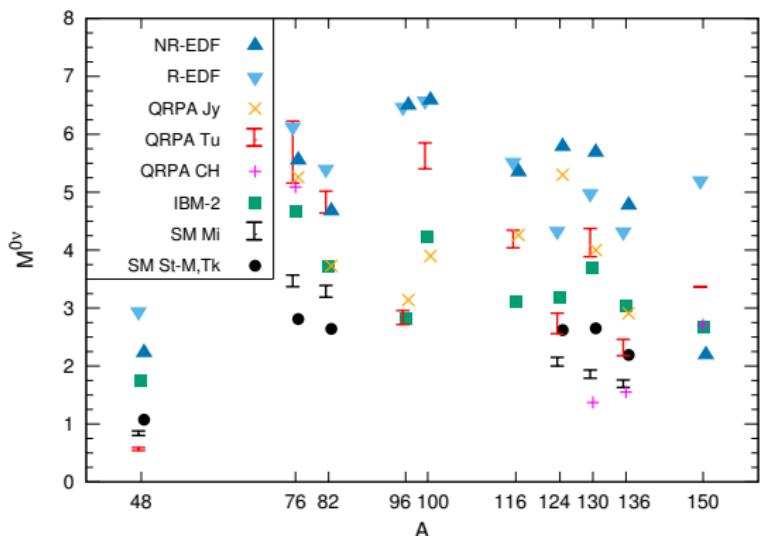


# $0\nu\beta\beta$ decay nuclear matrix elements

Large difference in nuclear matrix element calculations: factor  $\sim 2 - 3$

$$\langle 0_f^+ | \sum_{n,m} \tau_n^- \tau_m^- \sum_X H^X(r) \Omega^X | 0_i^+ \rangle$$

$\Omega^X$  = Fermi ( $\mathbb{1}$ ), GT ( $\sigma_n \sigma_m$ ), Tensor  
 $H(r)$  = neutrino potential



How can  
nuclear matrix elements  
calculations improve?

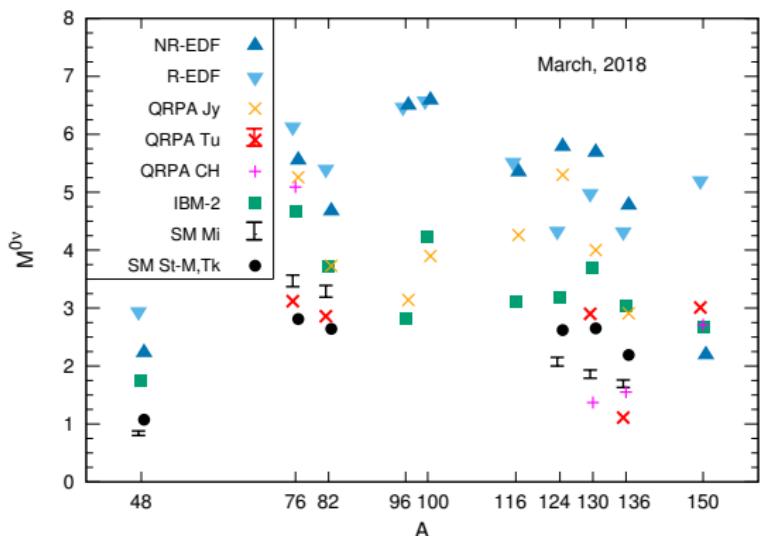
How can  
nuclear structure experiments  
guide  $0\nu\beta\beta$  decay?

# $0\nu\beta\beta$ decay nuclear matrix elements

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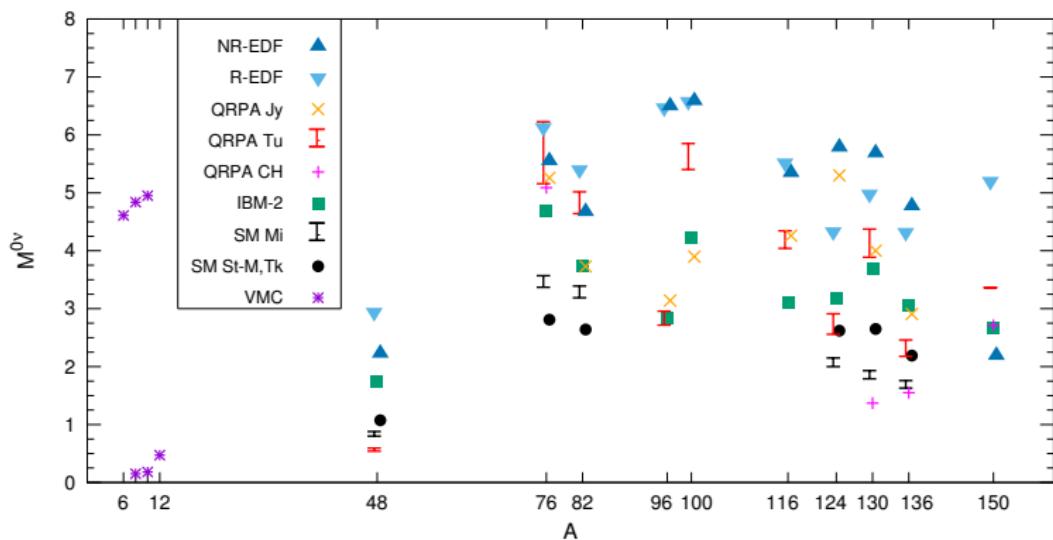
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# $0\nu\beta\beta$ decay nuclear matrix elements

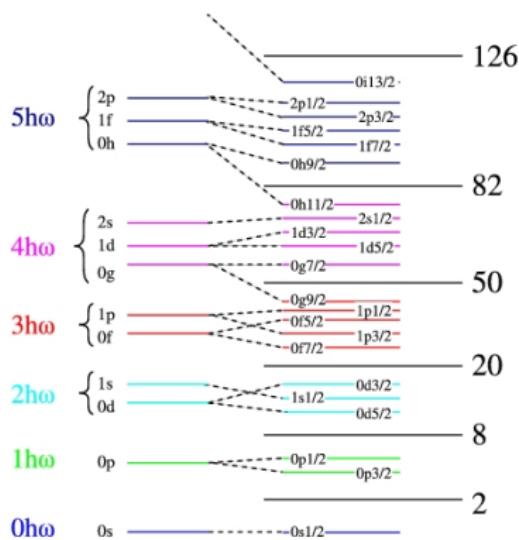
Large difference in nuclear matrix element calculations: factor  $\sim 2 - 3$

$$\langle 0_f^+ | \sum_{n,m} \tau_n^- \tau_m^- \sum_X H^X(r) \Omega^X | 0_i^+ \rangle$$

$\Omega^X$  = Fermi ( $\mathbb{1}$ ), GT ( $\sigma_n \sigma_m$ ), Tensor  
 $H(r)$  = neutrino potential



# Configuration space



Nuclear shell model configuration space  
only keep essential degrees of freedom

- High-energy orbits: always empty
- Configuration space:  
where many-body problem is solved
- Inert core: always filled

$$H|\Psi\rangle = E|\Psi\rangle \rightarrow H_{\text{eff}}|\Psi\rangle_{\text{eff}} = E|\Psi\rangle_{\text{eff}}$$

$$|\Psi\rangle_{\text{eff}} = \sum_{\alpha} c_{\alpha} |\phi_{\alpha}\rangle, \quad |\phi_{\alpha}\rangle = a_{i1}^+ a_{i2}^+ \dots a_{iA}^+ |0\rangle$$

Shell model codes (1 major oscillator shell)  
 $\sim 10^{10}$  Slater dets. Caurier et al. RMP77 (2005)

QRPA calculations suggest  
larger spaces ( $\gtrsim 2$  major shells) needed

Dimension  $\sim$

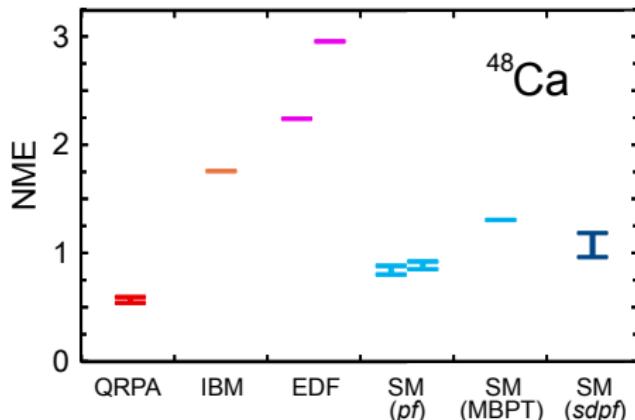
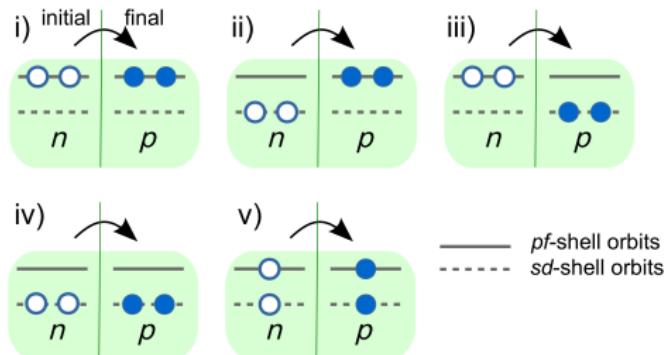
$$\binom{(p+1)(p+2)}{N}_{\nu} \binom{(p+1)(p+2)}{Z}_{\pi}$$

# Shell model configuration space: two shells

For  $^{48}\text{Ca}$  enlarge configuration space from  $pf$  to  $sdpf$

4 to 7 orbitals, dimension  $10^5$  to  $10^9$   
increases matrix elements  
but only moderately 30%

Iwata et al. PRL116 112502 (2016)



Contributions dominated by pairing  
2 particle – 2 hole excitations  
enhance the  $\beta\beta$  matrix element,

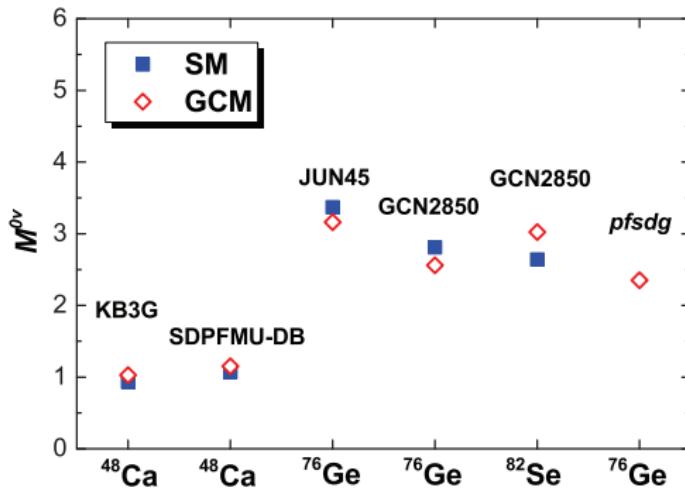
Contributions dominated by  
1 particle – 1 hole excitations  
suppress the  $\beta\beta$  matrix element

# $^{76}\text{Ge}$ matrix element in two shells

Large configuration space calculations in 2 major oscillator shells

Include all relevant correlations: isovector/isoscalar pairing, deformation

Many-body approach: generating coordinate method (GCM)



GCM approximates shell model calculation

Degrees of freedom, or generating coordinates, validated against exact shell model in small configuration space

Jiao et al. PRC96 054310 (2017)

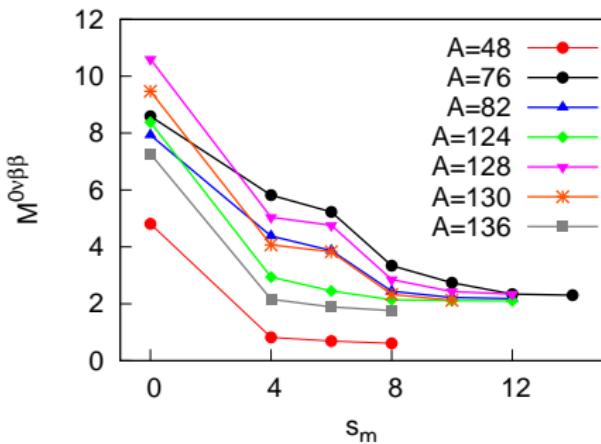
$^{76}\text{Ge}$  nuclear matrix element in 2 major shells

very similar to shell model nuclear matrix element in 1 major shell

# Pairing correlations and $0\nu\beta\beta$ decay

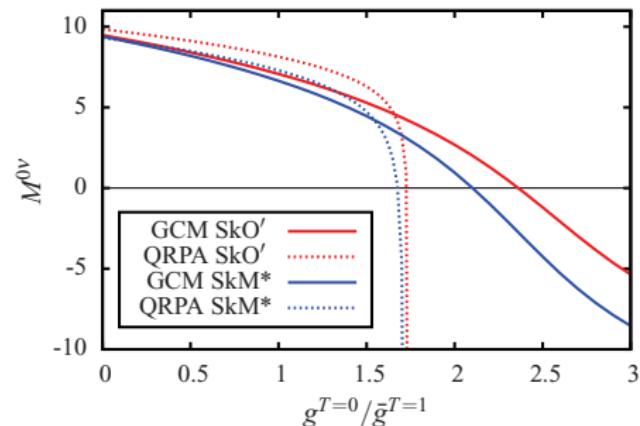
$0\nu\beta\beta$  decay favoured by proton-proton, neutron-neutron pairing,  
but it is disfavored by proton-neutron pairing

Ideal case: superfluid nuclei  
reduced with high-seniorities



Caurier et al. PRL100 052503 (2008)

Addition of isoscalar pairing  
reduces matrix element value



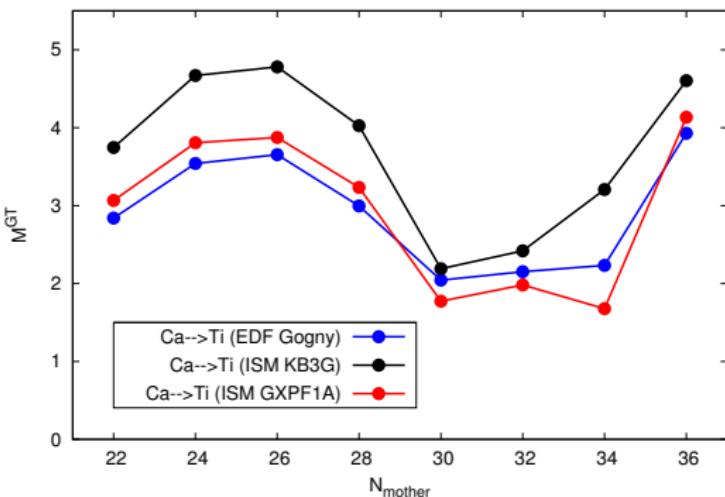
Hinohara, Engel PRC90 031301 (2014)

Related to approximate  $SU(4)$  symmetry of the  $\sum H(r)\sigma_i\sigma_j\tau_i\tau_j$  operator

# $0\nu\beta\beta$ decay without correlations

Non-realistic spherical (uncorrelated) mother and daughter nuclei:

- Shell model (SM): zero seniority, neutron and proton  $J = 0$  pairs
- Energy density functional (EDF): only spherical contributions



In contrast to full  
(correlated) calculation  
SM and EDF NMEs agree!

NME scale set by  
pairing interaction

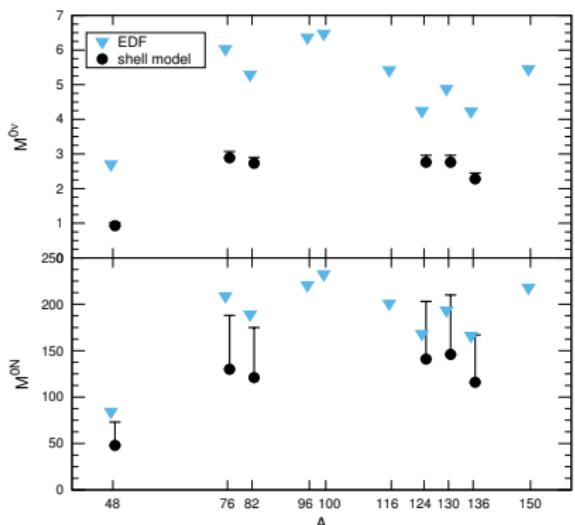
JM, Rodríguez, Martínez-Pinedo,  
Poves PRC90 024311(2014)

NME follows generalized  
seniority model:

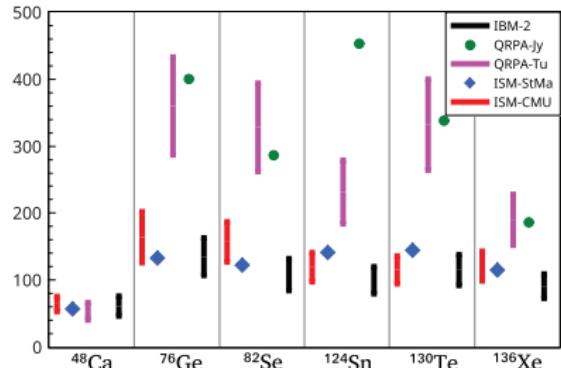
$$M_{GT}^{0\nu\beta\beta} \simeq \alpha_\pi \alpha_\nu \sqrt{N_\pi + 1} \sqrt{\Omega_\pi - N_\pi} \sqrt{N_\nu} \sqrt{\Omega_\nu - N_\nu + 1}, \text{ Barea, Iachello PRC79 044301(2009)}$$

# Heavy-neutrino exchange nuclear matrix elements

Contrary to light-neutrino-exchange, for heavy-neutrino-exchange decay shell model, IBM, and EDF matrix elements agree reasonably!



Song et al. PRC95 024305 (2017)  
JM, JPG 45 014003 (2018)



Neacsu et al. PRC100 052503 (2015)

Suggests differences in treating longer-range nuclear correlations dominant in light-neutrino exchange

# Heavy-neutrino matrix element

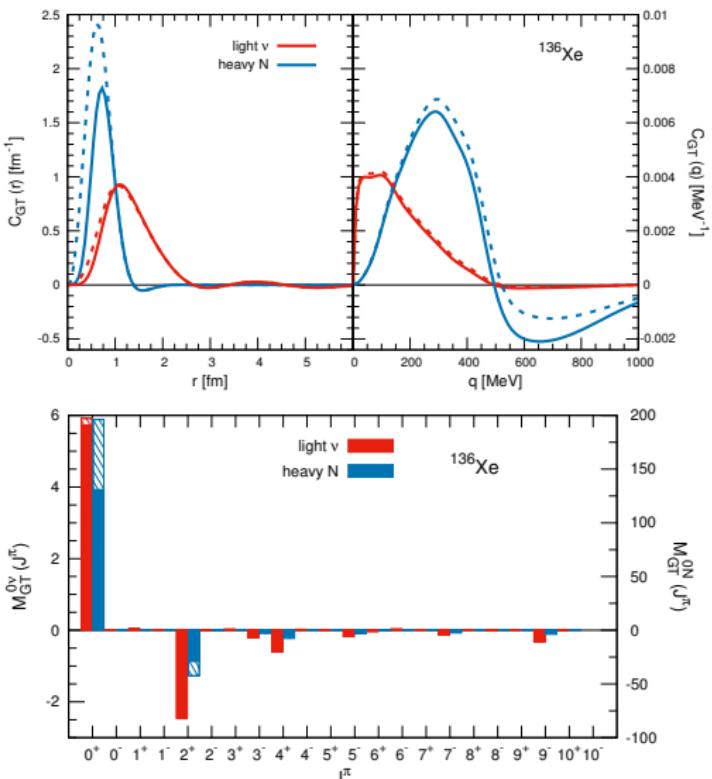
Compared to  
light-neutrino exchange

heavy neutrino exchange  
dominated by  
shorter internucleon range,  
larger momentum transfers

heavy neutrino exchange  
contribution  
from  $J > 0$  pairs smaller:  
pairing most relevant

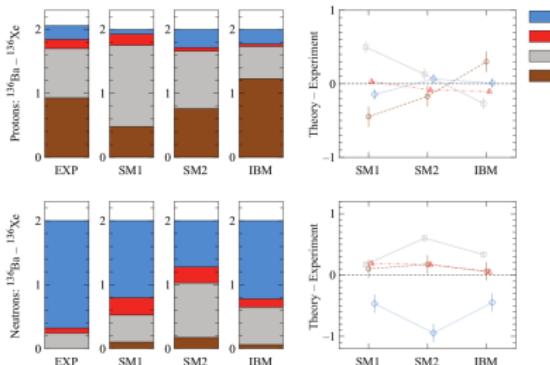
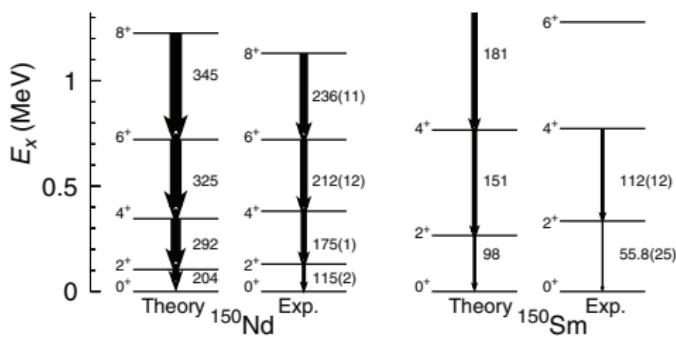
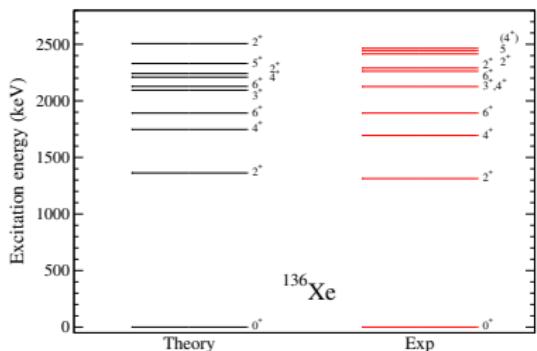
⇒

Long-range correlations  
(except pairing)  
not under control



# Tests of nuclear structure

Spectroscopy well described: masses, spectra, transitions, knockout...



Schiffer et al. PRL100 112501(2009)

Kay et al. PRC79 021301(2009)

...

Szwec et al., PRC94 054314 (2016)

Rodríguez et al. PRL105 252503 (2010)

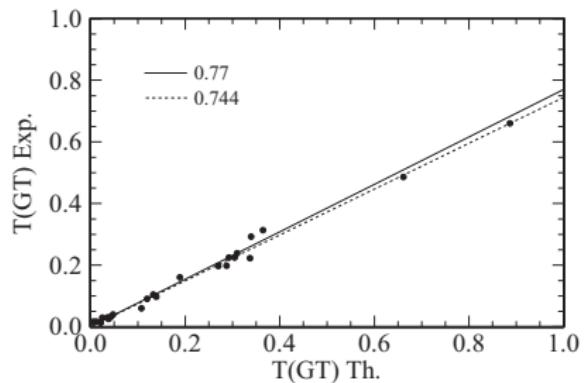
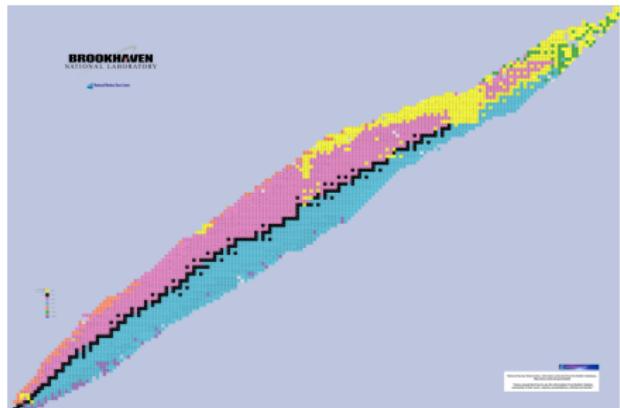
...

Vietze et al. PRD91 043520 (2015)

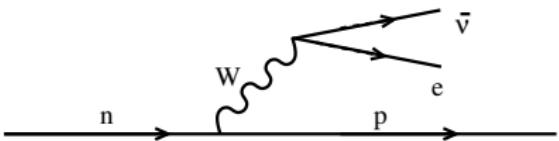
## $\beta$ decays

$\beta$  decays ( $e^-$  capture) main decay model along nuclear chart

In general well described by nuclear structure theory: shell model...



Martinez-Pinedo et al. PRC53 2602(1996)



$$\langle F | \sum_i [g_A \sigma_i \tau_i^-]^{\text{eff}} | I \rangle, \quad [\sigma_i \tau]^{\text{eff}} \approx 0.7 \sigma_i \tau$$

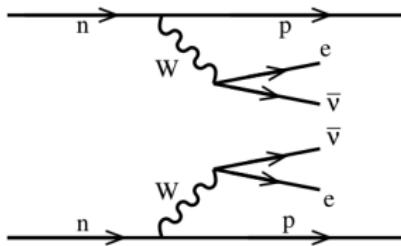
Gamow-Teller transitions:  
theory needs  $\sigma_i \tau$  "quenching"

# Two-neutrino $\beta\beta$ decay

Test of  $0\nu\beta\beta$  decay: comparison of predicted  $2\nu\beta\beta$  decay vs data

Shell model  
reproduce  $2\nu\beta\beta$  data  
including "quenching"  
common to  $\beta$  decays  
in same mass region

Shell model prediction  
previous to  
 $^{48}\text{Ca}$  measurement!



**Table 2**

The ISM predictions for the matrix element of several  $2\nu$  double beta decays (in  $\text{MeV}^{-1}$ ). See text for the definitions of the valence spaces and interactions.

	$M^{2\nu}(\text{exp})$	$q$	$M^{2\nu}(\text{th})$	INT
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.047	kb3
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.048	kb3g
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.065	gxpfl
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140 \pm 0.005$	0.60	0.116	gcn28:50
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140 \pm 0.005$	0.60	0.120	jun45
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	$0.098 \pm 0.004$	0.60	0.126	gcn28:50
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	$0.098 \pm 0.004$	0.60	0.124	jun45
$^{128}\text{Te} \rightarrow ^{128}\text{Xe}$	$0.049 \pm 0.006$	0.57	0.059	gcn50:82
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	$0.034 \pm 0.003$	0.57	0.043	gcn50:82
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	$0.019 \pm 0.002$	0.45	0.025	gcn50:82

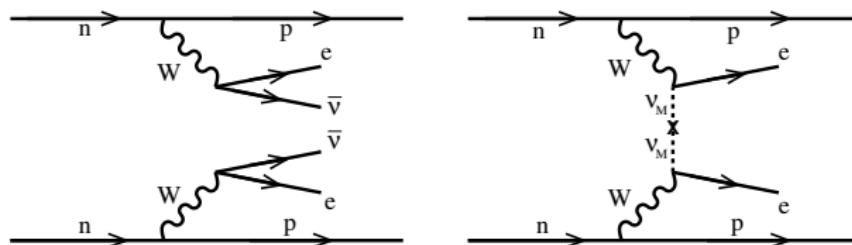
Caurier, Nowacki, Poves PLB711 62(2012)

$$M^{2\nu\beta\beta} = \sum_k \frac{\langle 0_f^+ | \sum_n \sigma_n \tau_n^- | 1_k^+ \rangle \langle 1_k^+ | \sum_m \sigma_m \tau_m^- | 0_i^+ \rangle}{E_k - (M_i + M_f)/2}$$

# $\mu$ -capture, $\nu$ -nucleus scattering

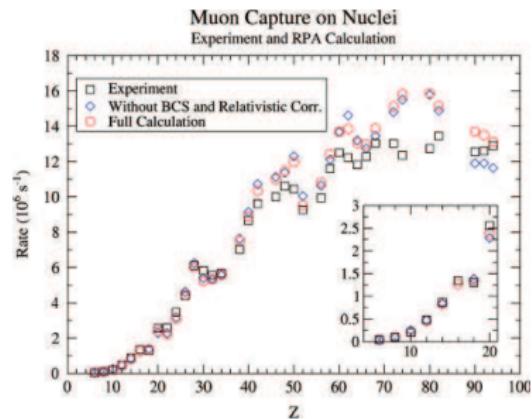
Momentum transfers very different in  $\beta\beta$  decays:

$2\nu\beta\beta$  decay ( $q \sim 1$  MeV) and  $0\nu\beta\beta$  decay ( $q \sim 100$  MeV)



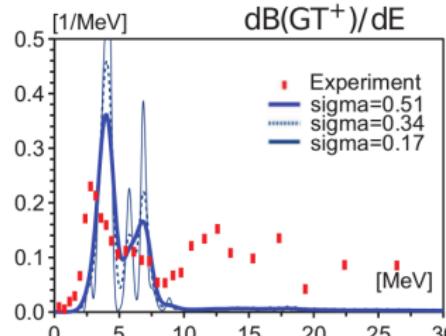
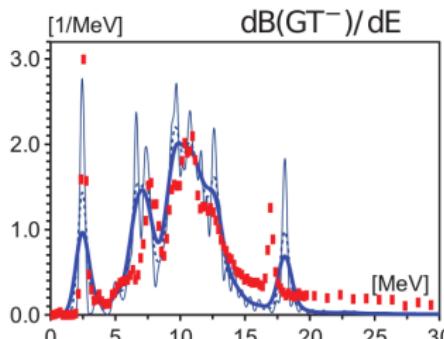
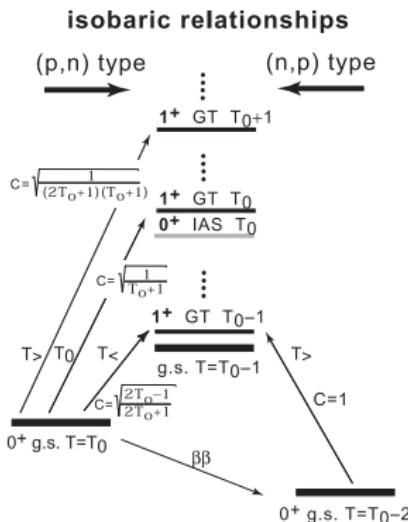
Muon-capture,  
neutrino-nucleus scattering  
(to low-energy states)  
probe similar momentum  
transfers than  $0\nu\beta\beta$  decay

Several multipolarities ( $J$  values)  
contribute, like in  $0\nu\beta\beta$  decay



# Gamow-Teller strength distributions

Gamow-Teller (GT) distributions well described by theory (quenched)



Iwata et al. JPSCP 6 03057 (2015)

$$\langle 1_f^+ | \sum_i [\sigma_i \tau_i^\pm]_{\text{eff}} | 0_{\text{gs}}^+ \rangle, \quad [\sigma_i \tau_i^\pm]_{\text{eff}} \approx 0.7 \sigma_i \tau_i^\pm$$

$$M^{2\nu\beta\beta} = \sum_k \frac{\langle 0_f^+ | \sum_n \sigma_n \tau_n^- | 1_k^+ \rangle \langle 1_k^+ | \sum_m \sigma_m \tau_m^- | 0_i^+ \rangle}{E_k - (M_i + M_f)/2}$$

Frekers et al.

NPA916 219 (2013)

# Double Gamow-Teller strength distribution

Measurement of Double Gamow-Teller (DGT) resonance  
in double charge-exchange reactions  $^{48}\text{Ca}(\text{pp},\text{nn})^{48}\text{Ti}$  proposed in 80's

Auerbach, Muto, Vogel... 1980's, 90's

Recent experimental plans in RCNP, RIKEN ( $^{48}\text{Ca}$ ), INFN Catania

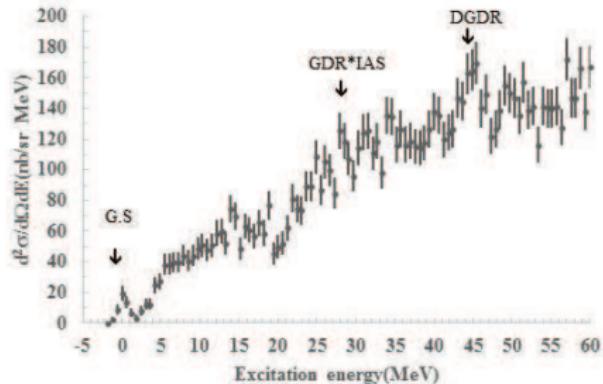
Takaki et al. JPS Conf. Proc. 6 020038 (2015)

Capuzzello et al. EPJA 51 145 (2015), Takahisa, Ejiri et al. arXiv:1703.08264

Promising connection to  $\beta\beta$  decay,  
two-particle-exchange process,  
especially the (tiny) transition  
to ground state of final state

Two-nucleon transfers related to  
 $0\nu\beta\beta$  decay matrix elements

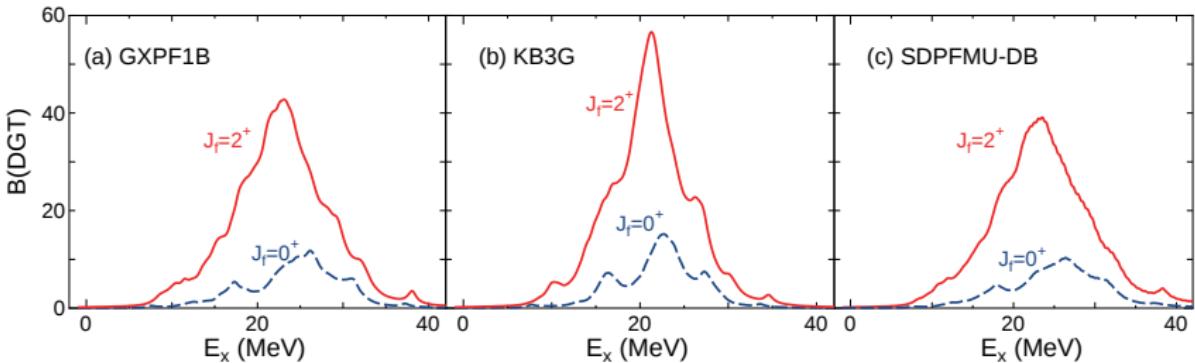
Brown et al. PRL113 262501 (2014)



# $^{48}\text{Ca}$ Double Gamow-Teller distribution

Calculate with shell model  $^{48}\text{Ca } 0^+_{\text{gs}}$  Double Gamow-Teller distribution

$$B(DGT^-; \lambda; i \rightarrow f) = \frac{1}{2J_i + 1} \left| \left\langle {}^{48}\text{Ti} \right| \left[ \sum_i \sigma_i \tau_i^- \times \sum_j \sigma_j \tau_j^- \right]^{(\lambda)} \right| {}^{48}\text{Ca}_{\text{gs}} \right|^2$$



Shell model calculation with Lanczos strength function method

Double GT resonances in one and two shells rather similar result

Shimizu, JM, Yako, PRL120 142502 (2018)

# Double Gamow-Teller distribution and pairing

Study the sensitivity of Double GT distribution to pairing correlations

Add/remove pairing

$$H' = H + G^{JT} P^{JT}$$

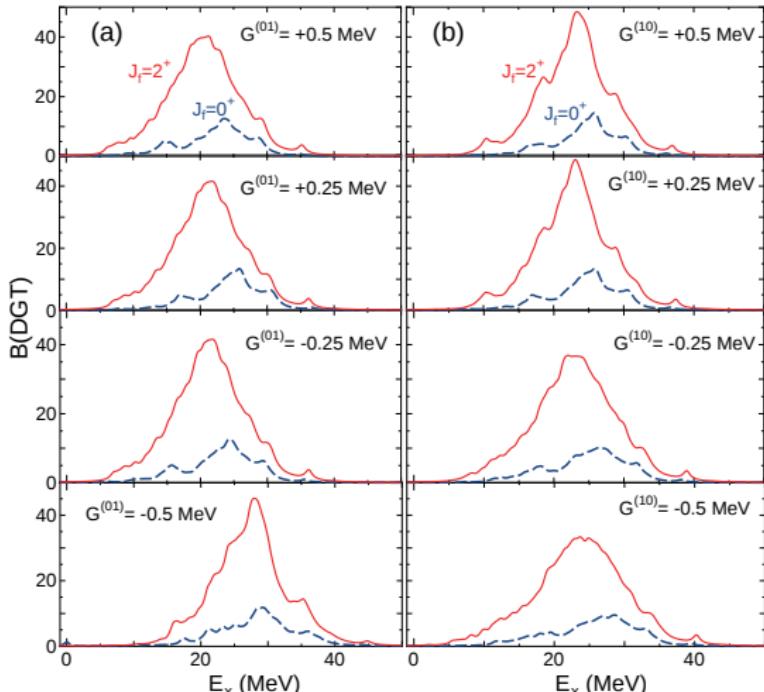
like-particle ( $T=1$ ) or  
proton-neutron ( $T=0$ )

Position of the  
DGT giant resonance  
very sensitive to  
like-particle pairing

DGT resonance width  
probes isoscalar pairing

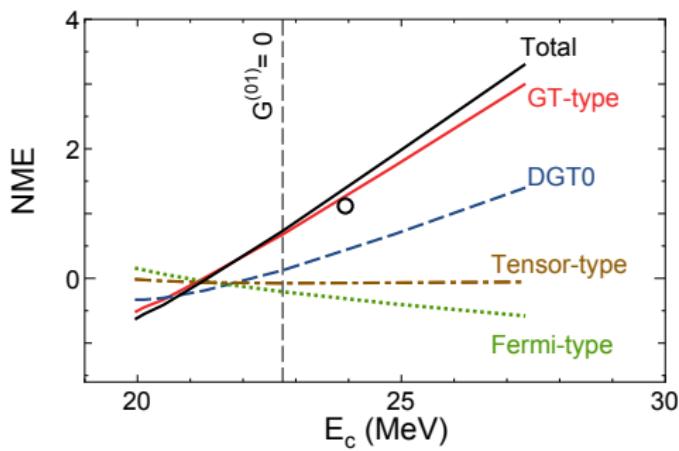
Shimizu, JM, Yako

PRL120 142502 (2018)



# $^{48}\text{Ca}$ double GT giant resonance and $0\nu\beta\beta$ decay

Correlation between Double Gamow-Teller resonance in  $^{48}\text{Ca}$  and  $0\nu\beta\beta$  decay nuclear matrix element



Energy of DGT resonance  
with accuracy to  $\sim 1\text{MeV}$ ,  
can give insight on value of  
 $0\nu\beta\beta$  decay matrix element

$$E_{\text{av}} = \frac{\sum_f E_f B(DGT^-, i \rightarrow f)}{\sum_f B(DGT^-, i \rightarrow f)}$$

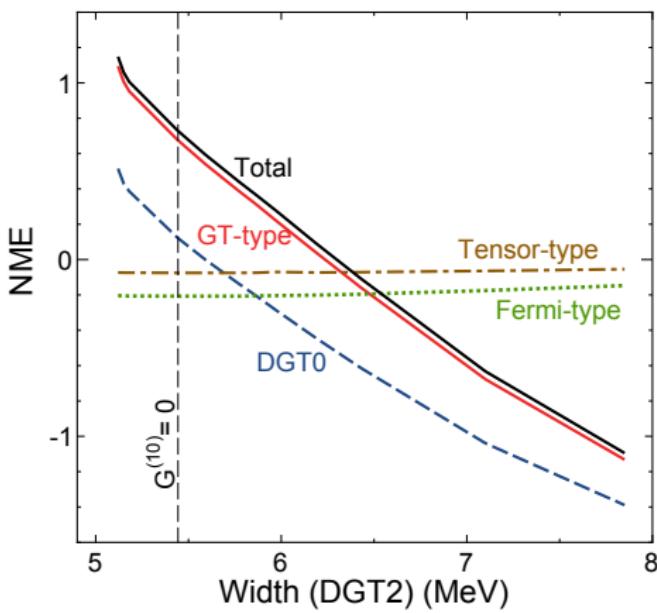
Good test of  
nuclear structure calculation

Shimizu, JM, Yako,  
PRL120 142502 (2018)

Relatively consistent with  $sdpf$  calculation (open circle)

# $^{48}\text{Ca}$ double GT resonance width and $0\nu\beta\beta$ decay

Correlation between the width of the double GT giant resonance and the  $0\nu\beta\beta$  decay nuclear matrix element



Double GT resonance width probably not very useful to determine  $0\nu\beta\beta$  matrix element

Large experimental precision much better than 1 MeV needed

Nuclear matrix element changes sign (not observable)

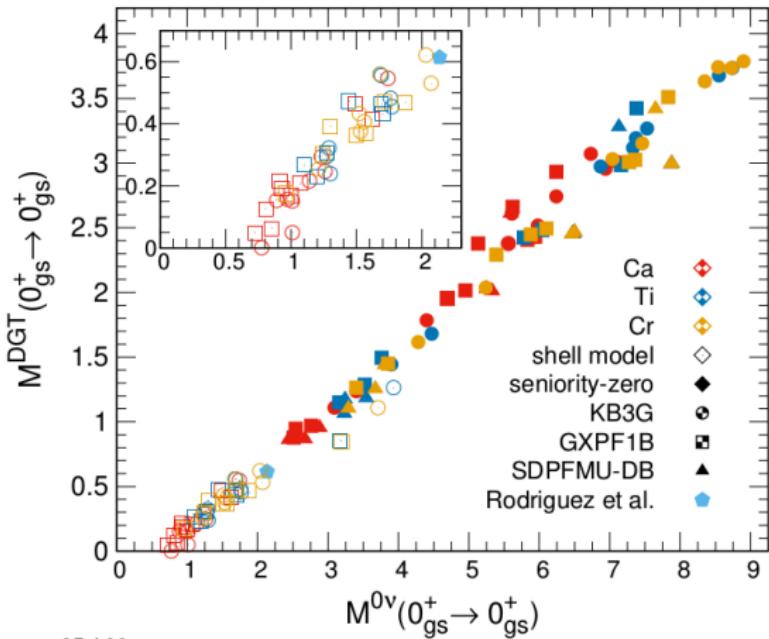
$$\sigma_{DGT} = \sqrt{\frac{\sum_f (E_f - E_{av})^2 B(\text{DGT}^-, i \rightarrow f)}{\sum_f B(\text{DGT}^-, i \rightarrow f)}}$$

# DGT to ground state and $0\nu\beta\beta$ decay

DGT transition to ground state of final nucleus:

Ca, Ti, Cr isotopic chains

$$M^{\text{DGT}} = \langle \text{Final}_{\text{gs}} | [(\sum_i \sigma_i \tau_i^-) \times (\sum_j \sigma_j \tau_j^-)]^0 | \text{Initial}_{\text{gs}} \rangle|^2$$

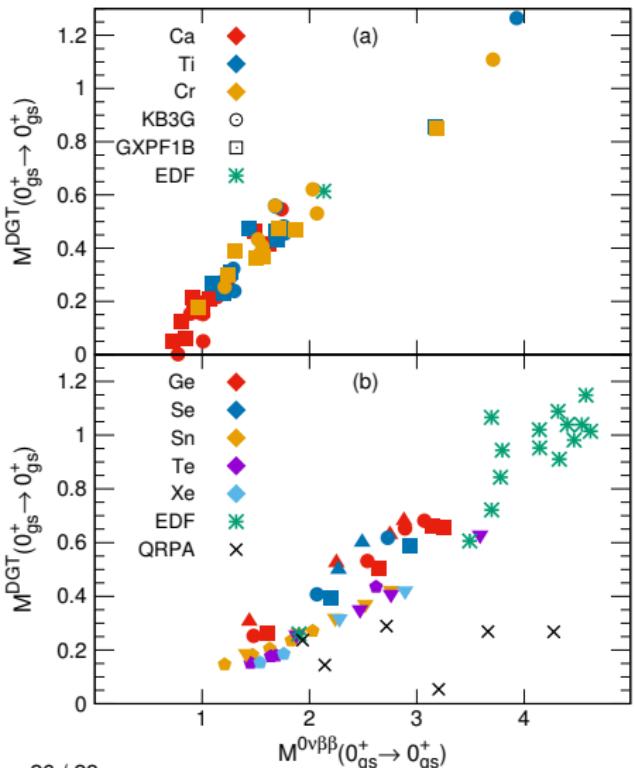


Very good linear correlation between DGT and  $0\nu\beta\beta$  decay nuclear matrix elements

Linear correlation holds for  $\sim 25$  transitions studied for simplified wf's (seniority-zero), for different interactions

Shimizu, JM, Yako,  
PRL120 142502 (2018)

# DGT and $0\nu\beta\beta$ decay: heavy nuclei



DGT transition to ground state

$$M^{\text{DGT}} = \sqrt{B(\text{DGT}_-; 0; 0_{\text{gs}}^+ \rightarrow 0_{\text{gs}}^+)}$$

very good linear correlation  
with  $0\nu\beta\beta$  decay  
nuclear matrix elements

Correlation holds  
across wide range of nuclei,  
from Ca to Ge and Xe

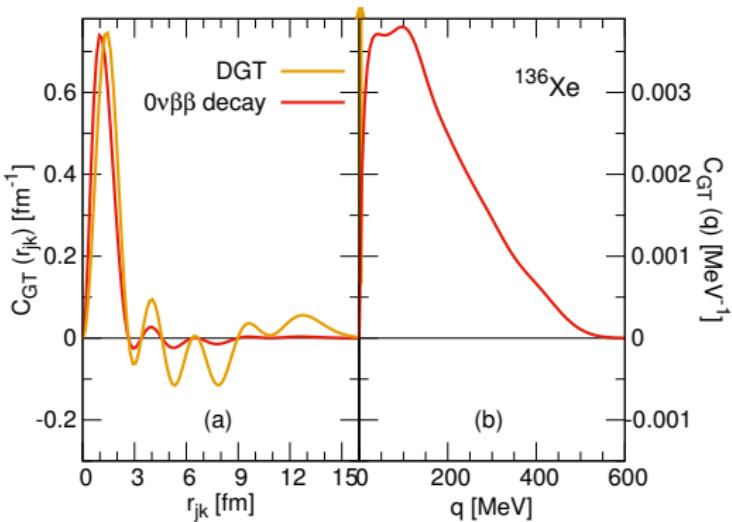
Common to shell model and  
energy-density functional theory  
 $0 \lesssim M^{0\nu\beta\beta} \lesssim 5$   
disagreement to QRPA

Shimizu, JM, Yako,  
PRL120 142502 (2018)

# Short-range character of DGT, $0\nu\beta\beta$ decay

Correlation between DGT and  $0\nu\beta\beta$  decay matrix elements explained by transition involving low-energy states combined with dominance of short distances between exchanged/decaying neutrons

Bogner et al. PRC86 064304 (2012)



$0\nu\beta\beta$  decay matrix element limited to shorter range

Short-range part dominant in double GT matrix element due to partial cancellation of mid- and long-range parts

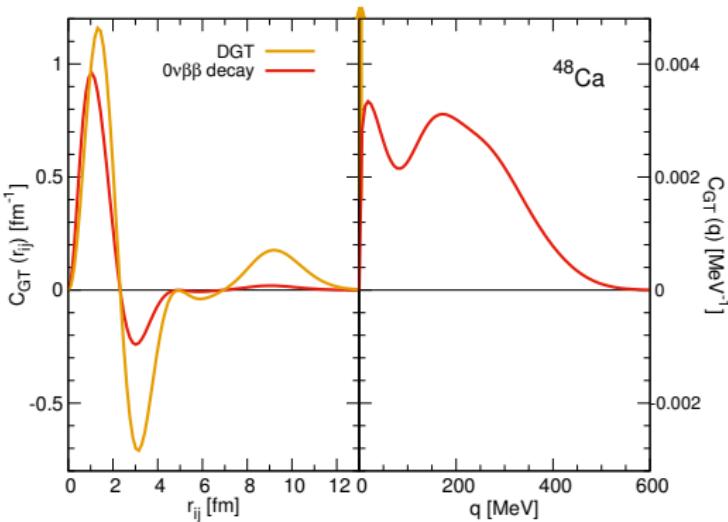
Long-range part dominant in QRPA DGT matrix elements

Shimizu, JM, Yako,  
PRL120 142502 (2018)

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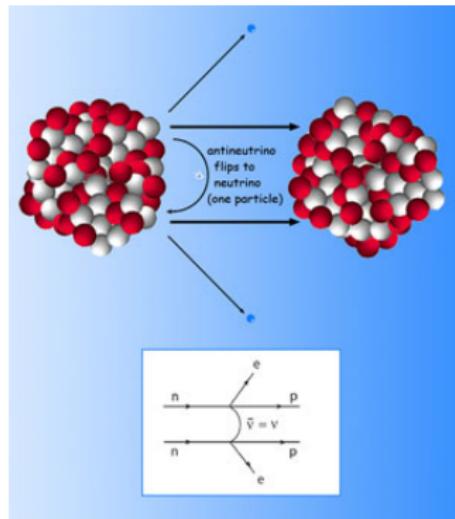
Shimizu, JM, Yako,  
PRL120 142502 (2018)

# Summary

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Nuclear matrix elements are key  
for the design of next-generation tonne-scale  $0\nu\beta\beta$  decay experiments  
and for fully exploiting the experimental results

- Present matrix element calculations disagree  
Need improved calculations,  
guidance from other nuclear experiments
- Shell model nuclear matrix elements  
in two shells for  $^{48}\text{Ca}$ ,  $^{76}\text{Ge}$ ,  
suggest moderate enhancement ( $\lesssim 30\%$ )
- Double Gamow-Teller transitions  
pursued in RIKEN, INFN LNS, RCNP Osaka  
can provide very useful insight on  
value of  $0\nu\beta\beta$  decay matrix elements

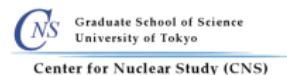


# Collaborators

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