

# EM response and weak decays in light nuclei

Saori Pastore

ECT\*-18: Exploring the role of electro-weak currents in Atomic Nuclei  
Trento, IT - April 2018



## Open Questions in Fundamental Symmetries and Neutrino Physics

Majorana Neutrinos, Neutrinos Mass Hierarchy,  
CP-Violation in Neutrino Sector, Dark Matter

WITH

Mereghetti & Dekens & Cirigliano & Carlson & Graesser (LANL)  
de Vries (Nikhef) & van Kolck (AU+CNRS/IN2P3)

Baroni (USC) & Schiavilla (ODU+JLab) & Gandolfi (LANL) & Piarulli & Pieper & Wiringa (ANL)  
Girlanda (Salento U.) & Viviani & Marcucci & Kiewsky (Pisa U.+INFN)

## REFERENCES

PRC78(2008)064002 - PRC80(2009)034004 - PRL105(2010)232502 - PRC84(2011)024001 - PRC87(2013)014006 - PRC87(2013)035503 -  
PRL111(2013)062502 - PRC90(2014)024321 - JPhysG41(2014)123002 - PRC93(2016)011550

\*\*\* PRC97(2018)014606 - PRC97(2018)022501 - arXiv:1802.10097 \*\*\*

## Fundamental Physics Quests: Double Beta Decay

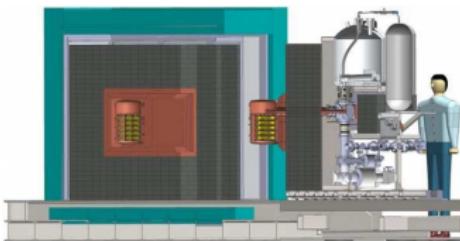
observation of  $0\nu\beta\beta$ -decay

→

lepton #  $L = l - \bar{l}$  not conserved

→

implications in  
matter-antimatter imbalance

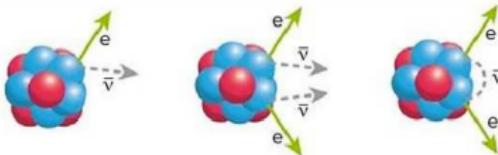


Majorana Demonstrator

$0\nu\beta\beta$ -decay  $\tau_{1/2} \gtrsim 10^{25}$  years (age of the universe  $1.4 \times 10^{10}$  years)

need 1 ton of material to see (if any)  $\sim 5$  decays per year

\* Decay Rate  $\propto$  (nuclear matrix elements) $^2 \times \langle m_{\beta\beta} \rangle^2$  \*

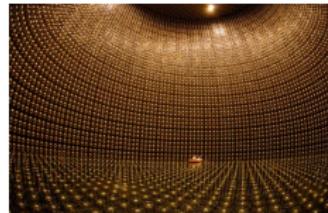


Standard  $\beta$  Decay

Double  $\beta$  Decay

Neutrinoless Double  $\beta$  Decay

# Fundamental Physics Quests: Accelerator Neutrinos



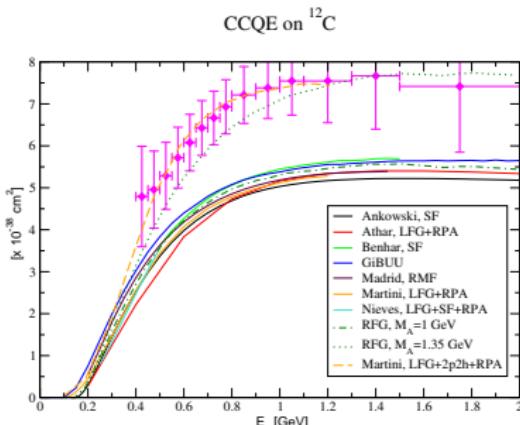
neutrinos oscillate  
 →  
 they have tiny masses  
 =  
**BSM** physics  
 Beyond the Standard Model  
 Simplified 2 flavors picture:

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2 L}{2E_\nu} \right)$$

\* Unknown \*  
**v-mass** hierarchy, CP-violation,  
 accurate mixing angles

DUNE, MiniBoone, T2K, Minerva ... active material \*  $^{12}C$ ,  $^{40}Ar$ ,  $^{16}O$ ,  $^{56}Fe$ , ... \*

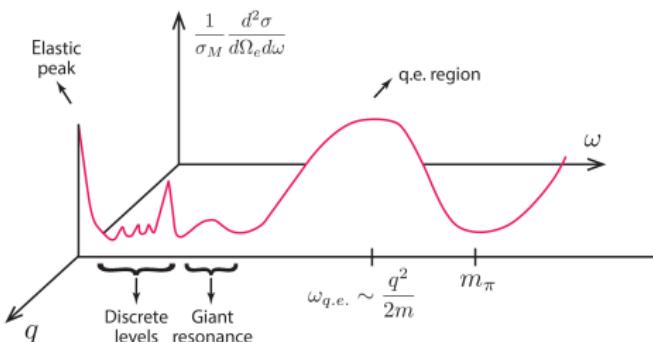
## Neutrino-Nucleus scattering



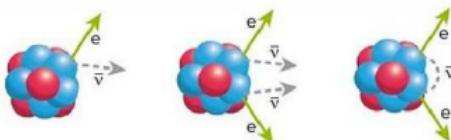
Alvarez-Ruso arXiv:1012.3871

# Nuclear Structure and Dynamics

- \* An accurate understanding of nuclear structure and dynamics is required to extract new physics from nuclear effects \*



- \*  $\omega \sim$  few MeV,  $q \sim 0$ : EM decay,  $\beta$ -decay,  $\beta\beta$ -decays
- \*  $\omega \lesssim$  tens MeV: Nuclear Rates for Astrophysics
- \*  $\omega \sim 10^2$  MeV: Accelerator neutrinos,  $\nu$ -nucleus scattering



Standard  $\beta$  Decay

Double  $\beta$  Decay

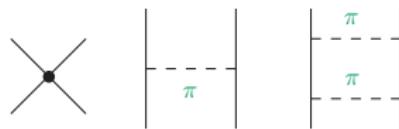
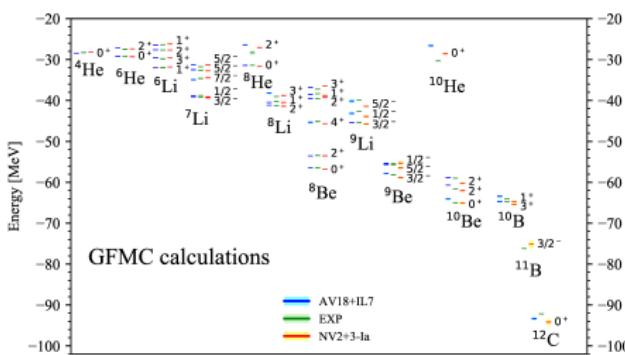
Neutrinoless Double  $\beta$  Decay

# Nuclear Interactions

The nucleus is made of A non-relativistic interacting nucleons and its energy is

$$H = T + V = \sum_{i=1}^A t_i + \sum_{i < j} v_{ij} + \sum_{i < j < k} V_{ijk} + \dots$$

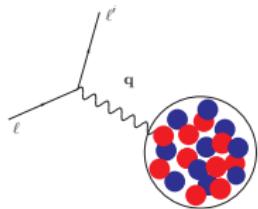
where  $v_{ij}$  and  $V_{ijk}$  are two- and three-nucleon operators based on EXPT data fitting and fitted parameters subsume underlying QCD



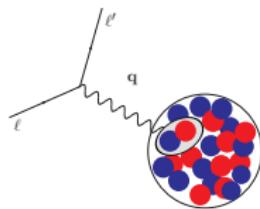
- \* QMC: AV18+UIX / AV18+IL7  
Wiringa+Schiavilla+Pieper *et al.*
- \* QMC: NN(N2LO)+3N(N2LO) ( $\pi\&N$ )  
Gerzelis+Tews+Epelbaum+Gandolfi+Lynn *et al.*
- \* QMC: NN(N3LO)+3N(N2LO) ( $\pi\&N\&\Delta$ )  
Piarulli *et al.*

# Nuclear Currents

1b



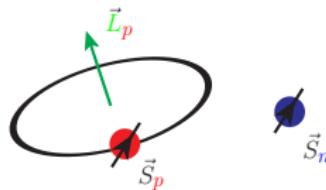
2b



$$\rho = \sum_{i=1}^A \rho_i + \sum_{i < j} \rho_{ij} + \dots ,$$

$$\mathbf{j} = \sum_{i=1}^A \mathbf{j}_i + \sum_{i < j} \mathbf{j}_{ij} + \dots$$

\* Nuclear currents given by the sum of  $p$ 's and  $n$ 's currents, **one-body currents (1b)**



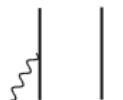
\* Two-body **2b** currents essential to satisfy current conservation

\* We use MEC (SNPA) or  $\chi$ EFT currents



# Electromagnetic Currents from Chiral Effective Field Theory

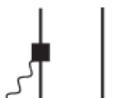
**LO** :  $j^{(-2)} \sim eQ^{-2}$



**NLO** :  $j^{(-1)} \sim eQ^{-1}$



**N<sup>2</sup>LO** :  $j^{(-0)} \sim eQ^0$

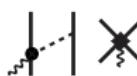


\* 3 unknown Low Energy Constants:  
fixed so as to reproduce  $d$ ,  ${}^3H$ , and  ${}^3\text{He}$  magnetic moments

**N<sup>3</sup>LO** :  $j^{(1)} \sim eQ$



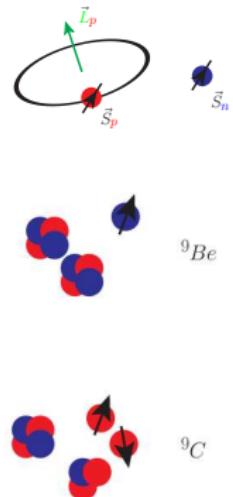
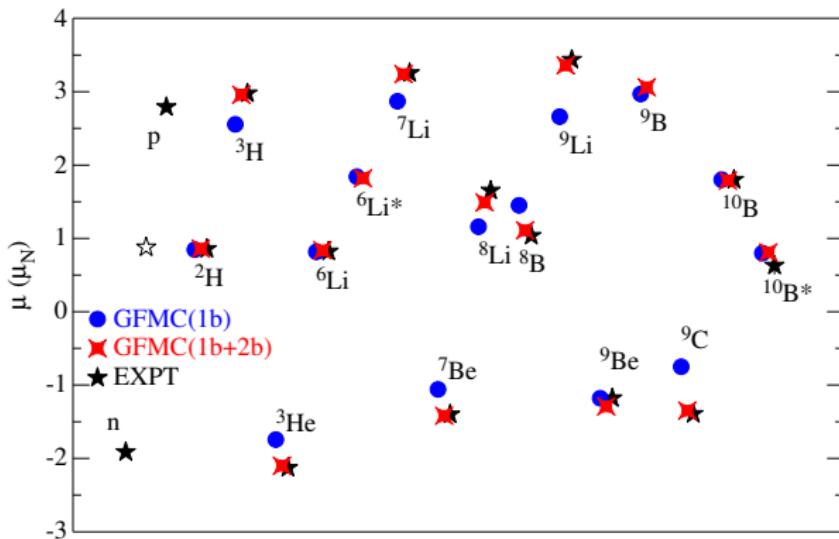
unknown LEC's →



Pastore *et al.* PRC78(2008)064002 & PRC80(2009)034004 & PRC84(2011)024001  
\* analogue expansion exists for the Axial nuclear current - Baroni *et al.* PRC93 (2016)015501 \*

also derived by Park+Min+Rho NPA596(1996)515, Kölling+Epelbaum+Krebs+Meissner  
PRC80(2009)045502 & PRC84(2011)054008

# Magnetic Moments of Nuclei



| m.m.   | THEO        | EXP        |
|--------|-------------|------------|
| $^9C$  | -1.35(4)(7) | -1.3914(5) |
| $^9Li$ | 3.36(4)(8)  | 3.4391(6)  |

chiral truncation error based on EE *et al.* error algorithm, Epelbaum, Krebs, and Meissner EPJA51(2015)53

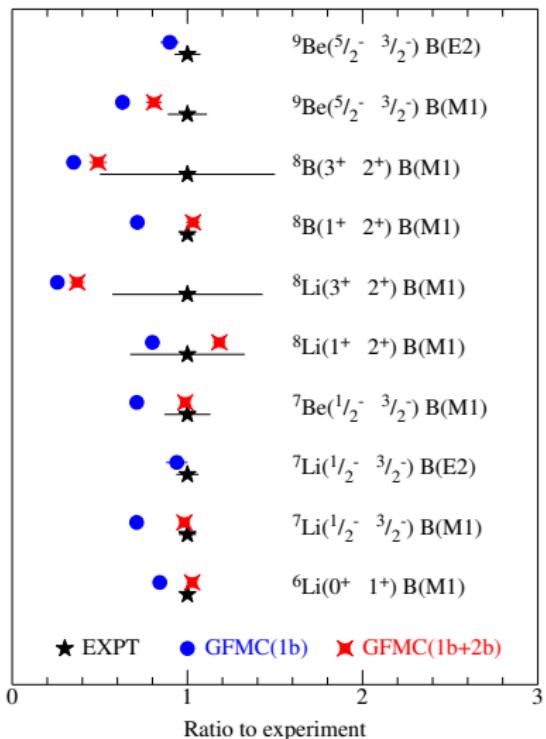
Pastore *et al.* PRC87(2013)035503

# Electromagnetic Transitions in Light Nuclei

- \* **2b** electromagnetic currents bring the THEORY in agreement with the EXPT
- \*  $\sim 40\%$  **2b**-current contribution found in  ${}^9\text{C}$  m.m.
- \*  $\sim 60 - 70\%$  of total **2b**-current component is due to one-pion-exchange currents
- \*  $\sim 20\text{-}30\%$  **2b** found in M1 transitions in  ${}^8\text{Be}$

One M1 prediction:  ${}^9\text{Li}(1/2 \rightarrow 3/2)^*$   
+ a number of B(E2)s

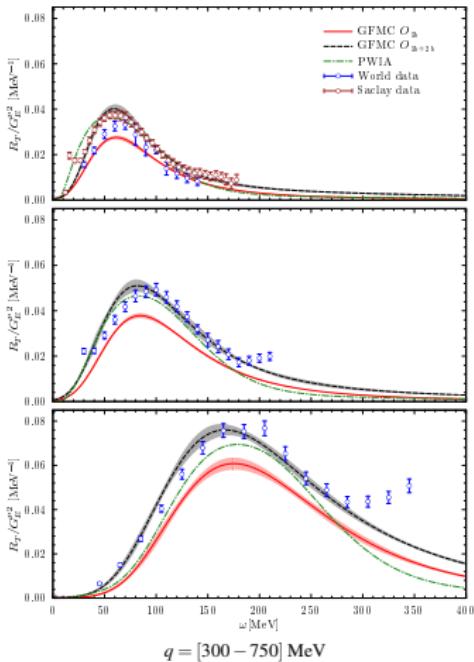
\*2014 TRIUMF proposal Ricard-McCutchan *et al.*



Pastore *et al.* PRC87(2013)035503 & PRC90(2014)024321, Datar *et al.* PRL111(2013)062502

# Electron Scattering off $^{12}C$

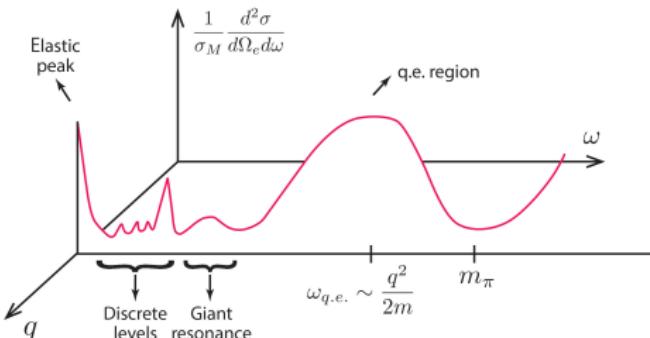
## Electromagnetic Transverse Responses



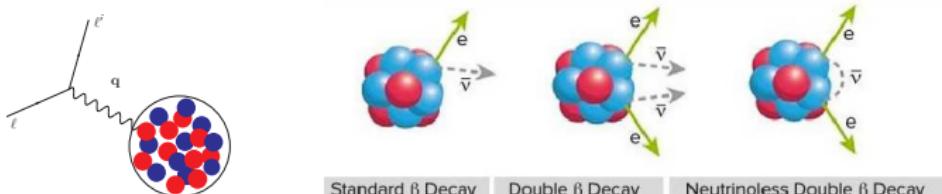
Lovato *et al.* - PRC91(2015)062501 + arXiv:1605.00248

Electron-scattering data are explained when  
two-body correlations and currents are accounted for!

## Nuclei and Neutrinos

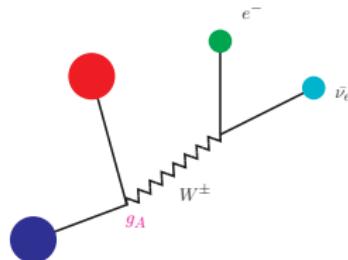


- \*  $\omega \sim$  few MeVs,  $q \sim 0$ : “ $g_A$ -problem” in single beta decays
- \* Scarce data at moderate values of momentum transfer
- \*  $\omega \sim 10^2$  MeV:  $\nu$ -A scattering “Anomalies” the QE region



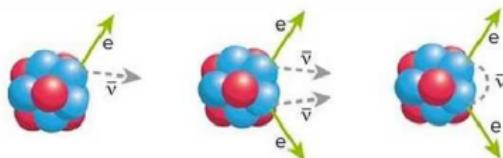
## Standard Beta Decay

The “ $g_A$  problem”  
and  
the role of two-body correlations and two-body currents



\* Matrix Element  $\langle \Psi_f | GT | \Psi_i \rangle \propto g_A$  and Decay Rates  $\propto g_A^2$  \*

$$(Z, N) \rightarrow (Z+1, N-1) + e + \bar{\nu}_e$$



Standard  $\beta$  Decay

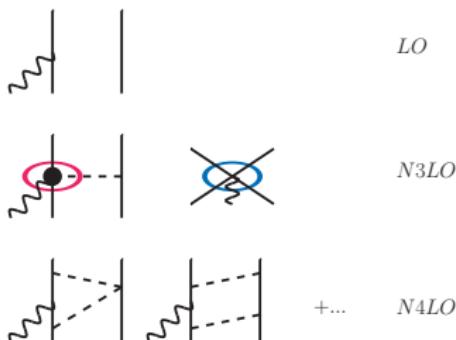
Double  $\beta$  Decay

Neutrinoless Double  $\beta$  Decay

# Nuclear Interactions and Axial Currents

$$H = T + V = \sum_{i=1}^A t_i + \sum_{i < j} v_{ij} + \sum_{i < j < k} V_{ijk} + \dots$$

so far results are available with **AV18+IL7** ( $A \leq 10$ )  
and SNPA or chiral currents (*a.k.a.* hybrid calculations)



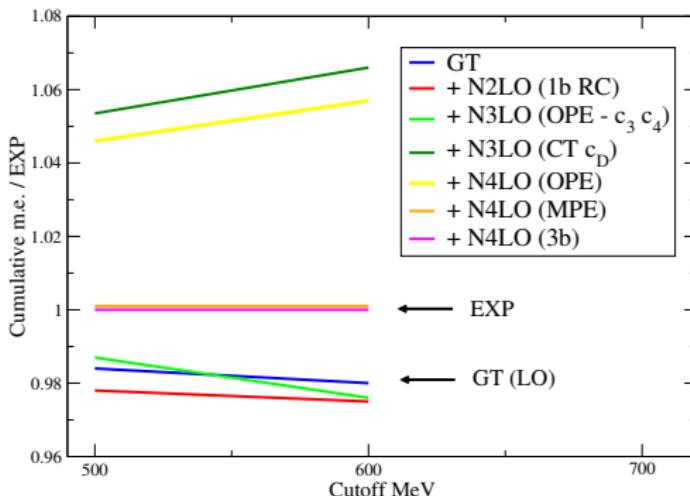
A. Baroni *et al.* PRC93(2016)015501

H. Krebs *et al.* Ann.Phys.378(2017)

- \*  $c_3$  and  $c_4$  are taken from Entem and Machleidt PRC68(2003)041001 & Phys.Rep.503(2011)1
- \*  $c_D$  fitted to GT m.e. of tritium Baroni *et al.* PRC94(2016)024003
- \* cutoffs  $\Lambda = 500$  and  $600$  MeV
- \* include also N4LO 3b currents (tiny)

\* derived by Park *et al.* in the '90  
used (mainly at tree-level) in many calculations  
\* pion-pole at tree-level derived  
by Klos, Hoferichter *et al.* PLB(2015)B746

## Tritium $\beta$ -decay



- \* Results based on AV18+UIX and Chiral Currents are qualitatively in agreement
  - \* All contributions “quench” but for the N3LO OPE (tiny due to a cancellation) and CT (fitted)
  - \* They quench too much, and this is compensated by the fitting of  $c_D$  to EXP GT
  - \* Use of N4LO 2b loop currents from [H. Krebs et al. Ann.Phys.378\(2017\)](#) leads to a reduced value of  $c_D$
- \*  $\sim 2\%$  additive contribution from two-body currents \*

A. Baroni *et al.* PRC93(2016)015501 & PRC94(2016)024003

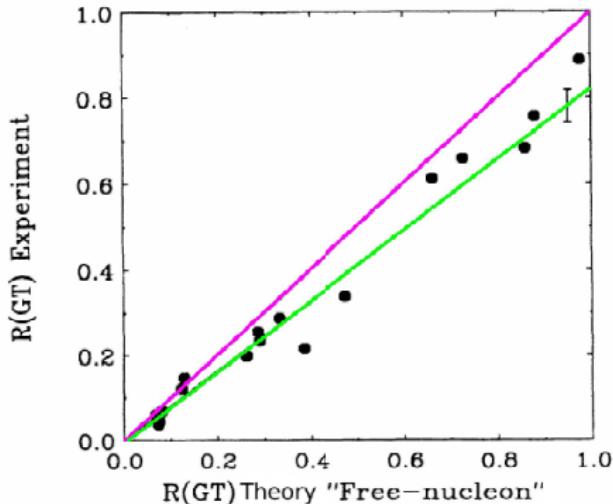
## $\chi$ EFT currents in $A > 3$ systems

$A = 7$  Captures

|            | gs                     | ex                     |
|------------|------------------------|------------------------|
| LO         | 2.334                  | 2.150                  |
| N2LO       | $-3.18 \times 10^{-2}$ | $-2.79 \times 10^{-2}$ |
| N3LO(OPE)  | $-2.99 \times 10^{-2}$ | $-2.44 \times 10^{-2}$ |
| N3LO(CT)   | $2.79 \times 10^{-1}$  | $2.36 \times 10^{-1}$  |
| N4LO(2b)   | $-1.61 \times 10^{-1}$ | $-1.33 \times 10^{-1}$ |
| N4LO(3b)   | $-6.59 \times 10^{-3}$ | $-4.86 \times 10^{-3}$ |
| TOT(2b+3b) | 0.050                  | 0.046                  |

- \* Large cancellations between CT at N3LO (with  $c_D$  fitted) and other 2b currents
- \*  $\lesssim 3\%$  additive contribution from 2b currents in the  $A \leq 10$  systems we considered
- \* this is in agreement with results obtained with “conventional” axial currents
- \* when using chiral axial currents  $\lesssim 1\%$  error from chiral truncation (in the currents)

## Single $\beta$ -decay: The “ $g_A$ problem”

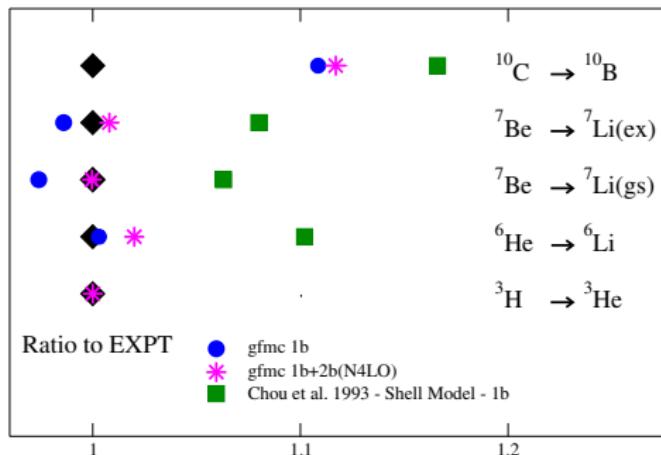


$$\text{in } 3 \leq A \leq 18 \longrightarrow g_A^{\text{eff}} \simeq 0.80 g_A$$

Chou *et al.* PRC47(1993)163

Missing Physics: 1. Correlations and/or 2. Two-body currents

## Single Beta Decay Matrix Elements in $A = 6-10$



gfmc (1b) and gfmc (1b+2b); shell model (1b)

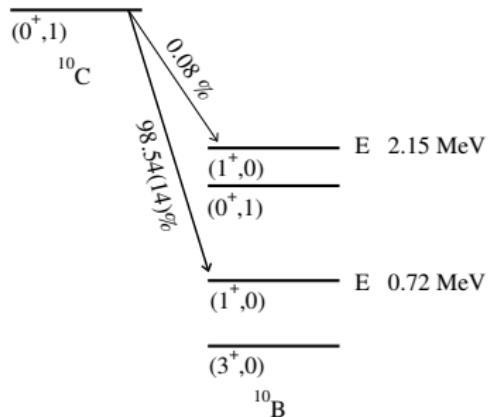
Pastore *et al.* PRC97(2018)022501

A. Baroni *et al.* PRC93(2016)015501 & PRC94(2016)024003

Based on  $g_A \sim 1.27$  no quenching factor

\* data from TUNL, Suzuki *et al.* PRC67(2003)044302, Chou *et al.* PRC47(1993)163

# $^{10}\text{B}$

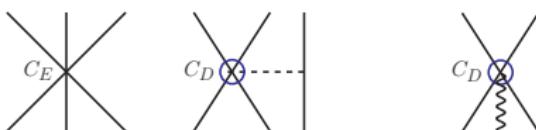


- \* In  $^{10}\text{B}$ ,  $\Delta E$  with same quantum numbers  $\sim 1.5$  MeV
- \* In  $A = 7$ ,  $\Delta E$  with same quantum numbers  $\gtrsim 10$  MeV

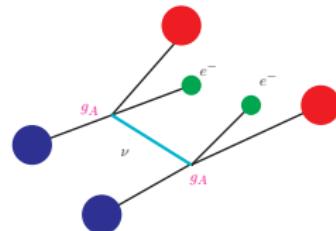
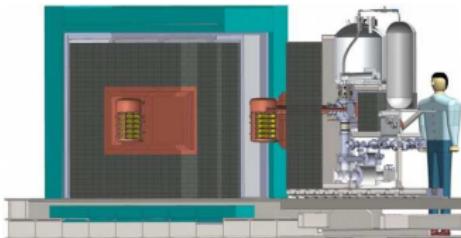
## Beta-decay

To do list:

- \* QMC calculations based on both chiral interactions and chiral currents
- \* In this case  $c_D$  enters **both** the 3b interaction and 2b axial current
  - \*  $c_D$  (and  $c_E$ ) depend on the fitting strategy, *e.g.*, EXP GT in tritium, EXP B.E. A=3, EXP B.E. A=4, scattering length, ...
  - \*  $c_D$  (and  $c_E$ ) depend on the regulator utilized in the fitting procedure
- \* Pions and nucleons d.o.f.'s:  
axial currents fully developed
- \* Pions, nucleons, and deltas d.o.f.'s (interaction by [Piarulli \*et al.\*](#)  
[PRC91\(2015\)024003-PRC94\(2016\)054007-PRL120\(2018\)052503](#)):  
axial currents at tree-level fully developed (on going)
- \* Benchmark with calculations by Gaute, Quaglioni *et al.*
- \* yesterday resolution: quote  $c_D$  and  $c_E$  and if 3NF is attractive or repulsive



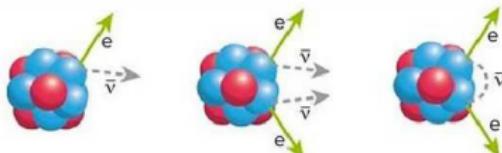
## Neutrinoless Double Beta Decay



“The average momentum is about **100 MeV**, a scale set by the average distance between the two decaying neutrons” cit. Engel&Menéndez

\* Decay rate  $\propto$  (nuclear matrix elements)<sup>2</sup>  $\times \langle m_{\beta\beta} \rangle^2$  \*

\* Nuclear matrix elements  $\propto g_A^2$  and Decay Rates  $\propto g_A^4$  \*

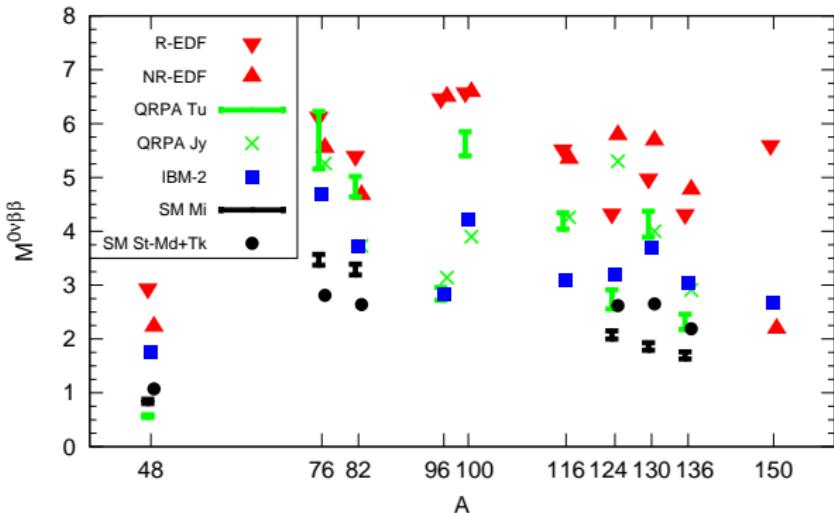


Standard  $\beta$  Decay

Double  $\beta$  Decay

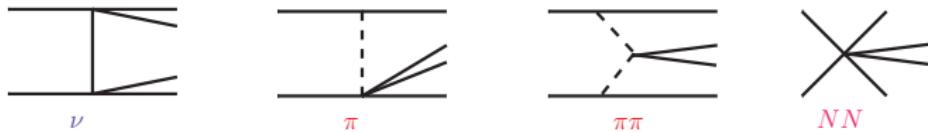
Neutrinoless Double  $\beta$  Decay

## Neutrinoless double beta decay: STATUS



Javier Menendez arXiv:1703.08921 (2017)

## Double beta-decay Potentials



$$v_{\nu} \sim L_{\nu} \tau_{1,+} \tau_{2,+} \frac{\sigma_1 \cdot \sigma_2}{m_{\pi} \mathbf{q}^2} + \dots + v_{\nu}^{\text{N2LO-loop}*}$$

$$v_{\pi\pi} \sim L_{\pi\pi} \tau_{1,+} \tau_{2,+} \frac{\sigma_1 \cdot \mathbf{q} \sigma_2 \cdot \mathbf{q}}{m_{\pi} (\mathbf{q}^2 + m_{\pi}^2)^2}$$

$$v_{\pi} \sim L_{\pi} \tau_{1,+} \tau_{2,+} \frac{\sigma_1 \cdot \mathbf{q} \sigma_2 \cdot \mathbf{q}}{m_{\pi}^3 (\mathbf{q}^2 + m_{\pi}^2)}$$

$$v_{NN} \sim L_{NN} \tau_{1,+} \tau_{2,+} \frac{\sigma_1 \cdot \sigma_2}{m_{\pi}^3}$$

$L_{\pi\pi}, L_{\pi}, L_{NN}$  encode hadronic and model dependent particle physics

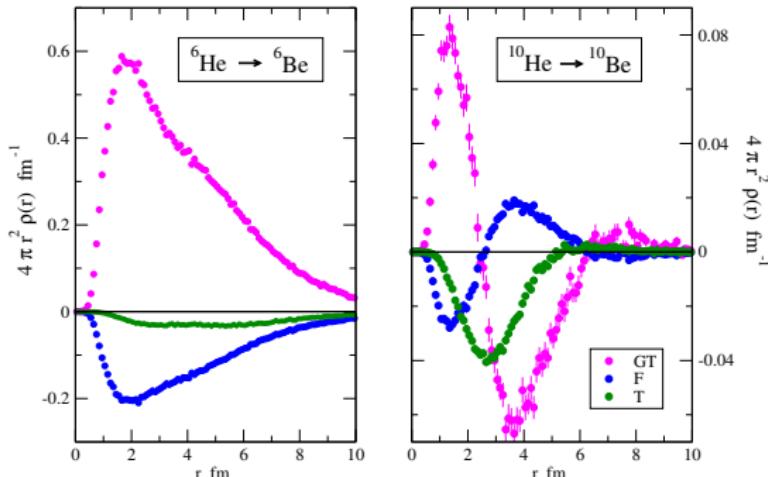
\* Cirigliano & Dekens & Mereghetti & Walker-Loud in arXiv:1710.01729

IN COLLABORATION WITH

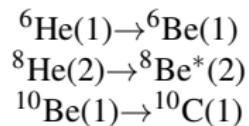
Emanuele Mereghetti & Wouter Dekens & Cirigliano & Carlson & Wiringa

PRC97(2018)014606

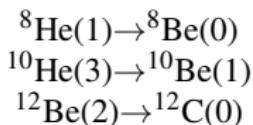
## F, GT, and T Transition Densities



\*  $\Delta T = 0$

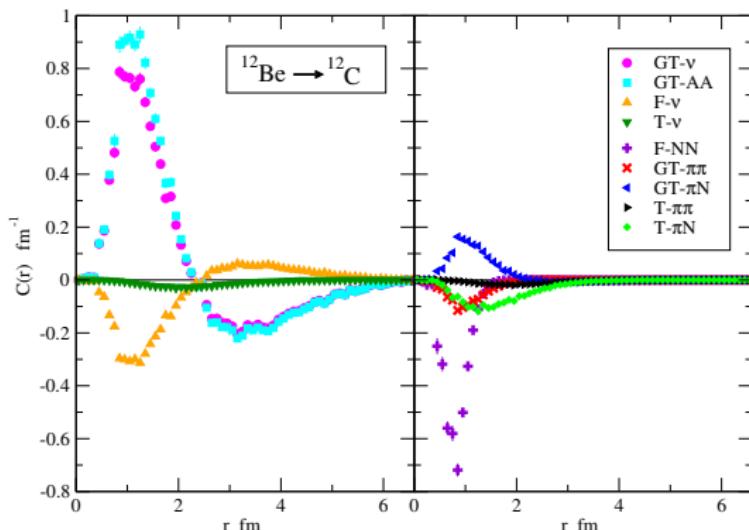


\*  $\Delta T = 2$



$$F = \tau_{1,+} \tau_{2,+} ; GT = \tau_{1,+} \tau_{2,+} \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 ; T = \tau_{1,+} \tau_{2,+} S_{12}$$

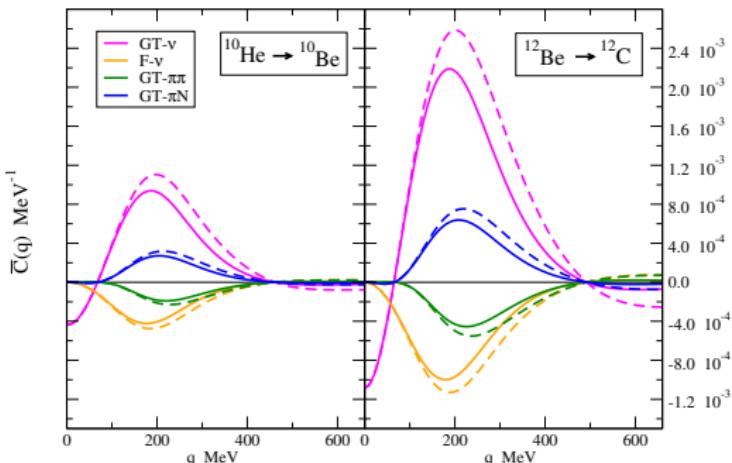
# Double beta-decay Matrix Elements



PRC97(2018)014606

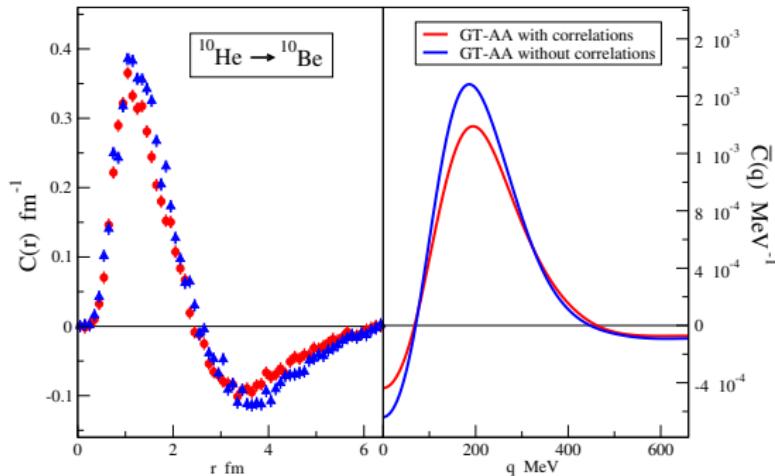
## Momentum Dependence and Sensitivity to N2LO effects

i.e., ‘dipole’ nucleonic form factors and  $v_v^{\text{N2LO-loop}}$



- \* Peaks at  $\sim 200 \text{ MeV}$
- \* Form factors on/off  $\rightarrow \sim 10\%$  variation same size as  $v_v^{\text{N2LO-loop}}$  from Cirigliano *et al.* arXiv:1710.01729
- \*  $A = 10$  highly suppressed w.r.t.  $A = 12$  (clusterization matter?)
- \*  $A = 12$  ‘most similar’ to experimental cases

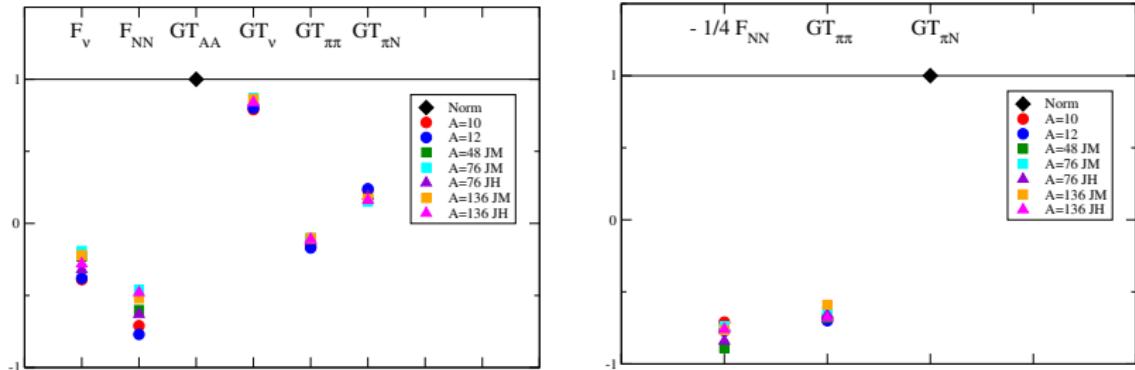
## Sensitivity to ‘pion-exchange-like’ correlations



- \* no ‘pion-exchange-like’ correlation operators  $U_{ij}$
- \* yes ‘pion-exchange-like’ correlation operators  $U_{ij}$
- \*  $\sim 10\%$  increase in the matrix elements corresponds to a ‘ $g_A$ -quenching’ of  $\sim 0.95$
- \* as opposed to  $\sim 0.83$  found in  $A = 10$  single beta decay

\* Correlations reduce the m.e.’s (also true for  $\mu$ ’s and GT’s) \*

## Comparison with calculations of larger nuclei



JM = Javier Menendez private communication

JH = Hyvärinen *et al.* PRC91(2015)024613

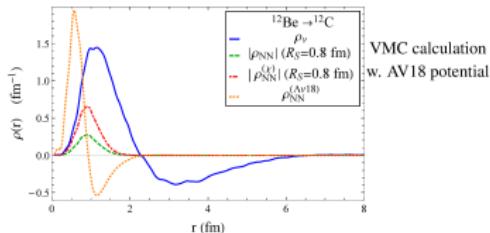
\* Relative size of the matrix elements is approximately the same in all nuclei

\* Short-range terms approximately the same in all nuclei

PRC97(2018)014606

# The contact!

## Impact on $0\nu\beta\beta$ nuclear matrix elements



- assuming  $C_1 = C_2$  & extract from AV18

$$M_{F\nu} = 0.191 \quad M_{GT\nu} = 0.400 \quad M_{F,NN} = 0.460$$

$\mathcal{O}(1)$  correction!

- need consistent treatment of weak and strong interactions



Courtesy of Emanuele Mereghetti

- \* renormalization requires to introduce a counter term at leading order

$$v_\nu = v_\nu^{\text{LO}} + v_{CT}$$

- \*  $v_{CT}$  is ‘partially’ determined by the isospin breaking NN potential ( $\propto (\tau_{1,z} + \tau_{2,z})$ )

Mereghetti & Dekens & Cirigliano & Graesser & de Vries & van Kolck & Pastore

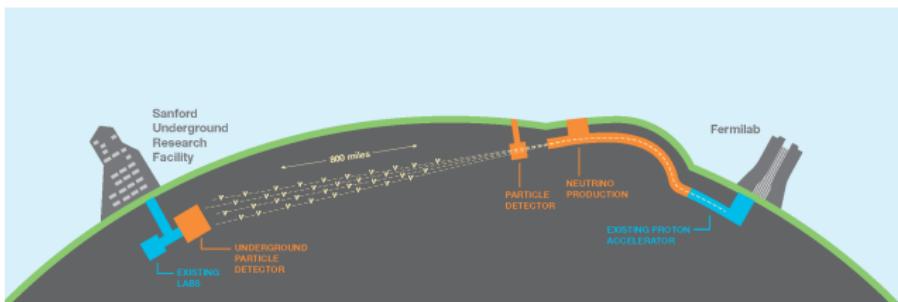
arXiv:1802.10097

## $e - A$ and $\nu - A$ Scattering

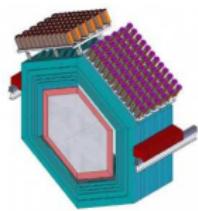
- How do nuclei interact with electrons and neutrinos in the GeV energy regime and how can calculations of these interaction cross sections be improved?

*i.e.*

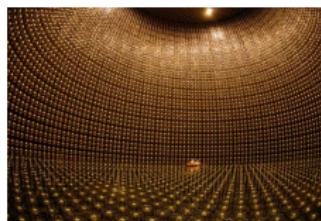
Towards a microscopic description of the  $\nu$ -A inclusive cross section:  
The Short-Time-Approximation



LBNF



Minerva



T2K

## Factorization: Short-Time Approximation

$$R_{\alpha}(q, \omega) = \sum_f \delta(\omega + E_0 - E_f) \langle 0 | O_{\alpha}^{\dagger}(\mathbf{q}) | f \rangle \langle f | O_{\alpha}(\mathbf{q}) | 0 \rangle$$

$$R_{\alpha}(q, \omega) = \int dt \langle 0 | O_{\alpha}^{\dagger}(\mathbf{q}) e^{i(H-\omega)t} O_{\alpha}(\mathbf{q}) | 0 \rangle$$

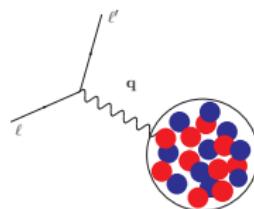
At short time, expand  $P(t) = e^{i(H-\omega)t}$  and keep up to 2b-terms

$$H \sim \sum_i t_i + \sum_{i < j} v_{ij}$$

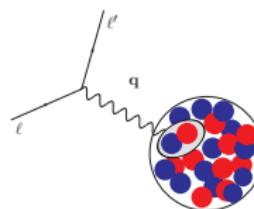
and

$$O_i^{\dagger} P(t) O_i + O_i^{\dagger} P(t) O_j + O_i^{\dagger} P(t) O_{ij} + O_{ij}^{\dagger} P(t) O_{ij}$$

1b



2b

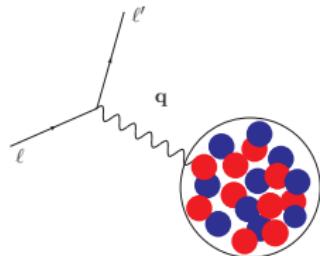


WITH  
Carlson & Gandolfi (LANL) *et al.*

## Factorization I: The Plane Wave Impulse Approximation (PWIA)

In PWIA:

Response functions given by incoherent scattering off single nucleons that propagate freely in the final state (plane waves)



$$R_{\alpha}(q, \omega) = \sum_f \delta(\omega + E_0 - E_f) \langle 0 | O_{\alpha}^{\dagger}(\mathbf{q}) | f \rangle \langle f | O_{\alpha}(\mathbf{q}) | 0 \rangle$$

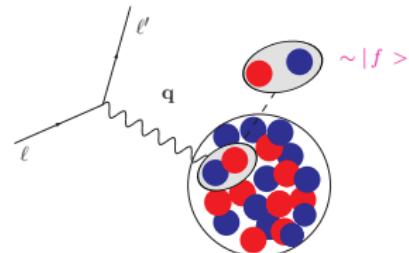
$$O_{\alpha}(\mathbf{q}) = O_{\alpha}^{(1)}(\mathbf{q}) = 1b$$

$$|f\rangle \sim e^{i(\mathbf{k}+\mathbf{q}) \cdot \mathbf{r}} = \text{free single nucleon w.f.}$$

## Factorization II: The Short-Time Approximation (STA)

In STA:

Response functions are given by the scattering off pairs of fully interacting nucleons that propagate into a correlated pair of nucleons



$$R_{\alpha}(q, \omega) = \sum_f \delta(\omega + E_0 - E_f) \langle 0 | O_{\alpha}^{\dagger}(\mathbf{q}) | f \rangle \langle f | O_{\alpha}(\mathbf{q}) | 0 \rangle$$

$$O_{\alpha}(\mathbf{q}) = O_{\alpha}^{(1)}(\mathbf{q}) + O_{\alpha}^{(2)}(\mathbf{q}) = 1b + 2b$$

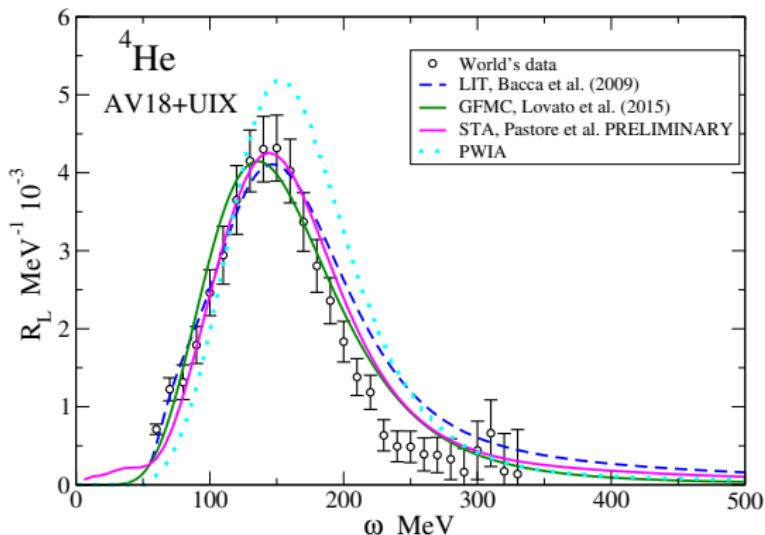
$$|f\rangle \sim |\psi_{p,P,J,M,L,S,T,M_T}(r, R)\rangle = \text{correlated two-nucleon w.f.}$$

\* We retain **two-body physics** consistently in the nuclear interactions and **electroweak currents**

\*  $R_{\alpha}(q, \omega)$  requires only direct calculation of g.s.  $|0\rangle$  w.f.'s \*

\* STA can be implemented to accommodate for more two-body physics, e.g., pion-production induced by  $e$  and  $\nu$

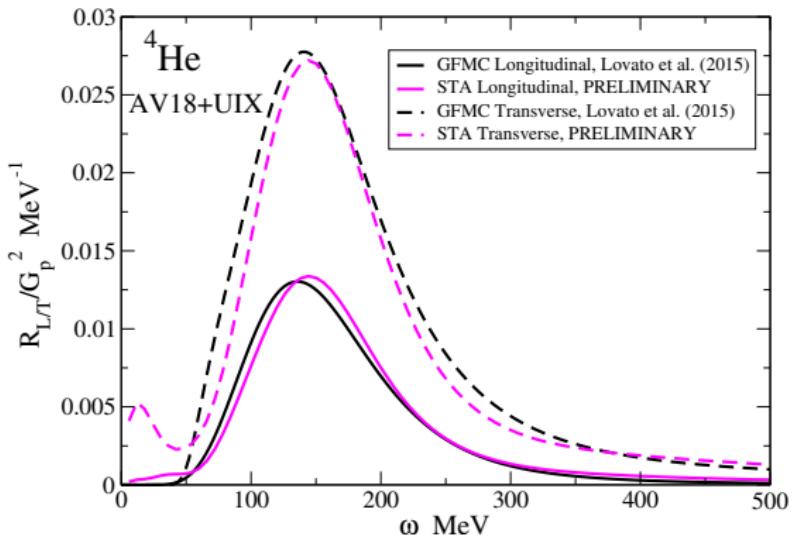
## The Short-Time Approximation



Longitudinal Response function at  $q = 500 \text{ MeV}$

\*Preliminary results\*

## The Short-Time Approximation



Longitudinal vs Transverse Response Function at  $q = 500$  MeV

\*Preliminary results\*

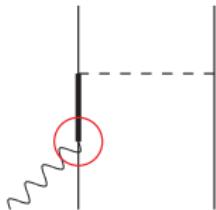
## Summary and Outlook

Two-nucleon correlations and two-body electroweak currents are crucial to explain available experimental data of both static (ground state properties) and dynamical (cross sections and rates) nuclear observables

- \* Two-body currents can give  $\sim 30 - 40\%$  contributions and improve on theory/EXPT agreement
- \* Calculations of  $\beta-$  and  $\beta\beta-$ decay m.e.'s in  $A \leq 12$  indicate two-body physics (currents and correlations) is required
- \* Short-Time-Approximation to evaluate  $v$ -A scattering in  $A > 12$  nuclei is in excellent agreement with exact calculations and data
  - \* We are developing a coherent picture for neutrino-nucleus interactions \*

## EXTRA SLIDES

## SNPA Two-body Axial Currents



- 1) One body has GT, relativistic corrections, PS from pion-pole diagrams
- 2) Two-body currents
  - 2.a) Major contribution from  $\Delta$ -excitation current
  - 2.b) Negligible contributions from  $A\pi, A\rho, A\pi\rho$
- 3)  $AN\Delta$  coupling fixed to tritium beta-decay
- 4)  $\sim 3\%$  additive correction from  $\Delta$ -current

Chemtob, Rho, Towner, Riska, Schiavilla, Marcucci ...

see, e.g., Marcucci *et al.* PRC63(2001)015801 and references therein

## Correlations in our formalism

Minimize expectation value of  $H = T + \text{AV18} + \text{IL7}$

$$E_V = \frac{\langle \Psi_V | H | \Psi_V \rangle}{\langle \Psi_V | \Psi_V \rangle} \geq E_0$$

using trial function

$$|\Psi_V\rangle = \left[ \mathcal{S} \prod_{i < j} \left( 1 + \textcolor{blue}{U}_{ij} + \sum_{k \neq i, j} \textcolor{red}{U}_{ijk} \right) \right] \left[ \prod_{i < j} f_c(r_{ij}) \right] |\Phi_A(JMTT_3)\rangle$$

- \* single-particle  $\Phi_A(JMTT_3)$  is fully antisymmetric and translationally invariant
- \* central pair correlations  $f_c(r)$  keep nucleons at favorable pair separation
- \* pair correlation operators  $\textcolor{blue}{U}_{ij}$  reflect influence of  $\textcolor{blue}{v}_{ij}$  (**AV18**)
- \* triple correlation operators  $\textcolor{red}{U}_{ijk}$  reflect the influence of  $\textcolor{red}{V}_{ijk}$  (**IL7**)

Lomnitz-Adler, Pandharipande, and Smith NPA361(1981)399

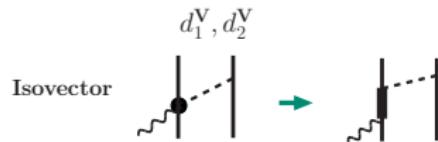
Wiringa, PRC43(1991)1585

## Electromagnetic LECs

$$d^S, d_1^V, d_2^V$$


$$c^S, c^V$$


$d^S$ ,  $d_1^V$ , and  $d_2^V$  could be determined by  
 $\pi\gamma$ -production data on the nucleon

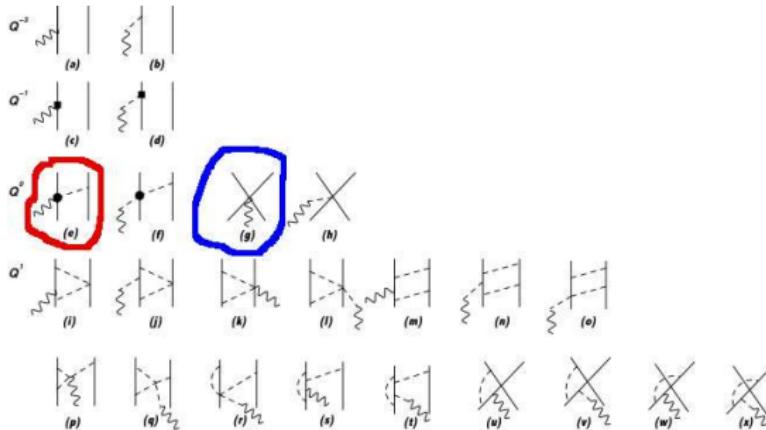


$d_2^V = 4\mu^* h_A / 9m_N(m_\Delta - m_N)$  and  
 $d_1^V = 0.25 \times d_2^V$   
assuming  $\Delta$ -resonance saturation

Left with 3 LECs: Fixed in the  $A = 2 - 3$  nucleons' sector

- \* Isoscalar sector:
  - \*  $d^S$  and  $c^S$  from EXPT  $\mu_d$  and  $\mu_S(^3\text{H}/^3\text{He})$
- \* Isovector sector:
  - \*  $c^V$  from EXPT  $npd\gamma$  xsec.  
or
  - \*  $c^V$  from EXPT  $\mu_V(^3\text{H}/^3\text{He})$  m.m.

## Two-body Axial Currents from $\chi$ EFT



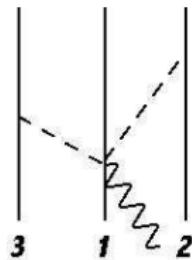
$c_D$

- \* fitted to GT m.e. of tritium beta-decay
- \* for both  $\chi$ EFT potentials and AV18+UIX
- \* because of N4LO two-body currents  $c_D$  value changes

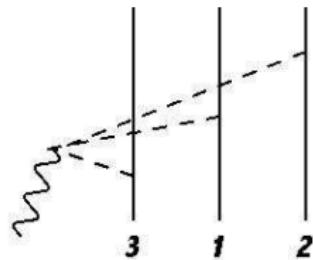
| $\Lambda$ | N3LO   |        | N4LO   |        |
|-----------|--------|--------|--------|--------|
|           | 500    | 600    | 500    | 600    |
| $c_D$     | -0.353 | -0.443 | -1.847 | -2.030 |

A. Baroni *et al.* PRC93(2016)015501 & PRC94(2016)024003

## Three-body Axial Currents from $\chi$ EFT



(a)

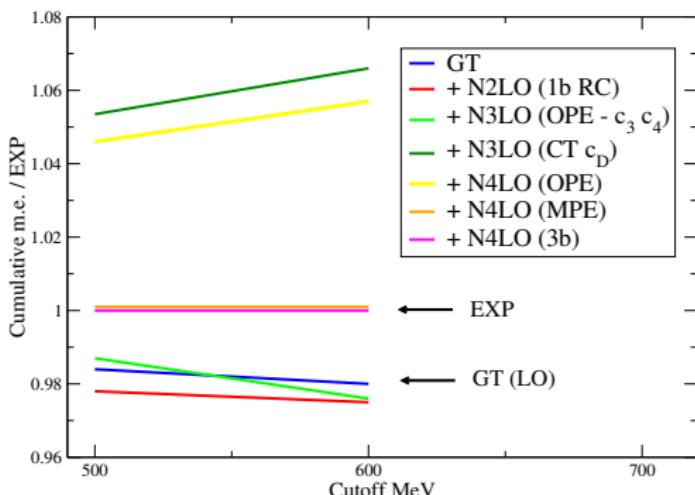


(b)

A. Baroni *et al.* PRC93(2016)015501 & PRC94(2016)024003

## Convergence and cutoff dependence

### Tritium $\beta$ -decay



\*  $\sim 2\%$  additive contribution from two-body currents

A. Baroni *et al.* PRC93(2016)015501 & PRC94(2016)024003

## $\chi$ EFT currents: a closer look

$A = 7$  Captures

|            | gs                     | ex                     |
|------------|------------------------|------------------------|
| LO         | 2.334                  | 2.150                  |
| N2LO       | $-3.18 \times 10^{-2}$ | $-2.79 \times 10^{-2}$ |
| N3LO(OPE)  | $-2.99 \times 10^{-2}$ | $-2.44 \times 10^{-2}$ |
| N3LO(CT)   | $2.79 \times 10^{-1}$  | $2.36 \times 10^{-1}$  |
| N4LO(2b)   | $-1.61 \times 10^{-1}$ | $-1.33 \times 10^{-1}$ |
| N4LO(3b)   | $-6.59 \times 10^{-3}$ | $-4.86 \times 10^{-3}$ |
| TOT(2b+3b) | 0.050                  | 0.046                  |

\* Large cancellations due to positive CT at N3LO with  $c_D$  fixed to GT m.e. of tritium

## Comparison with calculations of larger nuclei

| $(T_i) \rightarrow (T_f)$                         | F     |       |       | GT   |          |         |
|---|-------|-------|-------|------|----------|---------|
|   | v     | NN    | AA    | v    | $\pi\pi$ | $\pi N$ |
| $^8\text{He}(2) \rightarrow ^8\text{Be}(0)$       | -0.63 | -1.37 | 1     | 0.71 | -0.28    | 0.38    |
| $^{10}\text{He}(3) \rightarrow ^{10}\text{Be}(1)$ | -0.39 | -0.71 | 1     | 0.79 | -0.16    | 0.23    |
| $^{12}\text{Be}(2) \rightarrow ^{12}\text{C}(0)$  | -0.38 | -0.77 | 1     | 0.80 | -0.17    | 0.24    |
| $^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$       | Men   | -0.23 | -0.60 | 1    | 0.86     | -0.11   |
| $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$       | Men   | -0.19 | -0.46 | 1    | 0.87     | -0.10   |
|   | Hyv   | -0.32 | -0.63 | 1    | 0.84     | -0.12   |
| $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$     | Men   | -0.22 | -0.52 | 1    | 0.86     | -0.10   |
|   | Hyv   | -0.28 | -0.48 | 1    | 0.84     | -0.11   |

| $(T_i) \rightarrow (T_f)$                         | F    |          |         | GT       |         |  |
|---|------|----------|---------|----------|---------|--|
|   | NN   | $\pi\pi$ | $\pi N$ | $\pi\pi$ | $\pi N$ |  |
| $^8\text{He}(2) \rightarrow ^8\text{Be}(0)$       | 3.38 | -0.76    | 1       |          |         |  |
| $^{10}\text{He}(3) \rightarrow ^{10}\text{Be}(1)$ | 2.86 | -0.68    | 1       |          |         |  |
| $^{12}\text{Be}(2) \rightarrow ^{12}\text{C}(0)$  | 3.08 | -0.70    | 1       |          |         |  |
| $^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$       | Men  | 3.55     | -0.68   | 1        |         |  |
| $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$       | Men  | 2.97     | -0.63   | 1        |         |  |
|   | Hyv  | 3.34     | -0.66   | 1        |         |  |
| $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$     | Men  | 3.06     | -0.59   | 1        |         |  |
|   | Hyv  | 3.03     | -0.68   | 1        |         |  |

Men = Javier Menendez private communication

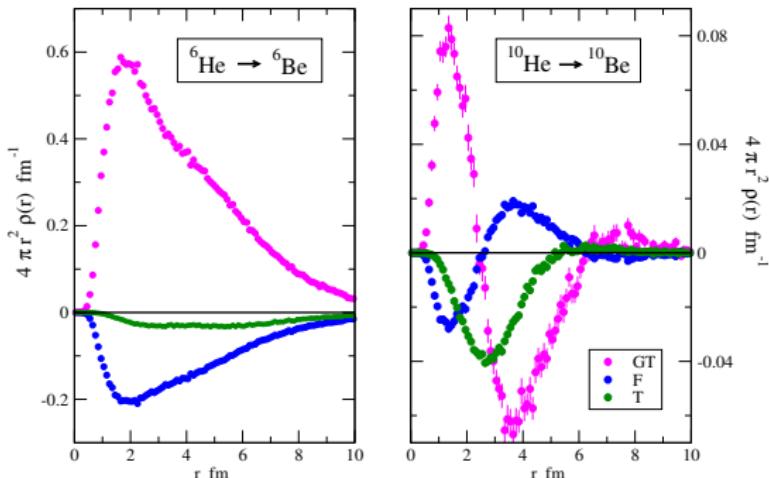
Hyv = Hyvärinen *et al.* PRC91(2015)024613

\* Relative size of the matrix elements is approximately the same in all nuclei

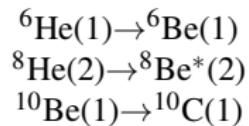
\* Short-range terms approximately the same in all nuclei



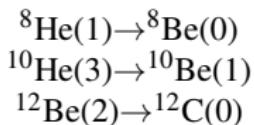
# F, GT, and T Transition Densities



\*  $\Delta T = 0$

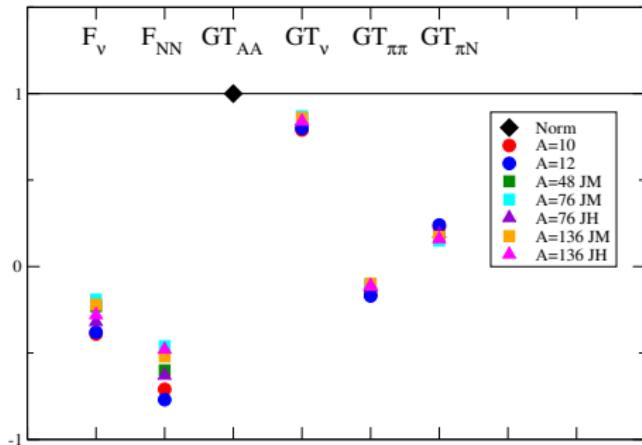


\*  $\Delta T = 2$



$$F = \tau_{1,+} \tau_{2,+} ; GT = \tau_{1,+} \tau_{2,+} \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 ; T = \tau_{1,+} \tau_{2,+} S_{12}$$

## Comparison with calculations of larger nuclei



JM = Javier Menendez private communication

JH = Hyvärinen *et al.* PRC91(2015)024613

\* Relative size of the matrix elements is approximately the same in all nuclei

\* Short-range terms approximately the same in all nuclei