

# Short-Range Correlations And The EMC Effect In Effective Field Theory

Exploring the role of electroweak currents in atomic nuclei

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TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

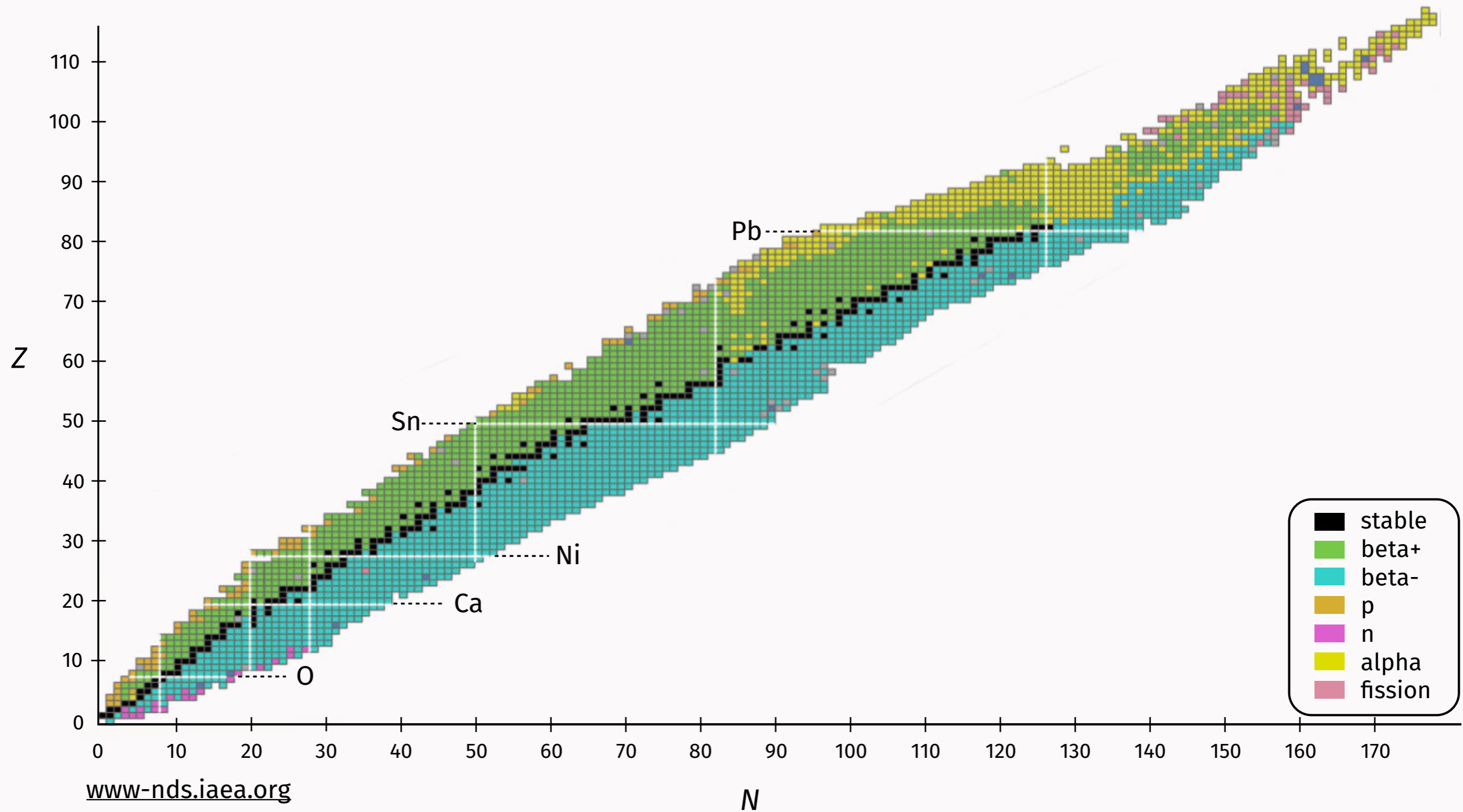


Bundesministerium  
für Bildung  
und Forschung

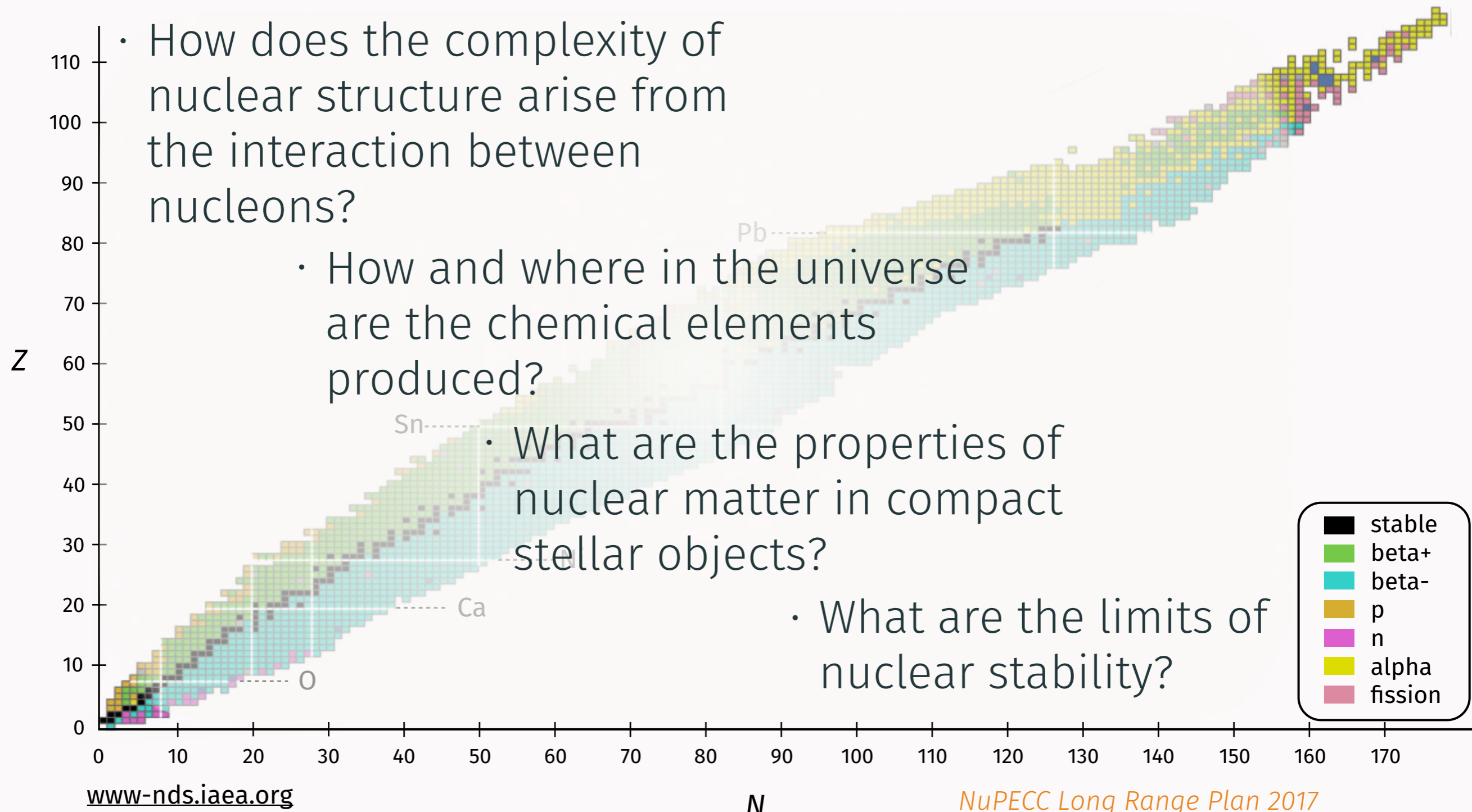
Joel E. Lynn

April 23, 2018

# The Nuclear Landscape



# The Nuclear Landscape



# Extending The Nuclear Landscape

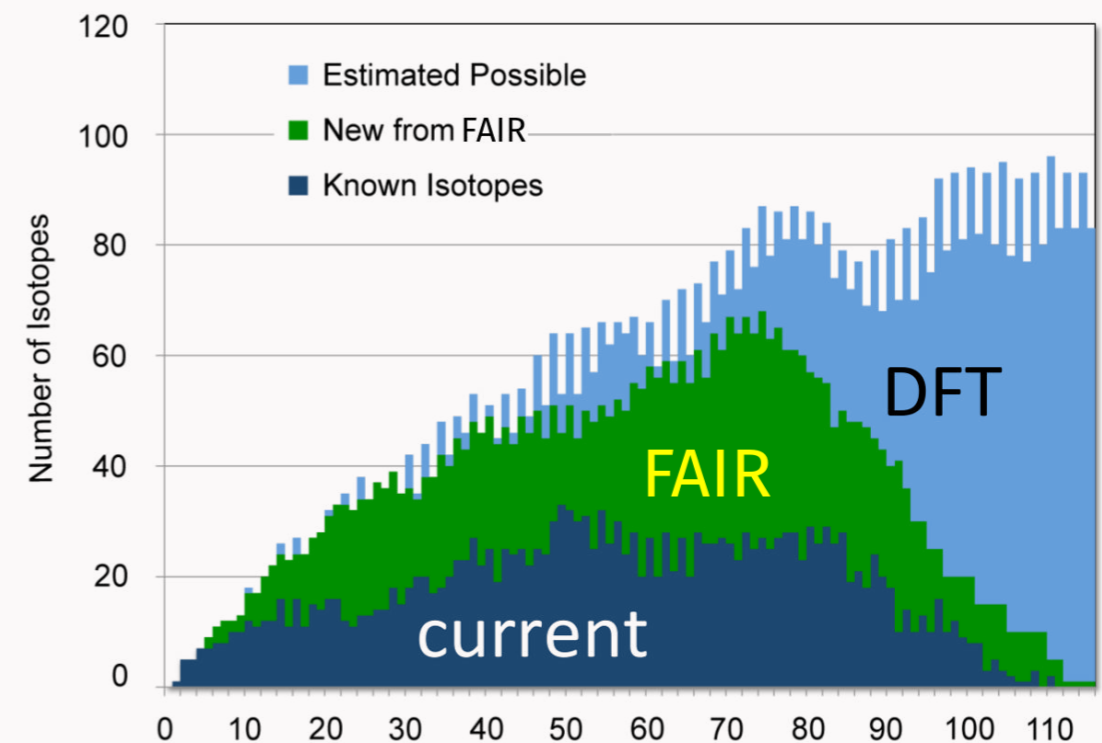
Cutting-edge experimental results

Neutron-star mergers



adapted from M. McLaughlin, APS  
Physics Viewpoint, October 16, (2017)

Rare-isotope facilities



adapted from A. B. Balentekin et al.,  
Mod. Phys. Lett. A **29**, 1430010 (2014)

# What Can Theory Offer?

Nuclear theory has experienced a renaissance in the past few decades thanks (in part) to two developments.

1. Advances in *ab initio* many-body methods.
2. Chiral effective field theory (EFT) for nuclear interactions.



# What Can Theory Offer?

Nuclear theory has experienced a renaissance in the past few decades thanks (in part) to two developments.

1. Advances in ***ab initio*** many-body methods.
2. Chiral effective field interactions.

work with protons + neutrons  
&  
controlled approximations



# Outline

- Quantum Monte Carlo Methods
- Local Chiral EFT
- The EMC effect and SRCs in EFT
- Outlook and Conclusion

# Quantum Monte Carlo (QMC) Methods

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QMC methods in two lines:

$$H |\Psi\rangle = E |\Psi\rangle$$
$$\lim_{T \rightarrow \infty} e^{-H\tau} |\Psi_T\rangle \rightarrow |\Psi_0\rangle$$

QMC methods in more than two lines:

J. Carlson et al, RMP **87**, 1067 (2015).

# QMC Methods - Variational Monte Carlo (VMC) Method

1. Start with a trial wave function  $\Psi_T$  and generate a random position:  $\mathbf{R} = \mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_A$ .
2. Metropolis algorithm: Generate new positions  $\mathbf{R}'$  based on the probability  $P = \frac{|\Psi_T(\mathbf{R}')|^2}{|\Psi_T(\mathbf{R})|^2}$ .  $\rightarrow$  
3. Invoke the variational principle:  $E_T = \frac{\langle \Psi_T | H | \Psi_T \rangle}{\langle \Psi_T | \Psi_T \rangle} > E_0$ .

# QMC Methods - Diffusion Monte Carlo Method

- The wave function is imperfect:  $|\Psi_T\rangle = \sum_{i=0}^{\infty} \alpha_i |\Psi_i\rangle$  .
- Propagate in imaginary time to project out the ground state  $|\Psi_0\rangle$  .

$$\begin{aligned} |\Psi(\tau)\rangle &= e^{-(H-E_T)\tau} |\Psi_T\rangle \\ &= e^{-(E_0-E_T)\tau} \left[ \alpha_0 |\Psi_0\rangle + \sum_{i \neq 0} \alpha_i e^{-(E_i-E_0)\tau} |\Psi_i\rangle \right]. \end{aligned}$$

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$$|\Psi(\tau)\rangle \xrightarrow{\tau \rightarrow \infty} |\Psi_0\rangle .$$

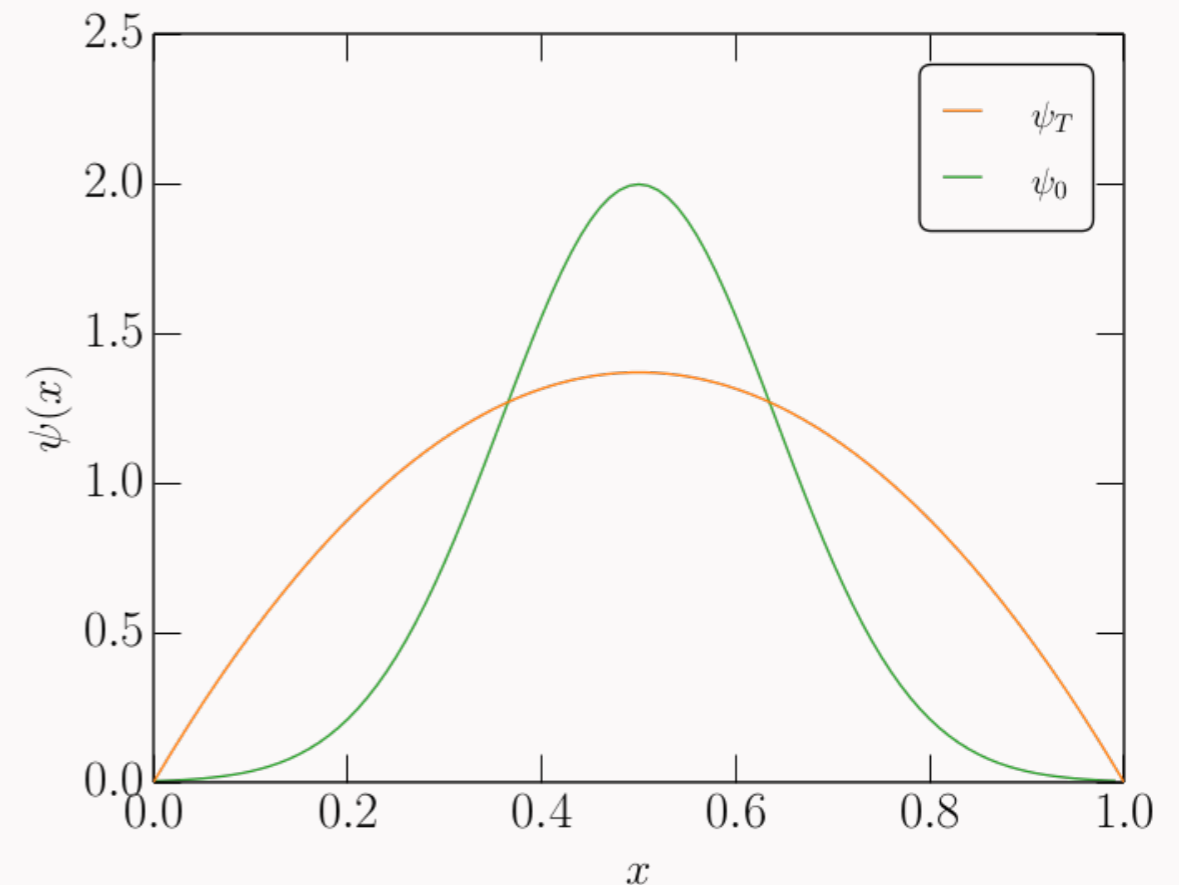
# QMC Methods - An Example

$$H = \frac{p^2}{2} + \frac{1}{2}\omega^2 x^2$$

$$\psi_0(x) = \left(\frac{\omega}{\pi}\right)^{1/4} e^{-\omega x^2/2}$$

Trial wave function; e.g.

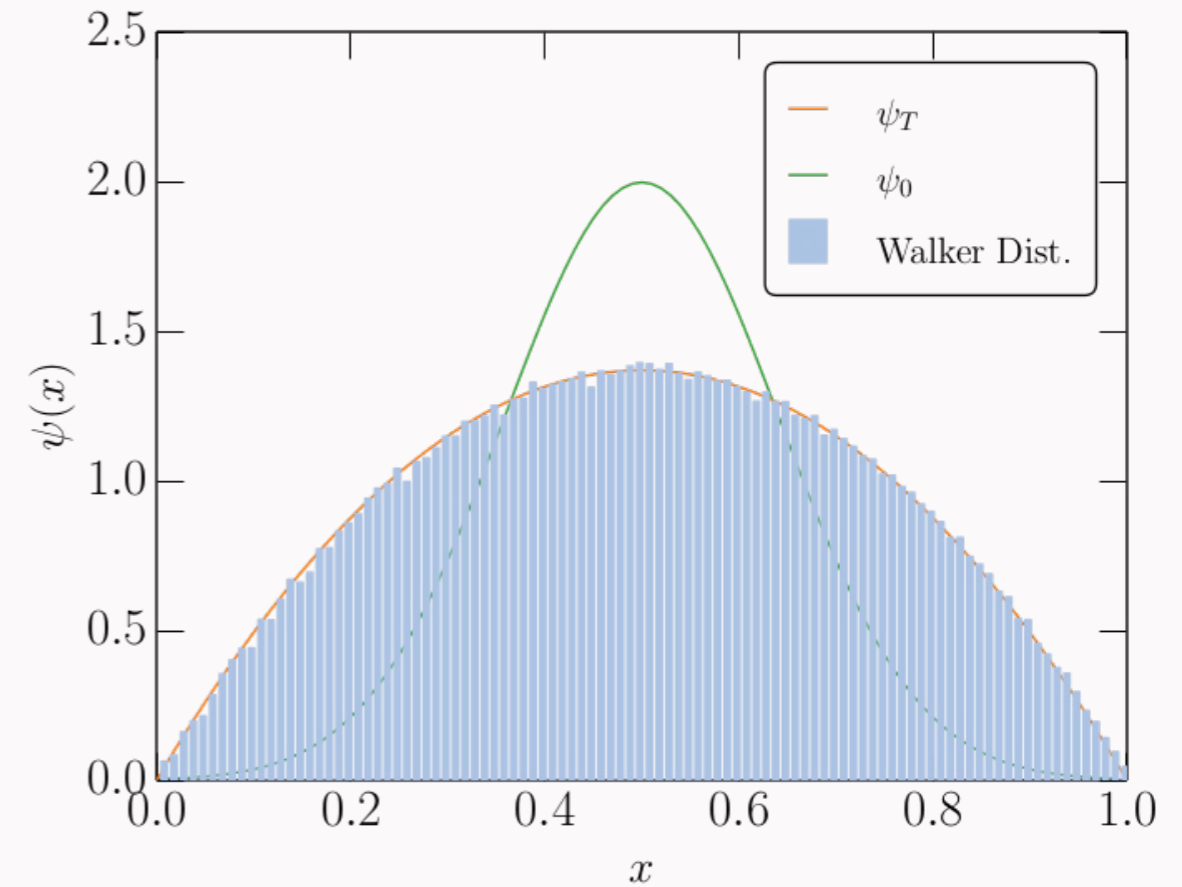
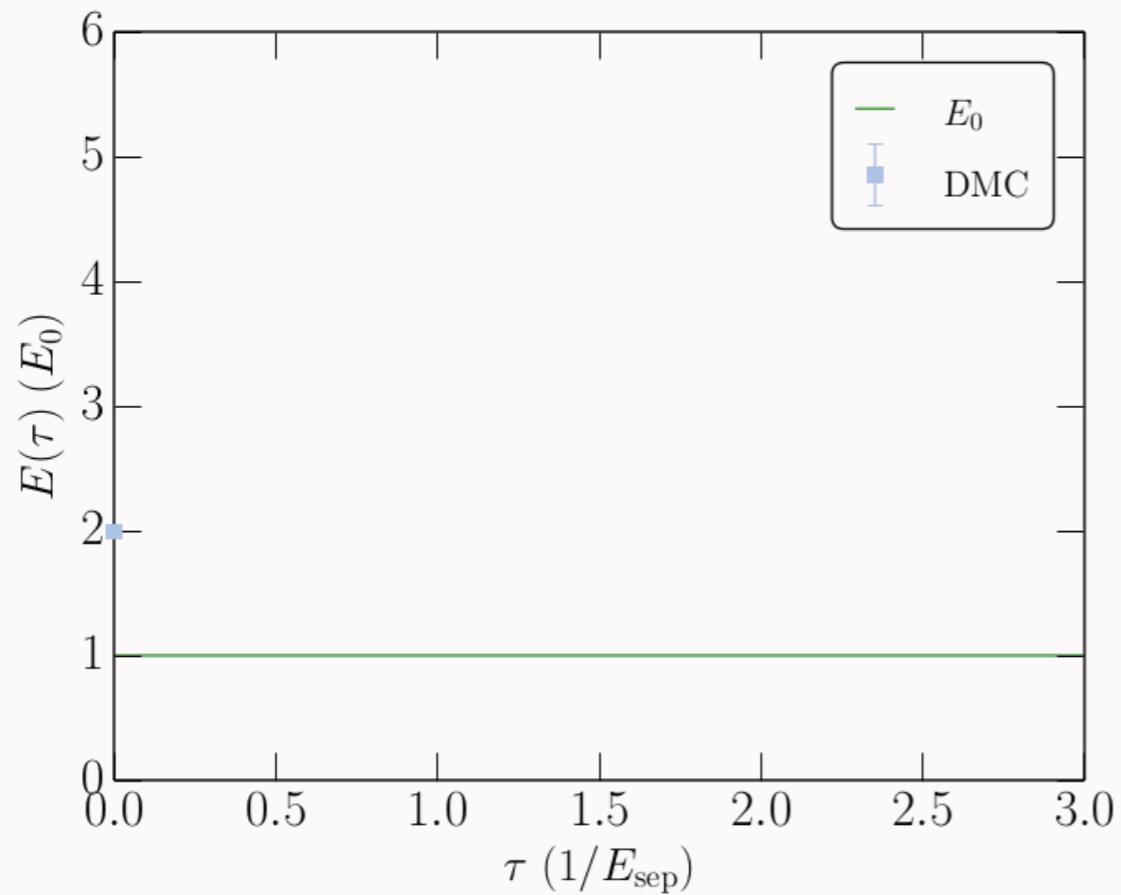
$$\Psi_T(x) = \sqrt{30}x(1-x).$$



# QMC Methods - An Example

Imaginary-time evolution:

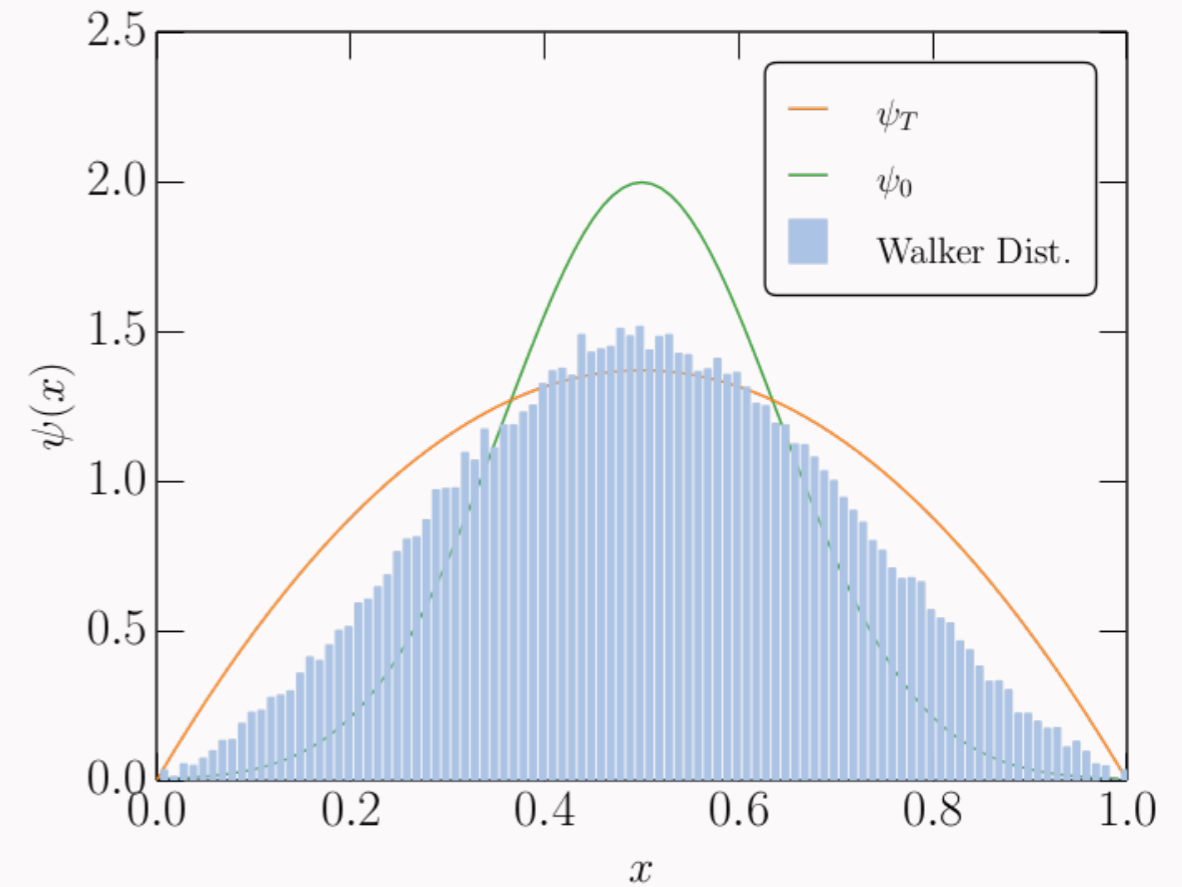
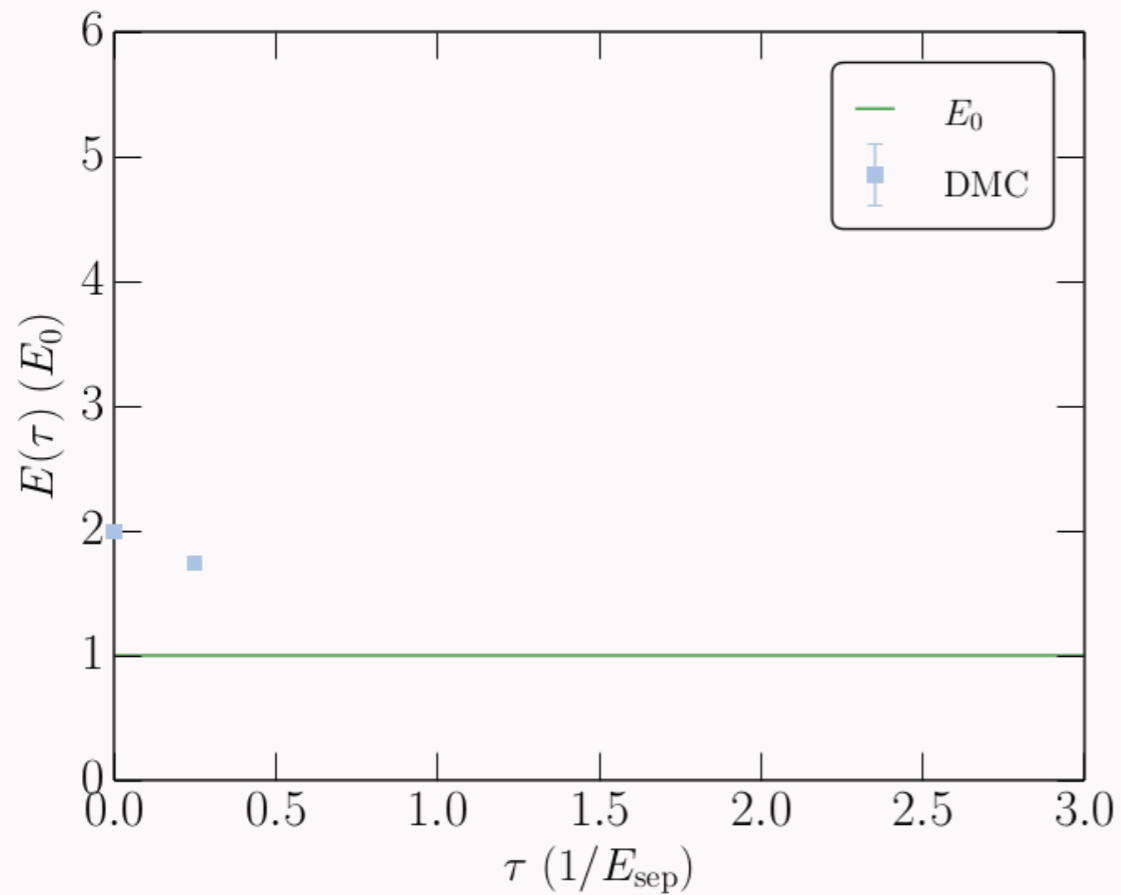
$$\tau = 0.00$$



# QMC Methods - An Example

Imaginary-time evolution:

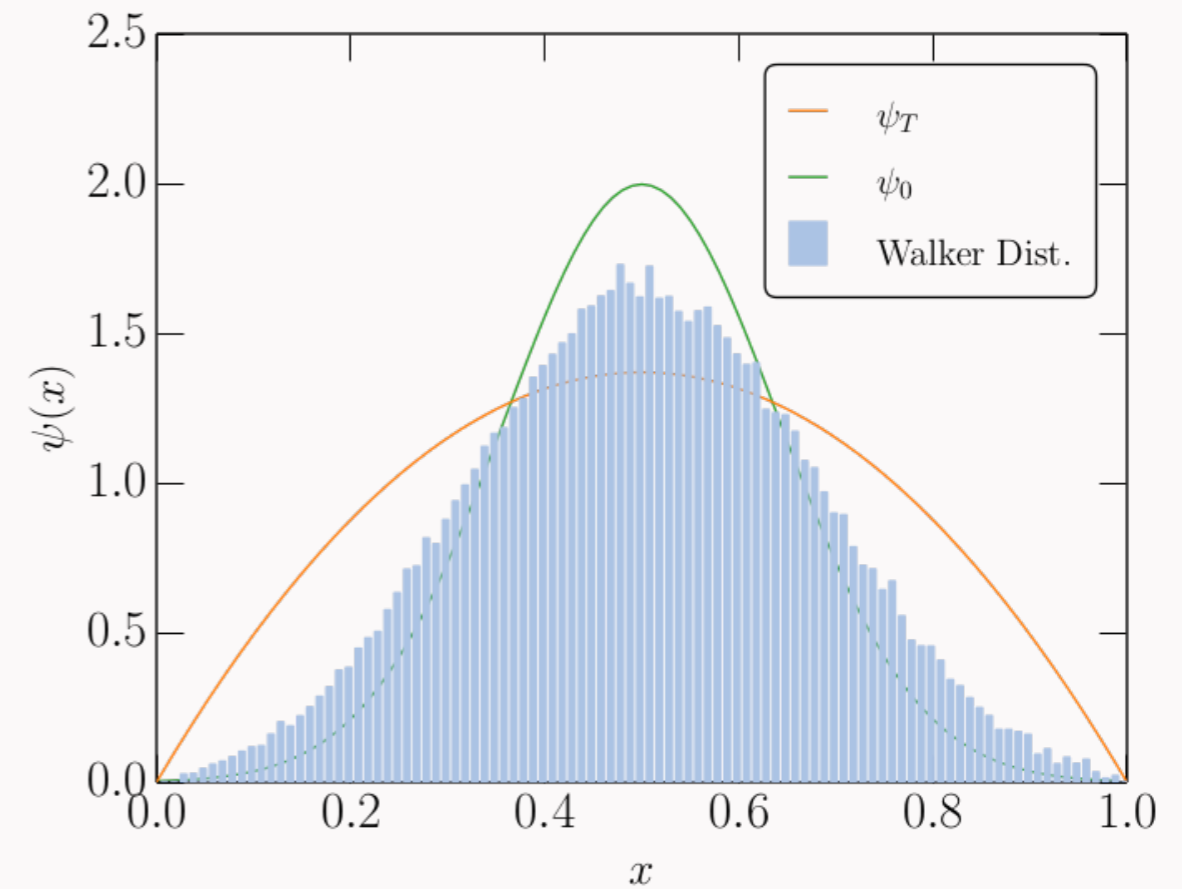
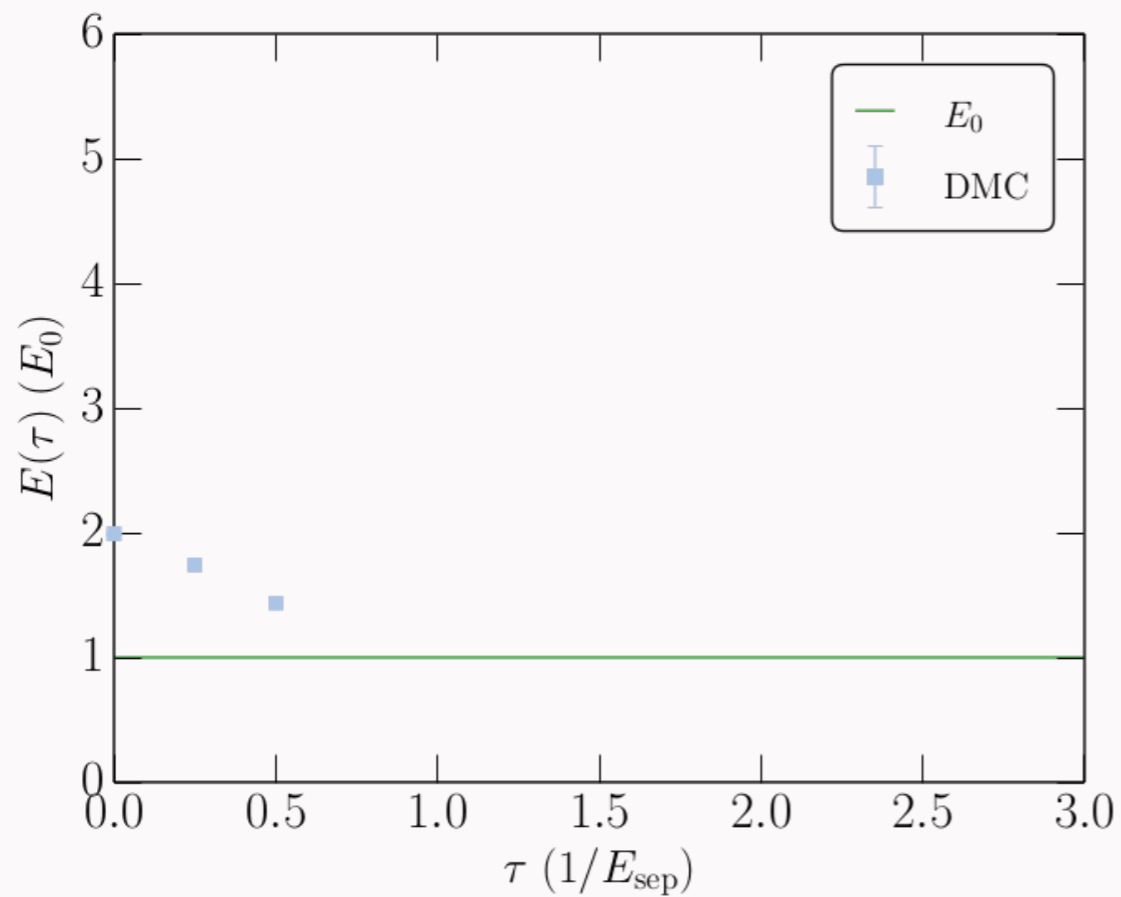
$$\tau = 0.25$$



# QMC Methods - An Example

Imaginary-time evolution:

$$\tau = 0.50$$

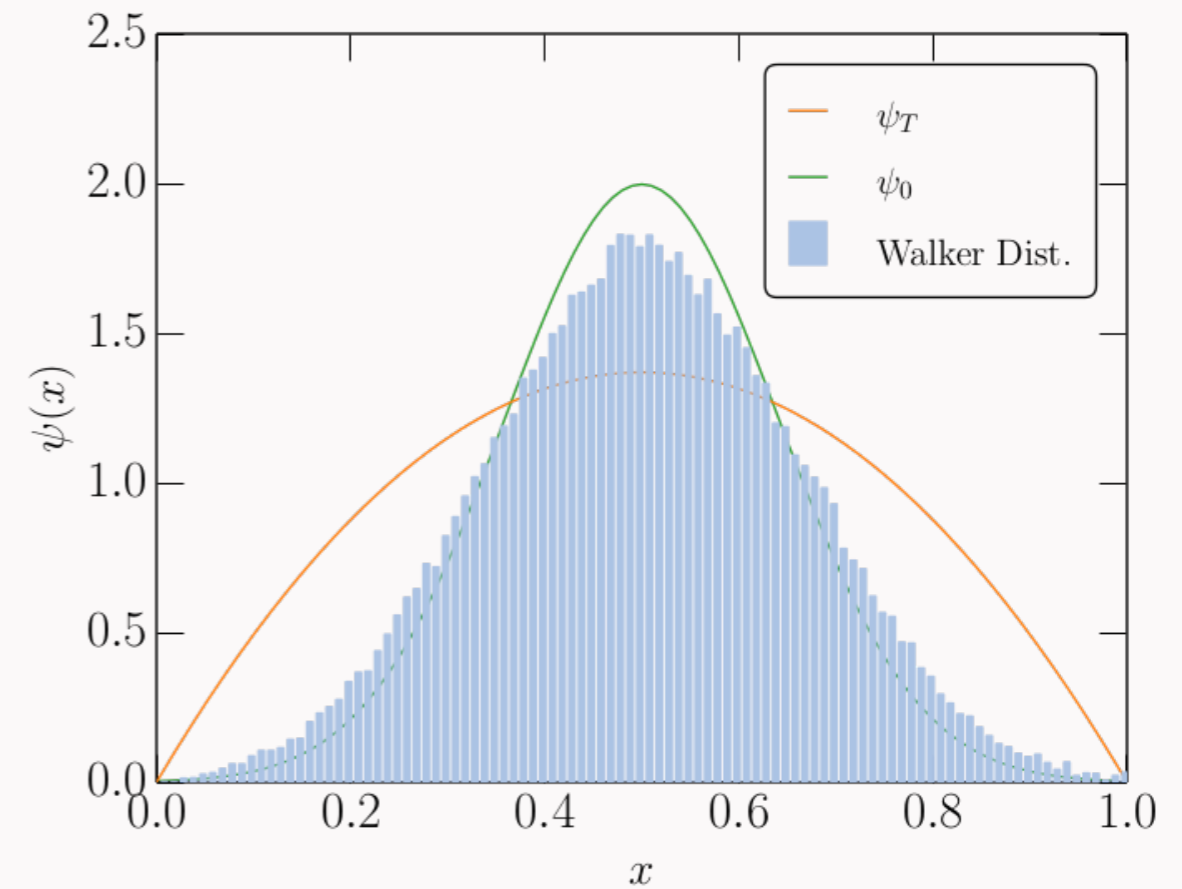
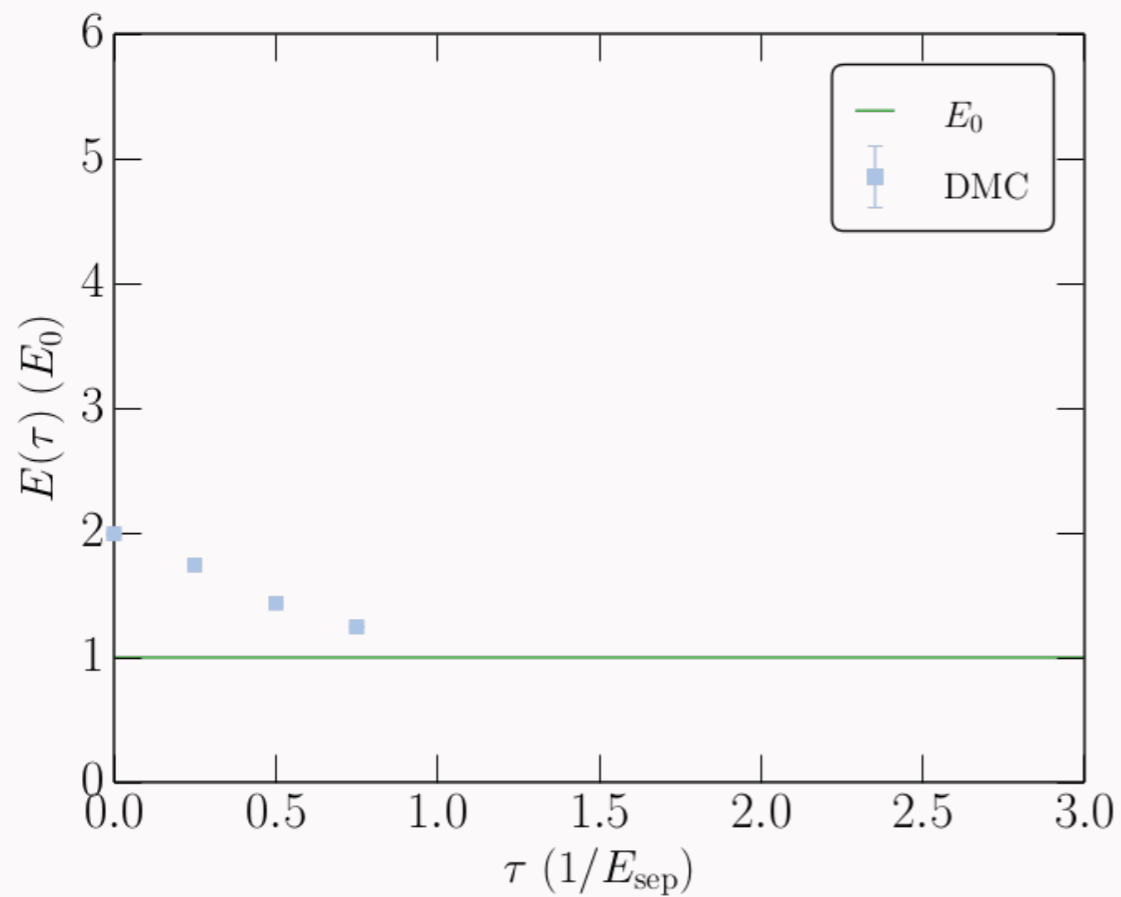




# QMC Methods - An Example

Imaginary-time evolution:

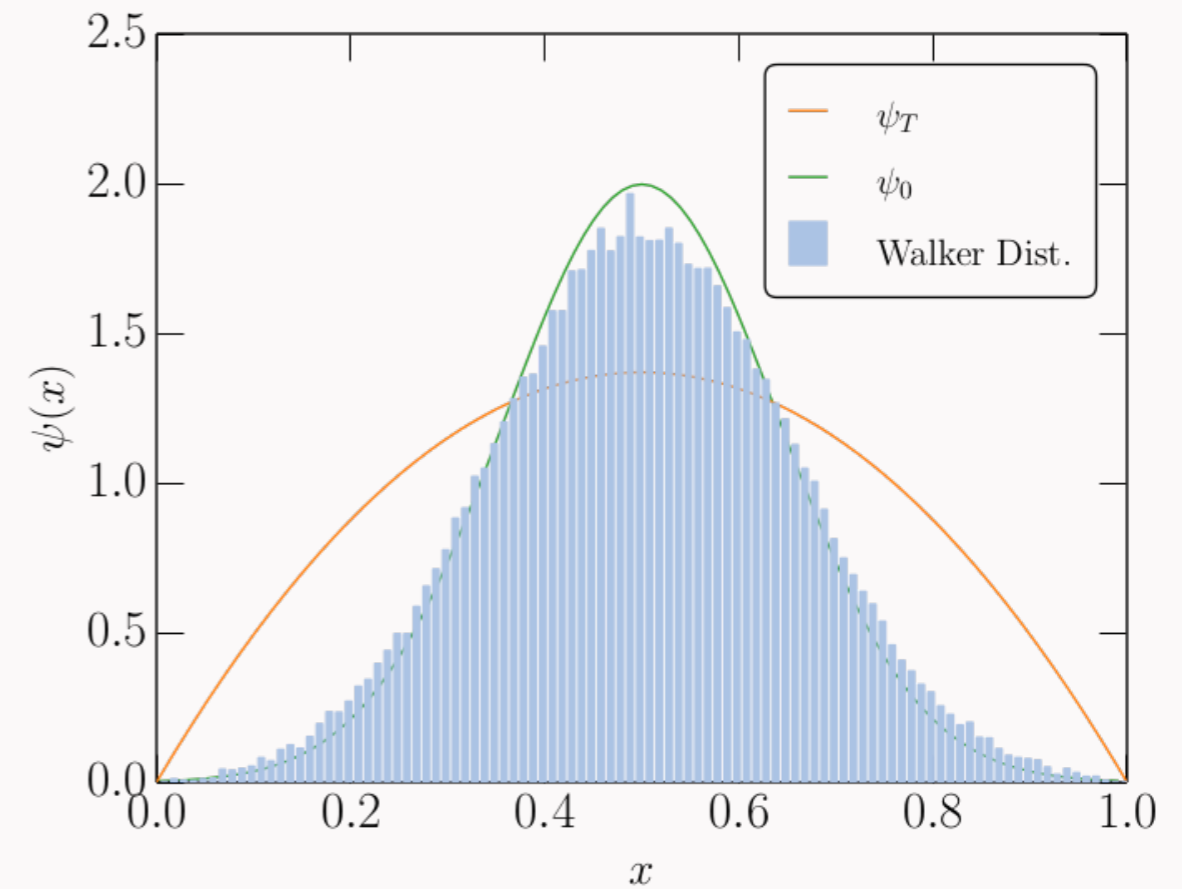
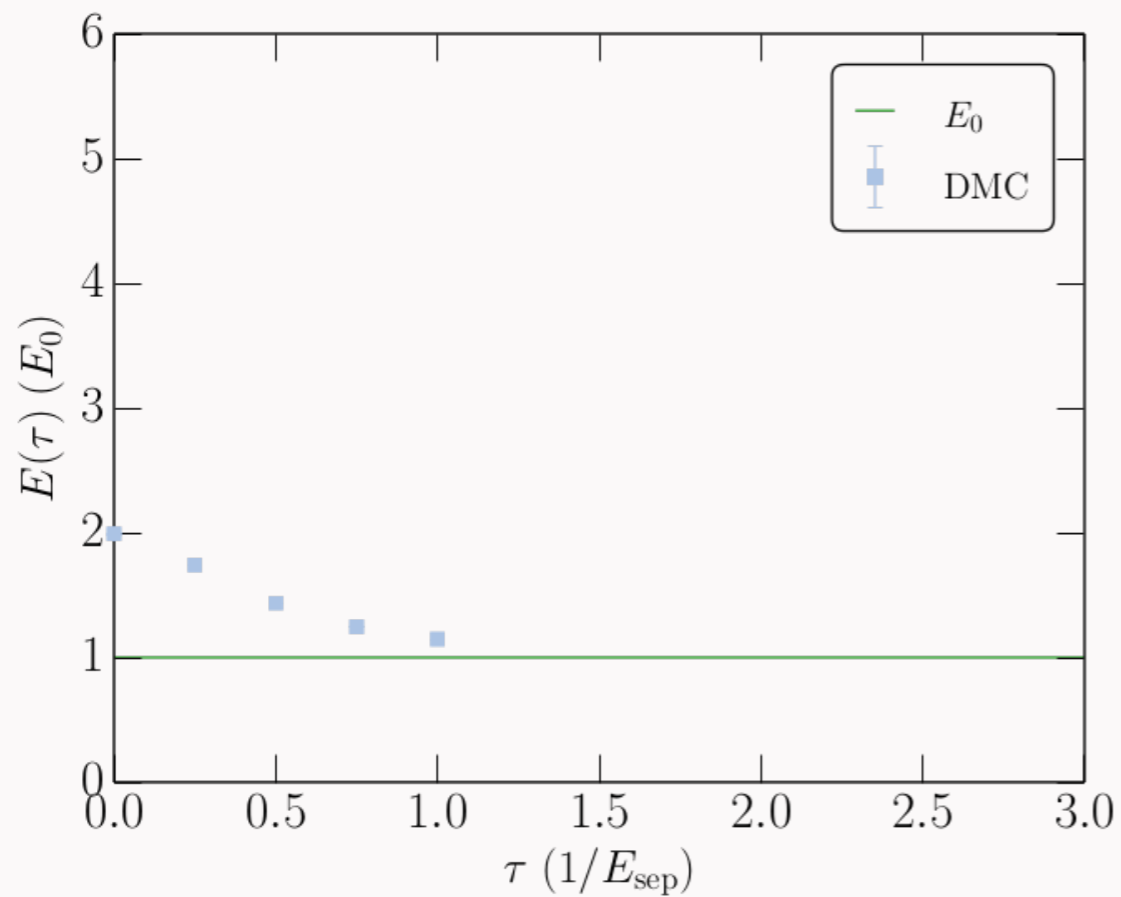
$$\tau = 0.75$$



# QMC Methods - An Example

Imaginary-time evolution:

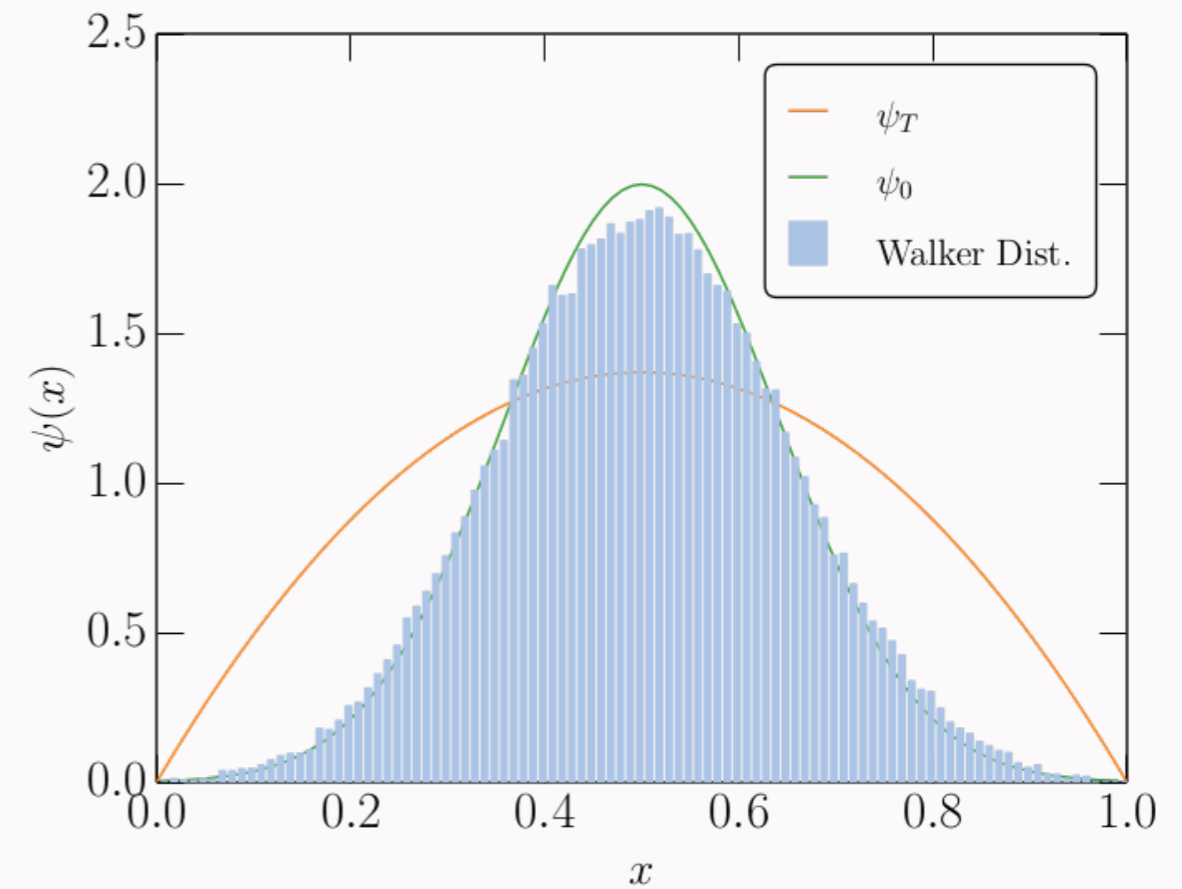
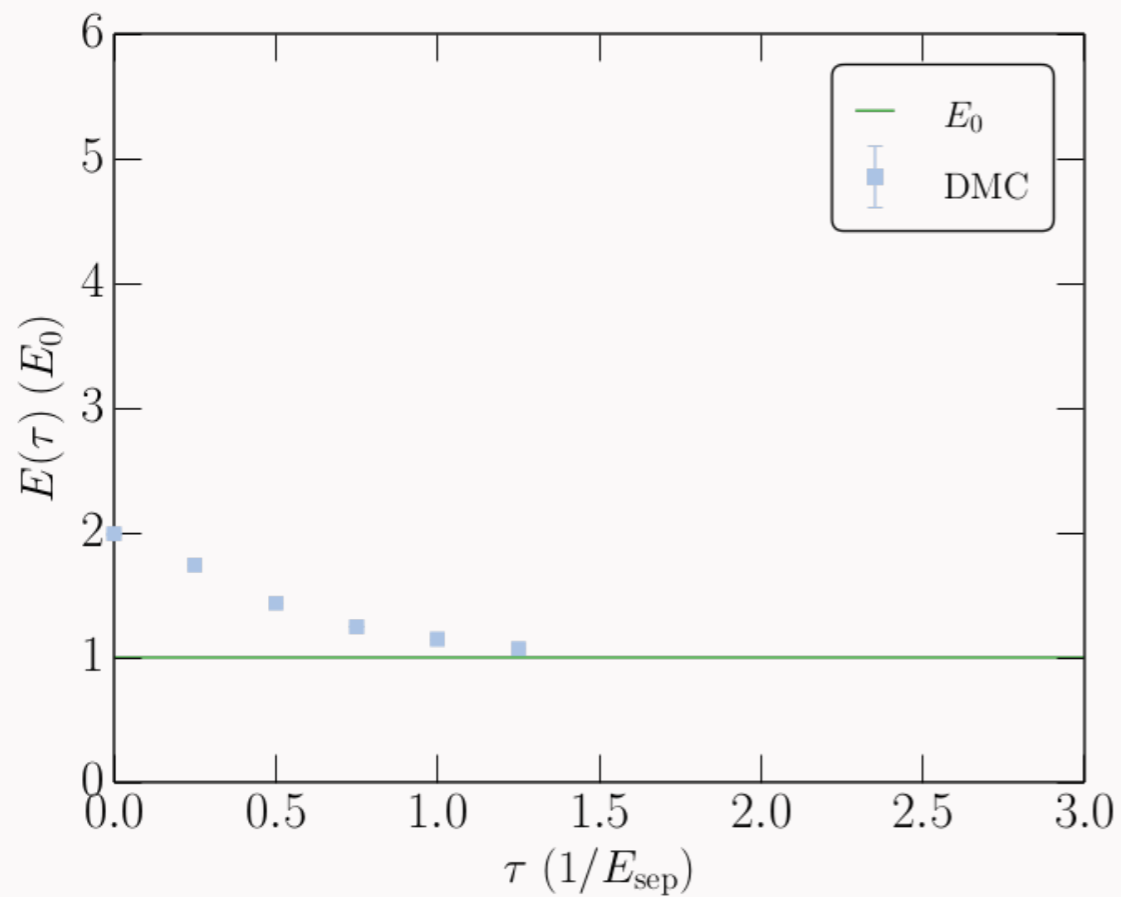
$$\tau = 1.00$$



# QMC Methods - An Example

Imaginary-time evolution:

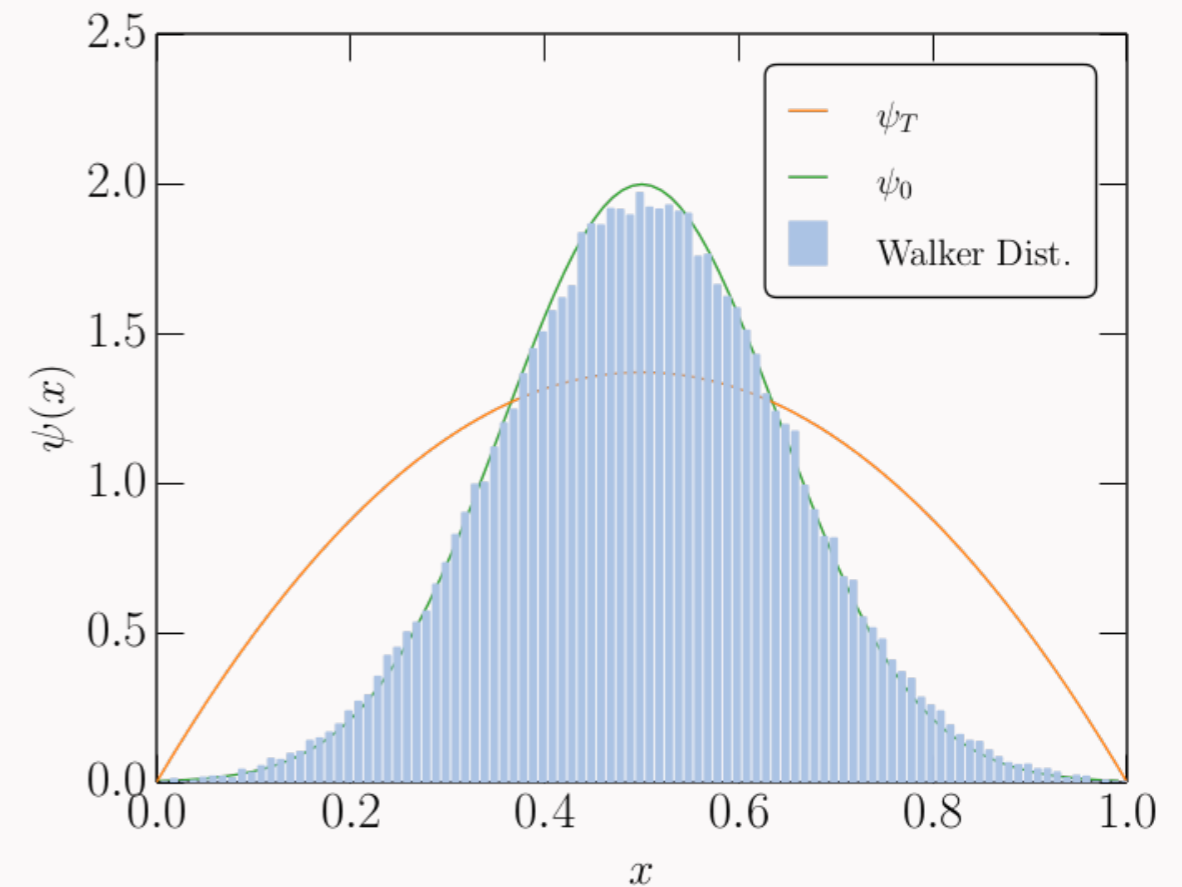
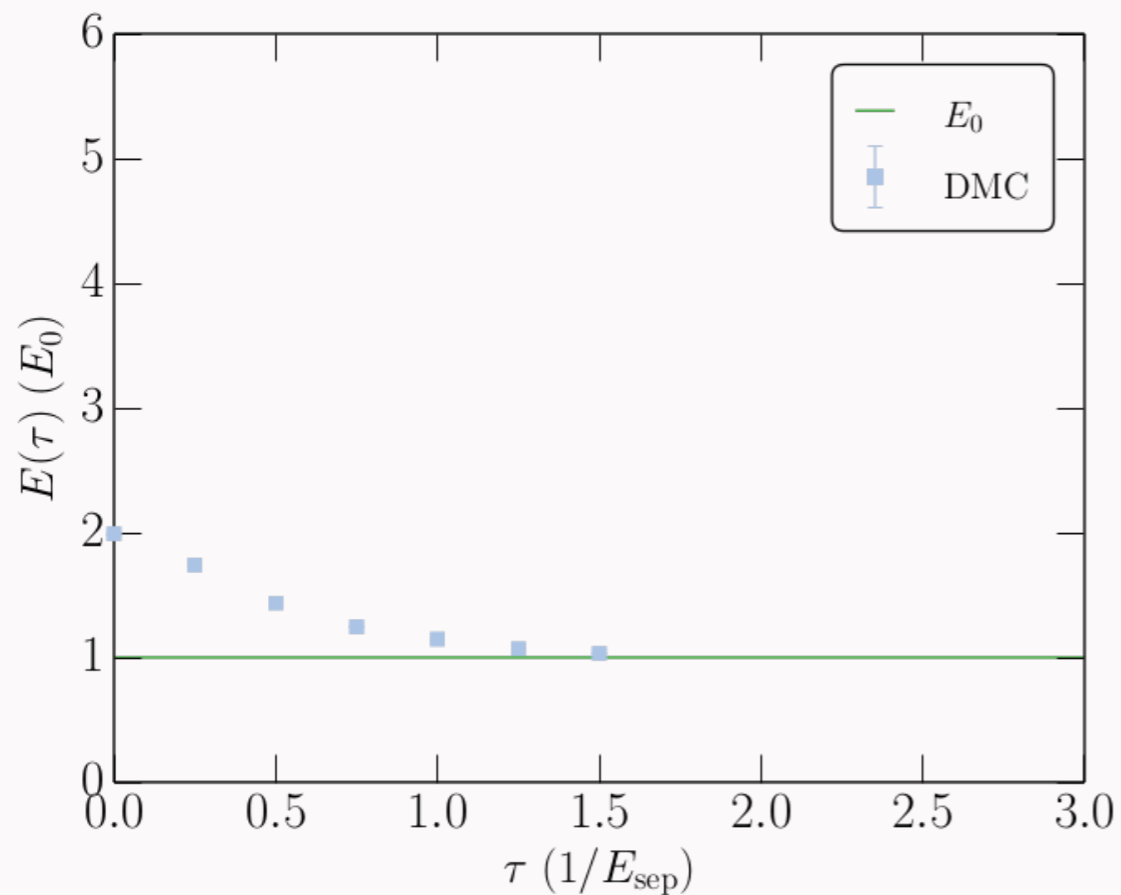
$$\tau = 1.25$$



# QMC Methods - An Example

Imaginary-time evolution:

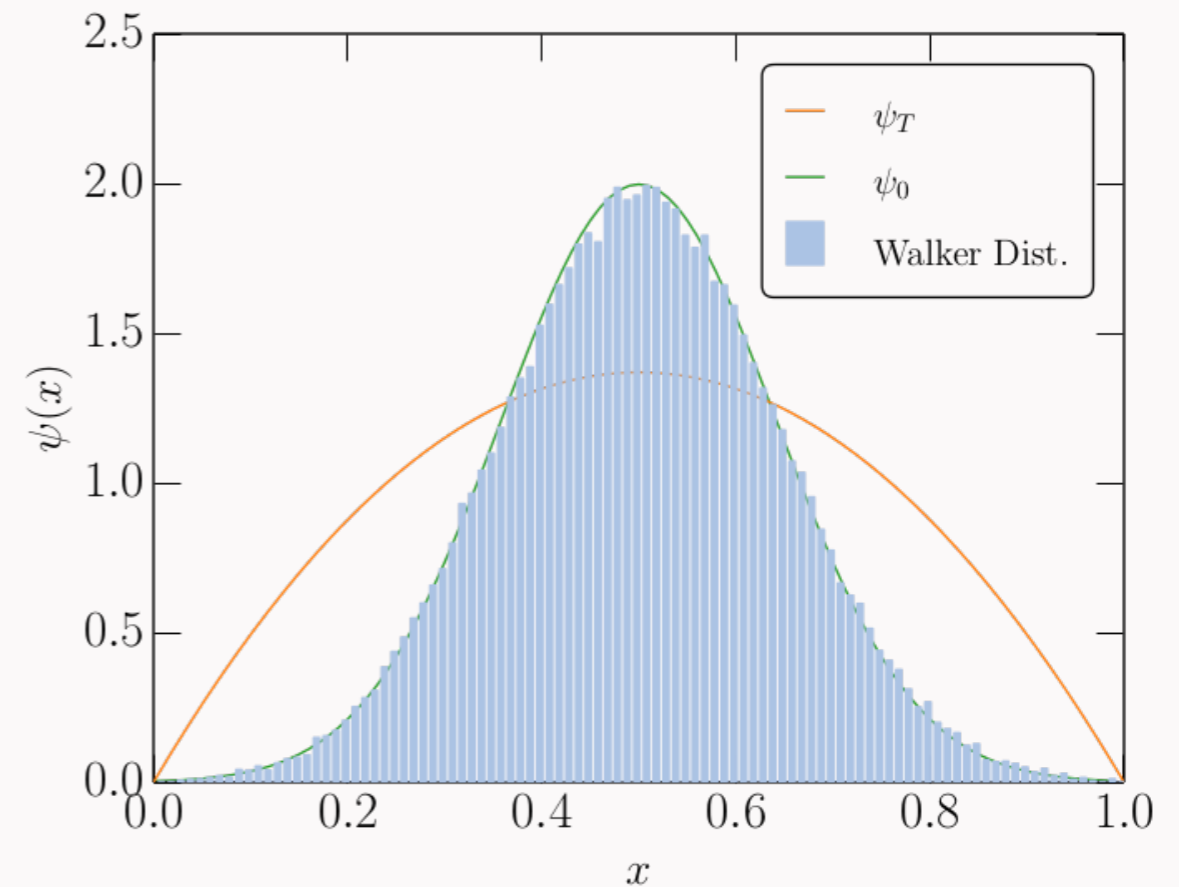
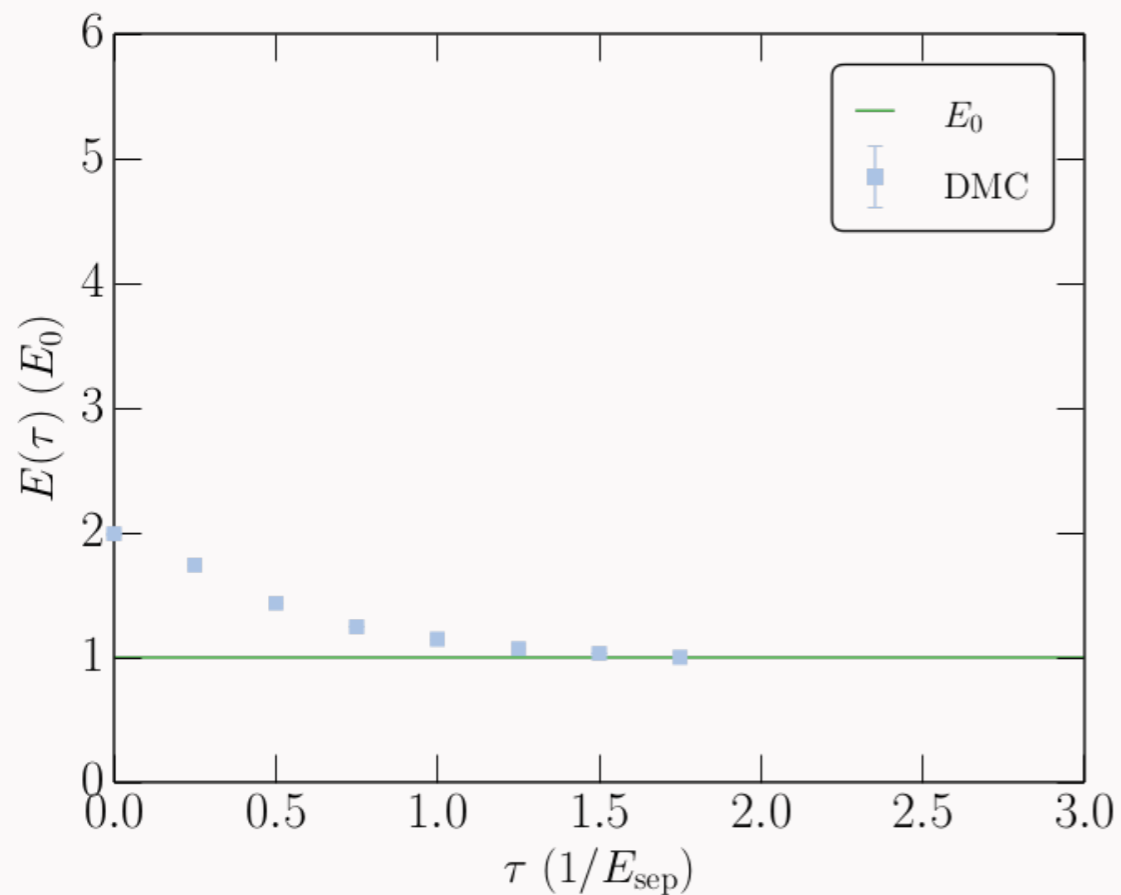
$$\tau = 1.50$$



# QMC Methods - An Example

Imaginary-time evolution:

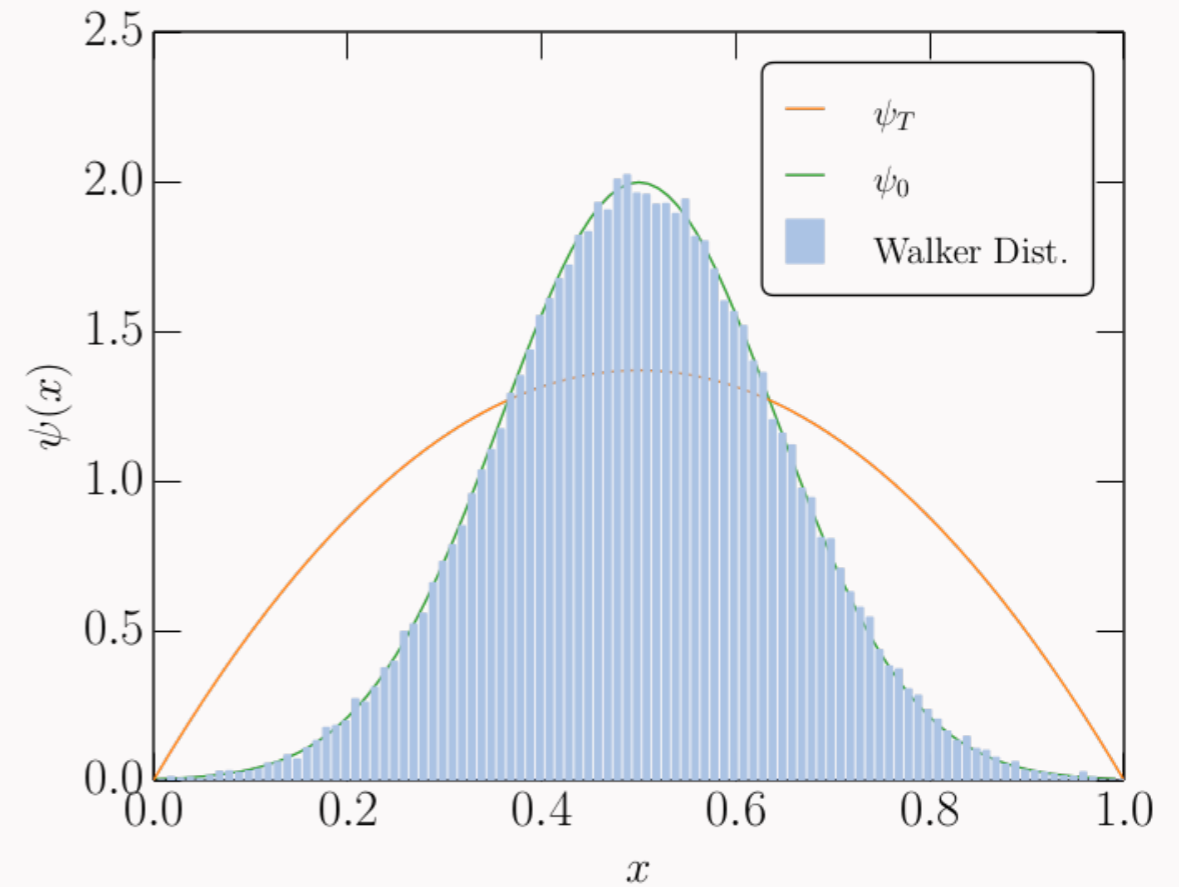
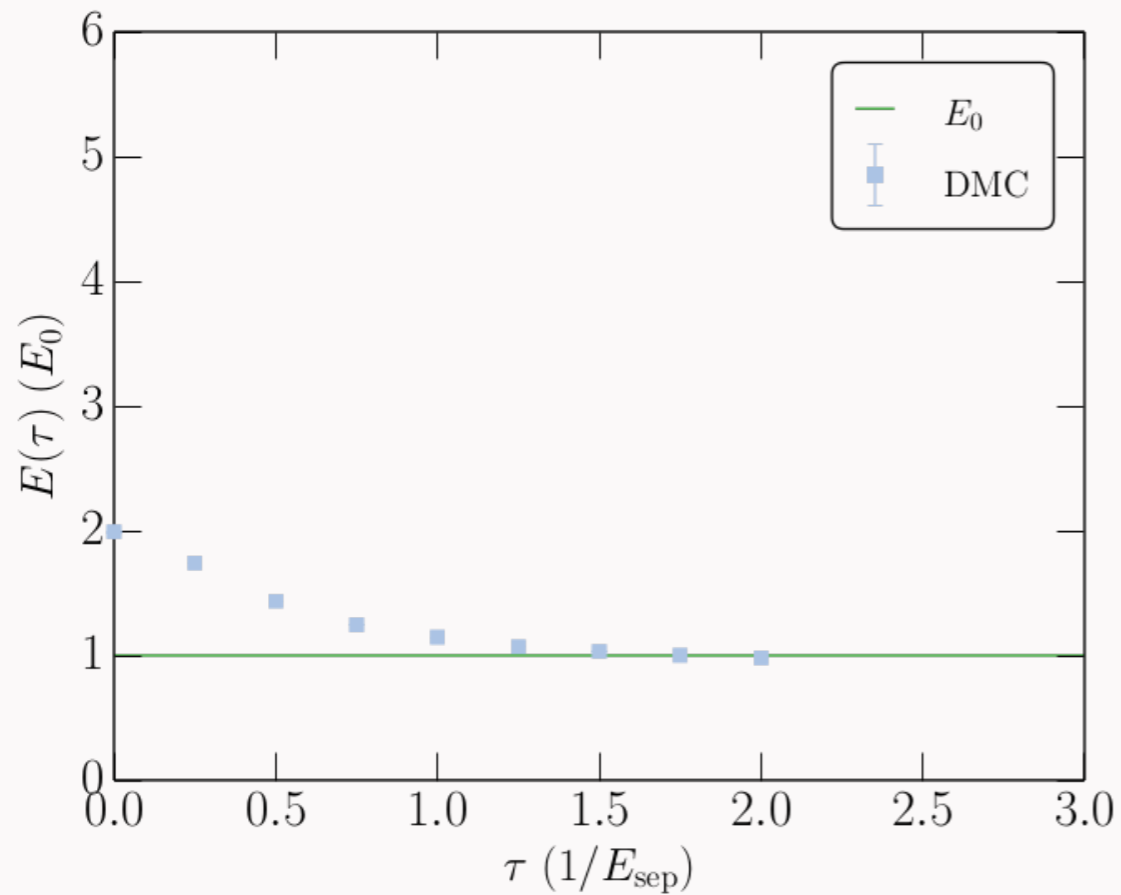
$$\tau = 1.75$$



# QMC Methods - An Example

Imaginary-time evolution:

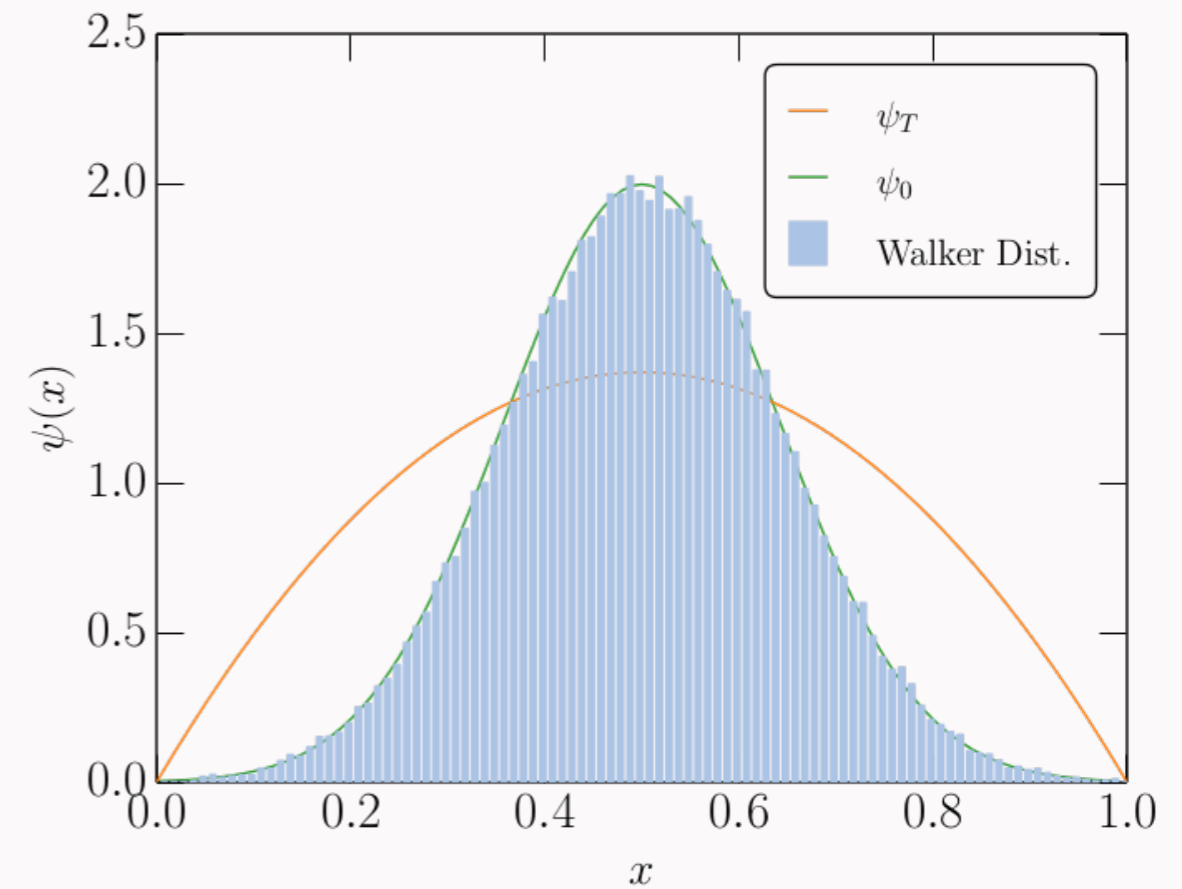
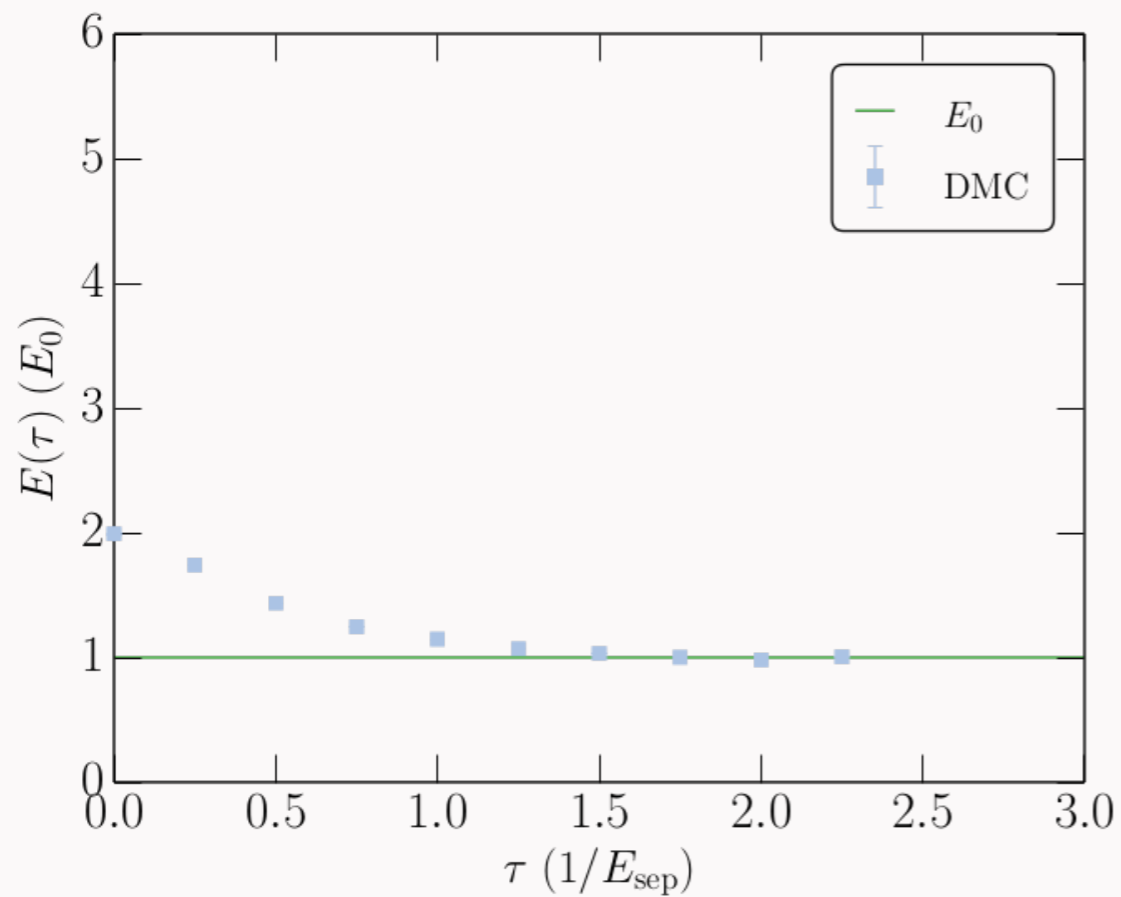
$$\tau = 2.00$$



# QMC Methods - An Example

Imaginary-time evolution:

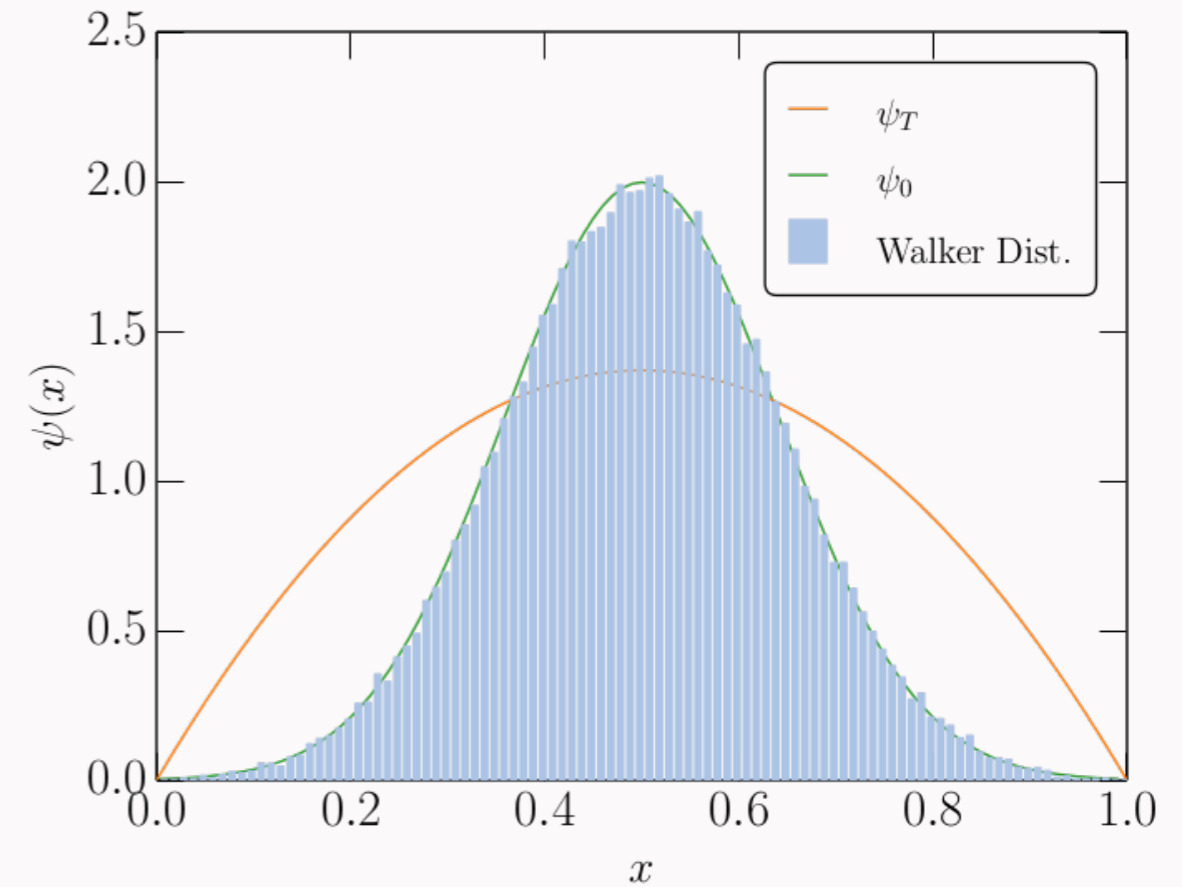
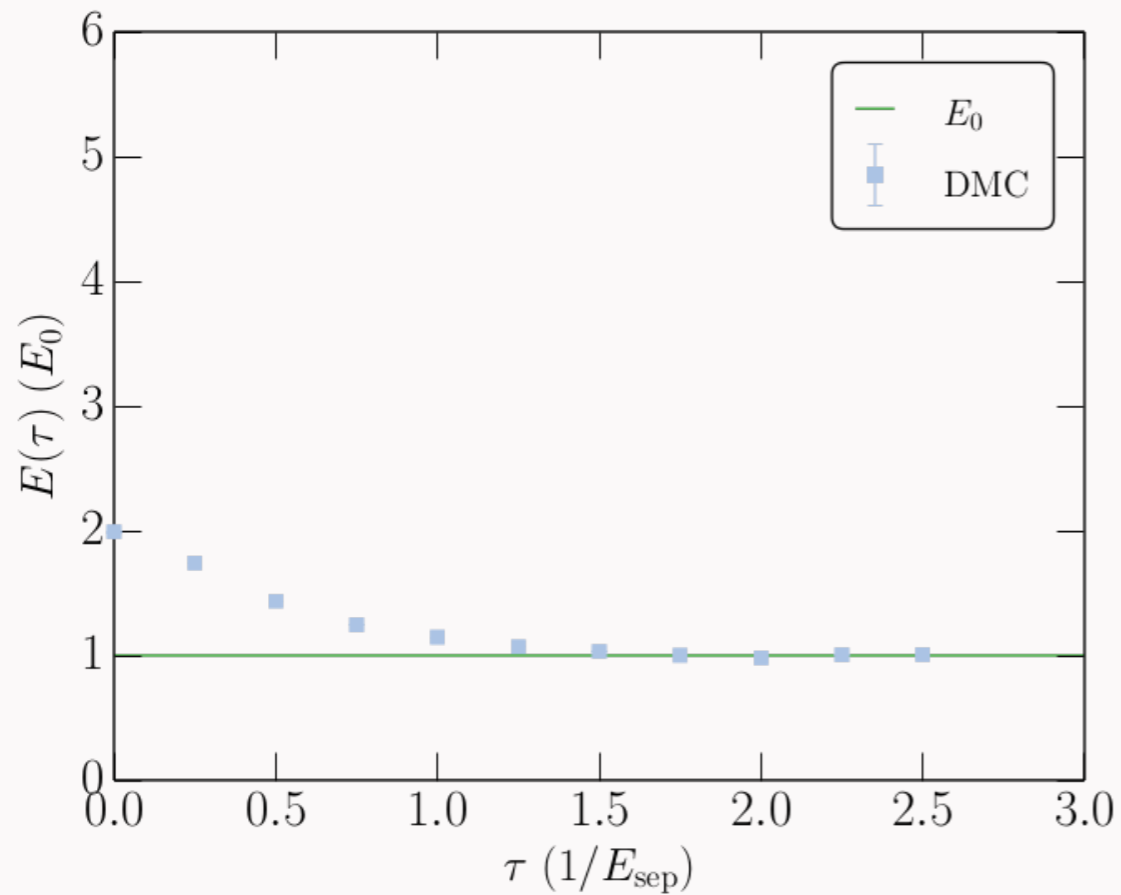
$$\tau = 2.25$$



# QMC Methods - An Example

Imaginary-time evolution:

$$\tau = 2.50$$

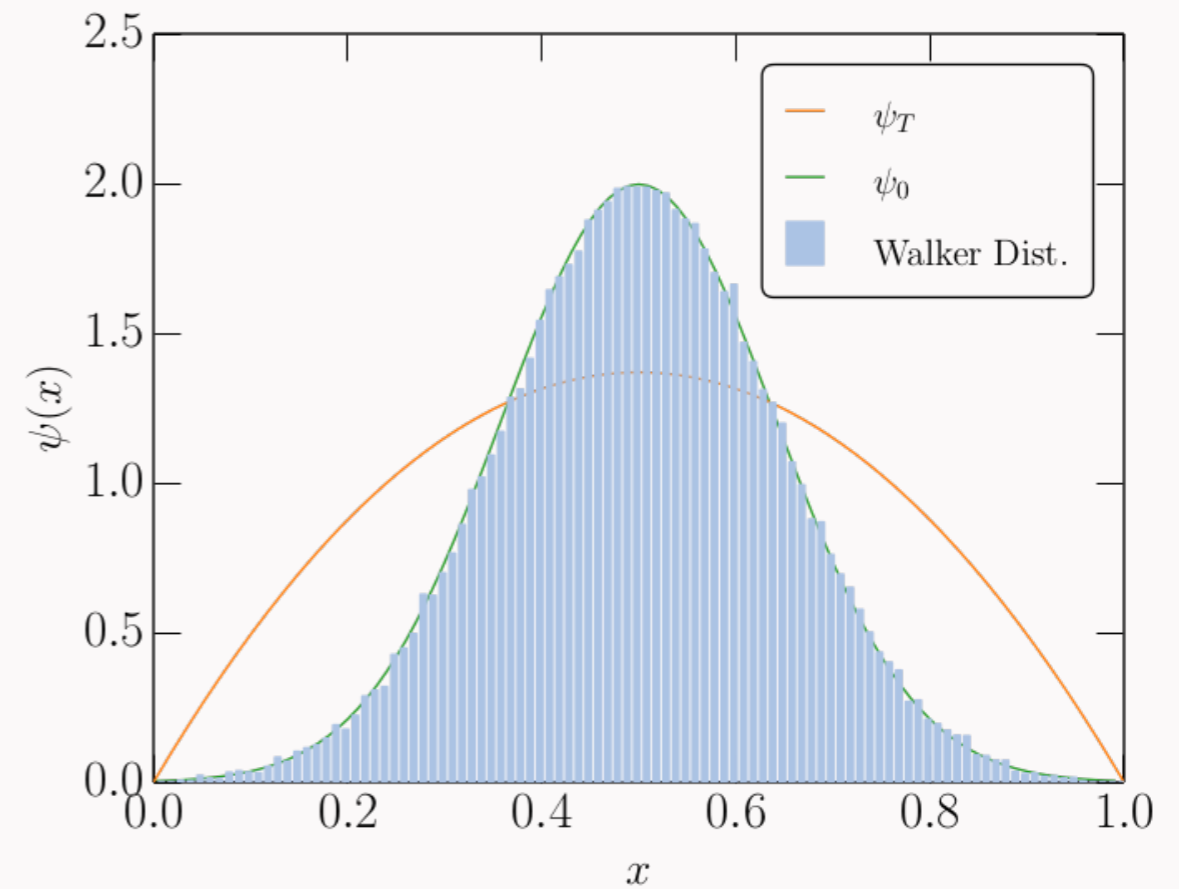
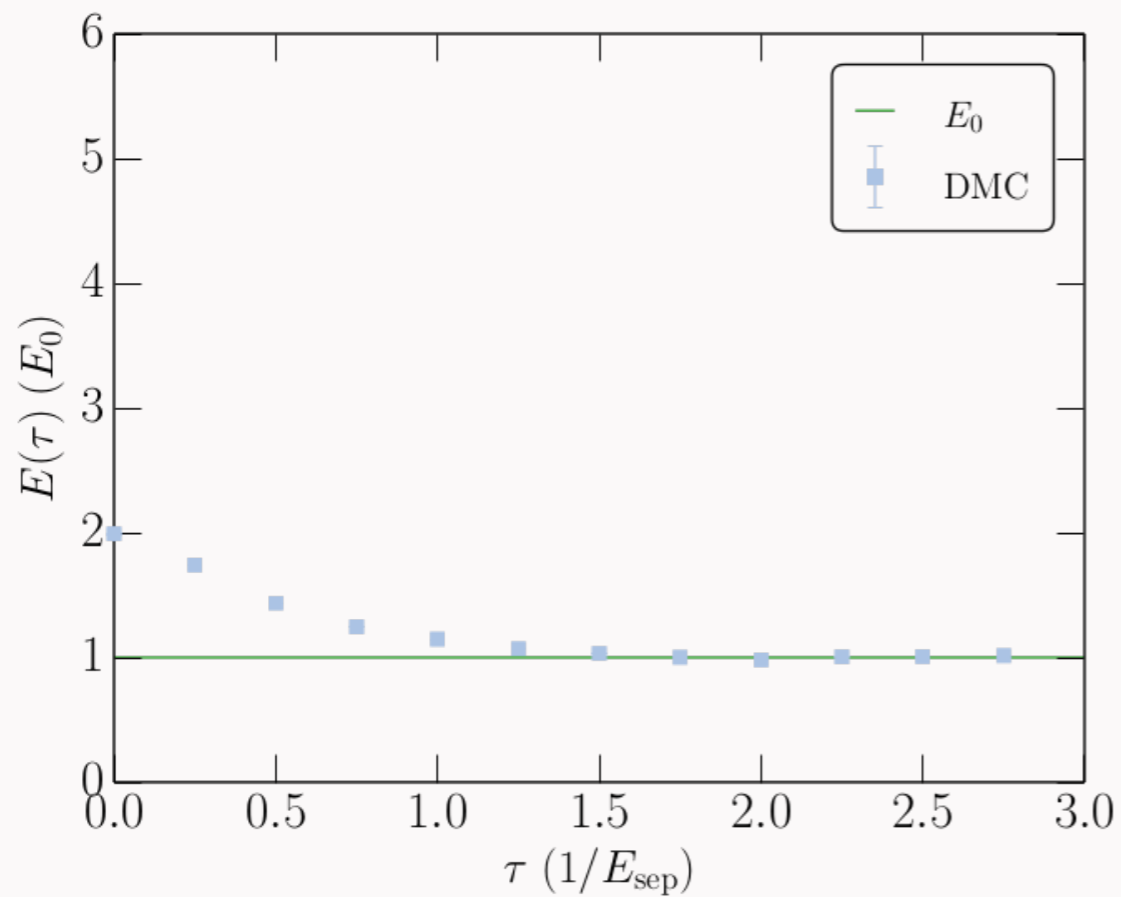




# QMC Methods - An Example

Imaginary-time evolution:

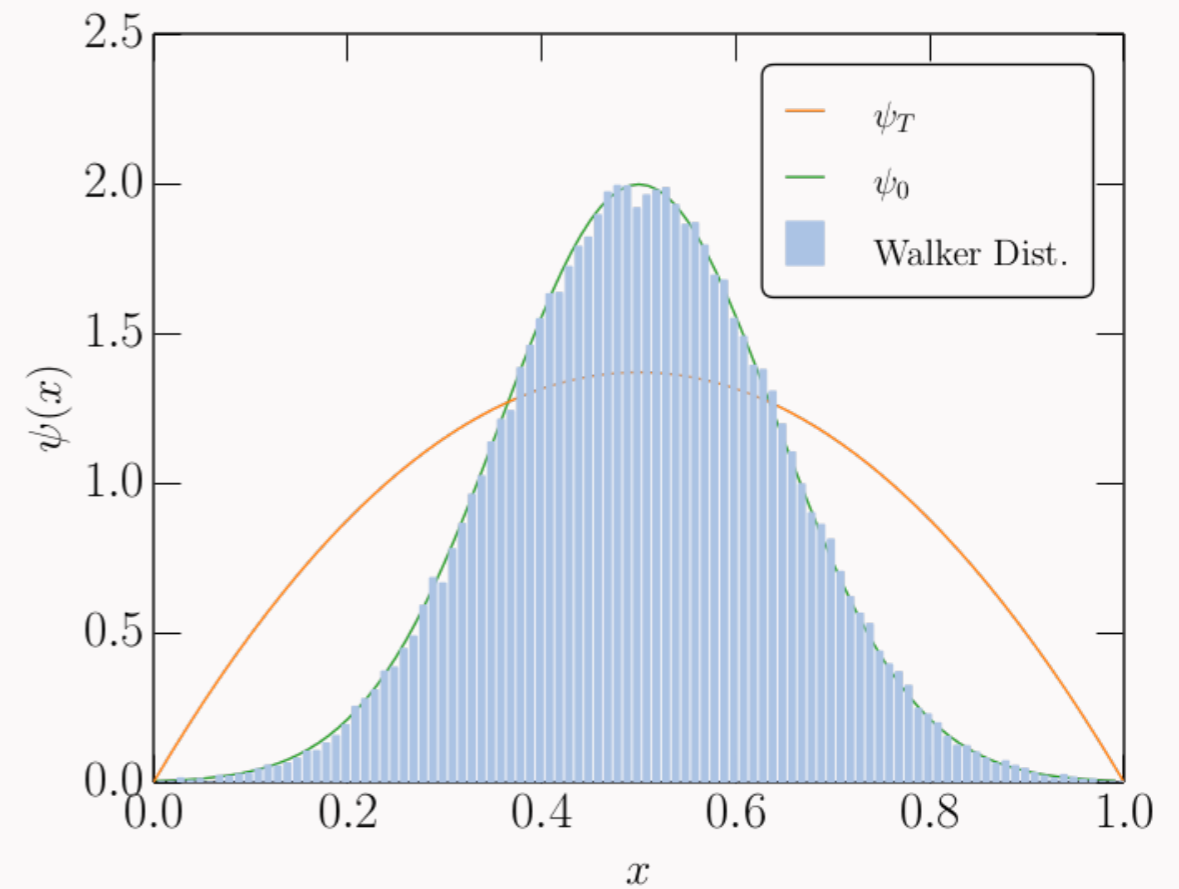
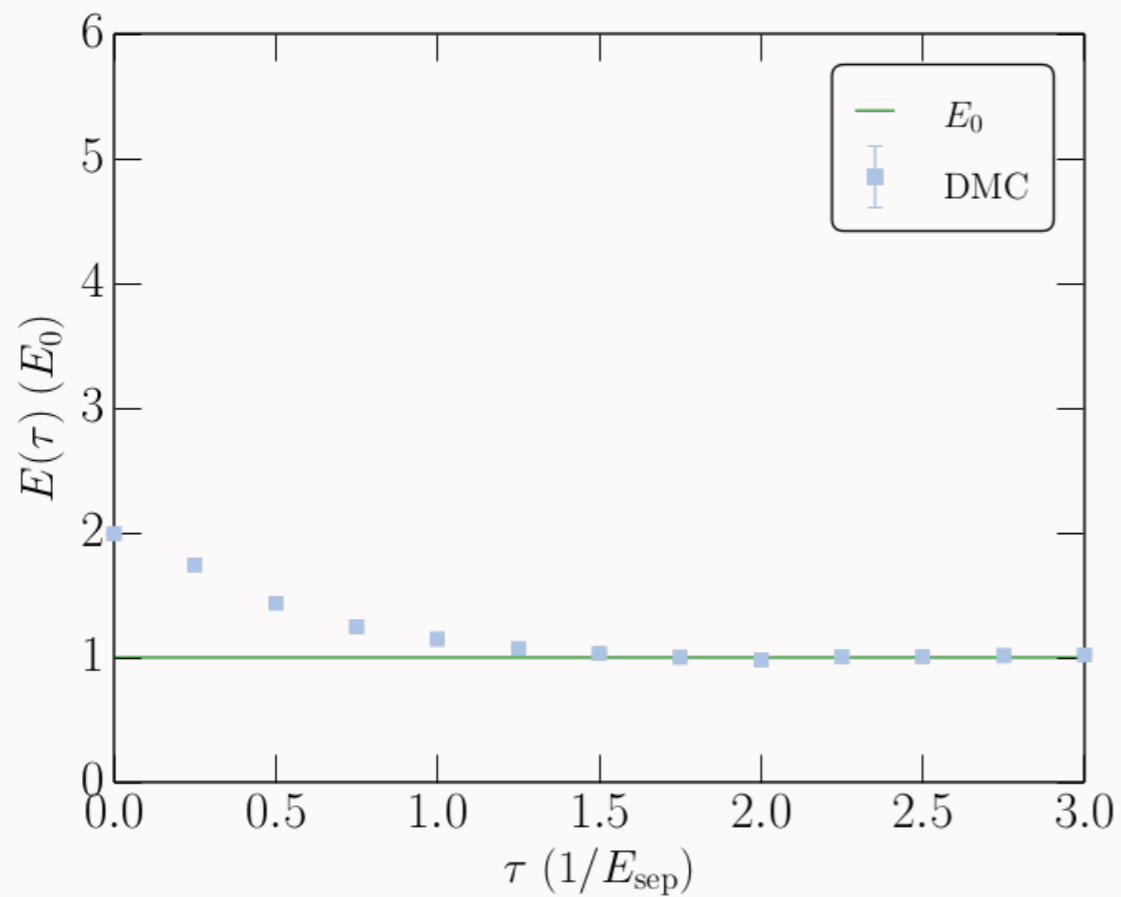
$$\tau = 2.75$$



# QMC Methods - An Example

Imaginary-time evolution:

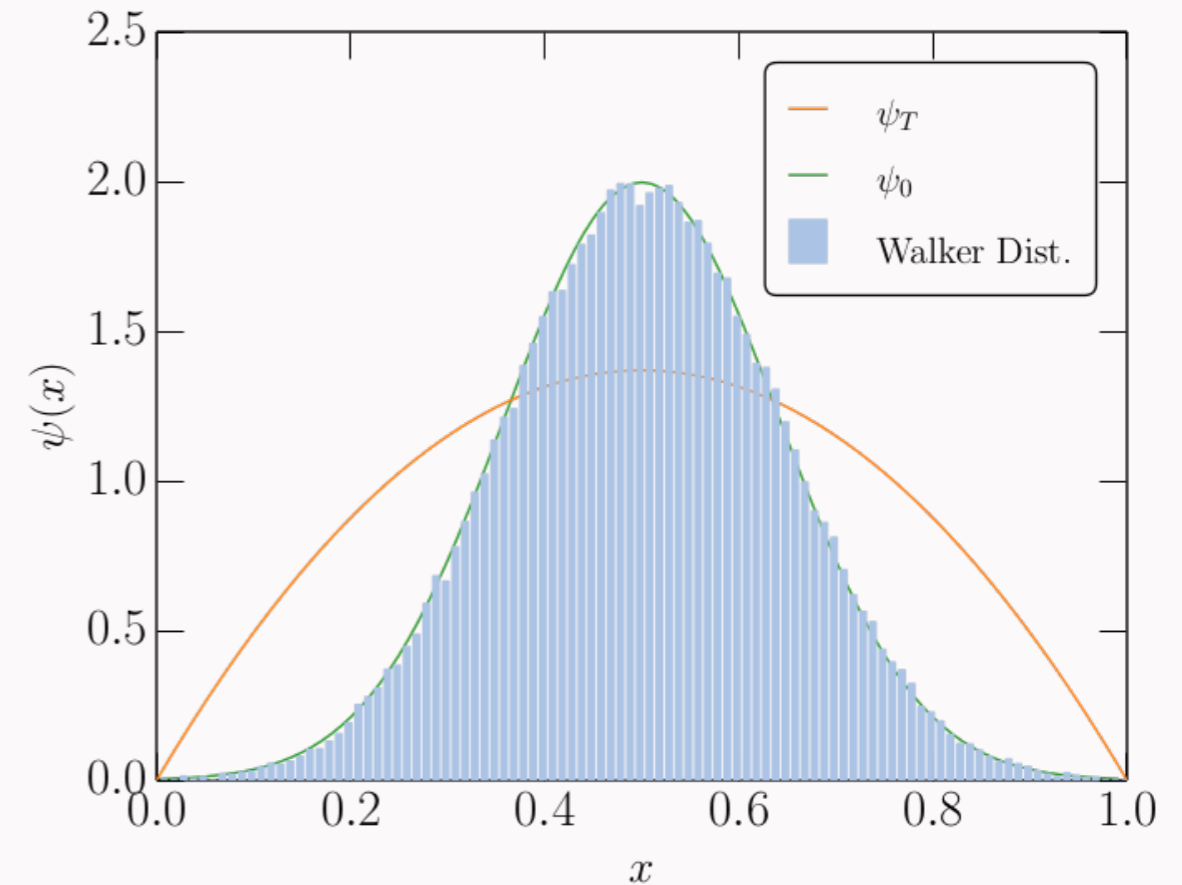
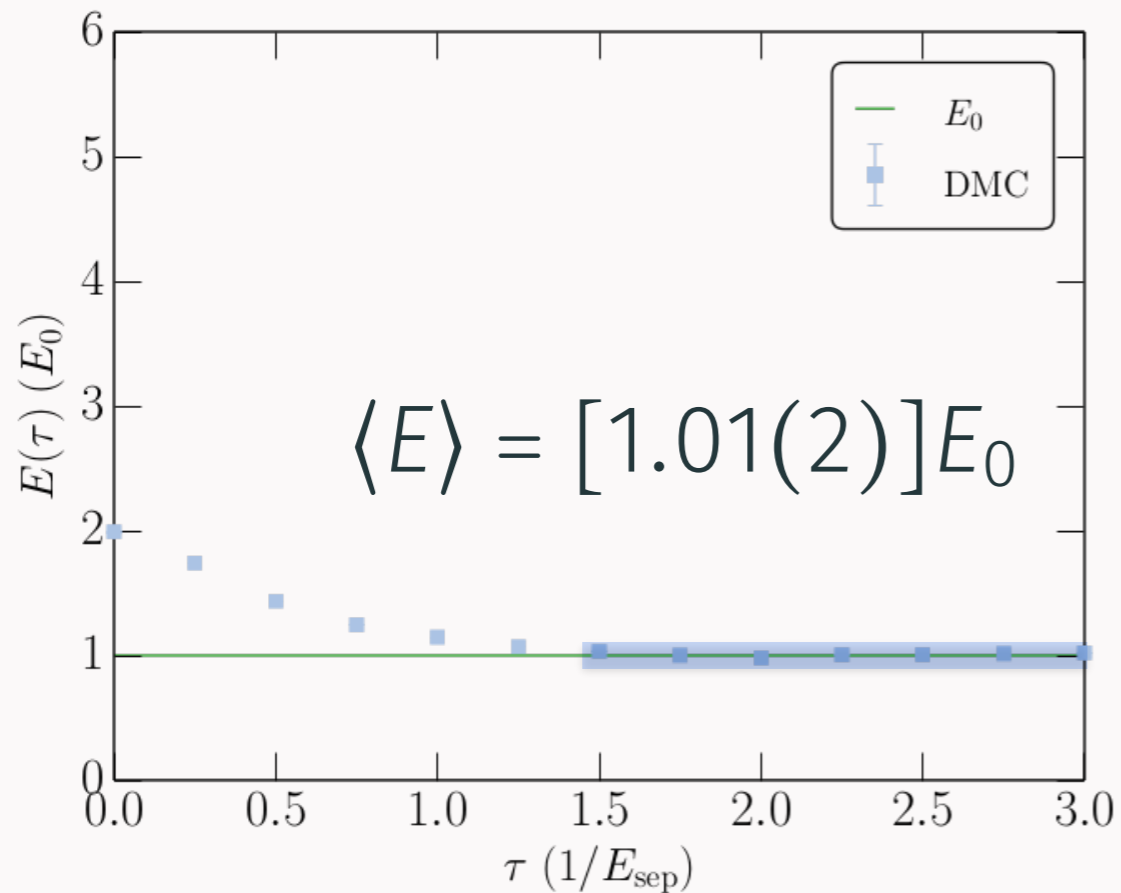
$$\tau = 3.00$$



# QMC Methods - An Example

Imaginary-time evolution:

$$\tau = 3.00$$



# QMC Methods - The Rug



fermion sign problem  
local regulators + Fierz ambiguity  
problems with scaling

# QMC Methods - Two Methods Used Below

## Green's function Monte Carlo (GFMC)

- Among the **most accurate** nuclear many-body *ab initio* methods.
- **Exponential scaling** in  $A$  (sum over all spin-isospin states).

## Auxiliary-field diffusion Monte Carlo (AFDMC)

- **Still in development** but now maturing quickly.
- **Polynomial scaling** in  $A$  (sample spin-isospin states).

# The Hamiltonian

Of course, the nuclear Hamiltonian is complicated.

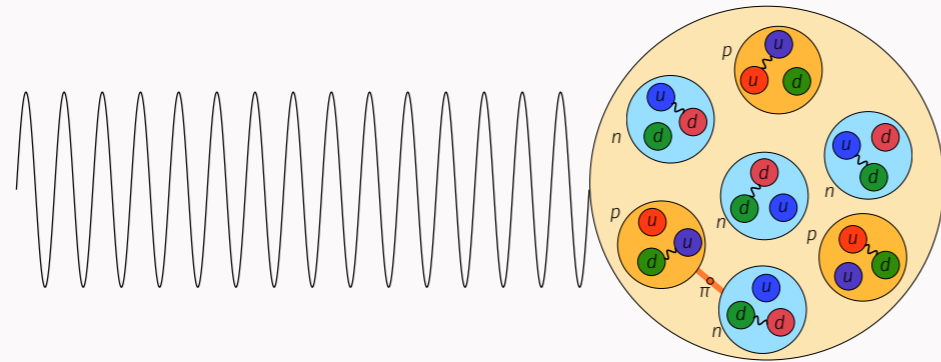
$$H = \sum_{i=1}^A \frac{\mathbf{p}_i^2}{2m_i} + \sum_{i<j}^A V_{ij} + \sum_{i<j<k}^A V_{ijk} + \dots$$

Where should it come from?

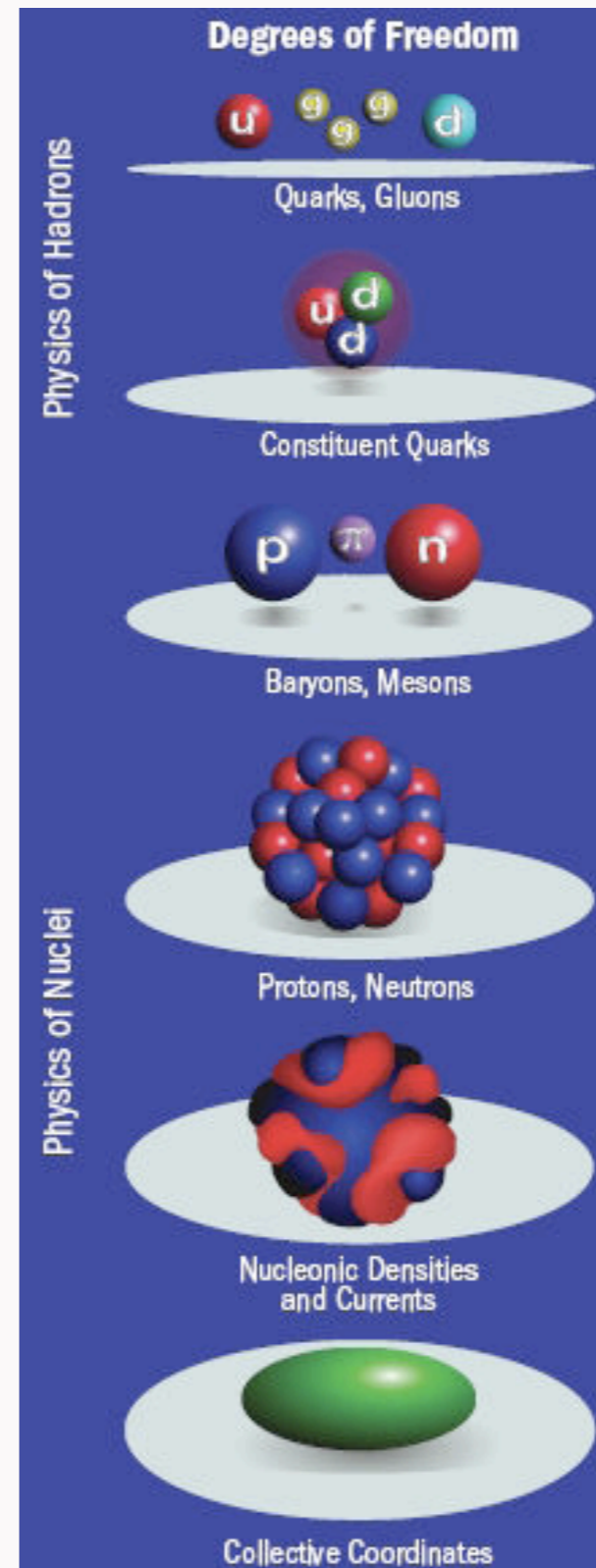
# Chiral EFT

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# Motivation - Chiral EFT



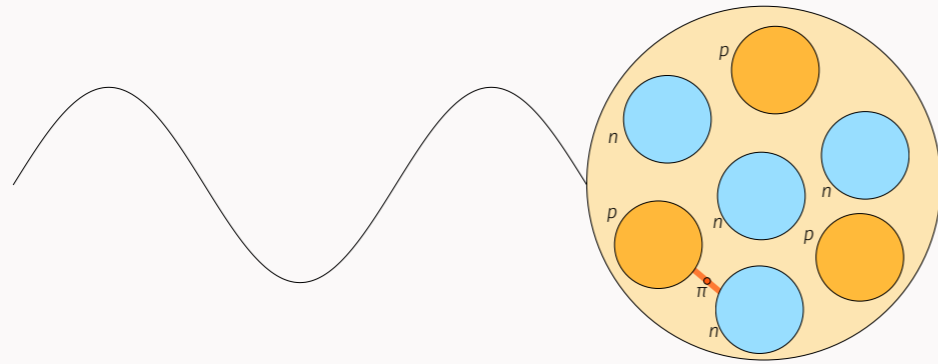
- If probed at high energies, substructure is resolved.
- At low energies, details are not resolved.
- Can replace fine structure by something simpler (think of multipole expansion): low-energy observables unchanged.



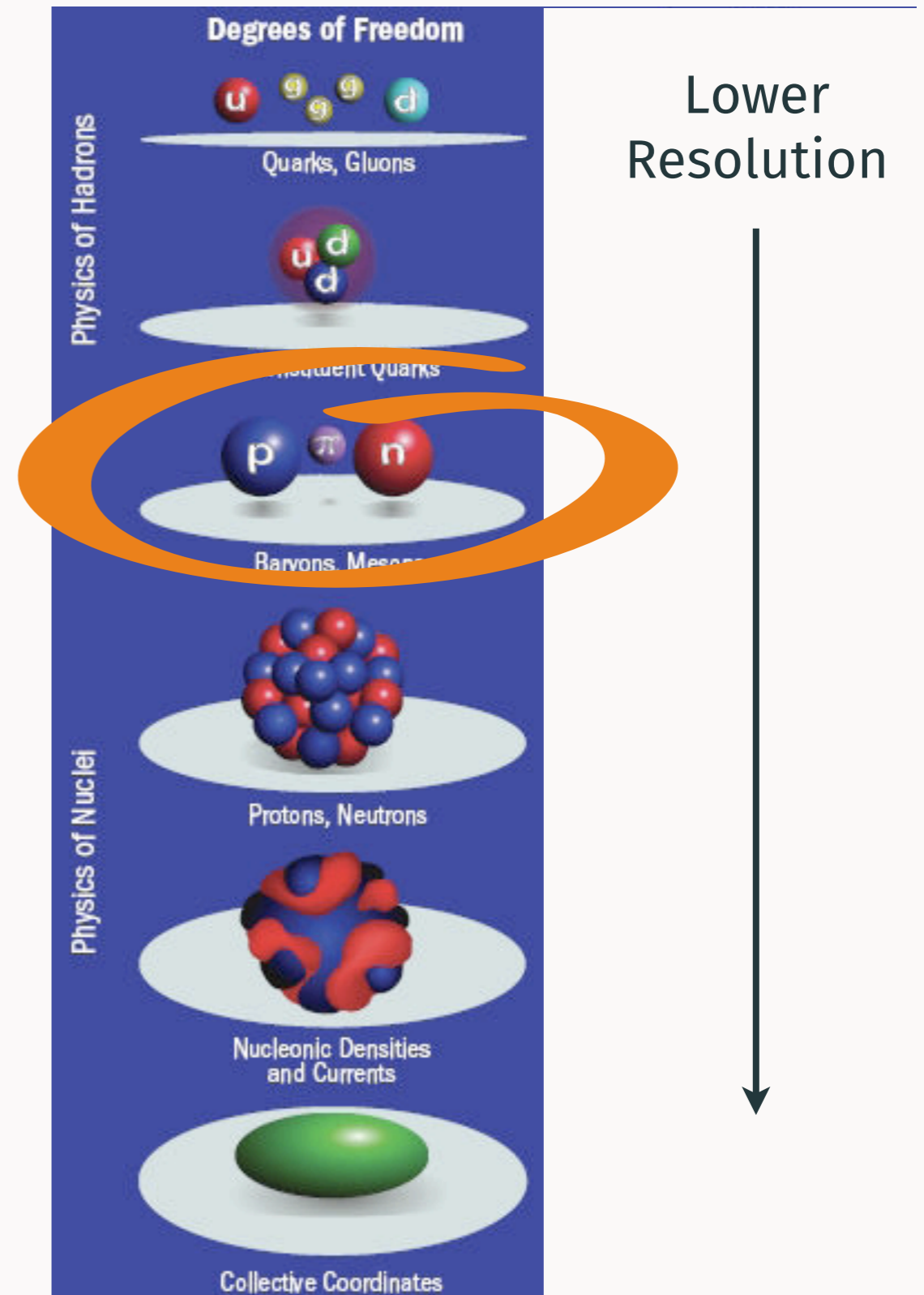
Lower  
Resolution



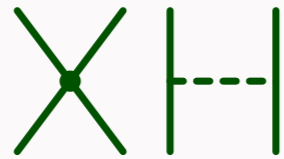
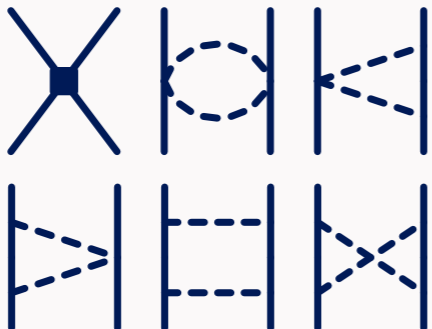
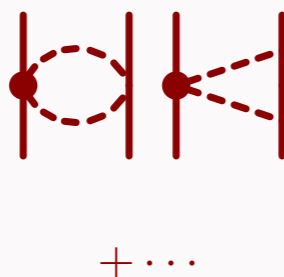
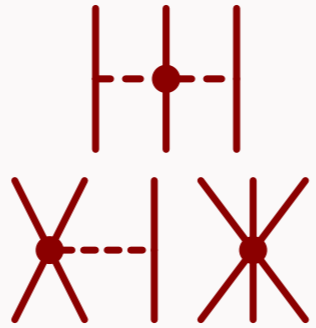

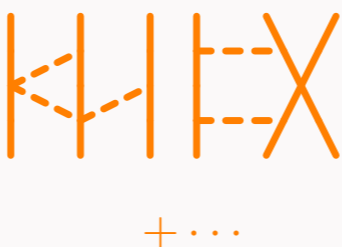
# Motivation - Chiral EFT



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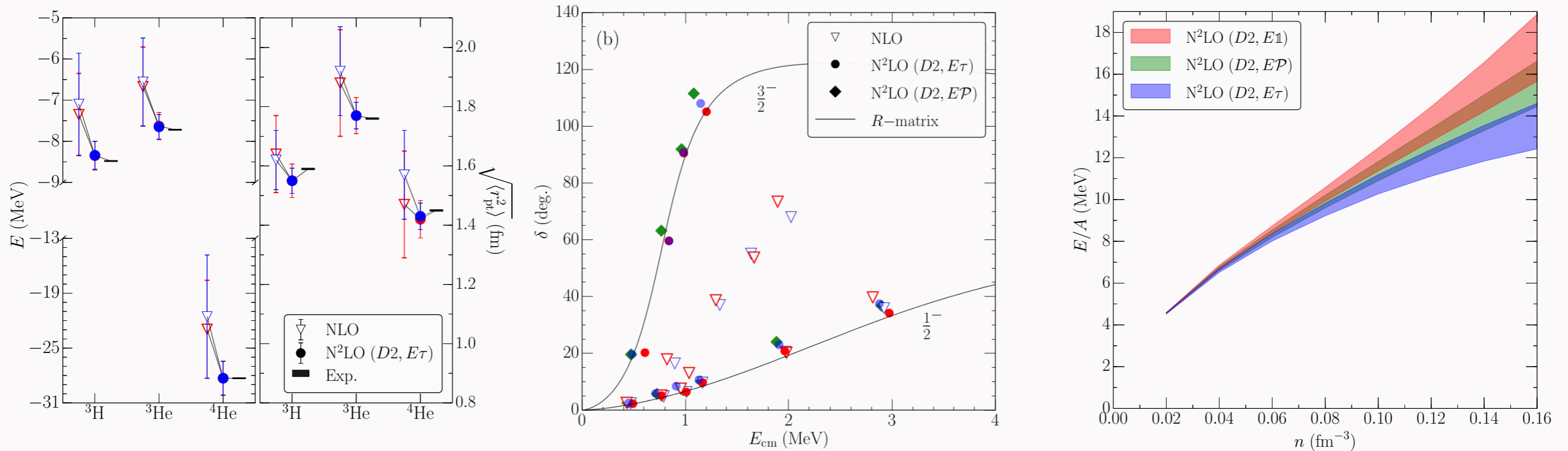
# Chiral EFT

		NN	NNN
LO	$\mathcal{O}\left(\frac{Q}{\Lambda_b}\right)^0$		-
NLO	$\mathcal{O}\left(\frac{Q}{\Lambda_b}\right)^2$		-
N <sup>2</sup> LO	$\mathcal{O}\left(\frac{Q}{\Lambda_b}\right)^3$		
N <sup>3</sup> LO	$\mathcal{O}\left(\frac{Q}{\Lambda_b}\right)^4$		

- Chiral EFT: Expand in powers of  $Q/\Lambda_b$ .  
 $Q \sim m_\pi \sim 100 \text{ MeV}$   
 $\Lambda_b \sim 500 \text{ MeV}$
- Long-range physics:  $\pi$  exchanges.
- Short-range physics: Contacts  $\times$  LECs.
- Many-body forces & currents enter systematically.

# Results

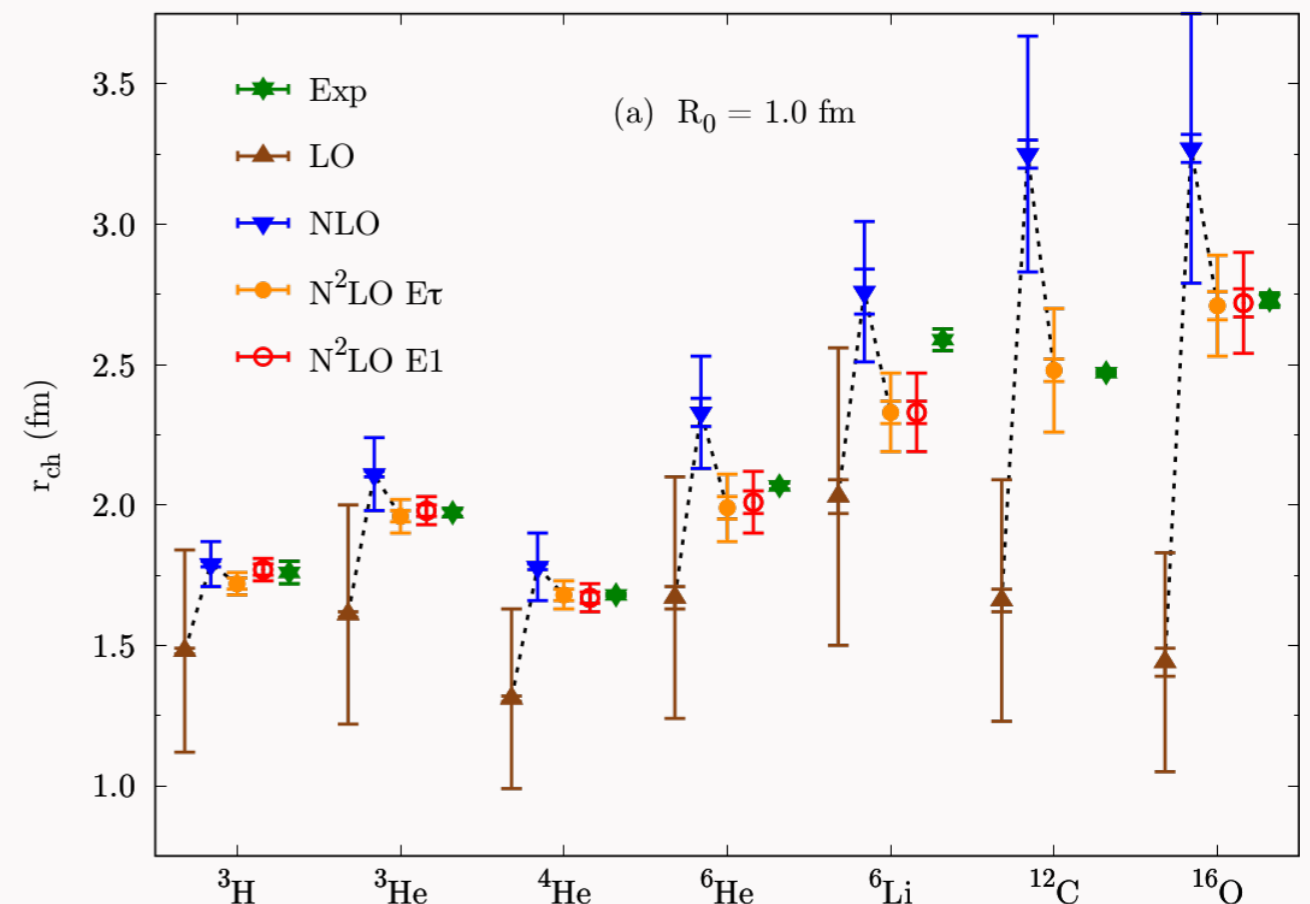
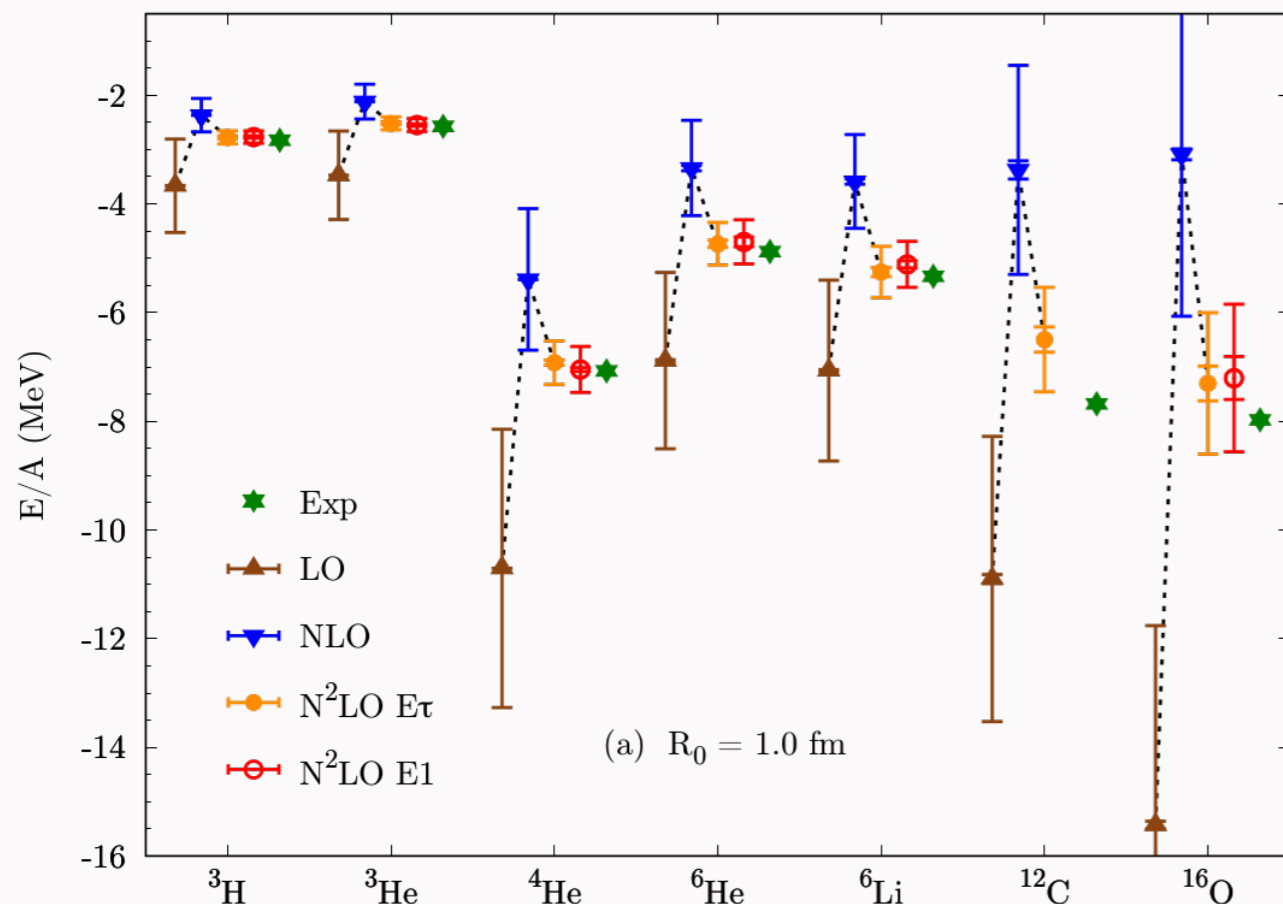
A simultaneous description of properties of light nuclei,  $n$ - $\alpha$  scattering and neutron matter is possible.  
Uncertainty analysis as in  
E. Epelbaum et al, EPJ **A51**, 53 (2015).



JEL et al, PRL **116**, 062501 (2016)

# AFDMC Results

Energies and charge radii of selected nuclei up to  $^{16}\text{O}$  well reproduced.



# SRCs & EMC Effect

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# Some History And Definitions

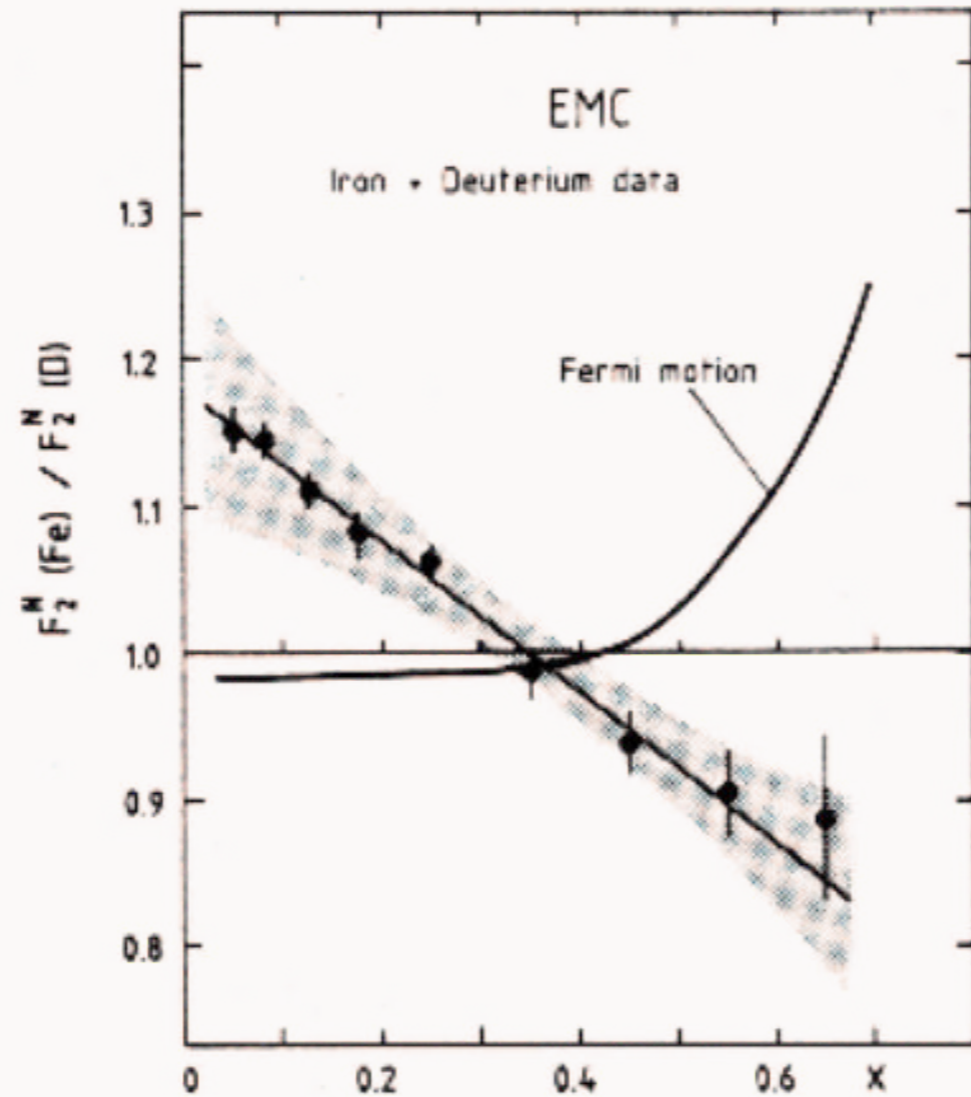
Deep inelastic scattering (DIS) cross section for EM interactions of charged leptons with nuclear targets:

$$\frac{d^2\sigma}{dQ^2 dx} \propto \frac{4\pi\alpha^2}{Q^4} \frac{F_2^A(x, Q^2)}{x}$$

Bjorken  $x = Q^2/(2p \cdot q)$ , and  $Q^2 = -q^2$  are defined in terms of the target four-momentum  $p$  and the momentum transfer from the lepton to the target,  $q$ .

# 1983 EMC Paper

One-picture/One-sentence summary



K. Rith, arXiv:1402.5000 [hep-ex] (2014)

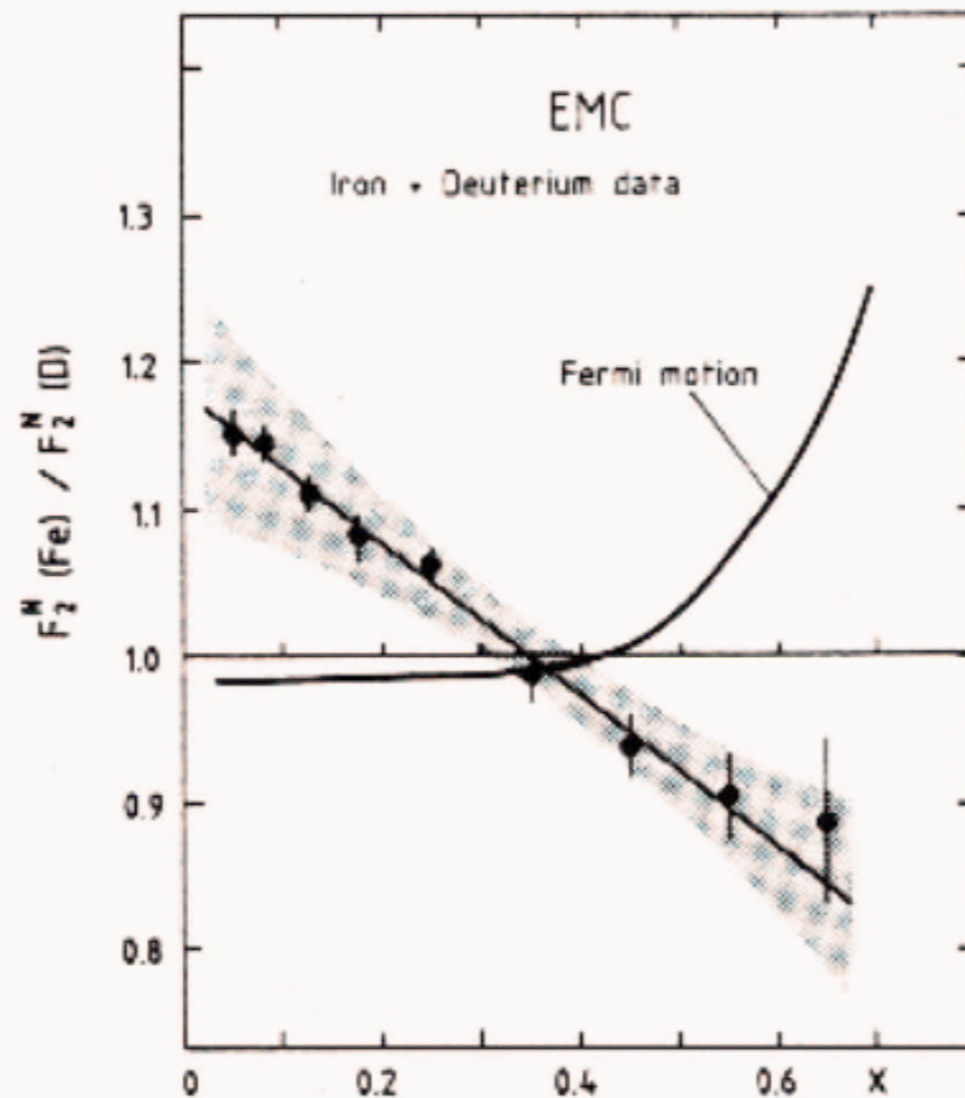
J. J. Aubert et al. (EMC), Phys. Lett. B. **123**, 275

“We are not aware of any published detailed prediction presently available which can explain the behaviour of these data.”

# 1983 EMC Paper

The strength of the EMC effect is given in terms of the slope:

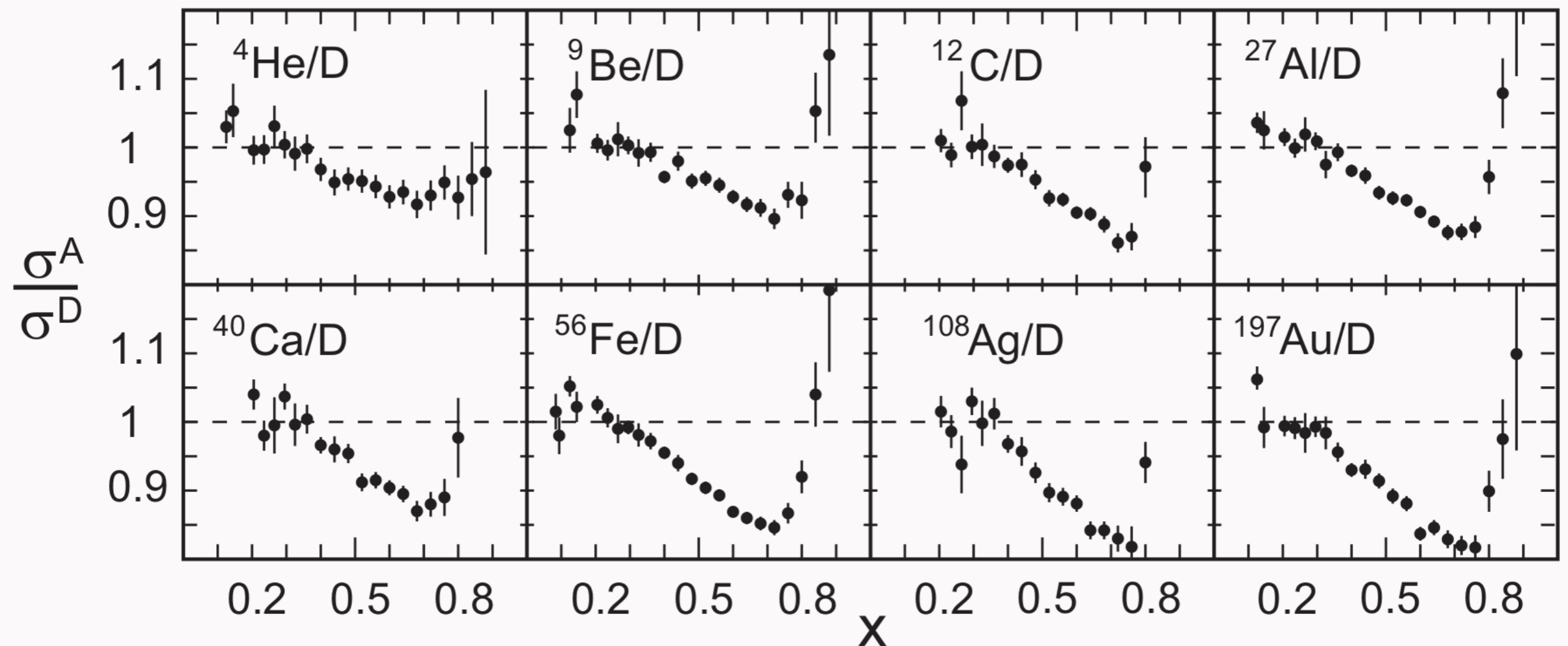
$$dR_{\text{EMC}}(A, x)/dx|_{0.35 < x < 0.7} \sim d(\sigma^A / \sigma^d) / dx|_{0.35 < x < 0.7}$$





# Some History And Definitions

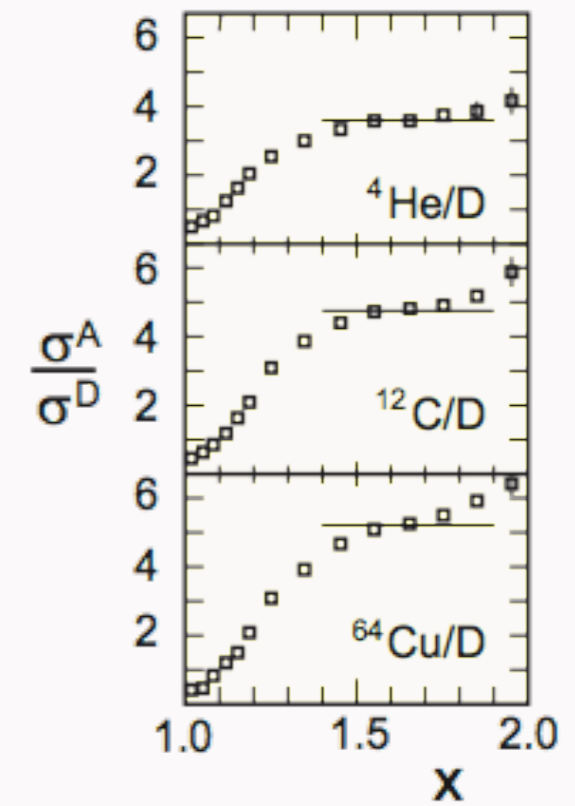
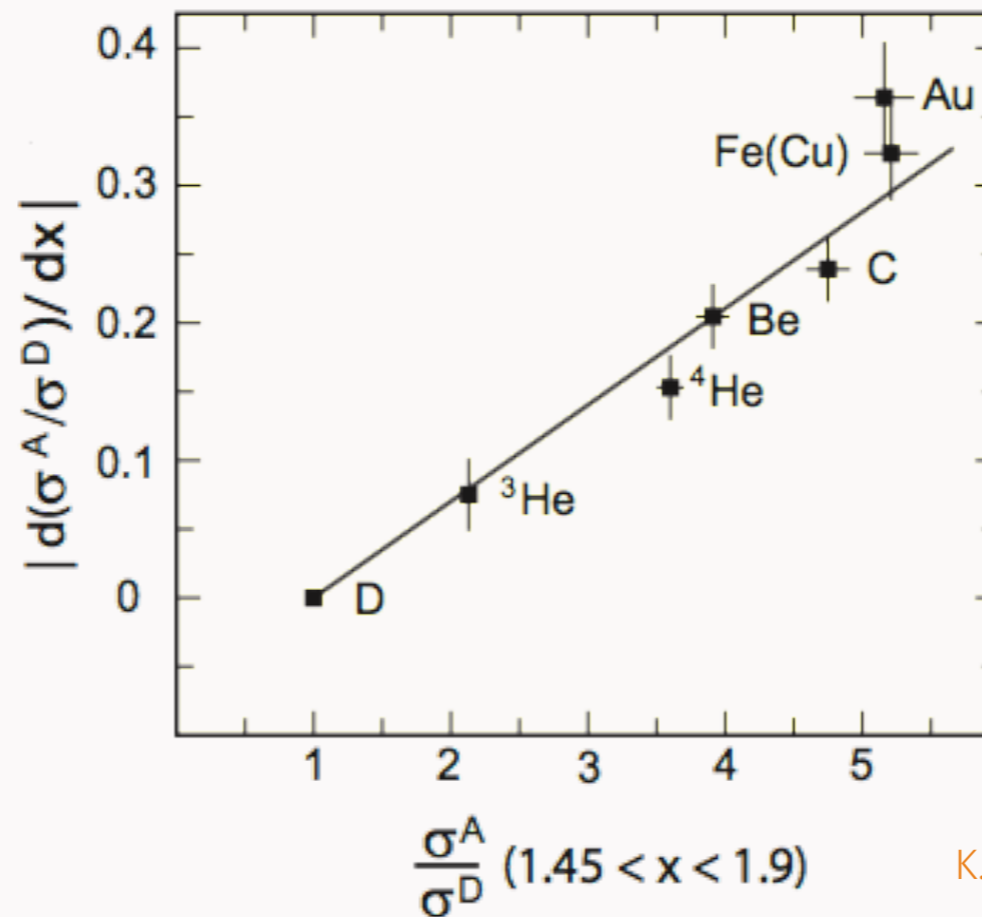
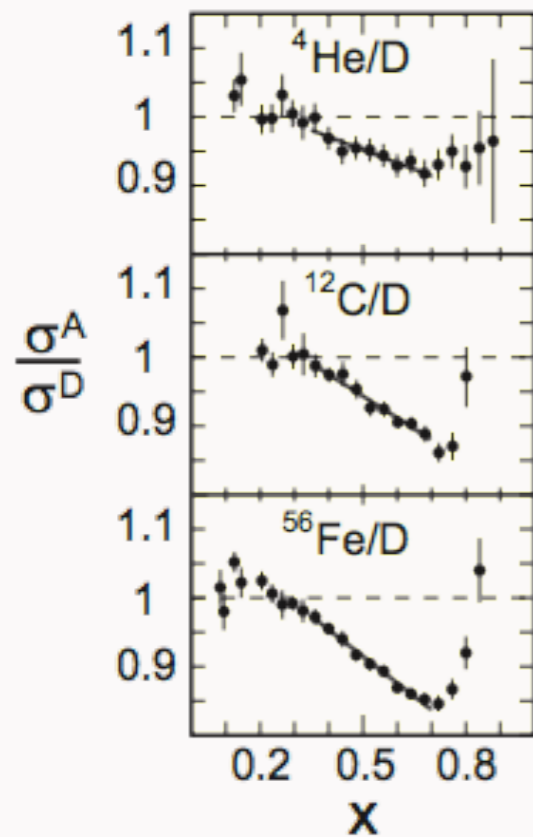
The ratio  $R_{\text{EMC}}(A, x) = \frac{2F_2^A(x, Q^2)}{AF_2^d(x, Q^2)} \sim \frac{2\sigma^A}{A\sigma^d}$  plays an important role.



# Later (~2000 And Beyond) Higher x Data

SRC scaling factor  $a_2(A, x) \equiv \frac{2\sigma^A}{A\sigma^D} \Big|_{1.5 < x < 2}$ .

$dR_{EMC}/dx \propto a_2$



K. Rith, arXiv:1402.5000 [hep-ex] (2014)

# Implications Of EFT

$$Q \gg \Lambda \gg P$$

J.-W. Chen & W. Detmold, Phys. Lett. B **625**, 165 (2005):

Structure functions factorize:  $F_2^A(x)/A = F_2^N(x) + g_2(A, \Lambda)f_2(x, \Lambda)$

$$g_2(A, \Lambda) = \frac{1}{A} \langle A | (N^\dagger N)^2 | A \rangle_\Lambda$$

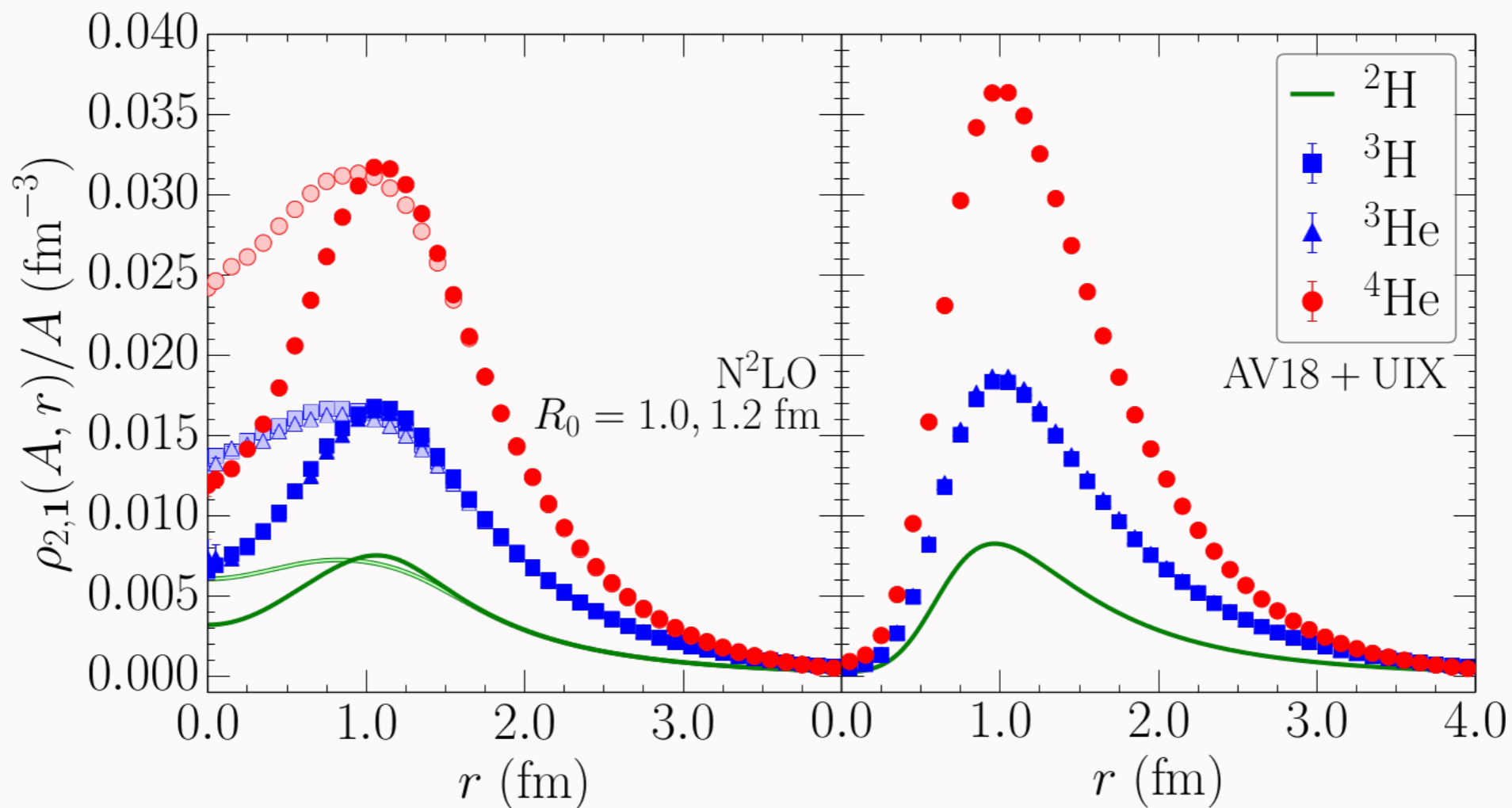
J.-W. Chen, W. Detmold, JEL, A. Schwenk,  
PRL **119**, 262502, (2017):

$$a_2(A, x > 1) = \frac{g_2(A, \Lambda)}{g_2(2, \Lambda)} \Rightarrow \frac{dR_{\text{EMC}}}{dx} \propto a_2.$$

# Two-Body Distribution Functions ( $g_2$ )

$$g_2(A, \Lambda) = \rho_{2,1}(A, r=0)/A, \quad \rho_{2,1}(A, r) \equiv \frac{1}{4\pi r^2} \langle \Psi_0 | \sum_{i < j} \delta(r - r_{ij}) | \Psi_0 \rangle$$

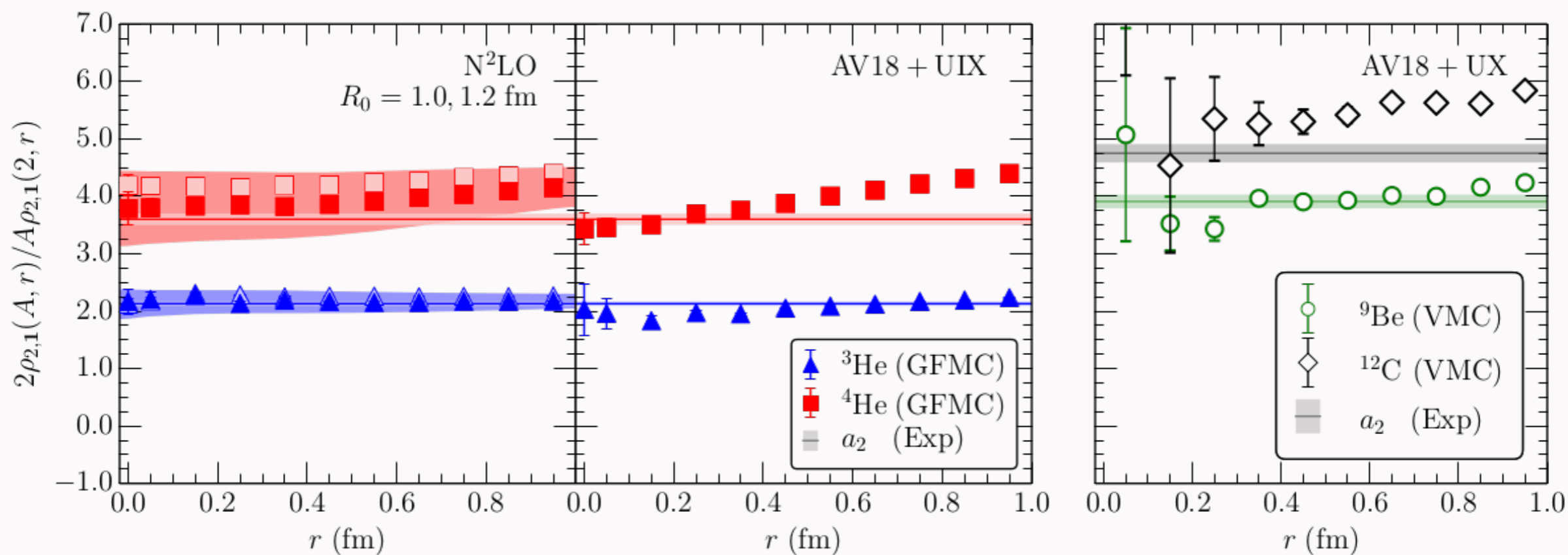
Scale and scheme dependent



# SRC Factors

$$a_2 \equiv \lim_{r \rightarrow 0} \frac{2\rho_{2,1}(A, r)}{A\rho_{2,1}(2, r)}$$

Scale and scheme *independent!*



# SRC Factors

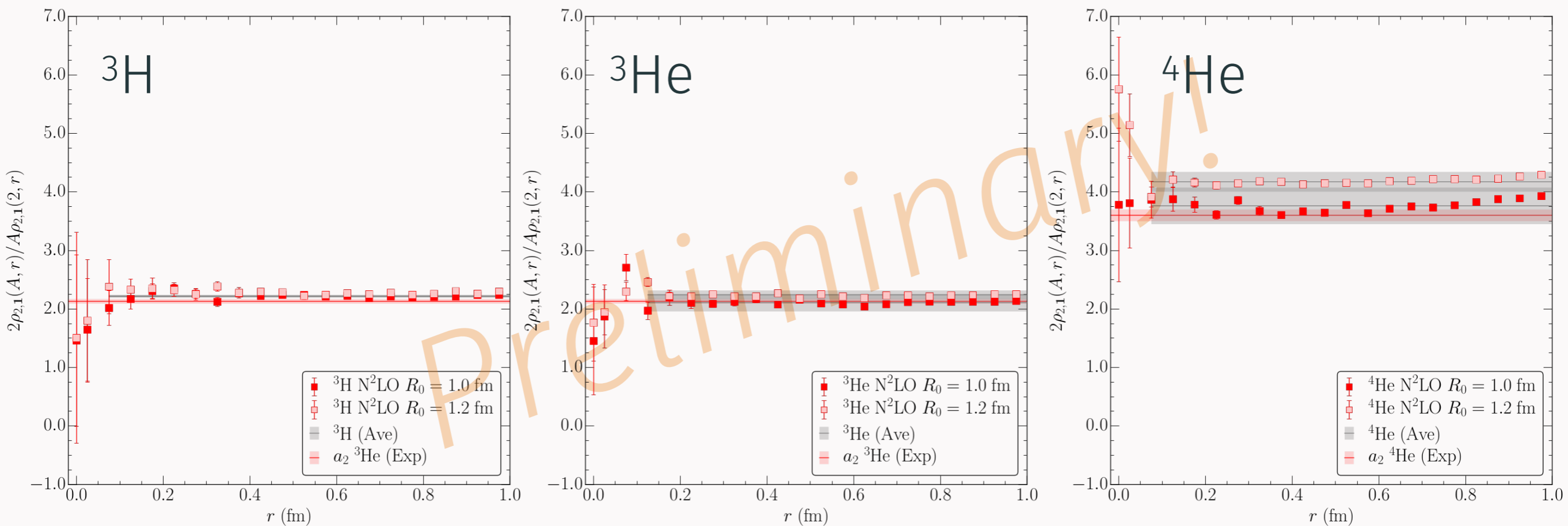
Detailed comparison of experiment and theory

	$N^2LO (R_0 = 1.0 - 1.2 \text{ fm})$	AV18+UIX	Exp
$^3\text{H}$	2.1(2) – 2.3(3)	2.0(4)	
$^3\text{He}$	2.1(2) – 2.1(3)	2.0(4)	2.13(4)
$^4\text{He}$	3.8(7) – 4.2(8)	3.4(3)	3.60(10)

# SRC Factors From AFDMC

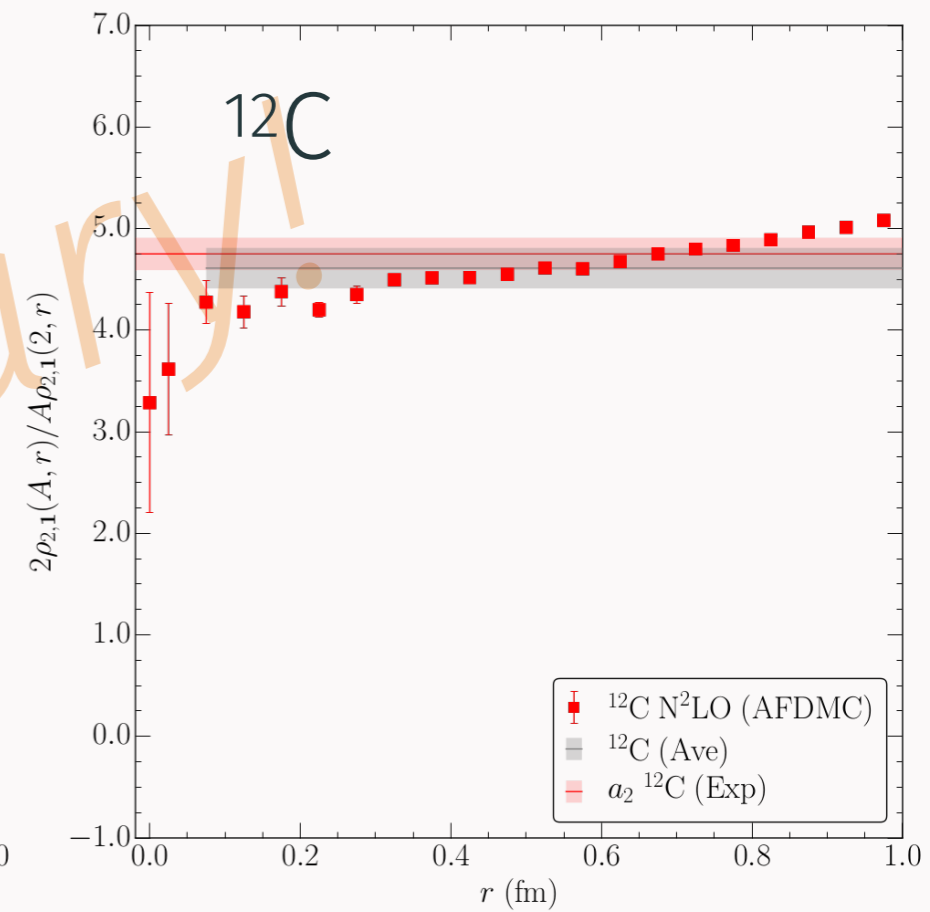
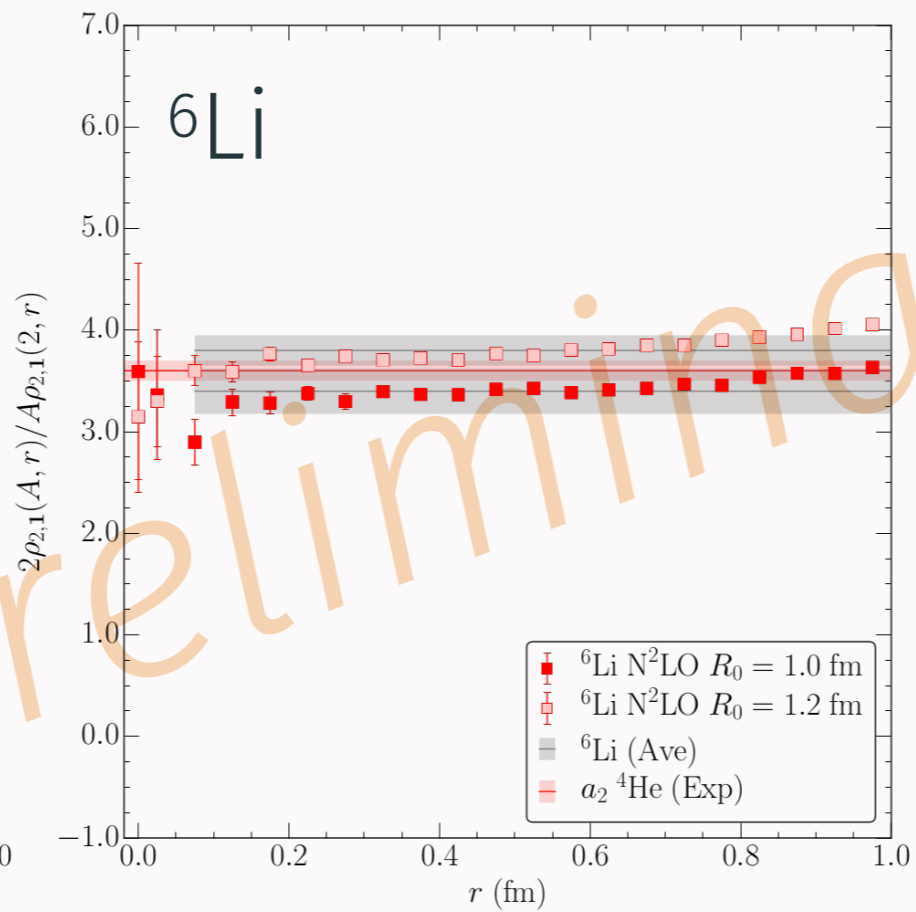
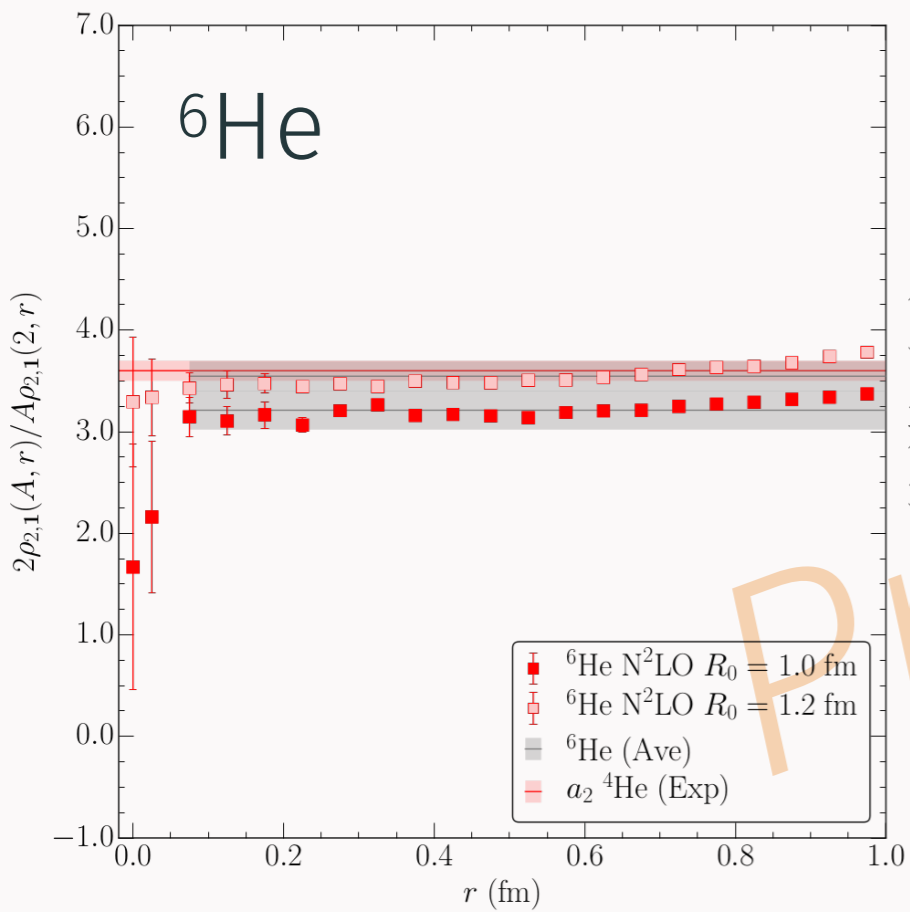
$$a_2 \equiv \lim_{r \rightarrow 0} \frac{2\rho_{2,1}(A, r)}{A\rho_{2,1}(2, r)}$$

Values extracted for  $a_2$  identical to GFMC results.



# SRC Factors From AFDMC

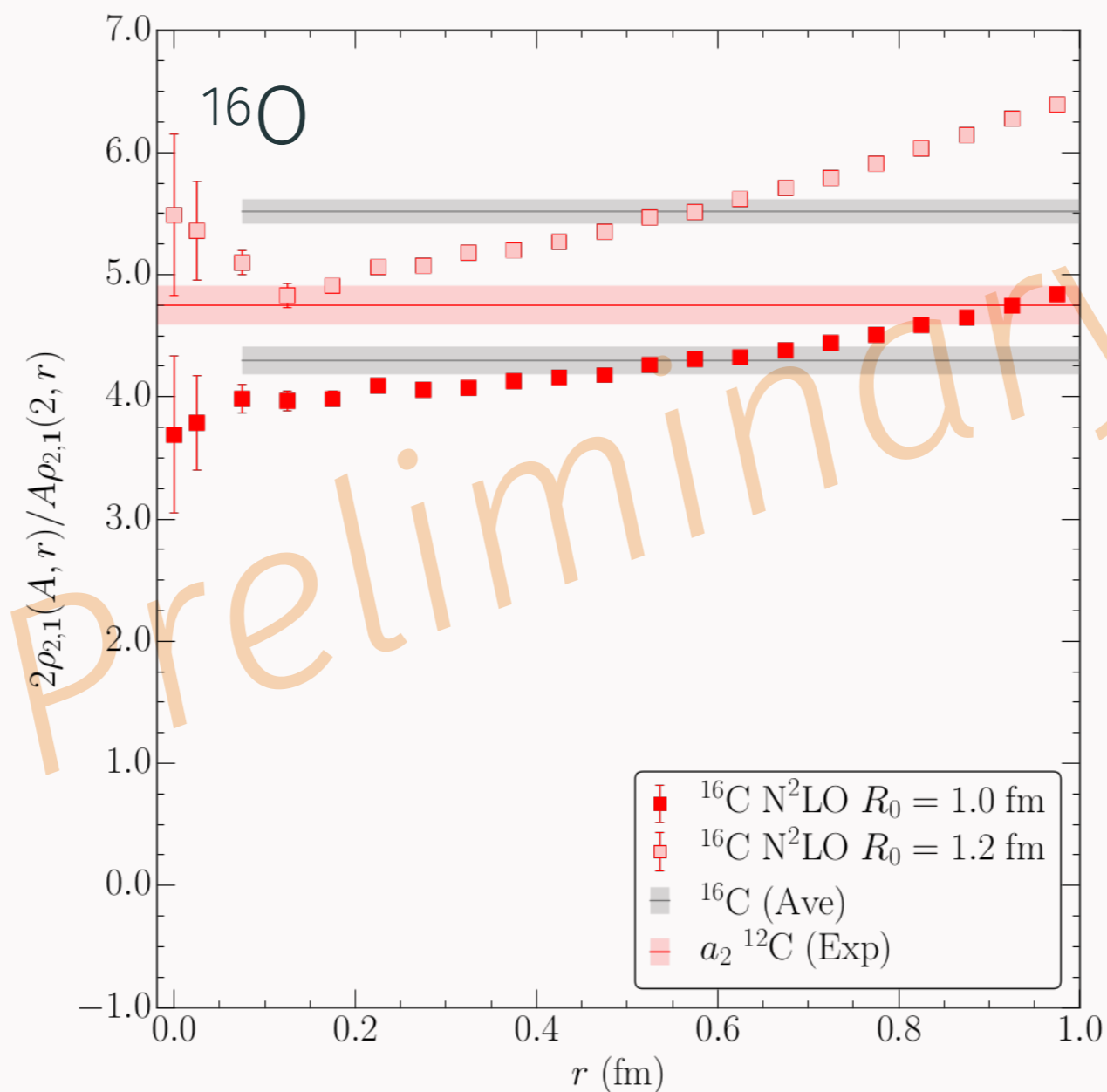
$$a_2 \equiv \lim_{r \rightarrow 0} \frac{2\rho_{2,1}(A, r)}{A\rho_{2,1}(2, r)}$$





# SRC Factors From AFDMC

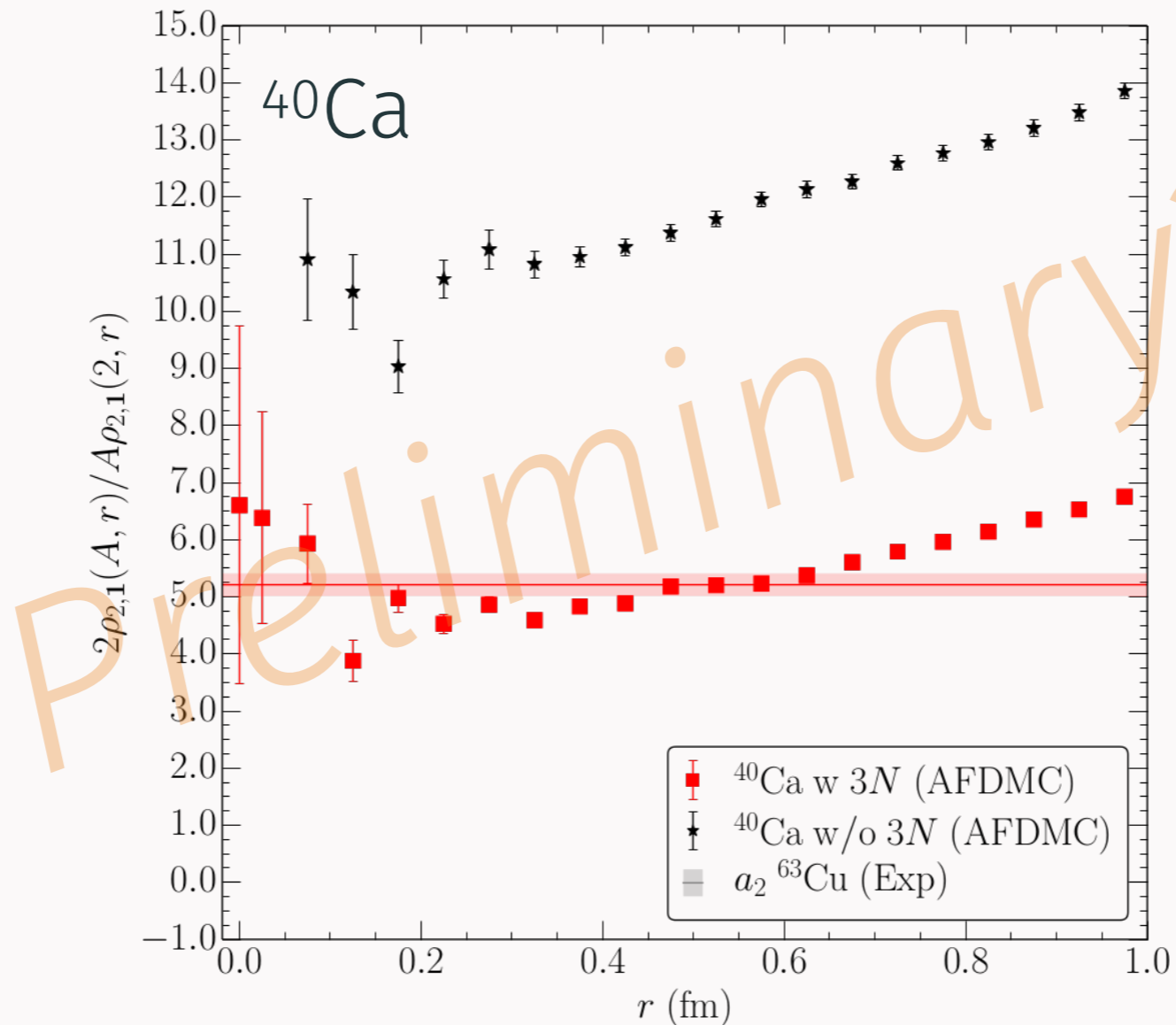
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# SRC Factors From AFDMC

$$a_2 \equiv \lim_{r \rightarrow 0} \frac{2\rho_{2,1}(A, r)}{A\rho_{2,1}(2, r)}$$

$^{40}\text{Ca}$  w/simplified interaction:  $a_2$  saturates as expected.



# SRC Factors From AFDMC

$$a_2 \equiv \lim_{r \rightarrow 0} \frac{2\rho_{2,1}(A, r)}{A\rho_{2,1}(2, r)}$$

	N <sup>2</sup> LO ( $R_0 = 1.0 - 1.2$ fm)	Exp.*
<sup>3</sup> H	2.2(3) – 2.3(3)	
<sup>3</sup> He	2.1(2) – 2.2(1)	2.13(4)
<sup>4</sup> He	3.8(3) – 4.2(2)	3.60(10)
<sup>6</sup> He	3.2(2) – 3.5(2)	
<sup>6</sup> Li	3.4(2) – 3.8(2)	
<sup>12</sup> C	4.6(2) –	4.75(16)
<sup>16</sup> O	4.3(1) – 4.5(1)	

\*O. Hen, G. A. Miller, E. Piassetzky, L. B. Weinstein, RMP **89**, 045002 (2017)

*Preliminary!*

# Summary

- **QMC methods + chiral EFT**: A powerful combination.
- EFT predicts (postdicts) the linear relationship between  $R_{EMC}$  and  $a_2$ .
- Two-body distributions are **scheme and scale dependent**, but ratios are **observable**.
- Our results for  $a_2$  seem to depend on the inclusion of  $3N$  interactions.
- EFT can shed light on the existence of  $a_3$  or the isospin dependence of the EMC effect.
- Values for  $a_2$  might provide an **uncorrelated observable** for fitting nuclear interactions.

# Acknowledgments

## Collaborators

- J. Carlson,  
S. Gandolfi,  
D. Lonardoni



- A. Schwenk



- I. Tews



- J.-W. Chen



- A. Gezerlis



- K. E. Schmidt



- W. Detmold



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**Thank you for your attention!**