

Complementary probes of the nuclear continuum

Karsten Riisager

Aarhus University

March 8, 2018

Resonance characteristics

Classical concept from mechanics, electrical circuits . . .

Here: quantum mechanical system in the continuum

- Wavefunction amplitude inside/outside nucleus
- Time delay between incoming/outgoing wave packets
- Breit-Wigner energy distribution
- Complex eigen-energy $E_0 + i\Gamma/2$
- Pole in S-matrix

All of these become problematic (at least when we wish to relate the concept to experimental data) when resonances become broader

A schematic model

p-wave neutrons in square well potential (radius a)

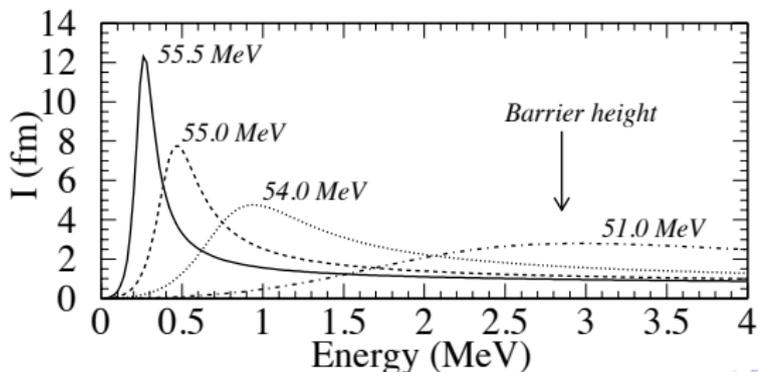
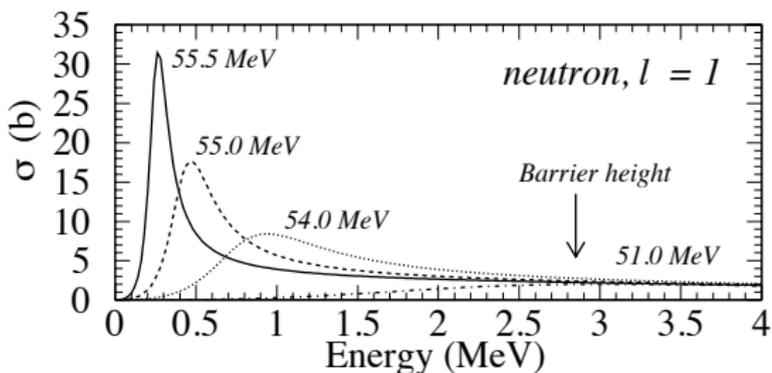
Simple system displaying resonances, almost analytical ($j_\ell(kr)$, $y_\ell(kr)$)

Easy to find phase shift δ_ℓ , this gives elastic scattering cross section

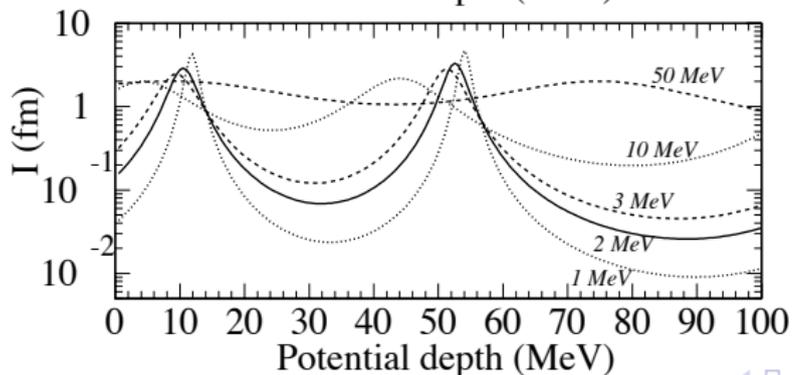
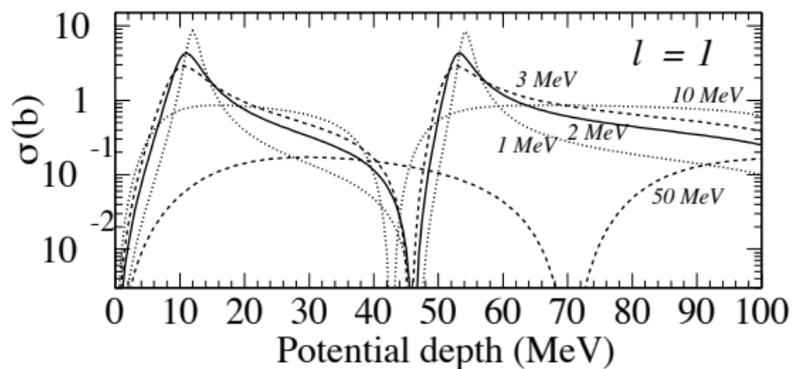
Chose wavefunction normalization as $\sin(kr + \delta_\ell - \ell\pi/2)/r$ for large radii r

For comparison, look also at integral $I = \int_0^a |R(r)|^2 r^2 dr$

Elastic scattering vs. overlap



Elastic scattering vs. overlap



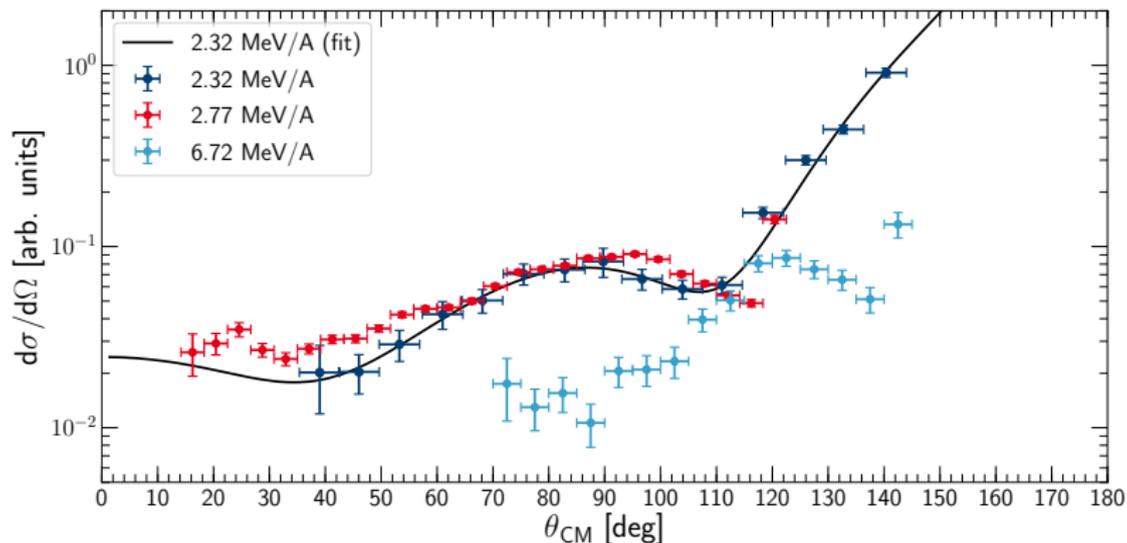
Resonance position

Different ways to define the position of a resonance

- The maximum elastic cross section
- The maximum of I (essentially identical to σ_{el})
- Phase shift passes $\pi/2$ ($|e^{2i\delta_\ell} - 1|$ maximal)
- R-matrix: $E_0 + \Delta - E = 0$, or (equivalently) δ_R through $\pi/2$ where $\delta_\ell = \phi_\ell + \delta_R$, ϕ_ℓ hard sphere phase shift
- Maximum in other observables - transfer cross section, beta-delayed particle spectrum ...

The broader the resonance, the larger the discrepancy in definitions

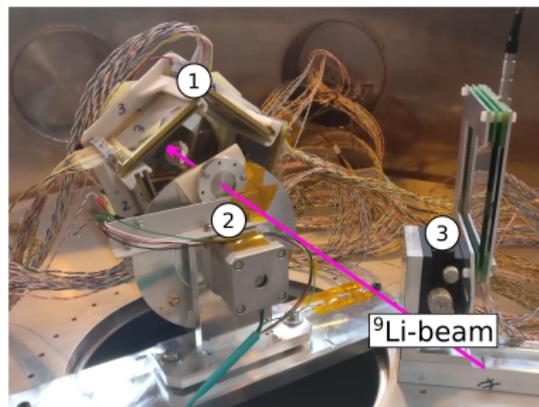
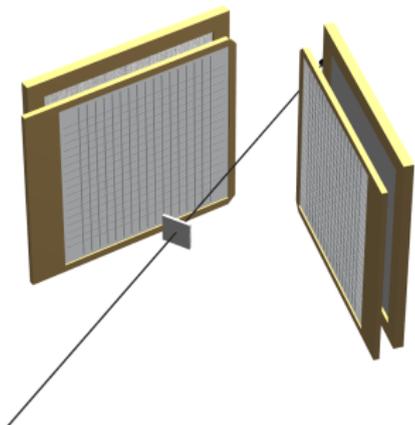
Example

 ^9Li elastic scattering on d

Jesper H Jensen

^9Li set-ups at REX/HIE-ISOLDE

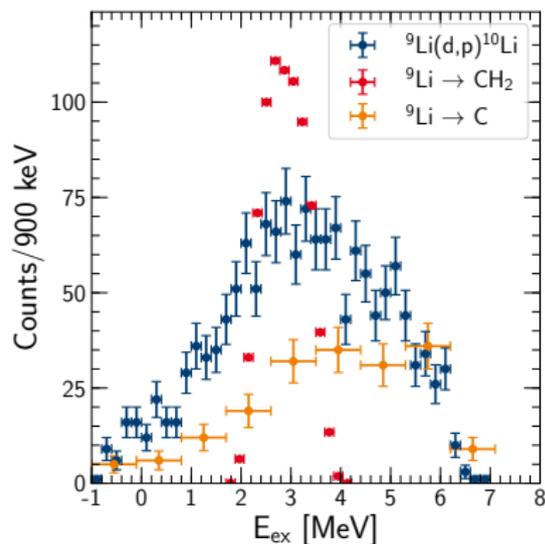
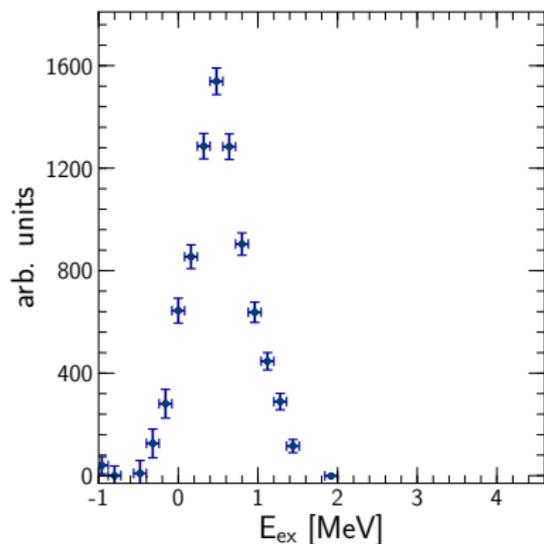
IS367 at 2.77 MeV/u and **IS561** at 6.72 MeV/u



Example

 $^9\text{Li}(d,p)$

Comparing data at 2.77 MeV/u and 6.72 MeV/u



Reminder on beta-decay

$$\beta^- \text{ decay: } {}^A Z \rightarrow {}^A (Z + 1) + e^- + \bar{\nu}_e$$

Two categories, Fermi and Gamow-Teller

type	$S_{e\nu}$	main strength	sum rule
F	0	IAS	$\sum B_F = Z - N $
GT	1	GTGR	$\sum B_{GT} = 3 N - Z $

For neutron-rich nuclei: only expect Gamow-Teller transitions

Beta strength in the continuum

Several earlier definitions, not internally consistent.

For broad resonances: R-matrix parameter squared (a la Γ), but for interfering levels no direct coupling to spectra.

Studies of sum rules by Bergman [Phys Lett B44 \(1973\) 23](#) and Romo [Nucl Phys A237 \(1975\) 275](#): will work with pure continuum and can be reformulated to include resonances.

This implies the GT sum rule remains valid with a continuum formulation:

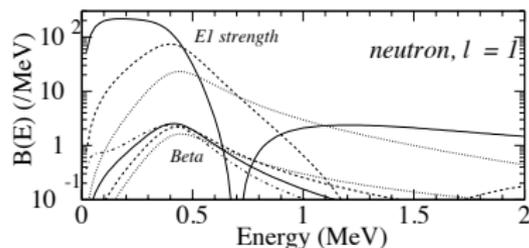
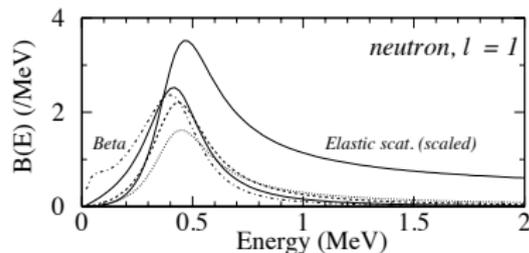
$$w(E)dE = \ln 2 \frac{g_A^2}{K} f(Q - E) B_{GT}(E) dE$$

Also makes life easier for the experimentalist. . .

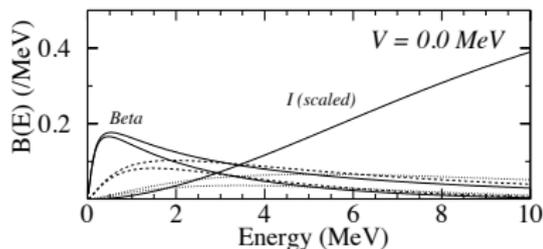
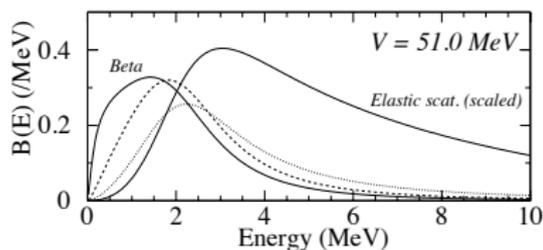
(Broad) resonances and beta-decay

Continue with the schematic model and “beta decay in the core”, i.e. simple overlap of neutron initial and final wavefunctions

- Initial p-wave halo neutron
- Binding energy 5, 1, 0.2, 0.02 MeV (dot, dash, solid, dash-dot)
- Final state p-wave neutron
- Square well, calculate also scattering + E1-strength
- The “resonance” changes shape and position



More extreme conditions:



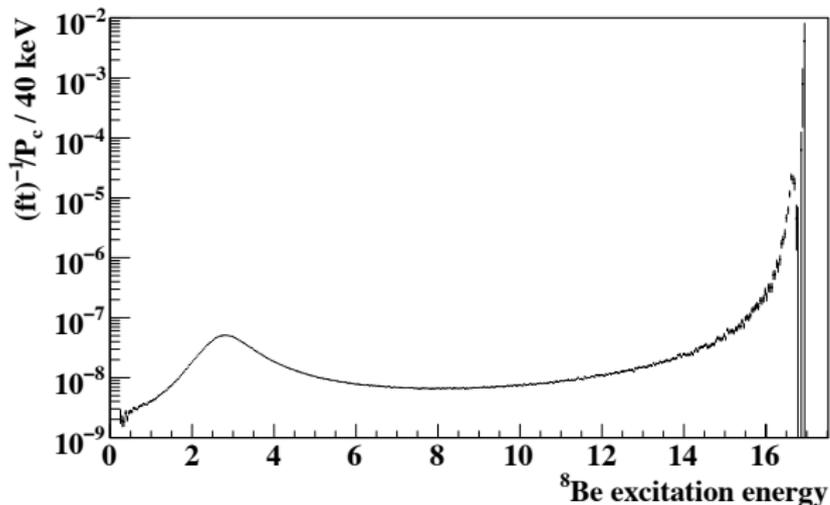
Contributions from extra-nuclear distances affect the shape.

Could be interpreted as decay directly to continuum states.

In general both direct and resonant contributions. Not wise to attempt a separation of the two.

E1-strength: similar, but more extreme.

Results for ^8B beta decay

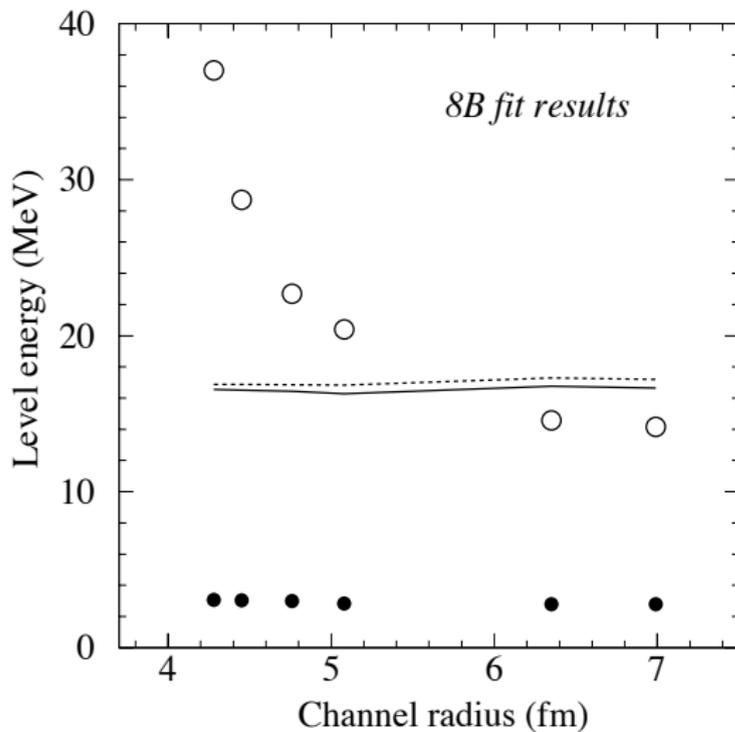


$^8\text{B} \xrightarrow{\beta} ^8\text{Be}^* \rightarrow 2\alpha$, corrected for beta phase space and penetrability factor

Results for ^8B beta decay

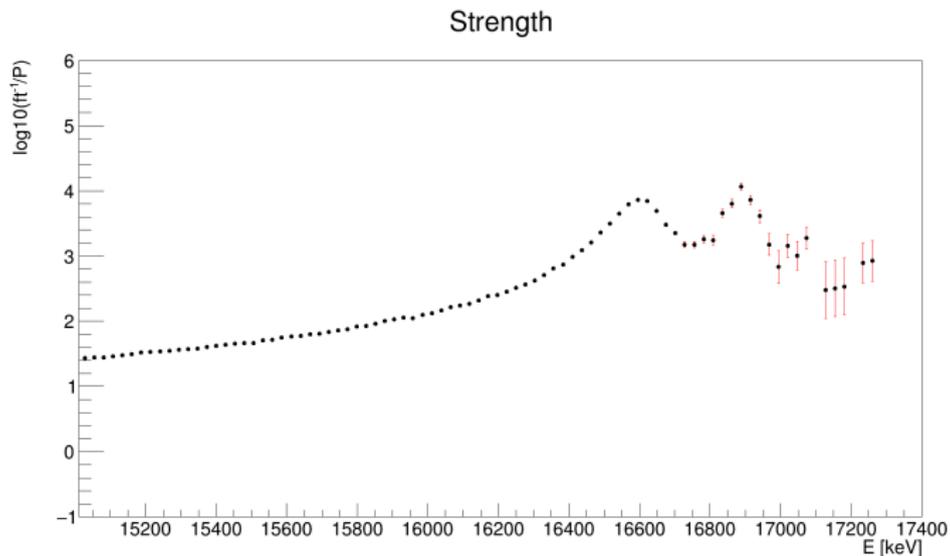
Previously established levels are stable.
 “Intruder” decreases strongly with channel radius.

Decays directly to continuum ?
 $^8\text{Be}(2^+)$ changing structure ?



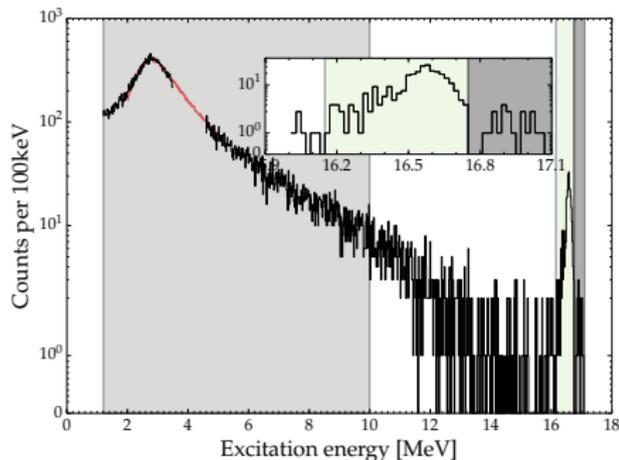
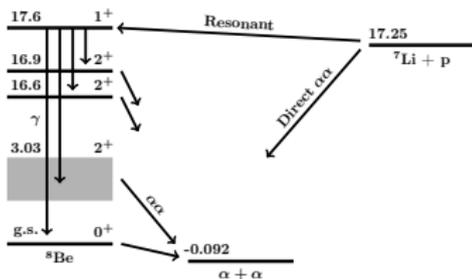
2017 ^8B decay experiment

16.6 +
16.9 MeV
doublet



A Gad and S Vinals

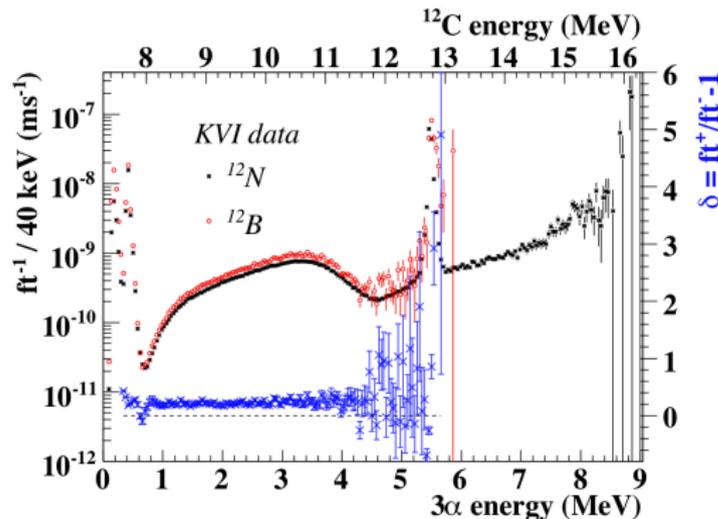
Examples

2018: ^8Be fed via gammas

M Munch et al., submitted - $^7\text{Li}(p,\gamma)\alpha\alpha$
 arXiv:1802.10404

Results for ^{12}N beta decay

Also effects in ^{12}N decay:
 Unphysical parameters if upper end is described with resonances.
 Similar effects seen in the model case.



S. Hyldegaard

Summary of main halo features

Adhere to: [A.S. Jensen et al., Rev. Mod. Phys. 76 \(2004\) 215](#)

Overview in: [K. Riisager, Phys. Scr. T152 \(2013\) 014001](#)

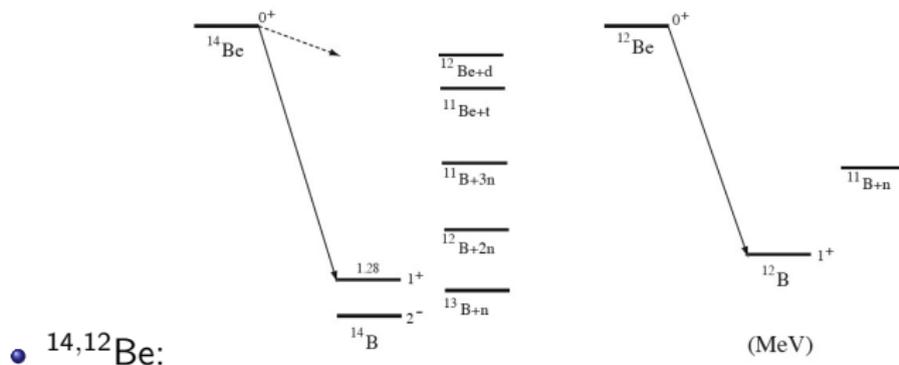
- Quantum system ! Tunneling into classically forbidden regions
- “Single-particle behaviour” \Rightarrow require clustering
- “Large” system – tunneling out of short-range potential
- In nuclei: mainly one- and two-neutron ground state halos
- Example 1n halos: ^{11}Be , $^{15,19}\text{C}$, ^{31}Ne
- Example 2n halos: ^6He , ^{11}Li , ^{14}Be , ^{22}C

Also: [I. Tanihata et al., Prog. Part. Nucl. Phys. 68 \(2013\) 215](#)

[T. Frederico et al., Prog. Part. Nucl. Phys. 67 \(2012\) 939](#)

Halo signatures in beta decay

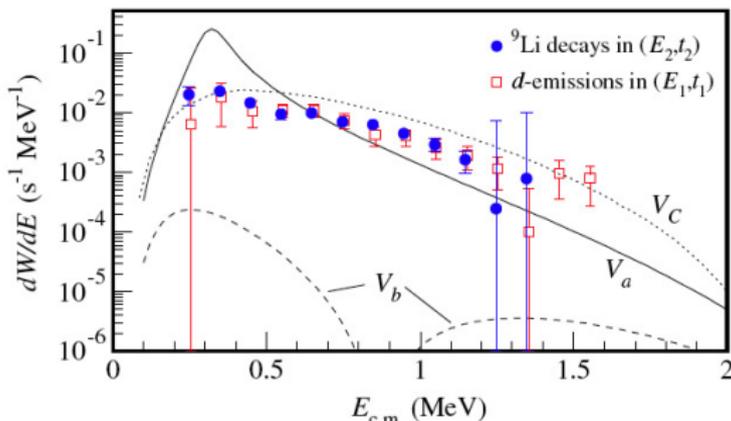
- Change in spatial overlap — moderate effect
- $\mathcal{O} | c + h \rangle = (\mathcal{O} | c \rangle) | h \rangle + | c \rangle (\mathcal{O} | h \rangle)$
- Decoupling of halo and core decays ?
 - Isospin symmetry ?
 - $\beta d, \beta p \dots$



- Useful spectroscopic information on halo composition, ^{11}Li

Beta-delayed deuteron emission – ^{11}Li

Halo specific decay mode - seen in ^6He and ^{11}Li
 Decays directly to continuum

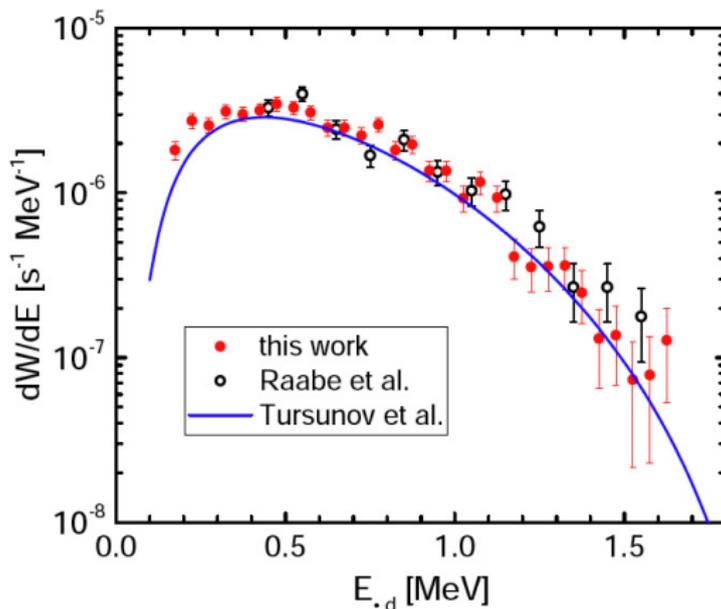


R. Raabe et al.,
 PRL 101 (08) 212501

Potential model calculations by Zhukov et al., PR C52 (95) 2461 (V_C , only Coulomb) and Baye et al., PR C74 (06) 064302 (V_a, V_b)

...and for ^6He

Several experiments, the latest with an OTPC:



M. Pfützner et al.,
 PR C92 (15) 014316
 Tursunov, Baye,
 Descouvemont,
 PR C97 (18) 014302

What about $^{11}\text{Be}(\beta p)$?

One-neutron system simpler to interpret than two-neutron system.
 However $Q_{\beta p} = 782 \text{ keV} - S_n$ vs $Q_{\beta d} = 3007 \text{ keV} - S_{2n}$!

^{11}Be the most favourable case [Baye + Tursunov, PL B696 \(11\) 464](#)
 with expected branching ratio 3.0×10^{-8} (F + GT)

Emitted protons have energy below 255 keV \rightarrow detect daughter nucleus ^{10}Be with halflife 1.5 My ?

Detection via Accelerator Mass Spectroscopy ...

What about non- β ^{11}Be decay ?

Bartosz Fornal and Benjamin Grinstein (arXiv:1801.01124):
Neutron decay to dark matter particle ?
(Different lifetime for neutron disappearance and proton appearance.)

Could also happen in nuclei with low separation energy
Marek Pfützner: ^{11}Be the most favourable case (arXiv:1803.01334)

Must compare rates for proton and ^{10}Be production

Proton detection via Warsaw optical TPC

Three attempts

All collections of ^{11}Be done at the ISOLDE facility at CERN.

- September 2001, $5.2(3) \times 10^{11}$ atoms, AMS at Uppsala, “upper limit” of $2.5(2.5) \times 10^{-6}$

M.J.G. Borge et al., *J. Phys. G40* (2013) 035109

- December 2012, 3 samples, $1.47(14) \times 10^{12}$ atoms, AMS at VERA, observation $8.3(9) \times 10^{-6}$

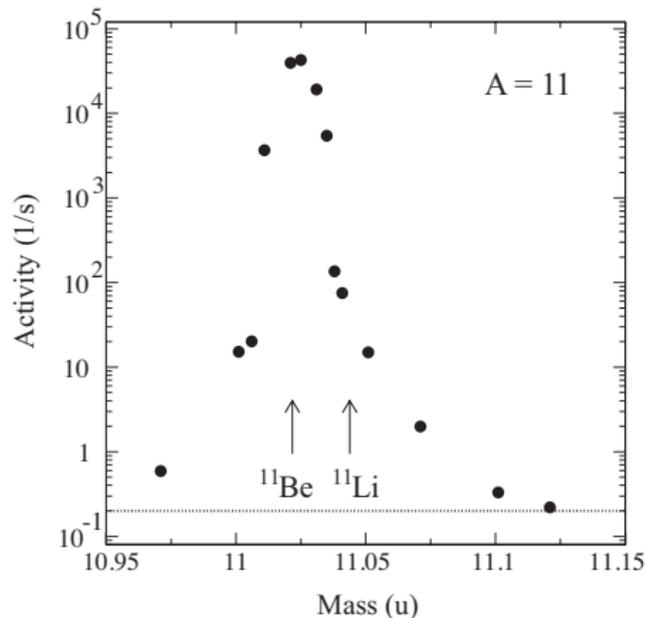
K.R. et al., *Phys. Lett. B732* (2014) 305

- May 2015, 12 samples, up to $2.98(27) \times 10^{11}$ atoms, AMS at VERA

preliminary: slightly inconsistent branching ratio

Experimental details

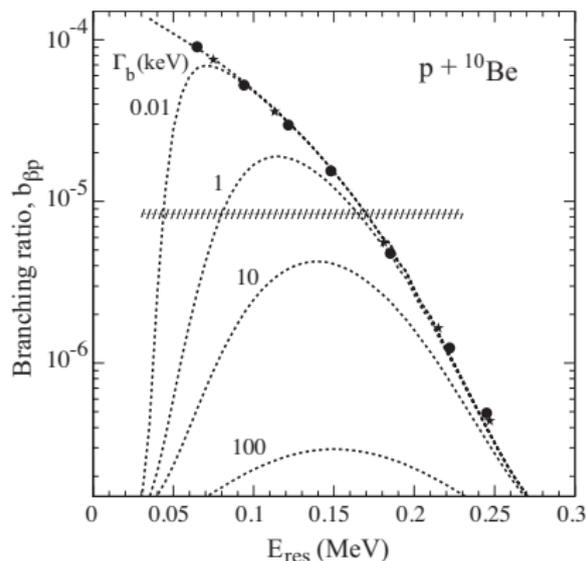
- Signal appears on ^{11}Be mass
- Suppress ^{11}Li contamination
- Signal only with laser ionization (no BeH)
- Normalize via ^{11}Be decay γ -rays



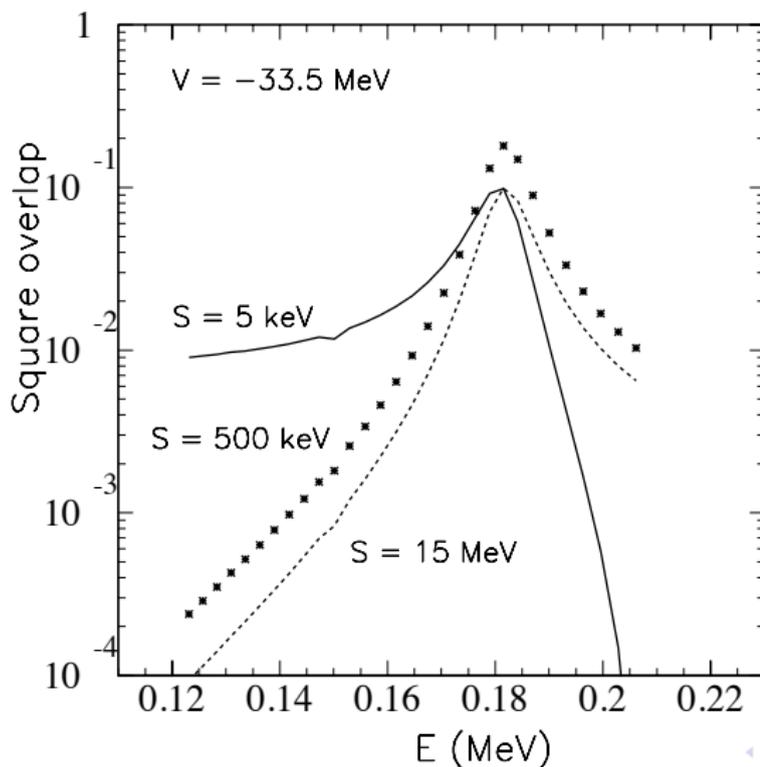
Branching ratio in simple model

Simple model:

- Detached decay of halo neutron
- Simple potential (square well/Woods-Saxon)
- Discretized final state (radius 1000 fm)
- **Need “resonance” to reproduce strength**



Dependence on halo binding energy



Final comments

- Limitations to the resonance concept. . .
- Beta strength in continuum – new definition
- Expect beta decay directly to continuum (at low binding)
- Indications for separate beta decays of core and halo
- **Surprisingly strong** beta strength for $^{11}\text{Be}(\beta\text{p})$, indication of a (so far unseen) resonance ? - or dark decay ?
- For experimentalists: Cannot always trust R-matrix !

$^8\text{B}(\beta\text{p})$? Would be “core decay”, expect branching ratio
 2.3×10^{-8}

Thanks to coworkers:

MAGISOL collaboration + Aksel S. Jensen

Some references

- M.J.G. Borge et al., J. Phys. G40 (2013) 035109 – ^{11}Be
- K.R., Nucl. Phys. A 925 (2014) 112 + Corrigendum N.P.A 925 (2014) 298 – [beta strength](#)
- K.R., H.O.U. Fynbo, S. Hyldegaard, A.S. Jensen, Nucl. Phys. A 940 (2015) 119 – [β to broad resonance](#)
- K.R. et al., Phys. Lett. B732 (2014) 305 – ^{11}Be