

Low-energy corrections to the eikonal description of elastic scattering and breakup of halo nuclei

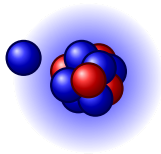
Chloë Hebborn and Pierre Capel

Université libre de Bruxelles

March the 5th 2018

Introduction

- **Halo nuclei** exhibit a very large matter radius
Compact core + one or two loosely-bound neutrons



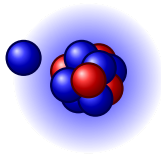
Ex : $^{11}\text{Be} \equiv ^{10}\text{Be} + \text{n}$, $^{15}\text{C} \equiv ^{14}\text{C} + \text{n}$

Short-lived : studied through **reactions processes**
(**elastic scattering, breakup,...**)

⇒ **Need an accurate reaction model to infer reliable information**

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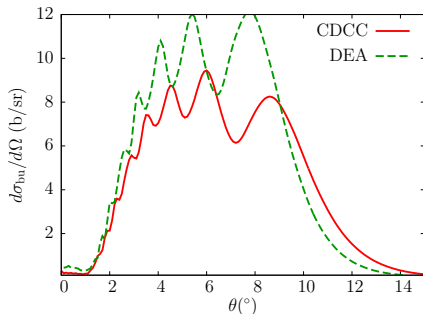
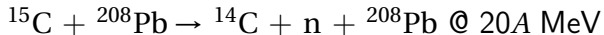
⇒ **Need an accurate reaction model to infer reliable information**

- **The eikonal approximation :**
 - ⊕ reduced computational time
 - ⊕ simple interpretation of the reaction
- Some experimental facilities will provide RIBs at $\sim 10A$ MeV
(e.g. HIE-ISOLDE @ CERN and ReA12 @ MSU)

⇒ **Is it valid at these energies ?**

Introduction

- Coulomb dominated reactions :

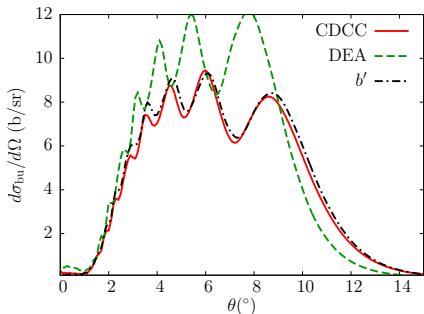
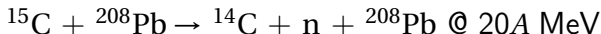


[T. Fukui, K. Ogata and P. Capel. PRC **90**, 034617 (2014)]

Introduction

- **Coulomb dominated reactions :**

Coulomb correction : $b \rightarrow b' = \frac{\eta + \sqrt{\eta^2 + b^2 k^2}}{k} \Rightarrow$ valid at low energies



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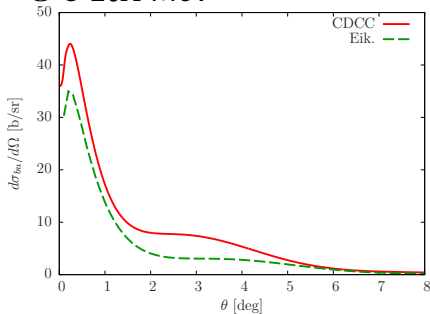
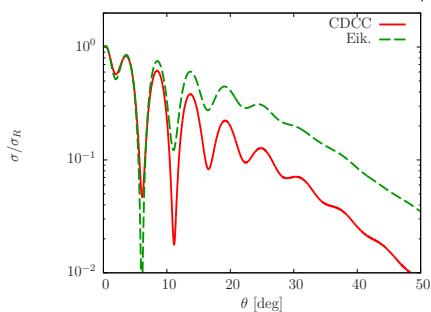
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- **Nuclear dominated reactions :**

$^{11}\text{Be} + ^{12}\text{C} @ 20\text{A MeV}$



- Eikonal overestimates elastic and underestimates breakup
- Eikonal dampens the oscillations

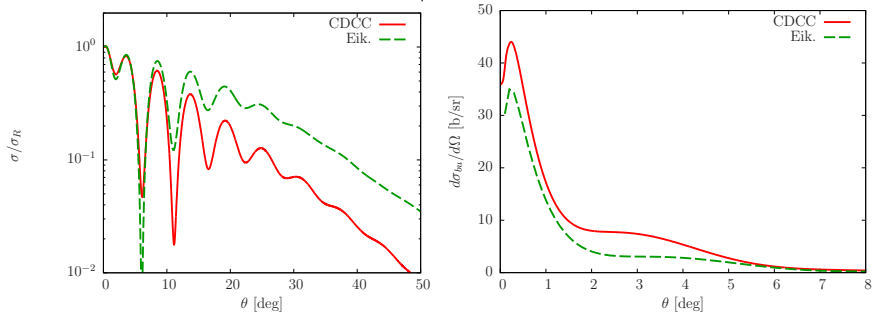
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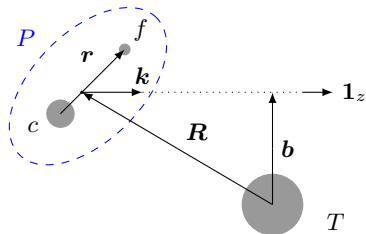
⇒ **Can a nuclear correction fix these issues?**

- 1 Eikonal model
 - Usual eikonal model
 - Dynamical Eikonal Approximation (DEA)
- 2 Semi-classical correction
 - Implementation
 - Elastic scattering @ 10A MeV
 - Generalisation to the DEA
- 3 Exact continued S -matrix correction
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 - Dependence on energy
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Reaction model : three-body collision

Reaction model :

- Assumptions : - Spinless particles
- Central potentials
- Two-body projectile (P) :
 $P \equiv$ core (c) + fragment (f)
Internal Hamiltonian : $h_{cf} = T_r + V_{cf}(r)$
- Structureless target (T)



Three-body Schrödinger equation :

$$[T_R + h_{cf} + V_{cT} + V_{fT}] \Psi(\mathbf{R}, \mathbf{r}) = E \Psi(\mathbf{R}, \mathbf{r})$$

with the initial condition $\Psi(\mathbf{R}, \mathbf{r}) \xrightarrow{Z \rightarrow -\infty} e^{ikZ + \dots} \Phi_0(\mathbf{r})$,

where Φ_0 is the ground state of P : $h_{cf} \Phi_0 = \epsilon_0 \Phi_0$

Three-body Schrödinger equation :

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① **Eikonal approximation** : at high energy, $\Psi \approx$ plane wave (e^{ikZ})

$$\text{Factorization : } \Psi(\mathbf{R}, \mathbf{r}) = e^{ikZ} \hat{\Psi}(\mathbf{R}, \mathbf{r}) \quad \text{with } |\Delta_{\mathbf{R}} \hat{\Psi}| \ll k \left| \frac{\partial}{\partial Z} \hat{\Psi} \right|$$

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Dynamical Eikonal Approximation (DEA) uses only ①

$$\Rightarrow i\hbar v \frac{\partial}{\partial Z} \hat{\Psi}(\mathbf{b}, Z, \mathbf{r}) = [h_{cf} - \epsilon_0 + V_{cT} + V_{fT}] \hat{\Psi}(\mathbf{b}, Z, \mathbf{r}),$$

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② **Adiabatic approximation** : $h_{cf} \approx \epsilon_0$

Usual eikonal model uses ①+② :

$$\Psi^{\text{eik}}(\mathbf{b}, Z, \mathbf{r}) = e^{ikZ} e^{i[\chi_{cT}(b_{cT}) + \chi_{fT}(b_{fT})]} \Phi_0(\mathbf{r}),$$

$$\text{with } \chi_j(b_j) = -\frac{1}{\hbar v} \int_{-\infty}^Z V_j(\mathbf{b}_j, Z') dZ'$$

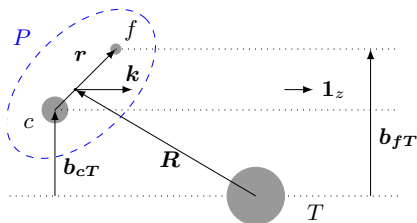
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Eikonal model : three-body collision

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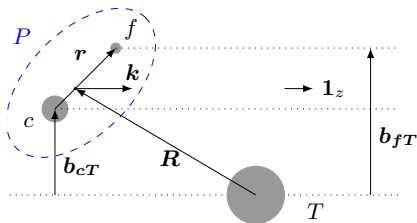
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- ⊖ Deflection and couplings between trajectories are neglected !
- ⊖ Valid only at high energy !

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⇒ Extension to low energies through corrections to account for the deflection of P

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Semi-classical correction

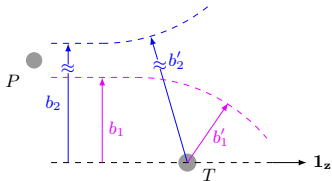
Idea : $\chi_j(b_j) \rightarrow \chi_j(b'_j)$, with b'_j the **complex** distances of closest approach [Analysis of two-body collisions in A. Vitturi *et al.* , PRC **56**, 1511, (1997).]

① Real part of the distances b'_j :

trajectories at b_1 is **nuclear dominated**
at b_2 is **Coulomb dominated**

→ b'_j computed exactly

[CH, P. Capel, *Proc. of the 55th International Winter Meeting on Nuclear Physics*, (2017).]



Semi-classical correction

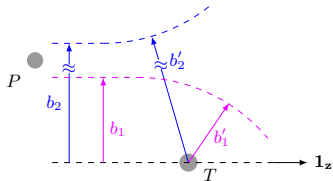
Idea : $\chi_j(b_j) \rightarrow \chi_j(b_j'')$, with b_j'' the **complex** distances of closest approach [Analysis of two-body collisions in A. Vitturi *et al.* , PRC **56**, 1511, (1997).]

① Real part of the distances b_j' :

trajectories at b_1 is **nuclear dominated**
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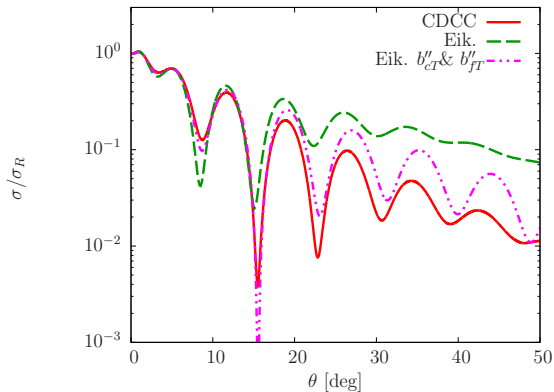
② Complex distances b_j'' :

→ b_j'' approximated by a **perturbation formula**

$$b_j'' = b_j' - i \frac{\text{Im}\{V_j(b')\}}{2 E_0 \frac{b^2}{b'^3} - \left[\frac{\partial}{\partial r} (\text{Re}\{V_j\}) \right]_{r=b'}}$$

[D. M. Brink, *Semi-classical methods in nucleus-nucleus scattering*, (1985).]

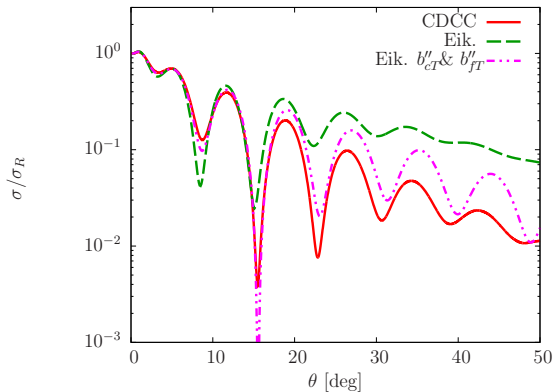
Elastic scattering $^{11}\text{Be}+^{12}\text{C}$ @ 10A MeV



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- ⊕ More absorption at large angles but not enough
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⇒ Influence of the dynamics of the projectile ?

Generalisation of the semi-classical correction to the DEA

DEA : no eikonal phases

⇒ replace b_j by b_j'' in the computation of the interaction

$$V_j(b_j, z) \rightarrow V_j(b_j'', z)$$

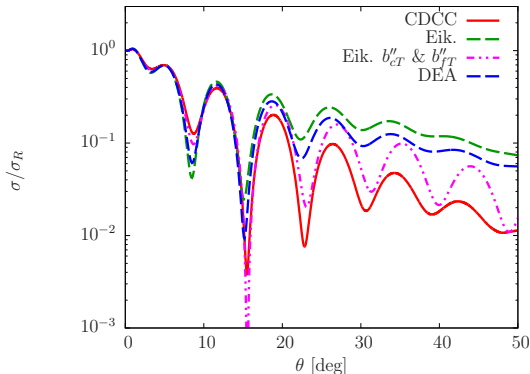
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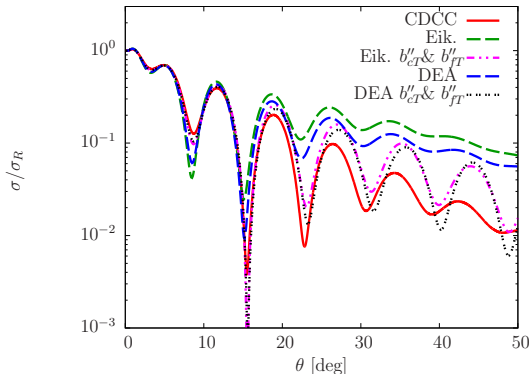
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 - ⊕ Accuracy gain
 - ⊖ Lack of absorption at large θ
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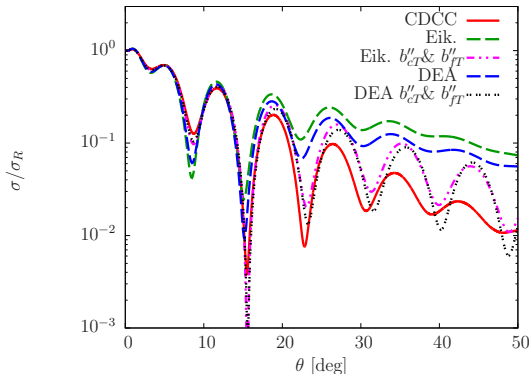
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Exact continued S-matrix : two-body collisions

Two-body collisions :

- Partial-wave expansion : $F(\theta) = \frac{1}{2ik} \sum_{l=0}^{+\infty} (2l+1) P_l(\cos(\theta)) \underbrace{[e^{2i\delta_l} - 1]}_{S_l}$
- Eikonal model : $f(\theta) = -ik \int_0^{+\infty} b J_0(qb) \underbrace{[e^{i\chi(b)} - 1]}_{S(b)} db$
- Relation between Legendre polynomial and Bessel function :

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→ **Exact continued S-matrix :**

use the exact S_l in the eikonal framework using $l = kb - 1/2$

$$\bar{f}(\theta) = -ik \int_0^{+\infty} b J_0(qb) [S_l - 1] db$$

[J. M. Brooke *et al.* , PRC **59**, 1560, (1999).]

Generalisation to three-body collisions :

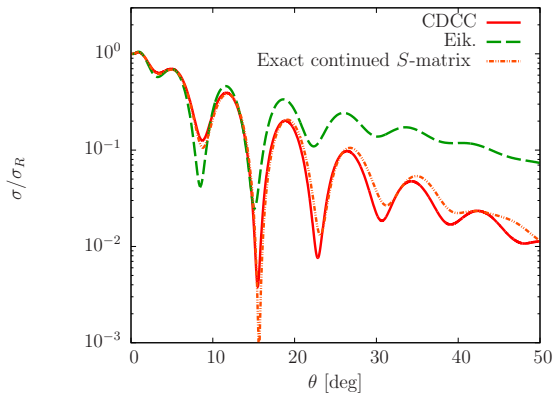
- Eikonal model : $f^{(2)}(\theta) = -ik \int_0^{+\infty} b db J_0(qb) [S^{(2)}(b_{cT}, b_{fT}) - 1]$
with $S^{(2)}(b_{cT}, b_{fT}) = \langle \Phi_0 | S(b_{cT}) S(b_{fT}) | \Phi_0 \rangle$
- **Exact continued S-matrix :**

$$\overline{f^{(2)}}(\theta) = -ik \int_0^{+\infty} b J_0(qb) [S_{l_c, l_f}^{(2)} - 1] db$$

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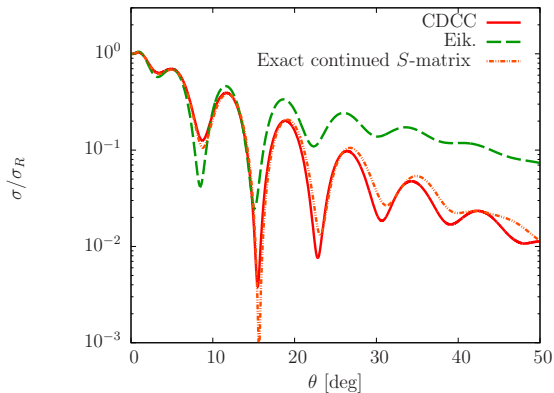
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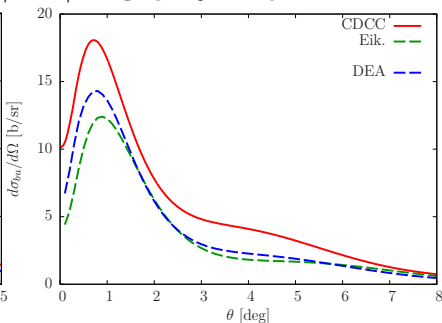
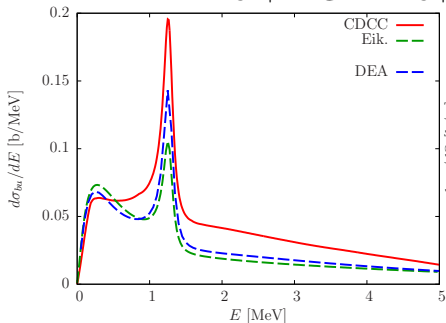
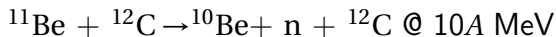
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What about breakup observables ?

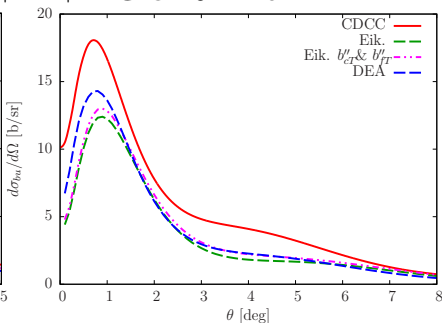
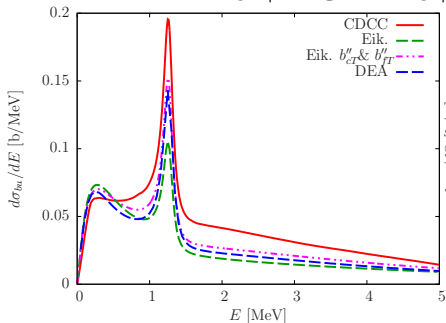
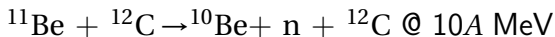
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Extension to breakup reactions



Small dynamical effects in breakup cross sections

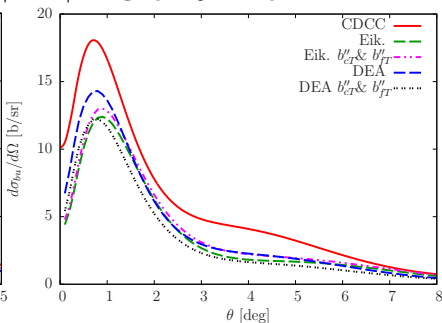
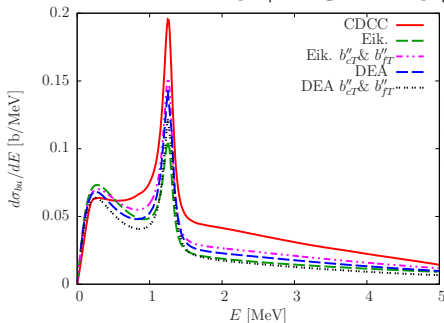
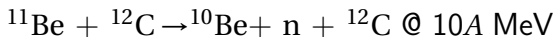
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Small dynamical effects in breakup cross sections

① **Semi-classical correction** : small correction to the eikonal model

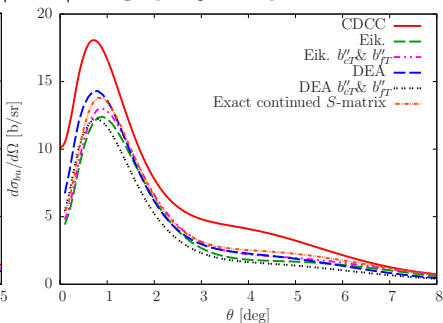
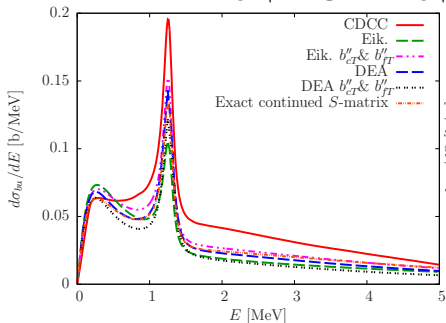
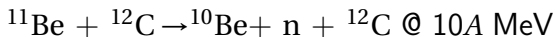
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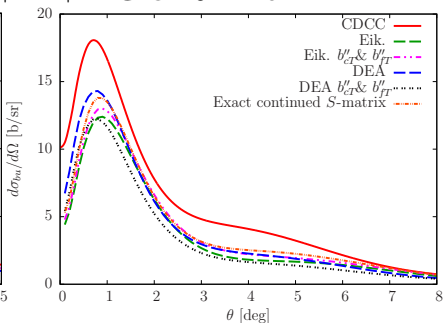
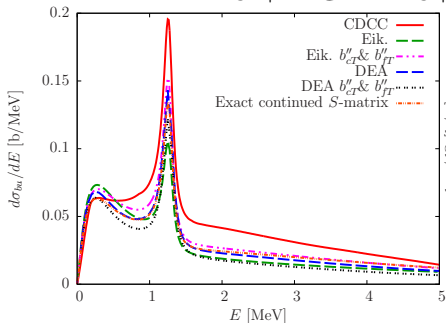
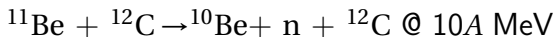
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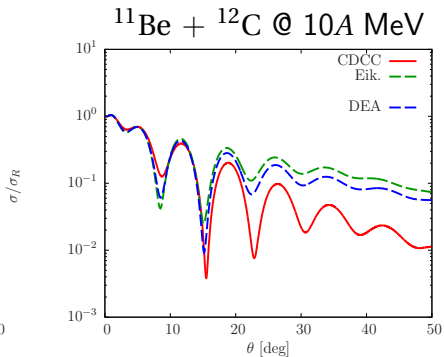
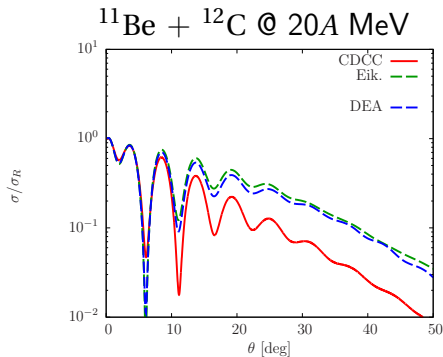
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but is as accurate as the DEA

How do both corrections vary with energy ?

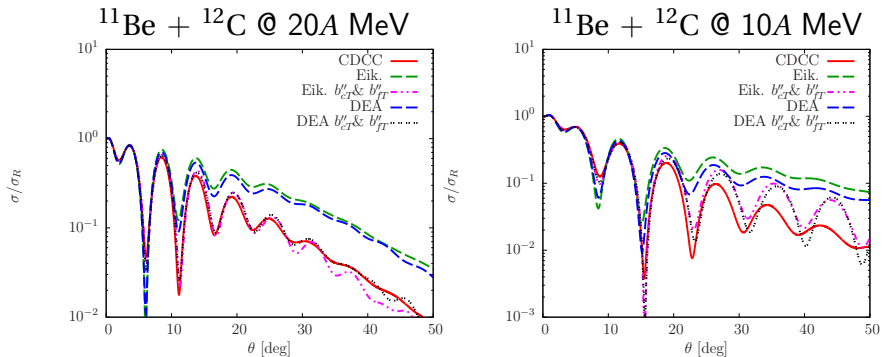
How sensitive are they to the potential parameters ?

- 1 Eikonal model
 - Usual eikonal model
 - Dynamical Eikonal Approximation (DEA)
- 2 Semi-classical correction
 - Implementation
 - Elastic scattering @ 10A MeV
 - Generalisation to the DEA
- 3 Exact continued S -matrix correction
 - Implementation
 - Elastic scattering @ 10A MeV
- 4 Extension to breakup
- 5 Sensitivity analyses of both corrections
 - Dependence on energy
 - Sensitivity to the potentials
- 6 Summary

Dependence on energy : elastic scattering

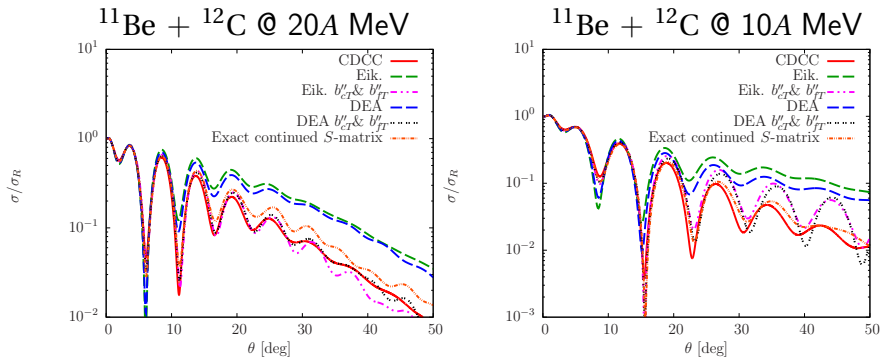


Dependence on energy : elastic scattering



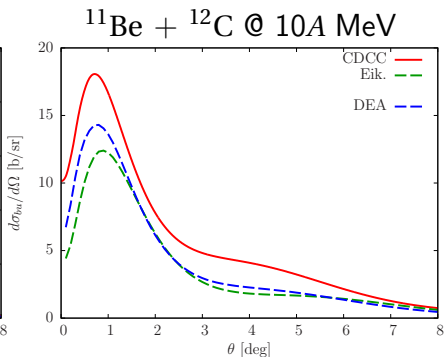
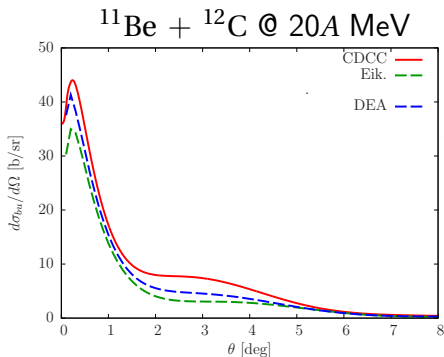
- ① **Semi-classical correction** : more efficient at high energy
Same accuracy in the eikonal model or the DEA

Dependence on energy : elastic scattering



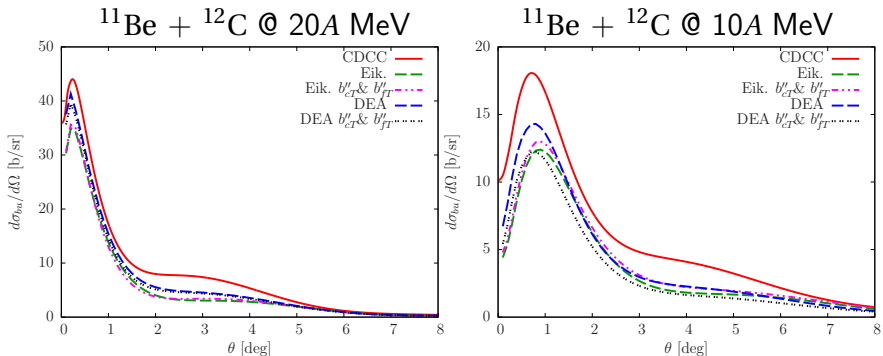
- ① **Semi-classical correction** : more efficient at high energy
Same accuracy in the eikonal model or the DEEA
- ② **Exact continued S -matrix** : more efficient at low energy

Dependence on energy : breakup



- Dynamical effects more important at lower energies

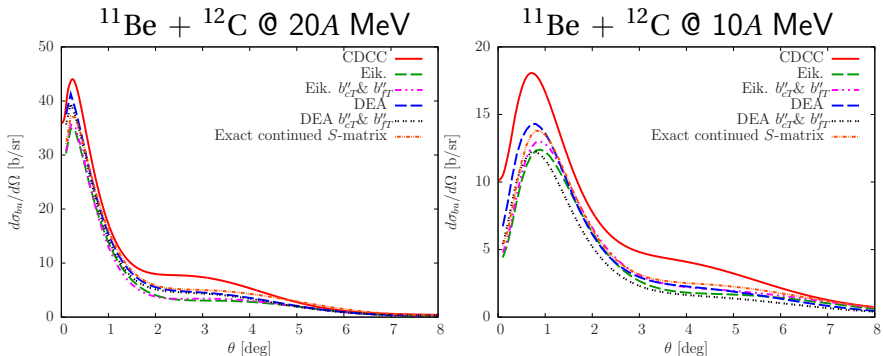
Dependence on energy : breakup



- Dynamical effects more important at lower energies

① **Semi-classical correction : larger effect at low energy**

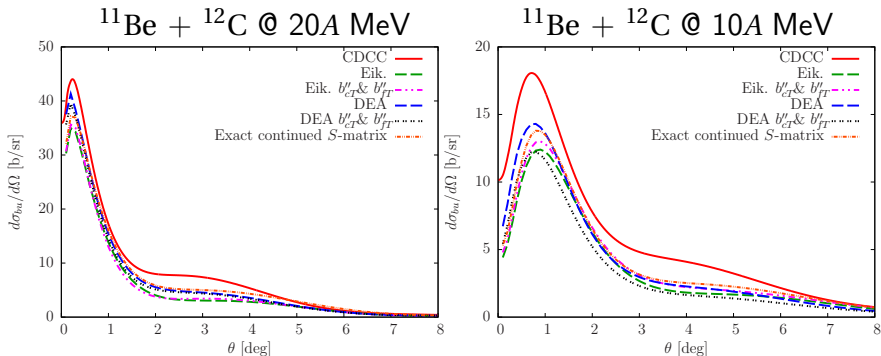
Dependence on energy : breakup



• Dynamical effects more important at lower energies

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Dependence on energy : breakup



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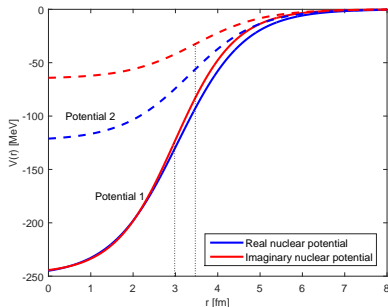
- ① **Semi-classical correction** : larger effect at low energy
- ② **Exact continued S-matrix** : larger effect at low energy

⇒ **No significant accuracy gain at both energies**

Sensitivity of both corrections to interaction potentials

Ongoing analysis

Main influence of ^{10}Be - ^{12}C potential \rightarrow test on two potentials



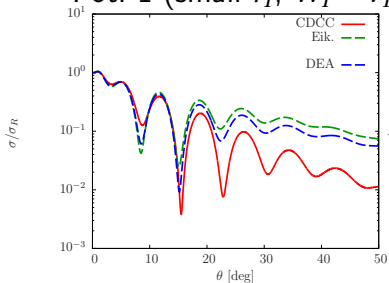
Different absorption parameters :

$$\left(\frac{W_I}{V_R}\right)_{\text{potential 1}} > \left(\frac{W_I}{V_R}\right)_{\text{potential 2}} \quad \text{but} \quad r_{I,\text{potential 1}} < r_{I,\text{potential 2}}$$

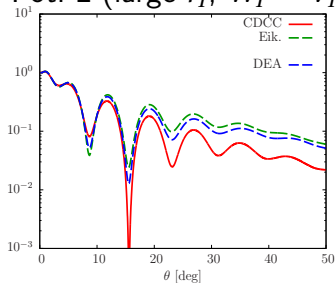
Sensitivity to interaction potentials : elastic scattering

Elastic scattering of ^{11}Be off ^{12}C at 10A MeV

Pot. 1 (small r_I , $W_I \sim V_R$)



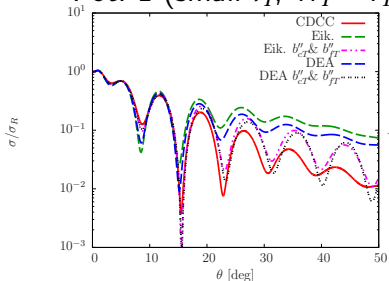
Pot. 2 (large r_I , $W_I \sim V_R/2$)



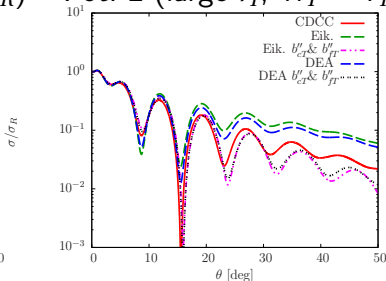
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① Semi-classical correction :

• Sensitive to r_I

→ undercorrection when r_I is small

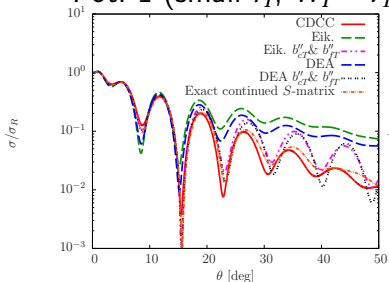
→ overcorrection when r_I is large

• Less accurate when $W_I \sim V_R$

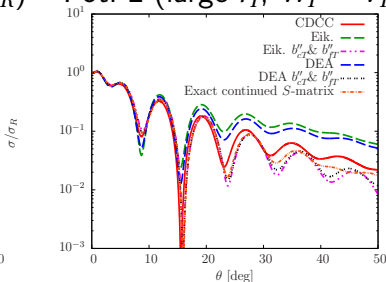
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② **Exact continued S-matrix :**

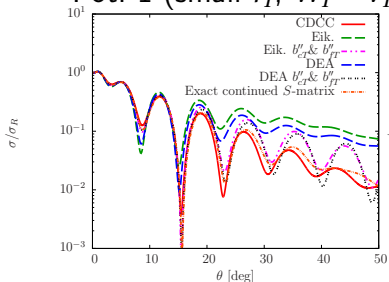
● **Also sensitive to r_I**

● **Same accuracy** for each potential

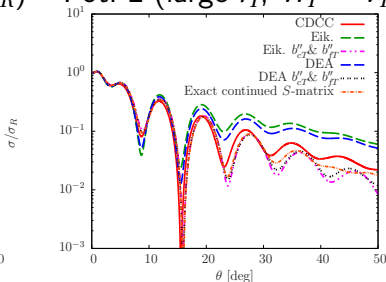
Sensitivity to interaction potentials : elastic scattering

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② **Exact continued S-matrix :**

• **Also sensitive to r_I**

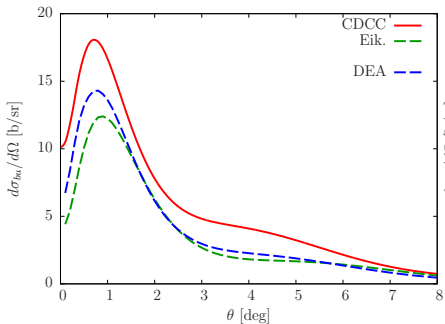
• **Same accuracy** for each potential

⇒ **Both corrections are potential-dependent**

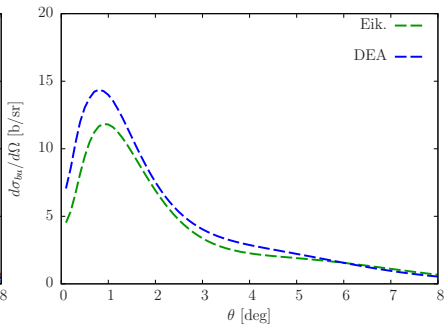
Sensitivity to interaction potentials : breakup

Breakup of ^{11}Be off ^{12}C at 10A MeV

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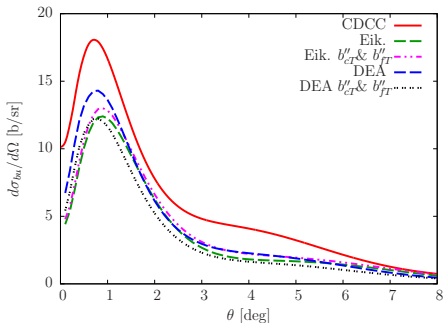
Pot. 2 (large r_I , $W_I \sim V_R/2$)



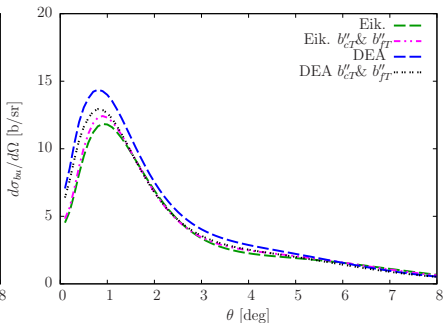
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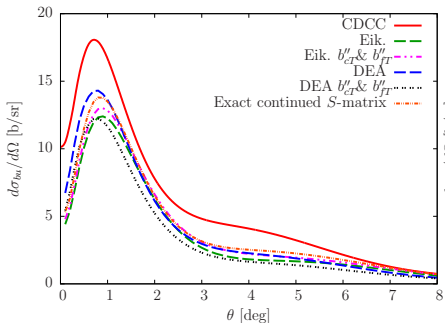


① Semi-classical correction : insensitive to the potential

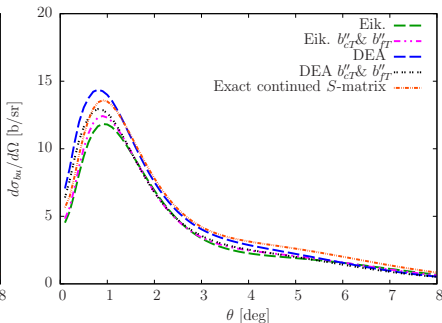
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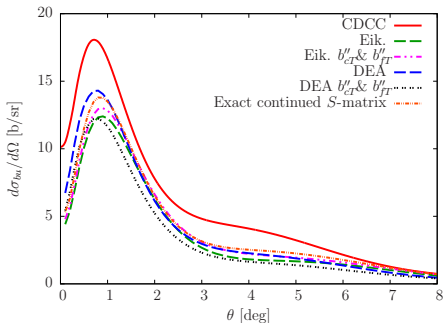


- ① Semi-classical correction : insensitive to the potential
- ② Exact continued S -matrix : insensitive to the potential

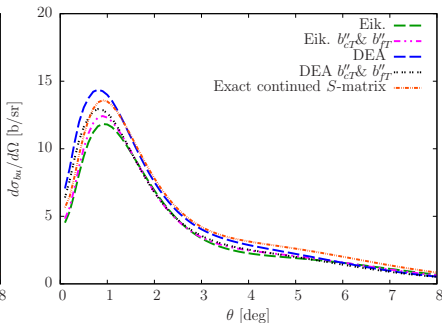
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Eikonal model : fast, easy **but valid only at high energies**

- Coulomb dominated reactions : use of b' shift
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Use of $b'' \in \mathbb{C}$ computed with the **whole optical potential**

- ⊕ Reproduces well the **elastic scattering**
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Use of each fragment's exact phase shifts

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- ⊕ **Similar accuracy** for different **potentials**
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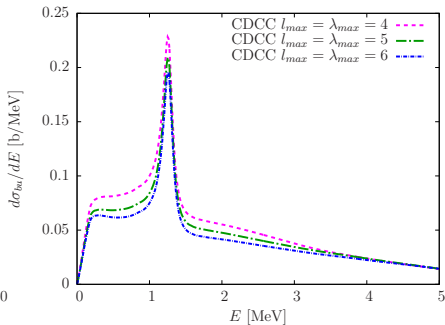
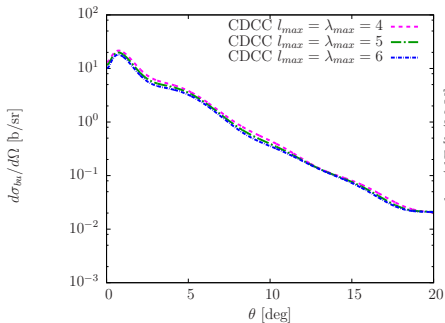
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⇒ **Need to improve the couplings between the « trajectories » within the eikonal model**

Convergence of CDCC computations at 10A MeV

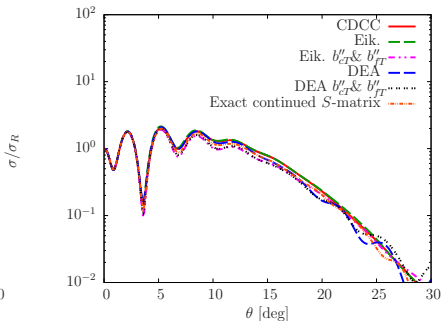
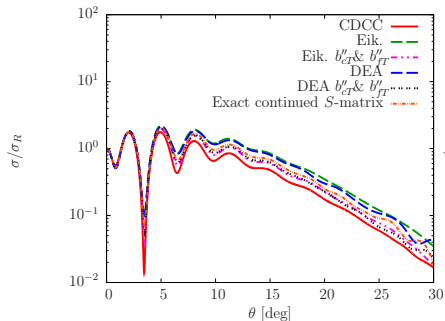


Sensitivity to the potential at 67A MeV

Elastic scattering of ^{11}Be off ^{12}C at 67A MeV

Pot. 1 (small r_I , $W_I \sim V_R$)

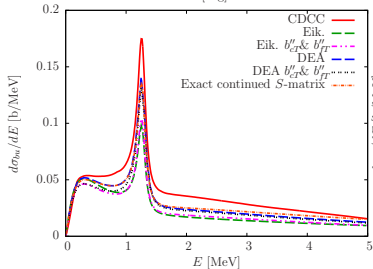
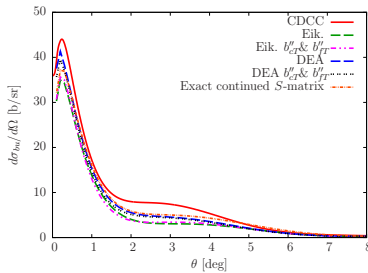
Pot. 2 (large r_I , $W_I \sim V_R/2$)



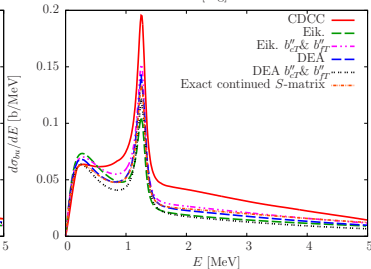
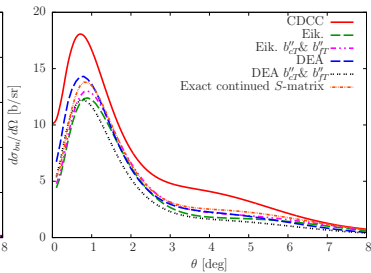
- **Sensitive to r_I** \rightarrow undercorrection when r_I is small
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Dependence on energy of breakup distributions

$^{11}\text{Be} + ^{12}\text{C} @ 20A \text{ MeV}$



$^{11}\text{Be} + ^{12}\text{C} @ 10A \text{ MeV}$



Sensitivity of both corrections to interaction potentials

Breakup of ^{11}Be off ^{12}C at 10A MeV

Pot. 1 (small r_I , $W_I \sim V_R$)

Pot. 2 (large r_I , $W_I \sim V_R/2$)

