

Study of “quenching factors” for (p, pn) and $(p, 2p)$ reactions through the Transfer to the Continuum formalism

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Contents

- 1 Quenching and (p, pN) reactions
 - Quenching factors
 - Description
 - Momentum distributions. Inclusive measurements
- 2 Reaction formalism
 - Transfer to Continuum: TC
- 3 Benchmarks with other reaction formalisms
 - DWIA
 - Faddeev
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Quenching factors

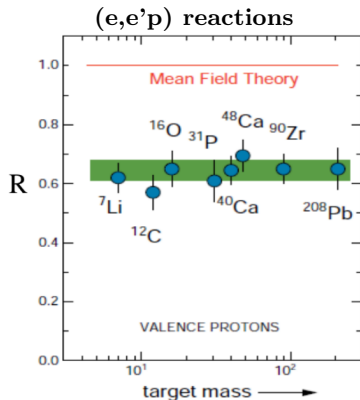
- SF from IPM or shell-model
- Can be related to experiment through:

$$\sigma_{\text{th}} = C^2 S \times \sigma_{s.p.}$$

- Quenching of spectroscopic factors:

$$R_s = \frac{\sigma_{\text{exp}}}{\sigma_{\text{th}}}$$

- Related to beyond-shell-model effects (Short-range correlations)

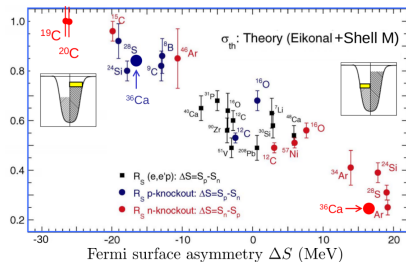


H. Dickhoff, C. Barbieri, Prog. Part. Nucl. Phys. 52, 377 (2004)
 NIKHEF data: L. Lapikas Nucl. Phys. A 553, 297c (1993)



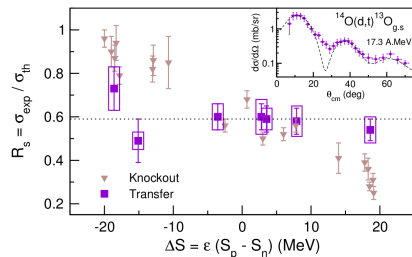
Quenching factors

Knockout reactions



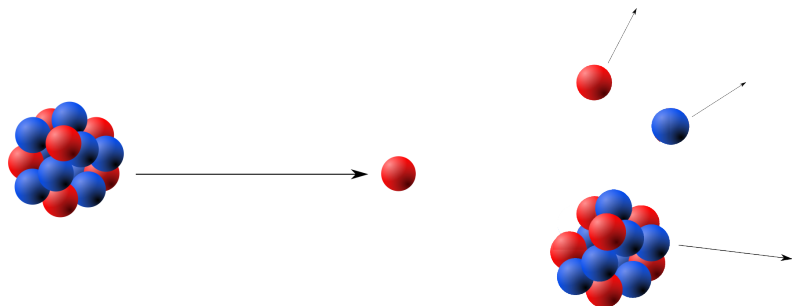
J. Tostevin & A. Gade, Phys.Rev. C 90, 057602 (2014)

Transfer reactions



F. Flavigny *et al*, Phys. Rev. Lett. 110, 122503 (2013)

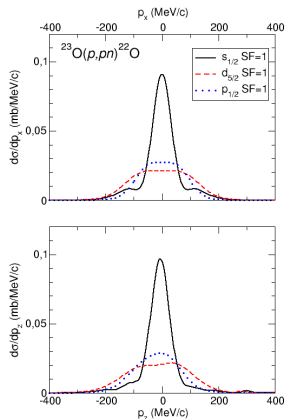
Different tendencies: reaction description in question?

(p, pN) reactions

- A proton and a nucleus collide in such a way that a proton or neutron is removed and the residual nucleus remains.
- High energies (~ 200 - 400 MeV) to increase mean free path of nucleon in nucleus.
- Used to obtain single-particle information of nuclei.
- It is sometimes referred to as “quasifree” because the main interaction can be modelled as if it were a free collision between the incoming proton and the removed nucleon.

Momentum distributions

- Momentum distributions of residual nucleus (core)
- Inclusive measurements: Only core is measured. Integration over all angles of ejected proton and nucleon
- **Shape** gives information about **quantum numbers** of extracted nucleon
- **Magnitude** gives information about **s.p. occupation numbers**



A.M.M. PRC **92**, 044605(2015)



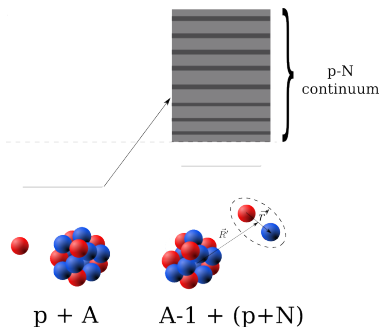
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Reaction formalism: Transfer to Continuum

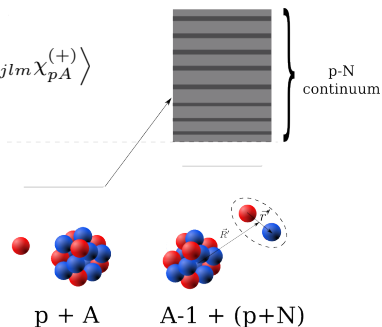
- We consider a calculation without explicit IA, including interaction with residual nucleus in matrix element and without factorization approximation.



Reaction formalism: Transfer to Continuum

- We consider a calculation without explicit IA, including interaction with residual nucleus in matrix element and without factorization approximation.
- Prior representation of the T-matrix for the process $p + A \rightarrow p + N + C$, approximating the exact wf $\Psi_f^{(-)}$ by a 3-body CDCC wf $\psi_f^{3b-CDCC(-)}$

$$\mathcal{T}_{if}^{3b} = \left\langle \psi_f^{3b-CDCC(-)} \left| V_{pN} + U_{pC} - U_{pA} \right| \psi_{jlm} \chi_{pA}^{(+)} \right\rangle$$



Reaction formalism: Transfer to Continuum

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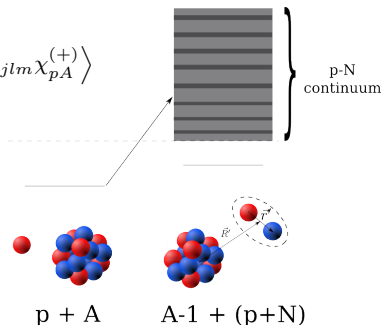
$$\mathcal{T}_{if}^{3b} = \left\langle \psi_f^{3b-CDCC(-)} | V_{pN} + U_{pC} - U_{pA} | \psi_{jlm} \chi_{pA}^{(+)} \right\rangle$$

- p-N continuum states discretized in energy bins
Deuteron included for (p, pn)

$$\phi_n^{j,\pi}(k_n, \vec{r}') = \sqrt{\frac{2}{\pi N}} \int_{k_{n-1}}^{k_n} \phi_n^{j,\pi}(k, \vec{r}') dk$$

- 3-body final state wavefunction expanded in proton-nucleon states

$$\psi_f^{3b-CDCC(-)} \approx \sum_{n,j,\pi} \phi_n^{j,\pi}(k_n, \vec{r}') \chi_{n,j,\pi}^{(-)}(K_{pn}^{\vec{r}'}, \vec{R}')^{\prime}$$



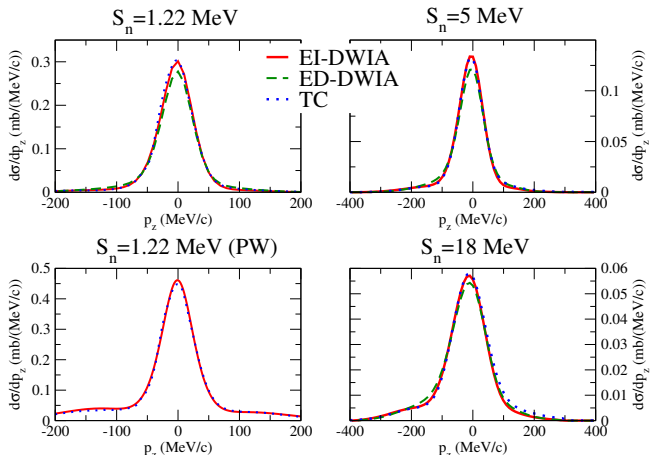
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Benchmark with DWIA: $^{15}\text{C}(p, pn)^{14}\text{C}$ @ 420 MeV/A

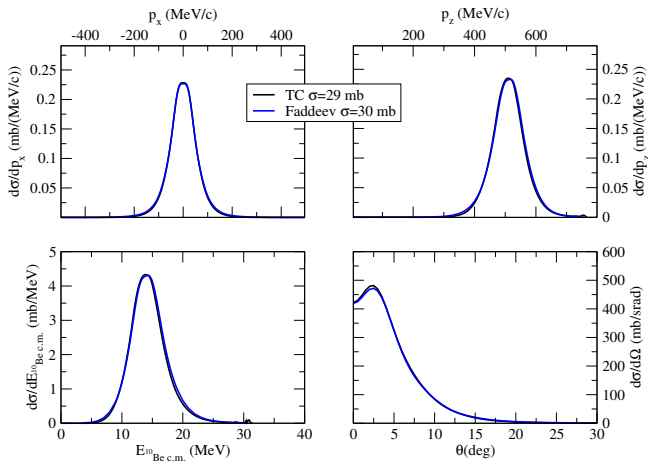
- In collaboration with K. Yoshida and K. Ogata (PRC **97** 024608 (2018))



See talk by K. Yoshida

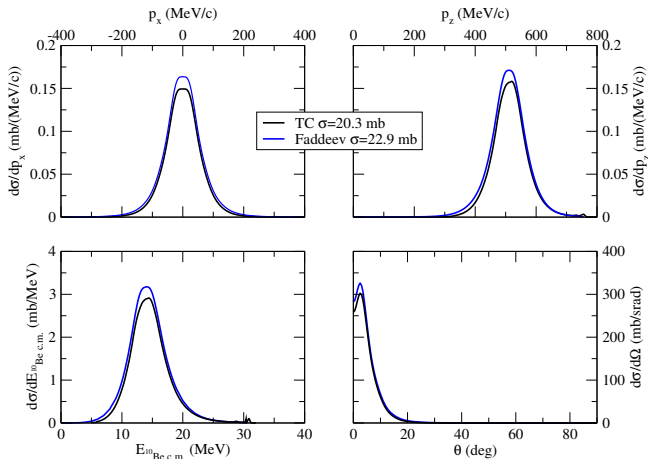
Benchmark with Faddeev: $^{11}\text{Be}(p, pn)^{11}\text{Be}$ @ 200 MeV/A (p wave)

- In collaboration with A. Deluva



Benchmark with Faddeev: $^{11}\text{Be}(p, pn)^{11}\text{Be}$ @ 200 MeV/A (p wave) Reid93

- In collaboration with A. Deltuva



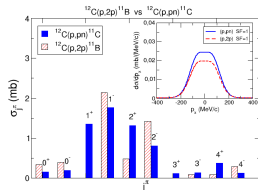
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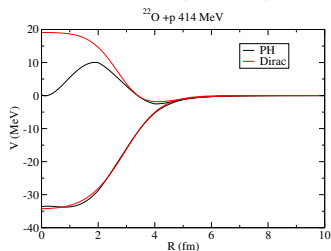
Inputs of the calculation

- Nucleon-nucleon interaction: Reid93



- Bound states from Woods-Saxon
 - $a = 0.7$ fm
 - r_0 chosen to reproduce HF rms (SkX)

- Distorting potentials
 - Folding from Paris-Hamburg g -matrix effective interaction and HF density (SkX)
 - Phenomenological Dirac parametrization (EDAD2)



- SF obtained using WBT interaction

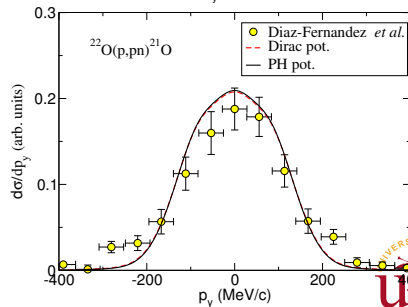
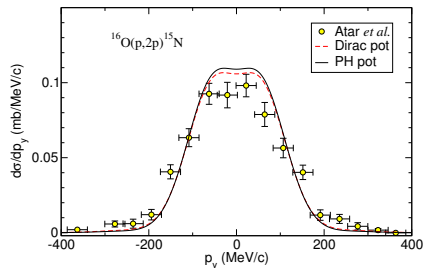
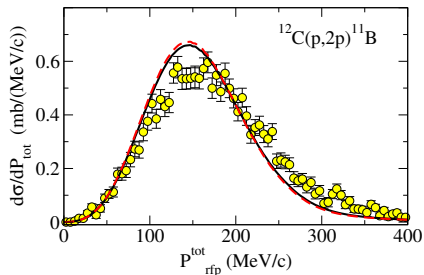
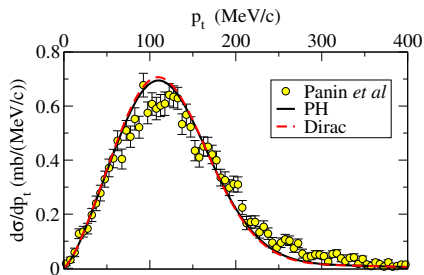


Experimental data

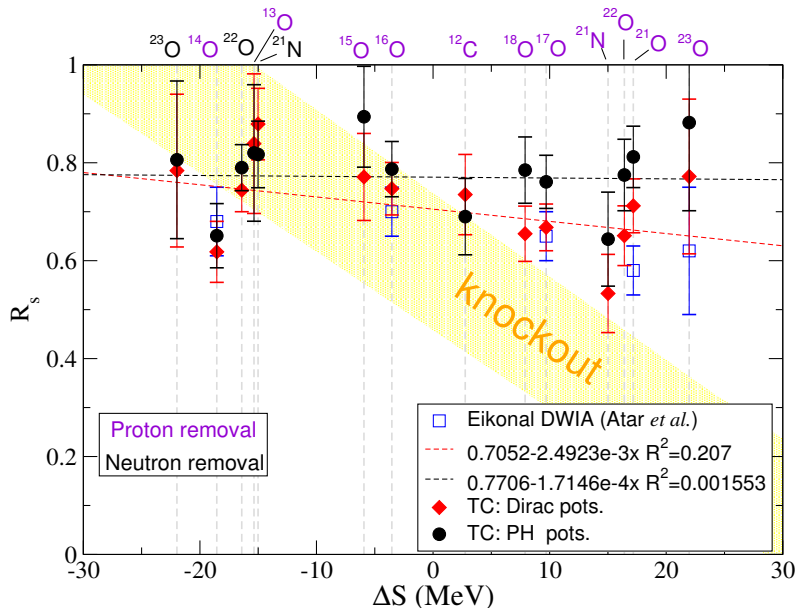
Reaction	E/A	Ref	Reaction	E/A	Ref
$^{13}\text{O}(p, 2p)$	401	1	$^{21}\text{O}(p, 2p)$	449	1
$^{14}\text{O}(p, 2p)$	351	1	$^{21}\text{N}(p, pn)$	417	2
$^{15}\text{O}(p, 2p)$	310	1	$^{21}\text{N}(p, 2p)$	417	2
$^{16}\text{O}(p, 2p)$	451	1	$^{22}\text{O}(p, pn)$	414	2
$^{17}\text{O}(p, 2p)$	406	1	$^{22}\text{O}(p, 2p)$	414	2
$^{18}\text{O}(p, 2p)$	368	1	$^{23}\text{O}(p, pn)$	445	2
$^{12}\text{C}(p, 2p)$	398	3	$^{23}\text{O}(p, 2p)$	445	2

- 1: L. Atar *et al* Phys. Rev. Lett. **120**, 052501 (2018)
- 2: P. Díaz-Fernández *et al* Phys. Rev. C **97**, 024311 (2018)
- 3: V. Panin *et al* Phys. Lett. B **753**, 204 (2016)

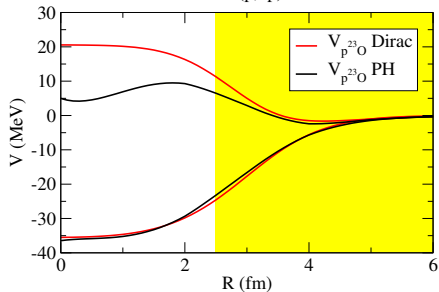
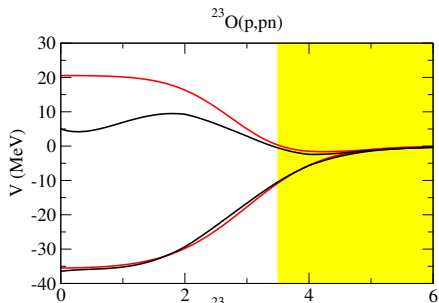
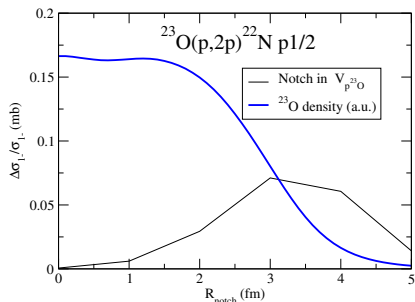
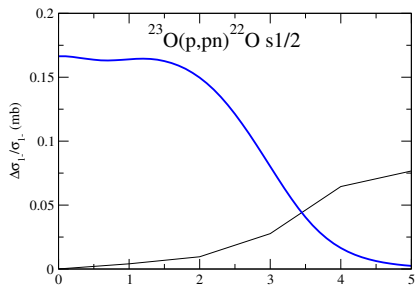
Momentum distributions



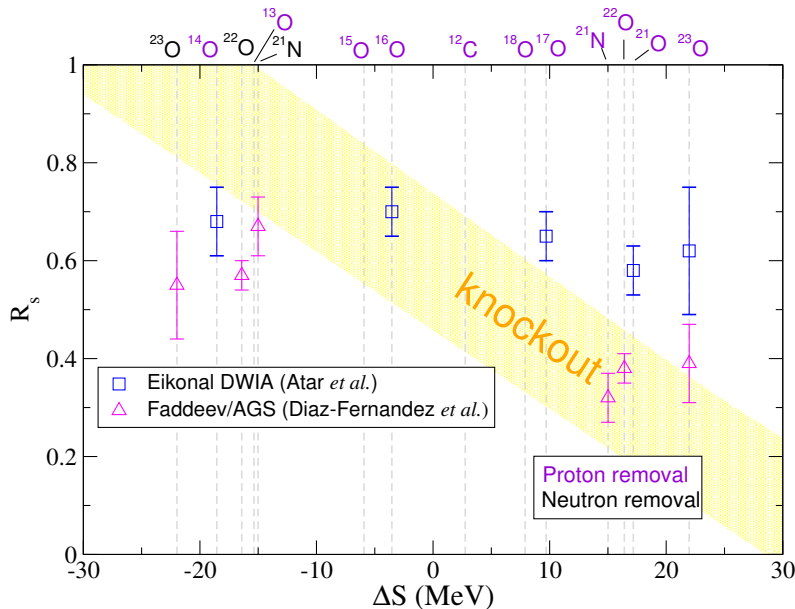
Quenching factors



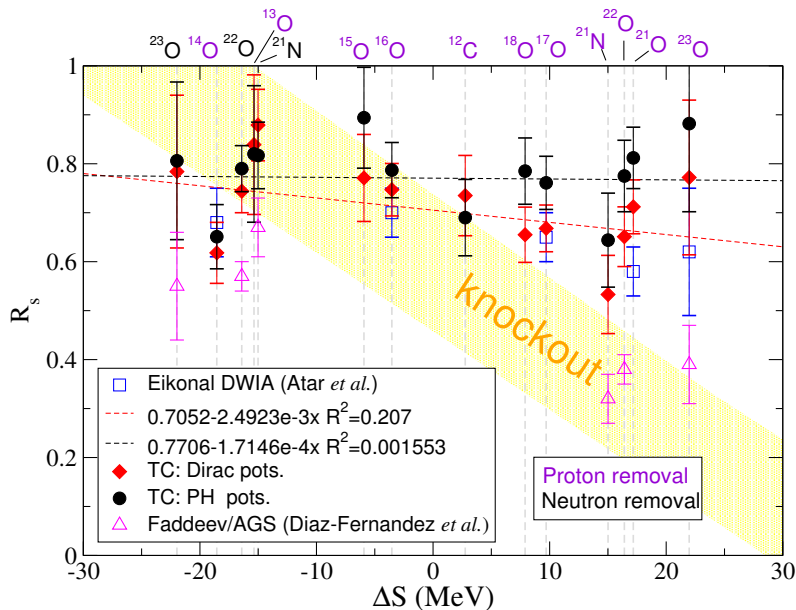
Notch test



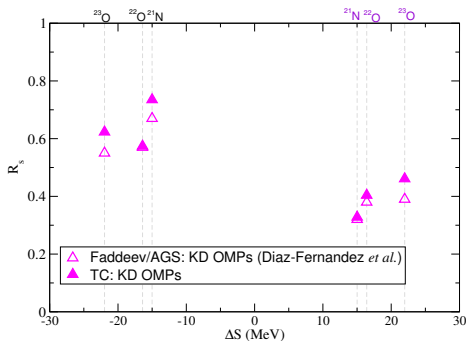
Quenching factors



Quenching factors



Quenching factors. KD potentials



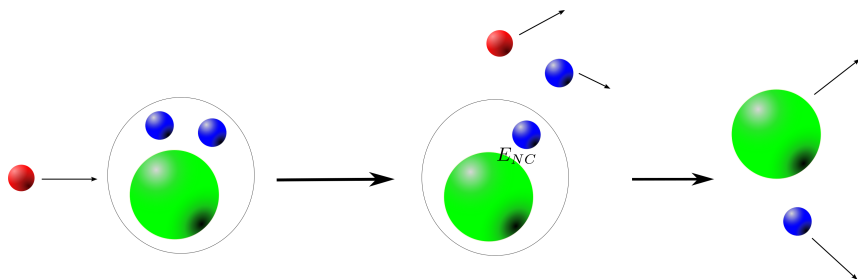
- Köning-Delaroche potentials at 200 MeV
- No relativistic modifications
- WS geometry: $r_0 = 1.25$ fm
 $a = 0.65$ fm

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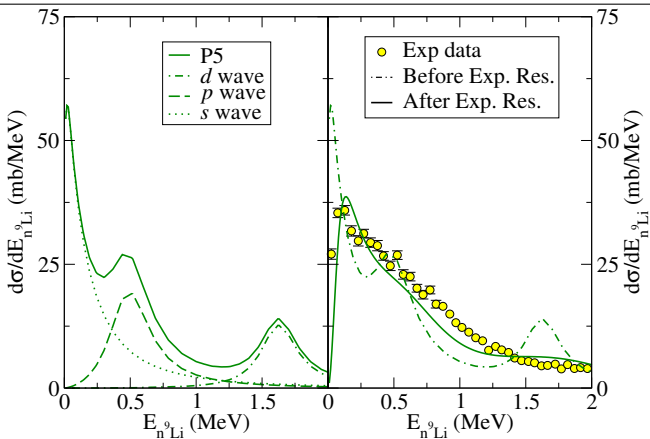
(p, pN) reactions with Borromean nuclei (in collaboration with J. Casal)



- A high-energy proton impinges on a Borromean system with two loosely bound nucleons
- The proton knocks out one nucleon, leaving the core and the other nucleon in a state with positive energy E_{N-C} (since the original nucleus was Borromean)
- The $N - C$ system decays emitting a low-energy nucleon

$^{11}\text{Li}(p, pn)^{10}\text{Li}^*$: $I_{9\text{Li}} = 0 + d$ wave

	E_p (MeV)	a (fm)	E_d (MeV)	% $p_{1/2}$	% $s_{1/2}$	% $d_{5/2}$	r_{mat} (fm)	r_{ch} (fm)
P5	0.50	-29.8	1.5	39	35	23	3.2	2.42

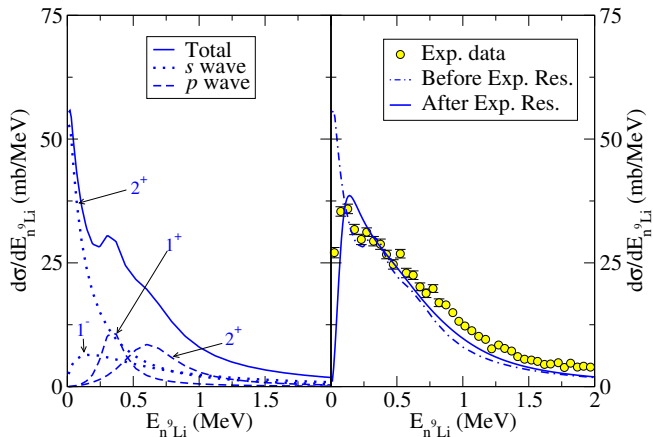


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$$^{11}\text{Li}(p, pn)^{10}\text{Li}^*: I_{9\text{Li}} = 3/2^-$$

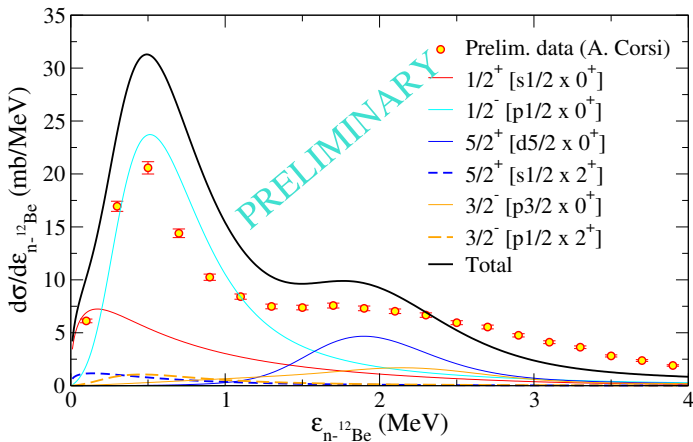
	E_r (MeV)		a (fm)		% $p_{1/2}$	% $s_{1/2}$	r_{mat} (fm)	r_{ch} (fm)
	1^+	2^+	1^-	2^-				
PII	0.37	0.61	-	-37.9	31	67	3.2	2.41



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$^{14}\text{Be}(p, pn)^{13}\text{Be}^*$



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Summary

- Transfer to Continuum (TC) developed for the study of (p, pN) reactions at high and intermediate energies.
- Benchmark with Faddeev and DWIA shows encouraging agreement
 - × Difference with Faddeev when using Reid93 (still unclear)
- “Quenching factors” obtained show small dependence on ΔS
 - Agreement with transfer experiments
 - Disagreement with mid-energy knockout reactions
- Good agreement with published eikonal DWIA R_s for small binding energies, but increased disagreement for larger binding energies
- Overall R_s 0.7~0.8 larger than overall value for R_s for $(e, e'p)$ with IPM 0.6~0.7
- Formalism has been extended to study Borromean nuclei: $^{11}\text{Li}(p, pn)^{10}\text{Li}$ has been published and analysis of $^{14}\text{Be}(p, pn)$ is underway



Collaborators

- K. Yoshida
- K. Ogata
- A. Deltuva
- J. Casal
- A. Corsi



Focus on peak

