

ECT\**@*2019.10.17

# **NS EOS and tidal deformability with nuclear energy functionals**

---

Chang-Hwan Lee / Pusan National University

# Dense Nuclear & Stellar Matter Studies

for **RAON** New Rare Isotope Accelerator & **MMA** Multi-Messenger Astrophysics

## **BUD<sup>2</sup>** Collaboration

**Busan** (**CHL**, Myungkuk KIM)

**Ulsan** (**Kyujin KWAK**, Young-Min KIM)

**Daegu** (**Chang Ho HYUN**, ...)

**Daejeon** (**Youngman KIM**, ...)

Montreal (**Sangyong JEON**, McGill)



# Dense Matter Physics in Korea *my personal point of view*

---

<i>Hadron Physics</i>		<i>Astrophysics</i>
NS EoS with <b>Effective Field Theories</b> (with D.P.Min, <b>M.Rho</b> & G.E.Brown)	<b>1990s</b>	NS Binary as a source of GW (with <b>G.E.Brown</b> @Stony Brook)
<b>Science-Business-Belt Project</b> initiated by <b>D.P. Min</b>	<b>2003</b>	<b>Korean Gravitational Wave Group</b> Nuclear physics + Astrophysics + Mathematics + Artificial Intelligence
<b>RAON project</b> was approved	<b>2006</b>	
<b>New Transport DJBUU</b> <b>Nuclear Structure DRHBc</b>	<b>2009</b>	<b>KGWG</b> joined LIGO Scientific Collab.
<b>First run of RAON</b> Symmetry Energy (later)	<b>2017</b>	<b>GW from NS-NS mergers</b> (Multi-messenger Astrophysics) Tidal deformability of NS
	<b>2021</b>	<b>BUD<sup>2</sup> Collaboration</b> for Astro-Hadron Physics

# *ECT\* Workshops co-organized by Koreans & Europeans*

<i>Hadron Physics</i>		<b>ECT*</b> established in 1993
NS EoS with <b>Effective Field Theories</b> (with D.P.Min, <b>M.Rho</b> & G.E.Brown)	1990s	<i>Astrophysics</i>   <b>1994 Director: B. Mottelson</b> Organized by M. Rho & W. Weise (my first visit to ECT* as a Ph.D. student)
Science-Business-Belt Project initiated by <b>D.P. Min</b>	2003	Nuclear physics + Astrophysics + Mathema   <b>2004 Director: W. Weise</b>
RAON project was approved	2006	
Transport Studies history by YM Kim's talk application by MG Kim's talk	2009	Novel Approaches to the Nuclear Many-Body Problem: From Nuclei to Stellar Matter Organisers: C-H. Lee (Co-ordinator) ( <i>Pusan National Univ.</i> ), N. Kaiser ( <i>TU Munich</i> ), A. Schwenk ( <i>Ohio State Univ.</i> ) [p. 36]
	2017	(Multi-meson theory + many-body theory + Tidal deformations + <b>2015 Director: W. Weise</b>
First run of RAON Symmetry Energy (later)	2021	ECT*-APCTP Joint Workshop: From Rare Isotopes to Neutron Stars Francesca Gulminelli (LPC and University of Caen, France) Chang-Hwan Lee (Pusan National University, Busan, Korea) Yongseok Oh (Kyungpook National University, Daegu, Korea) Jürgen Schaffner-Bielich (Goethe University Frankfurt, Germany)
BUD Collaboration for Astro-Hadron Physics		

Novel Approaches to Nuclear Many-Body Problem:  
From Nuclei to Stellar Matter  
ECT\*, Sep. 6-17, 2004  
(organized by CH Lee, N Kaiser, A Schwenk)



# Works with G.E. Brown & H.A. Bethe

1999

## The formation of high-mass black holes in low-mass X-ray binaries

G.E. Brown<sup>a,1</sup>, C.-H. Lee<sup>a,2</sup>, Hans A. Bethe<sup>b,3</sup>

2000

## HYPERCritical ADVECTION-DOMINATED ACCRETION FLOW

G. E. BROWN AND C.-H. LEE

Department of Physics and Astronomy, State University of New York, Stony Brook, New York 11794

AND

H. A. BETHE

## A theory of gamma-ray bursts

G.E. Brown<sup>a</sup>, C.-H. Lee<sup>a</sup>, R.A.M.J. Wijers<sup>a</sup>, H.K. Lee<sup>b</sup>, G. Israelian<sup>c</sup>, H.A. Bethe<sup>d</sup>

2001

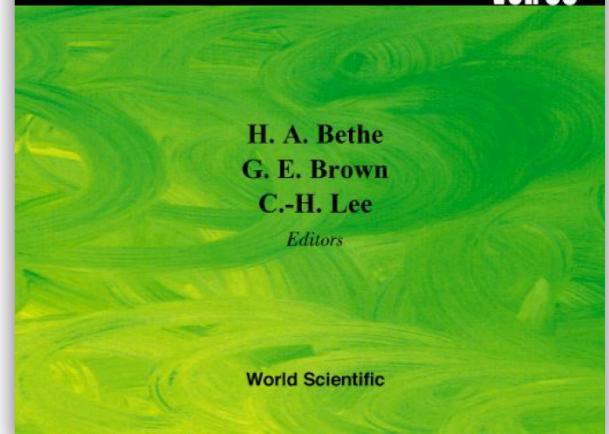
## Formation of high mass X-ray black hole binaries

G.E. Brown<sup>a</sup>, A. Heger<sup>b</sup>, N. Langer<sup>c</sup>, C.-H. Lee<sup>a,d,\*</sup>, S. Wellstein<sup>e</sup>, H.A. Bethe<sup>f</sup>

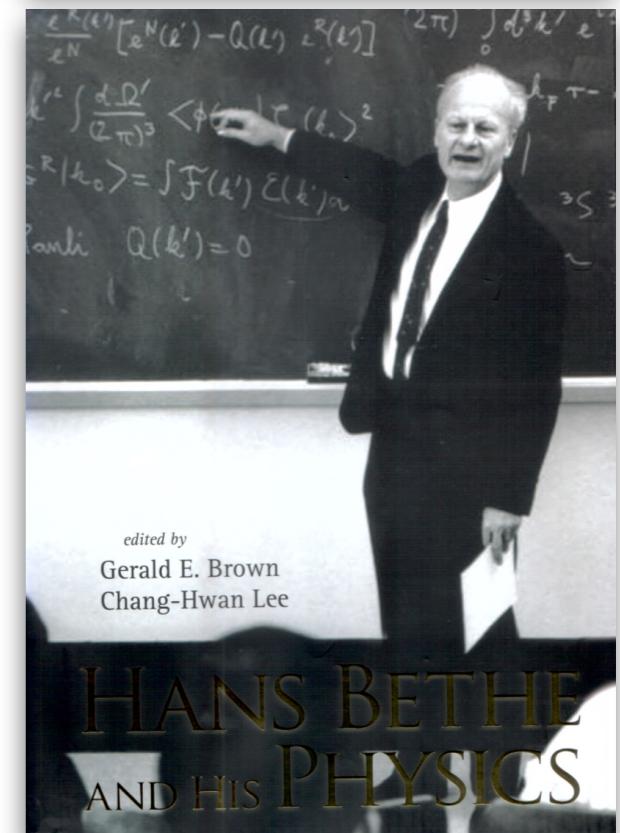
## FORMATION AND EVOLUTION OF BLACK HOLES IN THE GALAXY

*A Reprint Volume with Commentary*

World Scientific Series in 20th Century Physics Vol.33



2003



2006

# Contents

---

## 1. Introduction of RAON

- new rare isotope accelerator in Korea

## 2. Possible origin of high-mass neutron stars

- NS binary evolution (work done before GW detection)

## 3. New development in BUD<sup>2</sup> Collaboration

- KIDS: new energy density functional
- Application of KIDS to NS properties

## 4. Prospects

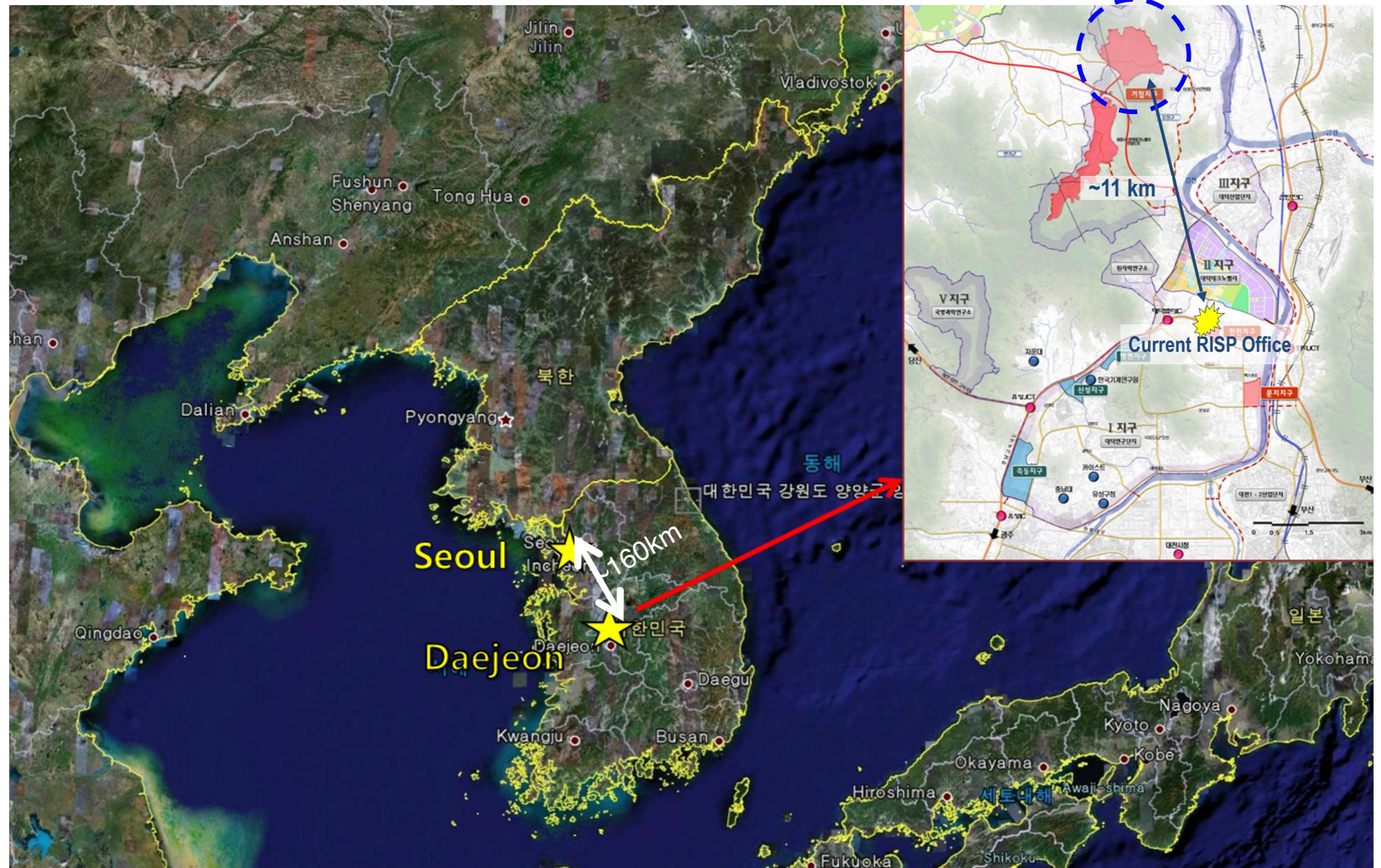
## ◦ Laboratory probes of the nuclear matter EOS

---



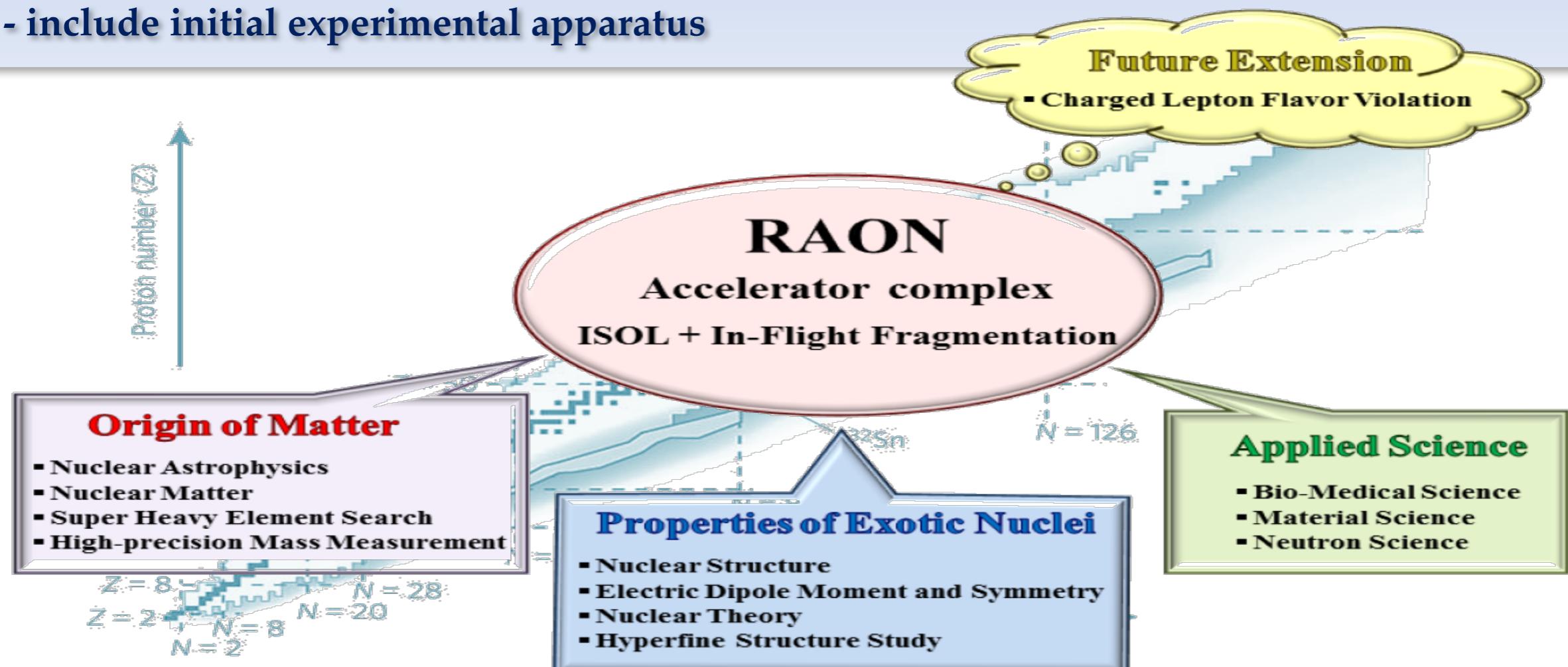
*Courtesy of  
Youngman Kim (IBS)  
Seung-Woo Hong (RAON User Liaison Center, SKKU)*

# RAON Site : Sindong in Daejeon

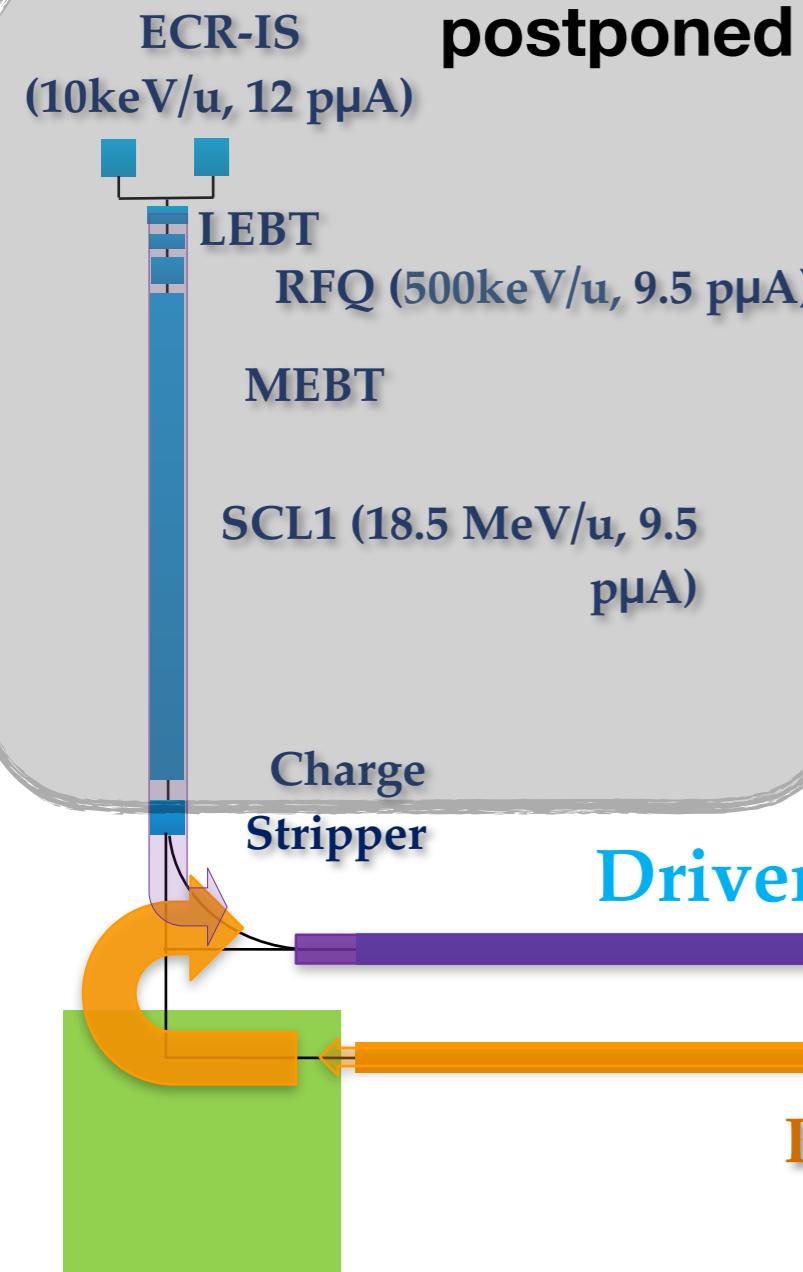


# Rare Isotope Science Project (RISP)

- Goal : To build a heavy ion accelerator complex RAON for rare isotope science researches in Korea
  - Project period : 2011.12 - 2021.12
  - Total Budget : ~\$ 1.43 billion
    - include initial experimental apparatus
- (Facilities ~ \$ 0.46 bill., Bldgs & Utilities ~ \$ 0.97 bill.)



# RAON Concept

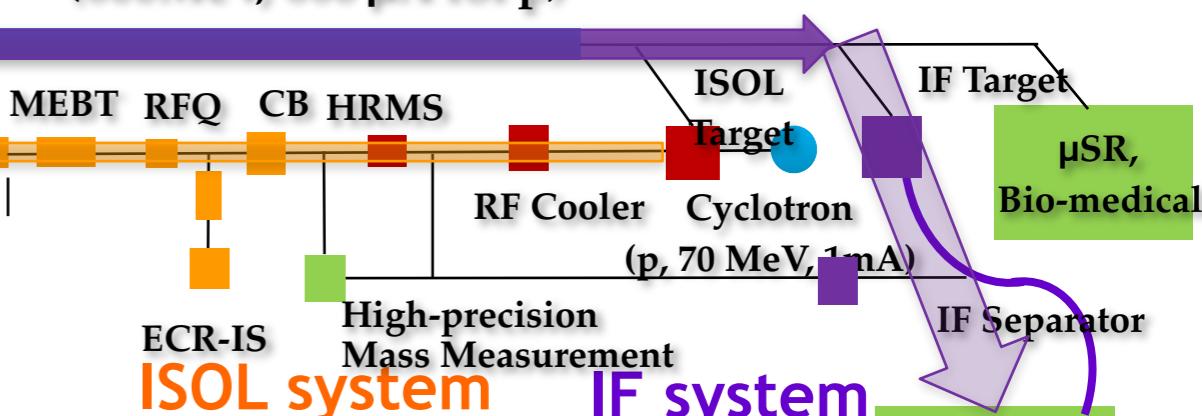


Low Energy Experiments  
Nuclear Astrophysics

CB : Charge Breeder  
HRMS : High Resolution Mass Separator

- ❑ High intensity **RI beams** by **ISOL & IF**
  - ISOL** : direct fission of  $^{238}\text{U}$  by 70MeV protons
  - IF** : 200MeV/u, 8.3pμA of  $^{238}\text{U}$
- ❑ High quality **neutron-rich RI beams**  
 $^{132}\text{Sn}$  with up to  $\sim 250\text{MeV/u}$ , up to  $\sim 10^8 \text{ pps}$
- ❑ More exotic **RI beams** by **ISOL+IF**

SCL2 (200 MeV/u, 8.3 pμA for  $\text{U}^{+79}$ )  
(600MeV, 660 μA for p)



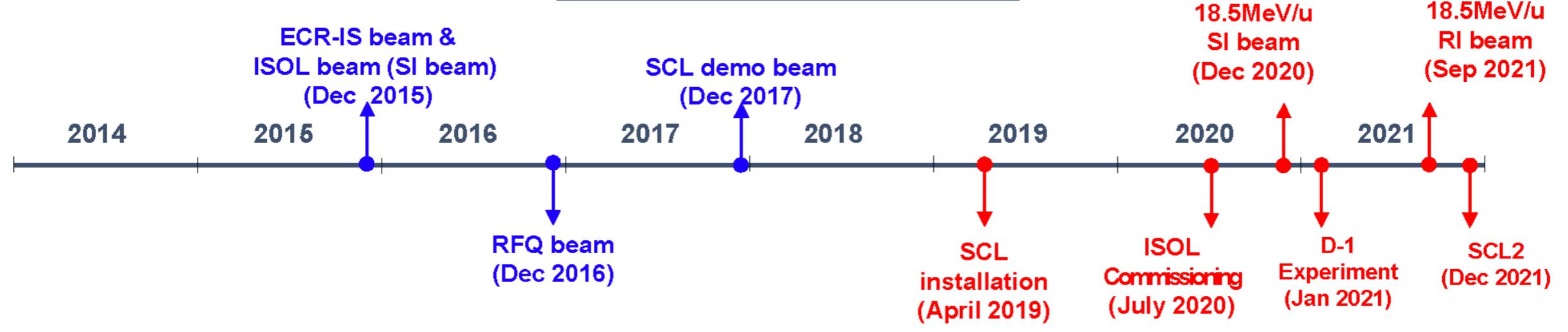
High Energy Experiments  
Nuclear Structure/  
Symmetry Energy

# 1. Overview

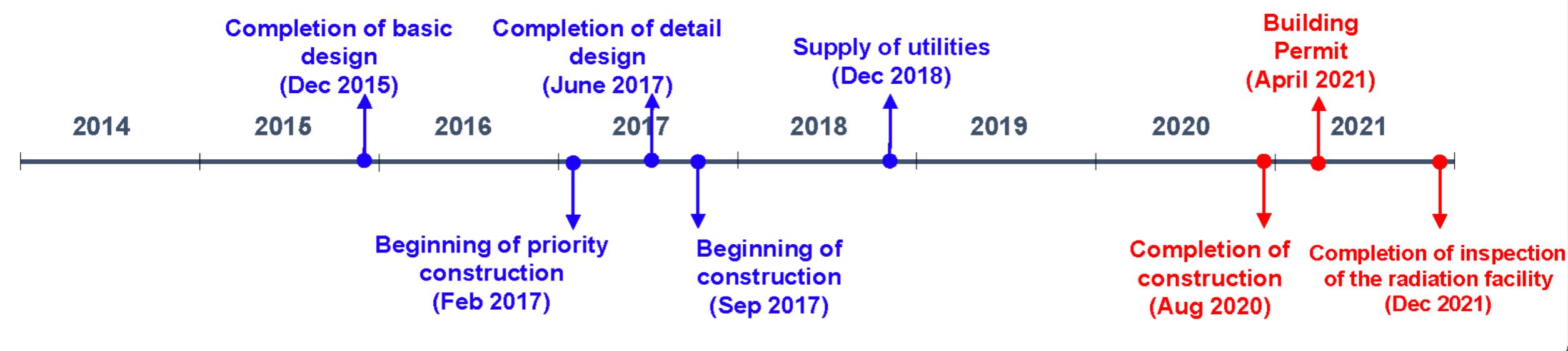
## Project Milestone



### System Installation



### Facility Construction





Sep. 2019

Area ~ 1M m<sup>2</sup>

13



Installation of the First Superconducting Cavities and Cryomodules<sup>14</sup>  
2019.9.26

## ▪ Accelerator

- Mass production for SCL3 is under way
- SCL2 is under pre-production phase
- **From April, 2019, installation for SCL will start from SCL3.**

## ▪ By the end of 2021, we will achieve

- **SI beams:** Stable ion beams ( $^{16}\text{O}$ ,  $^{40}\text{Ar}$ ) from ECRIS  $\rightarrow$  SCL3  $\rightarrow$  low E exp hall
- **RI beams:** RIBs extraction from ISOL  $\rightarrow$  re-acceleration through SLC3  $\rightarrow$  low E exp hall
- Stable / RI beams will be delivered to low-E experimental hall
- **Early phase experiments are going to be performed using KOBRA**
  - RIBs production at KOBRA ( $A < \sim 50$ , beam energy  $< 20$  MeV/u) using SI beams from SCL3
- Beam commissioning starts for SCL2
- Installation and commissioning for IF, LAMPS, Neutron, bio-medical and muSR
  - Collaborative works with RUA (RAON Users Association) via RULC (RAON Users Liason Center)

## ▪ Post RISP (2021 ~ )

- Beam acceleration for ISOL  $\rightarrow$  SCL3  $\rightarrow$  SCL2  $\rightarrow$  IF (**ISOL+IF**)
- Beam commissioning and experiments for IF, LAMPS, Neutron, bio-medical and muSR
- **Ramping-up to get the 400kW beams (more than 5 yrs)**
- Energy upgrade to 400MeV/u (requires budget)

# Contents

---

## 1. Introduction of RAON

- new rare isotope accelerator in Korea

## 2. Possible origin of high-mass neutron stars

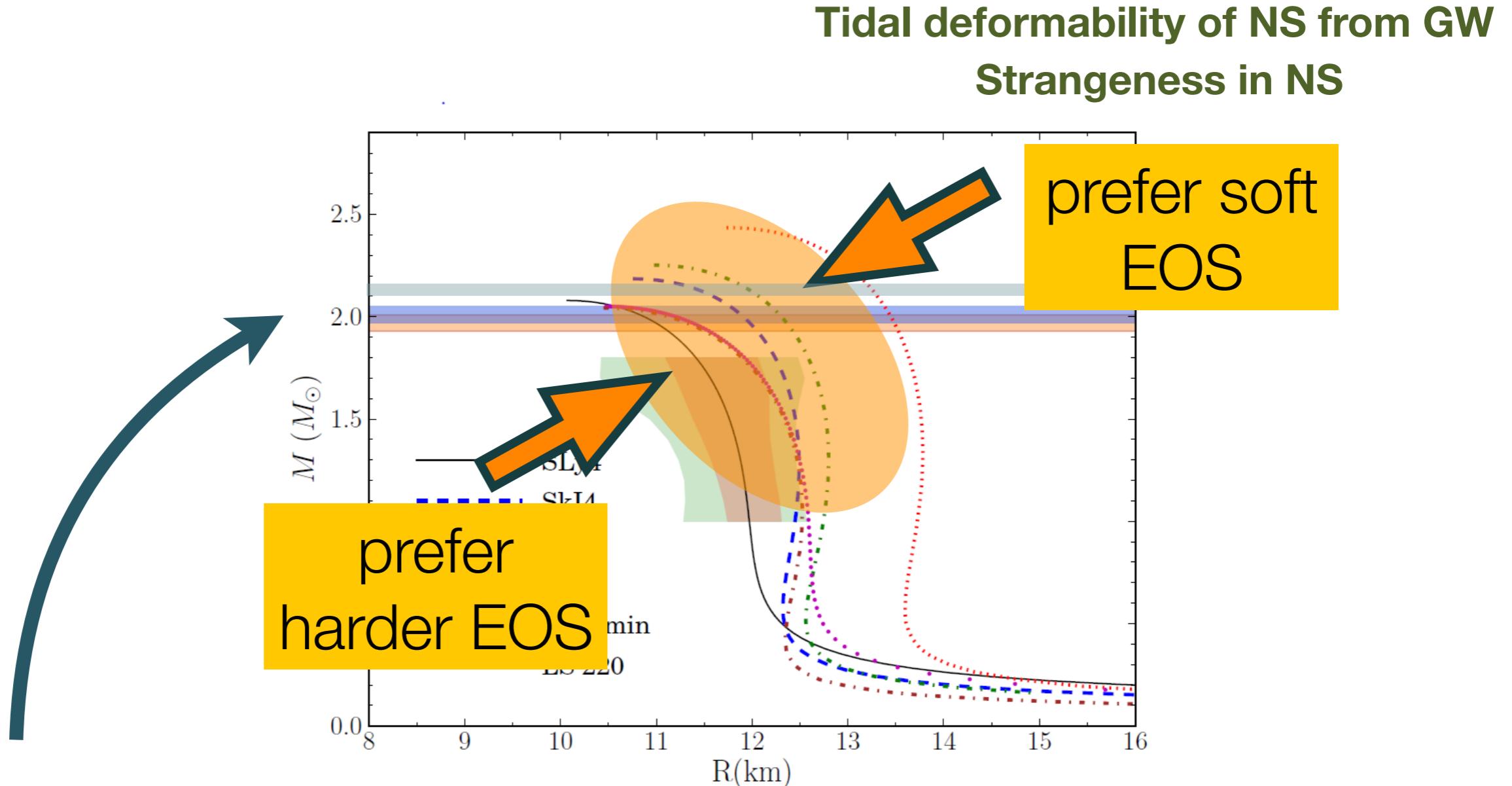
- NS binary evolution (work done before GW detection)

## 3. New development in BUD<sup>2</sup> Collaboration

- KIDS: new energy density functional
- Application of KIDS to NS properties

## 4. Prospects

# Mass & radius of neutron star

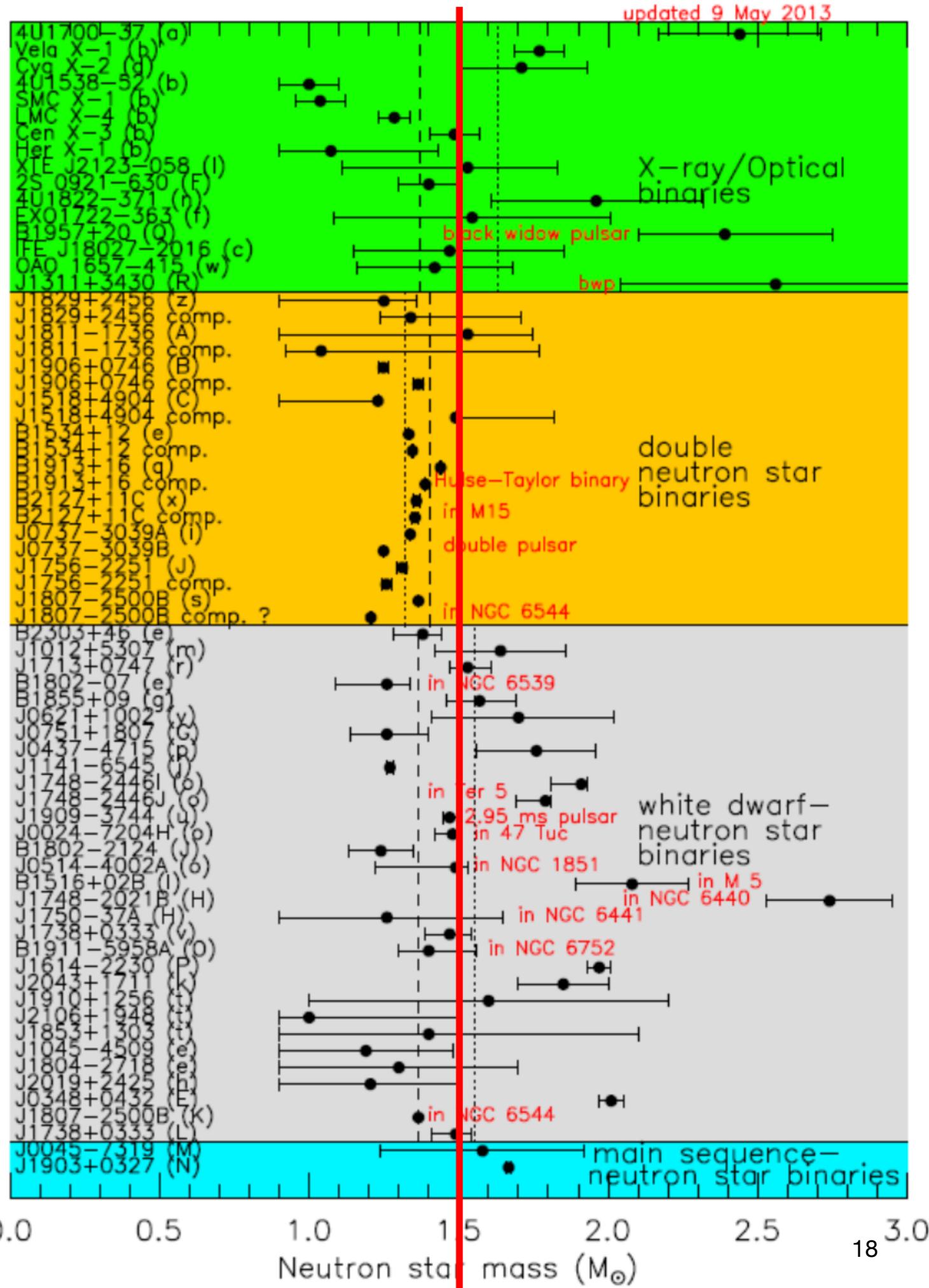


## Neutron Star-White Dwarf Binaries

1.97 solar mass NS : Nature (2010)

2.01 solar mass NS : Science (2013)

2.14 solar mass NS : Nature Astronomy (2019)



All well measured NS masses  
in NS-NS binaries are less than  
1.5 solar mass!

Why?

Prakash (2013)

# Our open questions

---

$2 M_{\odot}$  NS has been observed in NS-WD binaries

- Why all well-measured NS masses in NS-NS binaries are less than  $1.5 M_{\odot}$ ?
- What is the maximum mass of neutron stars?

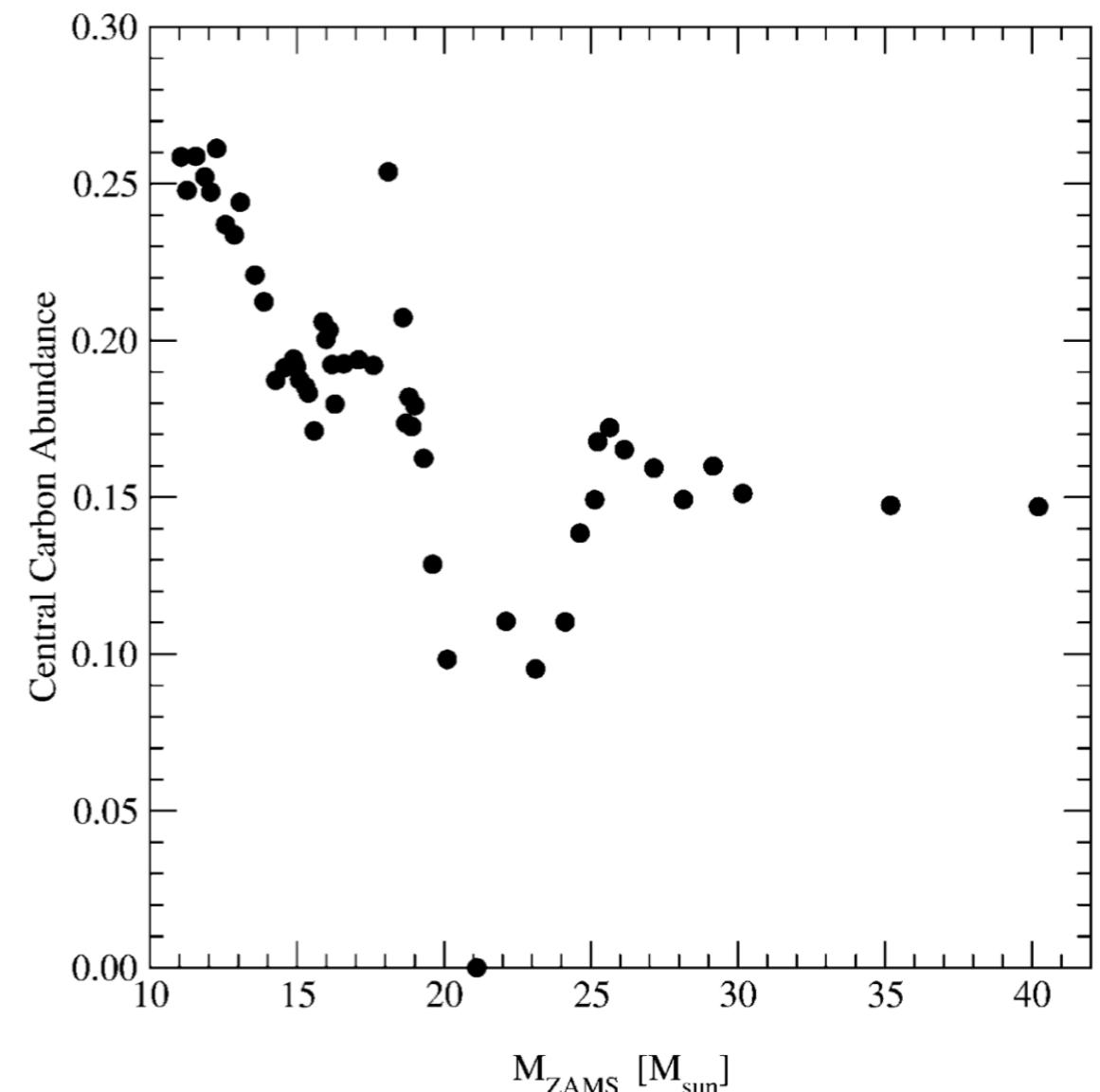
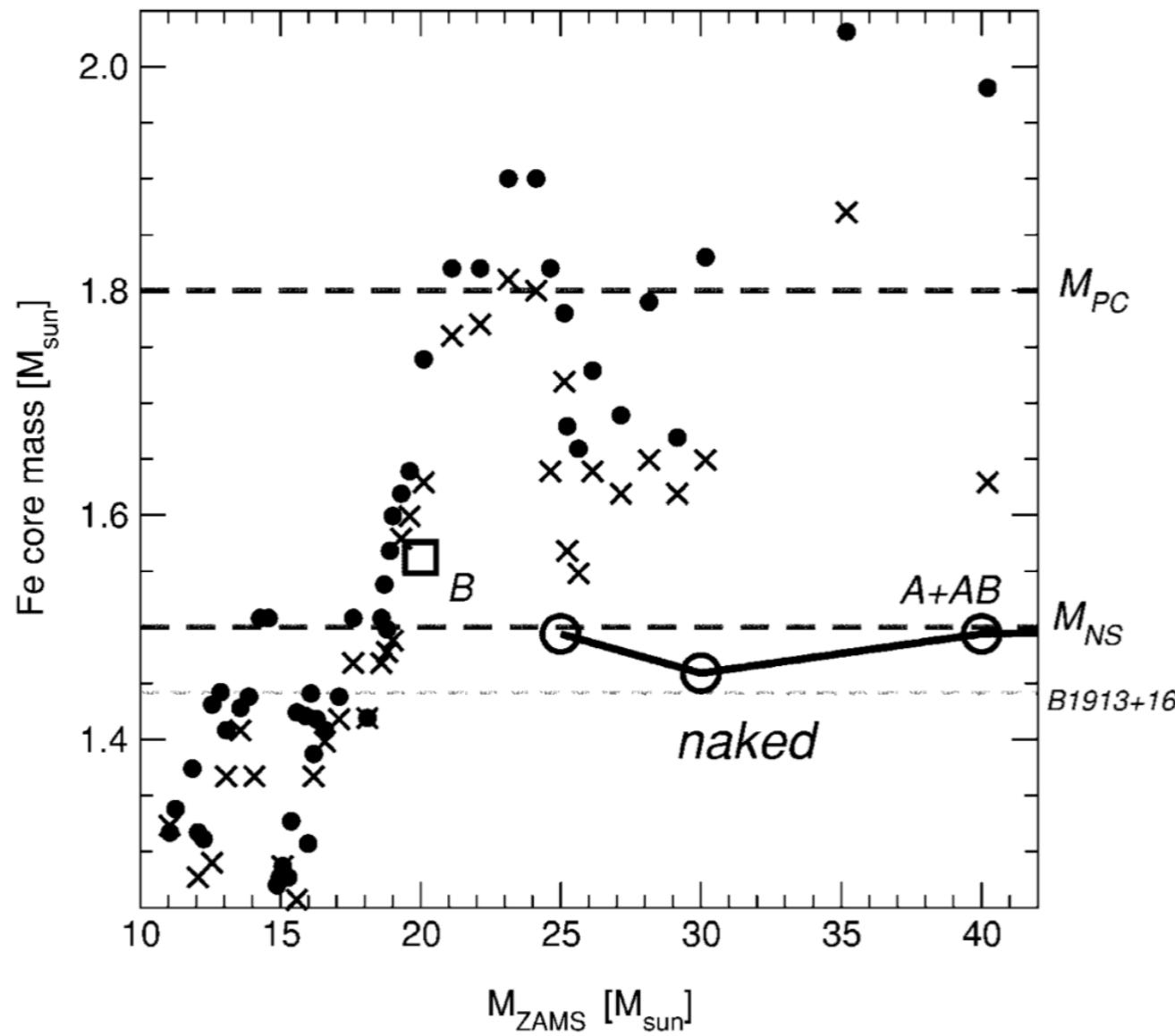
Before the observation of high-mass neutron stars

Lee, Park, Brown, ApJ 670 (2007) 741

We discussed the maximum mass of NS can be significantly higher than  $1.5 M_{\odot}$  as far as the evolution is concerned.

## Formation of high mass X-ray black hole binaries

G.E. Brown<sup>a</sup>, A. Heger<sup>b</sup>, N. Langer<sup>c</sup>, C.-H. Lee<sup>a,d,\*</sup>, S. Wellstein<sup>e</sup>, H.A. Bethe<sup>f</sup>



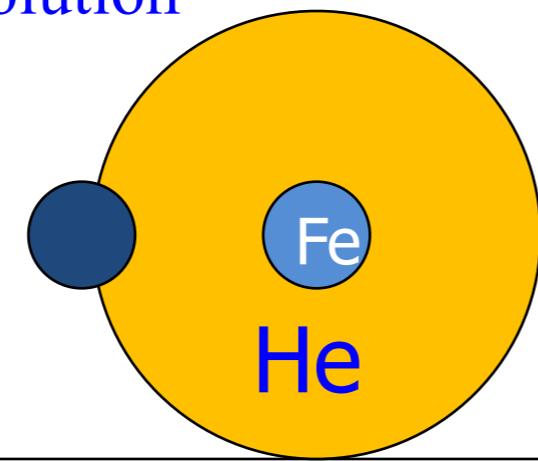
In close binaries (evolution without H envelope)

low Fe core mass NS mass = 1.3 - 1.5 solar mass

# Fate of first born NS

Common envelope evolution

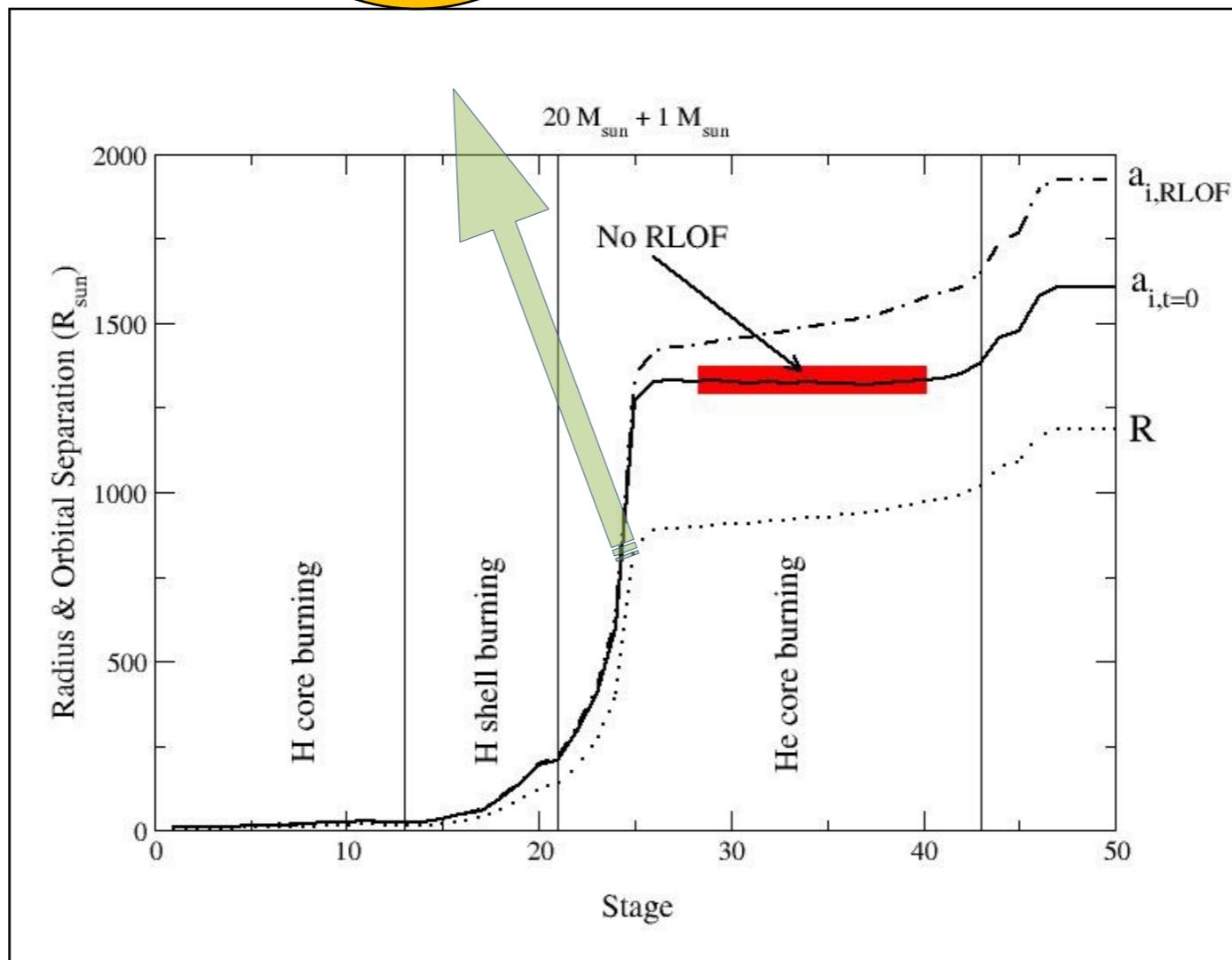
1<sup>st</sup>-born NS



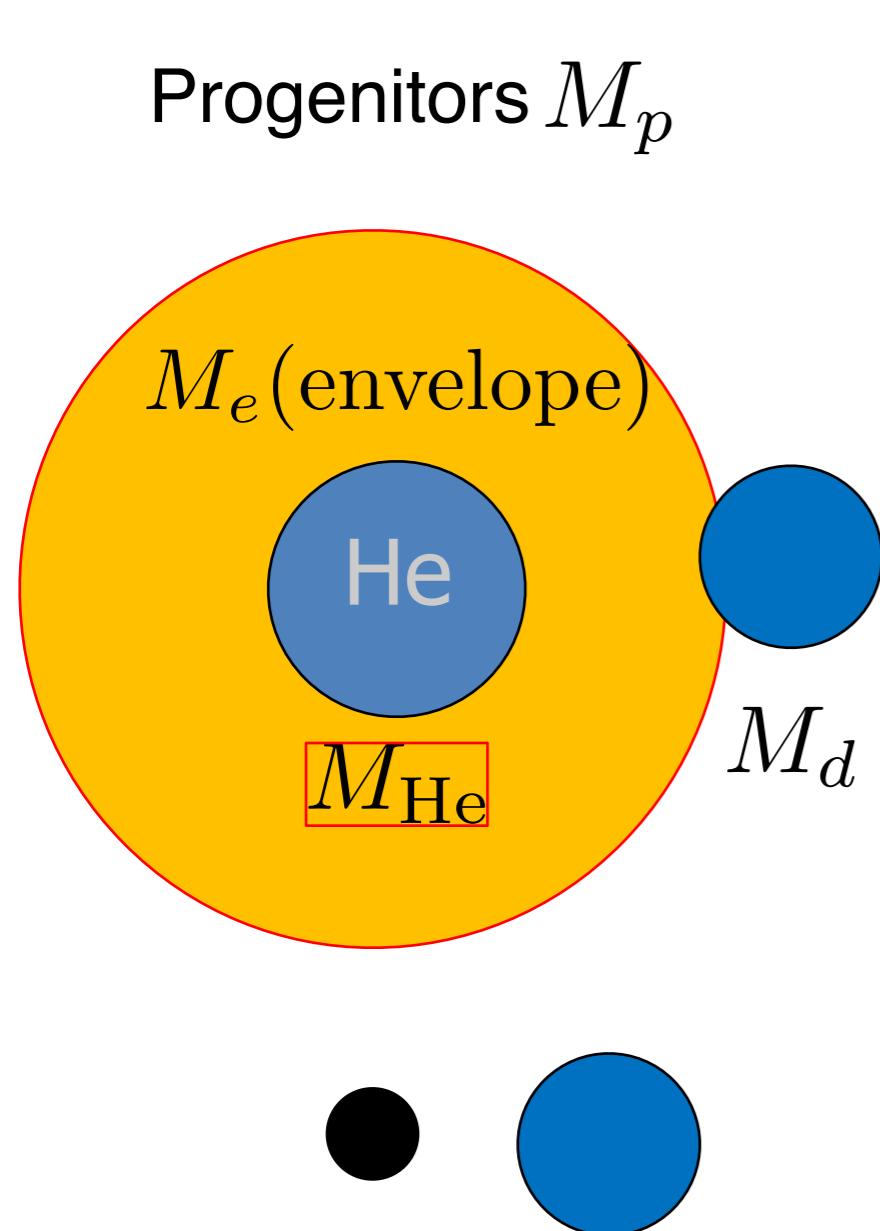
NS with accretion

2<sup>nd</sup> NS/WD

Evolution of Companion



# Common envelope evolution



Gravitational self-energy of H envelope

Progenitors  $M_p$



$$\frac{GM_p M_e}{\lambda R} = \frac{GM_p M_e}{\lambda r_L a_i} = \alpha_{\text{ce}} \left( \frac{GM_{\text{He}} M_d}{2a_f} - \frac{GM_p M_d}{2a_i} \right)$$



Change of binary orbital energy

Q) How to determine  $\lambda\alpha_{\text{ce}}$

# What we have discovered in Soft X-ray transients (BH binary)

## Formation and evolution of black hole X-ray transient systems

G.E. Brown<sup>a</sup>, C.-H. Lee<sup>a,b,\*</sup>, T.M. Tauris<sup>c</sup>

$$\lambda\alpha_{ce} \approx 0.2 - 0.5$$

*New Astronomy 6 (2001) 331*

DISCOVERY OF A BLACK HOLE MASS-PERIOD CORRELATION IN SOFT X-RAY TRANSIENTS  
AND ITS IMPLICATION FOR GAMMA-RAY BURST AND HYPERNOVA MECHANISMS

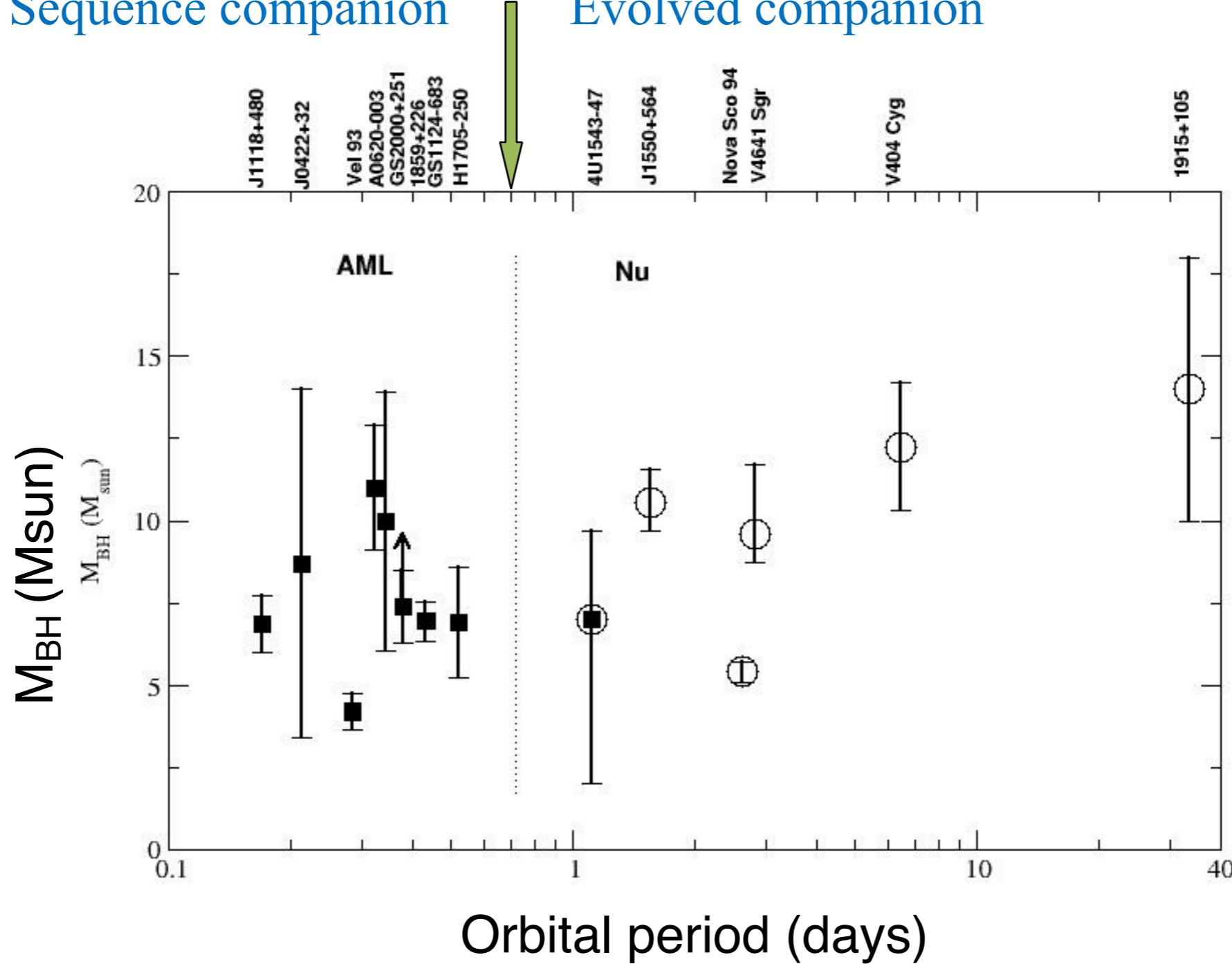
C.-H. LEE,<sup>1,2,3</sup> G. E. BROWN,<sup>3</sup> AND R. A. M. J. WIJERS<sup>3,4</sup>

*CHL, G.E. Brown, R.A.M.J. Wijers, ApJ 575 (2002) 996*

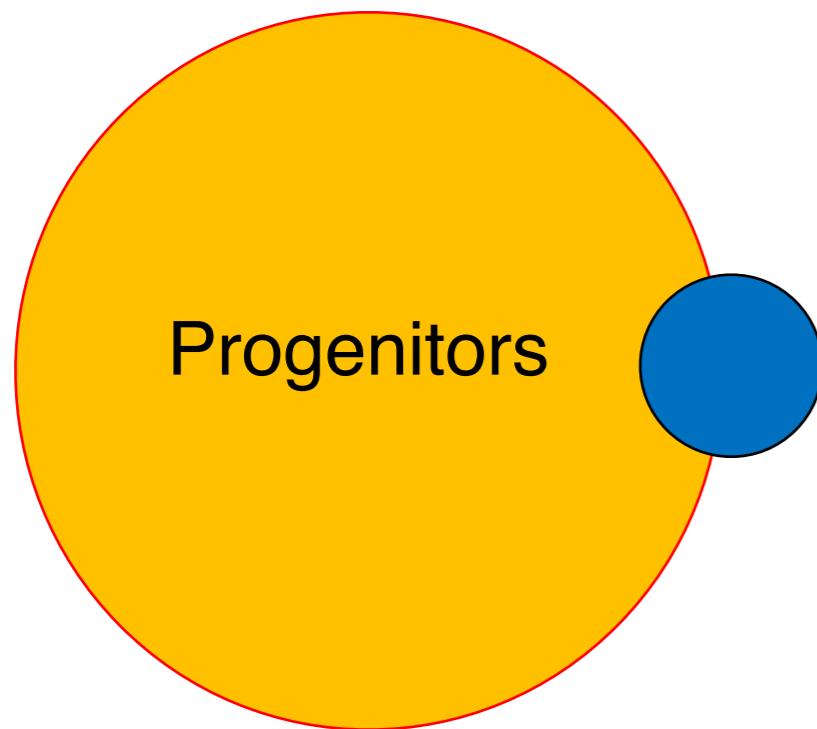
$$\lambda\alpha_{ce} = 0.2$$

# BH Binaries / Soft X-ray Transients

Main Sequence companion      Evolved companion

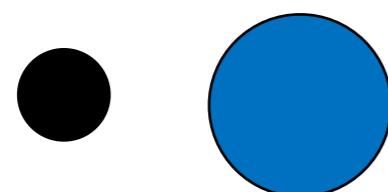
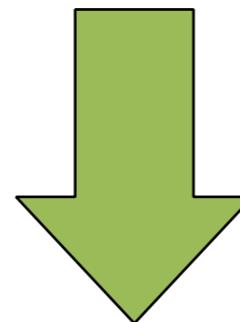


Q) How can we understand  
the population of SXTs ?



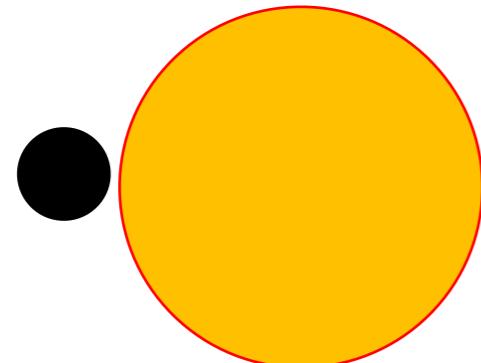
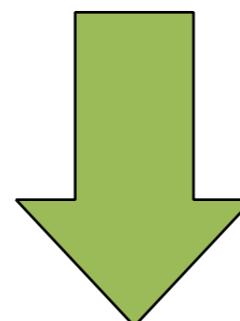
Progenitors

Q1) Evolution of BH/NS Progenitor



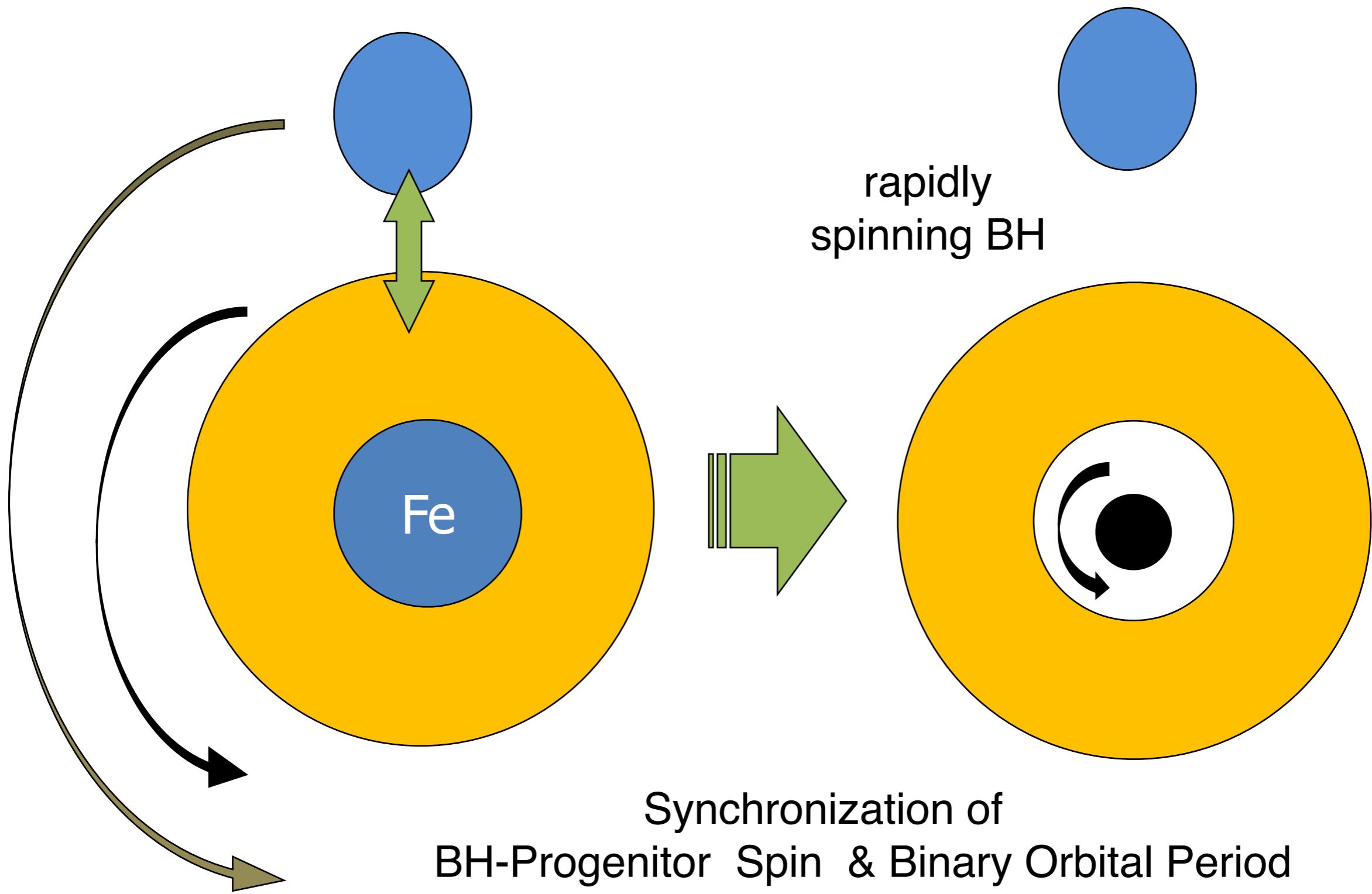
Current Observation

Q2) What happens at birth ?

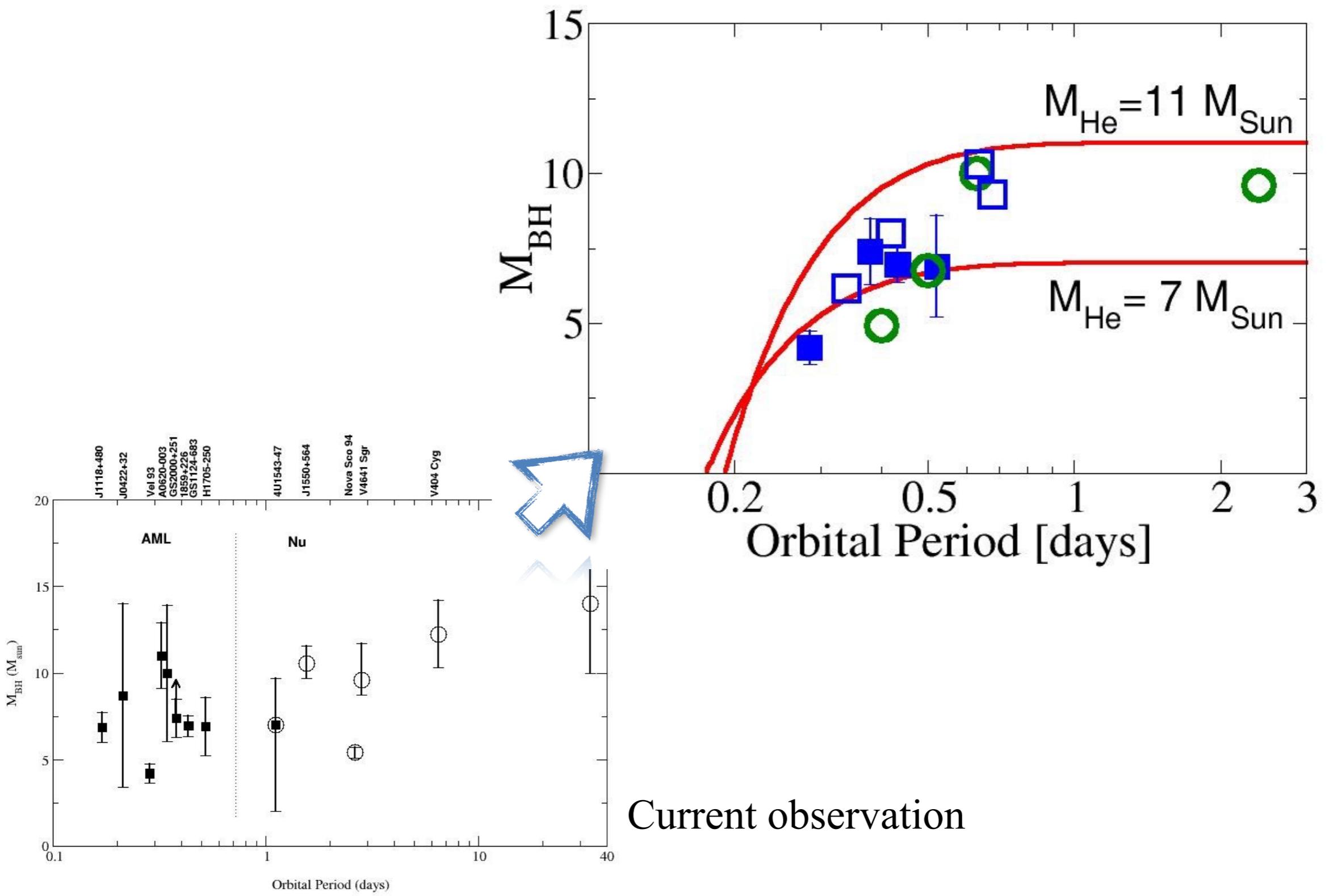


Q3) Evolution of Donor Star

## Tidal interaction just before BH formation

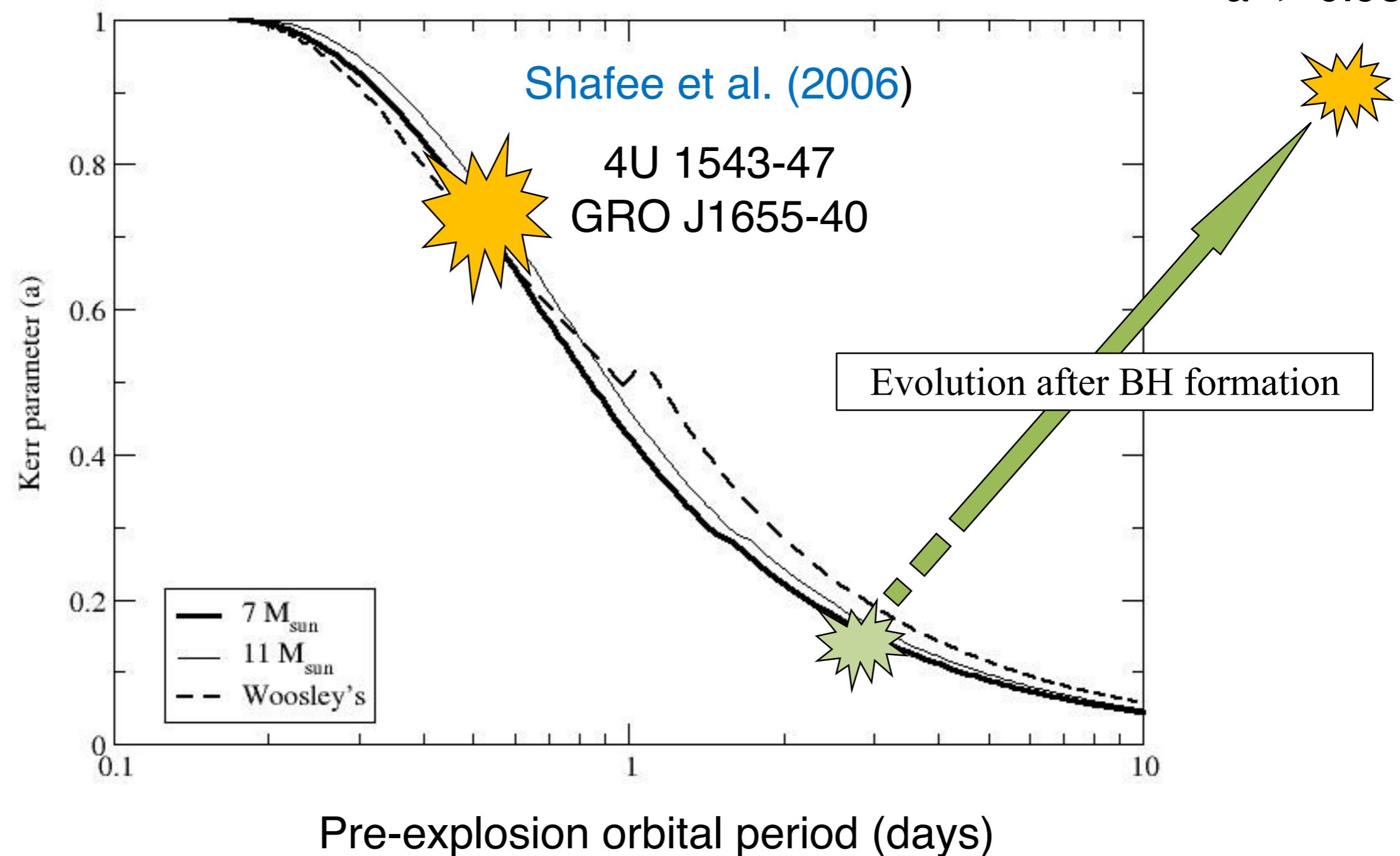


# Reconstructed BH Binaries at the time of birth

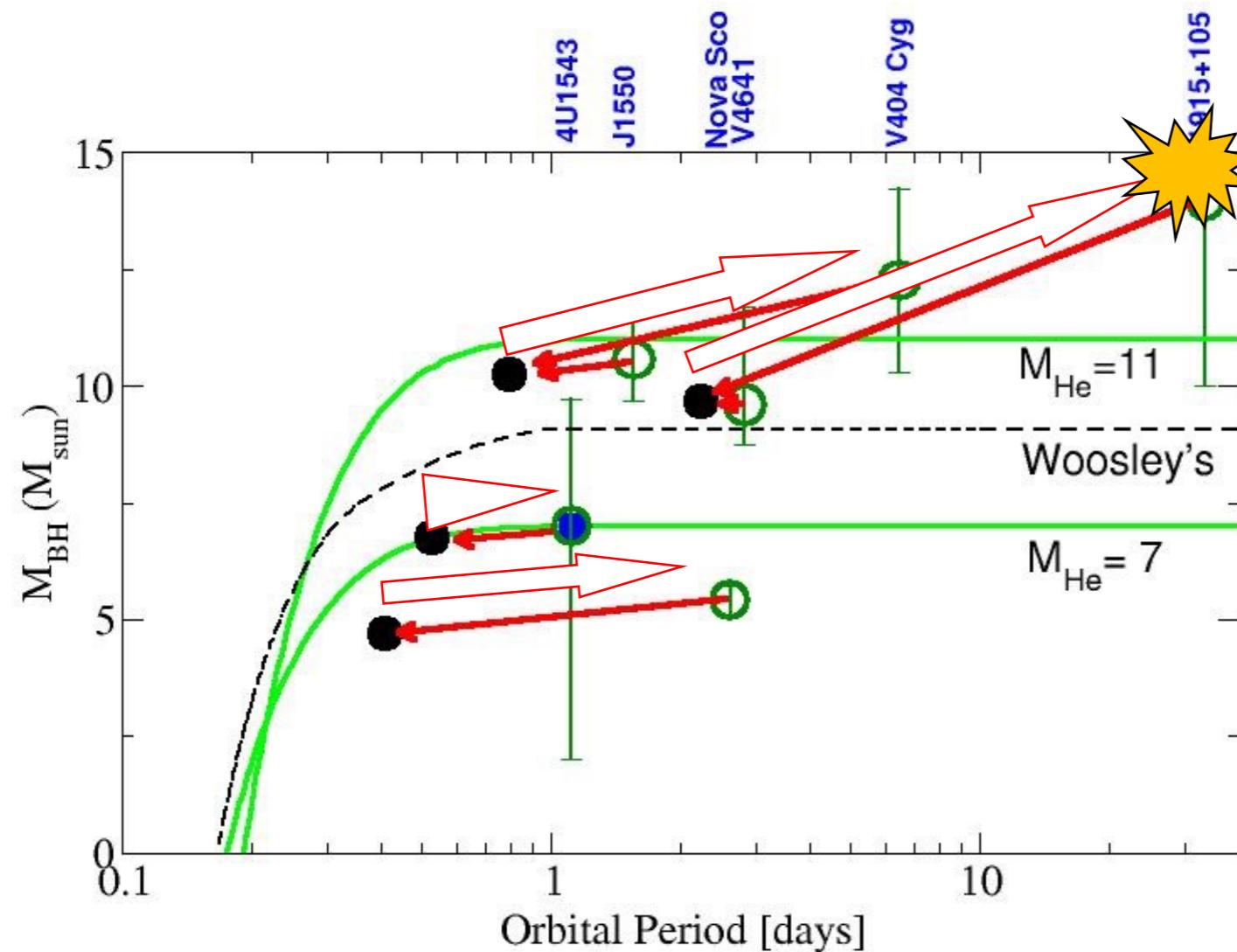


## Rapidly spinning black holes at birth

GRS 1915+105

 $a^* > 0.98$ 

## Evolution after BH formation



GRS 1915+105  
spin-up due to accretion

Kerr parameters for stellar mass black holes and their consequences for GRBs and hypernovae  
Moreno Mendez, Brown, Lee, Walter (ApJ 727:29, 2011)

What if we apply the same evolution to NS binaries

---

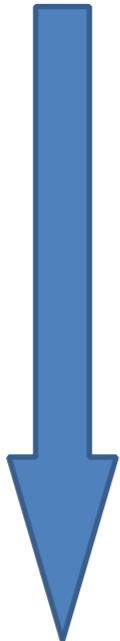
Lee, Park, Brown, ApJ 670,741(2007)

Lee, Cho, Nuclear Physics A 928 (2014) 296

## Eddington limit / critical accretion rate

---

$$L_{\text{Edd}} = \frac{4\pi c G M}{\kappa} \approx 1.3 \times 10^{38} \frac{M}{M_{\odot}} \text{erg s}^{-1}$$



$$\kappa = \sigma_T N_A$$

Thomson scattering cross section  $\sigma_T$

Avogadro's number  $N_A$

$$L_{\text{Edd}} = \eta \dot{M}_{\text{Edd}} c^2$$

$$\dot{M}_{\text{Edd}} = \frac{4\pi G M}{\kappa c \eta} \approx \frac{1}{\eta} 0.45 \times 10^{-8} \left( \frac{M}{M_{\odot}} \right) M_{\odot} \text{yr}^{-1}$$

# Super-critical accretion onto first born NS

---

- Eddington Accretion Rate : photon pressure balances the gravitation attraction
- If this limit holds, neutron star cannot be formed from the beginning (e.g. SN1987A;  $10^8$  Eddington Limit).
- Neutrinos can take the pressure out of the system allowing the supercritical accretion when accretion rate is bigger than  $10^4$  Eddington limit !  
( $T > 1$  MeV : Thermal neutrinos dominates !)

**Q) What is the implications of supercritical accretion?**

THE ASTROPHYSICAL JOURNAL, 541:918–923, 2000 October 1

## HYPERCritical ADVECTION-DOMINATED ACCRETION FLOW

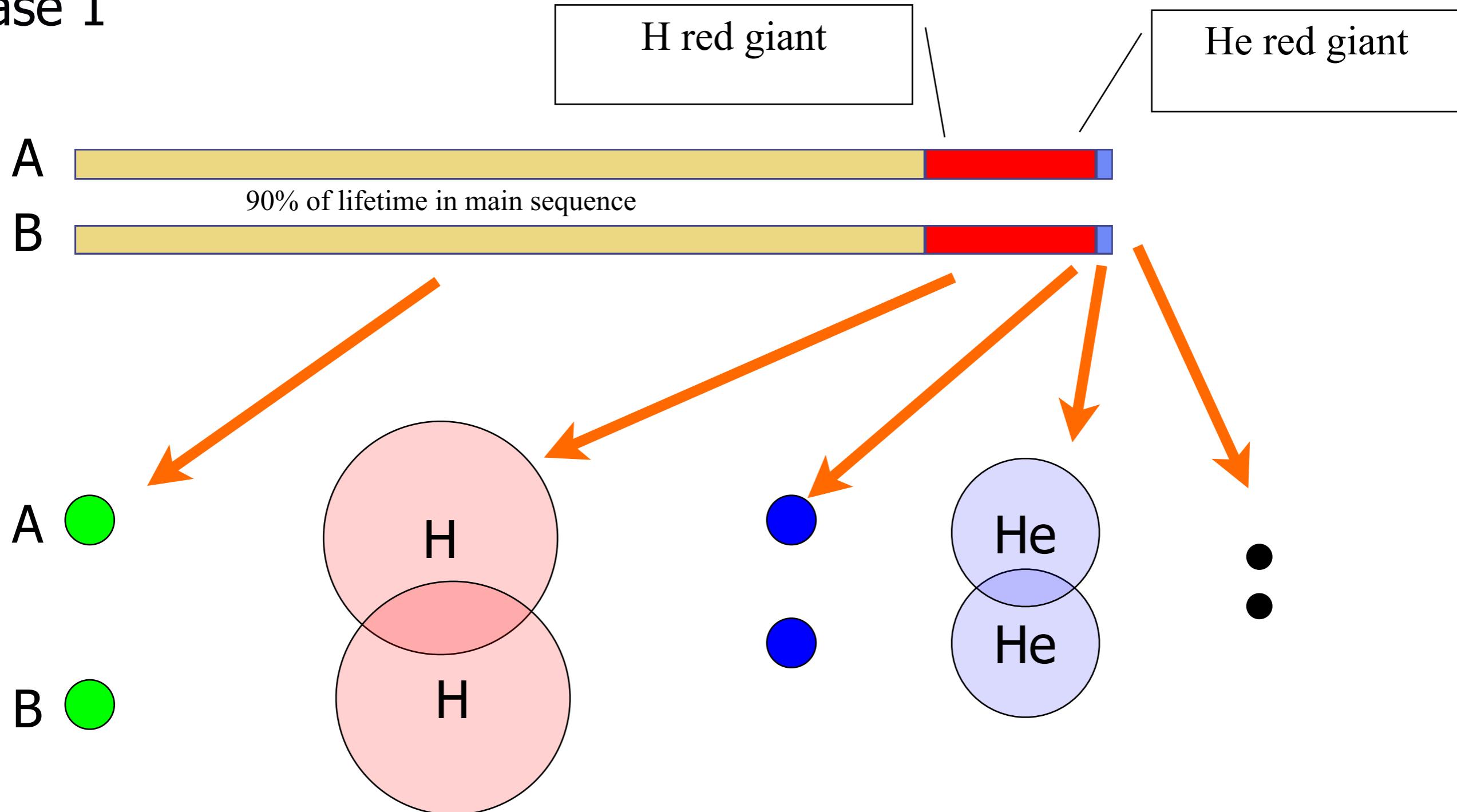
G. E. BROWN AND C.-H. LEE

Department of Physics and Astronomy, State University of New York, Stony Brook, New York 11794

AND

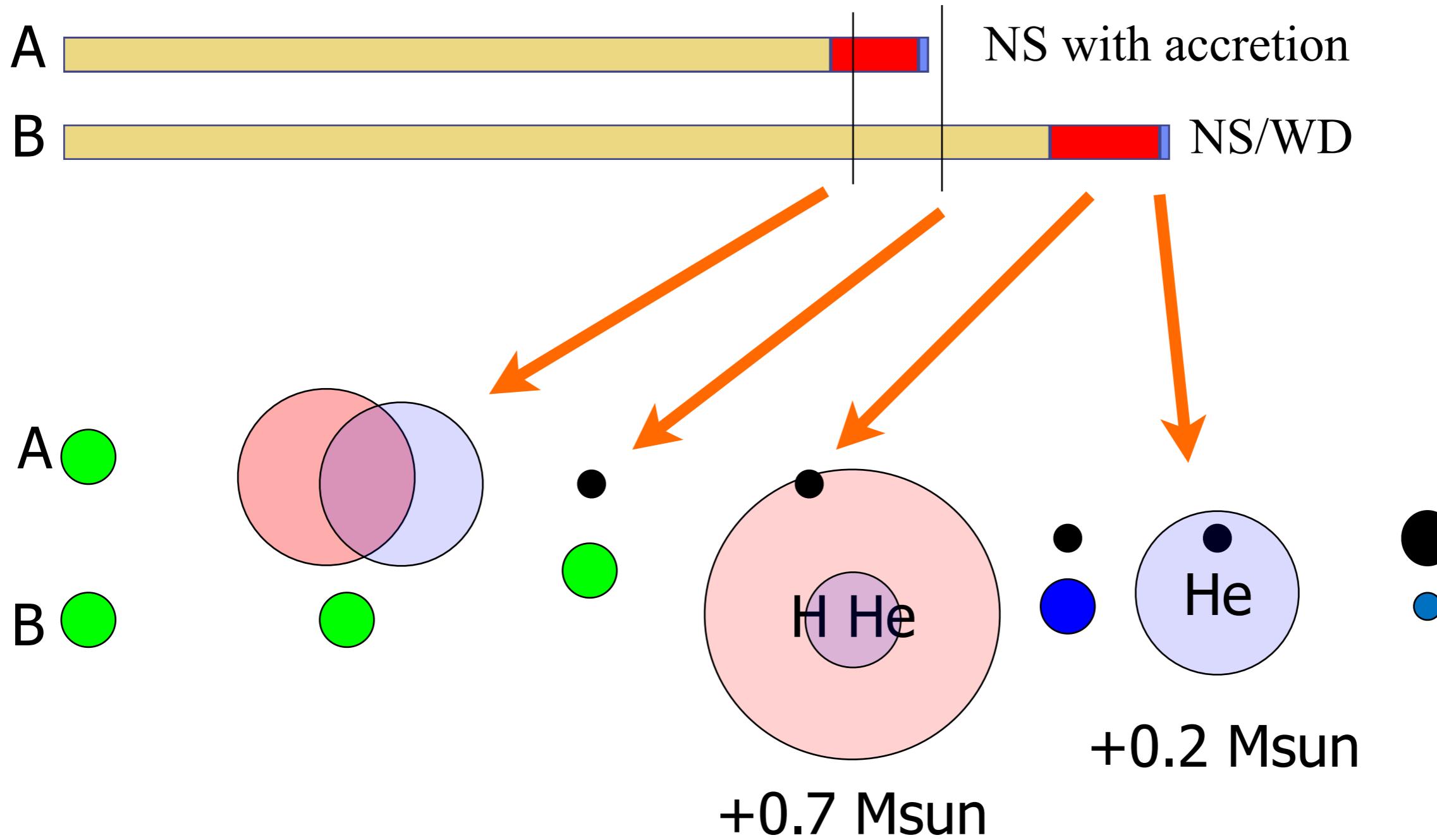
H. A. BETHE

# Case 1



Formation of nearly equal mass NS-NS binary

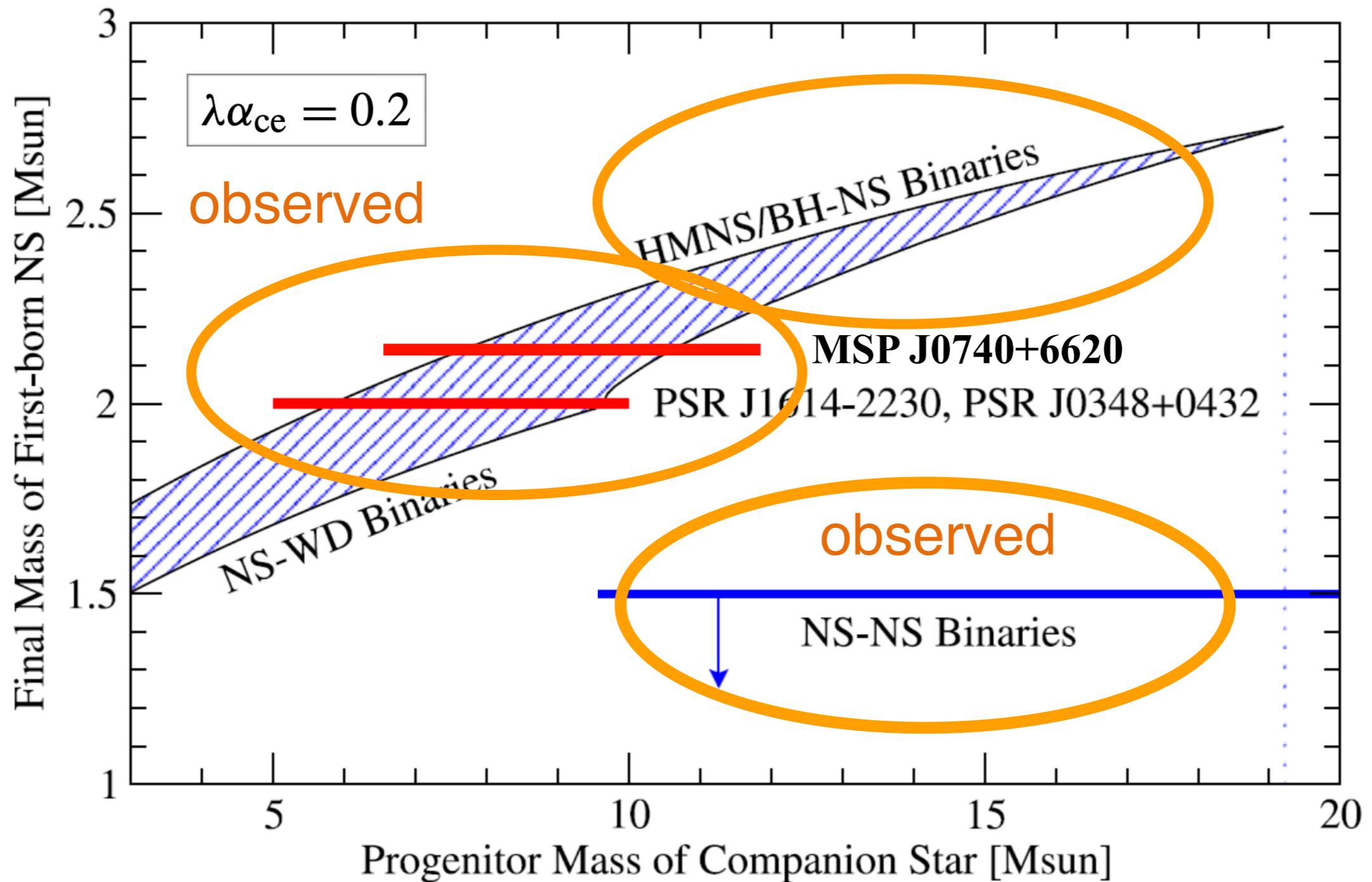
## Case 2



Supercritical Accretion: First born NS can accrete up to  $0.9 M_{\odot}$

# Final mass of first-born NS with supercritical accretion

C.-H. Lee, H.-S. Cho / Nuclear Physics A 928 (2014) 296–304



# Contents

---

## 1. Introduction of RAON

- new rare isotope accelerator in Korea

## 2. Possible origin of high-mass neutron stars

- NS binary evolution

## 3. New development in BUD<sup>2</sup> Collaboration

- KIDS: new energy density functional
- Application of KIDS to NS properties

## 4. Prospects

# KIDS Nuclear Energy Density Functional

- KIDS

Korea: IBS-Daegu-Sungkyunkwan

- Collaboration

- Model construction

P. Papakonstantinou, Y. Lim (IBS), C. H. Hyun (Daegu), T.-S. Park  
(Sungkyunkwan)

- Nuclear structures

H. Gil (Kyungpook) , E. In (Sungkyunkwan) P. Papakonstantinou,  
Y.-H. Song (IBS), C. H. Hyun, Y. Oh (Kyungpook)

- Heavy-ion collision

M. Kim (Pusan), H. Gil, Y. M. Kim (UNIST), P. Papakonstantinou,  
Y. Kim (IBS), C. H. Hyun, C.-H. Lee (Pusan), S. Jeon (McGill)

## Related publication

Phys. Rev. C 97, 014312 (2018)

Phys. Rev. C 98, 065805 (2018)

Phys. Rev. C 99, 064319 (2019)

Phys. Rev. C 100, 014312 (2019)

# Strategy

1. Expand energy density in powers of  $k_F/m_\rho$ .
2. Fix  $\alpha_i$  to  $\rho_0=0.16\text{fm}^{-3}$ ,  $E/A=16.0\text{ MeV}$ ,  $K_0=240\text{ MeV}$  of symmetric nuclear matter (SNM).
3. Fit  $\beta_i$  to the APR EoS of pure neutron matter (PNM).
4. Consider 3, 4, and 5 terms for  $\beta_i$  while fixing  $\alpha_i$  to 3 terms.

$$\mathcal{E}(\rho, \delta) = \mathcal{T}(\rho, \delta) + \sum_{i=0} c_i(\delta) \rho^{1+i/3},$$

$$\rho = \rho_n + \rho_p$$

$$c_i(\delta) = \alpha_i + \delta^2 \beta_i,$$

$$\delta \equiv (\rho_n - \rho_p)/\rho$$

Expansion parameter  $k_F/m_\rho$ : less than 1 even at  $\rho = 8\rho_0$ .

# Result1: validity of systematic expansion

- \* Naturalness: Order of coefficients  $10^{-1} \sim 10^1$
- \* Dimensionless coefficients

$$\boxed{\mathcal{E}_i(\rho, \delta) = c_i(\delta) \rho^{1+i/3} = \left[ \left( \frac{\nu}{6\pi^2} \right)^{1+i/3} c_i(\delta) m_\rho^{2+i} \right] m_\rho \left( \frac{k_F}{m_\rho} \right)^{3+i}}$$

$$c_i^{\text{dim}}(\delta) = \left( \frac{\nu}{6\pi^2} \right)^{1+i/3} c_i(\delta) m_\rho^{2+i}$$

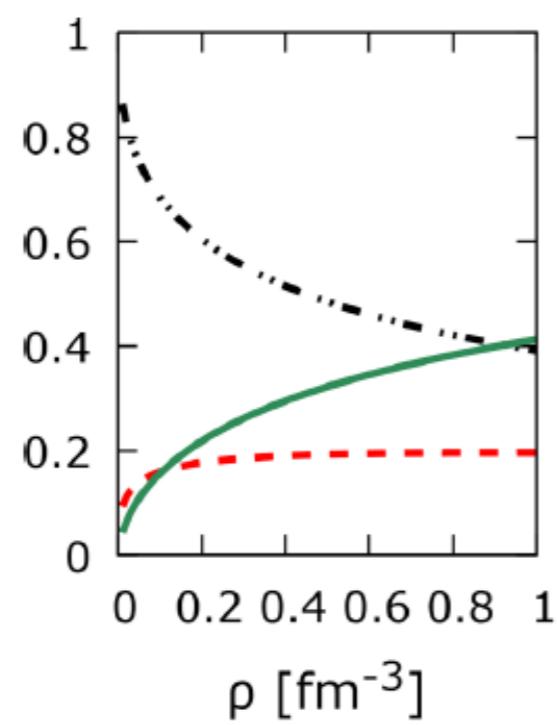
	$c_0^{\text{dim}}$	$c_1^{\text{dim}}$	$c_2^{\text{dim}}$	$c_3^{\text{dim}}$
$\delta=0$	-3.6	6.6	0.6	
$\delta=1$	-1.1	3.4	-5.9	3.3

## Result2: Convergence

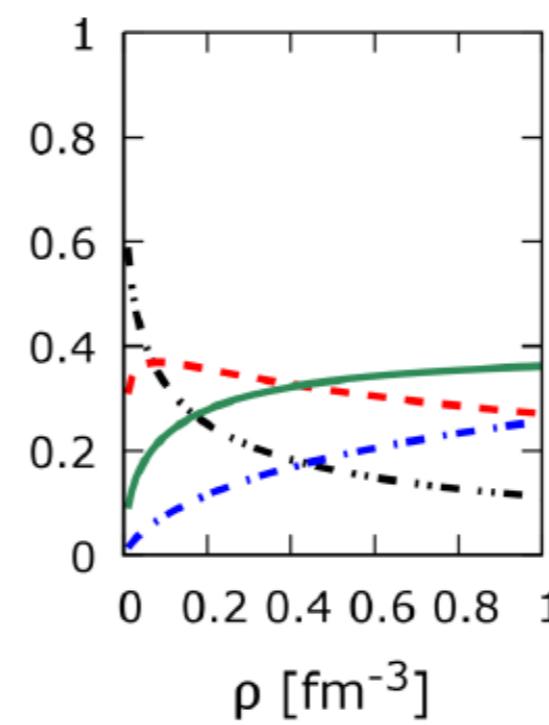
Ratio of magnitude of individual interaction term divided by their sum

Pure Neutron Matter

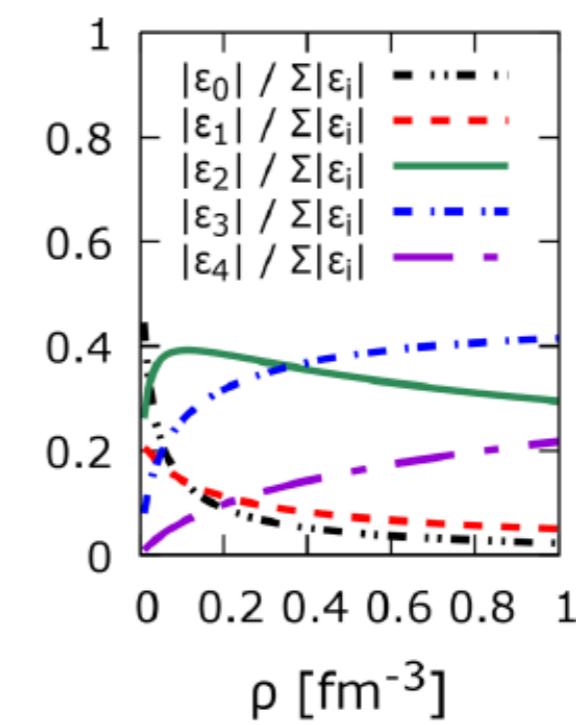
$$\mathcal{E}_i(\rho, \delta) = c_i(\delta)\rho^{1+i/3}$$



(a) P3

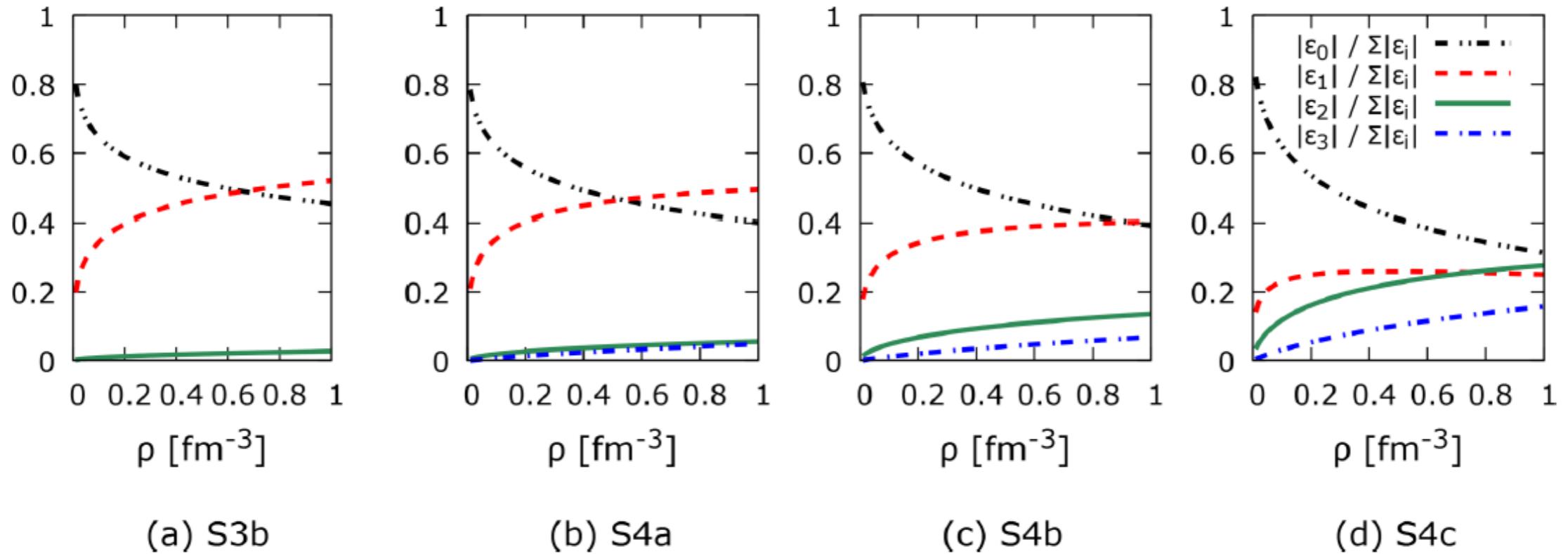


(b) P4



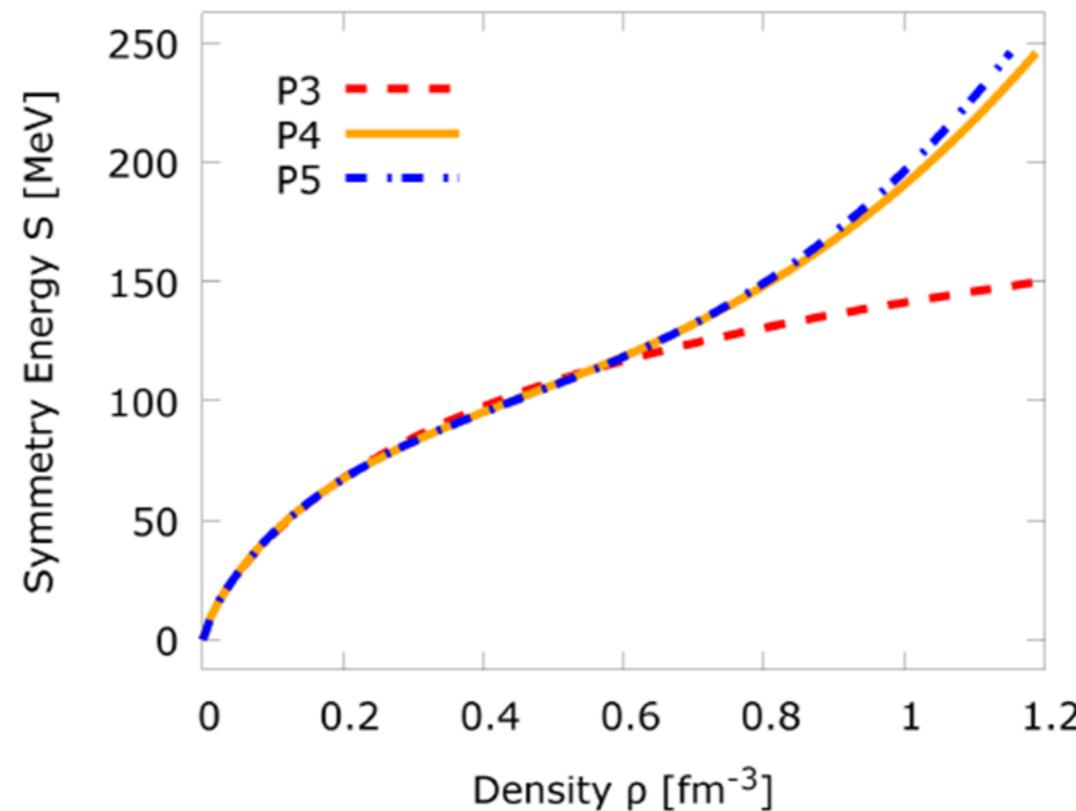
(c) P5

## Symmetric Nuclear Matter



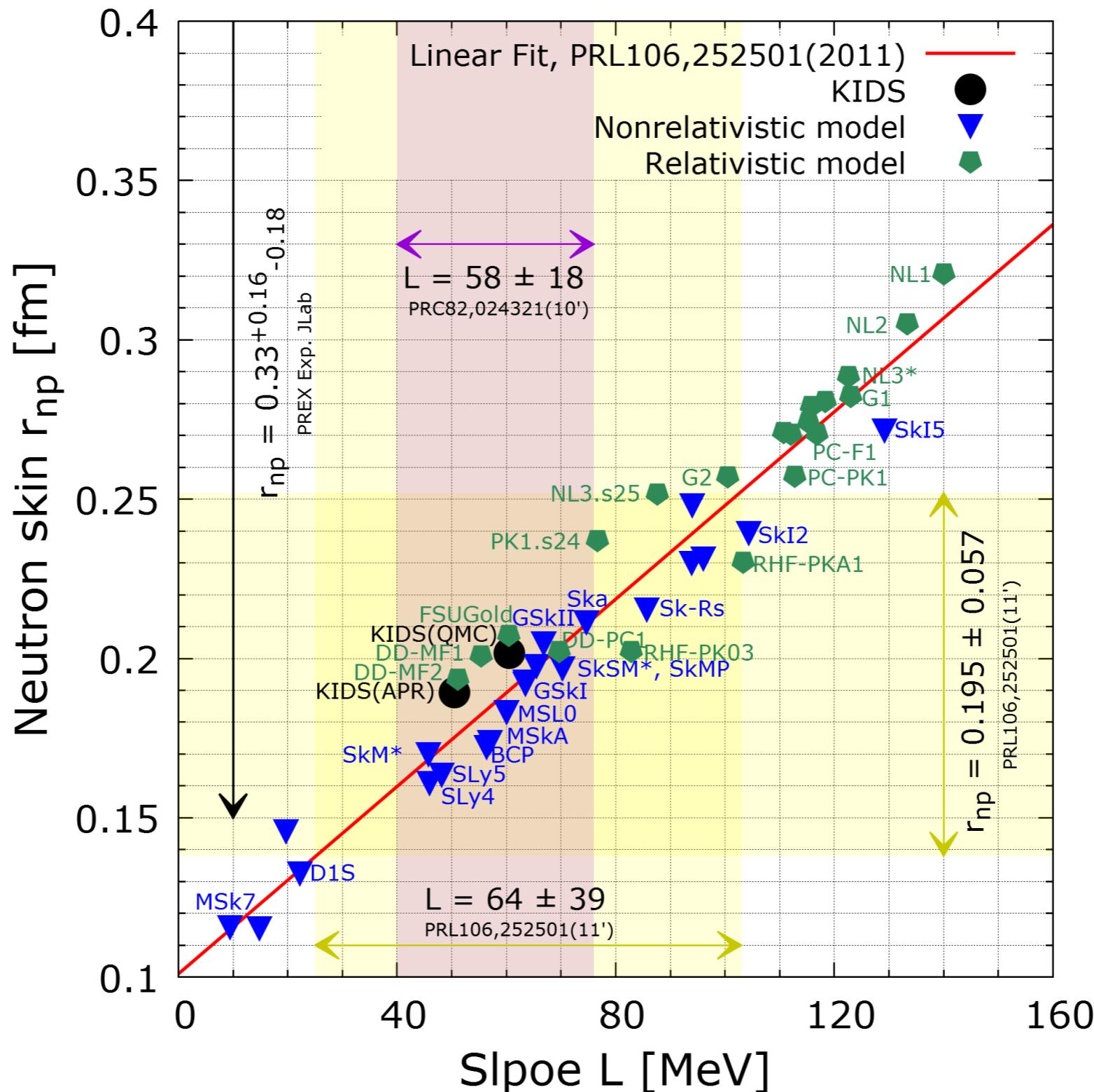
- \* Hierarchy ( $|\varepsilon_0| > |\varepsilon_1| > |\varepsilon_2| > \dots$ ) is valid at low densities.
- \* However, hierarchy is better for SNM.

# Result3: Symmetry Energy



- No difference up to  $\rho \sim 0.6 \text{ fm}^{-3}$  ( $\sim 4\rho_0$ ): Higher order terms ( $\rho^{6/3}, \rho^{7/3}$ ) are negligible.
- Marginal difference between P4 and P5 up to  $\rho \sim 1.2 \text{ fm}^{-3}$  ( $\sim 8\rho_0$ ): Four terms are sufficient for neutron stars.

# Correlation between neutron skin thickness $r_{np}$ and slope parameter L of $^{208}\text{Pb}$

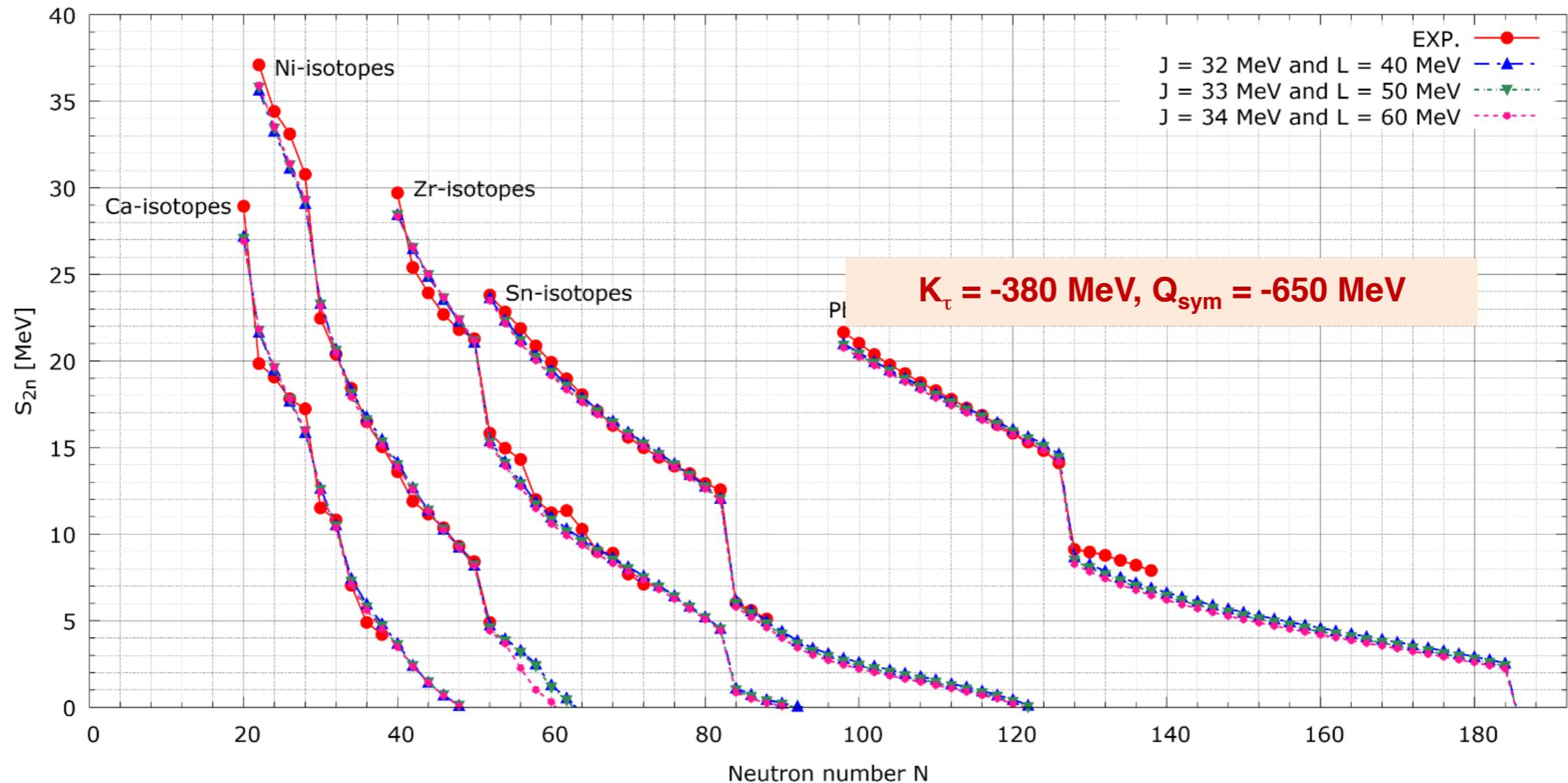


In the KIDS model,  $J$ ,  $L$ ,  $K_{\text{sym}}$ , ... can be chosen arbitrary, so one can check the correlation more systematically.

$$S(\rho) = J + L x + \frac{1}{2} K_{\text{sym}} x^2 + \mathcal{O}(x^3) \quad K_{\tau} \equiv K_{\text{sym}} - 6L - \frac{Q_0}{K_0} L. \quad x \equiv (\rho - \rho_0)/3\rho_0$$

**S<sub>2n</sub>**

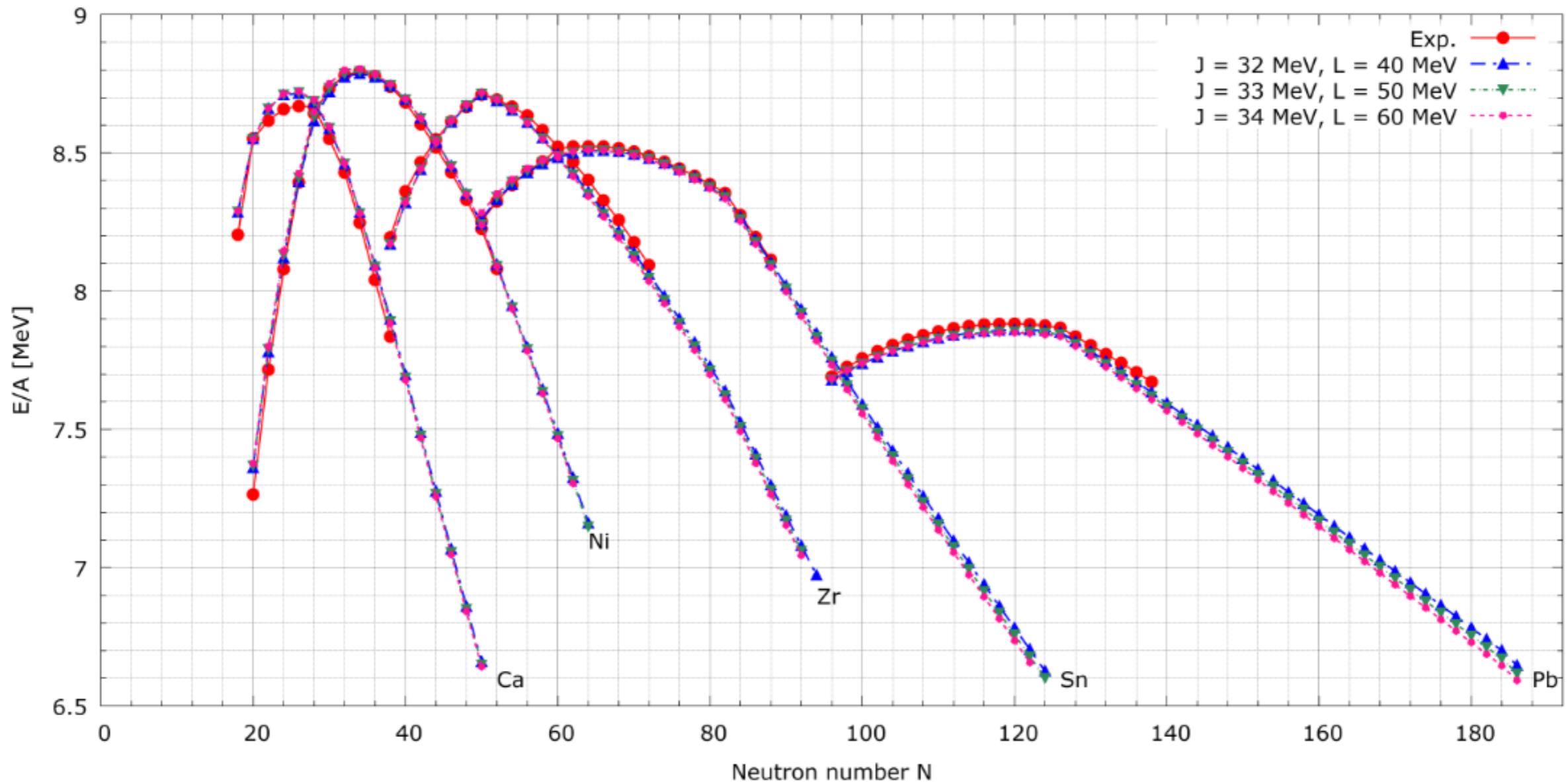
two-neutron separation energy S<sub>2n</sub>



For a given  $K_{\tau}$  One find ( $J$ ,  $L$ ) combinations that can reproduce experimental  $S_{2n}$

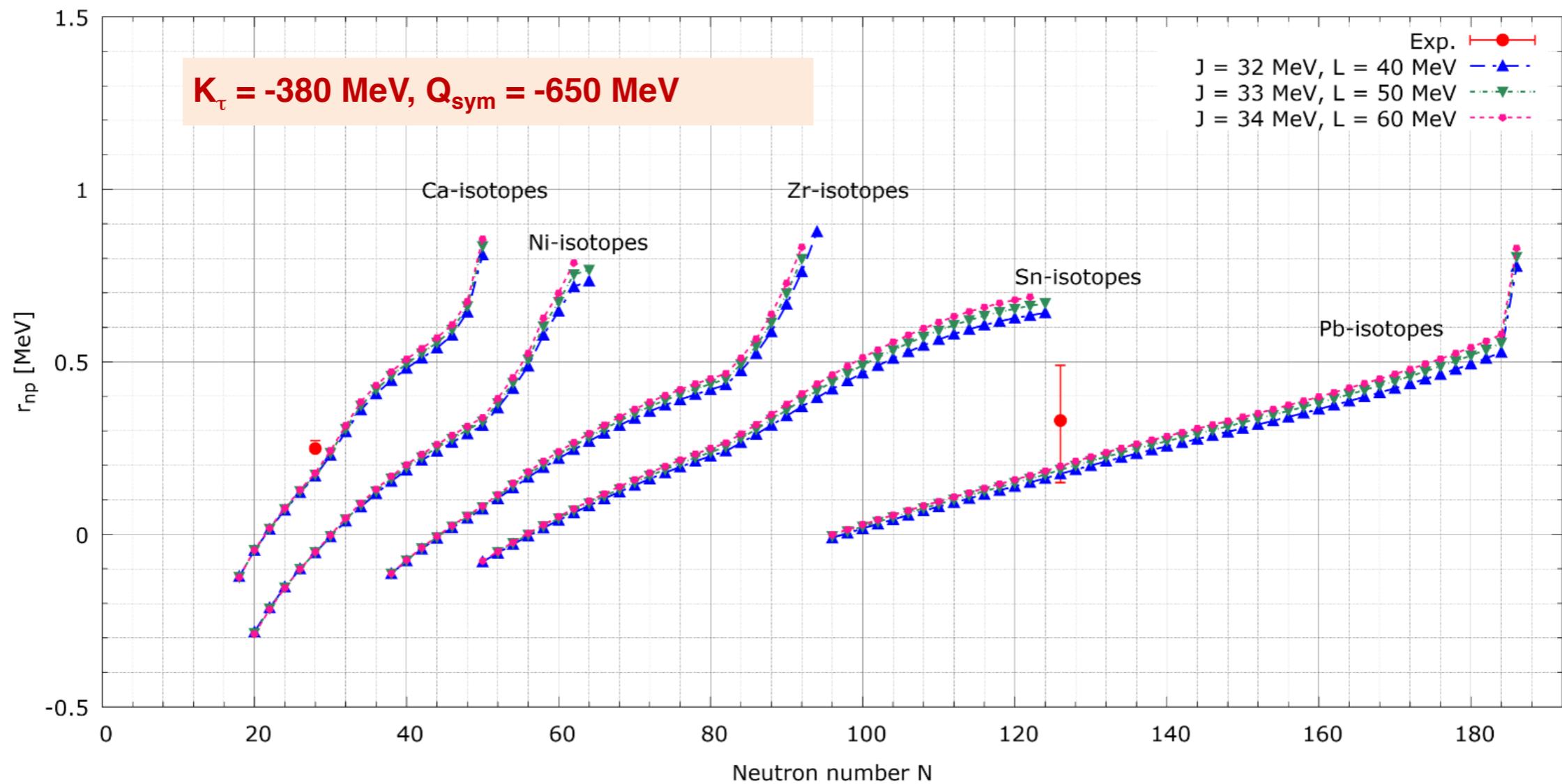
## Binding energy per nucleon

$K_\tau = -380 \text{ MeV}$ ,  $Q_{\text{sym}} = -650 \text{ MeV}$



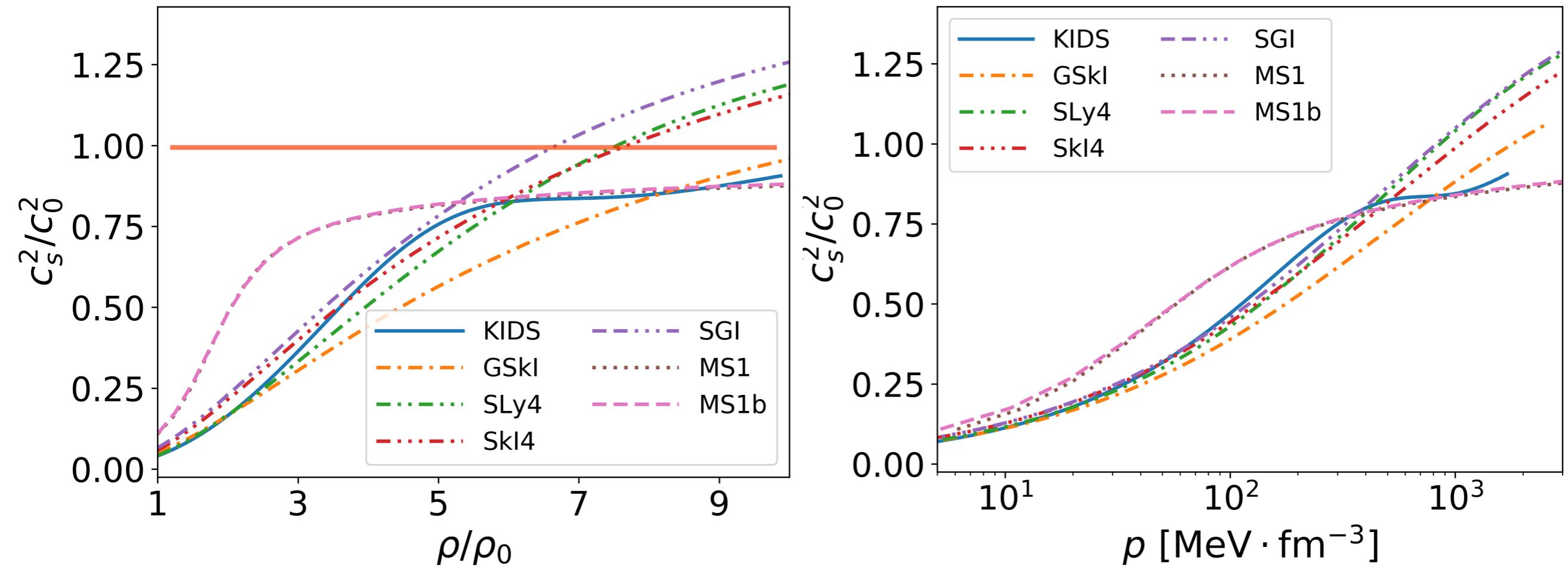
**r<sub>np</sub>**

## neutron skin thickness r<sub>np</sub>



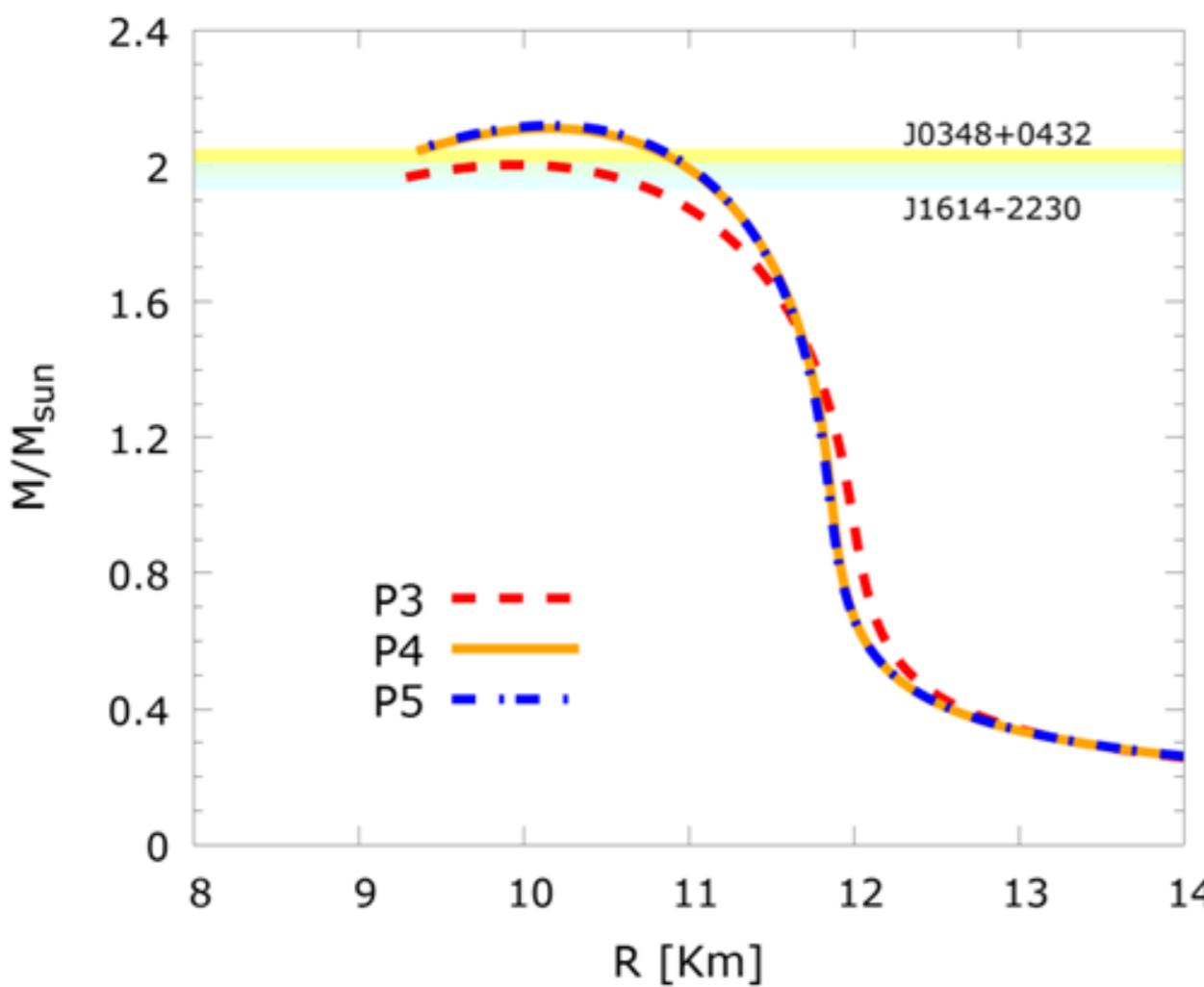
- **J and L can be correlated strongly via  $S_{2n}$  of neutron-rich nuclei.**
- **Measurement of  $r_{np}$ ,  $S_{2n}$  and neutron drip line can provide more stringent constraints and correlations of J, L and  $K_{\text{sym}}$ .**

# speed of sound



# Result4: Neutron Star

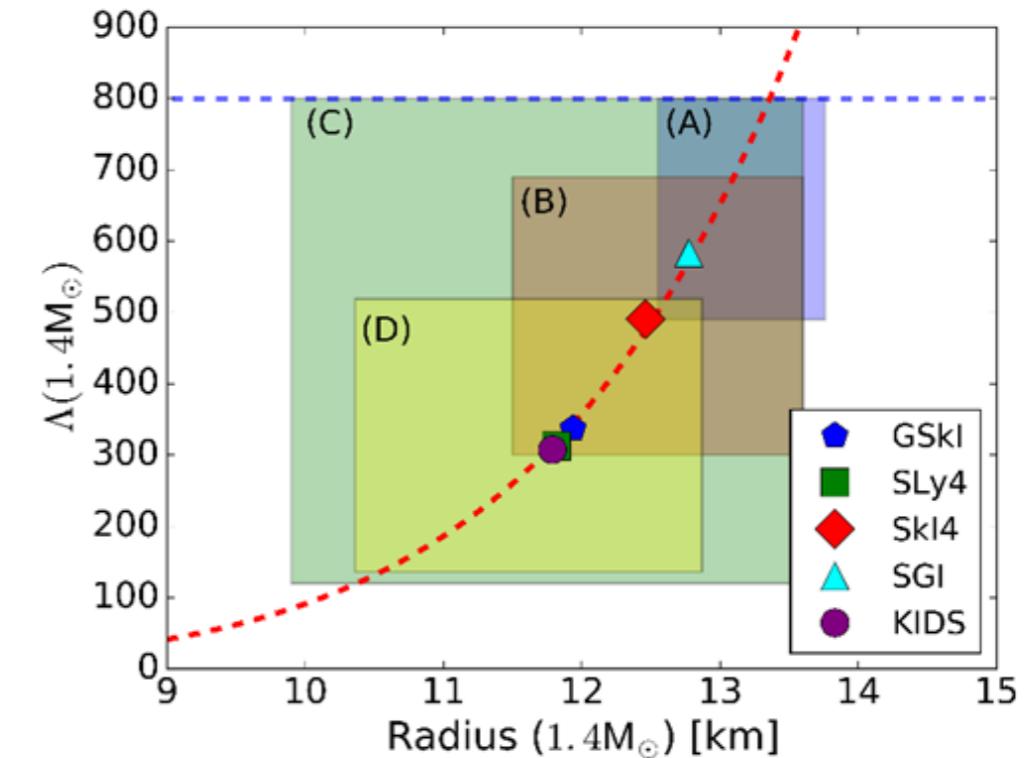
## Mass-Radius Relation



## Tidal Deformability

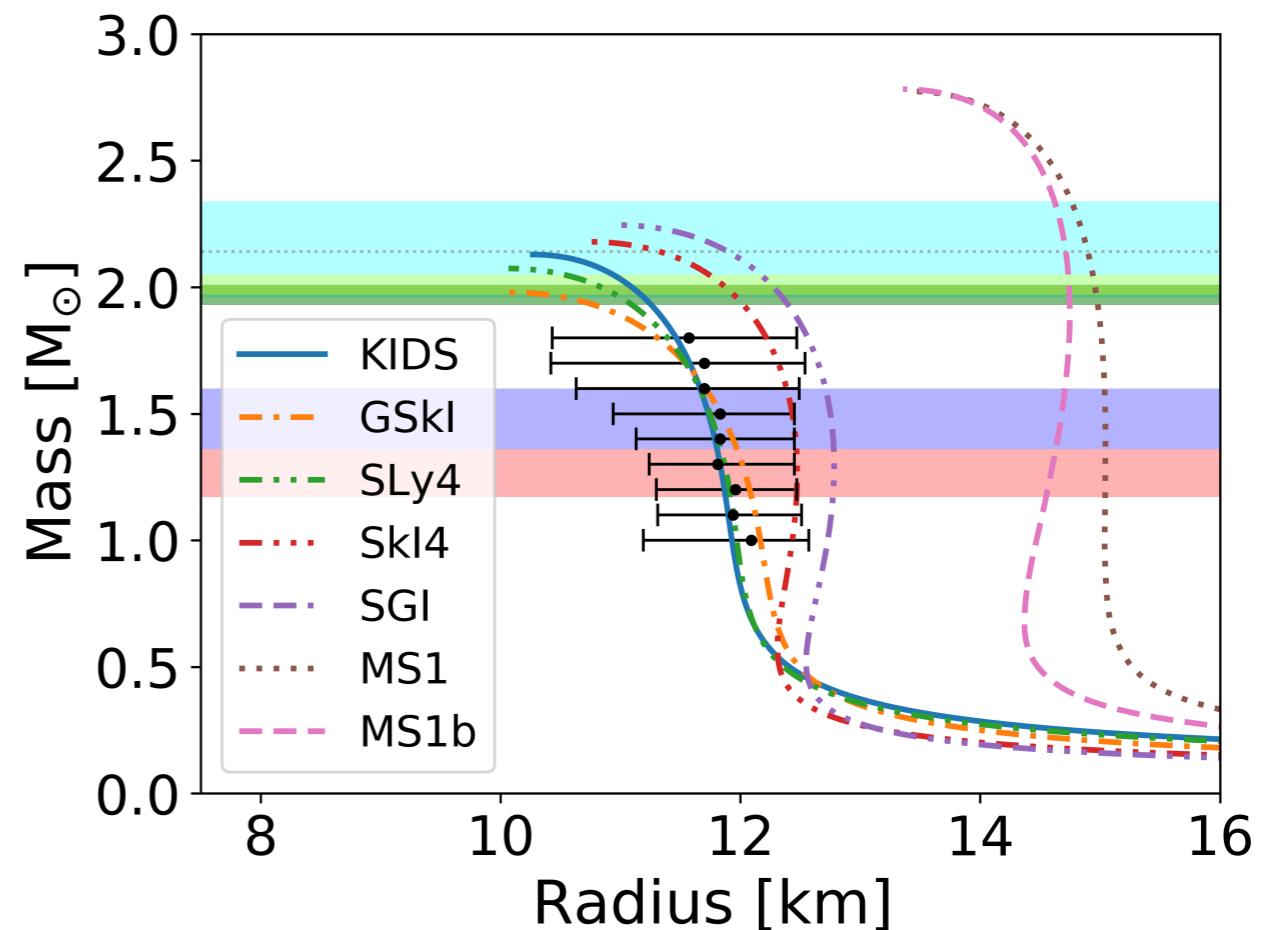
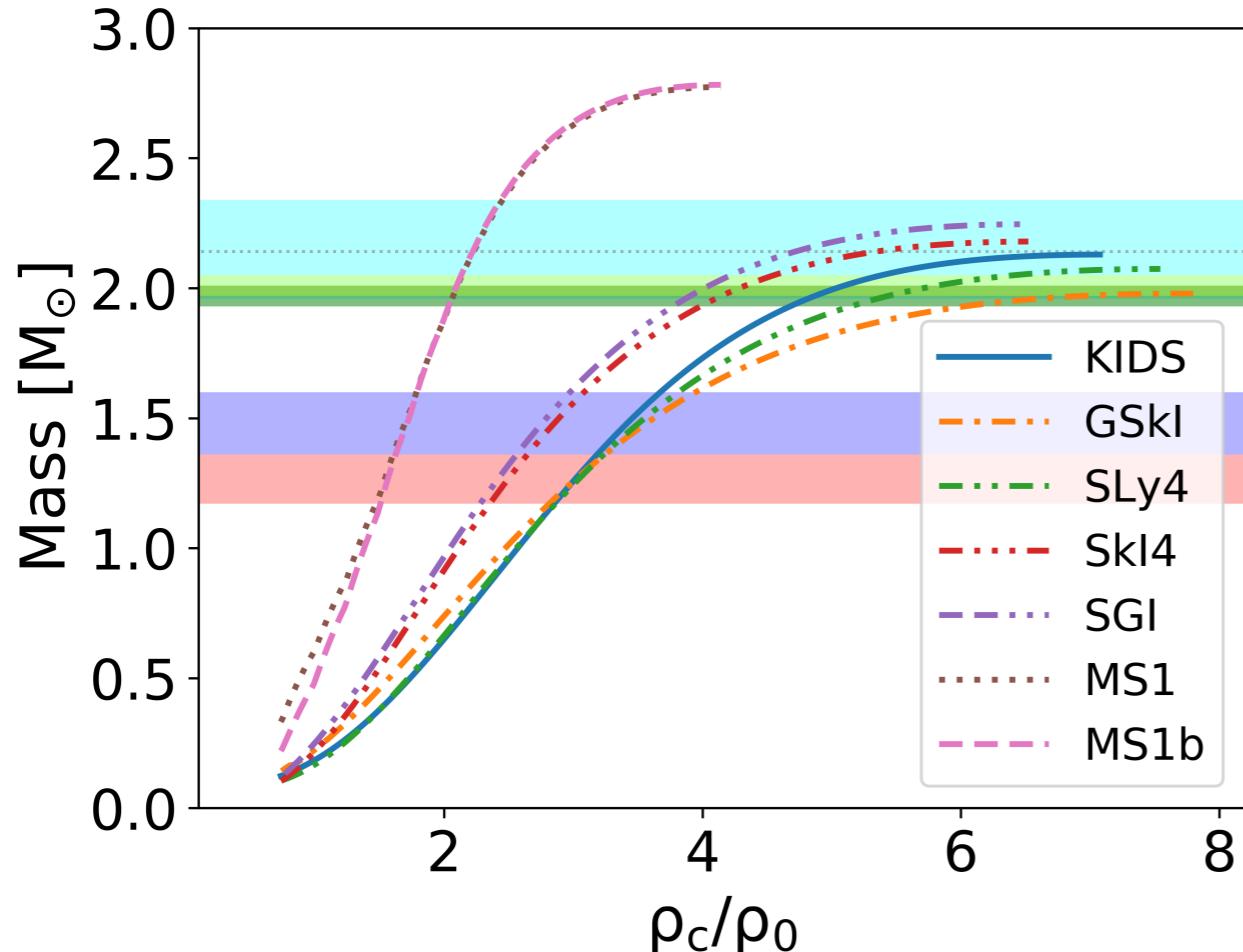
	P3	P4	P5
$\Lambda_{1.4}$	316	304	289

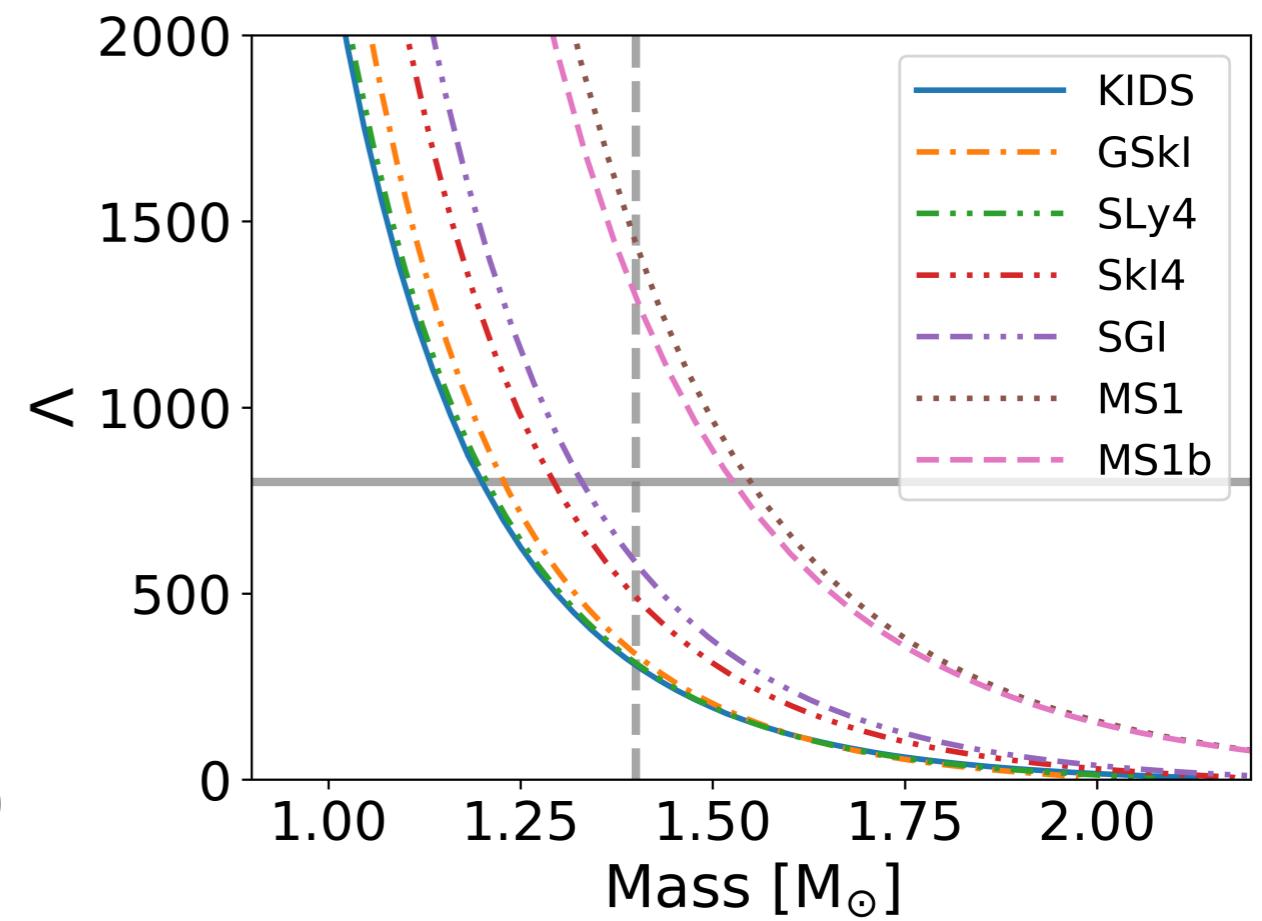
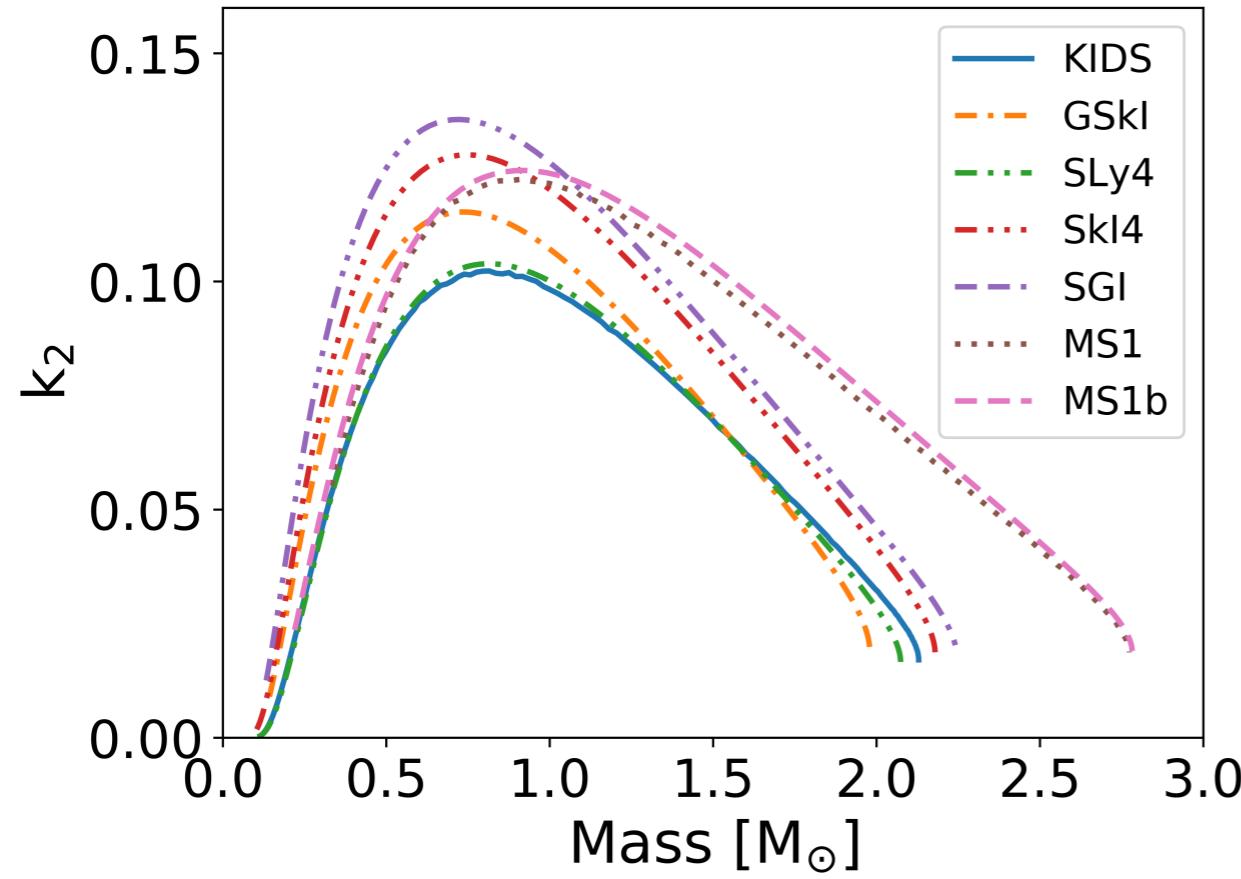
arXiv:180511581v1:  $70 < \Lambda_{1.4} < 580$



Red dot curve:  $\Lambda \propto R^{7.5}$  by E. Annala et al., PRL120(2018)

# Neutron star properties





# Contents

---

## 1. Introduction of RAON

- new rare isotope accelerator in Korea

## 2. Possible origin of high-mass neutron stars

- NS binary evolution

## 3. New development in BUD<sup>2</sup> Collaboration

- KIDS: new energy density functional
- Application of KIDS to NS properties

## 4. Prospects

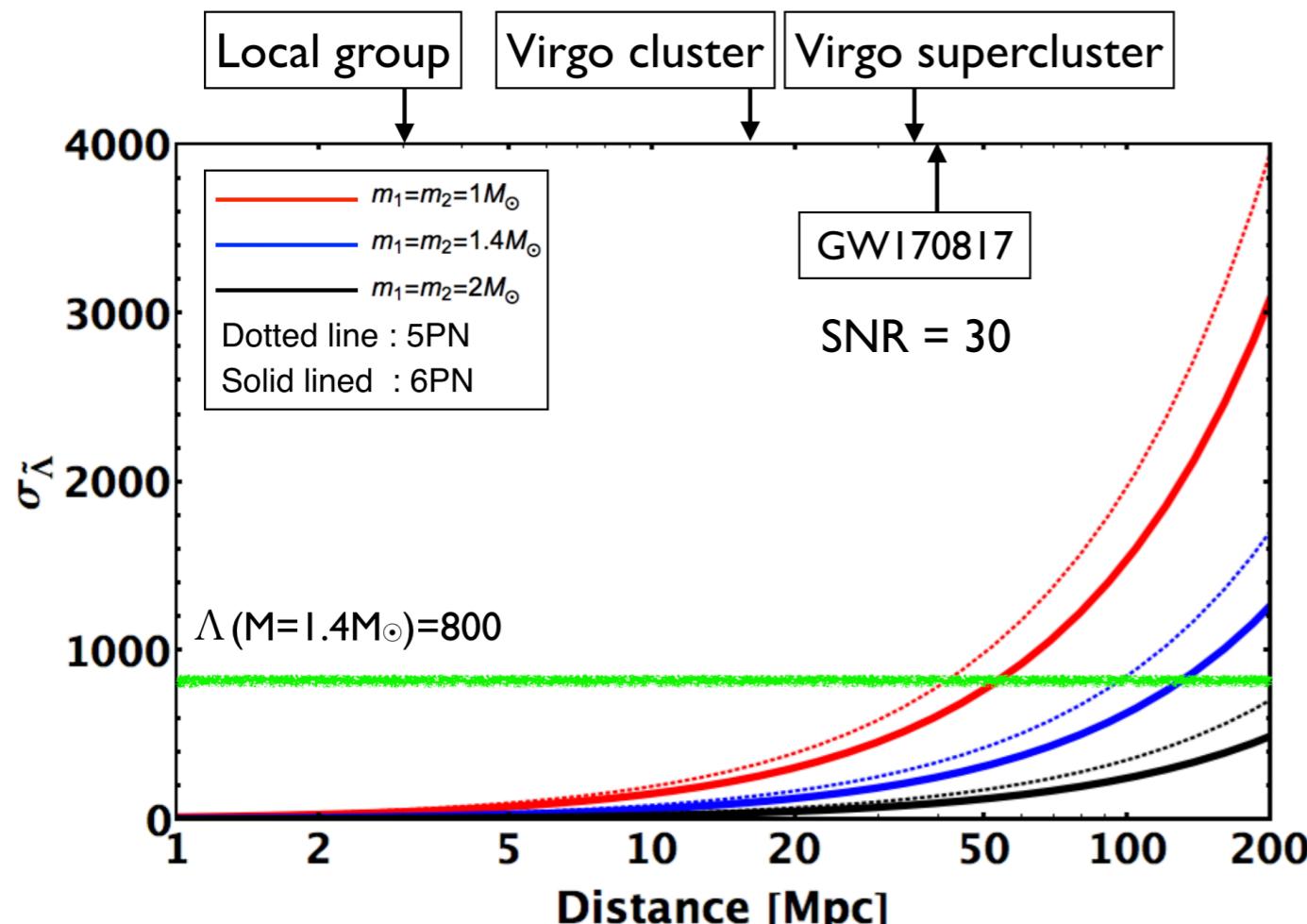
## With RAON & MMA Observation

---

- We developed a new effective model **KIDS**
- We also developed a new transport code **DJBUU**
- With new results from RAON, NICER, and Multi-messenger (GW & EM) observations, we will be able to have better understanding on the physics of dense matter and NS properties.

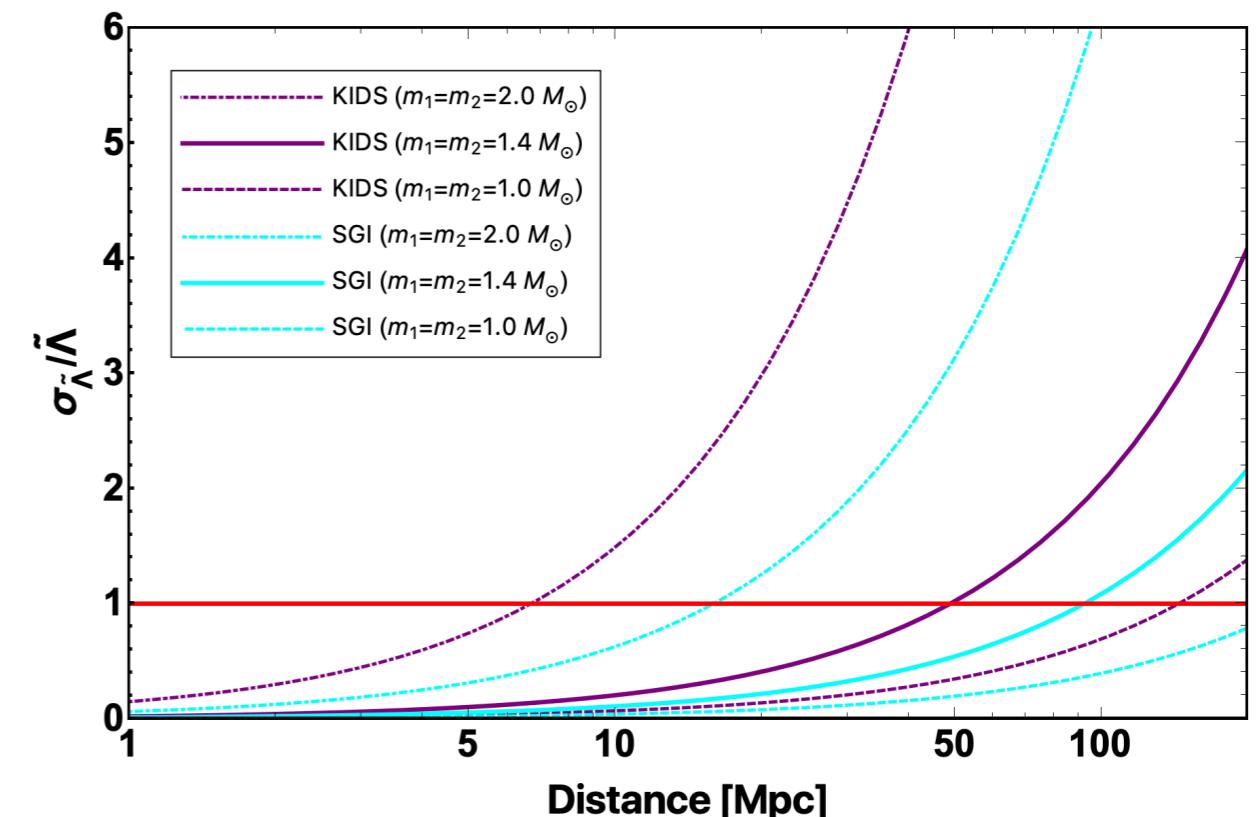
- BUD<sup>2</sup>-McGill Collaboration  
DJBUU (*DaeJeon Boltzmann-Uehling-Uhlenbeck*)  
\*\* DaeJeon is city name in Korea where RAON will be built  
\*\* S. Jeon (McGill) \*\* developed MARTINI for RHIC/LHC

# Measurement error vs. source distance



For one detector with optimal condition

Y.B. Choi, H. S. Cho, Y. Kim, C.-H. Lee



## GW from NS mergers

- April 25, 2019 : NS-NS merger candidate (500 Mly, 153 Mpc)
- April 26, 2019 : NS-BH merger candidate (1.2 Gly, 368 Mpc)

*Binary interactions  
are always interesting*

*Thanks*

