

# ECT\*

EUROPEAN CENTRE FOR THEORETICAL STUDIES  
IN NUCLEAR PHYSICS AND RELATED AREAS

## The Valencia model for neutrino-nucleus interactions

Luis Alvarez Ruso



# Valencia

From Wikipedia, the free encyclopedia

*This article is about the city in Spain. For other uses, see [Valencia \(disambiguation\)](#).*

**Valencia** (/vəˈlɛnsiə/; Spanish: [baˈlenθja]), officially **València** (Valencian: [vaˈlɛnsia]),<sup>[4]</sup> on the east coast of Spain, is the capital of the autonomous community of Valencia and the third-largest city in Spain after Madrid and Barcelona, with around 800,000 inhabitants in the administrative centre. Its urban area extends beyond the

## The Valencia model for neutrino-nucleus interactions

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# Introduction

- Valencia: IFIC (UV, CSIC)
  - Oset, Vicente Vacas, Nieves...
  - Interactions of particles with nucleons and nuclei
    - E.g. with electroweak probes:
      - $\gamma^{(*)}$ ,  $W^{\pm}$ ,  $Z$   $N \rightarrow N'$ ,  $N' \pi$ ,  $N' \pi \pi$ , ...
    - Incoherent (semi-)inclusive scattering in nuclei
    - Coherent particle production
  - Few-GeV/intermediate energy region: hadronic degrees of freedom

# Introduction

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    - Incoherent (semi-)inclusive scattering in nuclei
    - Coherent particle production
  - Few-GeV/intermediate energy region: hadronic degrees of freedom
- First application to neutrino interactions:  
Quasielastic neutrino (anti-neutrino) reactions in nuclei and the axial vector form-factor of the nucleon  
S. K. Singh, E. Oset, NPA542 (1992)

# Elementary processes

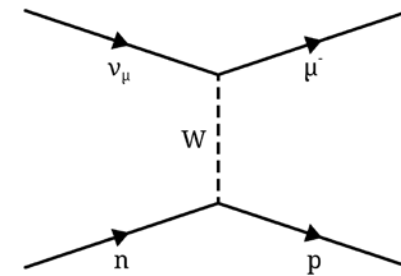
## ■ QE scattering

$$\text{CCQE} : \nu(k) + n(p) \rightarrow l^-(k') + p(p')$$

$$\bar{\nu}(k) + p(p) \rightarrow l^+(k') + n(p')$$

$$\text{NCE} : \nu(k) + N(p) \rightarrow \nu(k') + N(p')$$

$$\bar{\nu}(k) + N(p) \rightarrow \bar{\nu}(k') + N(p')$$



$$\mathcal{M} = \frac{G_F \cos \theta_C}{\sqrt{2}} l^\alpha J_\alpha$$

$$J_\alpha = \bar{u}(p') \left[ \gamma_\alpha F_1^V + \frac{i}{2M} \sigma_{\alpha\beta} q^\beta F_2^V + \gamma_\mu \gamma_5 F_A + \frac{q_\mu}{M} \gamma_5 F_P \right] u(p)$$

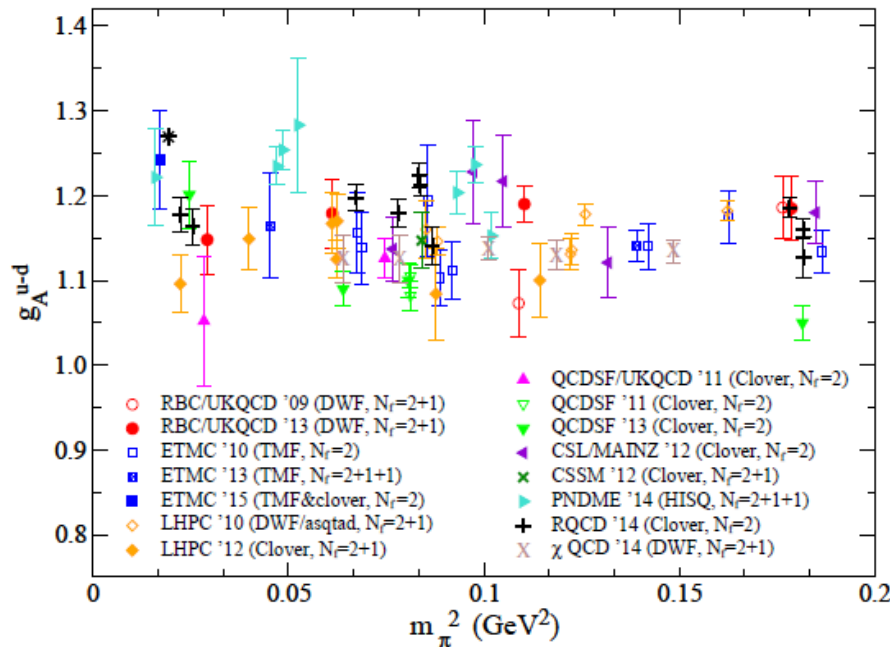
■ **Vector** form factors:  $F_{12}^V = F_{12}^p - F_{12}^n \leftarrow$  isospin symmetry

■ **Axial** form factors:

$$F_A(Q^2) = g_A F(Q^2), \quad F_P(Q^2) = \frac{2M^2}{Q^2 + m_\pi^2} F_A(Q^2), \quad Q^2 = -q^2 > 0$$

# $F_A$ & LQCD

- $g_A$  : **lower** than exp. values have been recurrently obtained



Constantinou, PoS CD15 (2015) 009

- Recent progress:
  - improved algorithms for a careful treatment of excited states
  - low pion masses
  - A per-cent-level determination of the nucleon **axial coupling** from QCD

Chang et al., Nature 558 (2018)

# $F_A$ & LQCD

## Recent progress:

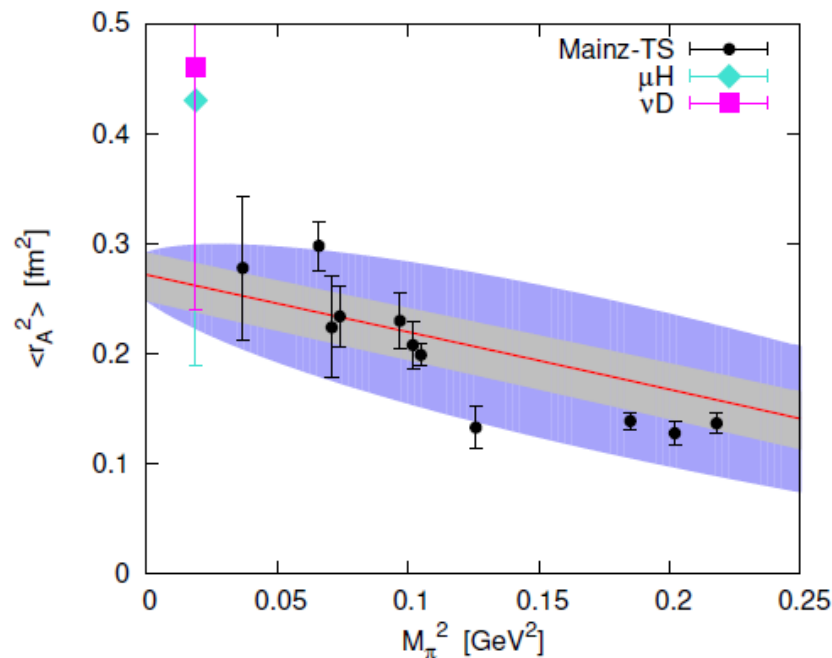
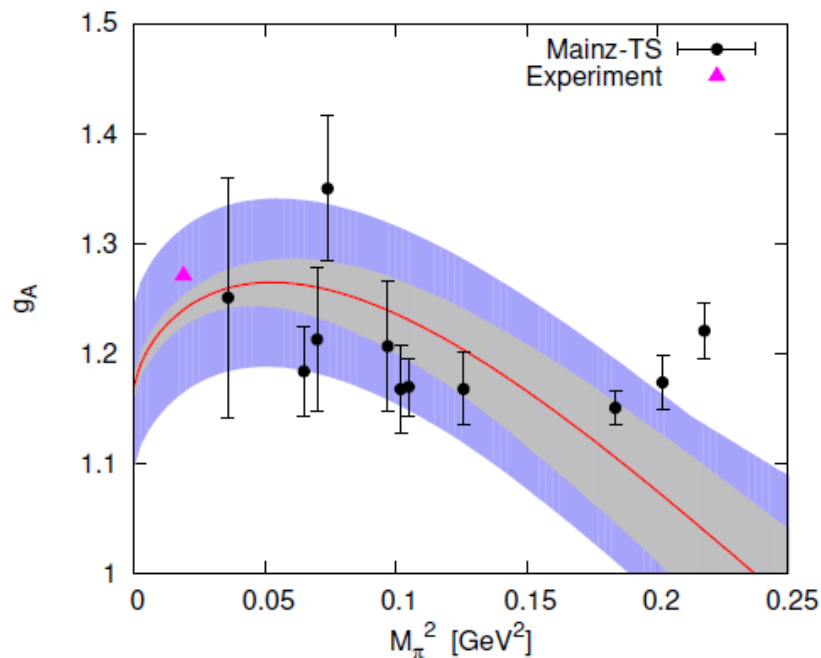
Alexandrou et al., PRD 96 (2017)

Capitani et al., arXiv:1705.06186

Gupta et al., PRD 96 (2017)

## Baryon ChPT analysis: Yao, LAR, Vicente Vacas, PRD 96 (2017)

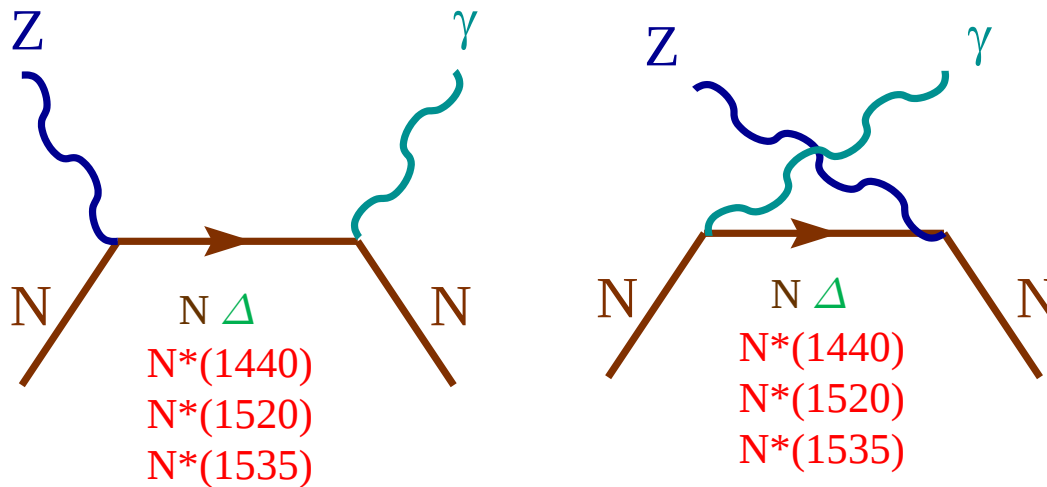
- $O(p^3)$ ,  $Q^2 < 0.36 \text{ GeV}^2$ ,  $130 \text{ MeV} < M_\pi < 473 \text{ MeV}$ , explicit  $\Delta(1232)$



- $g_A = 1.237(74)$ ,  $\langle r_A^2 \rangle = 0.263(38) \text{ fm}^2$

# Elementary processes

- Meson production:  $\nu_l N \rightarrow l N' \pi$  ← Eli's talk on Monday  
 $\nu_l N \rightarrow l N' \eta$  Alam, LAR, Vicente Vacas, in preparation
- NC photon emission:  $\nu_l N \rightarrow \nu_l N' \gamma$  Wang, LAR, Nieves, PRC89 (2014)



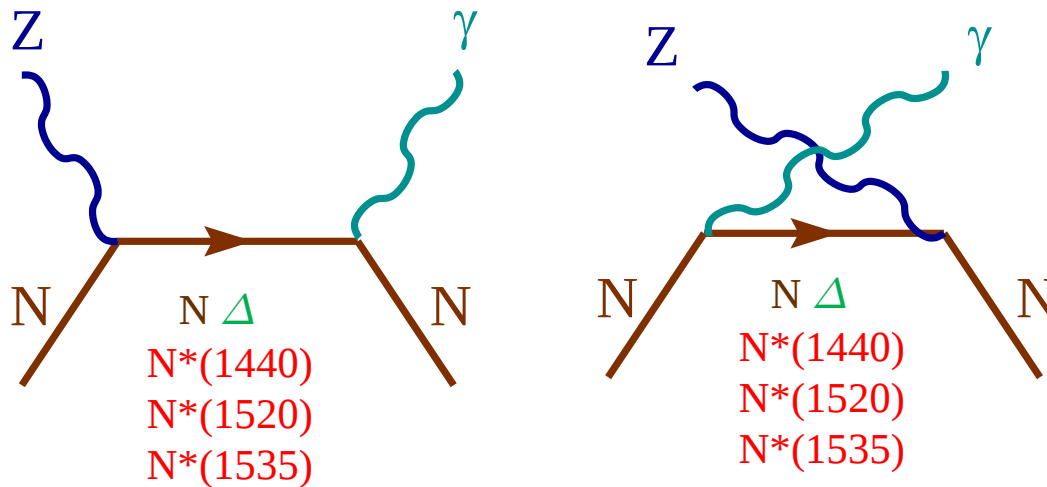
- Weak vector and EM  $N$ ,  $N$ - $\Delta$  and  $N$ - $N^*$  form factors extracted from electron scattering experiments

# Elementary processes

■ Meson production:  $\nu_l N \rightarrow l N' \pi$  ← Eli's talk on Monday

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■ NC photon emission:  $\nu_l N \rightarrow \nu_l N' \gamma$  Wang, LAR, Nieves, PRC89 (2014)



■ Weak axial  $N$ ,  $N-\Delta$  and  $N-N^*$  form factors:

■ (off-)diagonal **Goldberger-Treiman** relations for leading couplings

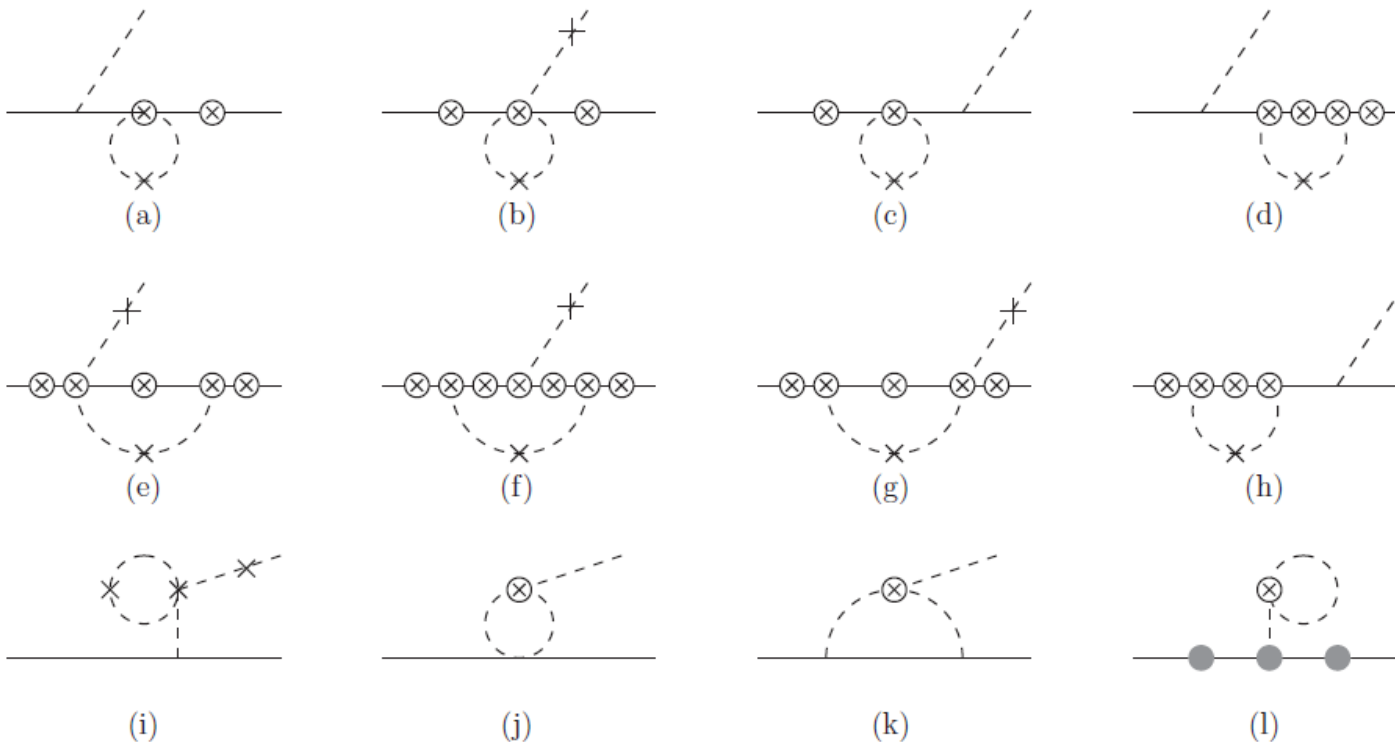
■  $q^2$  dependence: dipole

■  $N-\Delta$ : consistent with  $\nu_\mu d \rightarrow \mu^- \pi^+ p n$  ANL, BNL data

■  $N-N^*$ : estimated ( $M_A = 1$  GeV)

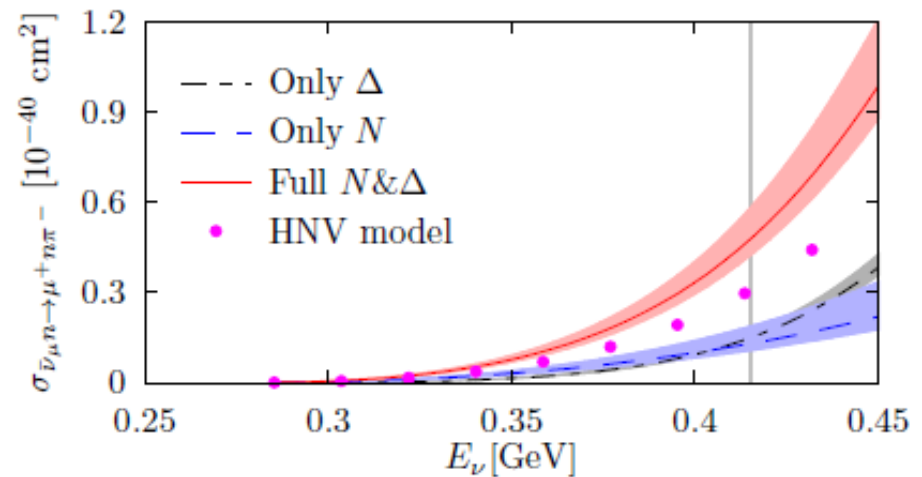
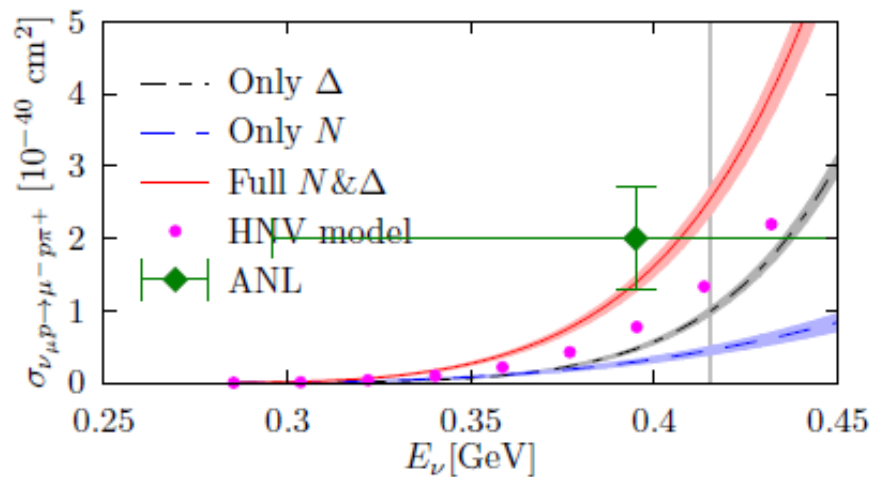
# Weak pion production in BChPT

- Yao, LAR, Hiller, Vicente Vacas, PRD 98 (2018);  
Yao, LAR, Vicente Vacas, arXiv:1901.00773, PLB (2019)
- First comprehensive study in ChPT
- $O(p^3)$  in EOMS regularization scheme
- Explicit  $\Delta(1232)$ , in the  $\delta$ -counting:  $\delta = m_\Delta - m_N \sim O(p^{1/2})$



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- Valid only close to threshold
- Benchmark for phenomenological models



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- Explicit  $\Delta(1232)$ , in the  $\delta$ -counting:  $\delta = m_\Delta - m_N \sim O(p^{1/2})$
- LECs :
  - 22 in total (CC case)
  - 7 unknown (but not very relevant)
    - 4 of them can be extracted from pion electroproduction
  - information about remaining 3 LEC could be obtained from **new** close-to-threshold **measurements** of  $\nu$ -induced  $\pi$  production on protons

# Elementary processes

- Strangeness production

- $\Delta S = 1$

- Kaon:  $\nu_l p \rightarrow l^- K^+ p$

$$\nu_l n \rightarrow l^- K^0 p$$

$$\nu_l n \rightarrow l^- K^+ n$$

Alam, Ruiz Simo, Athar, Vicente Vacas,  
PRD82 (2010)

- Background for proton decay  $p \rightarrow \nu K^+$

# Elementary processes

- Strangeness production

- $\Delta S = -1$  :

- Hyperon
  - $\bar{\nu}_l p \rightarrow l^+ \Sigma^0(\Lambda)$
  - $\bar{\nu}_l n \rightarrow l^+ \Sigma^-$

← Asia's talk on Tue

- Additional source of pions:  $Y \rightarrow N \pi$

- antiKaon:  $\bar{\nu}_l p \rightarrow l^+ K^- p$

Alam, Ruiz Simo, Athar, Vicente Vacas,  
PRD85 (2012)

$$\bar{\nu}_l p \rightarrow l^+ \bar{K}^0 n$$

$$\bar{\nu}_l n \rightarrow l^+ K^- n$$

- $\Sigma \pi$ :  $\bar{\nu}_l p \rightarrow l^+ \Sigma^0 \pi^0$

$$\bar{\nu}_l p \rightarrow l^+ \Sigma^+ \pi^-$$

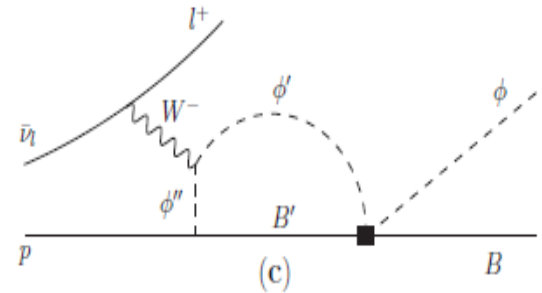
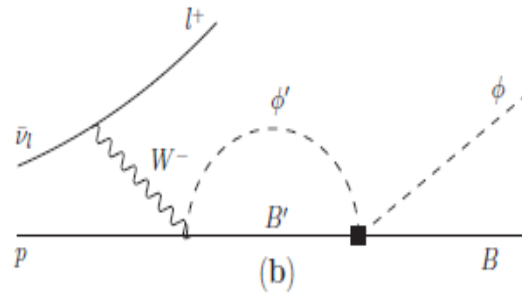
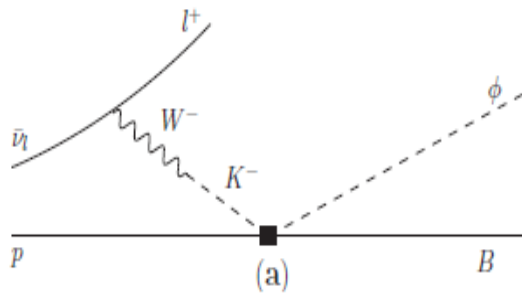
$$\bar{\nu}_l p \rightarrow l^+ \Sigma^- \pi^+$$

# Elementary processes

- Strangeness production

- $\bar{\nu}_l p \rightarrow l^+ \Sigma \pi$

- Ren, Oset, LAR, Vicente Vacas, PRC91 (2015)



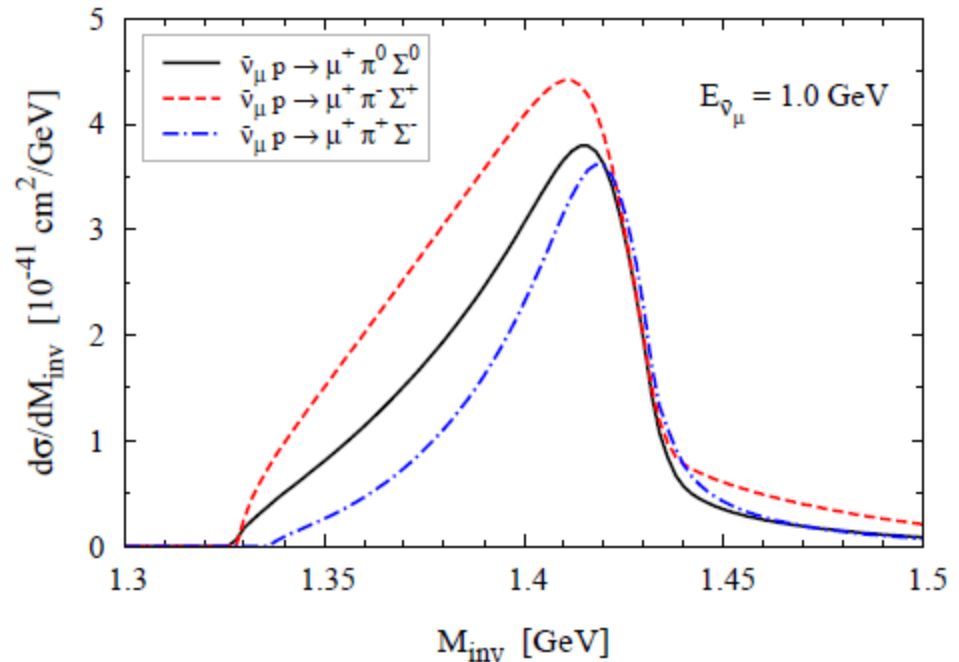
- T: Solution of the Bethe-Salpeter eq. in coupled channels

$$T = V + VGT = [1 - VG]^{-1}V$$

- V: from leading order chiral Lagrangian

# Elementary processes

- Strangeness production
- $\bar{\nu}_l p \rightarrow l^+ \Sigma \pi$
- Ren, Oset, LAR, Vicente Vacas, PRC91 (2015)
- $\Lambda(1405)$  dynamically generated
- Two poles:
  - $M \approx 1385 \text{ MeV}, \Gamma \approx 150 \text{ MeV}$
  - $M \approx 1420 \text{ MeV}, \Gamma \approx 40 \text{ MeV}$



# Incoherent scattering on nuclei

- **Many-body** framework in **infinite** nuclear matter
- $\Rightarrow$  **finite nuclei**: local density approximation  $\rho_{n,p}(r)$ 
  - 👉 cannot describe  $\omega \sim 10$ s MeV, **shell** effects, **giant resonances** (only accounts for their average strength)
  - 👉 simplicity
  - 👉 relativistic (in principle)
  - 👉 applicable for any nucleus with  $A \gtrsim {}^{12}\text{C}$  with **theoretically** or **experimentally** known  $\rho_{n,p}(r)$
  - 👉 applicable for **incoherent** (inclusive in the excited states of the **residual target**) processes

# $\nu$ -A scattering

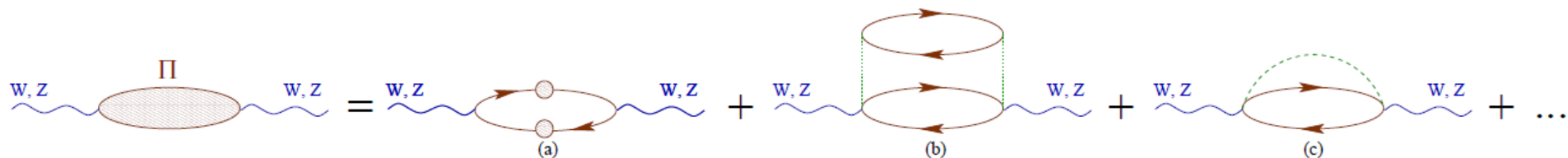
- **Inclusive cross section** per unit volume  
(well defined for an extended system)

$$\frac{d}{d^3r} \left( \frac{d\sigma}{dk'_0 d\Omega(\vec{k}')} \right) = \frac{G_F^2}{(2\pi)^2} \frac{|\vec{k}'|}{k_0} L_{\mu\nu} W^{\mu\nu}$$

$$W^{\alpha\beta} = W_s^{\alpha\beta} + iW_a^{\alpha\beta}$$

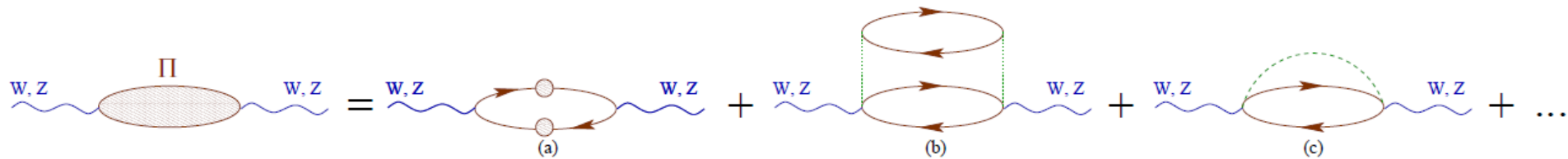
$$W_{(s,a)}^{\alpha\beta} = -\frac{1}{\pi} \text{Im} \Pi_{(s,a)}^{\alpha\beta}$$

- Polarization propagator:



# Polarization propagator

$$W_{(s,a)}^{\alpha\beta} = -\frac{1}{\pi} \text{Im} \Pi_{(s,a)}^{\alpha\beta}$$



■ Cutkosky rules:

$$\text{Im} \left[ \text{W,Z} \text{---} \text{loop} \text{---} \text{W,Z} \right] = \text{W,Z} \text{---} \text{loop} \text{---} \text{W,Z} = \text{cut}$$

■ Free **nucleon** propagator:

$$D(p) = (\not{p} + M)G_0(p)$$

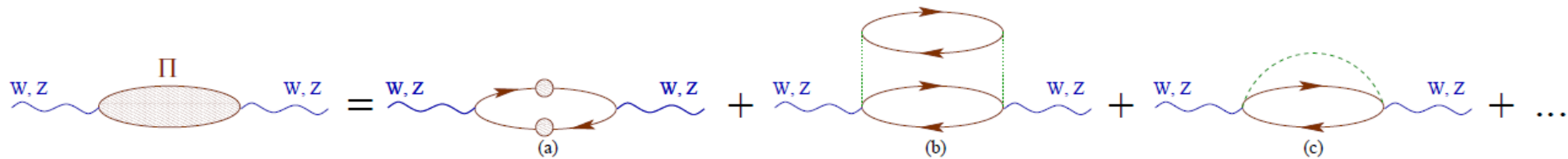
$$G_0(p) = \frac{1}{p^2 - M^2 + i\epsilon} + 2\pi i \delta(p^2 - M^2) \theta(p^0) n(\vec{p})$$

$$= \frac{n(\vec{p}) \theta(p^0)}{p^2 - M^2 - i\epsilon} + \frac{1 - n(\vec{p}) \theta(p^0)}{p^2 - M^2 + i\epsilon}$$

$$= \frac{1}{p^0 + E_p - i\epsilon} \left[ \frac{n(\vec{p})}{p^0 - E_p - i\epsilon} + \frac{1 - n(\vec{p})}{p^0 - E_p + i\epsilon} \right]$$

# Polarization propagator

$$W_{(s,a)}^{\alpha\beta} = -\frac{1}{\pi} \text{Im} \Pi_{(s,a)}^{\alpha\beta}$$



■ Cutkosky rules:

$$\text{Im} \left[ \text{W,Z} \text{ loop } \text{W,Z} \right] = \text{W,Z} \text{ loop } \text{W,Z} = \text{cut diagram}$$

The diagram shows the imaginary part of a fermion loop with external W and Z bosons, which is equal to the loop with a vertical cut line, which is then equal to a diagram with a cut line and an arrow.

■ Free **nucleon** propagator:

$$D(p) = (\not{p} + M)G_0(p)$$

$$G_0(p) = \frac{1}{p^2 - M^2 + i\epsilon} + 2\pi i \delta(p^2 - M^2) \theta(p^0) n(\vec{p})$$

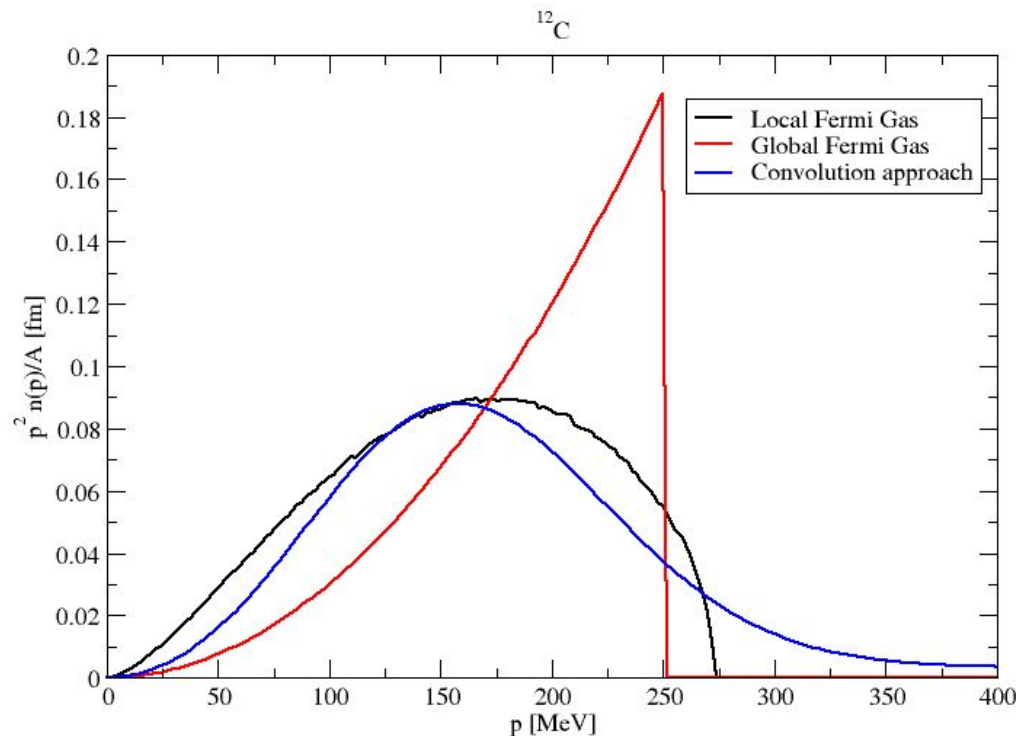
$$n(p, r) = \theta(p_F(r) - p) \quad p_F(r) = \left[ \frac{3}{2} \pi^2 \rho_{p,n}(r) \right]^{1/3}$$



⇔ Relativistic **Local** Fermi Gas

# Local Fermi Gas

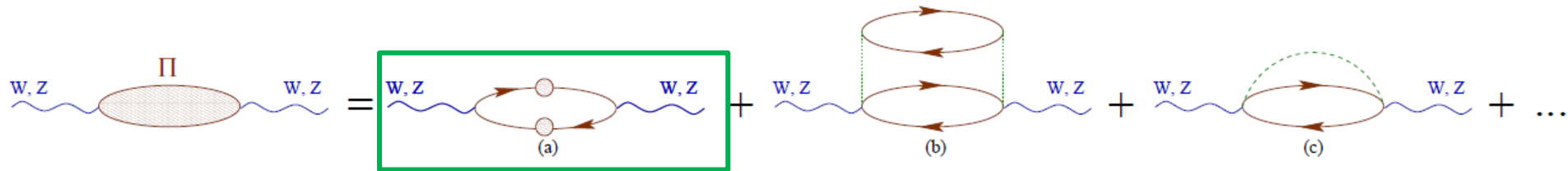
- Contains, through  $\rho(r)$ , empirical information about the **ground state** **absent** in the **Relativistic Global Fermi Gas**



Convolution model:  
Ciofi degli Atti, Simula, PRC 53 (1996)

# Polarization propagator

$$W_{(s,a)}^{\alpha\beta} = -\frac{1}{\pi} \text{Im} \Pi_{(s,a)}^{\alpha\beta}$$



■ Full **nucleon** propagator:

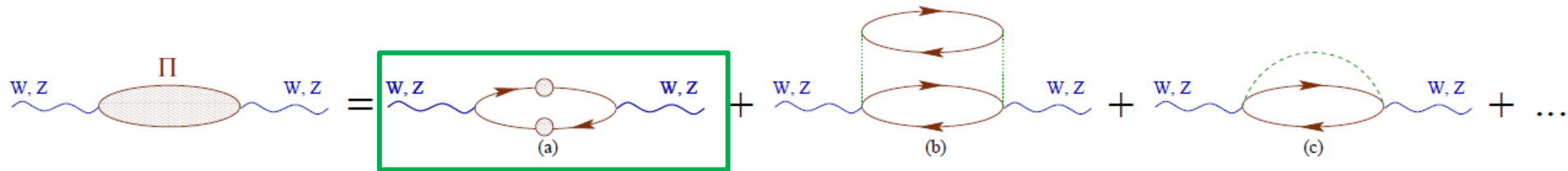
$$D(p) = (\not{p} + M)G(p)$$

$$G(p) = \frac{1}{p^0 + E_p - i\epsilon} \left[ \int_{-\infty}^{\mu} \frac{\mathcal{A}_h(\omega, \vec{p})}{p^0 - \omega - i\epsilon} d\omega + \int_{\mu}^{\infty} \frac{\mathcal{A}_p(\omega, \vec{p})}{p^0 - \omega + i\epsilon} d\omega \right]$$

$$\mu^2 = \vec{p}_F^2 + M^2 + \text{Re}\Sigma(\mu, p_F)$$

# Polarization propagator

$$W_{(s,a)}^{\alpha\beta} = -\frac{1}{\pi} \text{Im} \Pi_{(s,a)}^{\alpha\beta}$$



$$\text{Im} \Pi_{(s,a)}^{\alpha\beta} = -2\pi^2 \int \frac{d^4 p}{(2\pi)^4} H_{(s,a)}^{\beta\alpha} \mathcal{A}_p(p+q) \mathcal{A}_h(p)$$

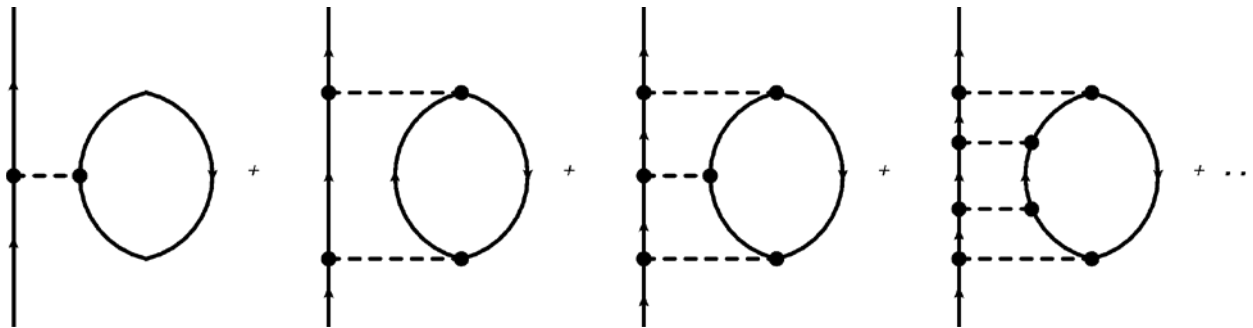
$$\mathcal{A}_{p,h}(p) = \mp \frac{1}{\pi} \frac{\text{Im}\Sigma(p)}{[p^2 - M^2 - \text{Re}\Sigma(p)]^2 + [\text{Im}\Sigma(p)]^2}$$

$$\Gamma^\mu = \gamma^\mu F_1 + \frac{i}{2M} \sigma^{\mu\nu} q_\nu F_2 - \gamma^\mu \gamma_5 F_A - \frac{q^\mu}{M} \gamma_5 F_P$$

$$H^{\alpha\beta} = \text{Tr} \left[ (\not{p} + M) \gamma^0 (\Gamma^\alpha)^\dagger \gamma^0 (\not{p}' + M) \Gamma^\beta \right] .$$

# Nucleon selfenergy

- Fernández de Córdoba, Oset, PRC46 (1992)
- Semiphenomenological approach
  - Non-relativistic
  - Effective NN potential derived from experimental NN cross section
  - Medium-polarization corrections

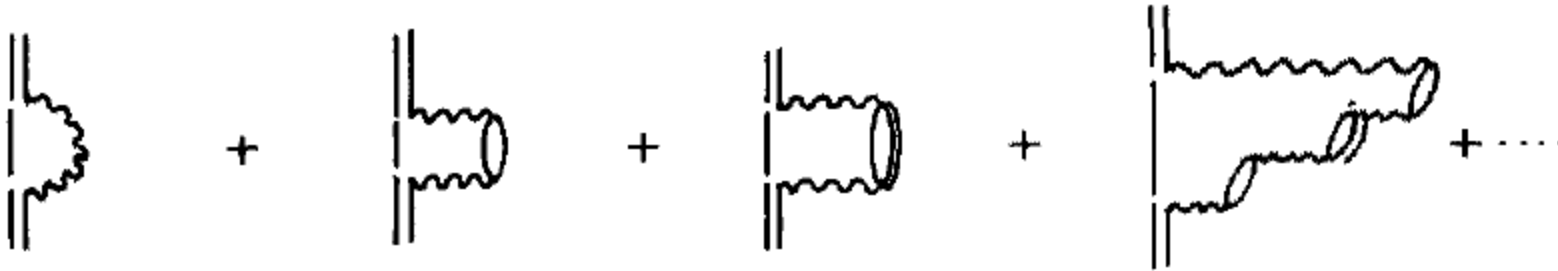


Sobczyk, Rocco, Lovato, Nieves, PRC97 (2018)

- $\text{Re}\Sigma$  obtained from  $\text{Im}\Sigma$  using dispersion relations
  - + Hartree term
  - + pheno  $C\rho$  with C fixed from binding energy

# $\Delta$ selfenergy

- Oset, Salcedo, NPA468 (1987)
- Many body calculation of  $\Delta$  selfenergy in the medium

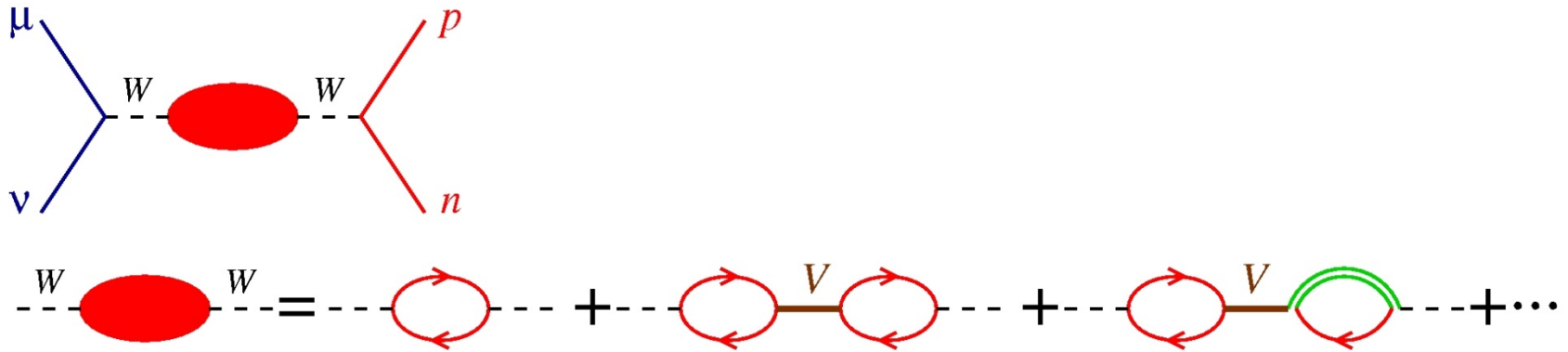


- Free width  $\Delta \rightarrow N \pi$  modified by Pauli blocking
- $\text{Im}\Sigma_{\Delta}(\rho)$ : in-medium broadening:
  - $\Delta N \rightarrow N N$
  - $\Delta N \rightarrow N N \pi$
  - $\Delta N N \rightarrow N N N$
- $\text{Re}\Sigma_{\Delta}(\rho) \approx -50 \text{ MeV } \rho/\rho_0$

$$\frac{1}{p^2 - m_{\Delta}^2 + im_{\Delta}\Gamma_{\Delta}(p^2)}$$

$$\begin{aligned} M_{\Delta} &\rightarrow M_{\Delta} + \text{Re}\Sigma_{\Delta}(\rho) \\ \Gamma_{\Delta} &\rightarrow \tilde{\Gamma}_{\Delta}(\rho) - 2\text{Im}\Sigma_{\Delta}(\rho) \end{aligned}$$

# RPA



## ■ RPA equation (schematically):

$$\Pi_{\text{RPA}} = \Pi_0 + \Pi_0 V \Pi_{\text{RPA}}$$

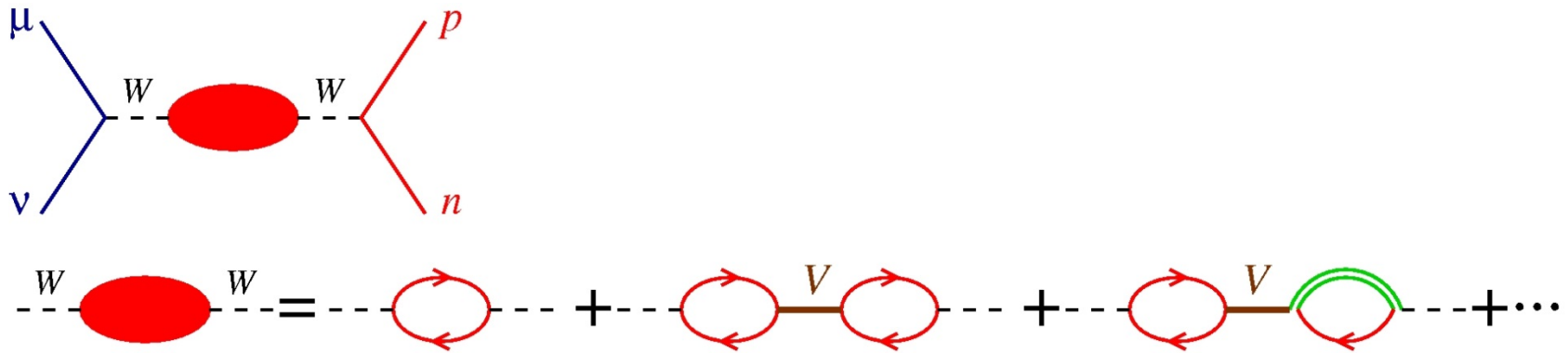
$V=V(\rho)$  ← effective, density dependent, **NN** interaction

$$V_{\text{NN}} = \vec{\tau}_1 \vec{\tau}_2 \sigma_1^i \sigma_2^j [\hat{q}_i \hat{q}_j V_L(q) + (\delta_{ij} - \hat{q}_i \hat{q}_j) V_T(q)] + g \vec{\sigma}_1 \vec{\sigma}_2 + f' \vec{\tau}_1 \vec{\tau}_2 + f I_1 I_2$$

$$V_L = \frac{f_{\text{NN}\pi}^2}{m_\pi^2} \left\{ \left( \frac{\Lambda_\pi^2 - m_\pi^2}{\Lambda_\pi^2 - q^2} \right)^2 \frac{\vec{q}^2}{q^2 - m_\pi^2} + g' \right\}$$

$$V_T = \frac{f_{\text{NN}\pi}^2}{m_\pi^2} \left\{ C_\rho \left( \frac{\Lambda_\rho^2 - m_\rho^2}{\Lambda_\rho^2 - q^2} \right)^2 \frac{\vec{q}^2}{q^2 - m_\rho^2} + g' \right\}$$

# Poor man's RPA



- **RPA equation** (schematically):

$$\Pi_{\text{RPA}} = \Pi_0 + \Pi_0 V \Pi_{\text{RPA}}$$

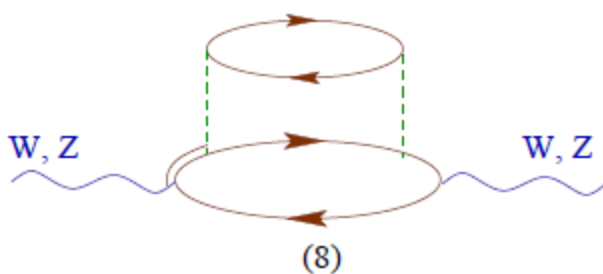
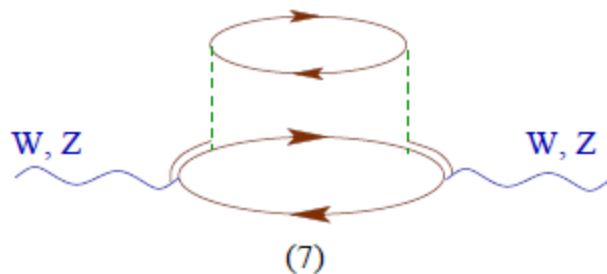
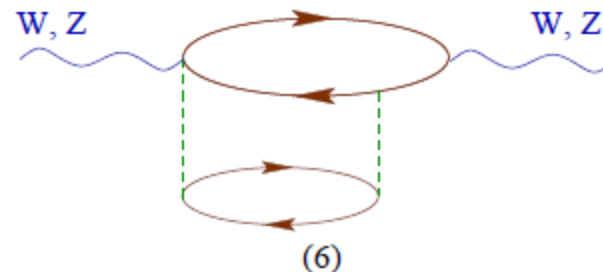
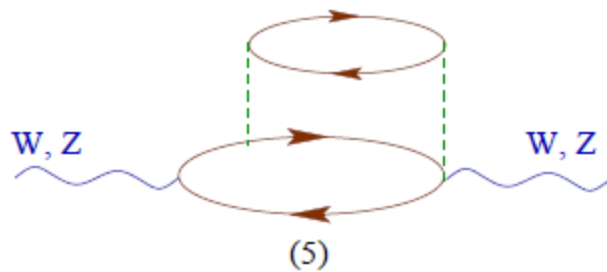
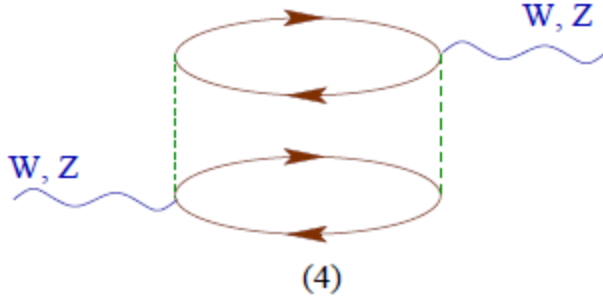
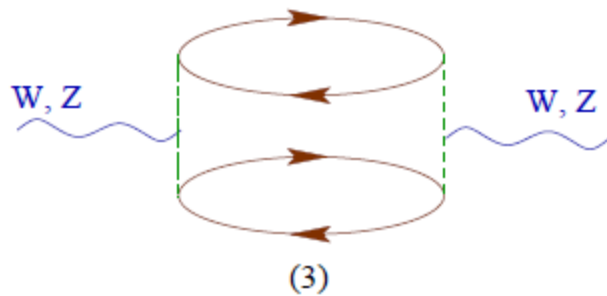
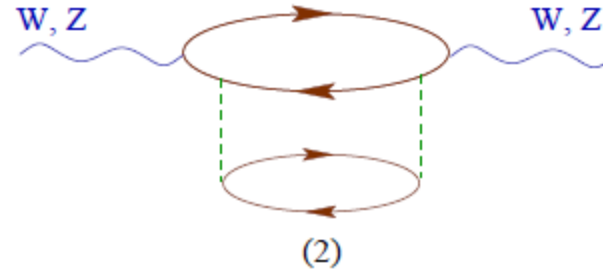
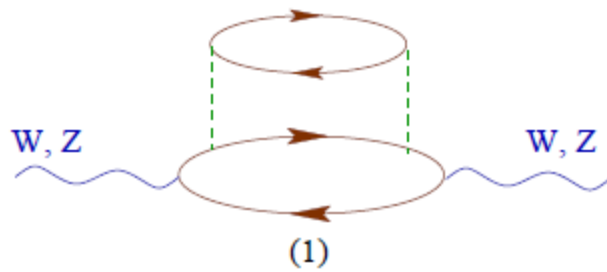
$V=V(\rho)$  ← effective, density dependent, **NN** interaction

- Non-relativistic **analytic** solution: new  $\rho$ -dependent terms of the **hadron tensor**.
- Incorporates **explicitly**  $\pi$  and  $\rho$  exchange and  $\Delta$ -hole states
- Describes correctly  $\mu$  capture on  $^{12}\text{C}$  and **LSND** CCQE

Nieves, Amaro, Valverde, PRC 70 (2004) 055503

Nieves, Sobczyk, Annals Phys. 383 (2017)

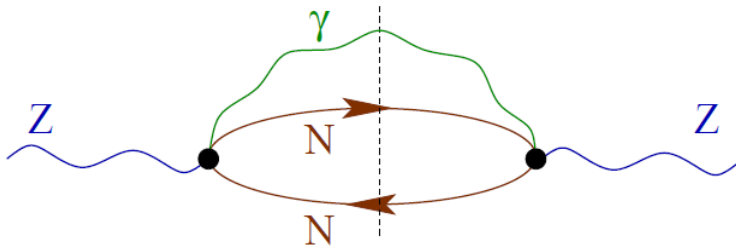
# 2p2h examples



# Photon emission in NC interactions

- $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma X$

- 1p1h1 $\gamma$  excitations:



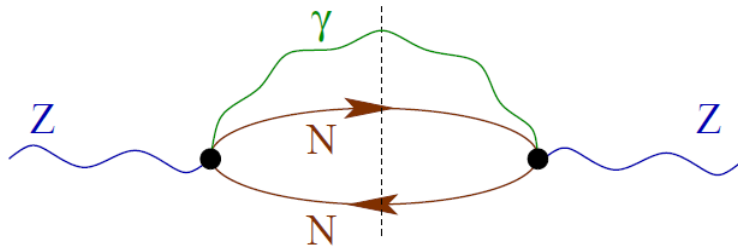
- In-medium  $\Delta(1232)$

Wang, LAR, Nieves, PRC89 (2014)

# Photon emission in NC interactions

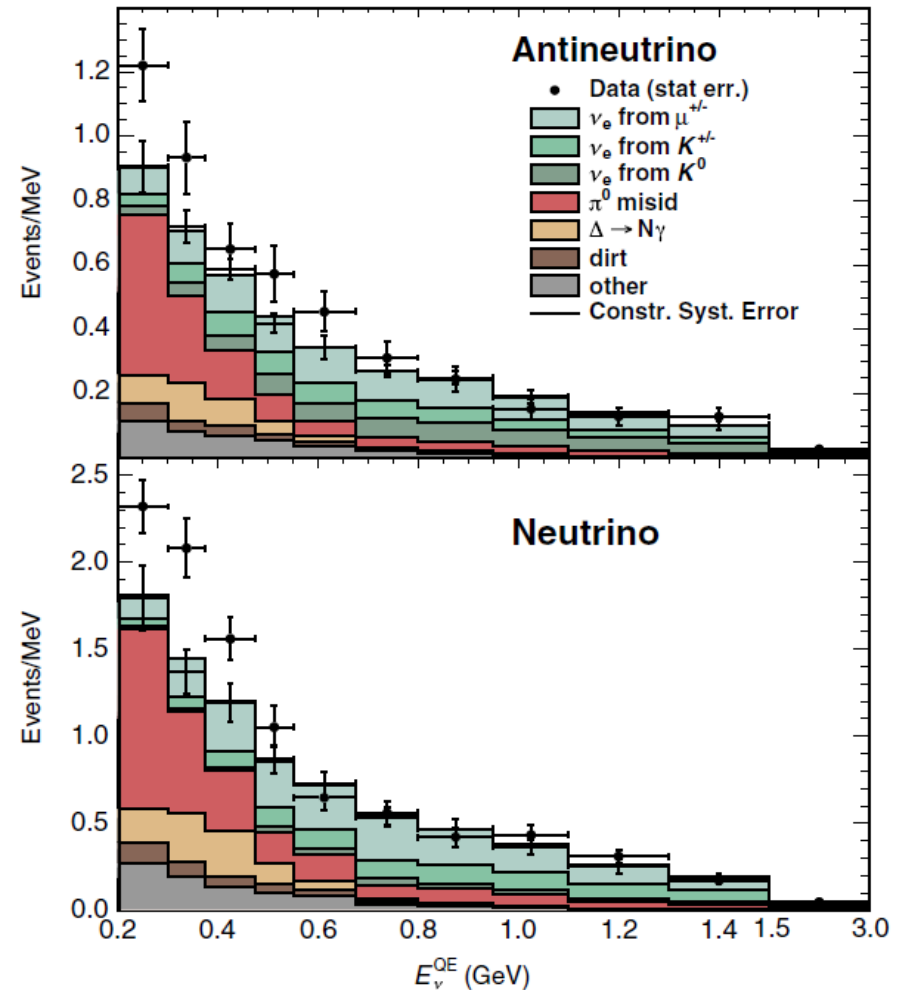
■  $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma X$

■  $1p1h1\gamma$  excitations:



■ In-medium  $\Delta(1232)$

Wang, LAR, Nieves, PRC89 (2014)

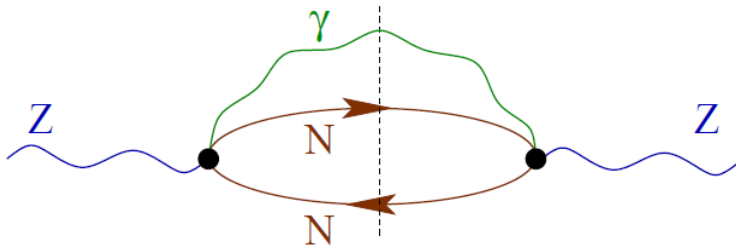


Aguilar-Arevalo et al., PRL110 (2013) 161801

# Photon emission in NC interactions

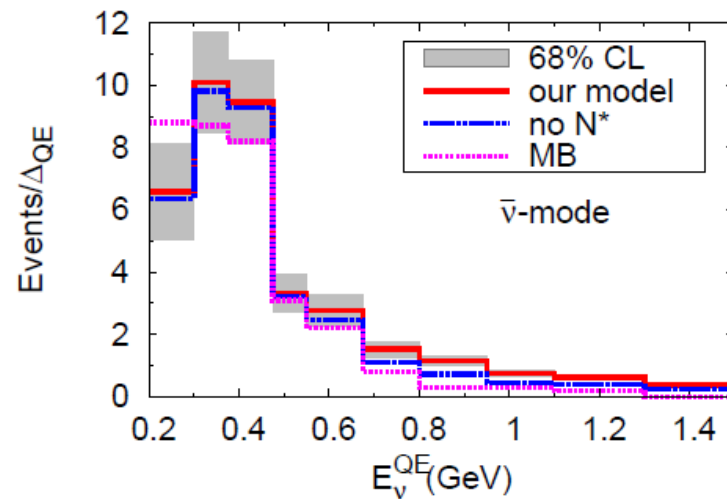
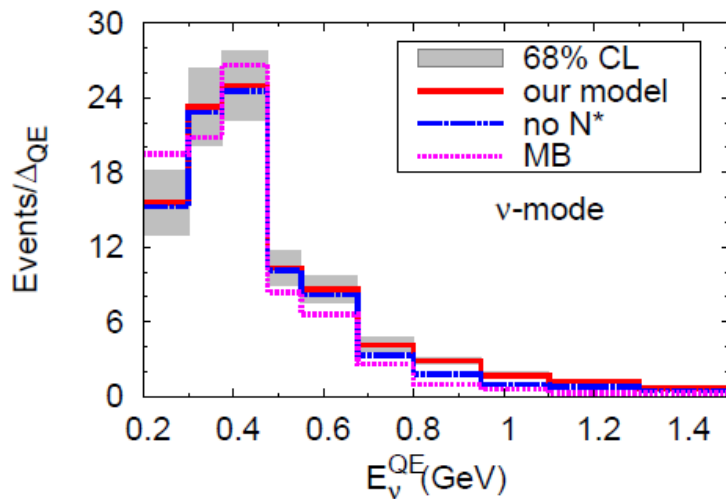
- $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma X$

- 1p1h1 $\gamma$  excitations:



- In-medium  $\Delta(1232)$

E. Wang, LAR, J. Nieves, PLB 740 (2015)

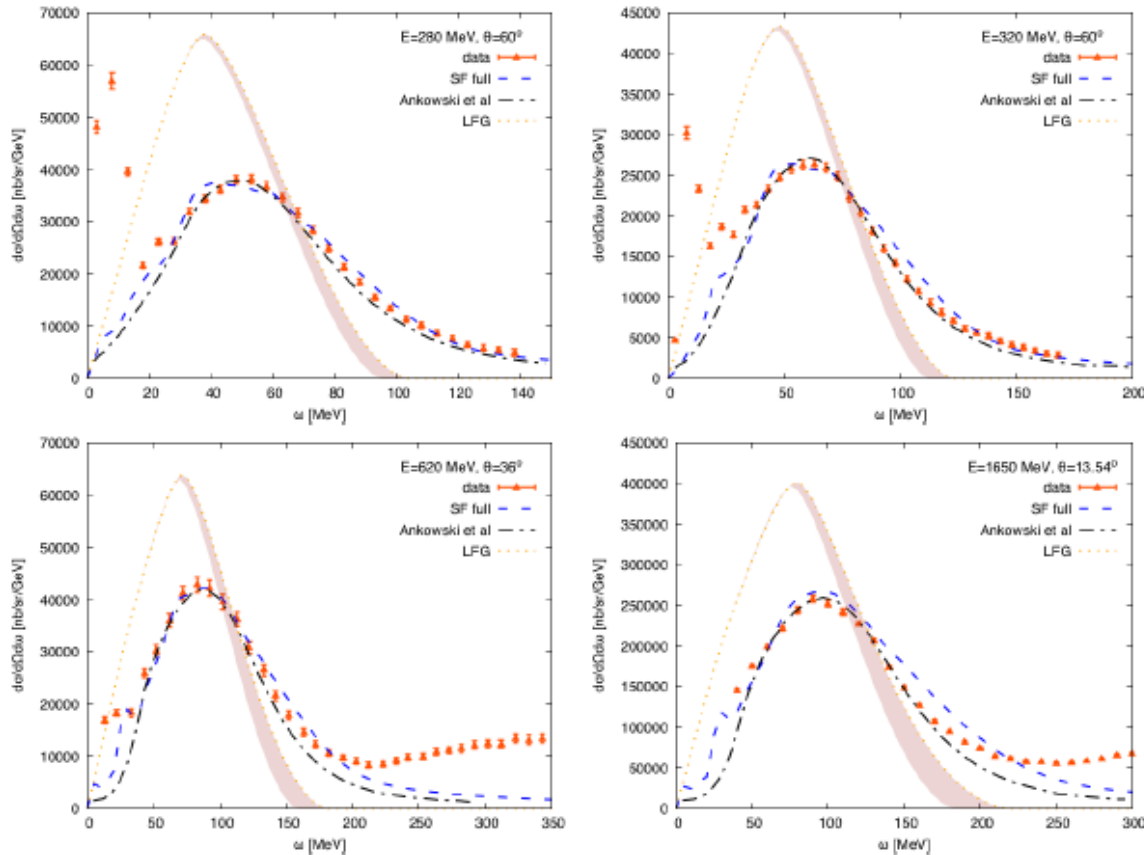


- NC $\gamma$  : insufficient to explain the excess of e-like events at MiniBooNE

- NC $\gamma$  : under analysis @ MicroBooNE

# Electron scattering

## ■ Inclusive $^{12}\text{C}(e,e')X$ in the QE region

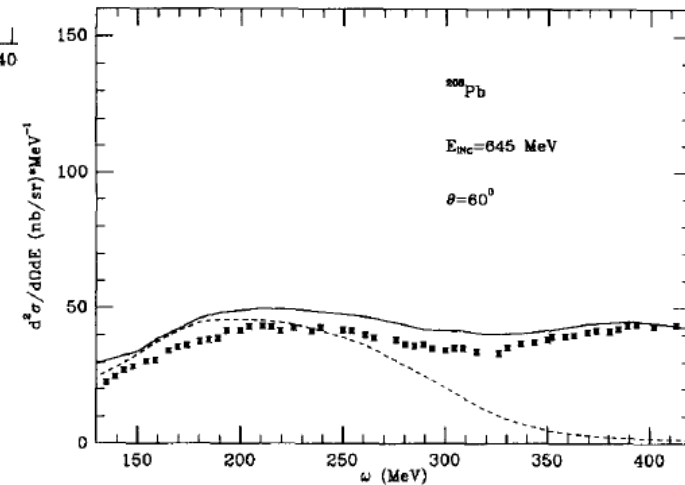
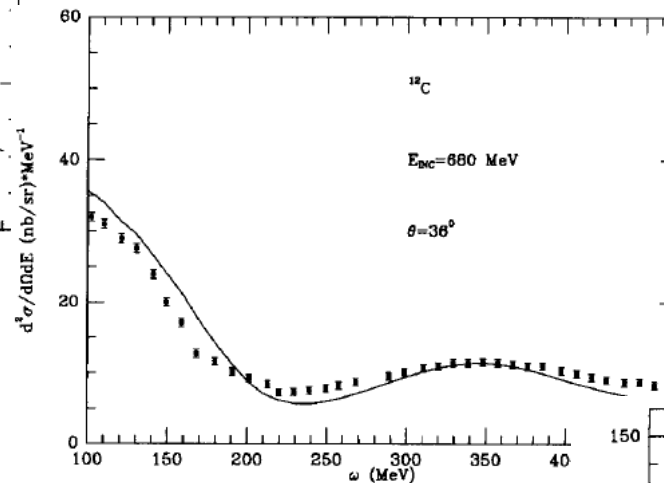
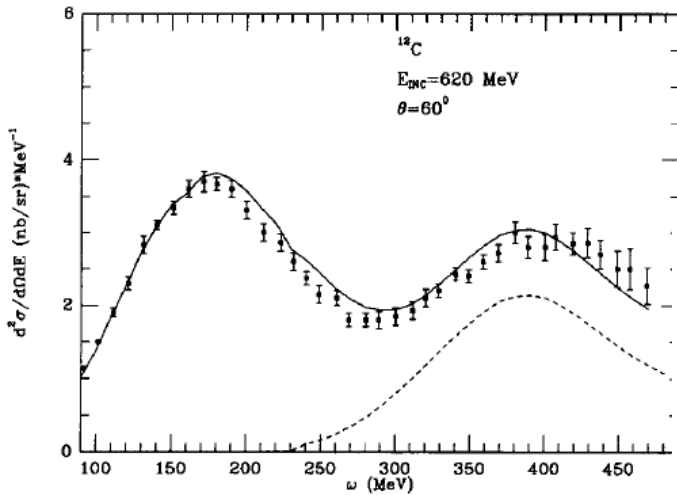


Nieves, Sobczyk, Annals Phys. 383 (2017)

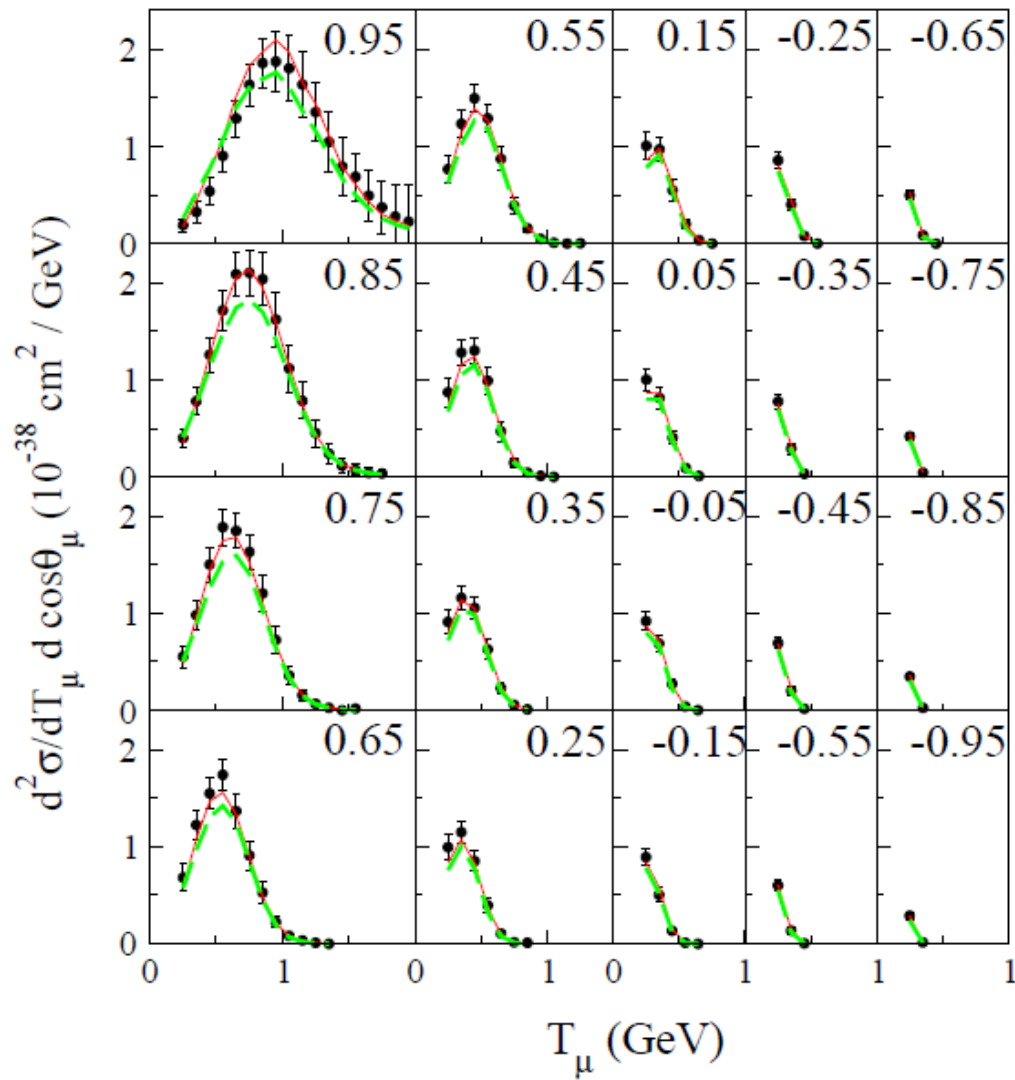
- “RPA effects in integrated decay rates or cross sections become significantly smaller when SF corrections are also taken into account (...)”

# Electron inclusive scattering

■ Gil, Nieves, Oset, NPA627 (1999)



# CCQE-like scattering



Nieves, Ruiz Simo, Vicente Vacas, PLB 707 (2012)

# Weak coherent reactions

■ **Coherent** = final **nucleus** remains in the **ground state**

■ Charged Current **coherent** particle production

$$\begin{aligned}\nu_l A &\rightarrow l^- m^+ A \\ \bar{\nu}_l A &\rightarrow l^+ m^- A\end{aligned}\quad m^\pm = \pi^\pm, K^\pm, \dots$$

■ Neutral Current **coherent** particle production

$$\begin{aligned}\nu A &\rightarrow \nu m^0 A \\ \bar{\nu} A &\rightarrow \bar{\nu} m^0 A\end{aligned}\quad m^0 = \gamma, \pi^0, \dots$$

# Weak coherent reactions

- Amplitude:  $\mathcal{M} \sim \frac{G}{\sqrt{2}} l_\mu J^\mu$

- Nuclear current:

$$J^\mu = \sum_i \sum_{r=p,n} \int d\vec{r} e^{i\vec{q}\cdot\vec{r}} \rho_r(r) \frac{1}{2} \text{Tr} [\bar{u} \Gamma_{i(r)}^\mu u] \phi_{\text{out}}^*$$

$i$ =all mechanisms

- Prescription for nucleon momenta:

$$p = \left( \sqrt{M^2 + \frac{1}{4} (\vec{q}_\gamma - \vec{q})^2}, \frac{\vec{q}_\gamma - \vec{q}}{2} \right) \quad p' = q - q_\gamma + p = \left( \sqrt{M^2 + \frac{1}{4} (\vec{q}_\gamma - \vec{q})^2}, -\frac{\vec{q}_\gamma - \vec{q}}{2} \right)$$

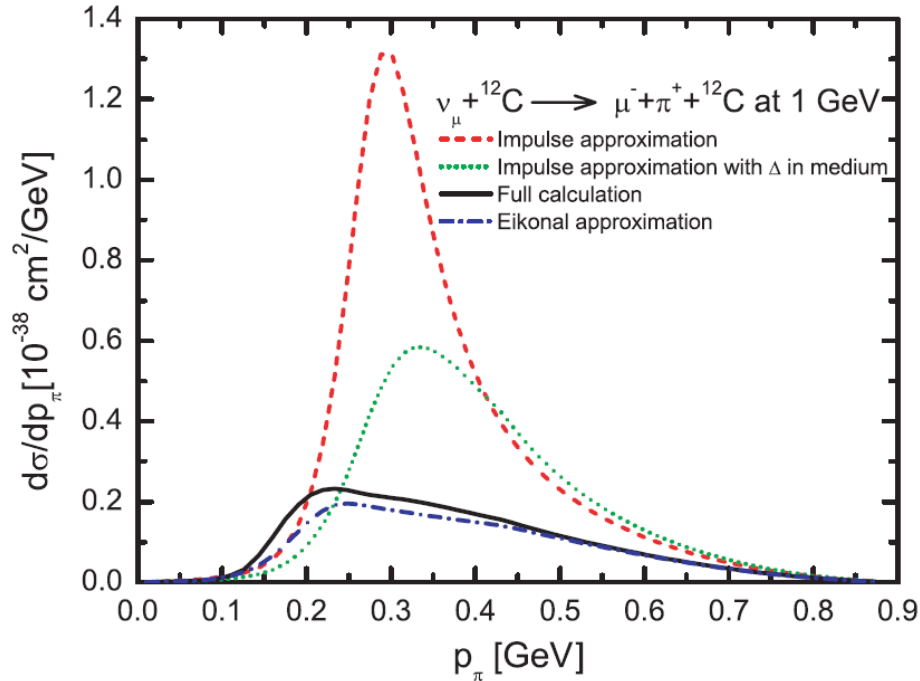
- Momentum **equally shared** by initial and final nucleons

- Meson distortion:

$$\left( -\vec{\nabla}^2 - \vec{p}_K^2 + 2\omega_K V_{\text{opt}} \right) \phi_{\text{out}}^* = 0 \quad \leftarrow \text{Klein-Gordon equation}$$

$$\vec{p}_K \phi_{\text{out}}^*(\vec{p}_K, \vec{r}) \rightarrow i\vec{\nabla} \phi_{\text{out}}^*(\vec{p}_K, \vec{r})$$

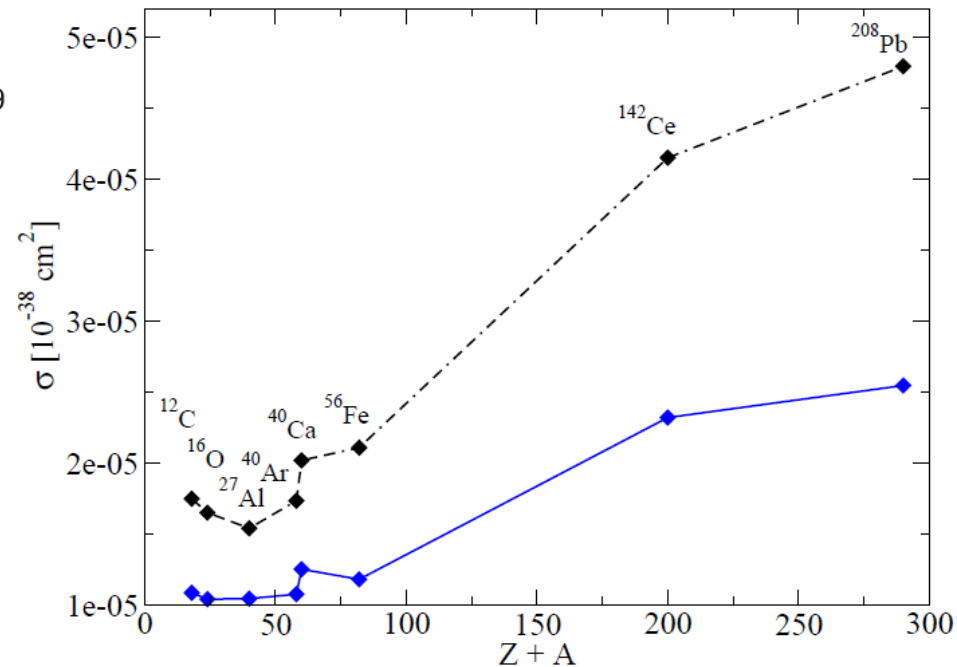
# Weak coherent reactions



LAR et al., PRC 75 (2007)

LAR et al., PRC 87 (2013);

$$\nu_\mu A \rightarrow \mu^- K^+ A$$



# Conclusion

Visit **Valencia** for work:



or fun:

