

Towards double-beta decay matrix elements with nuclear reactions



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ECT*

EUROPEAN CENTRE FOR THEORETICAL STUDIES
IN NUCLEAR PHYSICS AND RELATED AREAS



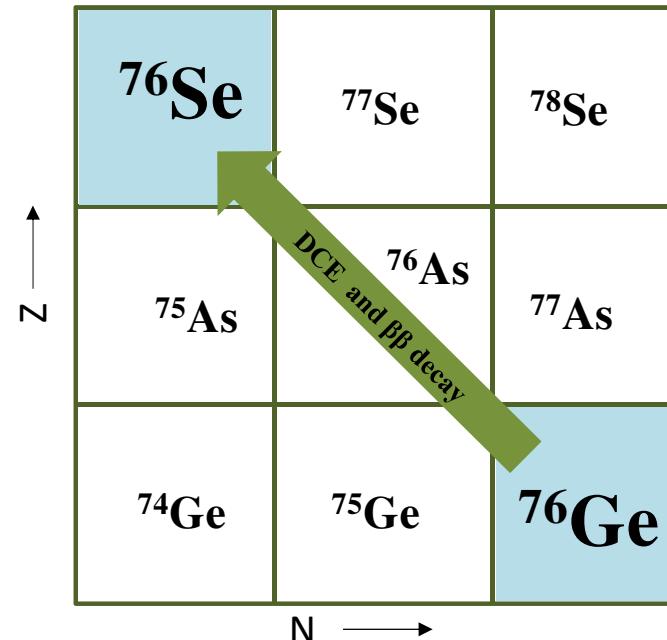
Progress and Challenges in Neutrinoless Double Beta Decay

15 - 19 July 2019

A new experimental tool

Nuclear reactions

Heavy-Ion induced Double Charge Exchange reactions (DCE) to stimulate in the laboratory the same nuclear transition (g.s. to g.s.) occurring in $O\nu\beta\beta$



F. Cappuzzello et al., EPJ A (2018) 54:72



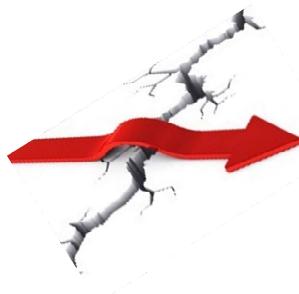
The Goals of the Research Program



Extraction from measured cross-sections of “*data-driven*” information on NME for all the systems candidate for $0\nu\beta\beta$

Nuclear Matrix Element (NME)

$$|M_{\varepsilon}^{0\nu\beta\beta}|^2 = \left| \langle \Psi_f | \hat{O}_{\varepsilon}^{0\nu\beta\beta} | \Psi_i \rangle \right|^2$$



- Constraints to the existing theories of NMEs (nuclear wave functions)
- Model-independent comparative information on the sensitivity of half-life experiments
- Complete study of the reaction mechanism



The NUMEN collaboration

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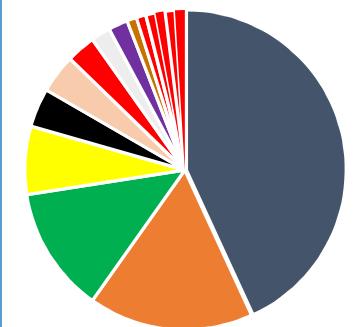
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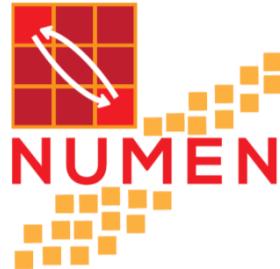
102 Researchers

34 Institutions

15 Countries



- Italy
- Mexico
- Brazil
- Turkey
- Germany
- China
- Morocco
- Greece
- Romania
- Israel
- France
- US
- Finland
- Spain
- Chile



NUMEN phases			
Phase 1	Phase 2	Phase 3	Phase 4
Feasibility study	Study of few cases + development of theory	Shutdown & Upgrade	Systematic study of all the targets
2013-2015	2015-2020	2021-2022	2022-...

$0\nu\beta\beta$ vs DCE



Differences

- DCE mediated by **strong interaction**, $0\nu\beta\beta$ by **weak interaction**
- Decay vs reaction **dynamics**
- DCE includes **sequential transfer mechanism**

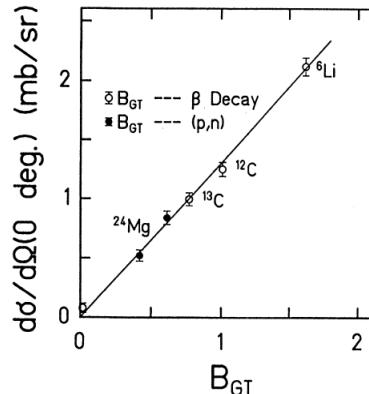
Similarities

- **Same initial and final states:** Parent/daughter states of the $0\nu\beta\beta$ decay are the same as those of the target/residual nuclei in the DCE
- **Similar operator:** Fermi, Gamow-Teller and rank-2 tensor components are present in both the transition operators, with tunable weight in DCE
- **Large linear momentum** (~ 100 MeV/c) available in the virtual intermediate channel
- **Same nuclear medium:** Constraint on the theoretical determination of quenching phenomena on $0\nu\beta\beta$
- **Off-shell propagation** through virtual intermediate channels

Connection between β -decay and SCE

Single β -decay strengths are proportional to single CEX cross-sections under specific conditions

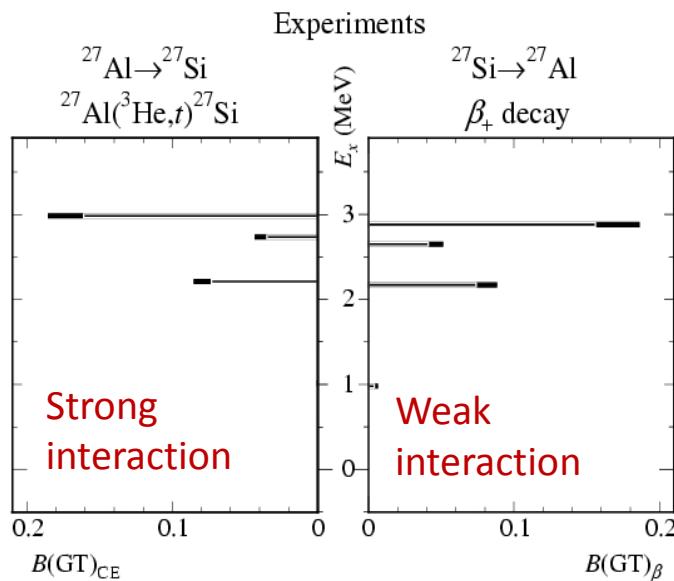
➤ For (p,n) , (n,p) , $(d,^2He)$



F. Osterfeld Rev. Mod. Phys. 64 (1992) 491
T.N. Taddeucci Nucl. Phys. A 469 (1997) 125
H. Ejiri Phys. Rep. 338 (2000) 256
H.M. Xu, et al., Phys. Rev. C 52 (1995) R1161
H. Ejiri Phys. Rep. 338 (2000) 256

➤ $(^3He,t)$

Y. Fujita Prog. Part. Nuc. Phys. 66 (2011)



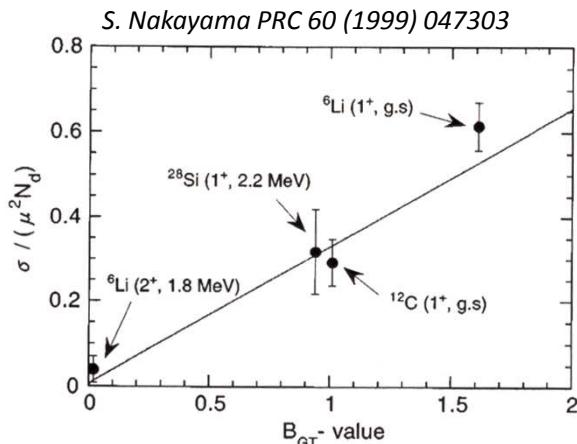
$$\frac{B(GT)_{[(^3He,t):q=0]}}{B(GT)_{[\beta\text{-decay}]}} = 1 \pm 0.02$$

(In general for $B(GT) > 0.05$)

$\Delta L = 0$ (high incident energy, small angles)
Tensor components negligible

Connection between β -decay and SCE

➤ For $(^7\text{Li}, ^7\text{Be})$



$$\frac{B(GT)[(^7\text{Li}, ^7\text{Be}); q=0]}{B(GT)[\beta\text{-decay}]} = 1 \pm 0.2$$

F. Cappuzzello et al., Nucl. Phys. A 739 (2004) 30-56
F. Cappuzzello et al. Phys. Lett. B 516 (2001) 21-26
F. Cappuzzello et al. EuroPhys. Lett. 65 (2004) 766-772
S.E.A. Orrigo, et al. Phys. Lett. B 633 (2006) 469-473
C. Nociforo et al. Eur. Phys. J. A 27 (2006) 283-288
M. Cavallaro Nuovo Cimento C 34 (2011) 1

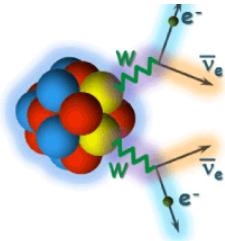
- ✓ **Confirmed** on different nuclei: ^{11}Be , ^{12}B , ^{15}C , ^{19}O (less accuracy)
- ✓ **Microscopic and unified description** of reaction and structure is mandatory for quantitative analyses

➤ Recently, the theory of heavy-ion SCE has been reformulated (NUMEN)

H. Lenske et al., Phys. Rev. C 98 (2018) 044620

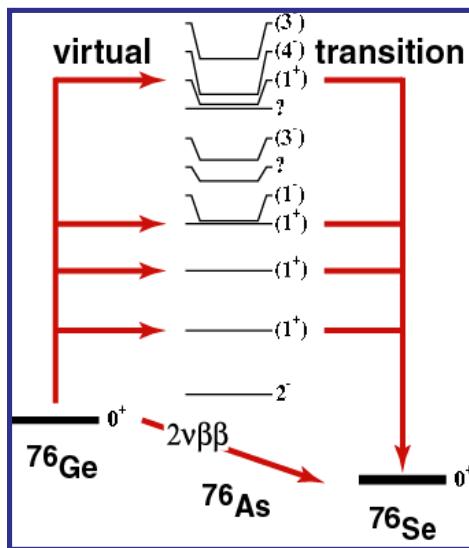
At small momentum transfer, distortion effects (due to the **strong absorption**) reduce to a simple scaling factor, allowing to define a reduced cross-section, given by NME of β -decay type

$2\nu\beta\beta$ - decay



q-available like ordinary β -decay
($q \sim 0.01 \text{ fm}^{-1} \sim 2 \text{ MeV/c}$)

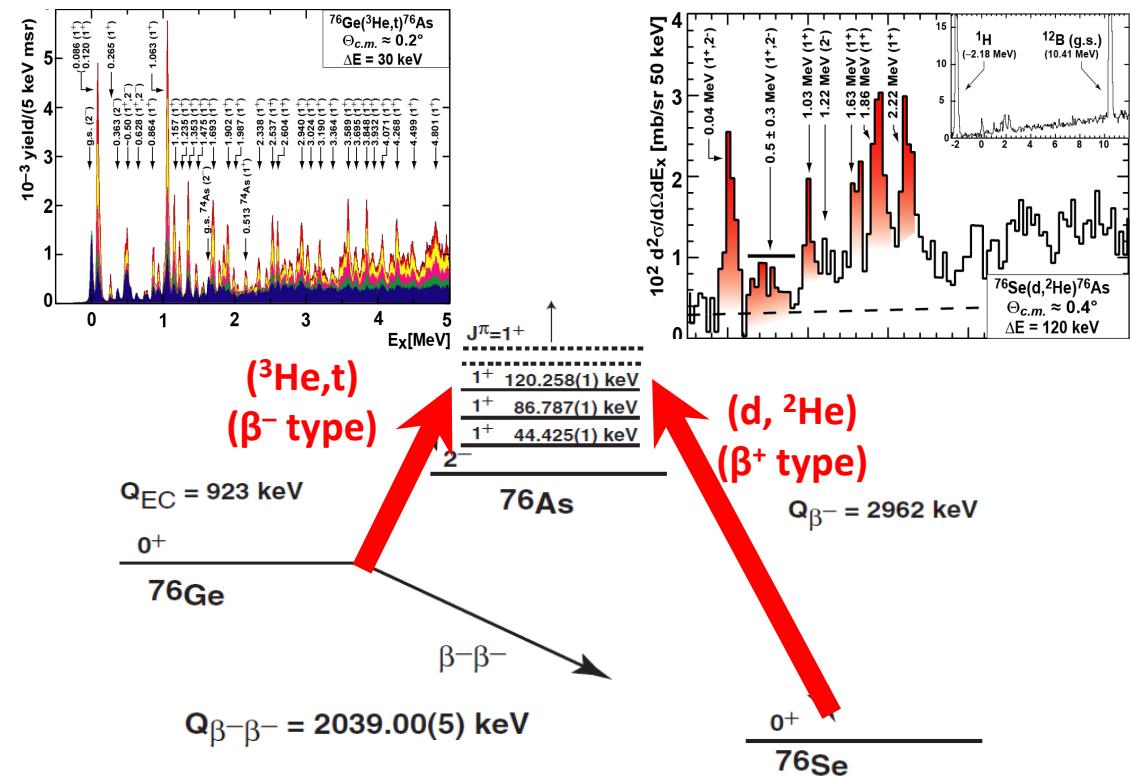
only allowed decays are possible ($L = 0$)



Single state dominance

Methodology:

Single CEX to populate intermediate states and approximation (SSD / all positive signs in the coherent sum of the amplitudes)

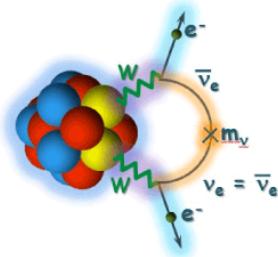


$$M^{2\nu} = \sum_m \frac{\langle 0_f^+ | \sigma \tau^- | m \rangle \langle m | \sigma \tau^+ | 0_i^+ \rangle}{E_m - (M_i + M_f)/2}$$

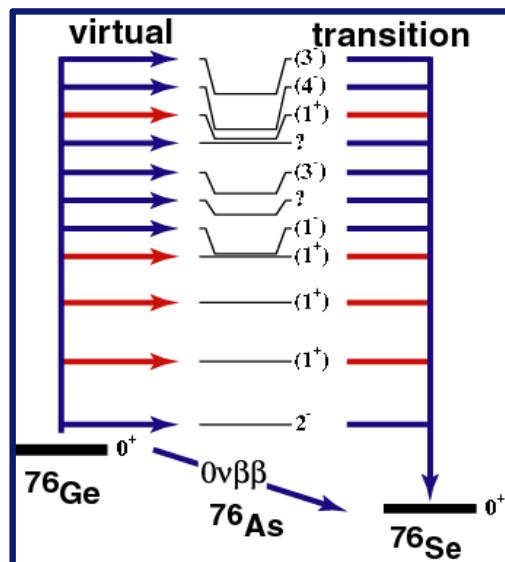
H. Ejiri Progr. Part. Nucl. Phys. 64 (2010) 249257

$0\nu\beta\beta$ - decay

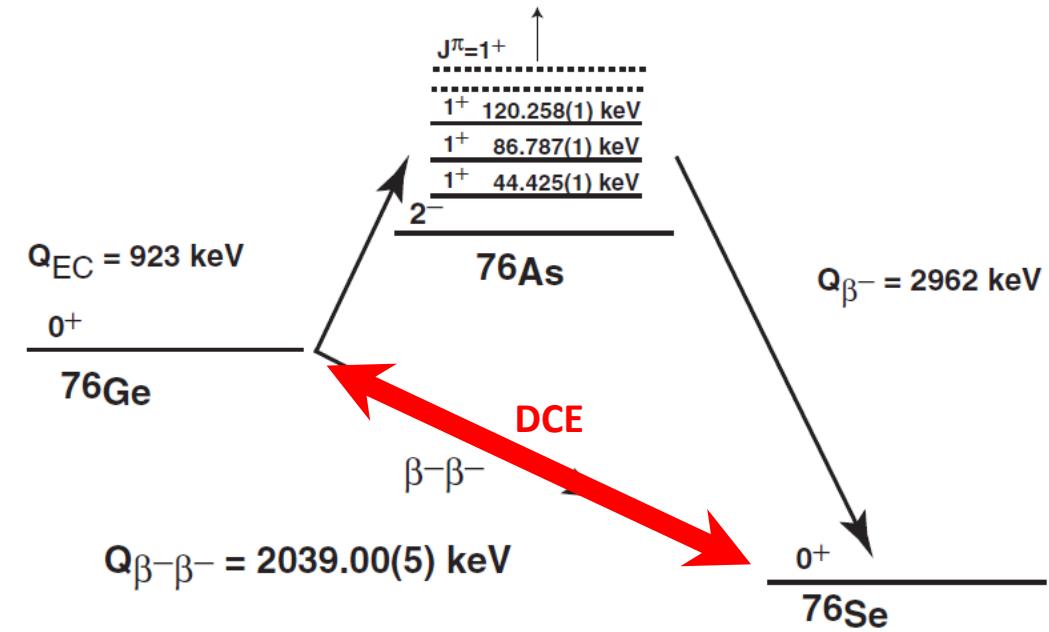
J.Hyvarinen and J.Suhonen PHYS. REV. C 91, 024613 (2015)



neutrino enters as virtual particle,
 $q \sim 0.5 \text{ fm}^{-1}$ ($\sim 100 \text{ MeV}/c$)
 forbiddenness weakened $L = 0, 1, 2, \dots$



Closure approximation



High multipolarities not
 accessible through single
 CEX reactions

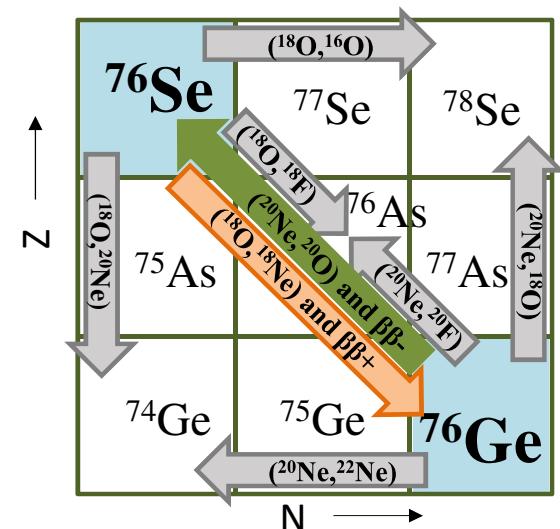
The experiments



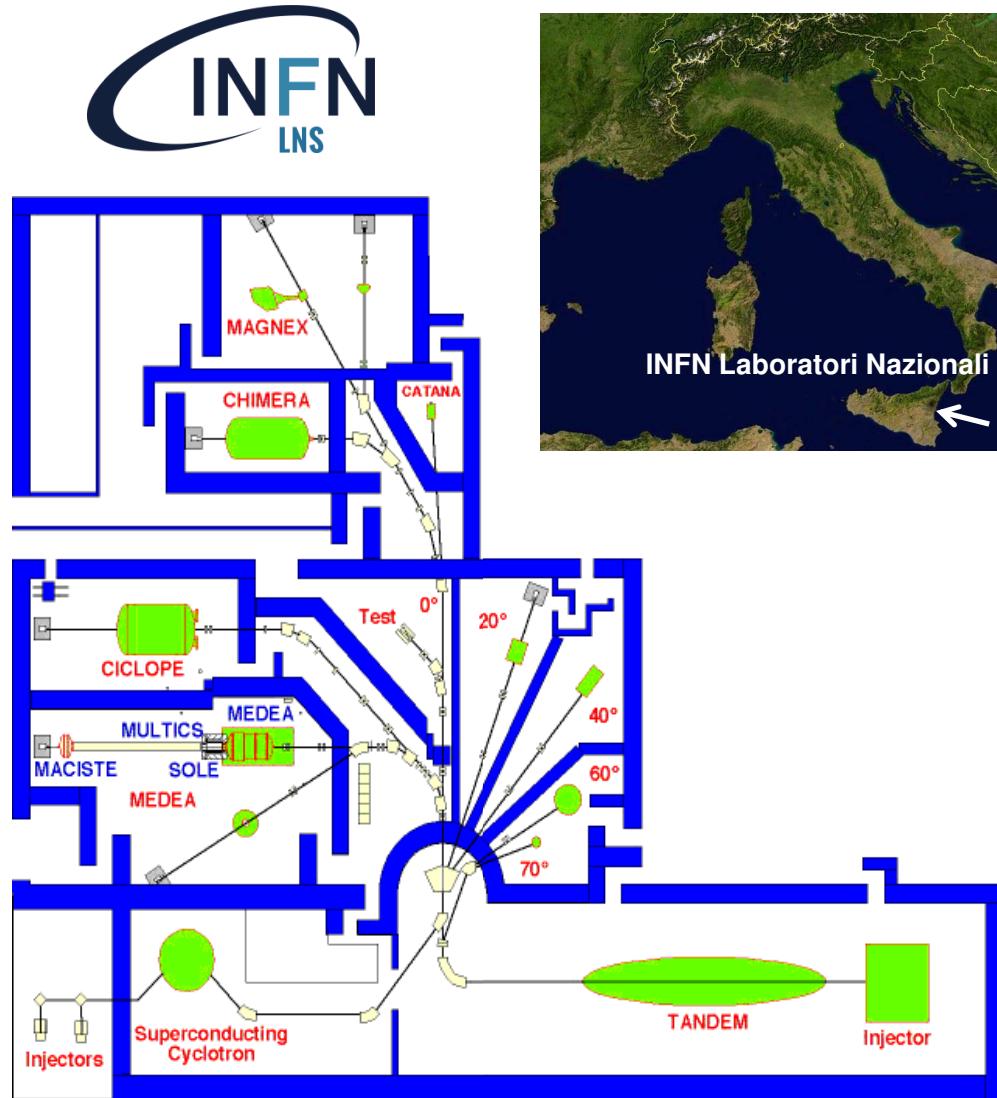
The experimental program



- **Transitions of interest for $0\nu\beta\beta$:**
Limited number of targets in phase 2,
systematic exploration of all the targets in phase 4
- **Two directions:**
 $\beta\beta^-$ via $(^{20}\text{Ne}, ^{20}\text{O})$ and $\beta\beta^+$ via $(^{18}\text{O}, ^{18}\text{Ne})$
- **Complete net** of reactions which can contribute to
the DCE cross-section:
1p-, 2p-, 1n-, 2n-transfer, SCE, (elastic)
- **Two (or more) incident energies**
to study the reaction mechanism



The INFN-LNS laboratory in Catania



The experimental facility

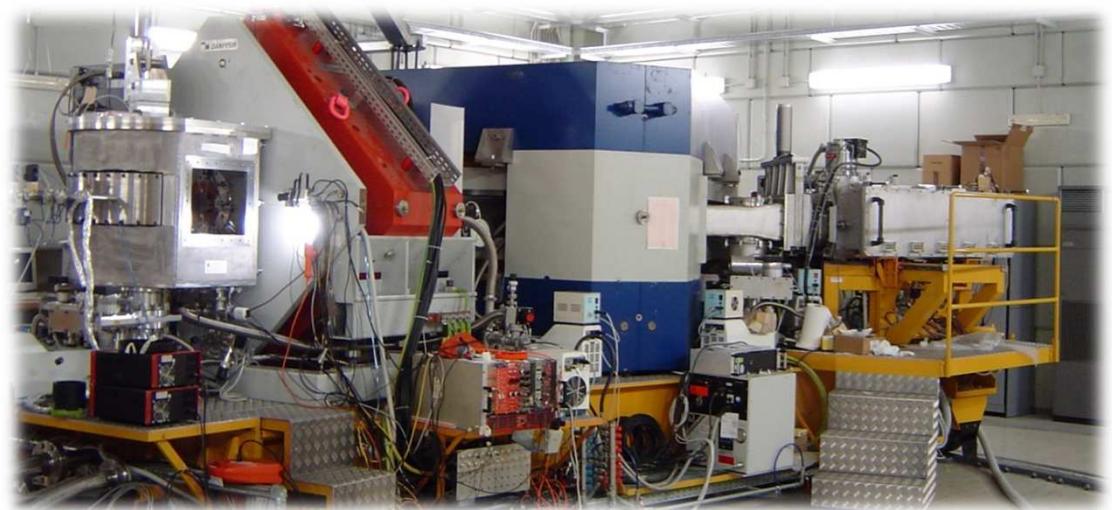
K800 Superconducting Cyclotron

- In operation since 1996.
- Accelerates from H to U ions
- Maximum energy 80 MeV/u.



MAGNEX magnetic spectrometer

F. Cappuzzello et al., Eur. Phys. J. A (2016) 52: 167



Optical characteristics	Current values
Maximum magnetic rigidity (Tm)	1.8
Solid angle (msr)	50
Momentum acceptance	-14%, +10%
Momentum dispersion (cm/%)	3.68

Good compensation of
the aberrations:
Trajectory reconstruction



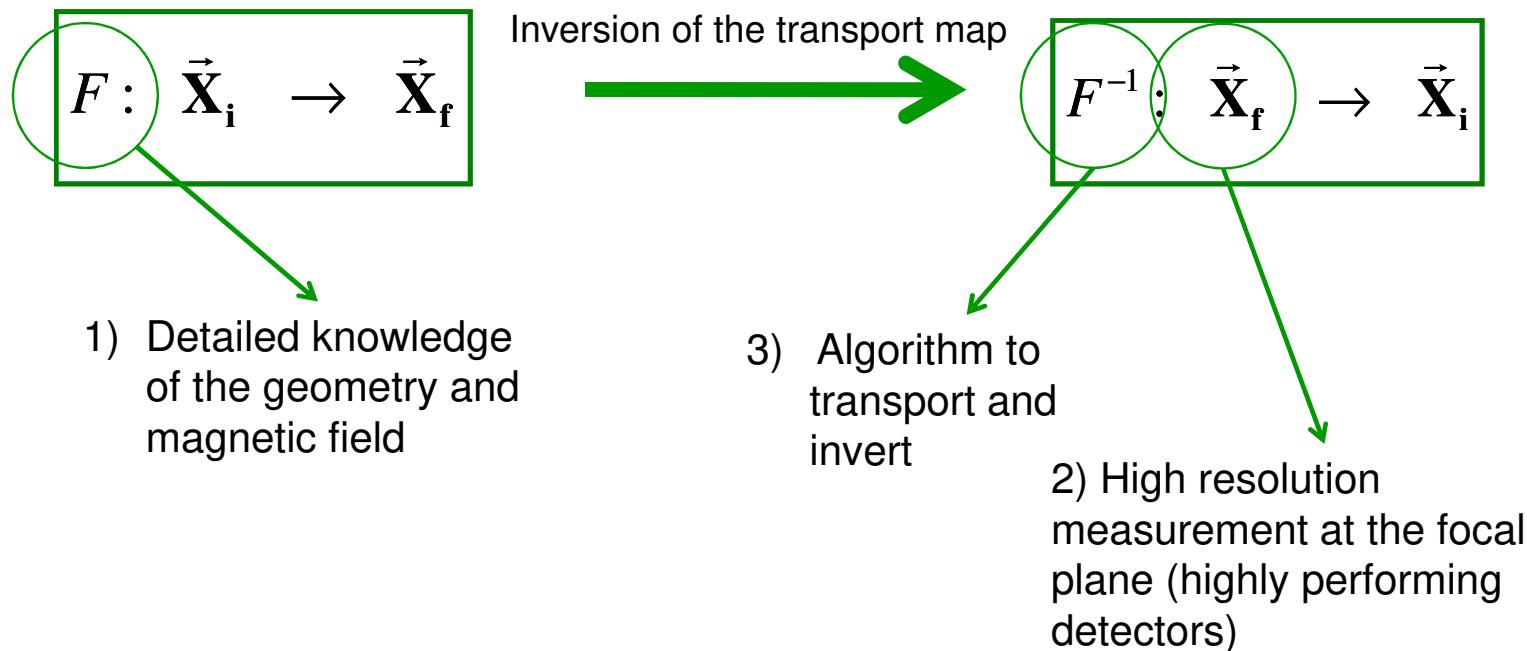
Measured resolutions:

- Energy $\Delta E/E \sim 1/1000$
- Angle $\Delta\theta \sim 0.2^\circ$
- Mass $\Delta m/m \sim 1/160$

Software ray-reconstruction

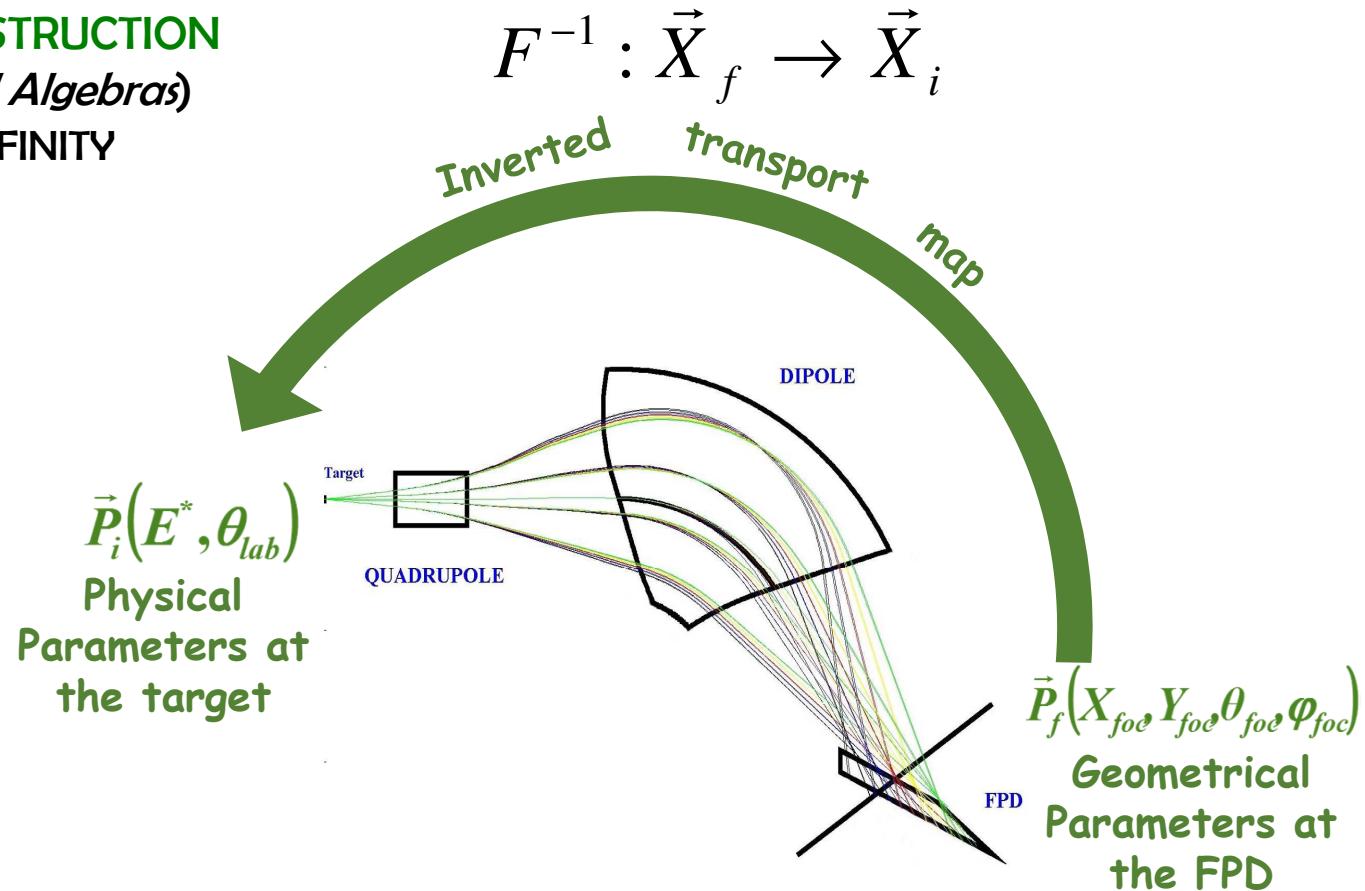
ALGEBRIC RAY-RECONSTRUCTION

- ✓ Solution of the **equation of motion** for each detected particle
- ✓ **Inversion** of the transport map
- ✓ Application to the final **measured parameters**

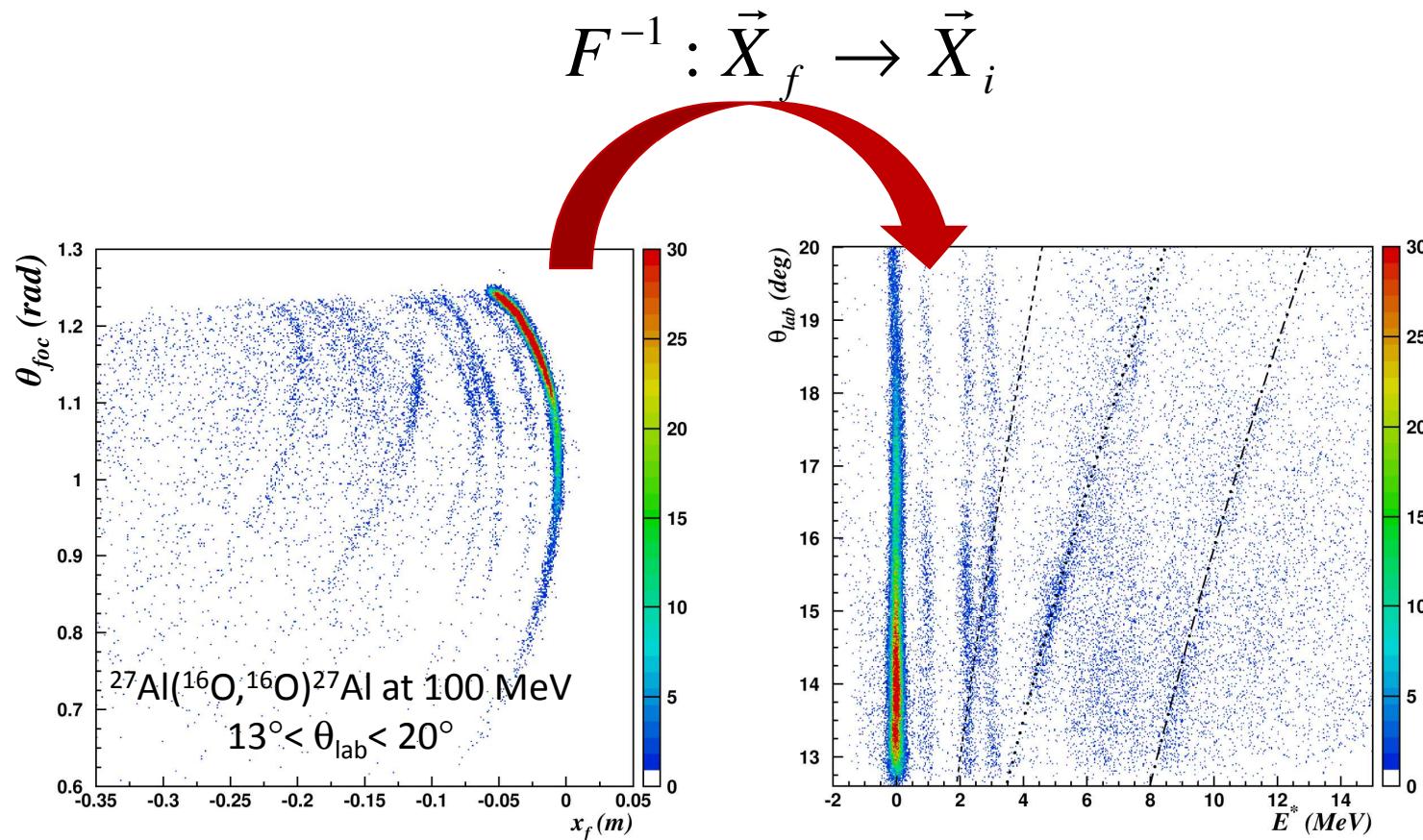


Algorithm to transport and invert

ALGEBRIC
RAY-RECONSTRUCTION
(Differential Algebras)
COSY-INFINITY



High energy and angular resolution

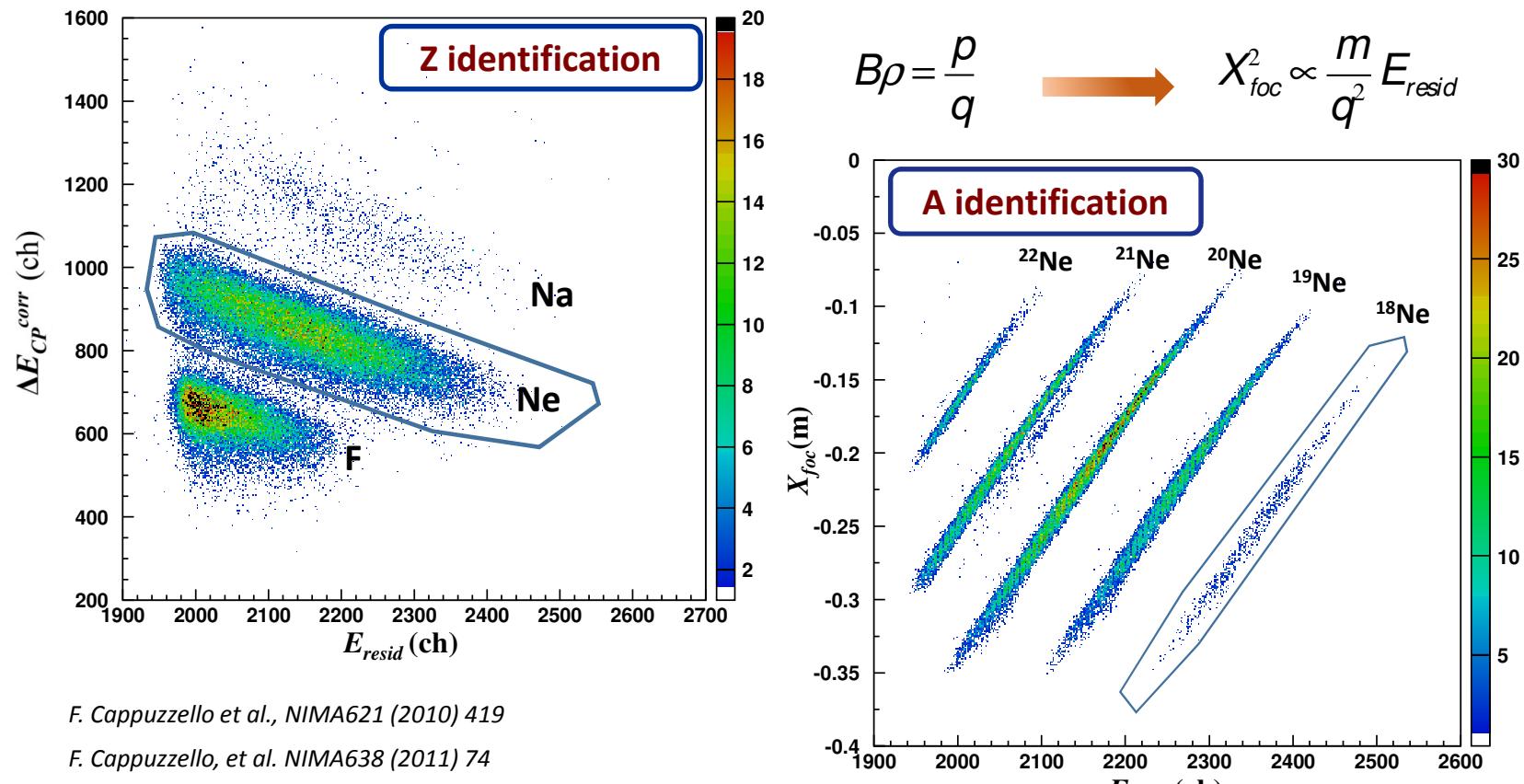


M. Cavallaro et al., NIMA 648 (2011) 46-51

F. Cappuzzello et al., NIMA 638 (2011) 74-82

Particle Identification

$^{40}\text{Ca}(^{18}\text{O}, ^{18}\text{Ne})^{40}\text{Ar}$ @ 270 MeV



F. Cappuzzello et al., NIMA621 (2010) 419

F. Cappuzzello, et al. NIMA638 (2011) 74

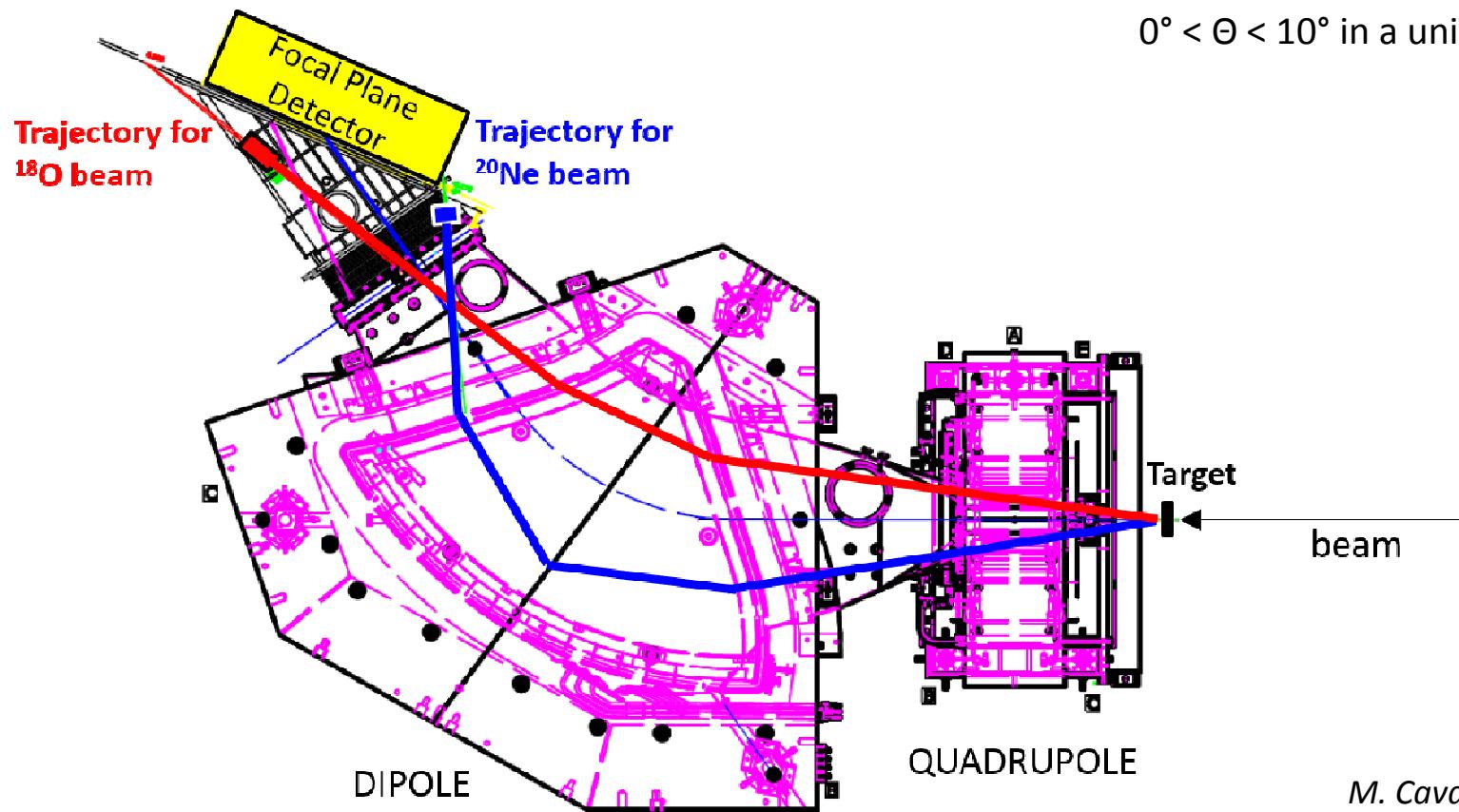
M.Cavallaro et al. EPJ A 48: 59 (2012)

D.Carbone et al. EPJ A 48: 60 (2012)

Cross-section measurement at zero-degrees

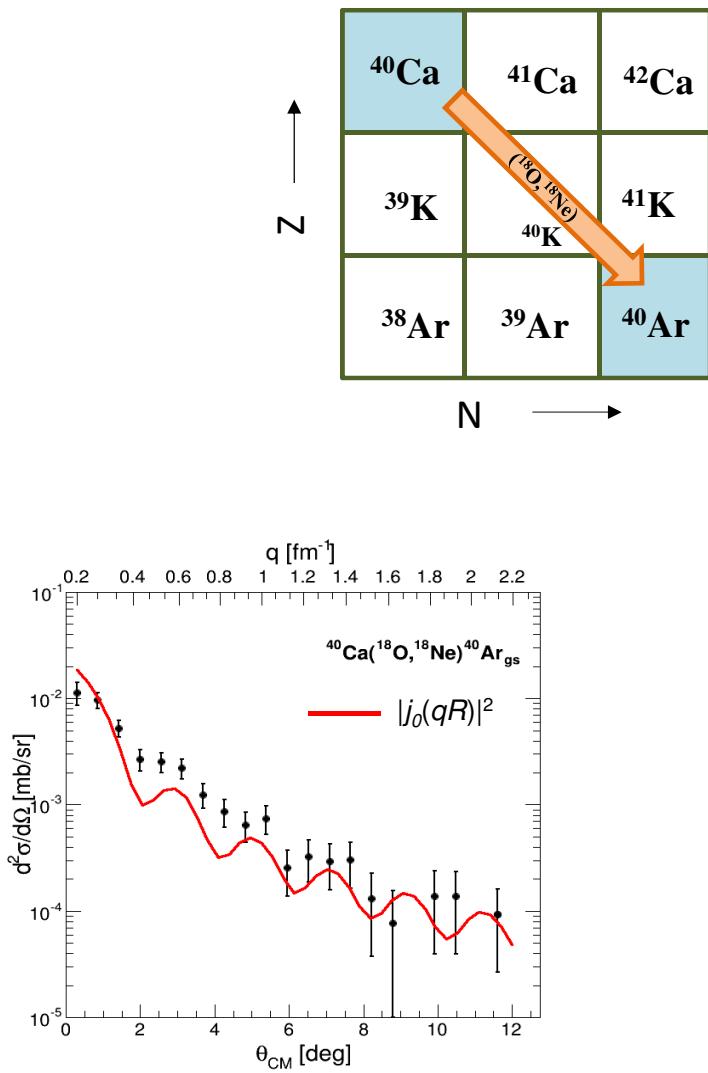
Measurement of the beam current at Faraday Cup

$0^\circ < \Theta < 10^\circ$ in a unique angular setting



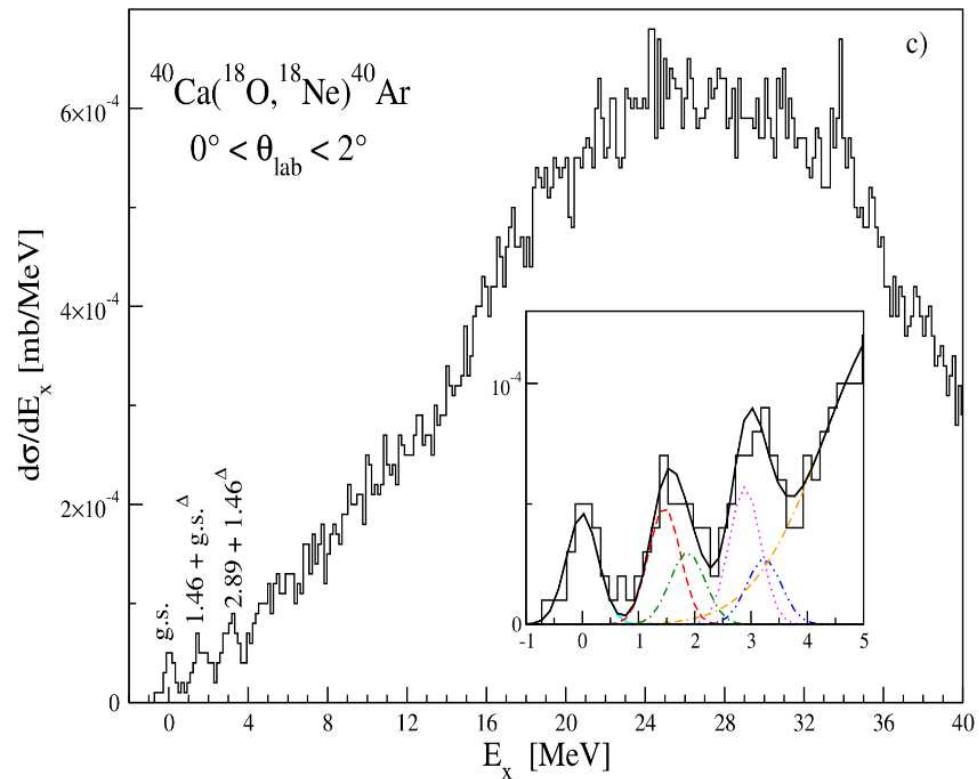
M. Cavallaro et al., NIM B (in press)
<https://doi.org/10.1016/j.nimb.2019.04.069>

The pilot experiment



$^{18}\text{O} + ^{40}\text{Ca}$ at 270 MeV

F. Cappuzzello, et al., Eur. Phys. J. A (2015) 51:145



Experimental feasibility: zero-deg, resolution (500 keV), low cross-section ($\mu\text{b}/\text{sr}$)

Limitations of the past HI-DCE experiments are overcome!

HI-DCE reaction mechanism



H. Lenske Giessen (Germany)
M. Colonna et al. INFN-LNS (Italy)
J.A. Lay Sevilla (Spain)
E.Santopinto et al. Genova (Italy)
J. Lubian et al. UFF (Brasil)

A fundamental property of direct reactions

The complicated many-body heavy-ion scattering problem is largely simplified for direct quasi-elastic reactions

$$V_\alpha(r_\alpha, \chi_\alpha) = U_\alpha(r_\alpha) + W_\alpha(r_\alpha, \chi_\alpha)$$

↓ ↓
Optical potential Residual interaction

For **charge exchange** reactions, $W_\alpha(r_\alpha, \chi_\alpha)$ is ‘small’ and can be treated **perturbatively**

In addition the reactions are **strongly localized at the surface** of the colliding systems and consequently large overlap of nuclear densities are avoided



Accurate description in **fully quantum approach**, eg. Distorted Wave techniques

Microscopic derived double folding potentials are good choices for $U_\alpha(r_\alpha)$

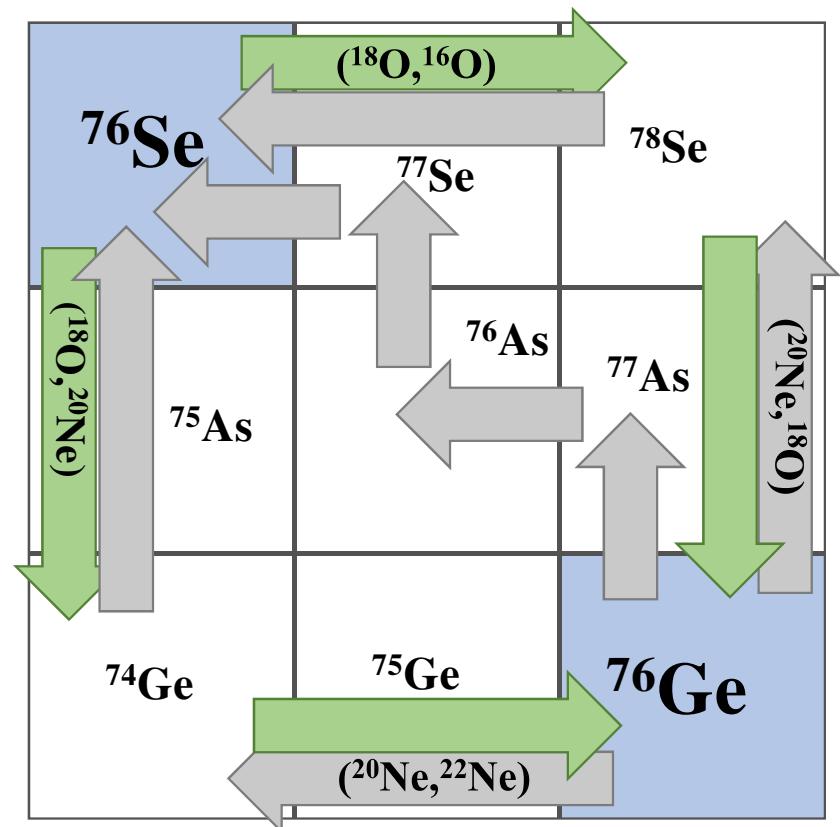
Microscopic form factors work for charge exchange reactions

Cross section is a combination of three different kinds of reaction dynamics

1. Multi-nucleon transfer (proton pick-up/stripping followed by neutron stripping/pick-up)

- ✓ Single-nucleon transfer (mean field driven)
suppressed because of 4th order
- ✓ Sequential transfer of 2p/2n pairs is of 2nd order
- ✓ Transfer or 2p/2n pairs followed by 2n/2p pairs
could be of interest for 0νββ NME

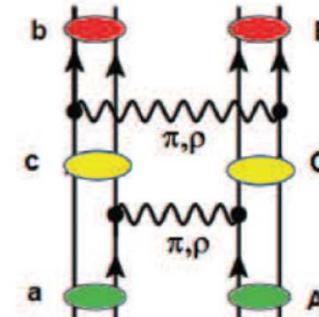
B.A.Brown *et al.* PRL 113, 262501 (2014)



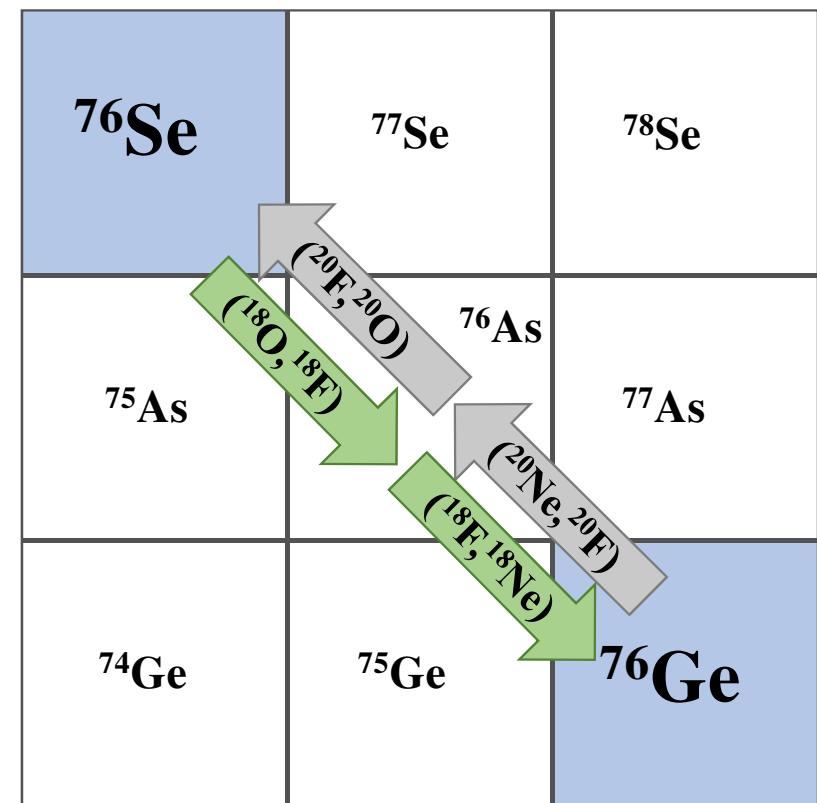
2. Double Single Charge Exchange (DSCE)

DSCE reaction amplitude

$$M_{\alpha\beta}^{(DSCE)} = \langle \chi_{\beta}^{(-)} bB | T_{NN} g T_{NN} | aA \chi_{\alpha}^{(+)} \rangle$$



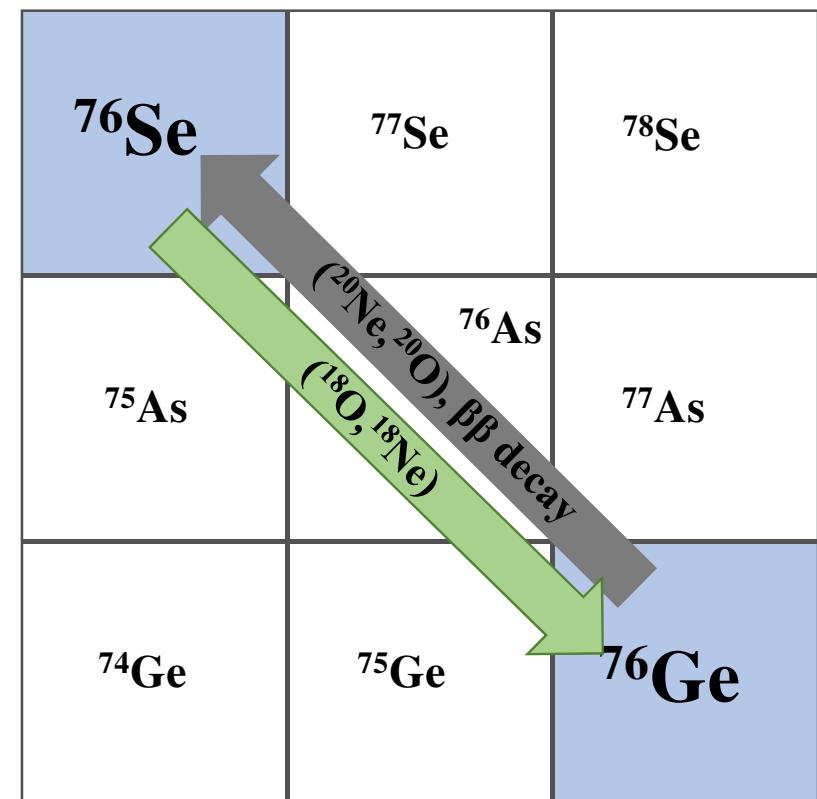
- ✓ **Two-step process** (two consecutive uncorrelated SCE), no correlation between vertices
- ✓ **Probing twice isovector nucleon-nucleon interaction** between a pair of uncorrelated nucleon in the target and projectile
- ✓ **Analogy with $2\nu\beta\beta$ decay** which is a sequential decay process where the leptons are emitted subsequently in an uncorrelated manner.
- ✓ The transition operator will be **dependent on the projectile target combination and on incident energy**. The angular distributions will show the typical behaviour of a two-step reaction, namely a broader and flatter shape. These dependencies may be taken advantage of, for selecting suitable conditions to suppress or enhance DSCE.



3. Correlated Double Charge Exchange ('Majorana' mechanism MDCE)

- ✓ **Probing nucleonic short-range correlations** in the target and projectile (universal phenomena of nuclear matter) independent on the projectile target combination
- ✓ **Probing** nucleus-nucleus Initial (**ISI**) and Final (**FSI**) State Interaction
- ✓ **Correspondence with $0\nu\beta\beta$**

H. Lenske, CERN Proceedings 2019-001 (2019)
H. Lenske et al., Prog. Part. Nuc. Phys. (submitted)
E.Santopinto et al., Phys. Rev. C 98 (2018) 061601(R)

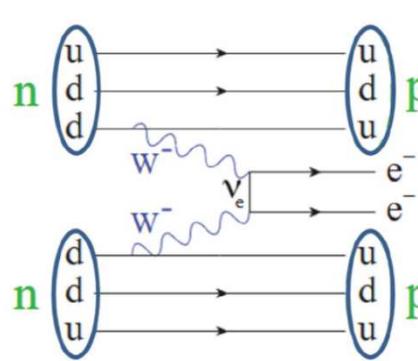


The “Majorana” mechanism for HI-DCE

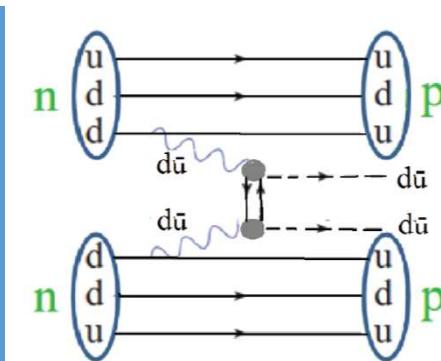
From H. Lenske, CERN Proceedings 2019-001 (2019)

Attempt to identify at elementary level a correspondence between strong and weak interaction

Elementary **weak interaction**
process mediating $0\nu\beta\beta$



Elementary **strong interaction**
process mediating 1-step DCE



The $pp \rightarrow nn\pi^+\pi^+$ reaction and
other double-pion production
channels have been investigated
at CELSIUS, COSY, HADES

Special class of two-body correlation:

- emission of virtual weak gauge boson W,
- exchange of a Majorana neutrino between two nucleons
- and emission of electrons

Can occur, in principle, in an **isolated nucleus**

Also two-body correlation:

- emission of virtual $q\bar{q}$ (π^- , ρ^-)
- exchange of a virtual charge-neutral $q\bar{q}$ pair (π^0 , ρ^0 , σ)
- and emission of charged $q\bar{q}$

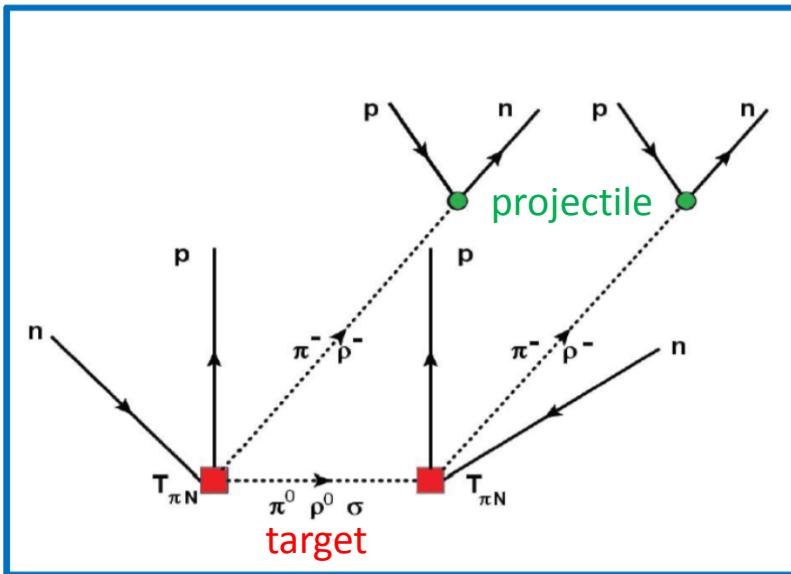
Inhibited by energy conservation, it **requires a reaction partner** which take care of the virtuality of the process by absorbing the two charged virtual mesons (->HIDCE)

The “*Majorana*” mechanism for HI-DCE

From H. Lenske, CERN Proceedings 2019-001 (2019)

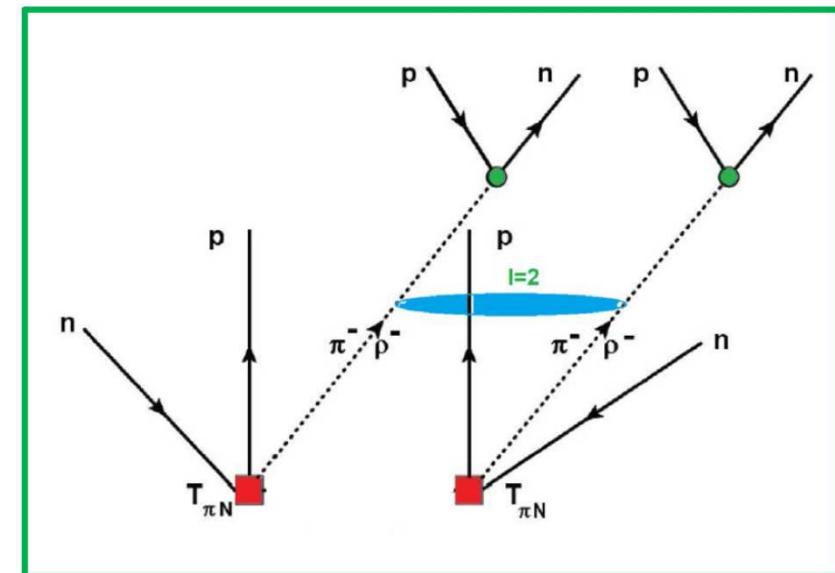
The target undergoes a correlated double meson pair decay and the projectile absorbs it

Correlation between nucleons



Universal because of generic **Short Range Correlation NN** dynamics

The nucleons emit the charged mesons independently and the mesons correlate



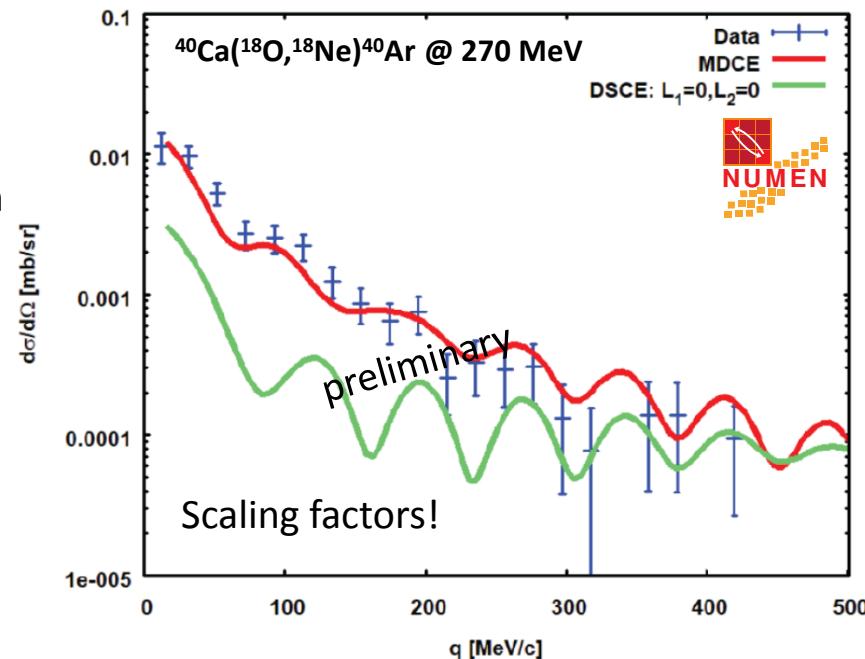
Universal because of generic **meson** dynamics

The “*Majorana*” mechanism for HI-DCE

H. Lenske, CERN Proceedings 2019-001 (2019)

- ✓ ISI and FSI ion-ion interaction from double folding
- ✓ QRPA transition densities for microscopic form factors
- ✓ One-step DWBA for the MDCE amplitudes and two-step DWBA for DSCE

First exploratory calculation



Caveat:

- ✓ Only π -correlations included
- ✓ Off shell momentum structure approximated with on-shell component

Shape of the measured angular distribution to disentangle the two processes??

Encouraging results, but still room for refinements

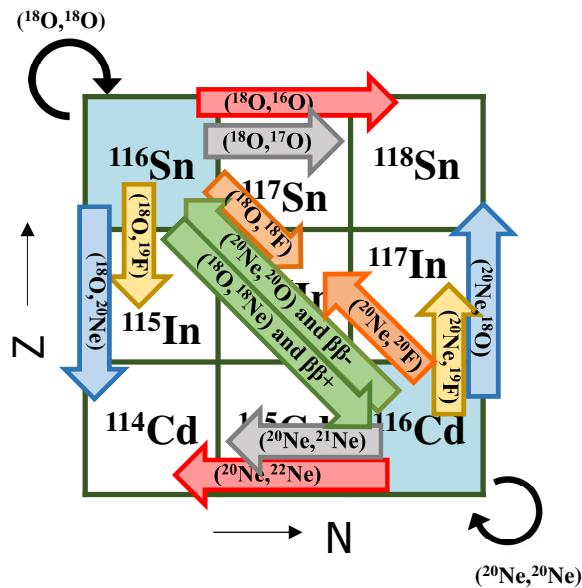
NUMEN runs – Phase 2

NUMEN runs – Phase 2



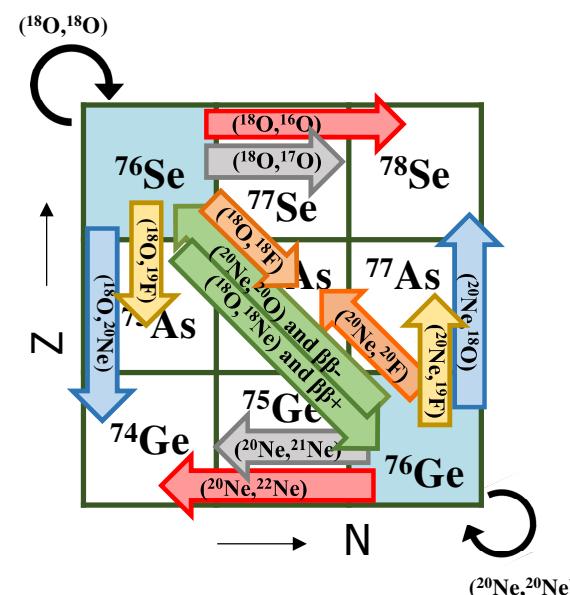
$^{116}\text{Cd} - ^{116}\text{Sn}$ case

@ 15 AMeV
 ➤ $^{18}\text{O} + ^{116}\text{Sn}$
 ➤ $^{20}\text{Ne} + ^{116}\text{Cd}$



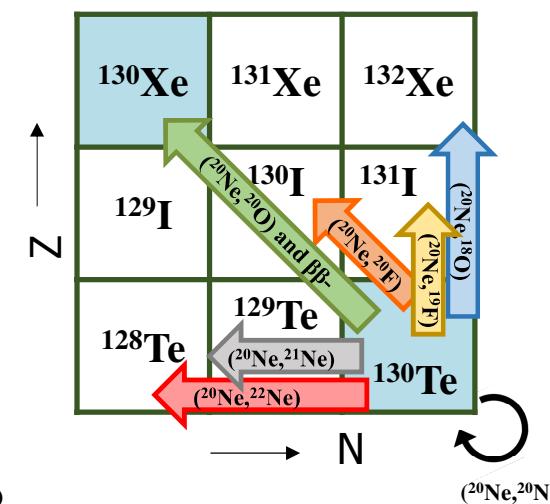
$^{76}\text{Ge} - ^{76}\text{Se}$ case

@ 15 AMeV
 ➤ $^{20}\text{Ne} + ^{76}\text{Ge}$
 ➤ $^{18}\text{O} + ^{76}\text{Se}$



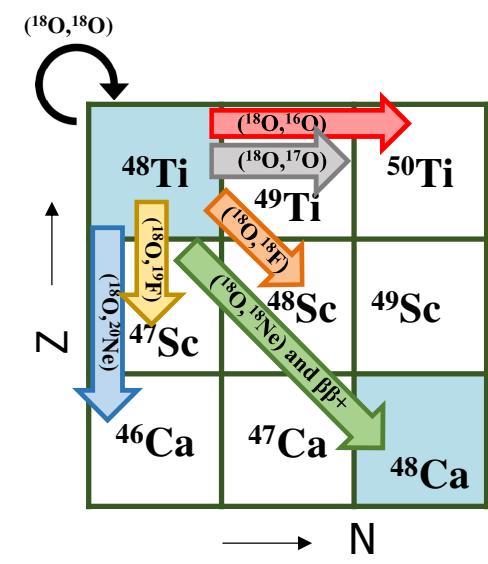
$^{130}\text{Te} - ^{130}\text{Xe}$ case

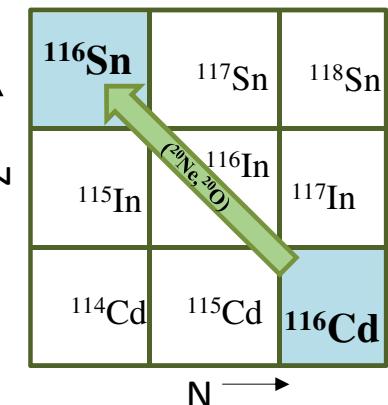
@ 15 AMeV
 ➤ $^{20}\text{Ne} + ^{130}\text{Te}$



$^{48}\text{Ca} - ^{48}\text{Ti}$ case

@ 15 AMeV
 ➤ $^{18}\text{O} + ^{48}\text{Ti}$



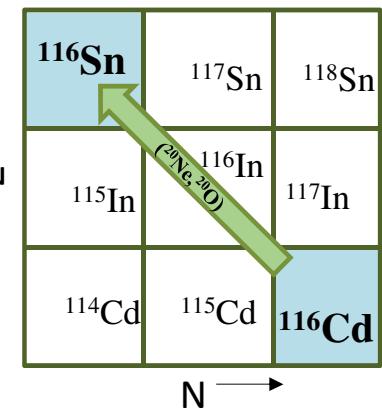


Experimental results

DCE reaction $^{116}\text{Cd}(^{20}\text{Ne}, ^{20}\text{O})^{116}\text{Sn}$

- g.s. \rightarrow g.s. transition isolated (FWHM 800 keV)
- Absolute cross section measured
- Analysis of cross-section sensitivity
 $<0.1 \text{ nb}$ in the Region Of Interest





Experimental results

DCE reaction $^{116}\text{Cd}(^{20}\text{Ne}, ^{20}\text{O})^{116}\text{Sn}$

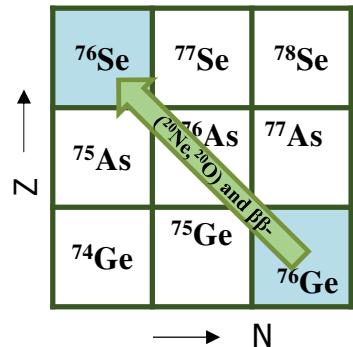


Selective enhancement of the g.s. (scaled for level density)

- Selectivity of the **reaction mechanism** (no fusion, direct process)
- And/or effect of **nuclear structure**
- Importance to describe the **full spectrum** (interference effects on gs NME, collective modes)

Experimental results

DCE $^{76}\text{Ge}({}^{20}\text{Ne}, {}^{20}\text{O}) {}^{76}\text{Se}$ @ 15 AMeV

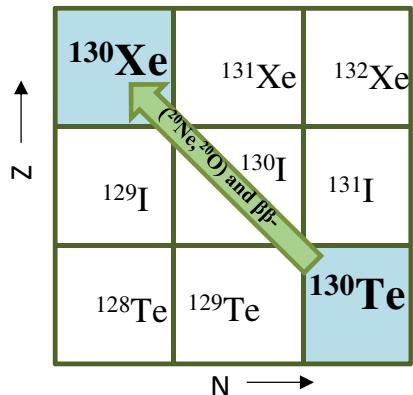


Still very preliminary!

About 50 counts in the ${}^{76}\text{Se}$ ground state region

Experimental results

DCE reaction $^{130}\text{Te}(^{20}\text{Ne}, ^{20}\text{O})^{130}\text{Xe}$



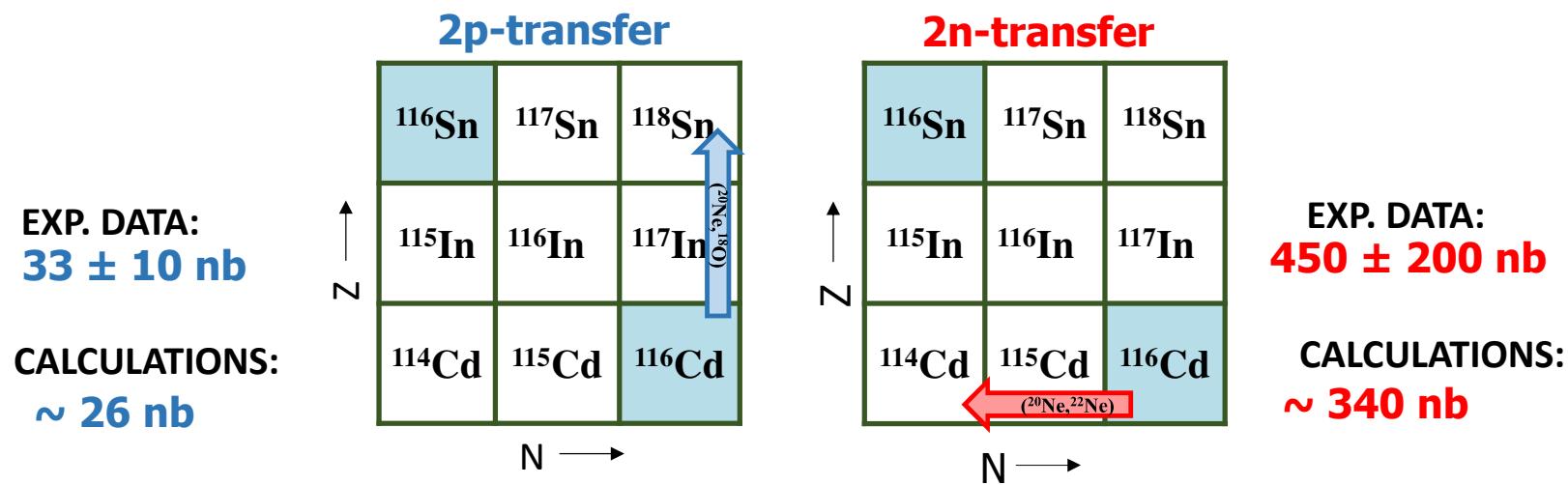
- g.s. \rightarrow g.s. transition maybe isolated
- Absolute cross section measured

Resolution ~ 500 keV FWHM

No spurious counts in the region $-10 < E_x < -2$ MeV

Experimental results

Multi-nucleon transfer



Cross section calculations (DWBA)
ISI and FSI from double folding
SA from IBM, shell model, QRPA

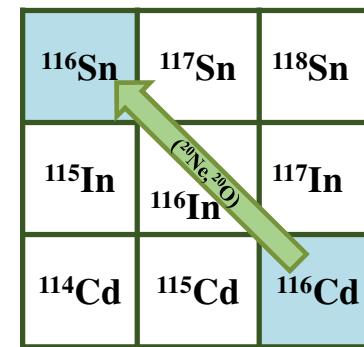


Agreement!

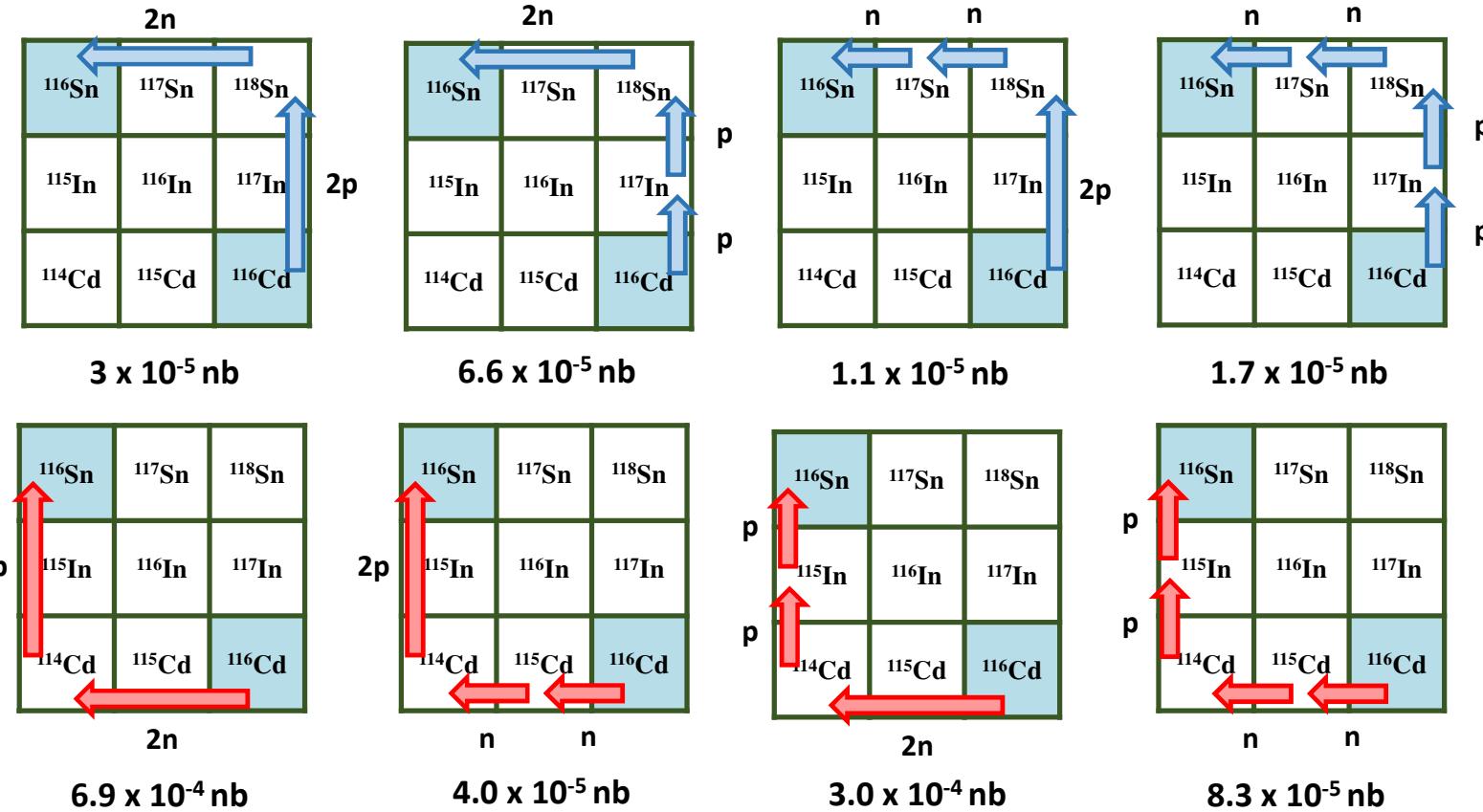
Multi-nucleon transfer routes

vs Diagonal process

(exp. cross section 12 ± 2 nb)



J.L. Ferreira, J. Lubian (UFF)

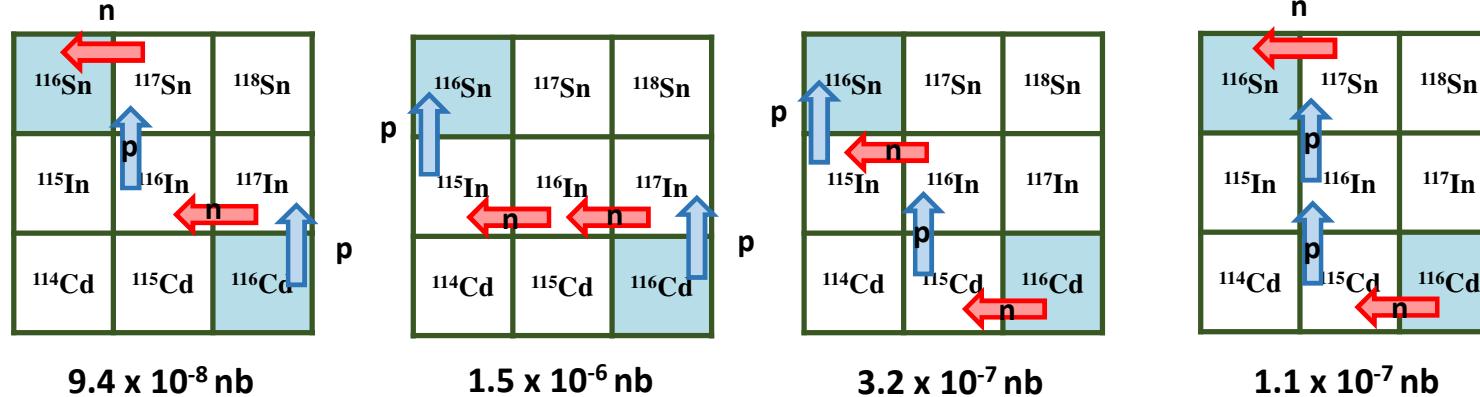


Multi-nucleon transfer routes

vs

Diagonal process

(exp. cross section 12 ± 2 nb)



Negligible contribution of multi-nucleon transfer
on the diagonal DCE process

Interplay between CEX + multi-nucleon transfer
(Work in progress)

Experimental results

Elastic and inelastic scattering $^{76}\text{Ge}({}^{20}\text{Ne}, {}^{20}\text{Ne})^{76}\text{Ge}$ @ 15 AMeV

A. Spatafora *et al.*, PRC (submitted)



Coupling with first low-lying exc. states (CC) to
describe ang. distr. at large momentum transfer



Present experimental limitations

Only few systems can be studied in the present condition (due to the **low cross-sections**)

Moving towards hot-cases

Much higher beam current is needed

Project of **upgrade of the Cyclotron (from 100 W to 5-10 kW)**
and LNS infrastructures (triggered by NUMEN physics case)
funded by national grant (PON) for 19.4 M€
To work with two orders of magnitude more intense beam



Conclusions and Outlooks

- **Second order isospin excitations** of nuclei are key information for interest for nuclear physics and neutrino physics
- Challenging projects on HI-DCE have started
- New results coming out for different systems
- A big challenge for experiments and nuclear theory
- The upgrade for the INFN-LNS cyclotron and the MAGNEX spectrometer will allow to build a unique facility for a systematic exploration of all the nuclei candidate for $0\nu\beta\beta$

Thank you!