

Key stellar & Nuclear Uncertainties in stellar Evolution Modelling

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Keele is Not Kiel (Germany) But Where is it?

West Midlands:



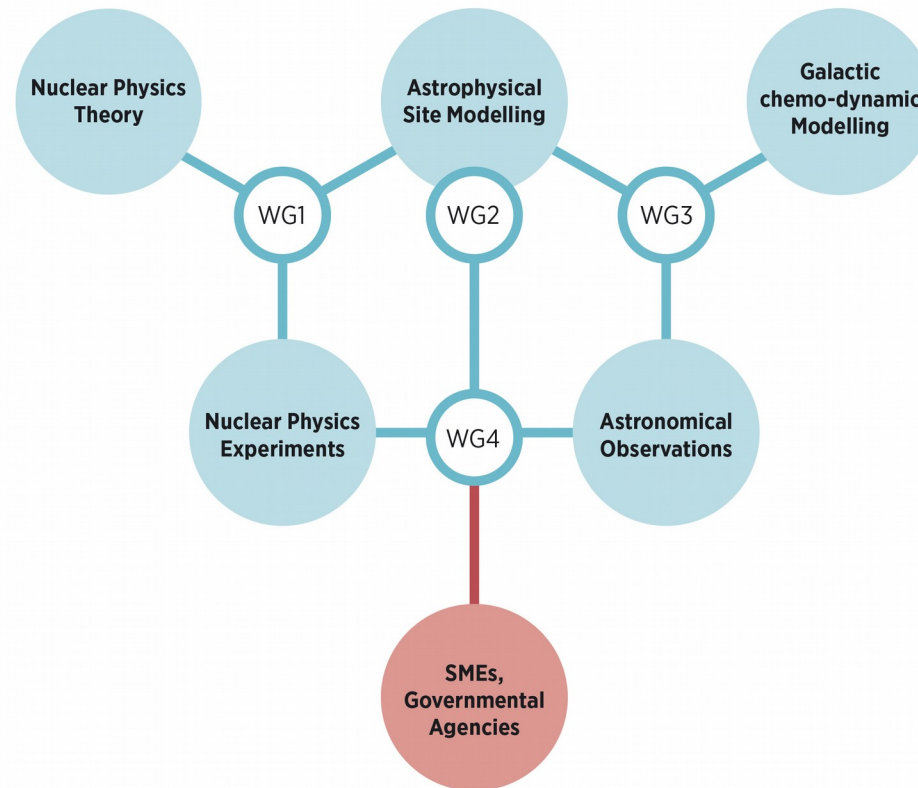
Keele area

is famous for pottery: Wedgwood, ...

Exciting HyDeploy.co.uk / SEND projects

Chemical Elements as Tracers of the Evolution of the Cosmos

A network to bring European research, science and business together to further our understanding of the early universe



Funding for
collaboration
visits: STSMs!!

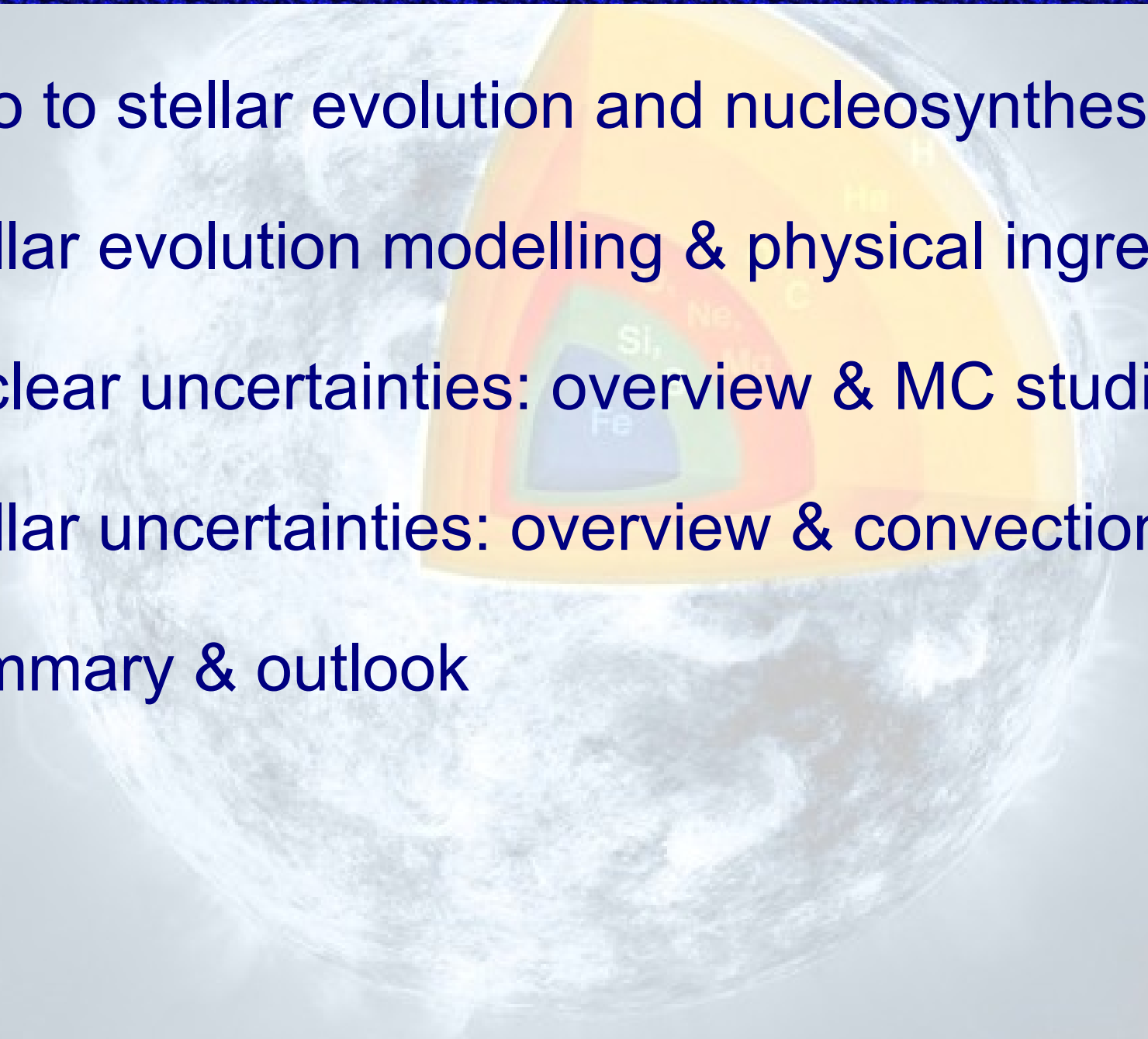
Formal
cooperation with
JINA-CEE
underway!!

30 countries joined ChETEC to coordinate research efforts in Nuclear Astrophysics:

Austria, Belgium, Bulgaria, Czech Rep., Croatia, Denmark, Estonia, Finland, France, Germany, Greece, Hungary, Ireland, Israel, Italy, Lithuania, Malta, The Netherlands, Norway, Poland, Portugal, Romania, Serbia, Slovakia, Slovenia, Spain, Sweden, Switzerland, Turkey and United Kingdom

Plan

- Intro to stellar evolution and nucleosynthesis sites
- Stellar evolution modelling & physical ingredients
- Nuclear uncertainties: overview & MC studies
- Stellar uncertainties: overview & convection
- Summary & outlook



Evolution of Surface Properties

Main sequence:

hydrogen burning

After Main Sequence:

Helium burning

Low and intermediate-mass stars:

MS $\rightarrow$ RG $\rightarrow$ HB/RC $\rightarrow$ AGB $\rightarrow$ WD

Massive stars:

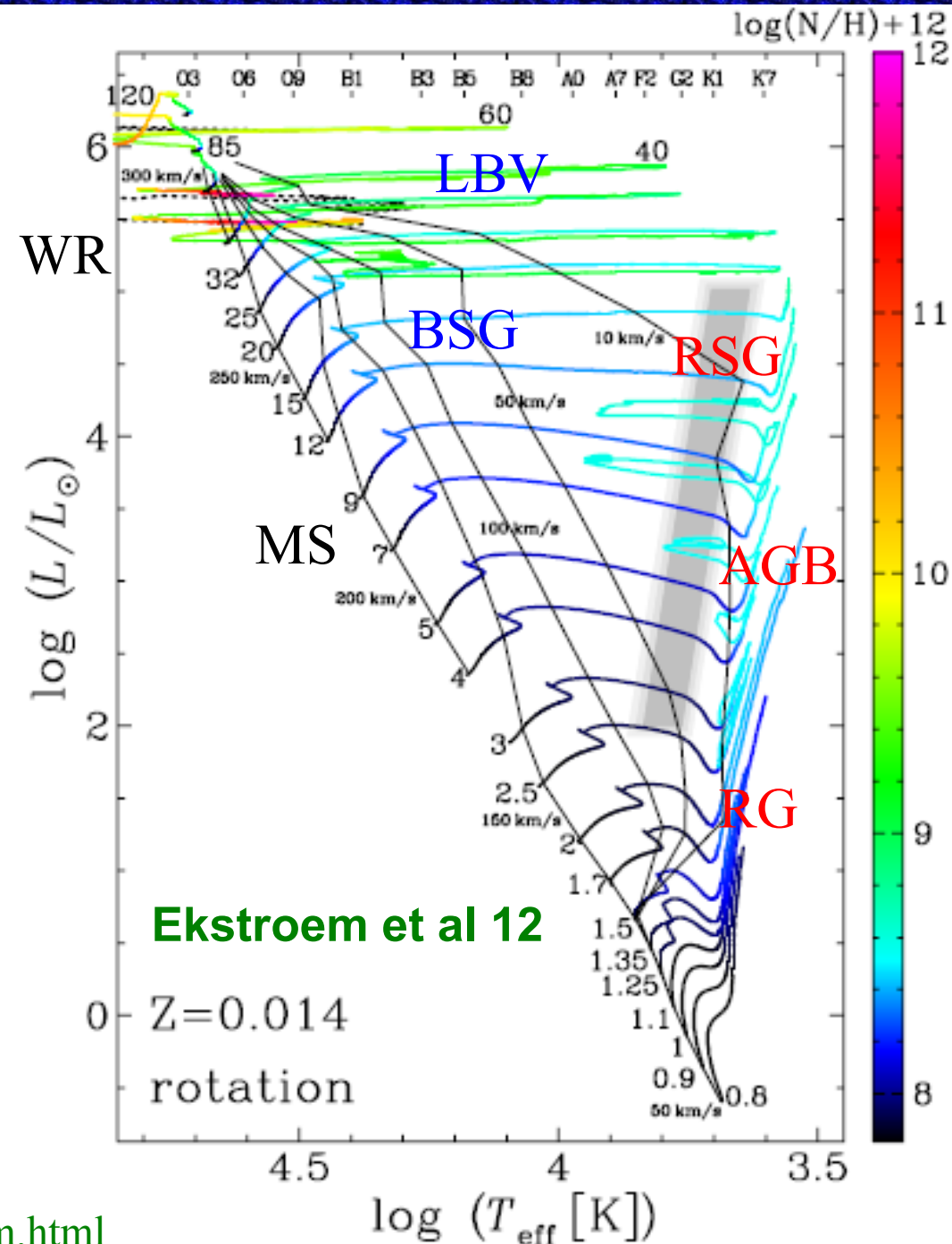
Supergiant stage (red or blue)

Wolf-Rayet (WR): $M > 20\text{--}25 M_{\odot}$

WR without RSG: $M > 40 M_{\odot}$

Advanced stages: C, Ne, O, Si

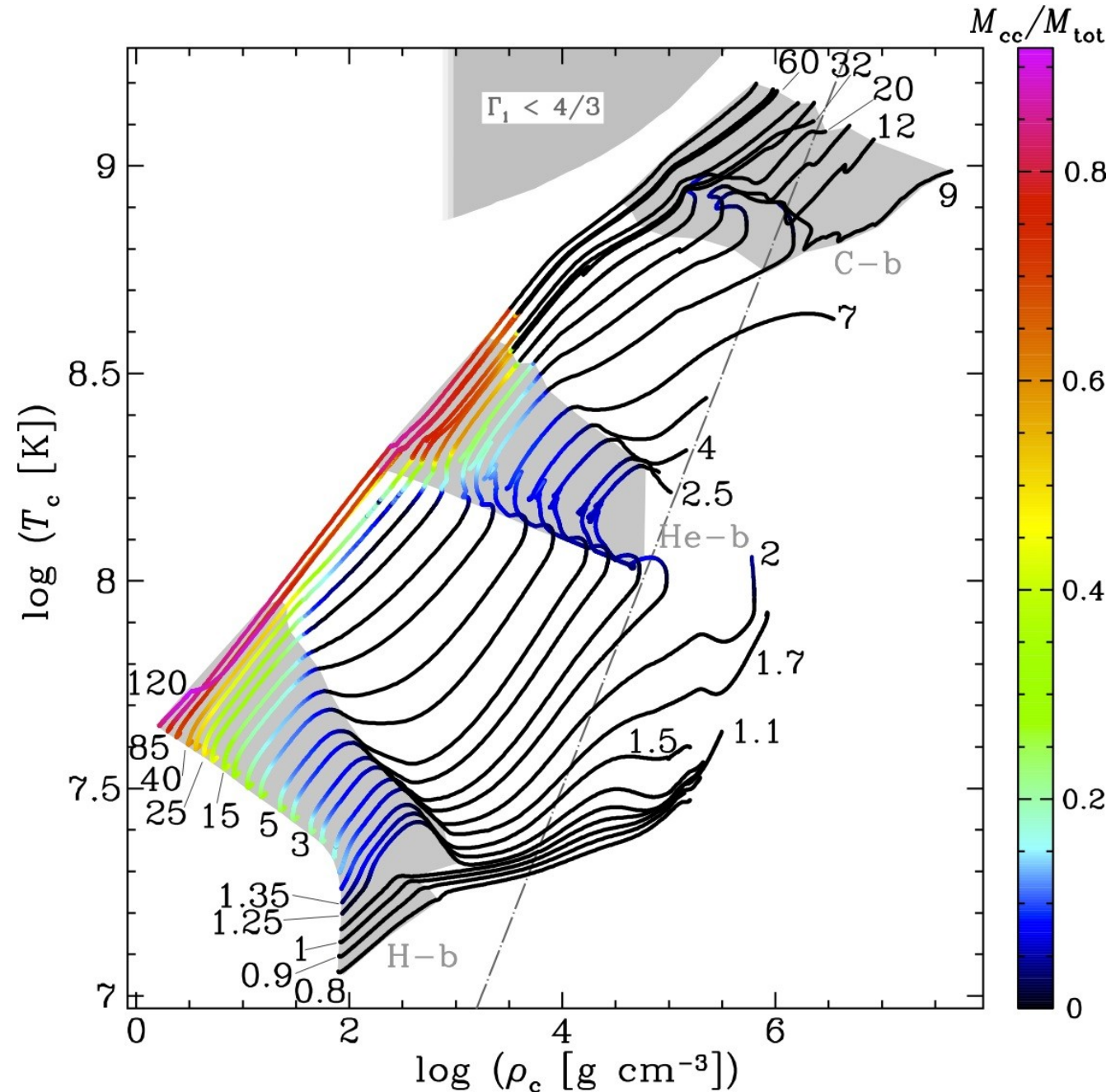
$\rightarrow$ iron core $\rightarrow$ SN/NS/BH



Central Temperature vs Central Density Diagram

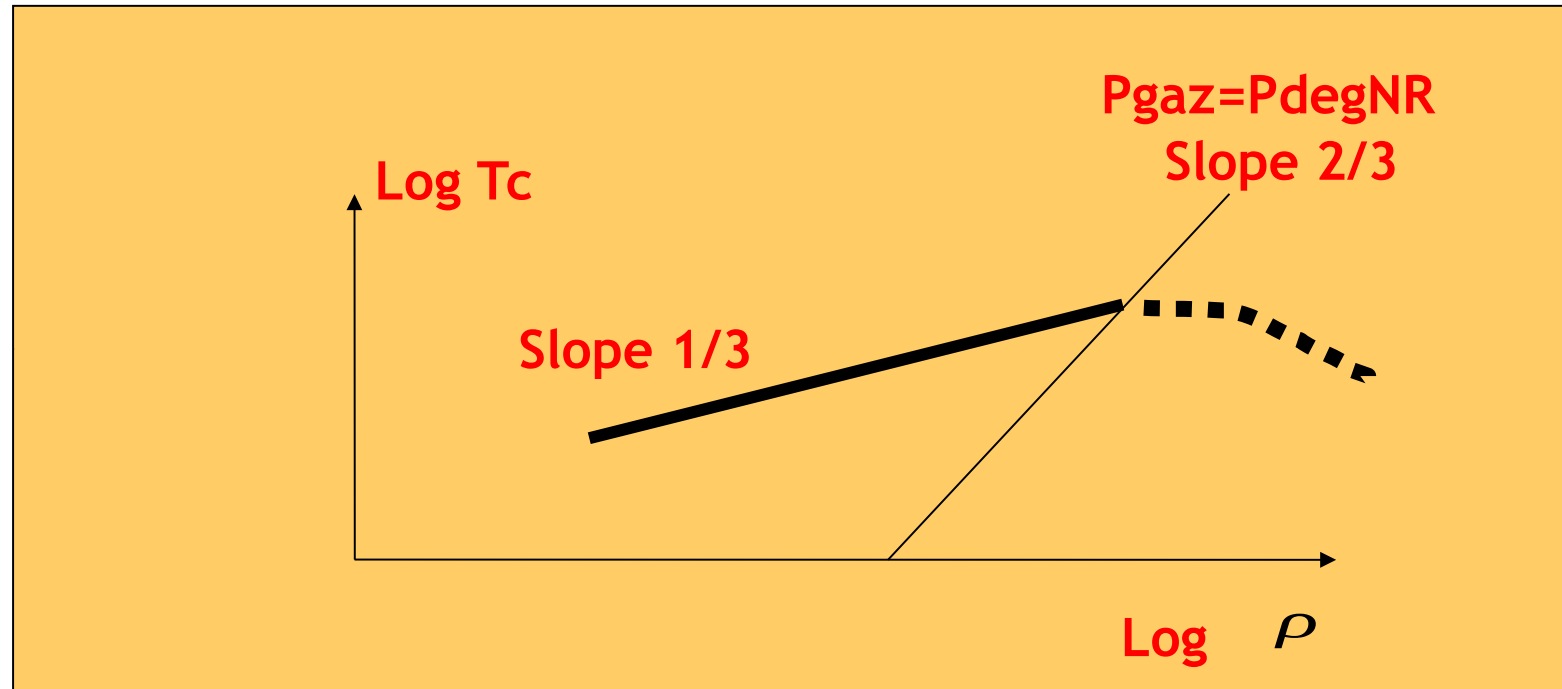
Evolution of central
properties

What is the slope of
the evolutionary
tracks?



Ekstroem et al 12

Evolution of the temperature and density at the centre

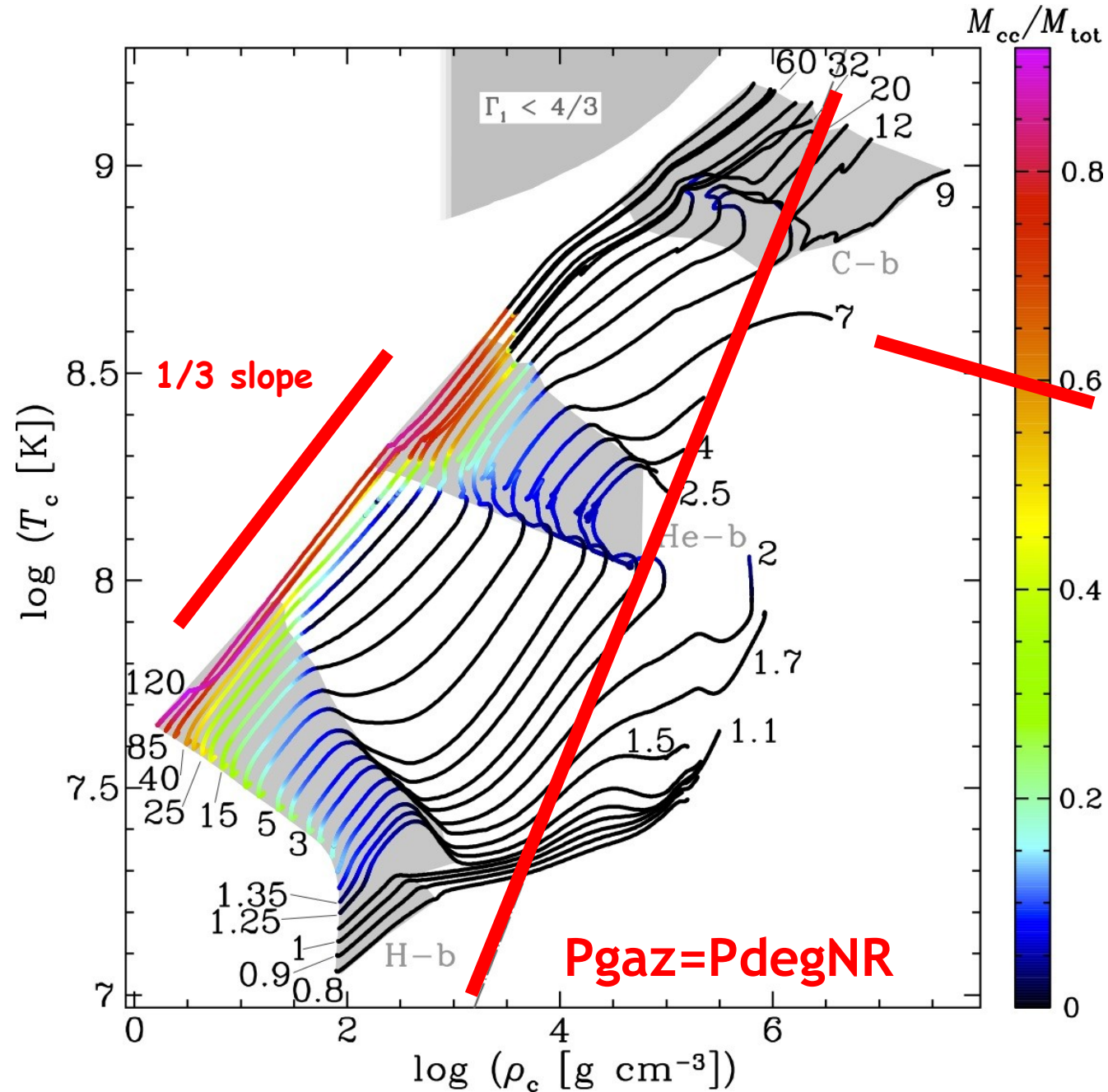


$P_{\text{gaz}} = P_{\text{degNR}}$

$$\frac{k}{\mu m_H} \rho T = K_1 \left(\frac{\rho}{\mu e} \right)^{5/3} \rightarrow T = K_1 \frac{\mu m_H}{k} \frac{1}{\mu_e^{5/3}} \rho^{2/3}$$

Non $\rightarrow$ Degenerate Conditions

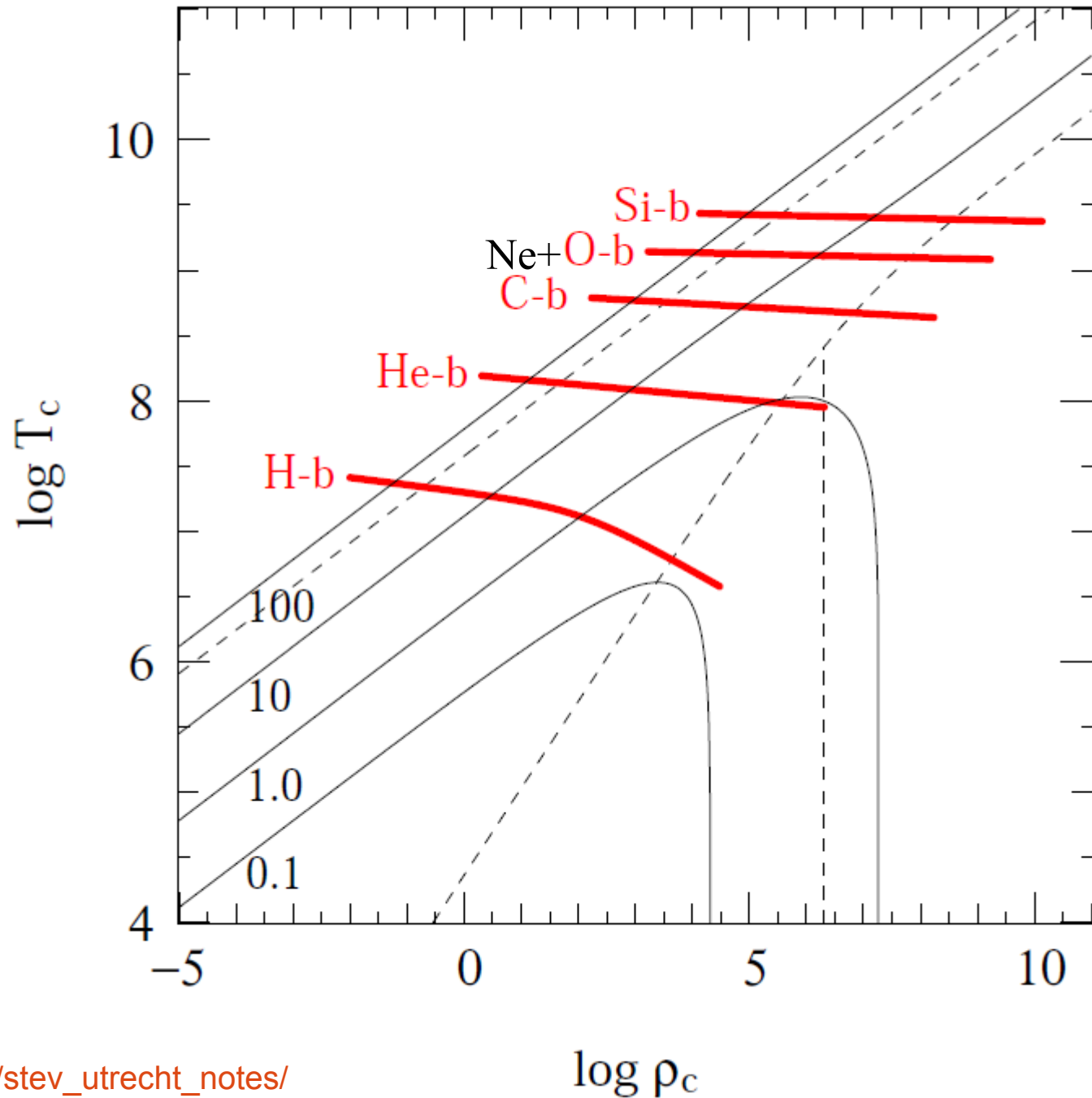
Evolution of central
properties



Ekström et al. (2012)
A&A, 537, A146

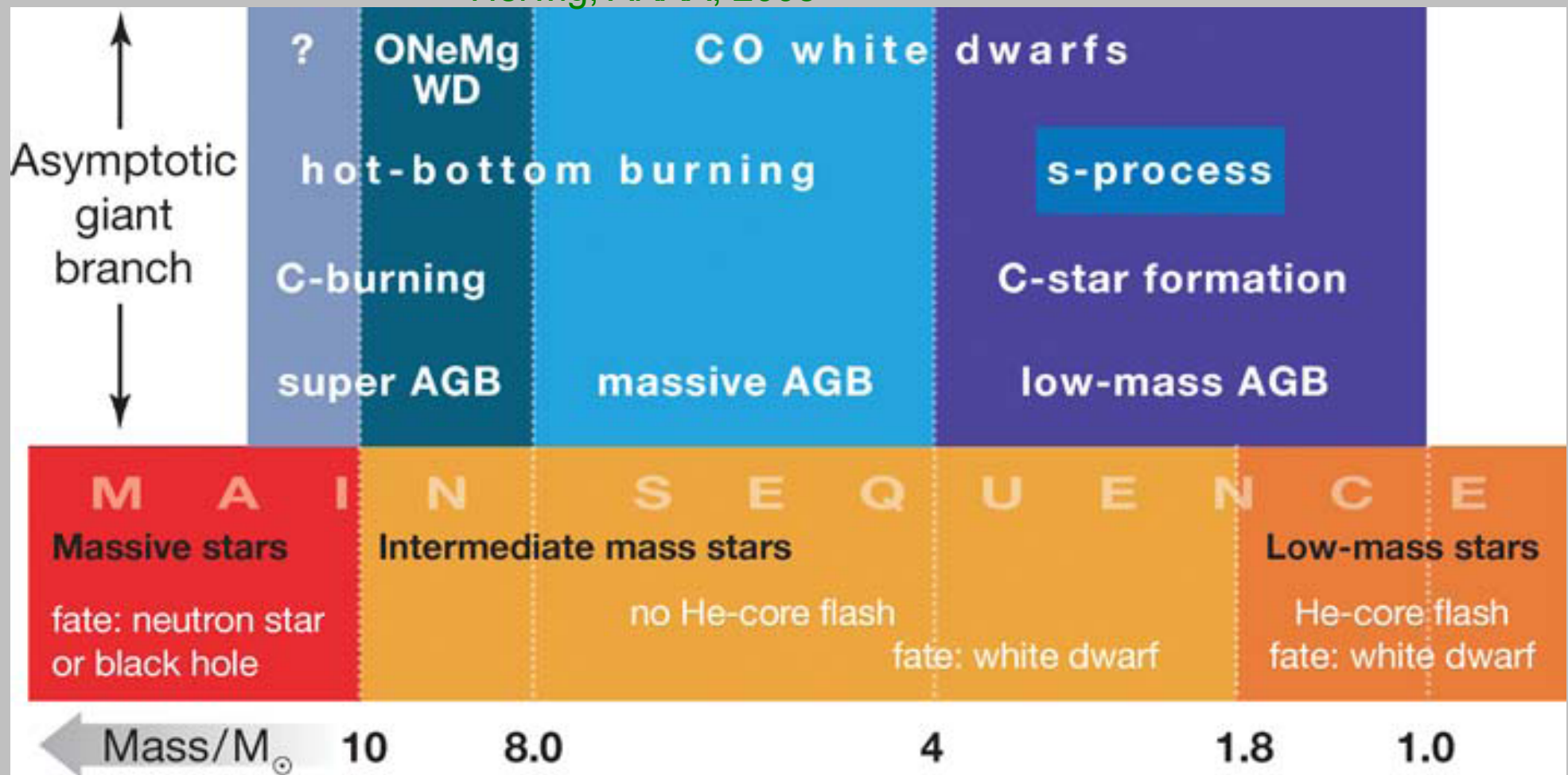
Mass Domains

$$\epsilon_{\text{nuc}} = \epsilon_0 \rho^\lambda T^\nu$$



Mass Domains

Herwig, ARAA, 2005

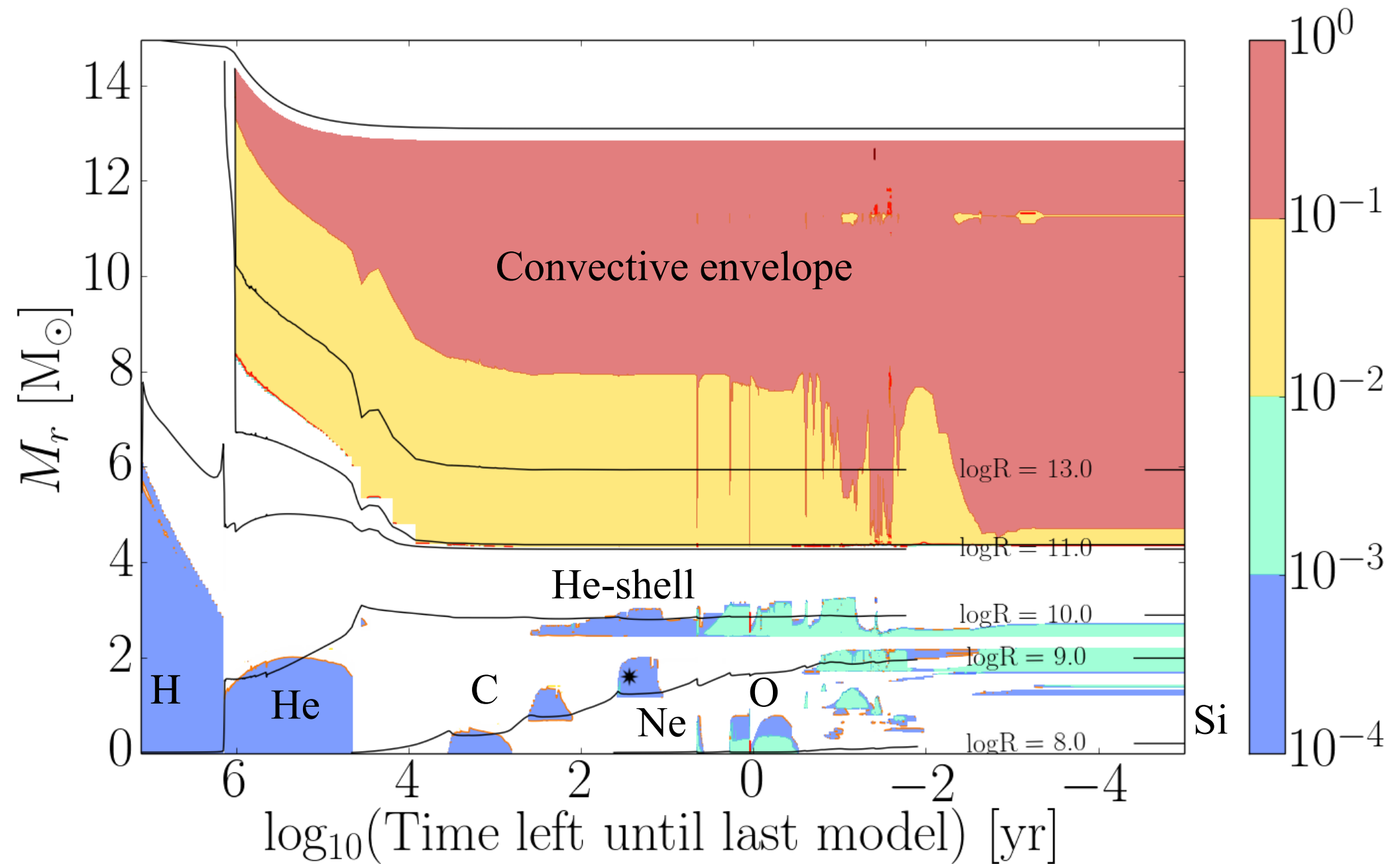


Massive stars: $> 9 M_{\odot}$: go through all burning stages

Intermediate-mass stars: $1.8 - 9 M_{\odot}$ do not ignite C-burning in centre (C-flash for SAGB stars)

Low-mass stars: $< 1.8 M_{\odot}$ do not ignite He-burning in centre (He-flash)

Structure Evolution of Massive Stars



Convection takes place during most burning stages

Massive Stars: Evolution of the chemical composition

Burning stages (lifetime [yr]):

Hydrogen (10^{6-7}): $^1\text{H} \rightarrow ^4\text{He}$

& $^{12}\text{C}, ^{16}\text{O} \rightarrow ^{14}\text{N}$

Helium (10^{5-6}): $^4\text{He} \rightarrow ^{12}\text{C}, ^{16}\text{O}$

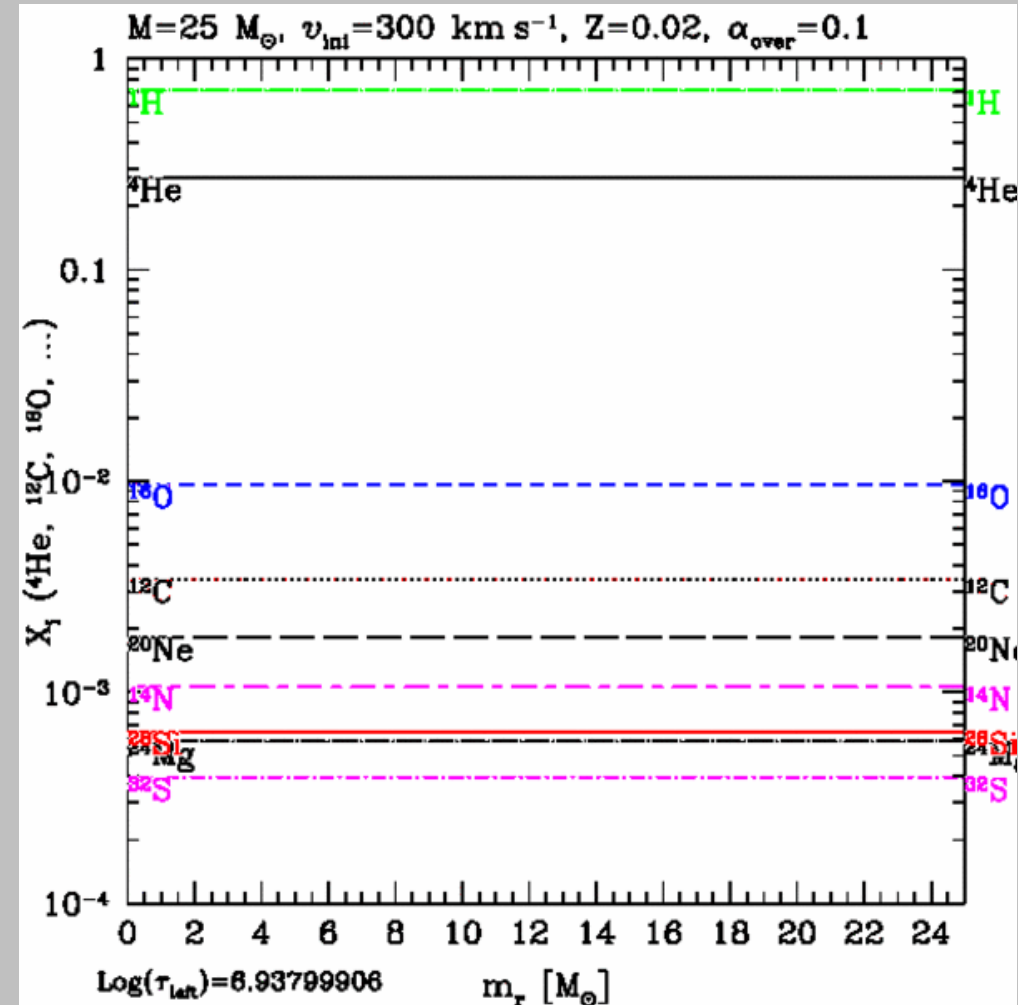
& $^{14}\text{N} \rightarrow ^{18}\text{O} \rightarrow ^{22}\text{Ne}$

Carbon (10^{2-3}): $^{12}\text{C} \rightarrow ^{20}\text{Ne}, ^{24}\text{Mg}$

Neon (0.1-1): $^{20}\text{Ne} \rightarrow ^{16}\text{O}, ^{24}\text{Mg}$

Oxygen (0.1-1): $^{16}\text{O} \rightarrow ^{28}\text{Si}, ^{32}\text{S}$

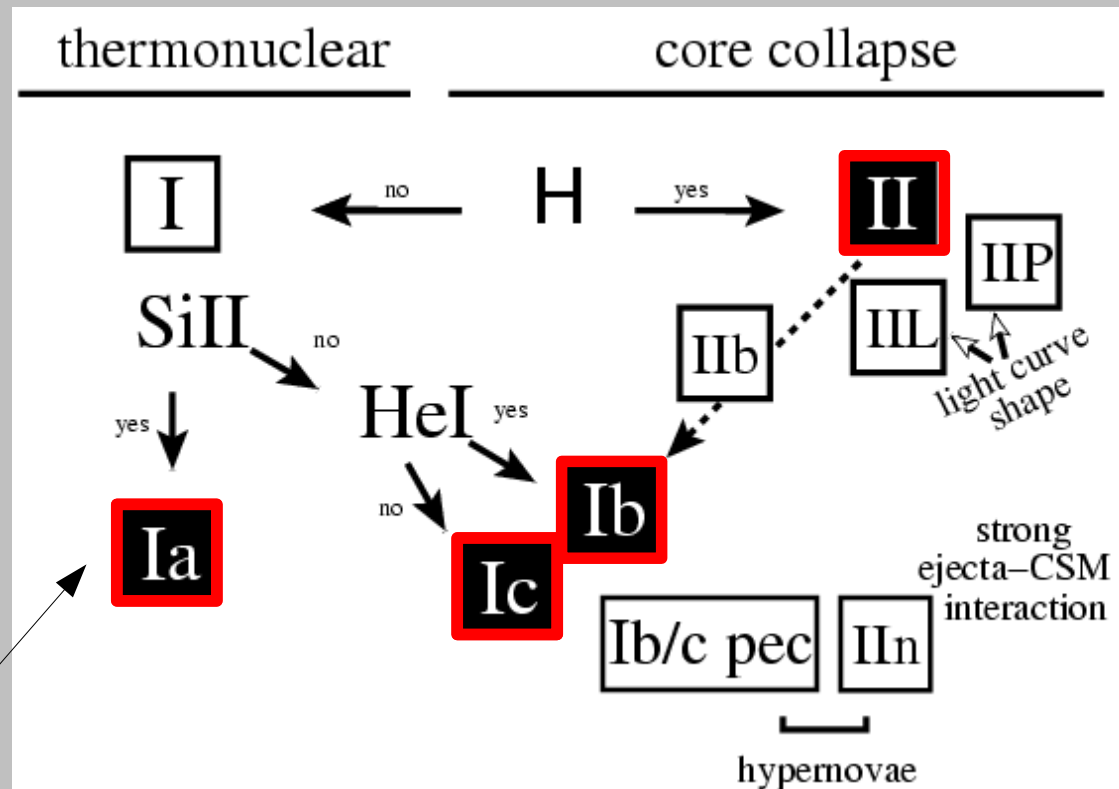
Silicon (10^{-3}): $^{28}\text{Si}, ^{32}\text{S} \rightarrow ^{56}\text{Ni}$



<http://www.astro.keele.ac.uk/~hirschi/animation/anim.html>

Supernova Explosion Types

Massive stars: → **SN II** (H envelope),
Ib (no H), **Ic** (no H & He) ← WR

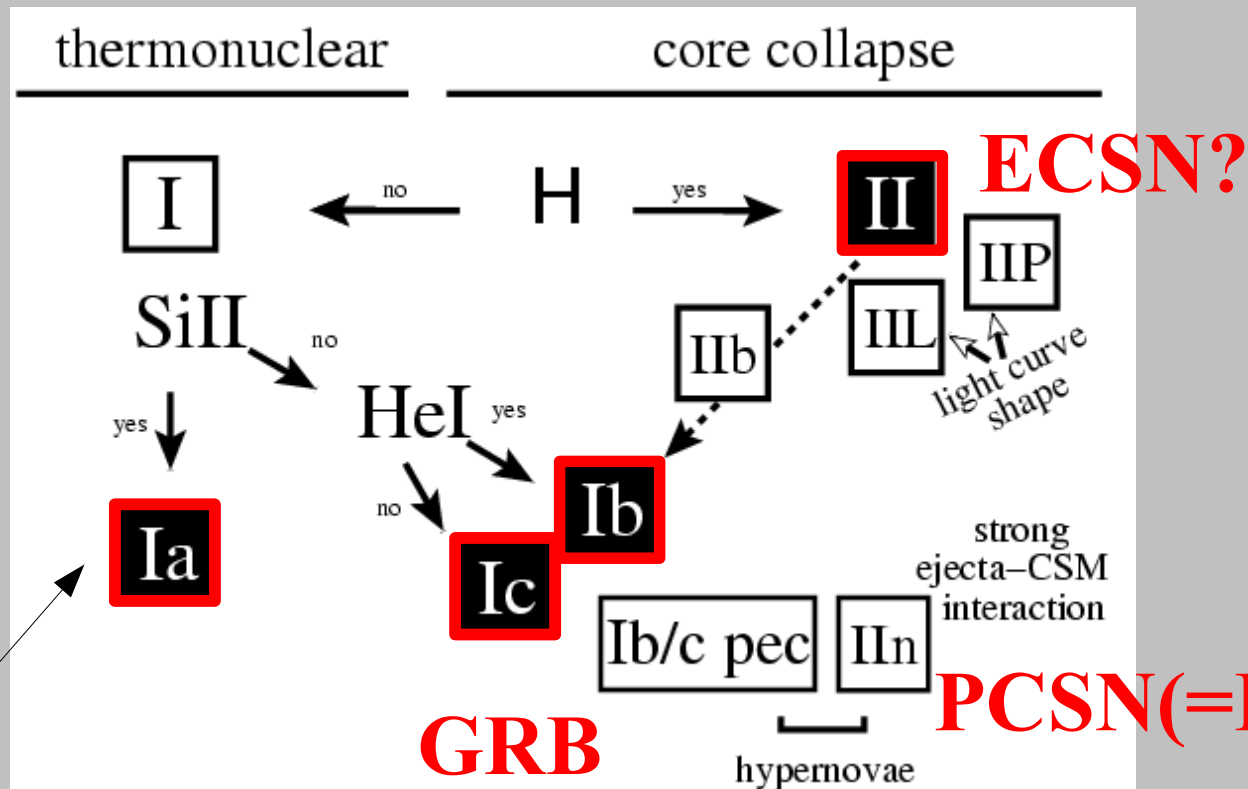


White dwarfs (WD):
in binary systems
Accretion →
Chandrasekhar
mass → SN **Ia**

(Turatto 03)

Supernova Explosion Types

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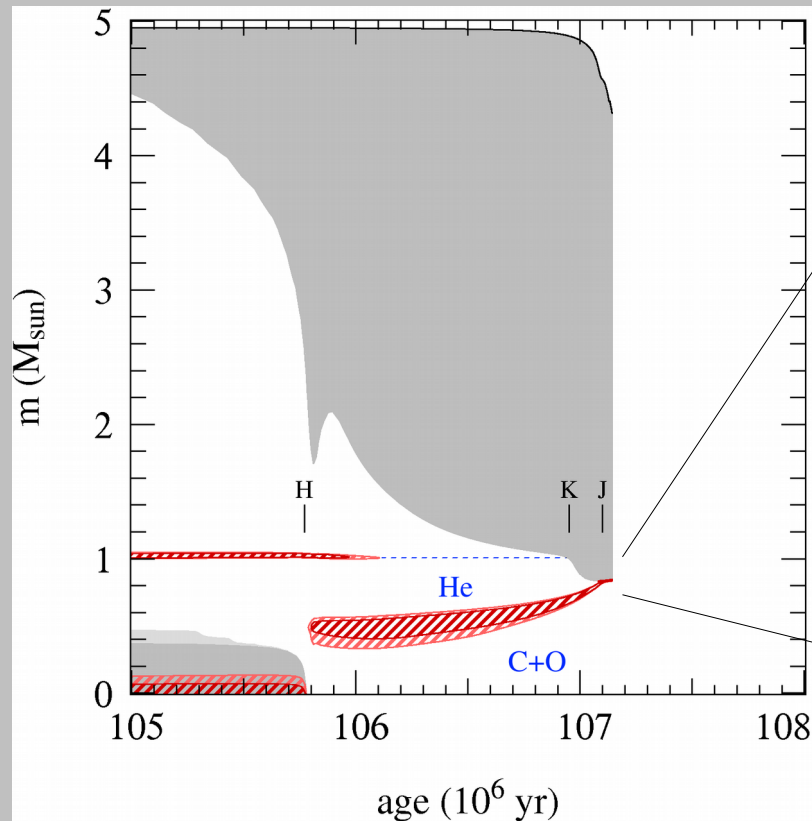
White dwarfs (WD):
 in binary systems
 Accretion →
 Chandrasekhar
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(Hirschi+05
 Woosley+06
 Yoon+06, ...)

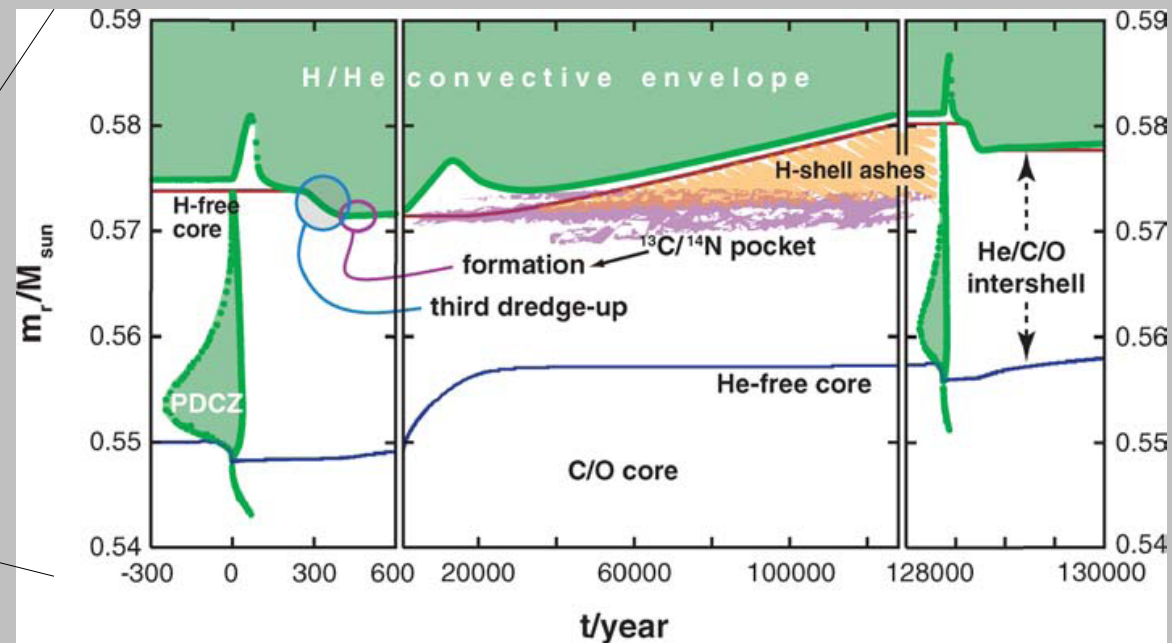
(Turatto 03)

Intermediate & Low-Mass Stars

5 $M_{\odot}$ star: AGB phase



Structure in AGB phase



Herwig, ARAA, 2005

From SE notes, O. Pols (2009)

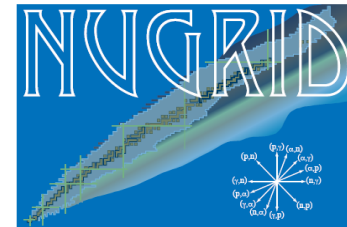
Woosley, Heger
& Weaver,
2002 RvMP
Vol. 74.
p. 1015

See Ritter+
2018,
MNRAS
For full grid of
models

TABLE III. The origin of the light and intermediate-mass elements.					
Species	Origin	Species	Origin	Species	Origin
¹ H	BB	³⁰ Si	C,Ne	⁵¹ V	α , Ia-det, xSi, xO, ν
² H	BB	³¹ P	C,Ne	⁵⁰ Cr	xSi, xO, α , Ia-det
³ He	BB, L*	³² S	xO, O	⁵² Cr	xSi, α , Ia-det
⁴ He	BB, L*, H	³³ S	xO, xNe	⁵³ Cr	xO, xSi
⁶ Li	CR	³⁴ S	xO, O	⁵⁴ Cr	nse-IaMCh
⁷ Li	BB, ν , L*, CR	³⁶ S	He(s), C, Ne	⁵⁵ Mn	Ia, xSi, ν
⁹ Be	CR	³⁵ Cl	xO, xNe, ν	⁵⁴ Fe	Ia, xSi
¹⁰ B	CR	³⁷ Cl	He(s), xO, xNe	⁵⁶ Fe	xSi, Ia
¹¹ B	ν	³⁶ Ar	xO, O	⁵⁷ Fe	xSi, Ia
¹² C	L*, He	³⁸ Ar	xO, O	⁵⁸ Fe	He(s), nse-IaMCh
¹³ C	L*, H	⁴⁰ Ar	He(s), C, Ne	⁵⁹ Co	He(s), α , Ia, ν
¹⁴ N	L*, H	³⁹ K	xO, O, ν	⁵⁸ Ni	α
¹⁵ N	novae, ν	⁴⁰ K	He(s), C, Ne	⁶⁰ Ni	α , He(s)
¹⁶ O	He	⁴¹ K	xO	⁶¹ Ni	He(s), α , Ia-det
¹⁷ O	novae, L*	⁴⁰ Ca	xO, O	⁶² Ni	He(s), α
¹⁸ O	He	⁴² Ca	xO	⁶⁴ Ni	He(s)
¹⁹ F	ν , He, L*	⁴³ Ca	C, Ne, α	⁶³ Cu	He(s), C, Ne
²⁰ Ne	C	⁴⁴ Ca	α , Ia-det	⁶⁵ Cu	He(s)
²¹ Ne	C	⁴⁶ Ca	C, Ne	⁶⁴ Zn	ν -wind, α , He(s)
²² Ne	He	⁴⁸ Ca	nse-IaMCh	⁶⁶ Zn	He(s), α , nse-IaMCh
²³ Na	C, Ne, H	⁴⁵ Sc	α , C, Ne, ν	⁶⁷ Zn	He(s)
²⁴ Mg	C, Ne	⁴⁶ Ti	xO, Ia-det	⁶⁸ Zn	He(s)
²⁵ Mg	C, Ne	⁴⁷ Ti	Ia-det, xO, xSi	<i>r</i>	ν -wind
²⁶ Mg	C, Ne	⁴⁸ Ti	xSi, Ia-det	<i>p</i>	xNe, O
²⁷ Al	C, Ne	⁴⁹ Ti	xSi	<i>s</i> (A < 90)	He(s)
²⁸ Si	xO, O	⁵⁰ Ti	nse-IaMCh, He(s)	<i>s</i> (A > 90)	L*
²⁹ Si	C, Ne	⁵⁰ V	C, Ne, xNe, xO		

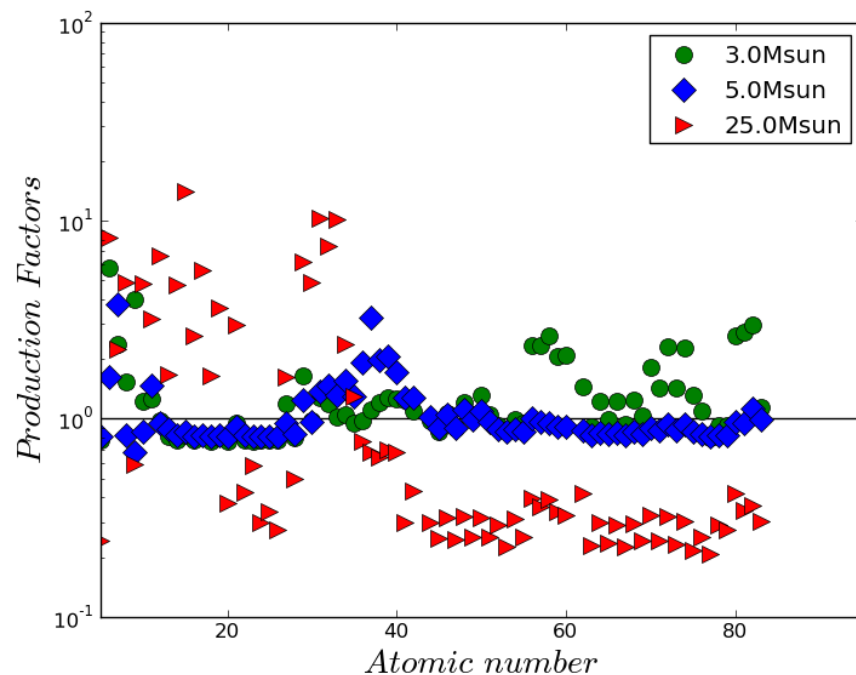
NuGrid :

- www.nugridstars.org
- data.nugridstars.org
- wendi.nugridstars.org

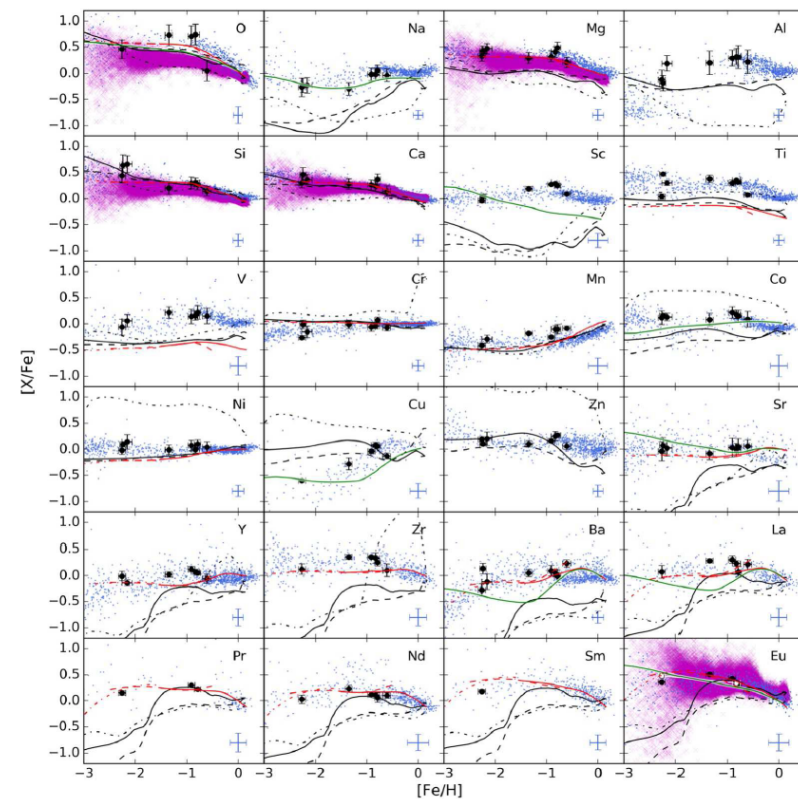


The Nucleosynthesis Grid (NuGrid) project maintains and develops tools for post-processing nucleosynthesis simulations, and applies these to produce complete sets of stellar yields.

Ritter+RH+2018, MNRAS



Final elemental production factors for a low mass AGB star (3 Msun), a massive AGB star (5 Msun), and a massive star (25 Msun) (MP+2016 ApJS, CR+18, MNRAS).



GCE simulations: OMEGA vs other codes, NuGrid yields vs other yields (BC+17, ...).

Stellar Models:

Stellar structure equations + physical ingredients:

- Nuclear reactions
 - Mass loss
 - Rotation
 - Convection
 - Magnetic fields
 - Binary interactions
 - Equation of state, opacities & neutrino losses
- including metallicity dependence

Stellar Structure Equations

The four structure equations to be solved are:

$$\begin{aligned}\frac{\partial r}{\partial m} &= \frac{1}{4\pi r^2 \rho} \\ \frac{\partial P}{\partial m} &= -\frac{Gm}{4\pi r^4} - \frac{1}{4\pi r^2} \frac{\partial^2 r}{\partial t^2} \\ \frac{\partial L_r}{\partial m} &= \epsilon_n - \epsilon_\nu - c_P \frac{\partial T}{\partial t} + \frac{\delta}{\rho} \frac{\partial P}{\partial t} \\ \frac{\partial T}{\partial m} &= -\frac{GmT}{4\pi r^4 P} \nabla\end{aligned}$$

(Assuming spherical symmetry: one-dimensional model)

Uncertain Nuclear Reactions

- Charged-particle reactions:

Key uncertain reactions dominating energy generation during secular evolution have already been identified

Explosive environments (e.g. Novae) have additional uncertain rates

- Weak interactions & neutron-captures:

Many reactions involved in e.g. s process.

How can we determine which are key?

Bottlenecks, branching points, neutron source/poison reactions

How to consider current uncertainty and importance?

Monte Carlo Sensitivity Studies

Monte Carlo Framework:

- PizBuin MC-wrapper

Rauscher+ 2016MNRAS.463.4153R

- Simple “brute force” approach
- Parallelised using OpenMP

Nuclear Reaction Network:

- Solver: WinNet (Winteler+ 12)
 - Reaction rates $\leftarrow$ reaclib (Rauscher & Thielemann 00)
- = McWinNet

beta-decay & (n,g) uncertainties are T-dependent!

Largest simulations: ~ 1000 trajectories $\times \sim 1$ min per run
 $\times 10,000$ MC iterations



Piz Buin mountain

Temp.-Dependent Uncertainties for (n,g)

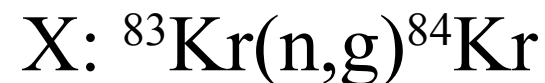
For details, see **T. Rauscher, ApJL, 775, 2011**

- Theoretical

- basic rates: ReacliB (Rauscher & Thielemann 2000)
- a constant **factor 2**

- Experimental

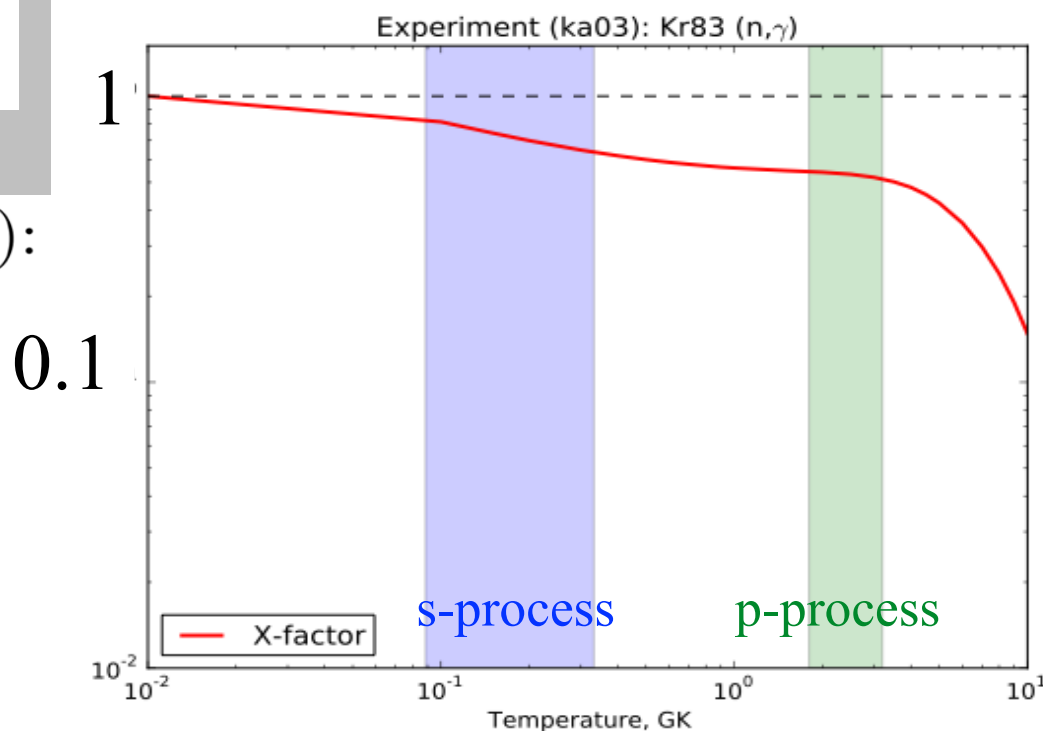
- base rates: KADoNiS v0.3 (Dillemann et al., 2009)
- the formula: Rauscher, ApJ, 775, 2011



$$U(T) = U_{\text{g.s.}}X + U_{\text{e.s.}}(1 - X)$$

- ground state (experimental based):
 $u_{\text{g.s.}} \sim 1.0 - 1.3$
- excited states (theory based):
 $u_{\text{e.s.}} = 5$ (given constant)

$X(T)$: the fraction of particles
in the ground state



Temp.-Dependent Uncertainties for beta-Decays

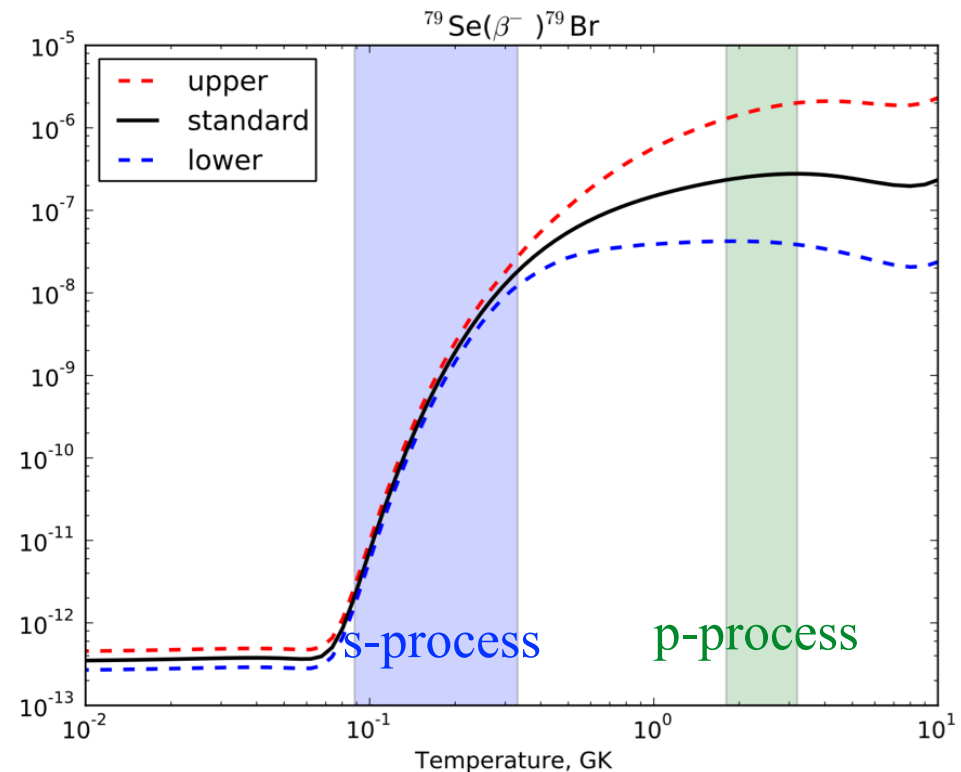
- beta-decay: only the ground state 1.3 (30%)
- beta-decay: T-dependent
(Takahashi & Yokoi 1987, Goriely 1999)

$$U(T) = \frac{u_{\text{g.s.}}}{g_0(T)} + u_{\text{e.s.}} \left(1 - \frac{1}{g_0(T)} \right)$$

Beta-decay: $^{79}\text{Se} \rightarrow ^{79}\text{Br}$

- ground state: $u_{\text{g.s.}} = 1.3$ (30 %)
- excited states: $u_{\text{e.s.}} = 10$

g_0 : partition function
of the ground state



S Process in Massive Stars

Kaeppler, et al, 2011, RvMP, 83, 157, ...

Weak s process: (slow neutron capture process) during core He- and shell C-burning

He: $T > 0.25$ GK

(~ 21.6 keV)

C: $T \sim 1$ GK

N-source: $^{22}\text{Ne}(\alpha, n)$

Seed: iron

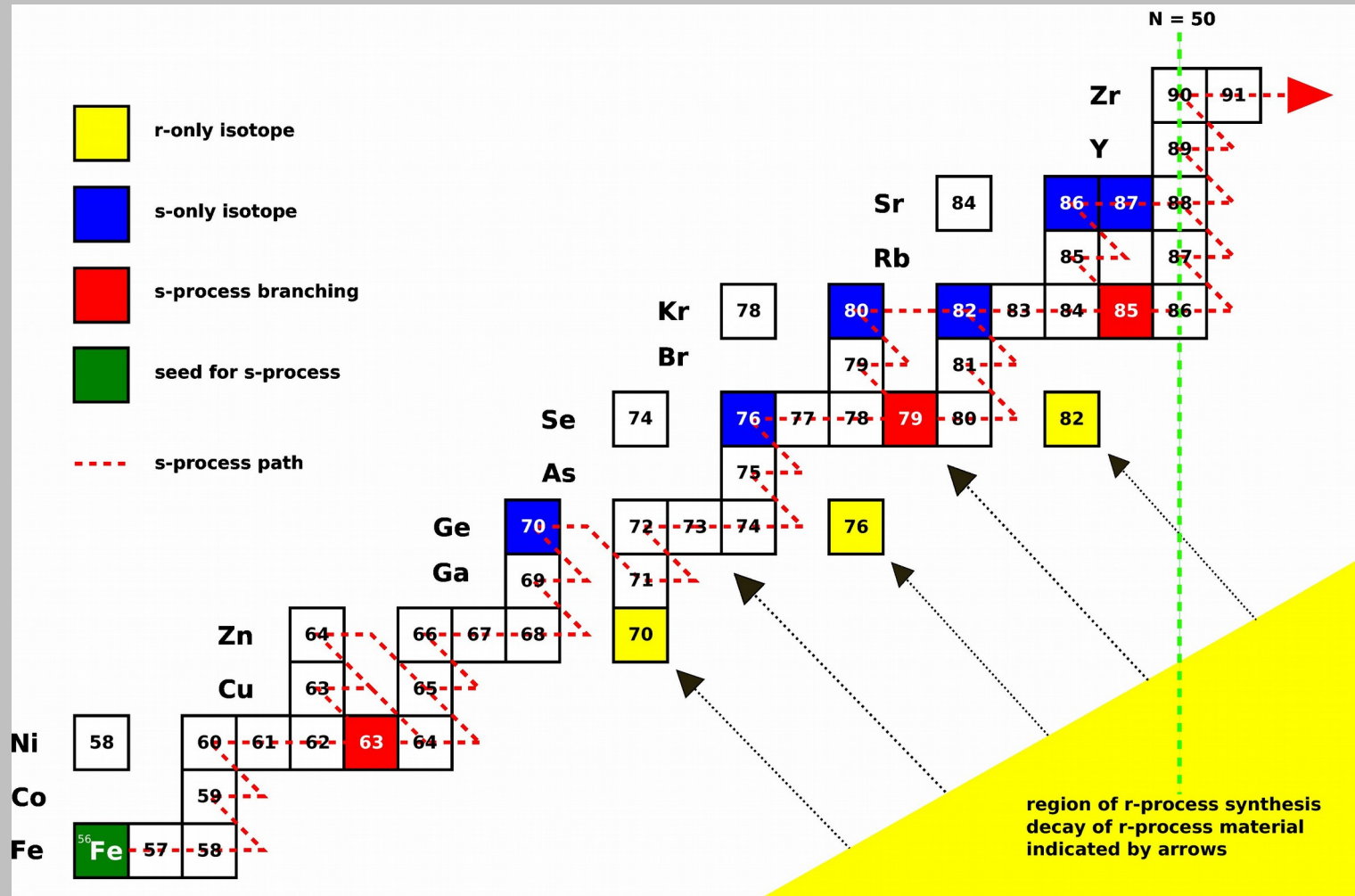
Poisons:

- He-b.: ^{22}Ne , ^{25}Mg ,

^{16}O , ^{12}C

- C-b.: ^{24}Mg , ^{25}Mg ,

^{16}O , ^{20}Ne

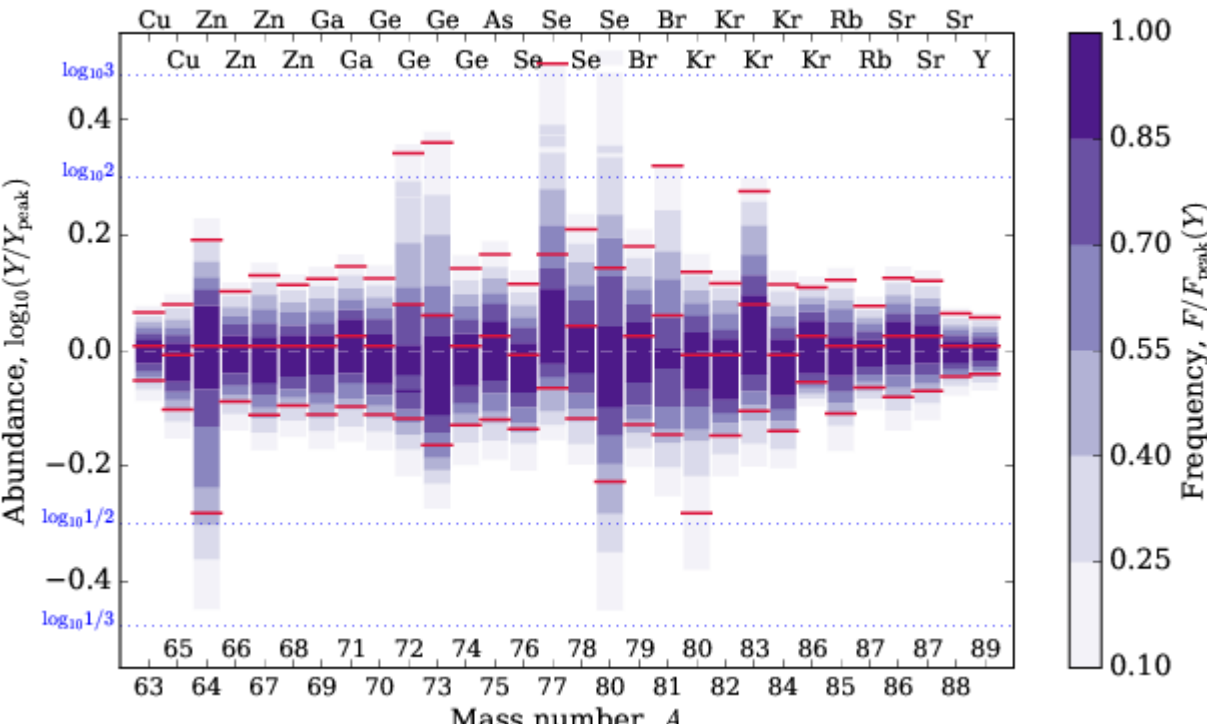
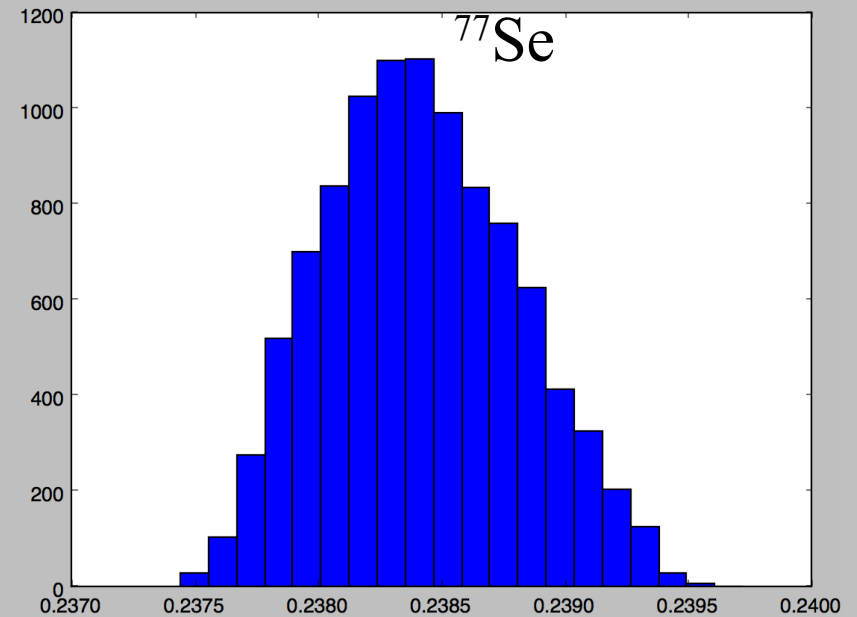
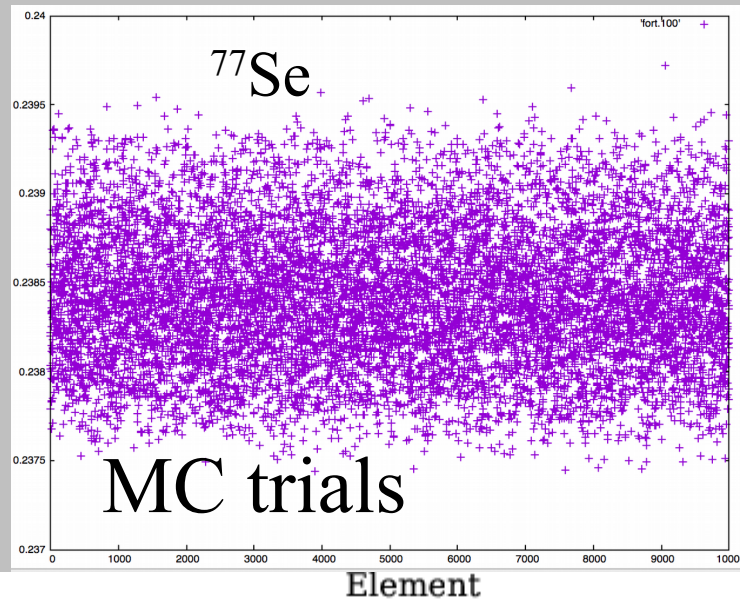


At solar Z : rotating models may produce up to 3x more s process
(See also Chieffi, Limongi, 2012ApJS..199...38L)

How much s process do massive rotating stars produce at low Z ?

Results for Weak s Process

N. Nishimura+ 2017: <http://adsabs.harvard.edu/abs/2017MNRAS.469.1752N>



Abundances

← MC: varying both
(n,g) & $\beta^{\pm}$

Key Reaction Lists for Weak s Process

N. Nishimura+ 2017: <http://adsabs.harvard.edu/abs/2017MNRAS.469.1752N>

Nuclide	$r_{\text{cor},0}$	$r_{\text{cor},1}$	$r_{\text{cor},2}$	Key Rate Level 1	Key Rate Level 2	Key Rate Level 3	X_0 (8, 30 keV)	Weak Rate (8, 30 keV)
^{64}Zn	<u>0.76</u>			$^{64}\text{Cu}(\beta^-)^{64}\text{Zn}$				1.30, 1.36
	-0.46	<u>-0.73</u>			$^{64}\text{Cu}(e^-, \nu_e)^{64}\text{Ni}$			e^- capture
^{67}Zn	<u>-0.67</u>			$^{67}\text{Zn}(n, \gamma)^{68}\text{Zn}$			1.00, 1.00	
^{72}Ge	<u>-0.85</u>			$^{72}\text{Ge}(n, \gamma)^{73}\text{Ge}$			1.00, 1.00	
^{73}Ge	<u>-0.84</u>			$^{73}\text{Ge}(n, \gamma)^{74}\text{Ge}$			0.88, 0.81	
^{74}Ge	-0.44	-0.54	<u>-0.67</u>			$^{74}\text{Ge}(n, \gamma)^{75}\text{Ge}$	1.00, 1.00	
^{75}As	-0.50	-0.59	<u>-0.70</u>			$^{75}\text{As}(n, \gamma)^{76}\text{As}$	1.00, 1.00	
^{77}Se	<u>-0.86</u>			$^{77}\text{Se}(n, \gamma)^{78}\text{Se}$			1.00, 1.00	
^{78}Se	<u>-0.71</u>			$^{78}\text{Se}(n, \gamma)^{79}\text{Se}$			1.00, 1.00	
	0.38	<u>0.68</u>			$^{68}\text{Zn}(n, \gamma)^{69}\text{Zn}$		1.00, 1.00	
^{80}Se	<u>-0.76</u>			$^{80}\text{Br}(\beta^-)^{80}\text{Kr}$				1.31, 4.70
	0.27	<u>0.73</u>			$^{80}\text{Br}(\beta^+)^{80}\text{Se}$			1.31, 4.70
	0.16	0.44	<u>0.88</u>			$^{80}\text{Br}(e^-, \nu_e)^{80}\text{Se}$		e^- capture
^{79}Br	-0.64	<u>-0.73</u>			$^{79}\text{Br}(n, \gamma)^{80}\text{Br}$		1.00, 1.00	
^{81}Br	<u>-0.80</u>			$^{81}\text{Kr}(n, \gamma)^{82}\text{Kr}$			1.00, 0.98	
^{83}Kr	<u>-0.76</u>			$^{83}\text{Kr}(n, \gamma)^{84}\text{Kr}$			0.81, 0.74	
^{84}Kr	-0.49	-0.65	<u>-0.76</u>			$^{84}\text{Kr}(n, \gamma)^{85}\text{Kr}$	1.00, 1.00	
^{86}Kr	<u>0.84</u>			$^{85}\text{Kr}(n, \gamma)^{86}\text{Kr}$			1.00, 1.00	
	-0.30	<u>-0.70</u>			$^{86}\text{Kr}(n, \gamma)^{87}\text{Kr}$		1.00, 1.00	
	-0.34	-0.62	<u>-0.90</u>			$^{85}\text{Kr}(\beta^-)^{85}\text{Rb}$		1.30, 1.30
^{87}Rb	-0.56	-0.65	<u>-0.95</u>			$^{87}\text{Rb}(n, \gamma)^{88}\text{Rb}$	1.00, 1.00	

Key Reaction Levels 1-3:

N. Nishimura+ 2017

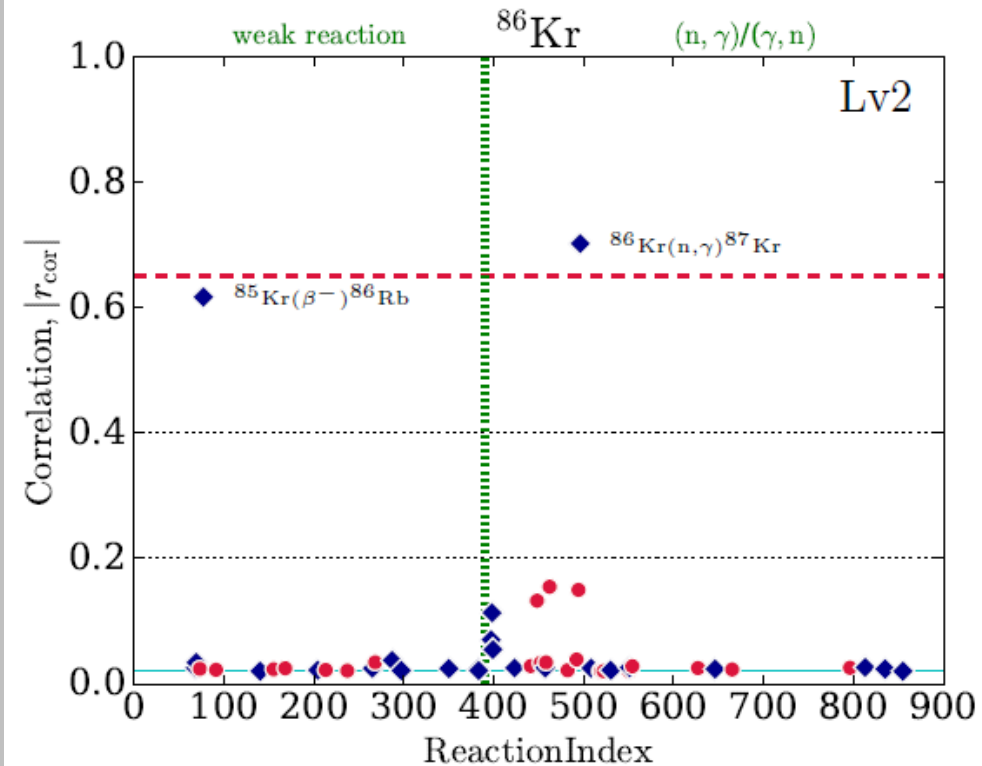
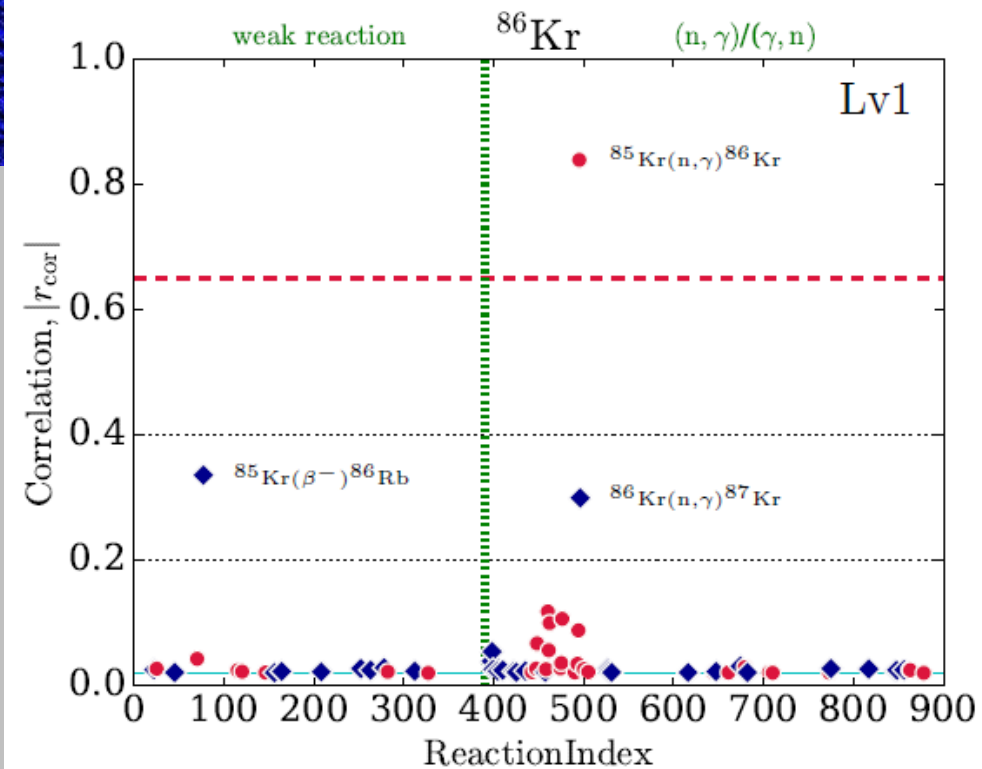
- Level 1 key rates dominate the uncertainty for a given isotope
- Once level 1 rates are fixed, *then* Level 2 rates become dominant

...

We adopt the Pearson product-moment correlation coefficient [Pearson \(1895\)](#) to quantify the correlation between rate variation and the final abundances (also used in [Rauscher et al. 2016](#)), defined by

$$r_{\text{cor}} = \frac{\sum_i^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_i^n (x_i - \bar{x})^2} \sqrt{\sum_i^n (y_i - \bar{y})^2}} \quad (4)$$

where x_i and y_i are variables with $\bar{x}$ and $\bar{y}$ being their arithmetic mean value, respectively. The summation is applied to all data for the MC runs $i = 1, 2, 3, \dots, n$. Here, x and y in Equation 4 correspond to variation factors f and final abundances Y .



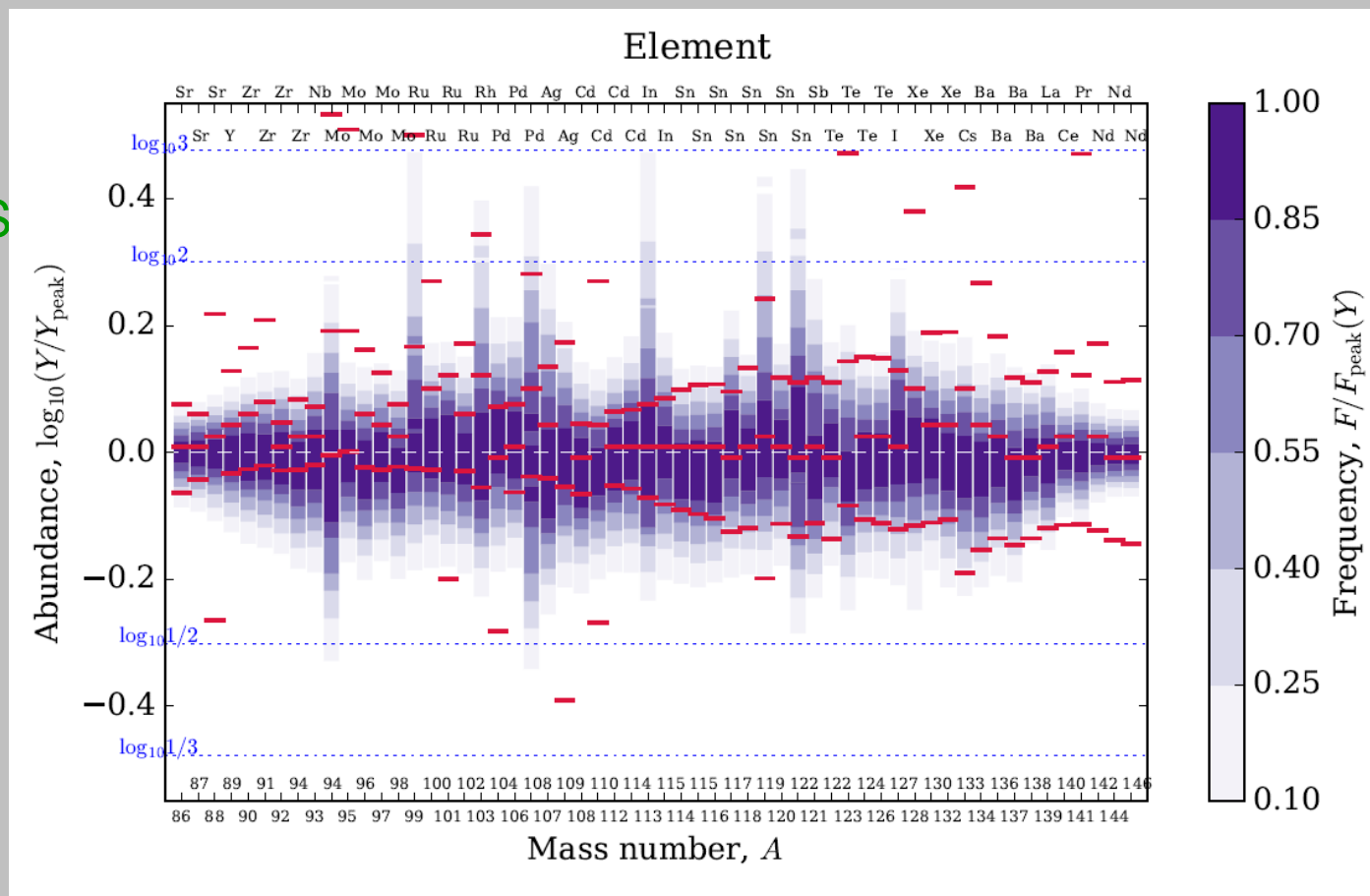
Key Reaction Lists

Priority lists established for:

- Enhanced (weak) s proc.
in low-Z fast rotating stars:
N. Nishimura+ 2017 MNRAS

- i process: Denissenkov+

2018JPhG...45e5203D



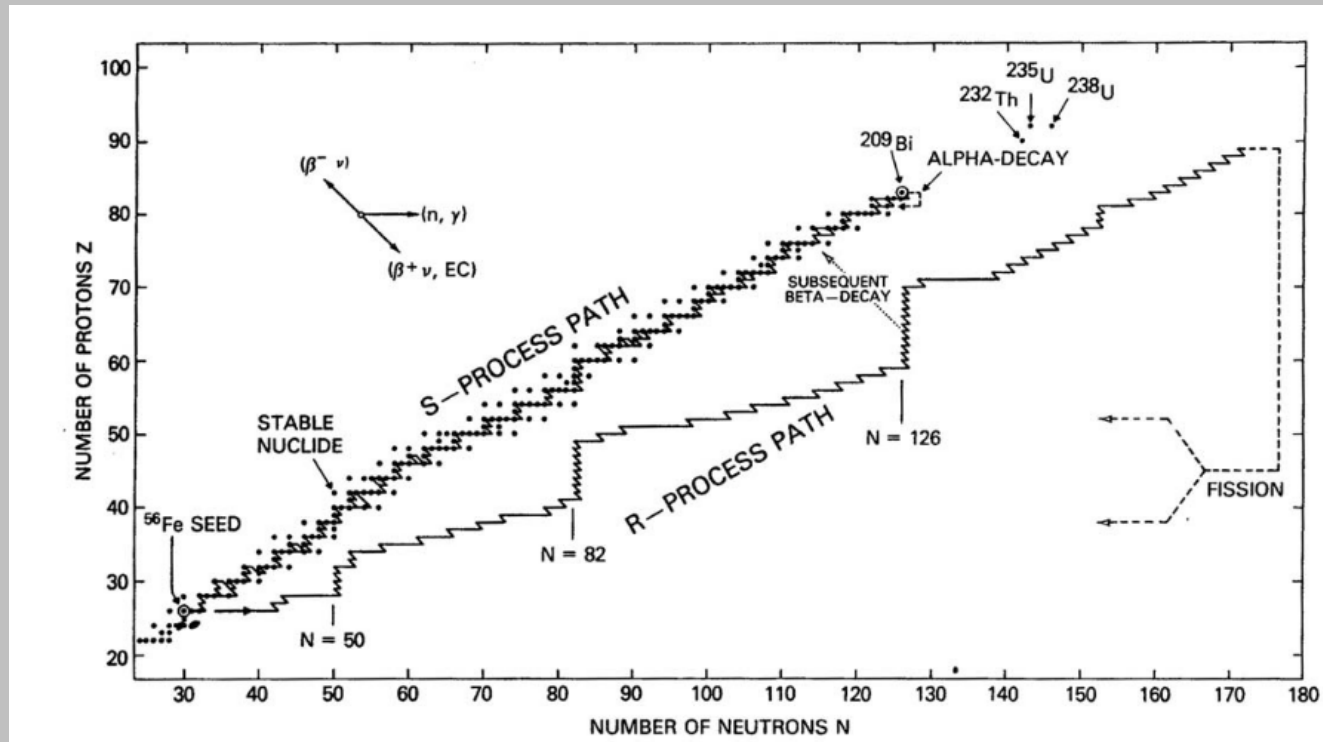
- Gamma (aka p) process in CCSNe: T. Rauscher+ 2016

<http://adsabs.harvard.edu/abs/2016MNRAS.463.4153R>

- Gamma (aka p) process in SNe Ia: Nishimura+ 2018, MNRAS

- Main s process (C13-pocket & TP) Cescutti + 2018, MNRAS

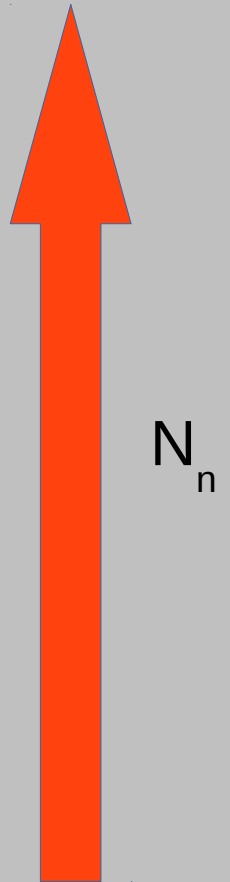
Paths of neutron capture processes



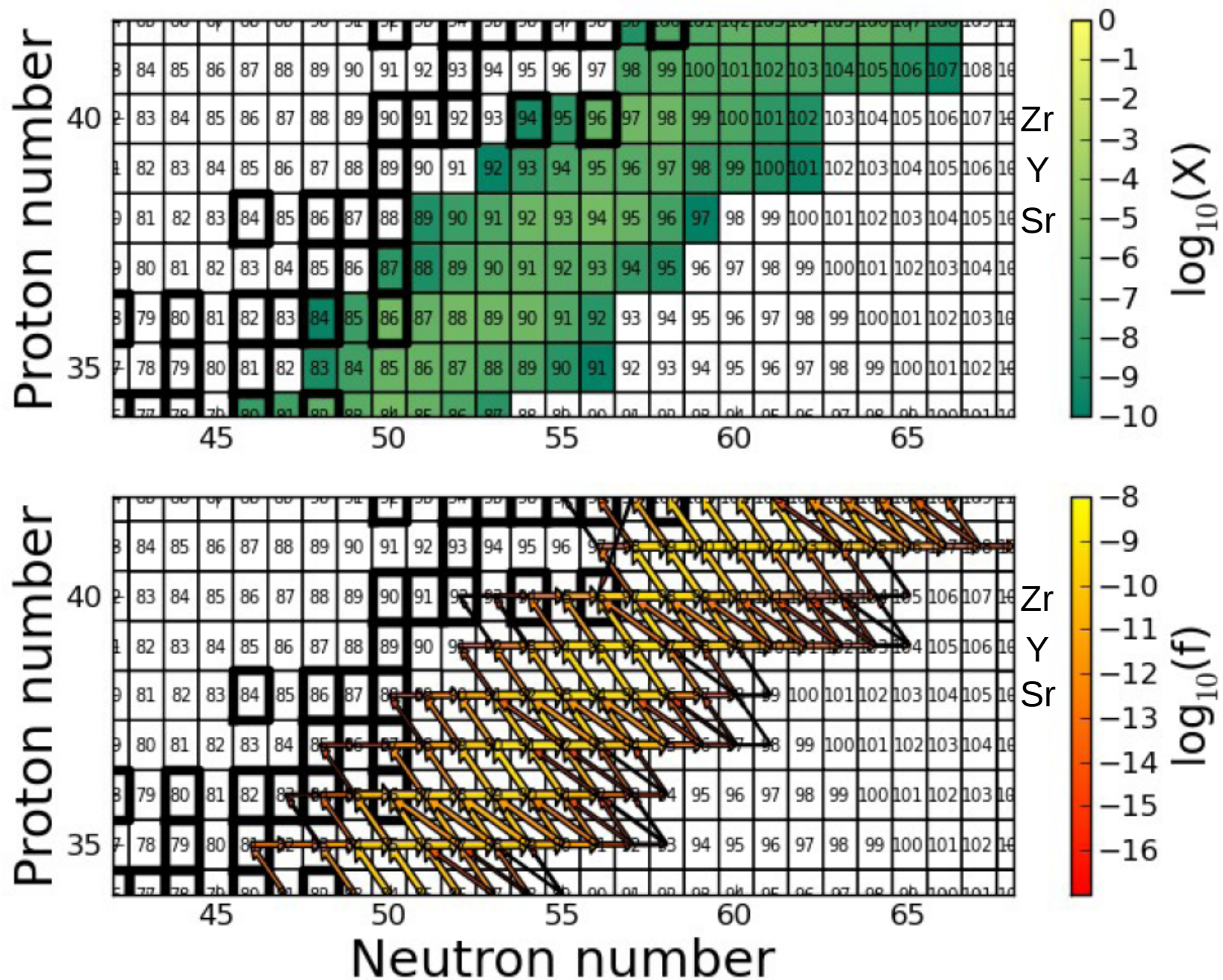
Cauldrons in the cosmos, 1988

List of neutron capture processes (with products observed/measured)

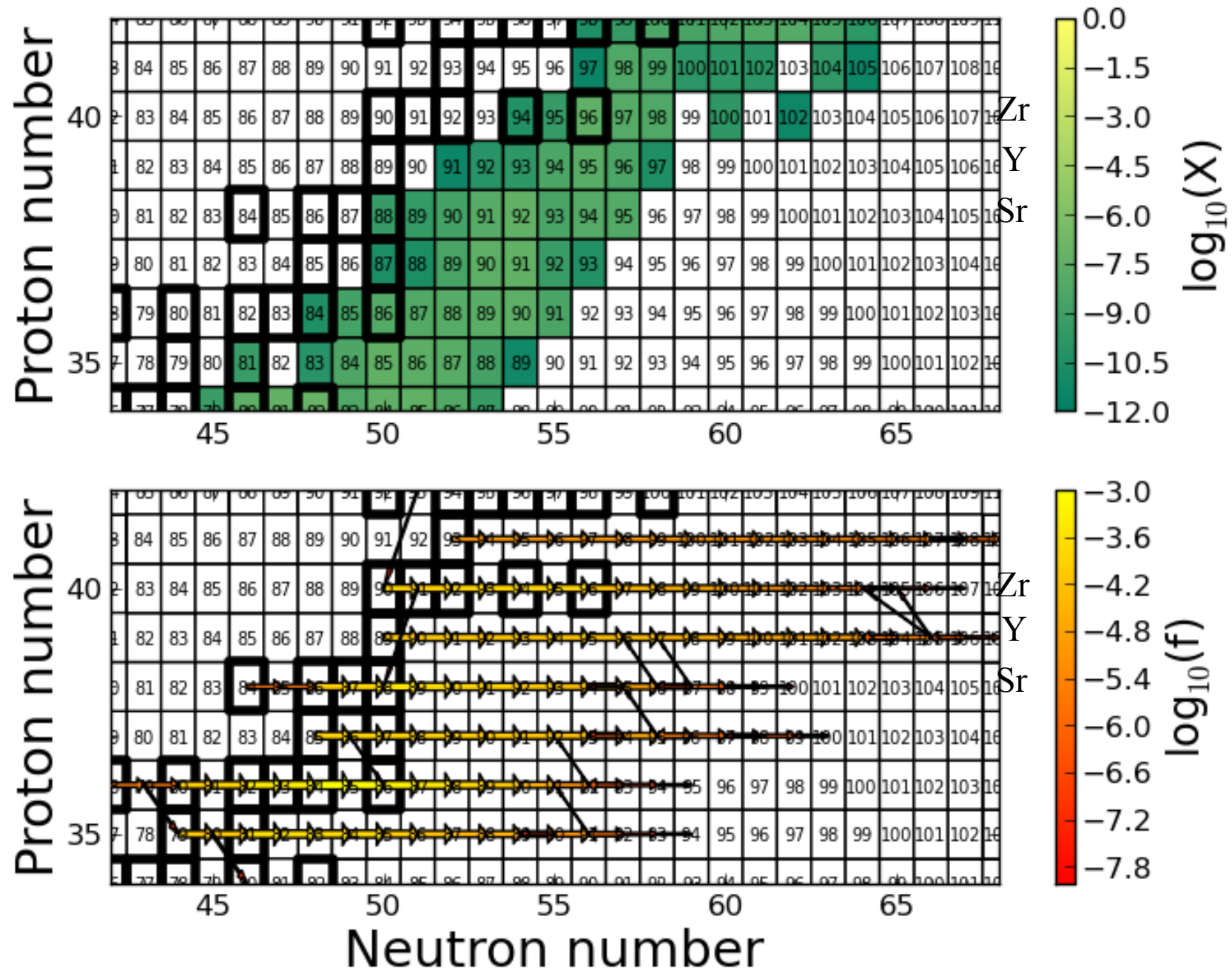
- The r process (neutrino-wind, NS mergers, jet-SNe, etc) - $N_n > 10^{20} \text{ n cm}^{-3}$;
- The n process (explosive He-burning in CCSN) - $10^{18} \text{ n cm}^{-3} < N_n < 10^{20} \text{ n cm}^{-3}$;
- The i process - $10^{13} \text{ n cm}^{-3} < N_n < 10^{16} \text{ n cm}^{-3}$;
- The s process (s process in AGB stars, s process in massive stars and fast rotators) – $N_n < 10^{13} \text{ n cm}^{-3}$.



Nucleosynthesis path of the i process: Se-Nb



Nucleosynthesis path of the n process: Se-Nb



THE ASTROPHYSICAL JOURNAL, 212:149–158, 1977 February 15
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1977

PRODUCTION OF ^{14}C AND NEUTRONS IN RED GIANTS

JOHN J. COWAN AND WILLIAM K. ROSE

Astronomy Program, University of Maryland, College Park

Received 1976 June 28

stellar/hydro

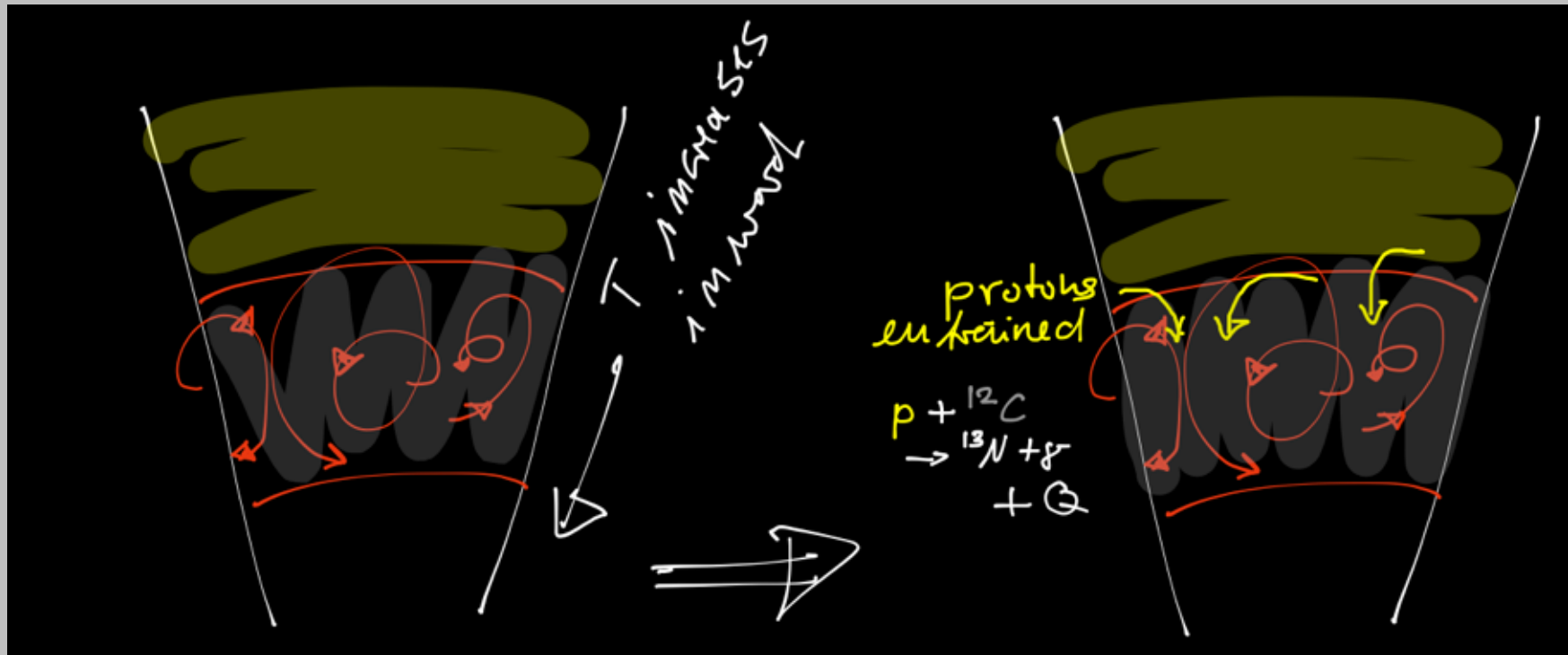
ABSTRACT

We have examined the effects of mixing various amounts of hydrogen-rich material into the intershell convective region of red giants undergoing helium shell flashes. We find that significant amounts of ^{14}C can be produced via the $^{14}\text{N}(n, p)^{14}\text{C}$ reaction. If substantial portions of this intershell region are mixed out into the envelopes of red giants, then ^{14}C may be detectable in evolved stars.

We find a neutron number density in the intershell region of $\sim 10^{15} - 10^{17} \text{ cm}^{-3}$ and a flux of $\sim 10^{23} - 10^{25} \text{ cm}^{-2} \text{ s}^{-1}$. This neutron flux is many orders of magnitude above the flux required for the classical s -process, and thus an intermediate neutron process (i -process) may operate in evolved red giants. The neutrons are principally produced by the $^{13}\text{C}(\alpha, n)^{16}\text{O}$ reaction.

In all cases studied we find substantial enhancements of ^{17}O . These mixing models offer a plausible explanation of the observations of enhanced ^{17}O in the carbon star IRC 10216. For certain physical conditions we find significant enhancements of ^{15}N in the intershell region.

nuclear/stellar



N13 and/or C13 are mixed for hours in regions with typical He-burning temperatures ($T_9 \sim 0.25\text{-}0.3$ GK), together with Fe-seed rich material.

Main source of neutrons: $\text{C13}(\alpha, n)\text{O16}$

Possible sites: low-Z LMS & MS; RAWD
Challenge: requires multi-D hydro simulations

i process in RAWD

Denissenkov + 2018: ArXiV 1809.03666

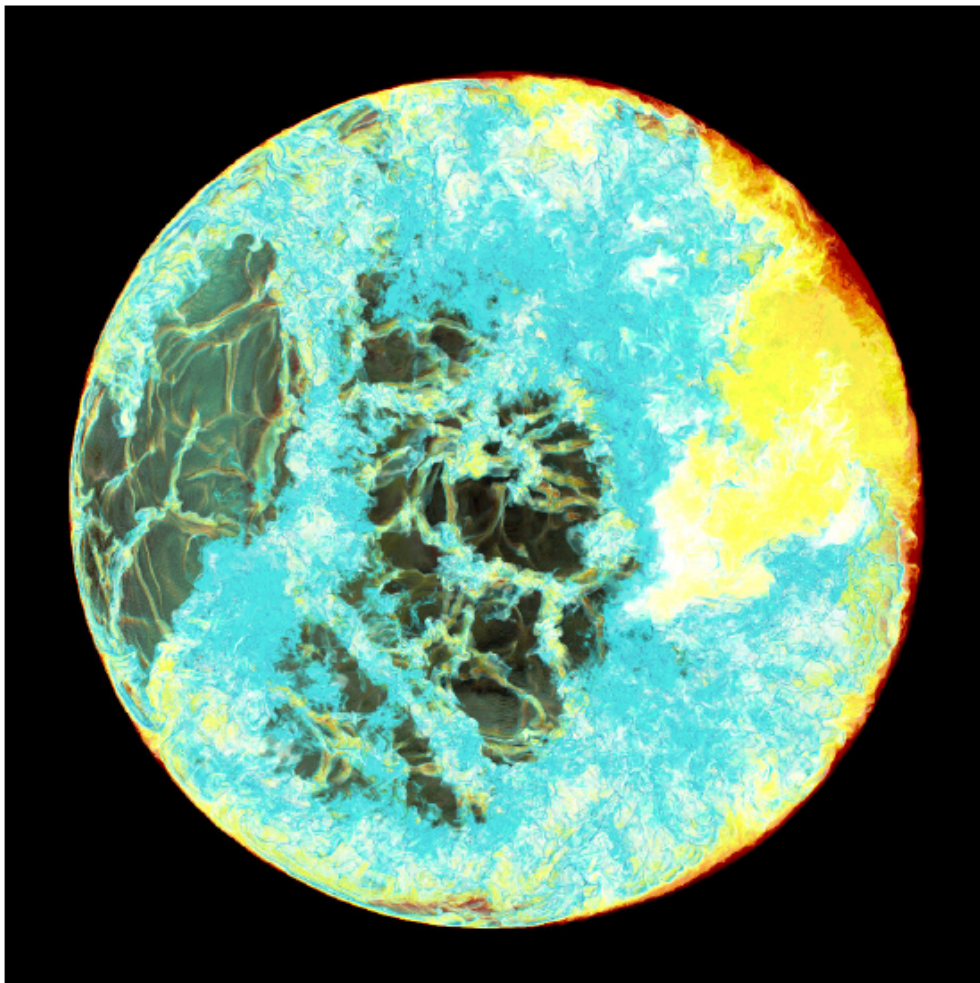


Figure 3. Fractional volume of the fluid ingested into the convection zone in run E10 at $t = 359.8$ min. The colour scale is logarithmic and very low concentrations are transparent. The front half of the sphere is not shown and the camera is looking into the back half of the sphere in this rendering.

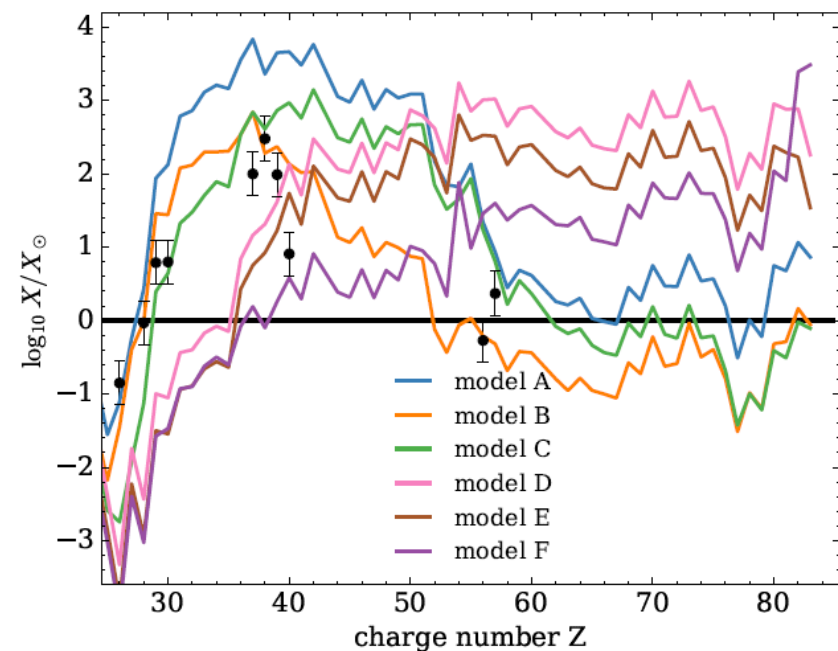


Figure 11. The elemental *i*-process yields (solar-scaled mass fractions) from our RAWD models. For comparison, the abundances of the first peak *n*-capture elements measured in Sakurai's object by [Asplund et al. \(1999\)](#) are shown as filled black circles with errorbars. They were interpreted by [Herwig et al. \(2011\)](#) as results of the *i*-process nucleosynthesis in the convective He shell during its very late thermal pulse in a model of Sakurai's object with a half-solar metallicity.



Stellar Explosions in Binary Systems – Type Ia Supernovae, Classical Novae and X-Ray Bursts

Jordi José

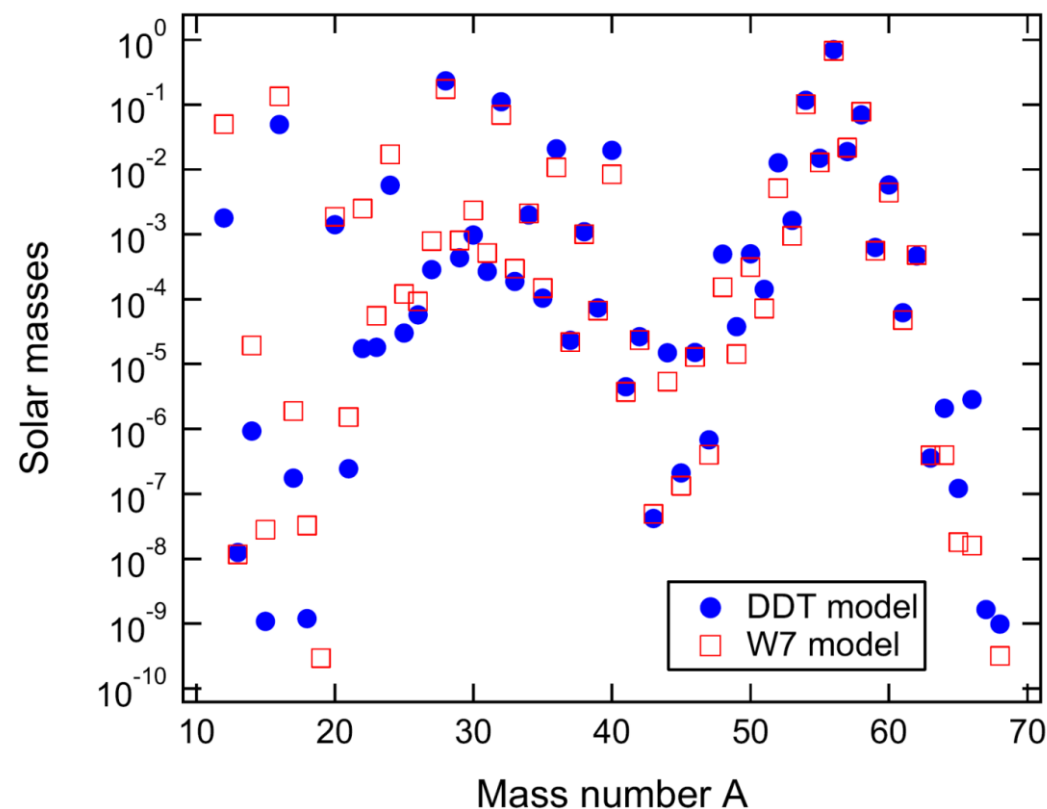
Dept. Physics, Technical Univ. of Catalonia (UPC)
& Space Research Institut of Catalonia (IEEC)
Barcelona

Type Ia Supernovae (problems, challenges & mysteries)

- * **homogeneity:** only $\sim 70\%$ of all SN Ia have similar spectra, light curves and peak absolute magnitudes (Li et al. 2011): **diversity of SNIa progenitors?**
- * **Scenario:** not understood ! **single degenerate** (WD + MS companion) vs **double degenerate** (WD + WD)
- * **Propagation of the burning front:** subsonic vs supersonic (what causes the predicted **deflagration/detonation transition?**)



* **Nucleosynthesis:** five burning regimes: “normal” and “ α -rich” freeze-out from nuclear statistical equilibrium (NSE) in the inner regions, and incomplete Si-, O-, and C/Ne-burning in the outermost layers (Thielemann et al. 1986; Woosley 1986)
systematic overproduction of some Fe-peak isotopes (^{50}Ti , ^{54}Cr)



Parikh, JJ, Seitenzahl & Röpke,
A&A (2013)

443 isotopes (H – Kr); 5267 links

W7 DDT W7+DDT

*Nuclear Uncertainties

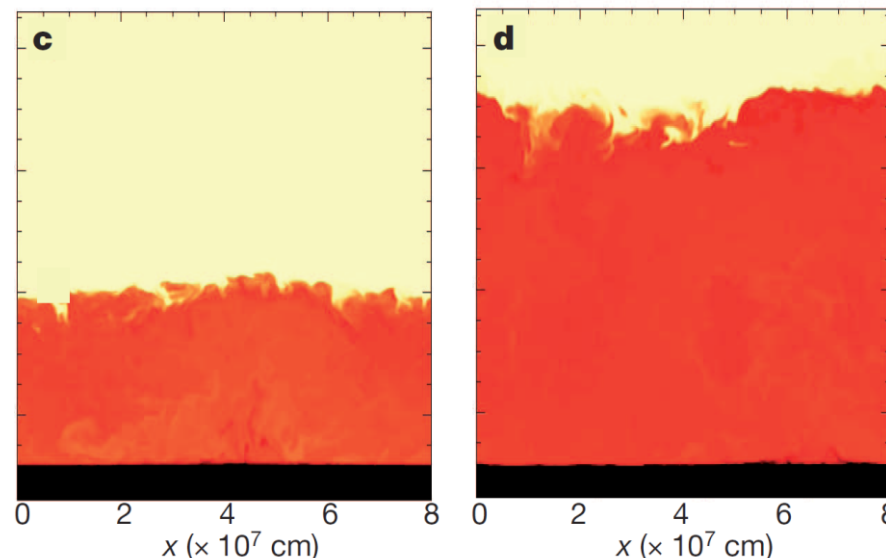
Parikh, JJ, Seitenzahl & Röpke,
A&A (2013)

Reaction	Importance		
	Case A	Case B	Case C
$^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$	X	X	X
$^{12}\text{C}(^{12}\text{C}, \alpha)^{20}\text{Ne}$	X	X	X
$^{12}\text{C}(^{12}\text{C}, p)^{23}\text{Na}$	X	X	X
$^{16}\text{O}(n, \gamma)^{17}\text{O}$	X		
$^{16}\text{O}(\alpha, \gamma)^{20}\text{Ne}$	X		
$^{20}\text{Ne}(n, \gamma)^{21}\text{Ne}$			X
$^{20}\text{Ne}(\alpha, p)^{23}\text{Na}$	X	X	X
$^{20}\text{Ne}(\alpha, \gamma)^{24}\text{Mg}$	X	X	X
$^{22}\text{Ne}(p, \gamma)^{23}\text{Na}$	X		X
$^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$			X
$^{23}\text{Na}(n, \gamma)^{24}\text{Na}$			X
$^{23}\text{Na}(\alpha, p)^{26}\text{Mg}$		X	
$^{24}\text{Na}(p, n)^{24}\text{Mg}$			X
$^{24}\text{Mg}(\alpha, \gamma)^{28}\text{Si}$			X
$^{25}\text{Mg}(n, \gamma)^{26}\text{Mg}$		X	X
$^{25}\text{Mg}(p, \gamma)^{26}\text{Al}$			X
$^{26}\text{Mg}(p, n)^{26}\text{Al}$			X
$^{27}\text{Al}(p, \gamma)^{28}\text{Si}$			X
$^{27}\text{Al}(\alpha, p)^{30}\text{Si}$	X		X
$^{28}\text{Si}(\alpha, p)^{31}\text{P}$			X
$^{30}\text{Si}(p, \gamma)^{31}\text{P}$	X		
$^{30}\text{Si}(\alpha, \gamma)^{34}\text{S}$	X		X
$^{30}\text{Si}(\alpha, n)^{33}\text{S}$			X
$^{32}\text{P}(p, n)^{32}\text{S}$			X
$^{34}\text{S}(\alpha, p)^{37}\text{Cl}$			X
$^{36}\text{S}(p, n)^{36}\text{Cl}$			X
$^{42}\text{Ca}(\alpha, \gamma)^{46}\text{Ti}$			X
$^{45}\text{Sc}(p, \gamma)^{46}\text{Ti}$		X	
$^{45}\text{Sc}(p, n)^{45}\text{Ti}$			X

Table 2. Summary of important reactions from Table 1. Variation of each of the listed rates by a factor of 10 (up or down) modified yields of at least *three* species by at least a factor of two in the W7 model (“Case A”) or the DDT model (“Case B”). If variation of the rate affected the yield of at least one species in *both* models, it is designated as “Case C”.

Classical Novae (problems, challenges & mysteries)

- * **Mixing** mechanism at work at the core-envelope interface during nova outbursts (**3D turbulent convection?**)
- * The amount of **mass ejected** predicted by 1-D models is smaller than values **inferred** observationally
- * Interaction between the nova ejecta, the disk and the stellar companion poorly studied:
origin of γ -ray emission at $E > 100$ MeV?



Casanova, JJ, García-Berro, Shore & Calder (2011)

* Nuclear Uncertainties

THE ASTROPHYSICAL JOURNAL SUPPLEMENT SERIES, 142:105–137, 2002 September

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THE EFFECTS OF THERMONUCLEAR REACTION-RATE VARIATIONS ON NOVA NUCLEOSYNTHESIS: A SENSITIVITY STUDY

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Received 2002 January 19; accepted 2002 April 25

≈ 7350 nuclear reaction network calculations

Main nuclear uncertainties: [$^{18}\text{F}(\text{p},\alpha)^{15}\text{O}$, $^{25}\text{Al}(\text{p},\gamma)^{26}\text{Si}$, $^{30}\text{P}(\text{p},\gamma)^{31}\text{S}$]

Type I X-Ray Bursts (problems, challenges & mysteries)

- * **Nucleosynthesis endpoint?**
- * Do they **contribute to the Galactic abundances** (i.e., do they lead to mass ejection?)
- * **Multidimensional effects** scarcely investigated

* Nuclear Uncertainties

THE ASTROPHYSICAL JOURNAL SUPPLEMENT SERIES, 178:110–136, 2008 September

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THE EFFECTS OF VARIATIONS IN NUCLEAR PROCESSES ON TYPE I X-RAY BURST NUCLEOSYNTHESIS

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~ **50,000** post-processing calculations

606 isotopes (^1H to ^{113}Xe) and **3551** nuclear processes

* Nuclear Uncertainties

TABLE 19

SUMMARY OF THE MOST INFLUENTIAL NUCLEAR PROCESSES, AS COLLECTED FROM TABLES 1–10

Reaction	Models Affected
$^{12}\text{C}(\alpha, \gamma)^{16}\text{O}^{\text{a}}$	F08, K04-B2, K04-B4, K04-B5
$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}^{\text{a}}$	K04-B1 ^b
$^{25}\text{Si}(\alpha, p)^{28}\text{P}$	K04-B5
$^{26g}\text{Al}(\alpha, p)^{29}\text{Si}$	F08
$^{29}\text{S}(\alpha, p)^{32}\text{Cl}$	K04-B5
$^{30}\text{P}(\alpha, p)^{33}\text{S}$	K04-B4
$^{30}\text{S}(\alpha, p)^{33}\text{Cl}$	K04-B4, ^b K04-B5 ^b
$^{31}\text{Cl}(p, \gamma)^{32}\text{Ar}$	K04-B1
$^{32}\text{S}(\alpha, \gamma)^{36}\text{Ar}$	K04-B2
$^{56}\text{Ni}(\alpha, p)^{59}\text{Cu}$	S01, ^b K04-B5
$^{57}\text{Cu}(p, \gamma)^{58}\text{Zn}$	F08
$^{59}\text{Cu}(p, \gamma)^{60}\text{Zn}$	S01, ^b K04-B5
$^{61}\text{Ga}(p, \gamma)^{62}\text{Ge}$	F08, K04-B1, K04-B2, K04-B5, K04-B6
$^{65}\text{As}(p, \gamma)^{66}\text{Se}$	K04, ^b K04-B1, K04-B2, ^b K04-B3, ^b K04-B4, K04-B5, K04-B6
$^{69}\text{Br}(p, \gamma)^{70}\text{Kr}$	K04-B7
$^{75}\text{Rb}(p, \gamma)^{76}\text{Sr}$	K04-B2
$^{82}\text{Zr}(p, \gamma)^{83}\text{Nb}$	K04-B6
$^{84}\text{Zr}(p, \gamma)^{85}\text{Nb}$	K04-B2
$^{84}\text{Nb}(p, \gamma)^{85}\text{Mo}$	K04-B6
$^{85}\text{Mo}(p, \gamma)^{86}\text{Tc}$	F08
$^{86}\text{Mo}(p, \gamma)^{87}\text{Tc}$	F08, K04-B6
$^{87}\text{Mo}(p, \gamma)^{88}\text{Tc}$	K04-B6
$^{92}\text{Ru}(p, \gamma)^{93}\text{Rh}$	K04-B2, K04-B6
$^{93}\text{Rh}(p, \gamma)^{94}\text{Pd}$	K04-B2
$^{96}\text{Ag}(p, \gamma)^{97}\text{Cd}$	K04, K04-B2, K04-B3, K04-B7
$^{102}\text{In}(p, \gamma)^{103}\text{Sn}$	K04, K04-B3
$^{103}\text{In}(p, \gamma)^{104}\text{Sn}$	K04-B3, K04-B7
$^{103}\text{Sn}(\alpha, p)^{106}\text{Sb}$	S01 ^b

TABLE 20

NUCLEAR PROCESSES AFFECTING THE TOTAL ENERGY OUTPUT BY MORE THAN 5% AND AT LEAST ONE ISOTOPE

Reaction	Models Affected
$^{15}\text{O}(\alpha, \gamma)^{19}\text{Ne}^{\text{a}}$	K04, K04-B1, K04-B6
$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}^{\text{a}}$	K04-B1, K04-B6
$^{22}\text{Mg}(\alpha, p)^{25}\text{Al}$	F08
$^{23}\text{Al}(p, \gamma)^{24}\text{Si}$	K04-B1
$^{24}\text{Mg}(\alpha, p)^{27}\text{Al}^{\text{a}}$	K04-B2
$^{26g}\text{Al}(p, \gamma)^{27}\text{Si}^{\text{a}}$	F08
$^{28}\text{Si}(\alpha, p)^{31}\text{P}^{\text{a}}$	K04-B4
$^{30}\text{S}(\alpha, p)^{33}\text{Cl}$	K04-B4, K04-B5
$^{31}\text{Cl}(p, \gamma)^{32}\text{Ar}$	K04-B3
$^{32}\text{S}(\alpha, p)^{35}\text{Cl}$	K04-B2
$^{35}\text{Cl}(p, \gamma)^{36}\text{Ar}^{\text{a}}$	K04-B2
$^{56}\text{Ni}(\alpha, p)^{59}\text{Cu}$	S01
$^{59}\text{Cu}(p, \gamma)^{60}\text{Zn}$	S01
$^{65}\text{As}(p, \gamma)^{66}\text{Se}$	K04, K04-B2, K04-B3
$^{69}\text{Br}(p, \gamma)^{70}\text{Kr}$	S01
$^{71}\text{Br}(p, \gamma)^{72}\text{Kr}$	K04-B7
$^{103}\text{Sn}(\alpha, p)^{106}\text{Sb}$	S01

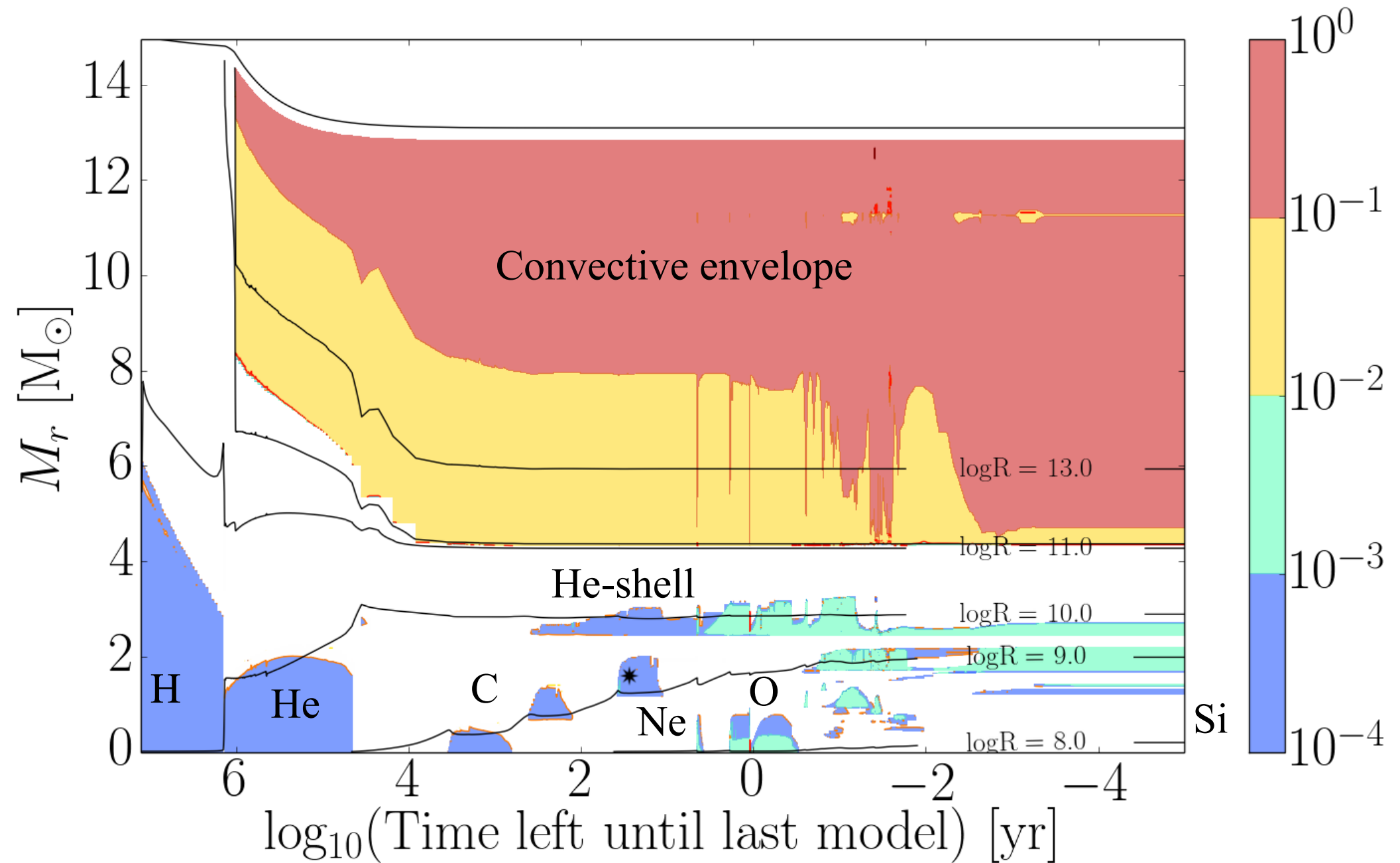
606 isotopes (^1H to ^{113}Xe) and 3551 nuclear processes

Stellar Models:

Stellar structure equations + physical ingredients:

- Nuclear reactions
 - Mass loss
 - Rotation
 - Convection
 - Magnetic fields
 - Binary interactions
 - Equation of state, opacities & neutrino losses
- including metallicity dependence

Evolution of Massive Stars



Convection takes place during most burning stages

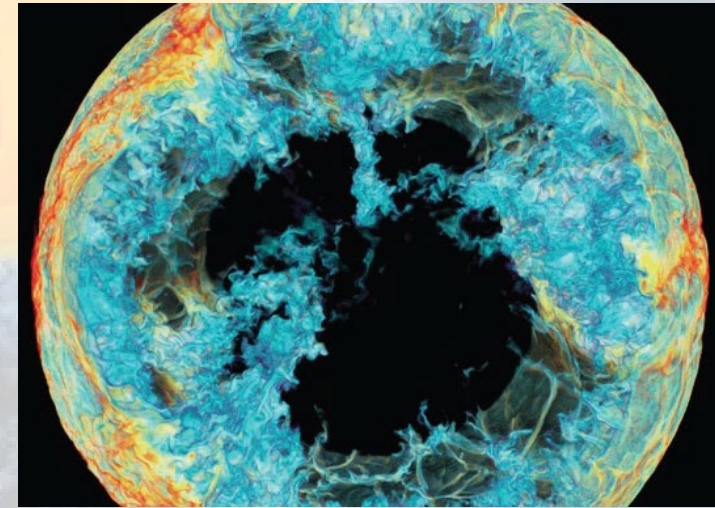
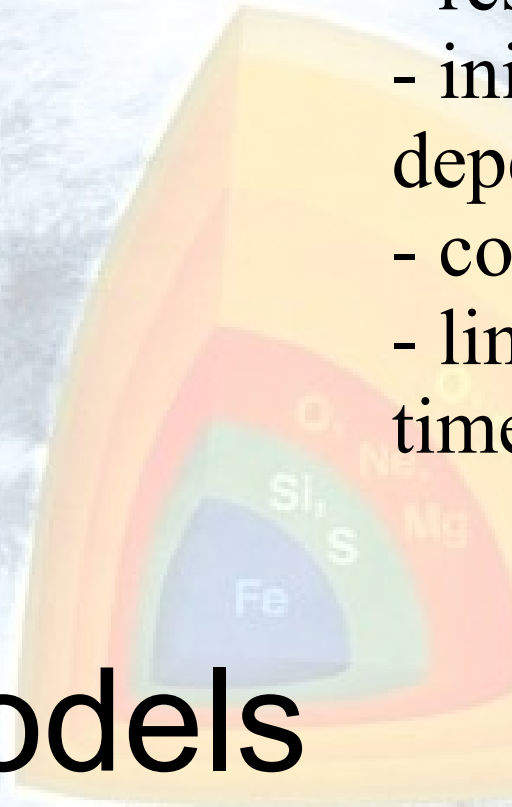
Advantages:

- model fluid instabilities (e.g. Rayleigh-Taylor)
- modeling 3D processes
- model diffusive and advective processes

Disadvantages:

- resolution dependent?
- initial condition dependent?
- computational cost
- limited to dynamical timescales ($t_{\text{conv}} \sim 1\text{s} - \text{days}$)

3D stellar models



Herwig, Woodward et al 2013

What's missing?

- full star or lifetime simulations
- Large scale (LES) and small scale (DNS) cannot be followed simultaneously

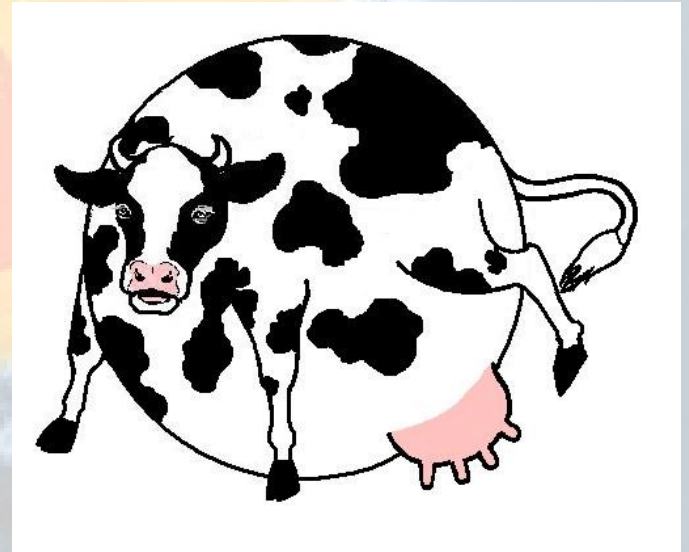
Advantages:

- model entire evolution ($\Delta t \sim 10^3$ yrs)
- compare to observations
- progenitor models
- large grids (M, Z)

Disadvantages:

- parametrized physics (e.g. convection)
- missing multi-D processes
- incapable of modelling turbulence

1D stellar models



What's missing?

- self-consistent physical descriptions of mass loss, **convection**, **rotation**, magnetic fields, opacity, binarity

Convection: Current Implementation in 1D Codes

Multi-D processes:

Major contributor to turbulent mixing

Turbulent entrainment at convective boundaries

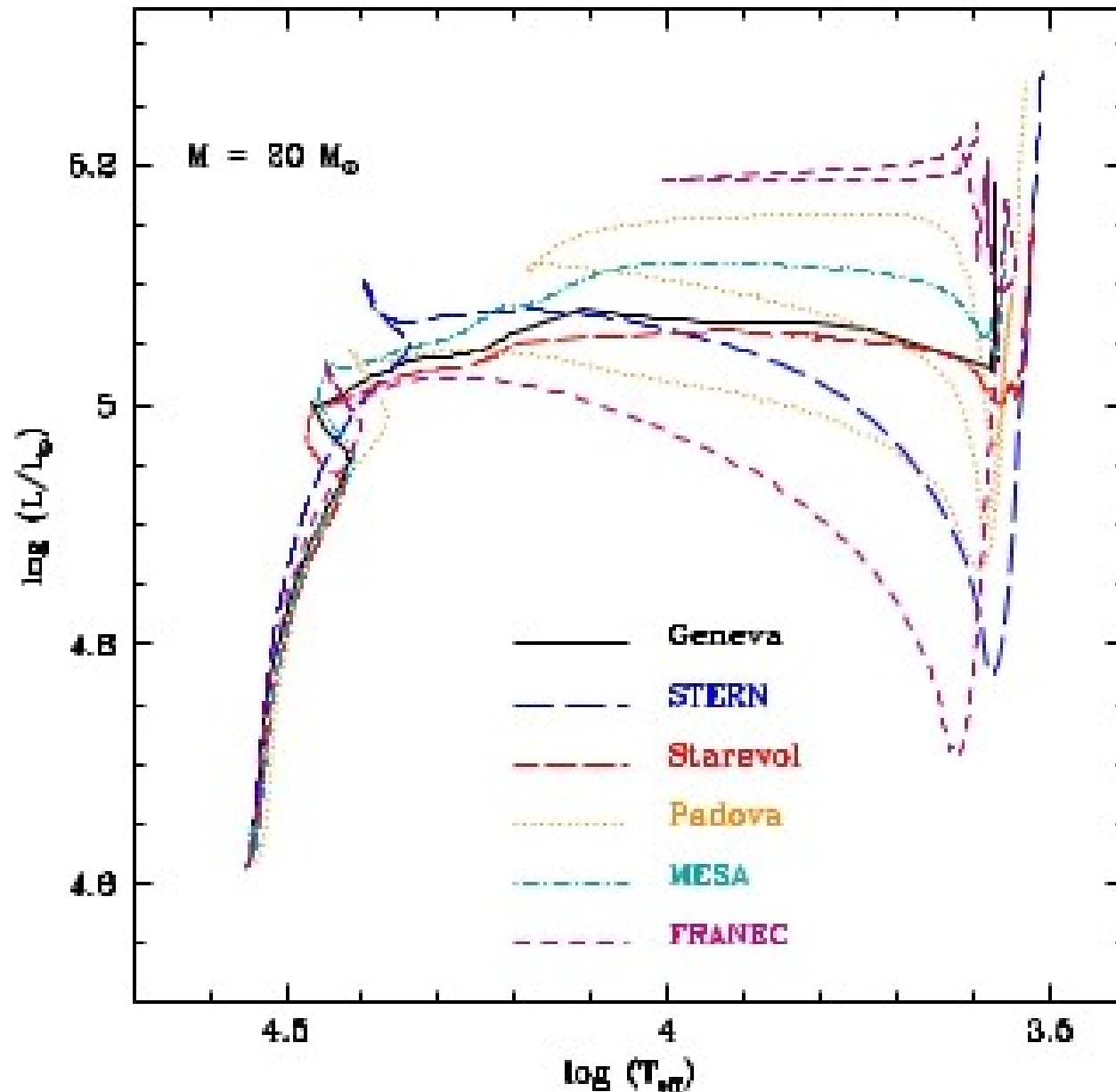
Internal gravity waves

1D prescriptions:

- Energy transport in convective zone: **mixing length theory (MLT)** *Bohm-Vitense (1957,58)*, or updates, e.g. FST: *Canuto & Mazitelli (1991)*
- Boundary location: Schwarzschild criterion OR Ledoux (+semi-convection)
- Convective boundary mixing (CBM, also composition dependent)

1D Model Uncertainties

Martins and Palacios (2013)



Different prescriptions for convective mixing and free parameters **strongly affect** post-MS evolution.

See also Jones et al 2015, *MNRAS*, 447, 3115

1D Model Uncertainties: Complex Convective History

Detailed convective shell history affects fate of models: strong/weak/failed explosions!!!

Sukhbold & Woosley, 2014ApJ...783...10S

Sukhbold, Ertl et al, 2016ApJ...821...38S,

Ugliano et al 2012, Ertl et al 2015

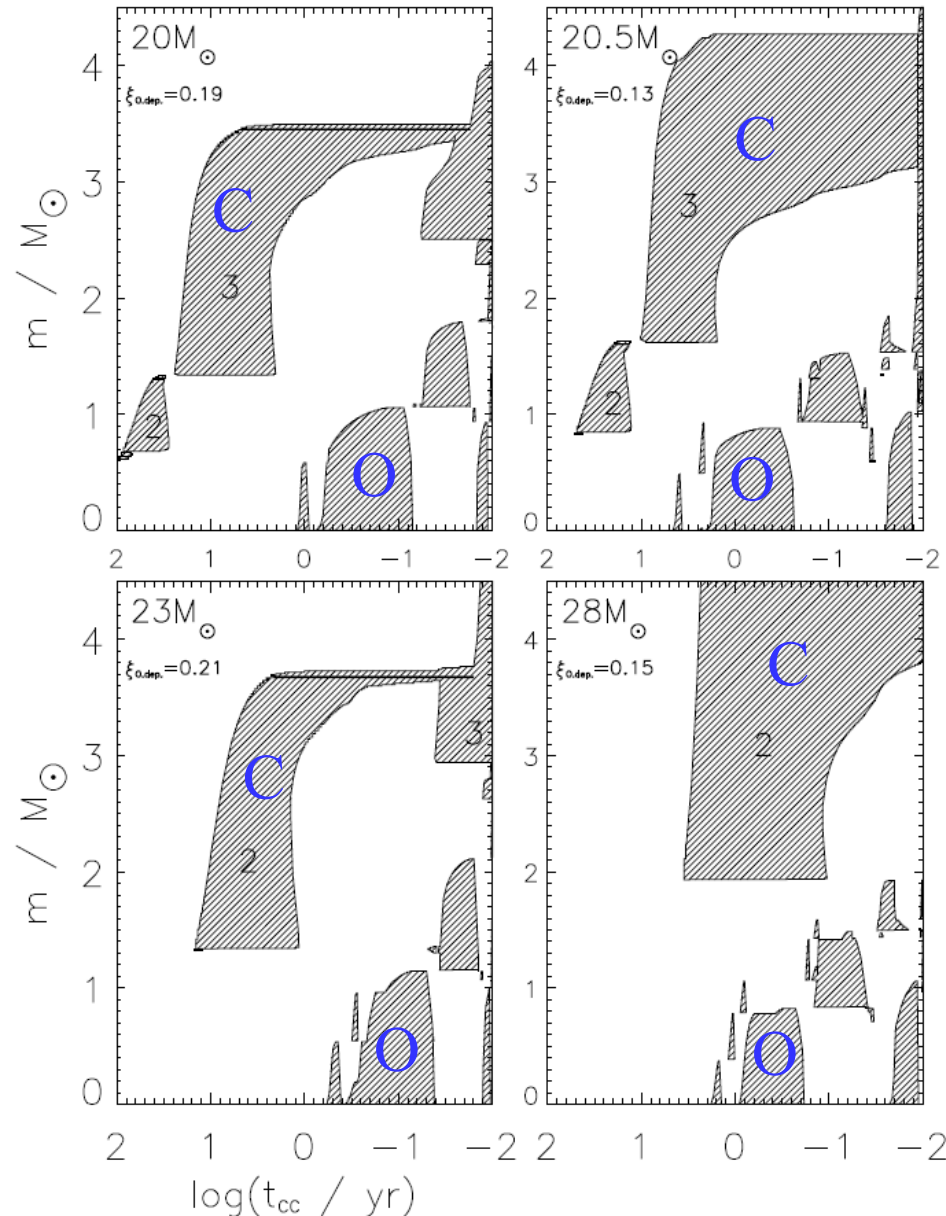


FIG. 13.— Convective history of four models showing the major

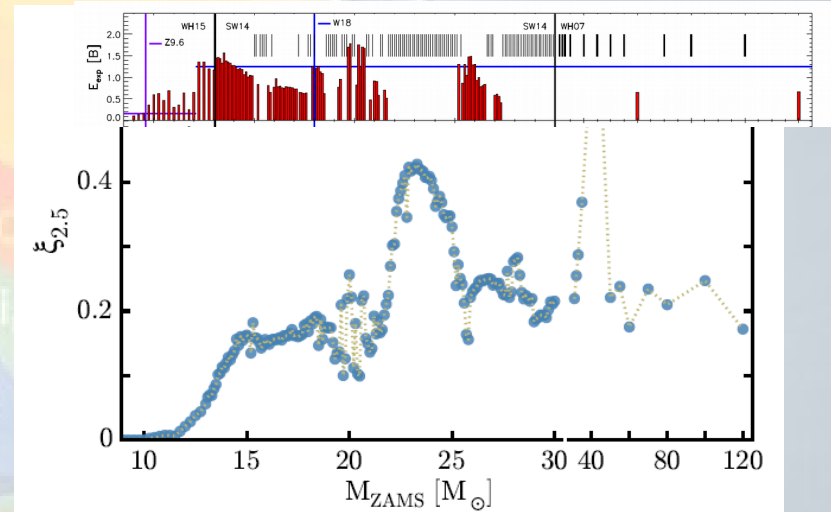


FIG. 1.— The compactness parameter, $\xi_{2.5}$, (eq. (1); O'Connor & Ott 2011) characterizing the inner $2.5 M_{\odot}$ of the presupernova star is shown as a function of zero-age main sequence (ZAMS) mass for all 200 models between 9.0 and $120 M_{\odot}$. The compactness

Non-monotonic behaviour!

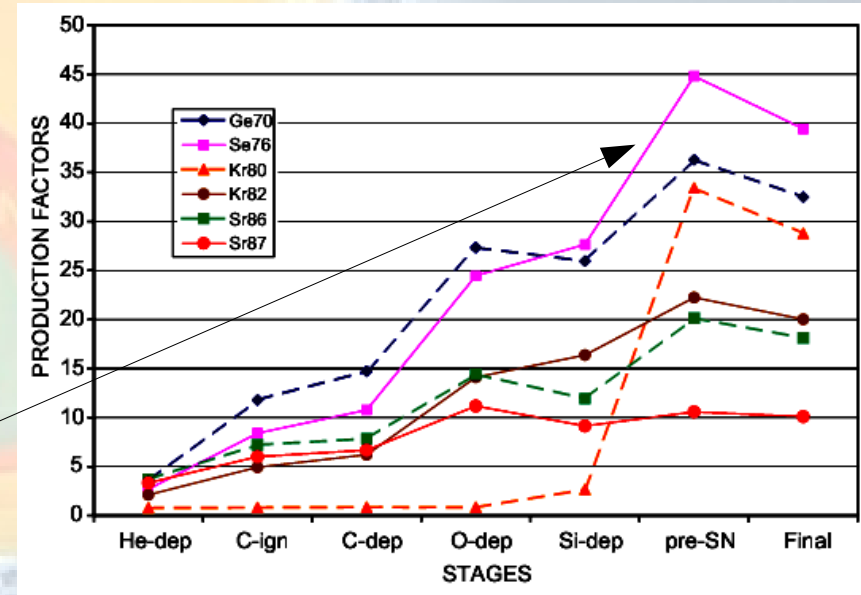
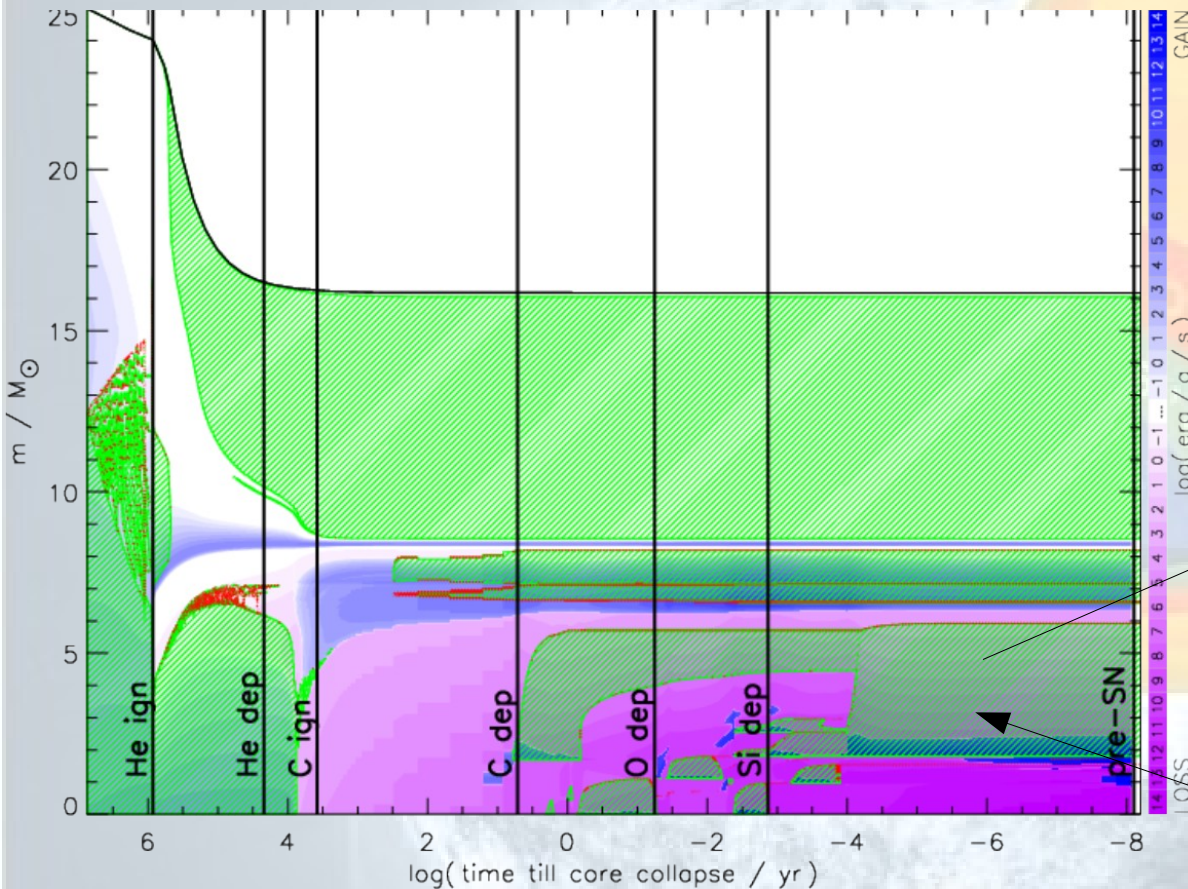
We are particularly interested in how the “explodability” of the presupernova models and their observable properties correlate with their “compactness” (Fig. 1; O'Connor & Ott 2011)

$$\xi_M = \frac{M/M_{\odot}}{R(M)/1000 \text{ km}} \Big|_{t_{\text{bounce}}}, \quad (1)$$

and other measures of presupernova core structure (§ 3.1.3; Ertl et al. (2015)). Using a standard central engine in presupernova models of variable compactness, a significant correlation in outcome is found (§ 4). As pre-

1D Model Uncertainties: Possible Shell Mergers

Tur, Heger et al 07/09/10



C/Ne/O shell mergers

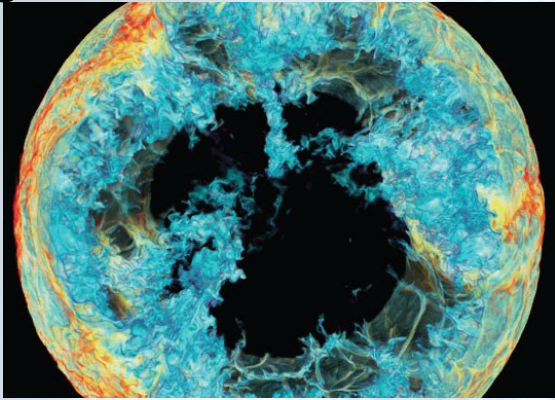
Rauscher, Heger and Woosley 2002: "Interesting and unusual nucleosynthetic results are found for one particular 20M model as a result of its special stellar structure."

Shell mergers also affect compactness

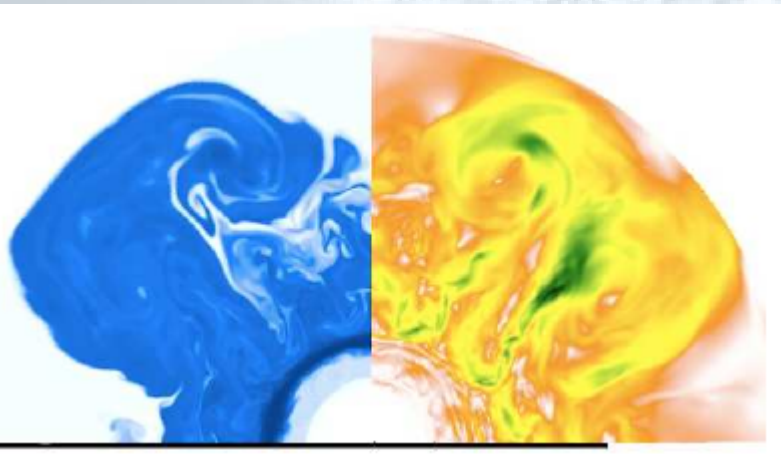
Convection physics uncertainties affect fate of models: strong/weak/failed explosions!!!

Way Forward: 1 to 3 to 1D link

Targetted 3D simulations

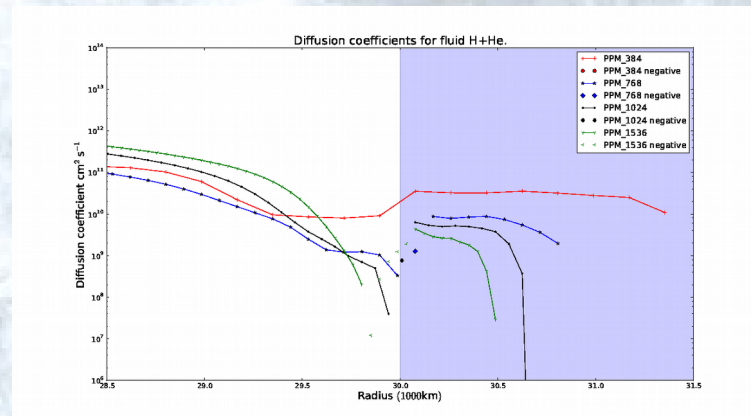
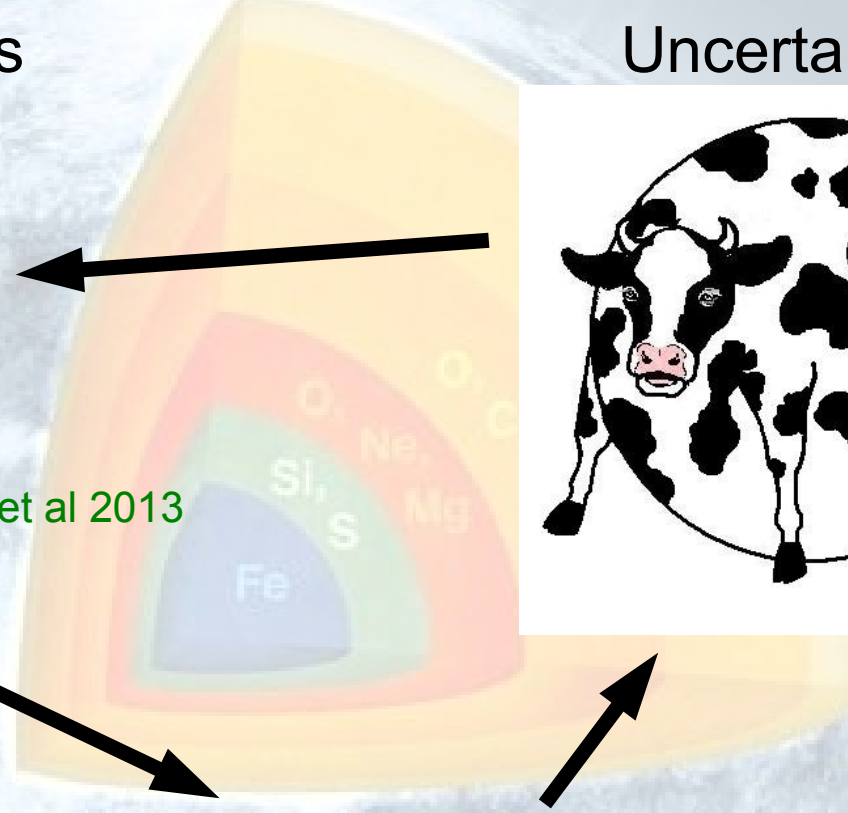
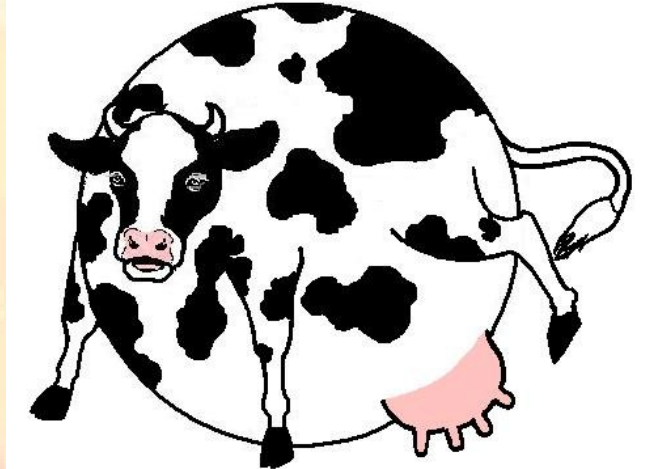


Herwig et al 06, Herwig, Woodward et al 2013



e.g. Arnett & Meakin 2011, ...
Mocak et al 2011,
Viallet et al 2013, ...

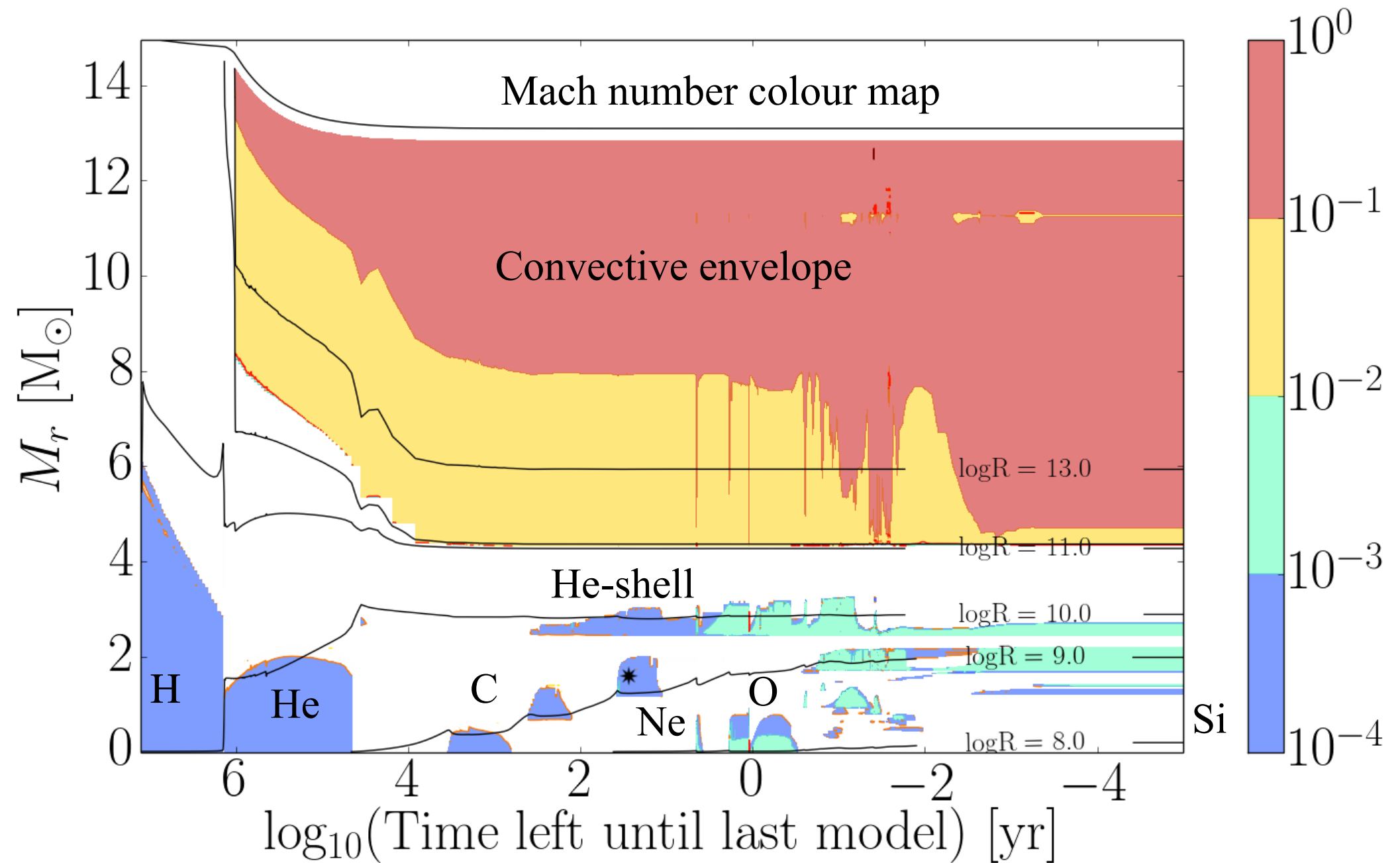
Uncertainties in 1D



Meakin et al 09 ; Bennett et al (thesis), Jones et al 16

→ Determine effective coefficient / improve theoretical prescriptions

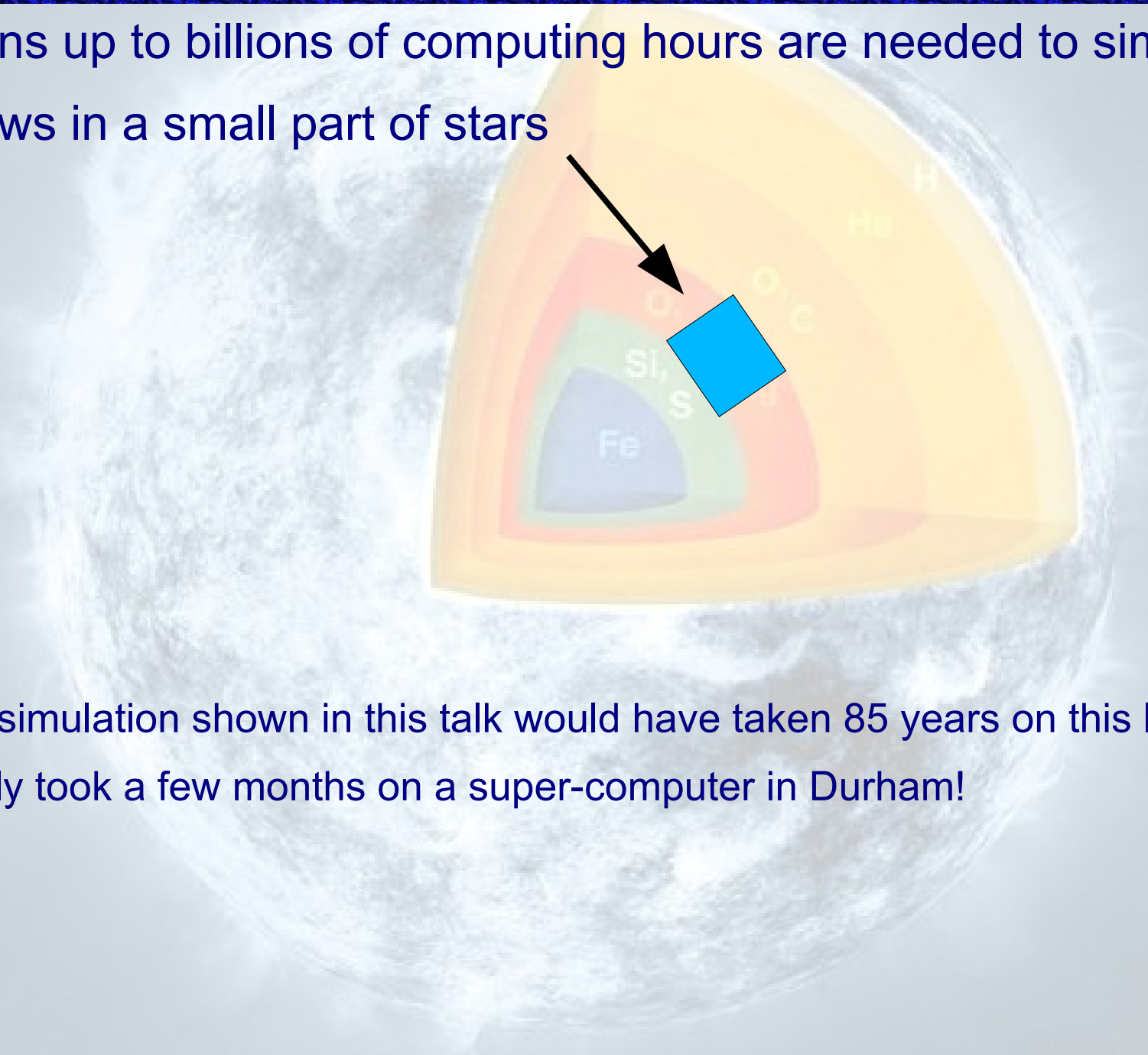
Where to Start?



Convection takes place during most burning stages

Large-Scale Hydrodynamic Simulations

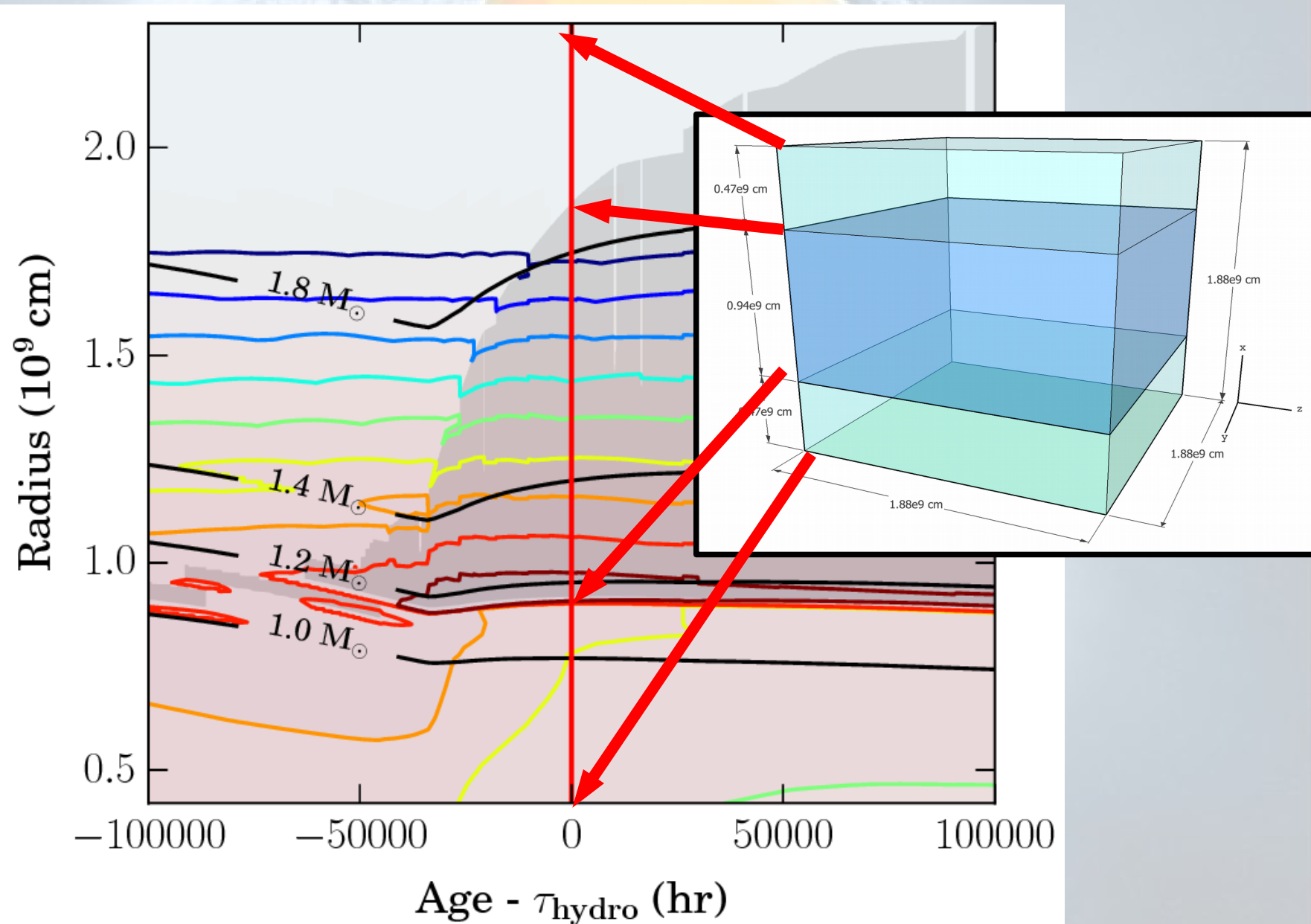
- Millions up to billions of computing hours are needed to simulate fluid flows in a small part of stars



The simulation shown in this talk would have taken 85 years on this laptop!!
It only took a few months on a super-computer in Durham!

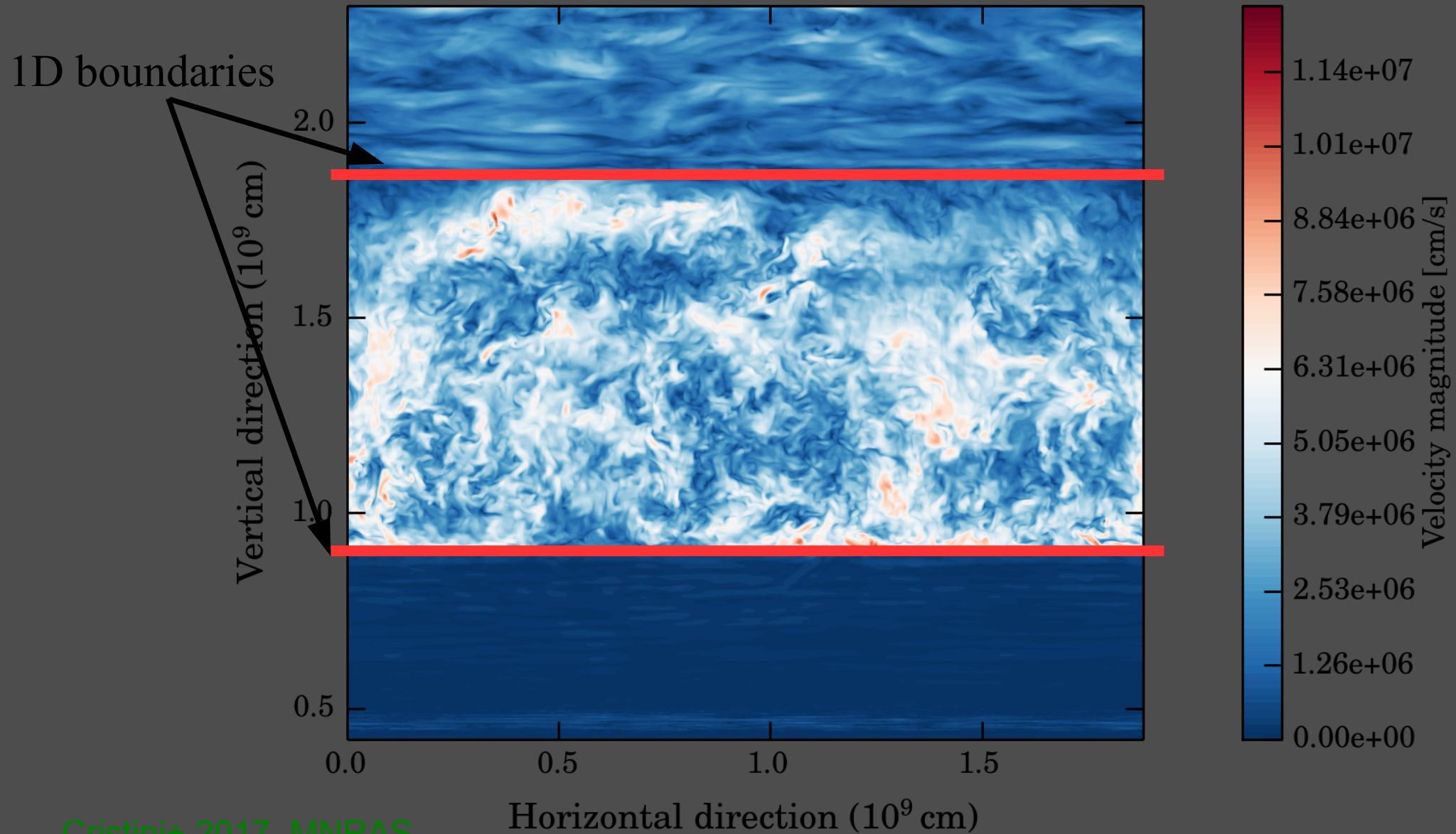
From 1D to 3D

C-shell in $15 M_{\odot}$, $Z=0.014$ 1D stellar evolution model



3D C-shell Simulations

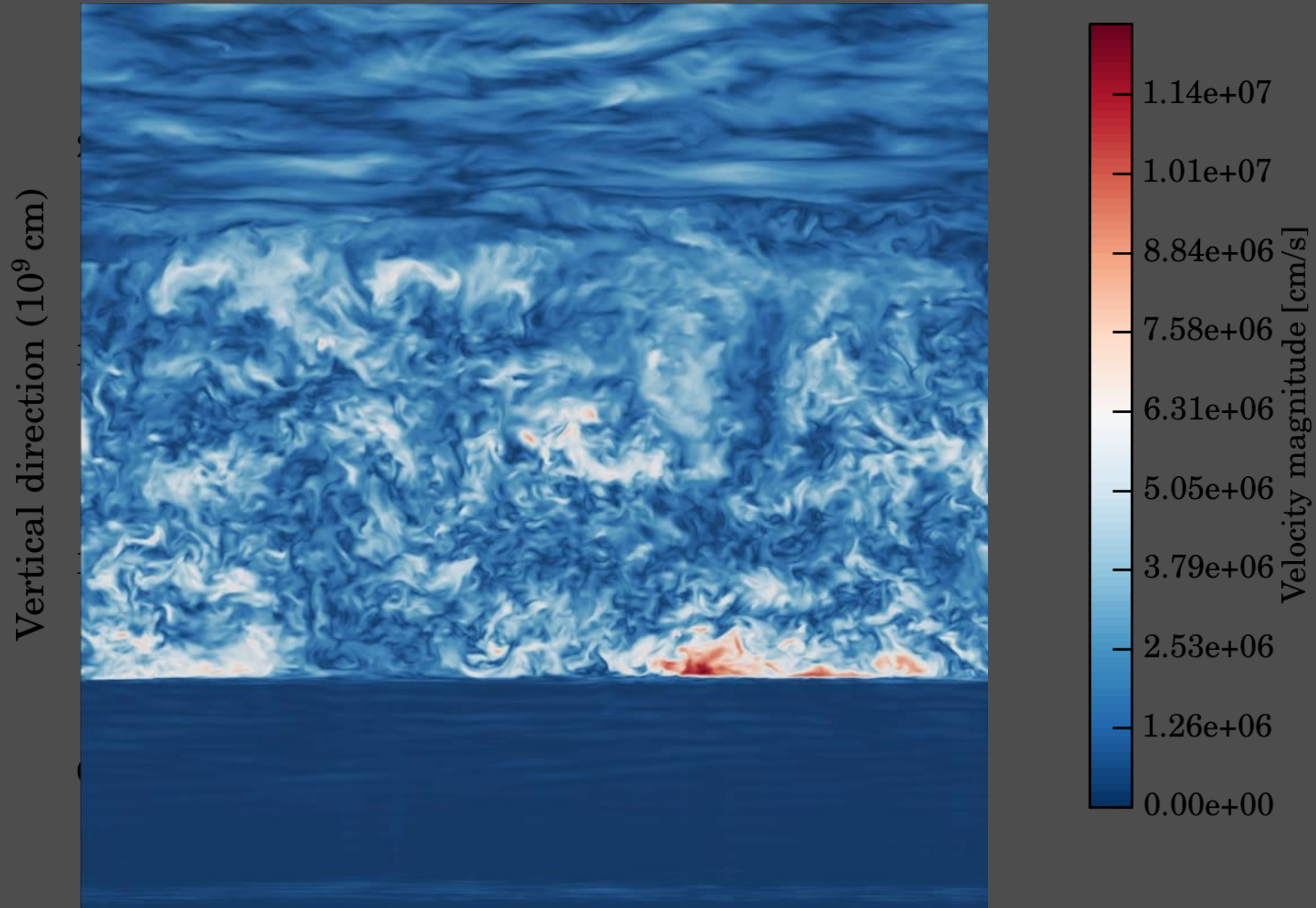
Snapshot from 1024^3 resolution run: Gas Velocity $\|\mathbf{v}\|$



3D C-shell Simulations: $|v|$ movie

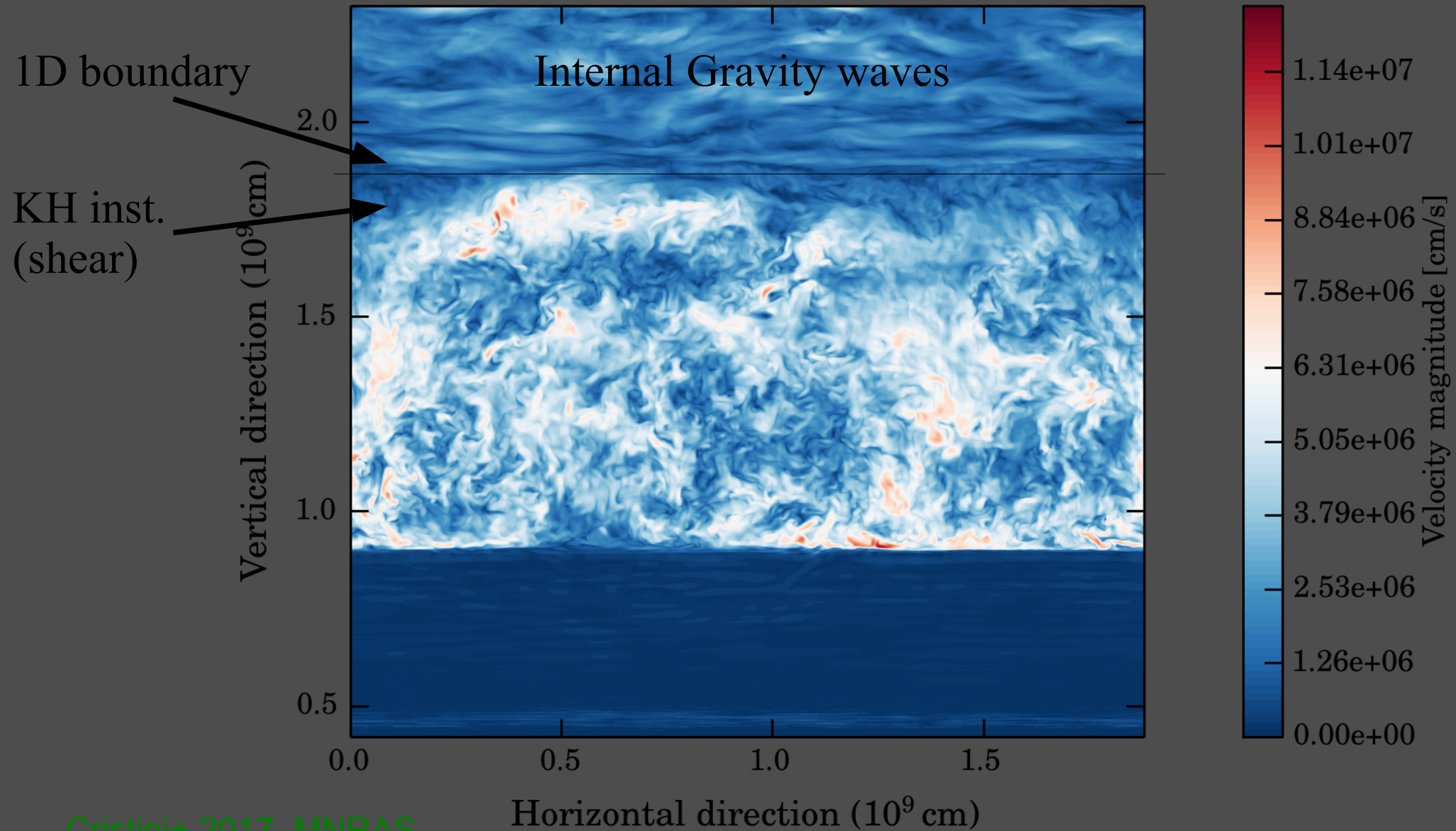
Cristini+ 2017, MNRAS

Gas Velocity $\|v\|$

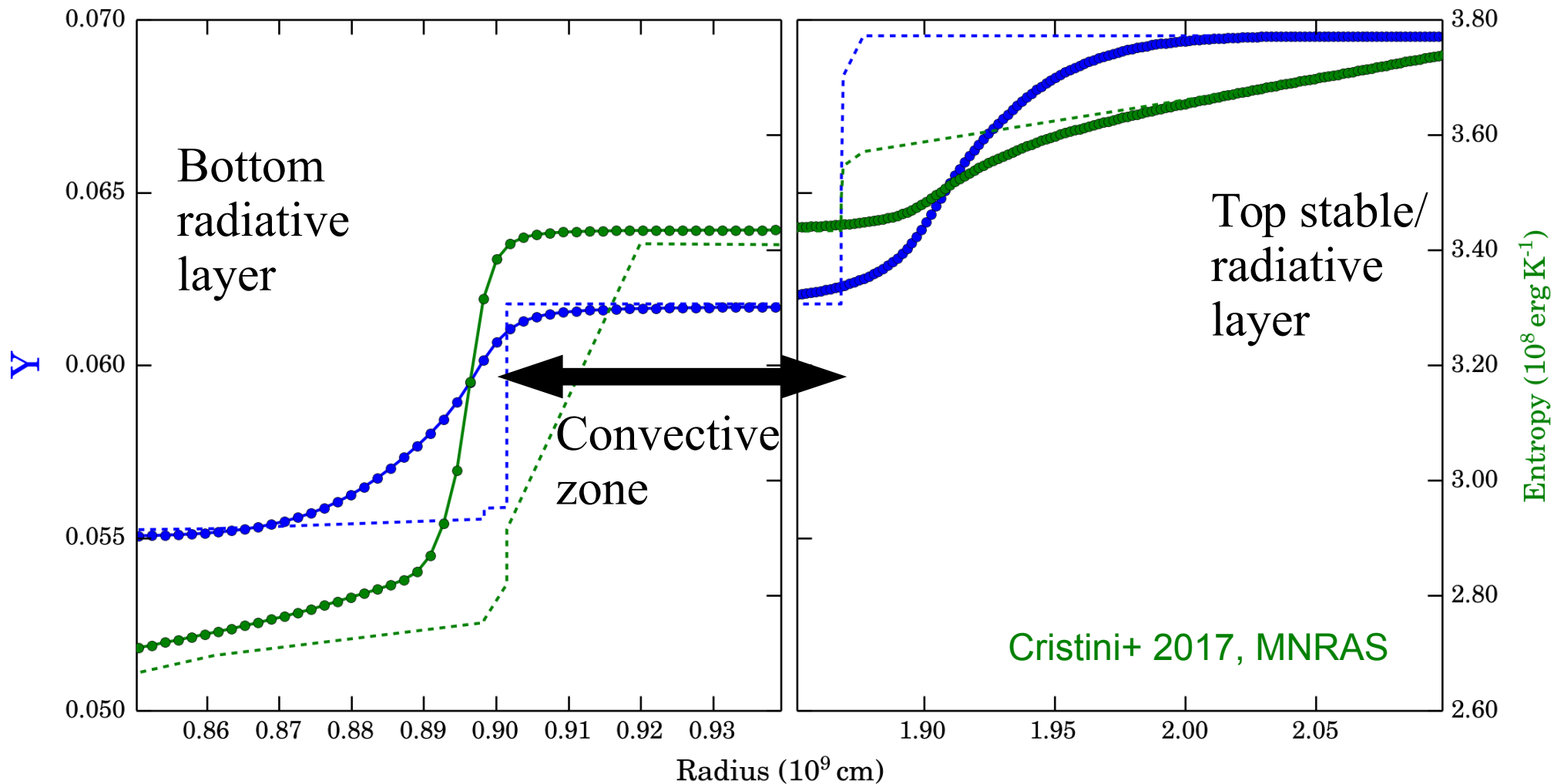


3D C-shell Simulations

Snapshot from 1024^3 resolution run: Gas Velocity $\|\mathbf{v}\|$

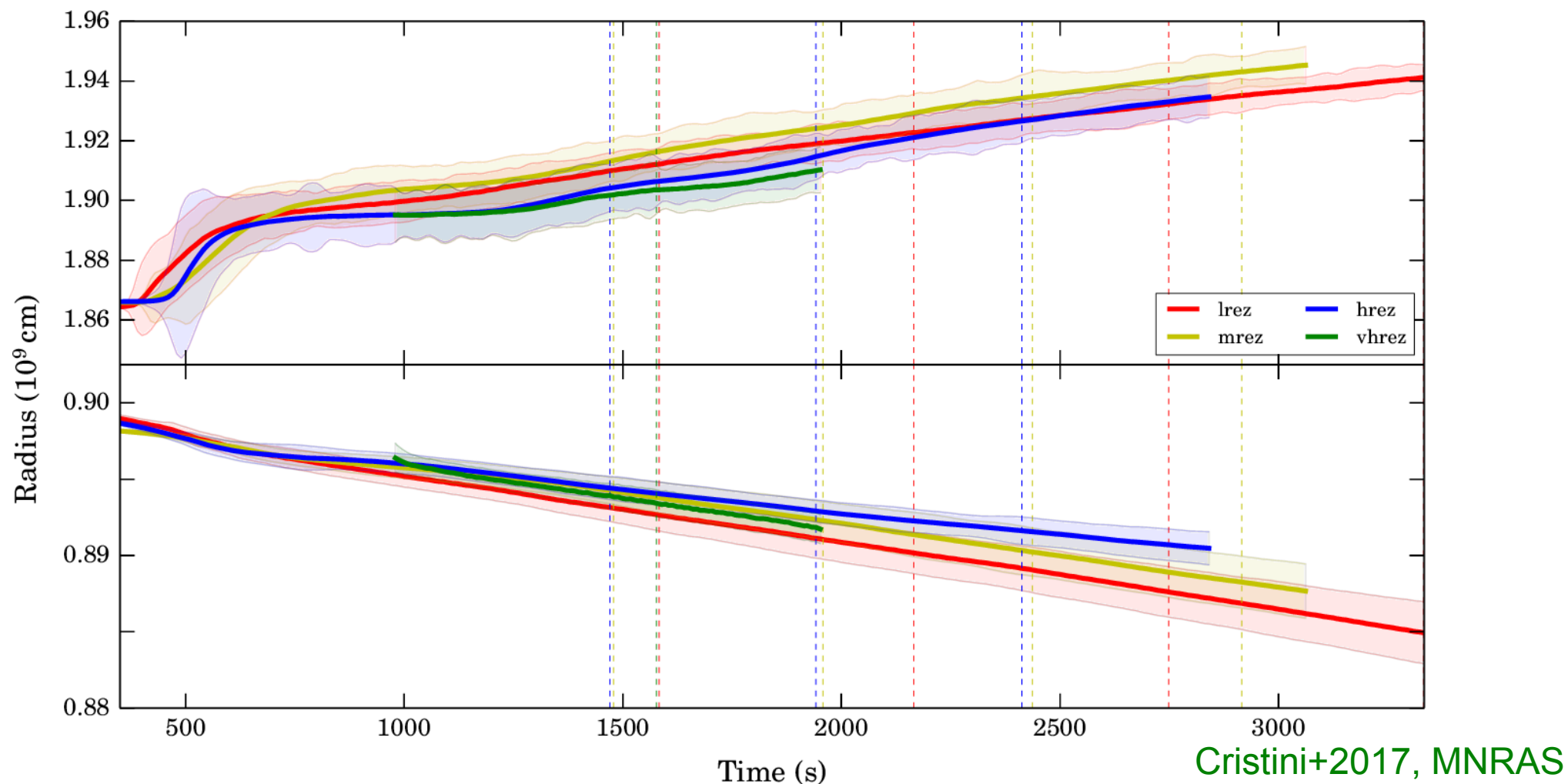


3D versus 1D



- Improved prescriptions for CBM needed!

Boundary Entrainment



Top: $u_e \sim 20,000$ cm/s; Bottom: $u_e \sim 3,000$ cm/s. *Rescaled for $\epsilon_{\text{ps}_{\text{burn}}}$ boosting (1/1000)*
 → In 1 year, top: $\Delta R \sim 6 \times 10^8$ cm, bottom: $\Delta R \sim 10^8$ cm: large but reasonable

Consistent with oxygen-shell results and entrainment law.

boundary layers

Stable Region
(IGW)

Shear Layer

Penetrative Overshoot /
Entrainment

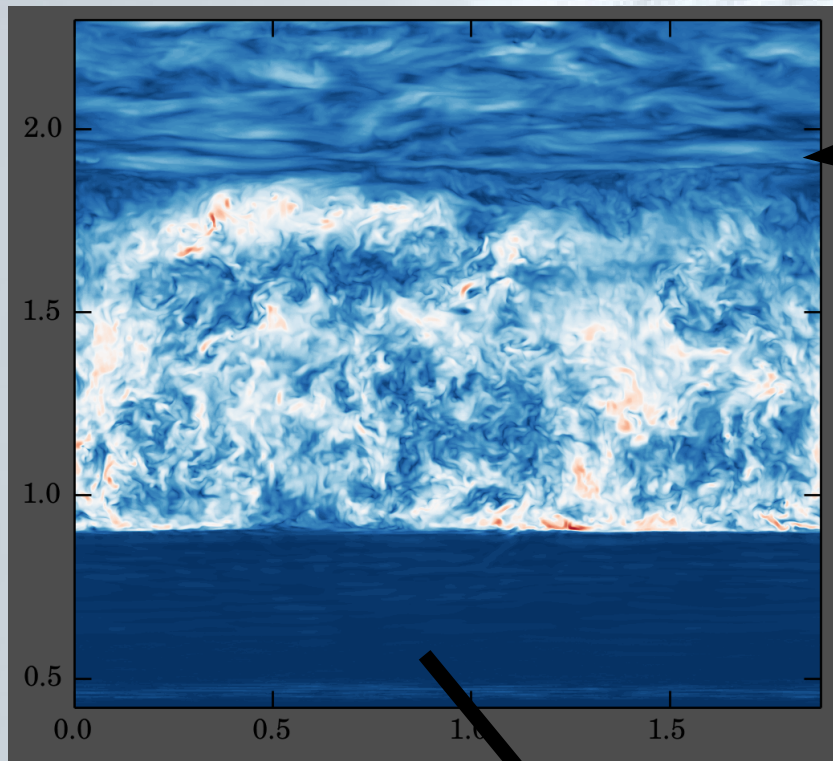
Convective Core
(or shell)

∇_{rad}

∇_{ad}

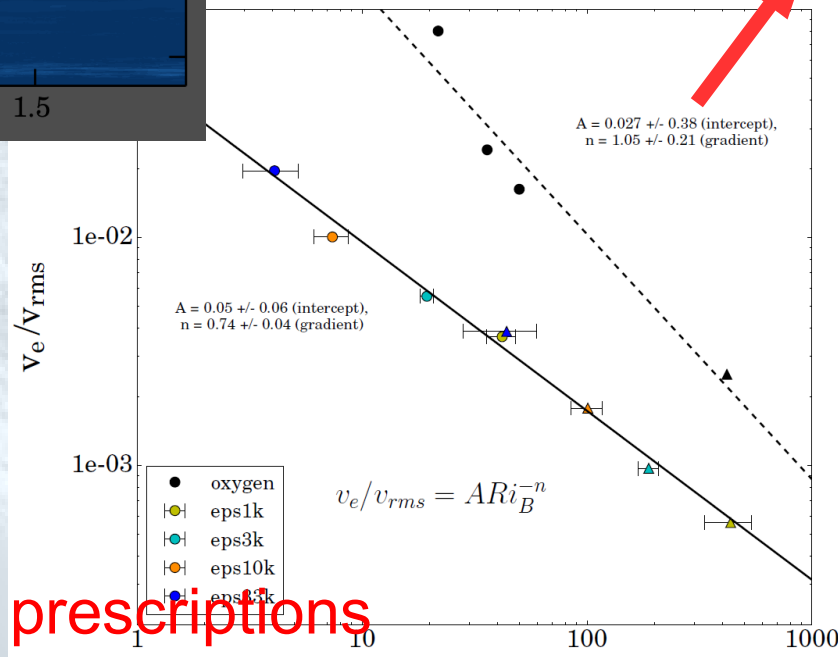
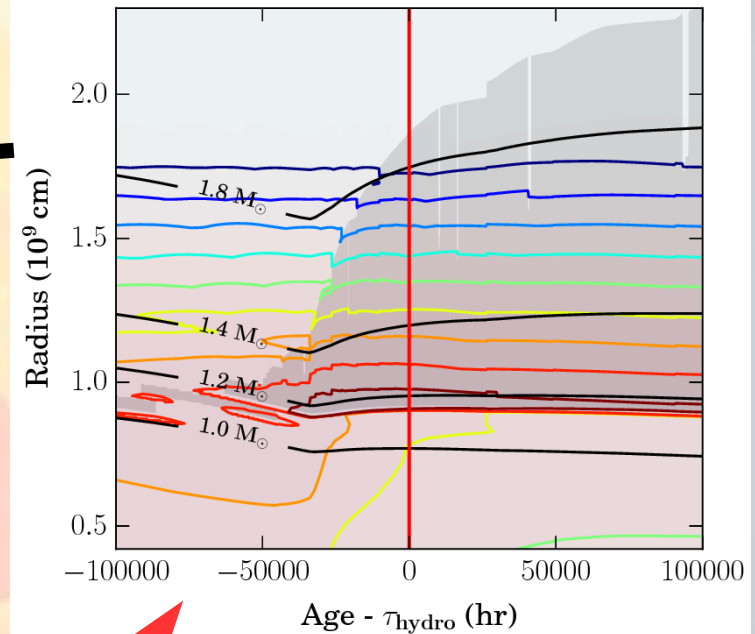
Way Forward: 1 to 3 to 1D link

Targeted 3D simulations



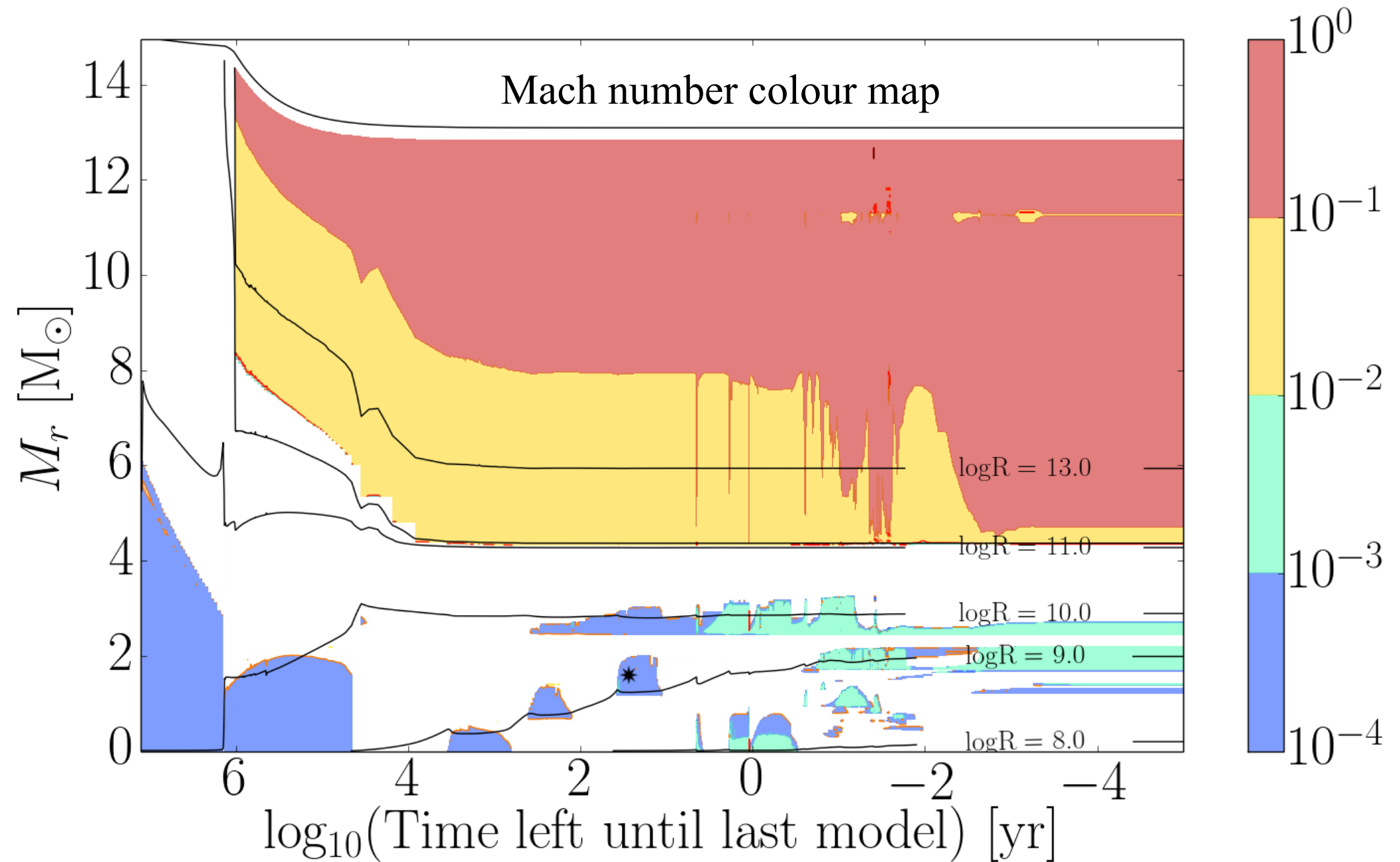
Cristini+2017

Uncertainties in 1D



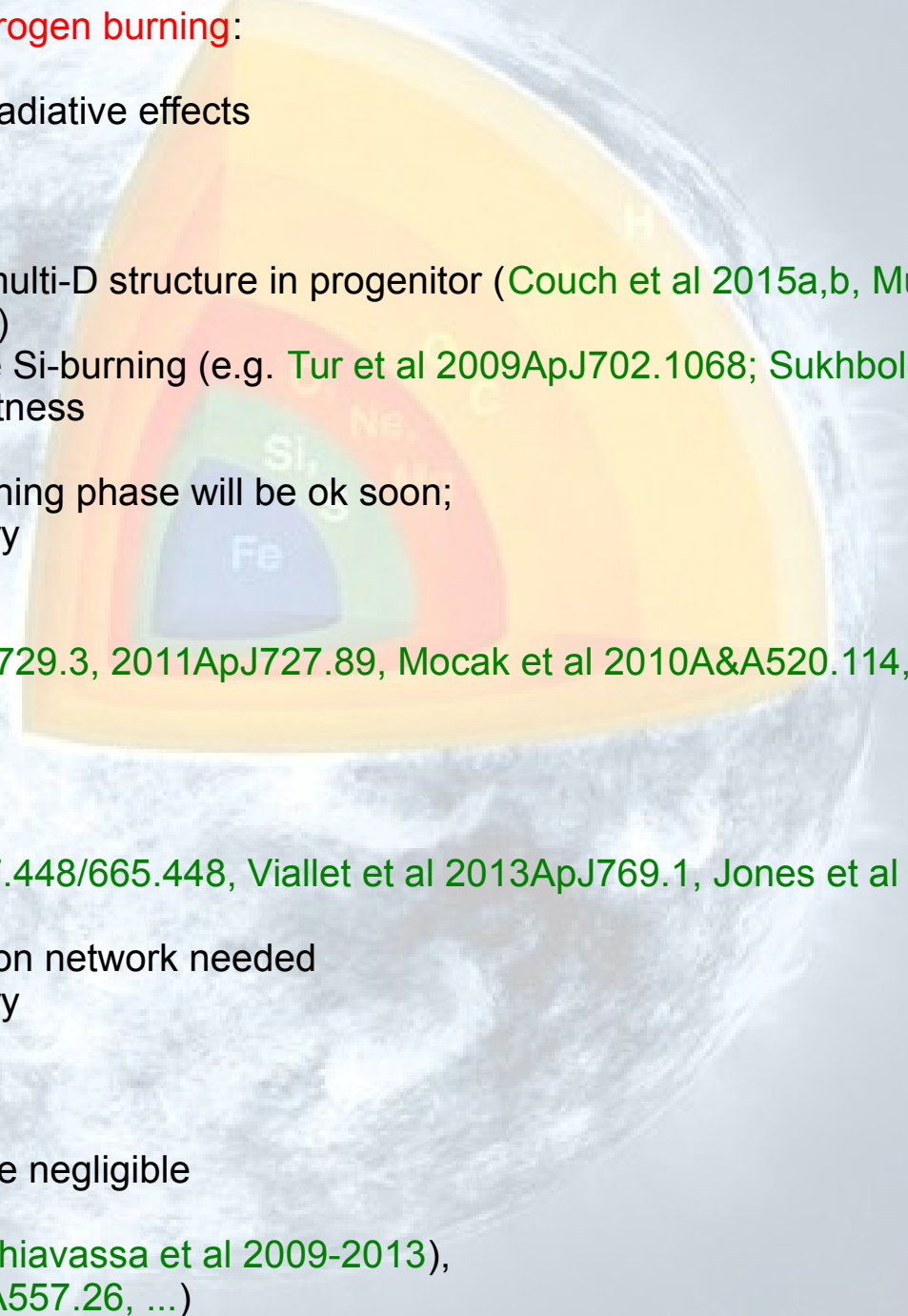
→ Improve theoretical prescriptions

Next Steps? Other Phases



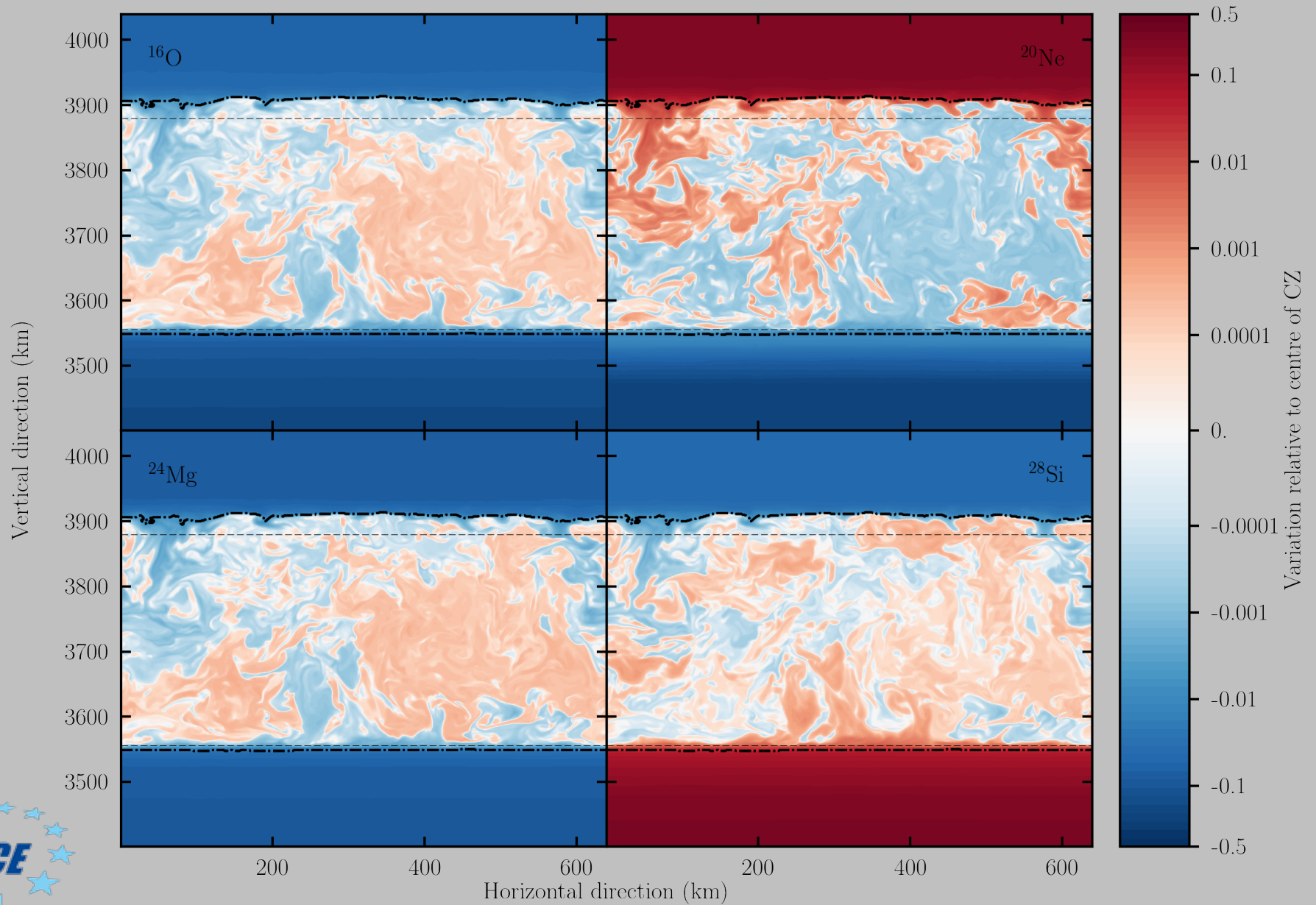
Low-Mach scheme better for H, He phases!

3D Hydro Efforts/Priority List

- 
- * **Convective boundary mixing during core hydrogen burning:**
 - +: many constraints (HRD, astero, ...)
 - -: difficult to model due to important thermal/radiative effects
 - -: long time-scale
 - * **Silicon burning:**
 - +: important to determine impact on SNe of multi-D structure in progenitor (Couch et al 2015a,b, Mueller & Janka [aph1409.4783](#), Mueller et al [ArXiv1605.01393](#))
 - +: possible shell mergers occurring after core Si-burning (e.g. Tur et al 2009ApJ702.1068; Sukhbold & Woosley 2014ApJ783.105) strongly affect core compactness
 - +: radiative effects small/negl.
 - -: $\sim 10^9$ CPU hours needed for full silicon burning phase will be ok soon;
 - -: might be affected by convective shell history
 - * **AGB thermal pulses/H-ingestion:**
 - +: already doable (e.g. Herwig et al 2014ApJ729.3, 2011ApJ727.89, Mocak et al 2010A&A520.114, Woodward et al 2015)
 - +: thermal/radiative effects not dominant
 - ?: applicable to other phases?
 - * **Oxygen shell:** (Meakin & Arnett 2007ApJ667.448/665.448, Viallet et al 2013ApJ769.1, Jones et al [ArXiv1605.03766](#))
 - +: similar to silicon burning but smaller reaction network needed
 - -: might be affected by convective shell history
 - * **Carbon shell:** (PhD A. Cristini)
 - +: not affected by prior shell history
 - +: first stage for which thermal effects become negligible
 - * Envelope of RSG (e.g. Viallet et al. 2013, Chiavassa et al 2009-2013),
 - * Solar-type stars (e.g. Magic et al. 2013A&A557.26, ...)

Ne-burning

Variation relative to centre of CZ, $t = 673.8$ s (dump 450)



Mass Loss: Types, Driving & Recipes

Mass loss driving mechanism and prescriptions at different stages:

- O-type & “LBV” stars (bi-stab.): line-driven Vink et al 2000, 2001
- WR stars (clumping effect): line-driven Nugis & Lamers 2000, Gräfener & Hamann (2008)
- RSG: Pulsation/dust? de Jager et al 1988
- RG: Pulsation/dust? Reimers 1975,78, with $\eta \sim 0.5$
- AGB: Super winds? Dust Bloeker et al 1995, with $\eta \sim 0.05$
- LBV eruptions: continuous driven winds? Owocki et al
- ...

What changes at low Z?

- Stars are **more compact**: $R \sim R(Z_0)/4$ (lower opacities) at $Z=10^{-8}$

$$\dot{M}(Z) = \dot{M}(Z_0) (Z/Z_0)^\alpha$$

- $\alpha = 0.5-0.6$ (Kudritzki & Puls 00, Ku02)

(Nugis & Lamers, Evans et al 05)

- $\alpha = 0.7-0.86$ (Vink et al 00,01,05)

$$Z(\text{LMC}) \sim Z_0/2.3 \Rightarrow \dot{M}/1.5 - \dot{M}/2$$

$$Z(\text{SMC}) \sim Z_0/7 \Rightarrow \dot{M}/2.6 - \dot{M}/5$$

Mass loss at low Z still possible?

RSG (and LBV?): no Z-dep.; CNO? (Van Loon 05, Owocky et al)

Mechanical mass loss $\leftarrow$ critical rotation

(e.g. Hirschi 2007, Ekstroem et al 2008, Yoon et al 2012)

The fate of VMS: PCSN/BH/CCSN?

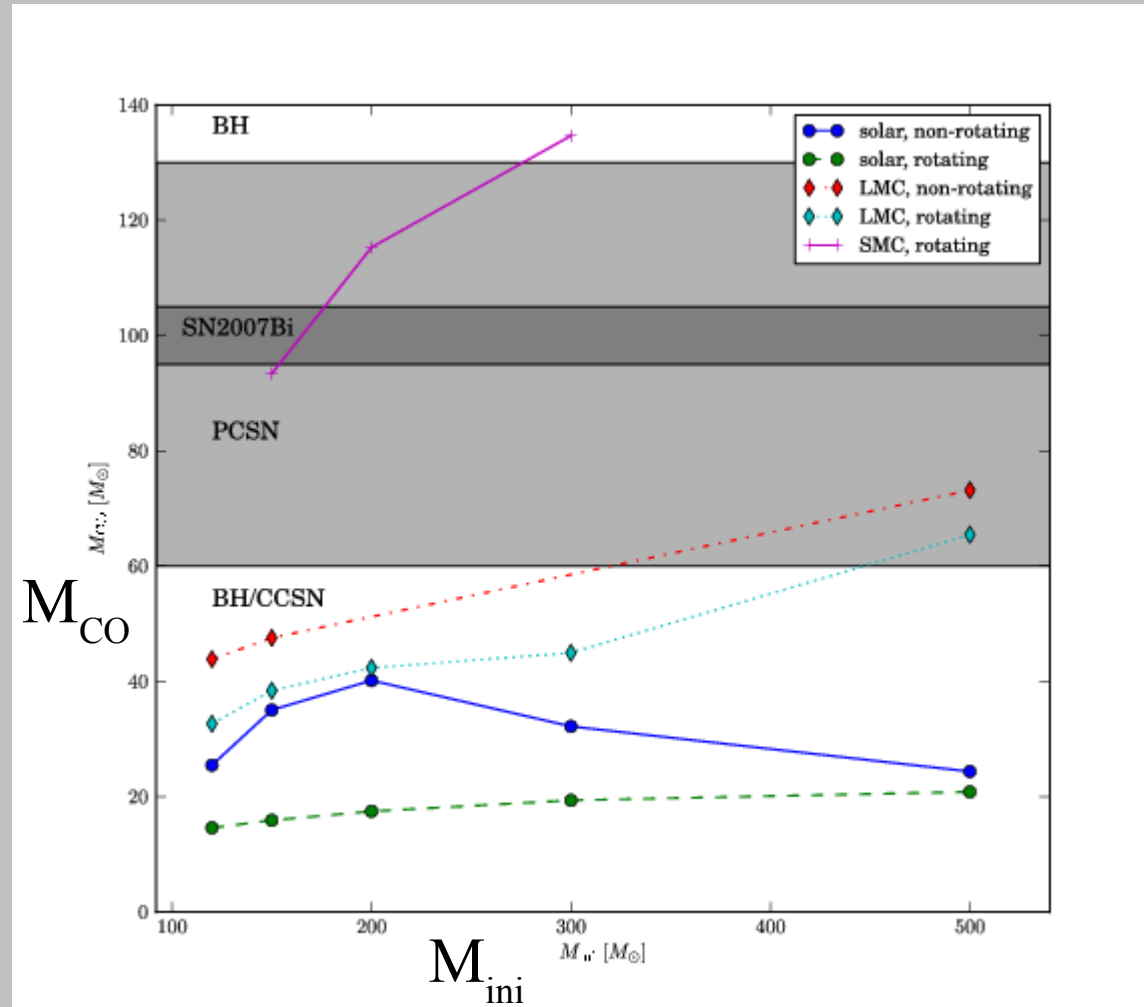
(Yusof et al 13 MNRAS, aph1305.2099)

Z_{solar} : no PCSN

(Rotating) models
with $Z < Z(\text{LMC})$
lose less mass,

and enter the
PCSN instability
region!

BUT mass loss
uncertain!



PCSN range
from
Heger &
Woosley
(2002)

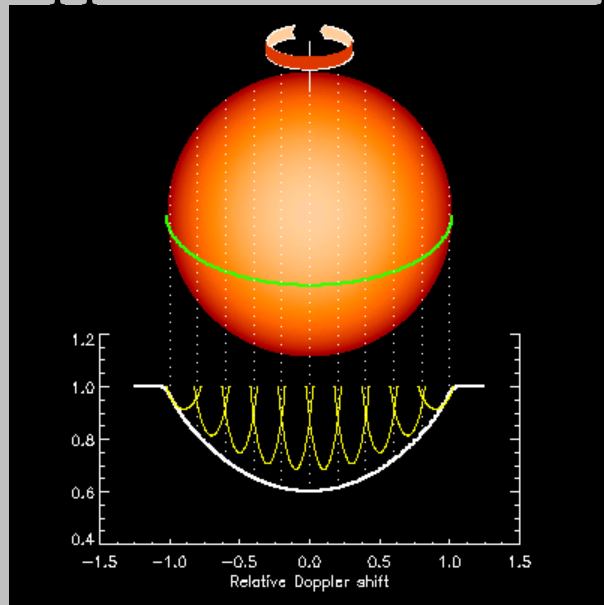
Consistent with Langer et al (2007): PCSN for $Z < Z_{\odot}/3$

Key Open Questions Concerning Mass Loss

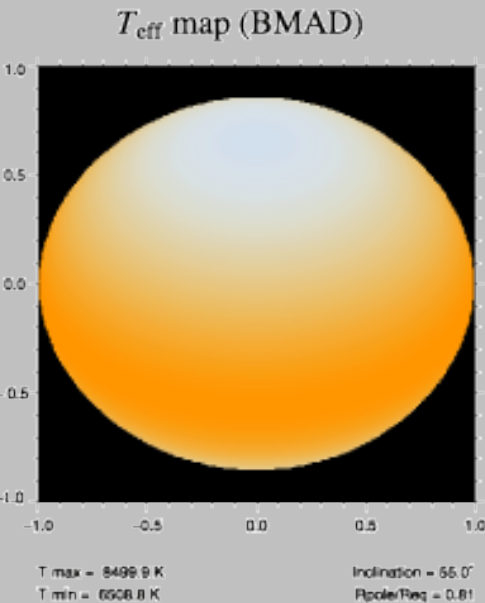
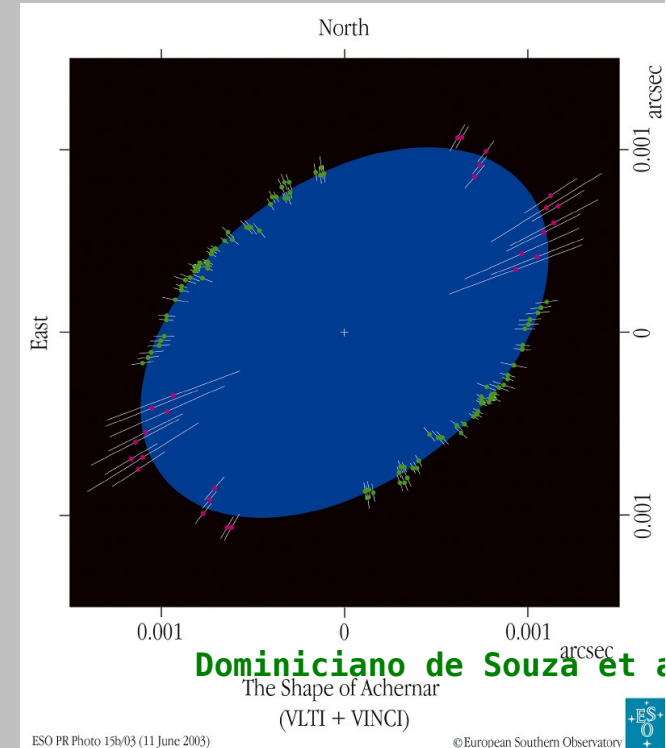
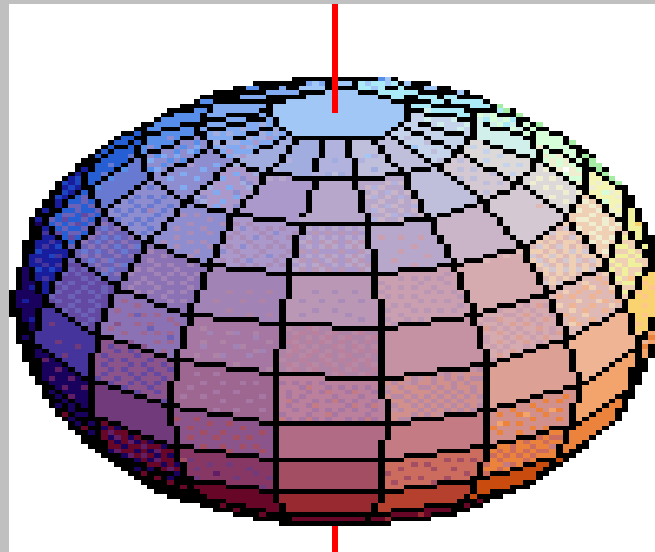
- Mass loss in cool parts of HRD: LBV & RSG, especially at low Z
- Position in & evolution across HRD: effects of rotation-induced mixing, feedback from mass loss Yusof et al 13, Langer 07, Sanyal et al 15, Kohler et al 15...
- **Mass loss near Eddington limit** Graefener & Hamann 08, Vink et al 11, ...
- Importance of clumping, porosity, inflation Fullerton et al 06, Graefener et al. 12, Vink et al, ...
- Which stars may explode in the LBV phase? Smith et al 11, ... , Vink et al, ...
- Look of WR stars: radius, spectra Graefener et al. 2012, Groh et al 2013-...
- Additional mass loss mechanisms? Critical rotation at low Z? Shell mergers in late phases of evolution? ... Hirschi 2007, Meynet et al 2006, ... , Smith & Arnett 2014, ...
- ...

Rotational Effects on Surface

Doppler-broadened line profile



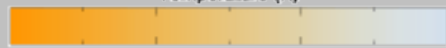
Fast rotators $\rightarrow$ oblate shape:



$\leftarrow$ Altair: pole brighter than equator: Effect compatible with von-Zeipel theorem (1924)

$\rightarrow$ enhanced mass loss (+ anisotropic)

Domiciano de Souza et al. 2005
Temperature (K)



Stellar Evolution with Rotation: Geneva Code

1.5D hydrostatic code (Eggenberger et al 2008)

Rotation: (Maeder & Meynet 2008)

Centrifugal force: **KEY FOR GRB prog.**

$$\vec{g}_{\text{eff}} = \vec{g}_{\text{eff}}(\Omega, \theta) = \left(-\frac{GM}{r^2} + \Omega^2 r \sin^2 \theta \right) \vec{e}_r + \Omega^2 r \sin \theta \cos \theta \vec{e}_\theta$$

Shellular rotation → still 1D: (Zahn 1992)

- Energy conservation:

$$\frac{\partial L_P}{\partial M_P} = \epsilon_{\text{nucl}} - \epsilon_\nu + \epsilon_{\text{grav}} = \epsilon_{\text{nucl}} - \epsilon_\nu - c_p \frac{\partial T}{\partial t} + \frac{\delta}{\rho} \frac{\partial P}{\partial t} \quad (2.9)$$

- Momentum equation:

$$\frac{\partial P}{\partial M_P} = -\frac{GM_P}{4\pi r_P^4} f_P \quad (2.10)$$

- Mass conservation (or continuity equation):

$$\frac{\partial r_P}{\partial M_P} = \frac{1}{4\pi r_P^2 \bar{\rho}} \quad (2.11)$$

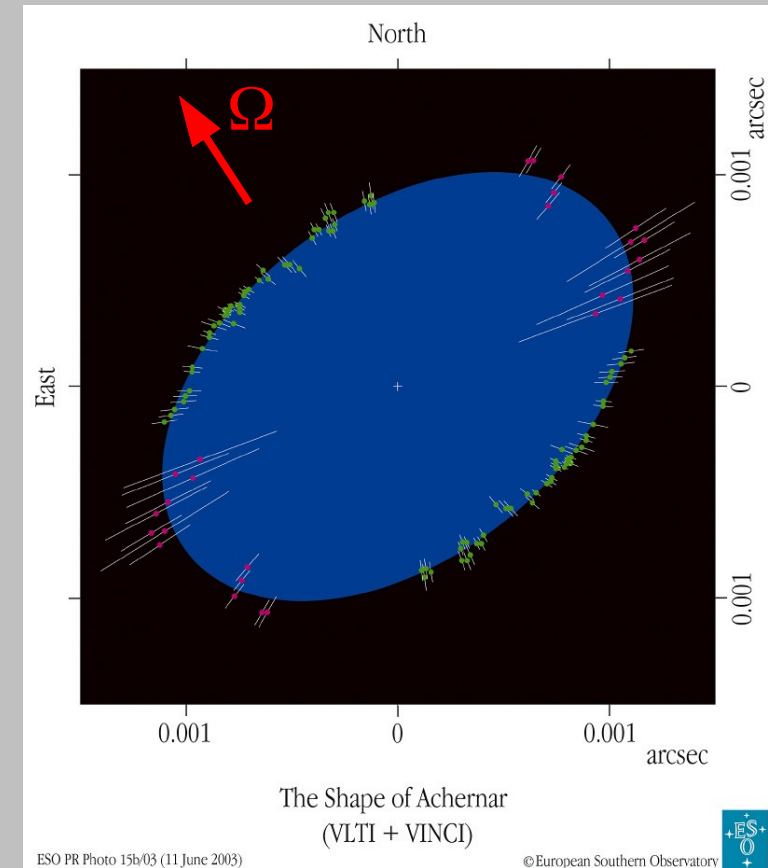
- Energy transport equation:

$$\frac{\partial \ln \bar{T}}{\partial M_P} = -\frac{GM_P}{4\pi r_P^4} f_P \min[\nabla_{\text{ad}}, \nabla_{\text{rad}} \frac{f_T}{f_P}] \quad (2.12)$$

where

$$\nabla_{\text{ad}} = \frac{P\delta}{\bar{T}\rho c_p} \quad (\text{convective zones}),$$

$$\nabla_{\text{rad}} = \frac{3}{16\pi acG} \frac{\kappa l P}{m \bar{T}^4} \quad (\text{radiative zones}),$$



$$f_P = \frac{4\pi r_P^4}{GM_P S_P} \frac{1}{\langle g^{-1} \rangle},$$

$$f_T = \left(\frac{4\pi r_P^2}{S_P} \right)^2 \frac{1}{\langle g \rangle \langle g^{-1} \rangle},$$

(Meynet and Meynet 97)

Rotation Induced Transport

Zahn 1992: strong horizontal turbulence

Transport of angular momentum:

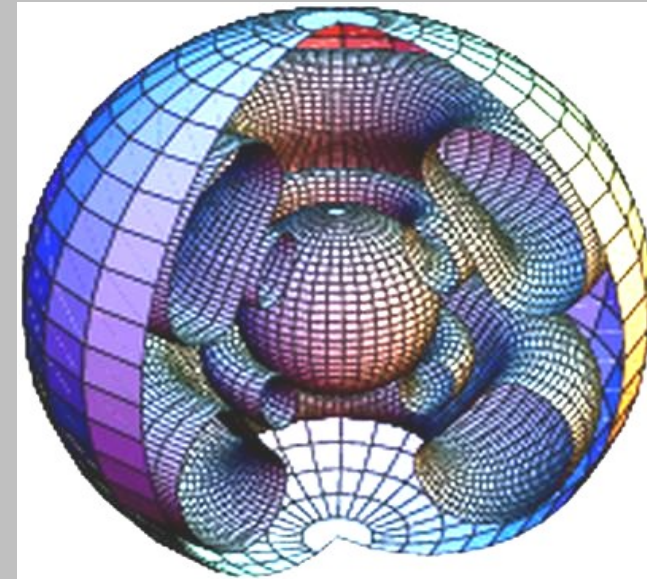
$$\rho \frac{d}{dt} (r^2 \bar{\Omega})_{M_r} = \underbrace{\frac{1}{5r^2} \frac{\partial}{\partial r} (\rho r^4 \bar{\Omega} U(r))}_{\text{advection term}} + \underbrace{\frac{1}{r^2} \frac{\partial}{\partial r} \left(\rho D r^4 \frac{\partial \bar{\Omega}}{\partial r} \right)}_{\text{diffusion term}}$$

Transport of chemical elements:

$$\rho \frac{dX_i}{dt} = \frac{1}{r^2} \frac{\partial}{\partial r} \left(\rho r^2 [D + D_{eff}] \frac{\partial X_i}{\partial r} \right) + \left(\frac{dX_i}{dt} \right)_{\text{nucl}}$$

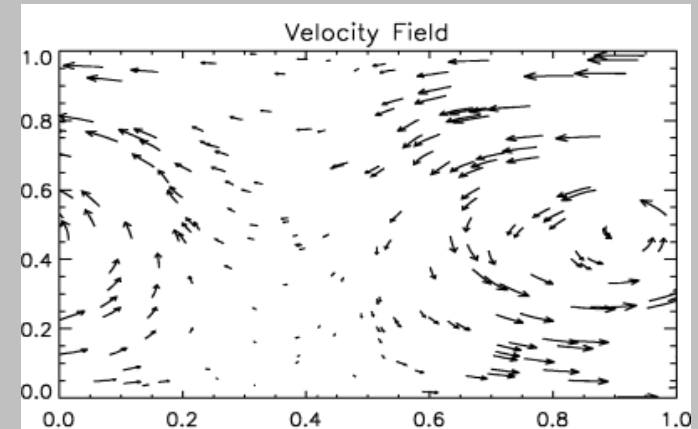
D: diffusion coeff. due to various transport mechanisms (convection, shear)

D_{eff}: diffusion coeff. due to meridional circulation + horizontal turbulence



Meynet & Maeder 2000

Shear instabilities

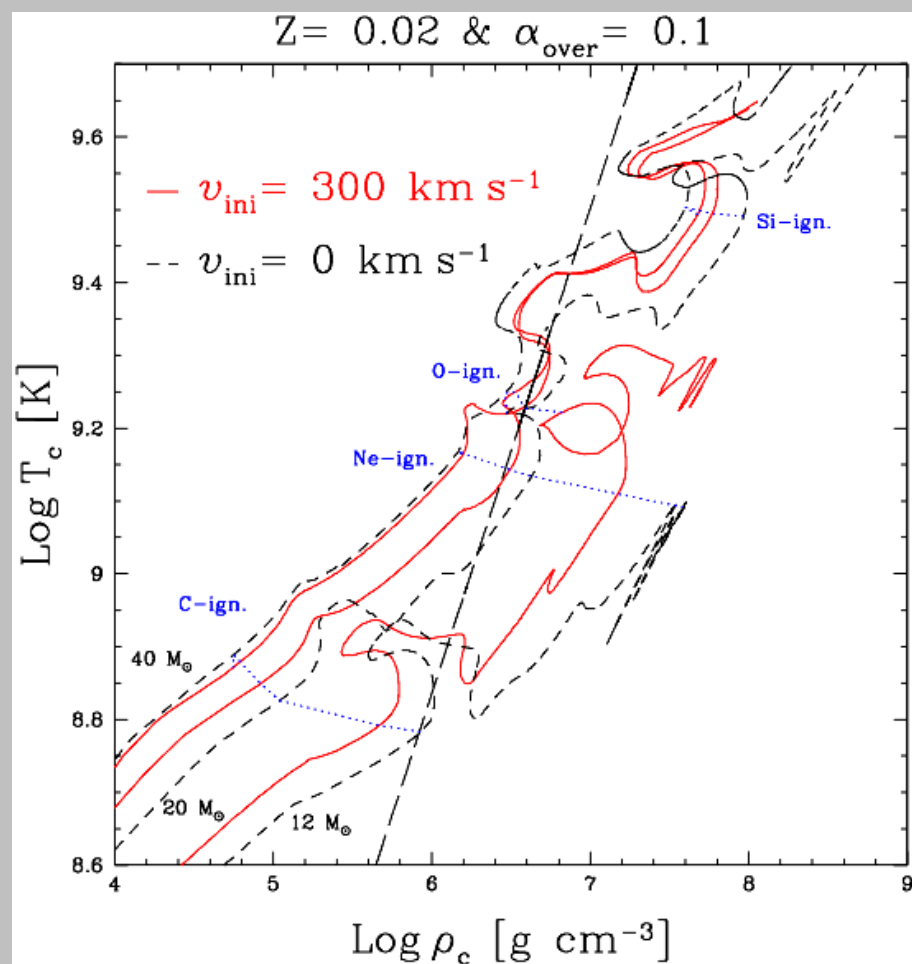
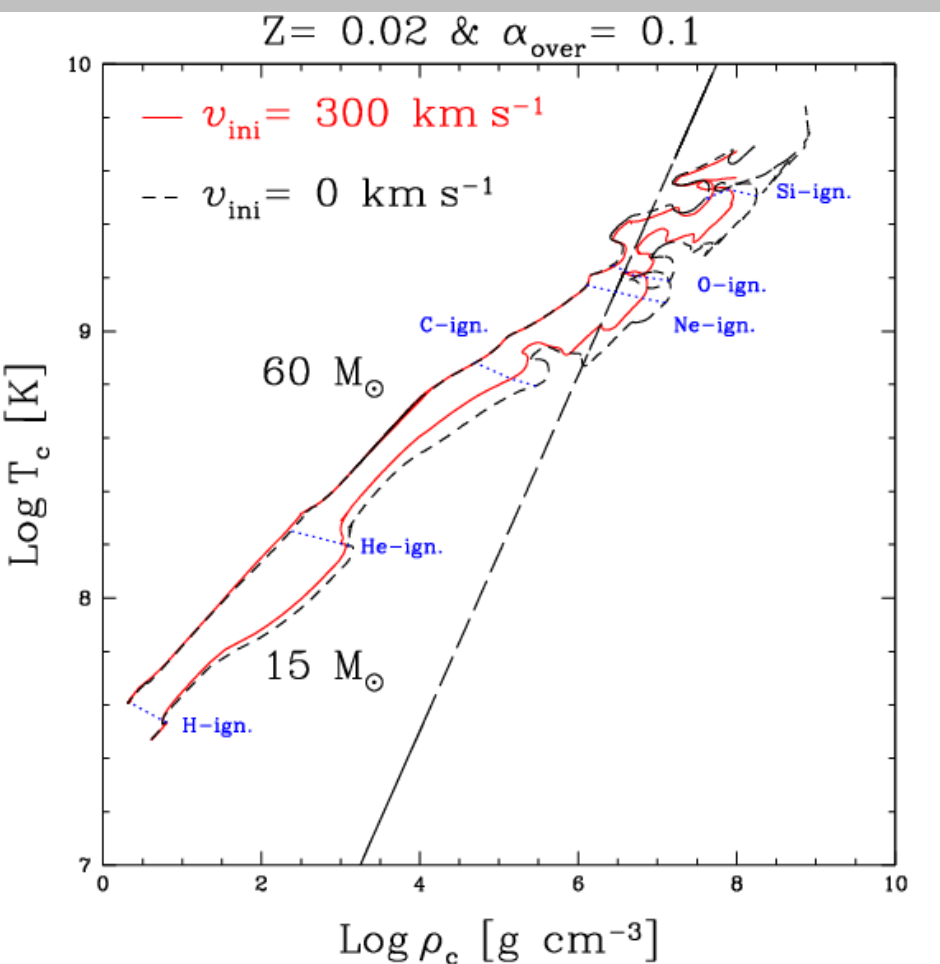


Brueggen & Hillebrandt 2000

Massive Stars

$M < \sim 30 M_{\odot}$: Rotational **mixing** dominates $\rightarrow$ bigger cores

$M > \sim 30 M_{\odot}$: **mass loss** dominates $\rightarrow$ $\sim$ or smaller cores



Key Open Questions Concerning Rotation

- Uncertainties in strength of rotation-induced mixing Hunter et al 07/08, Maeder et al 07, ...
- Importance/impact of diff. prescriptions & their implementations (advective vs diffusive) Meynet et al LNP, 13, Meynet/Maeder et al ..., Chieffi & Limongi et al 13, Heger et al 2000, Paxton et al 13 (MESA), Martins & Palacios, 13
- Interaction between magnetic fields and rotation: Solid body rotation? More or less mixing? Spruit 02, Heger et al 05-..., Yoon et al 06-... Maeder et al 2005-..., Potter et al 12, ...
- Impact of binary interactions on distribution of rotation velocities Langer et al 2012, de Mink et al 2013, ...
- Additional transport mechanism for Ω needed ←asteroseismology Cantiello et al. 14, Eggenberger 15; Spada et al. 16, Eggenberger et al 16, den Hartogh et al 2019
- ...

Key Open Questions Concerning Binary Interactions

... see e.g. De Marco & Izzard 2017 review on binaries

- Distributions: mass ratios, orbital separation, fraction of single stars ...
- Common envelope phase and outcome ...
- Efficiency of mass transfer: how conservative? Accretion rates for Novae? ...
- SN kicks and angular momentum accretion ...
- Triple stars ...
- ...

Advert for Recent Activities

- Main & weak s processes:

Large grid of massive star models + weak s proc (Frischknecht+2016, MNRAS):

Nugrid: set 1 (Pignatari+2016, ApJS), set1extension (Ritter+in 2018, MNRAS),

s process with new convective boundary mixing (CBM): (Battino+ ApJ 2016)

- **Nuclear uncertainties:** MC-based sensitivity studies for gamma-process (CCSNe: Rauscher+2016, MNRAS, SNIa: Nishimura+2018, MNRAS), weak s process (Nishimura+2017, MNRAS), main s process (Cescutti+in 2018)

- Stellar uncertainties:

Multi-D tests of convection (Cristini+ 2017, MNRAS) and rotation (Edelmann+2017, A&A)

- Reviews/book chapters: Springer Handbook of Supernovae

“Pre-supernova Evolution and Nucleosynthesis in Massive Stars and Their Stellar Wind Contribution”
(doi:10.1007/978-3-319-20794-0_82-1)

“Very Massive and Supermassive Stars: Evolution and Fate” (doi:10.1007/978-3-319-20794-0_120-1)

- ChETEC COST Action 2017-2021: see www.chetec.eu for details

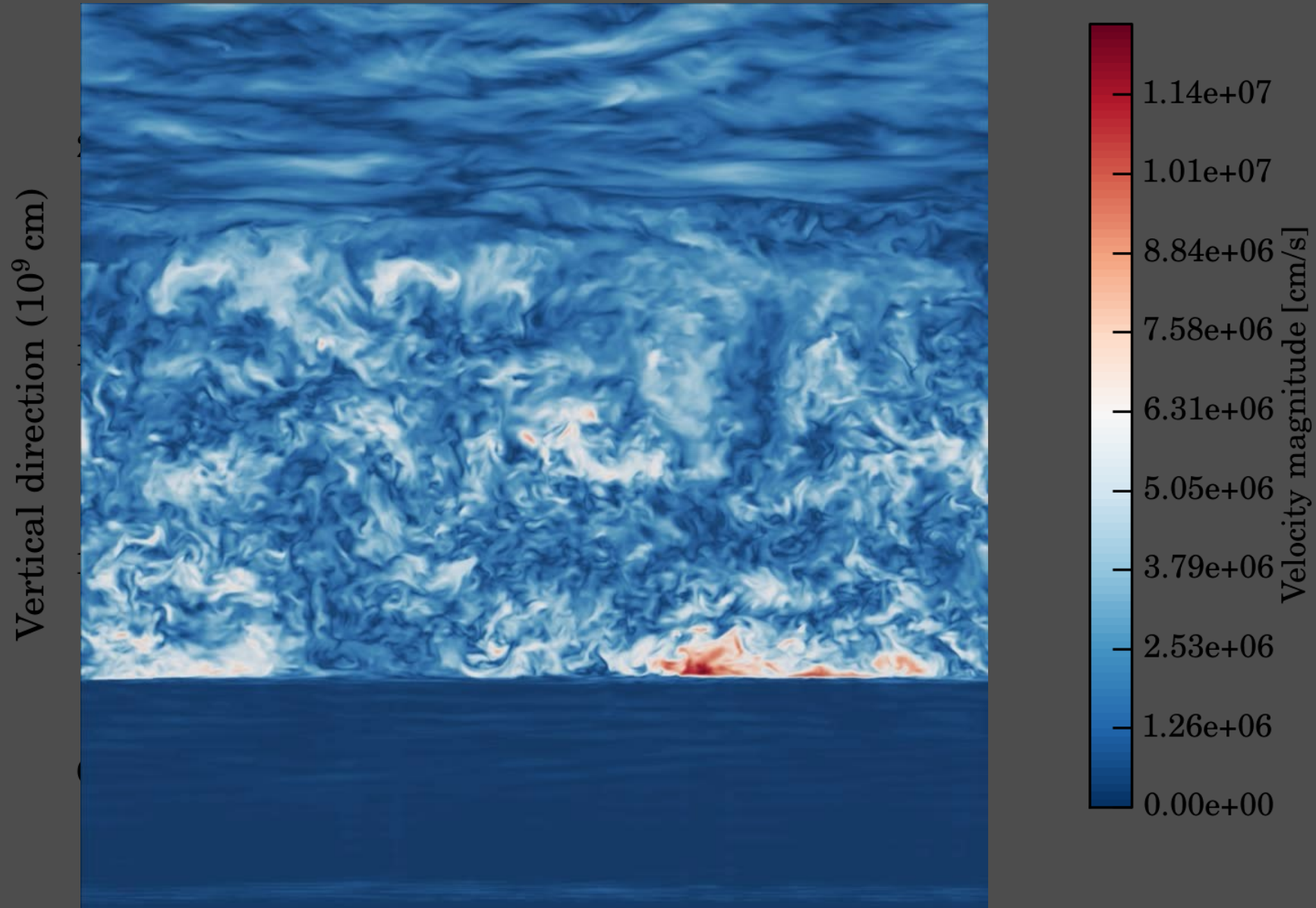
Conclusions & Outlook

- Physical ingredients still uncertain: nuclear reactions, convection, rotation, mass loss + B-fields, binarity
- Priority lists established: **large effort needed!**
- 1D to 3D to 1D work underway: **new CBM prescriptions under development!**
- Exciting times ahead: complex physics explored & CPU-GPU supercomputers enable us to do much more in multi-D

3D C-shell Simulations: $|v|$ movie

Cristini+ 2017, MNRAS

Gas Velocity $\|v\|$



Recent work

- Massive stars and the (not always) weak s process:

Large grid of massive star models + weak s proc (Frischknecht+2016, MNRAS):

Nugrid: set 1 (Pignatari+2016, ApJ), set1extension (Ritter+in subm.),

(main) s process with new convective boundary mixing (CBM): (Battino+ ApJ 2016)

- Nuclear uncertainties: MC-based sensitivity studies for gamma-process (Rauscher+2016, MNRAS), weak s process (Nishimura+2017, MNRAS), main s process (Cescutti+in prep)

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- ChETEC COST Action started in April 2017: see www.chetec.eu for details