

Probing D0-brane Black Holes

Evan Berkowitz

MCSMC: Monte Carlo String + M-Theory Collaboration

Forschungszentrum Jülich

Quantum Gravity meets Lattice QFT

2018-09-03

ECT*

1606.04948 1606.04951 EB, Enrico Rinaldi, Masanori Hanada, Pavlos Vranas,
Goro Ishiki, Shinji Shimasaki

1709.01932 Rinaldi, EB, Hanada, Maltz, and Vranas

+ forthcoming work

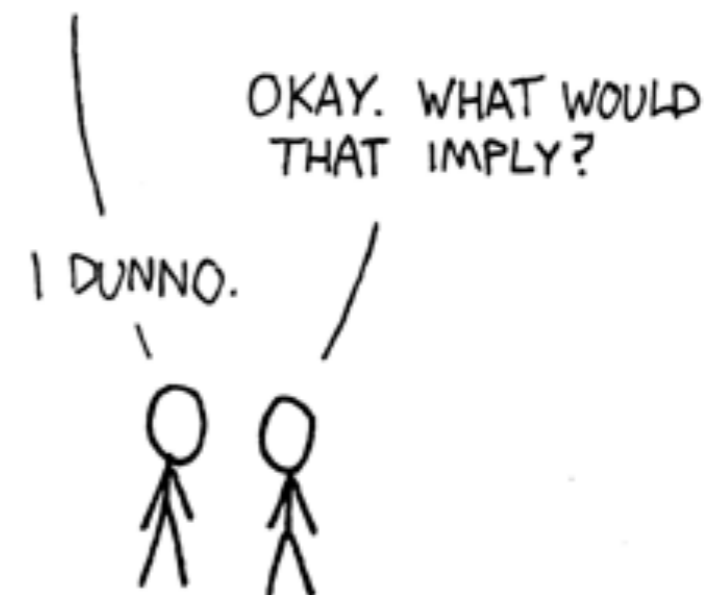
Parts of this work were performed under the auspices of the U.S. Department of Energy
by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344

Outline

- Gauge/Gravity Duality & Motivation
- The BFSS / D0 Matrix Model
- Monte Carlo, Fitting
- Tests of Holography
- Probes of Geometry

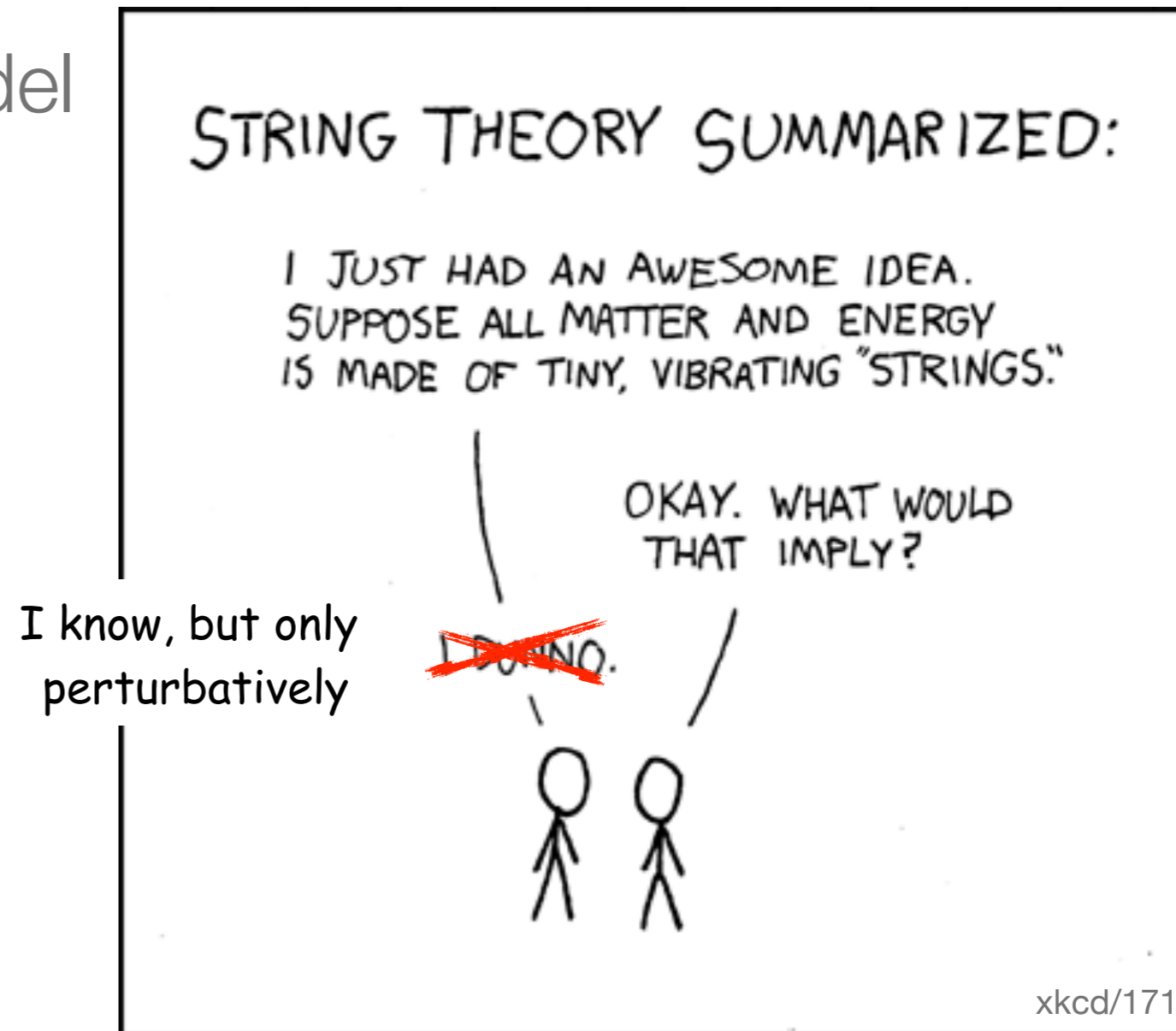
STRING THEORY SUMMARIZED:

I JUST HAD AN AWESOME IDEA.
SUPPOSE ALL MATTER AND ENERGY
IS MADE OF TINY, VIBRATING "STRINGS."



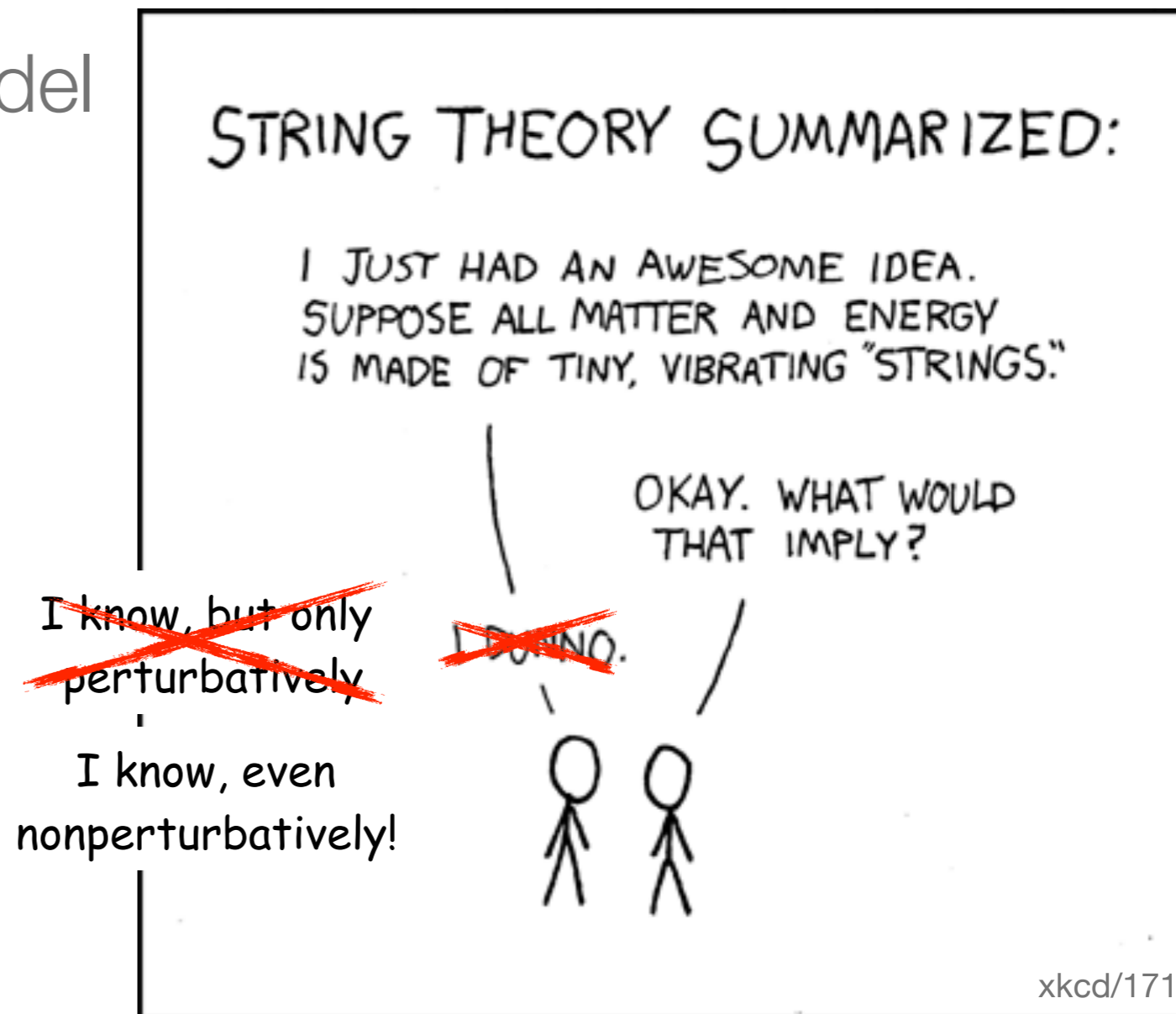
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Do you have the quantum data?

Interstellar



QUANTUM OF SOLACE

7^F
TM



COLUMBIA
PICTURES

QUANTUM OF SOLACE - 007 - SCREEN RESOLUTION 1280X1024 WIDESCREEN - THE ORIGINAL PICTURE BELONGS TO COLUMBIA & MGR™ PICTURE - MADE (FAN ART) BY ANTIROBOTIC

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0+1 D0 Brane QM / BFSS Matrix Model

Banks Fischler Shenker Susskind hep-th/9610043

$$L = \frac{1}{2g_{YM}^2} \text{Tr} \left\{ (D_t X_M)^2 + i\bar{\psi}^\alpha D_t \gamma_{\alpha\beta}^{10} \psi^\beta + \bar{\psi}^\alpha \gamma_{\alpha\beta}^M [X_M, \psi^\beta] + [X_M, X_{M'}]^2 \right\}$$

Yukawa
Self-interaction

$$D_t \cdot = \partial_t \cdot - i[A_t, \cdot]$$

γ^M left-handed part of 9+1D γ s

X_M 9 bosonic

ψ^α 16 fermionic

$N \times N$ matrices

- Obvious nonperturbative definition (discretized quantum mechanics)
- Defined for all N and g_{YM}
- Manifestly unitary

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- Obvious nonperturbative definition (discretized quantum mechanics)
- Defined for all N and g_{YM}
- Manifestly unitary
- 10D SUGRA at low temperature
- Dimensionful coupling, easy scale setting!
- Low T = strong coupling

BFSS Conjecture:
This theory \equiv M theory

IIA is in here too!

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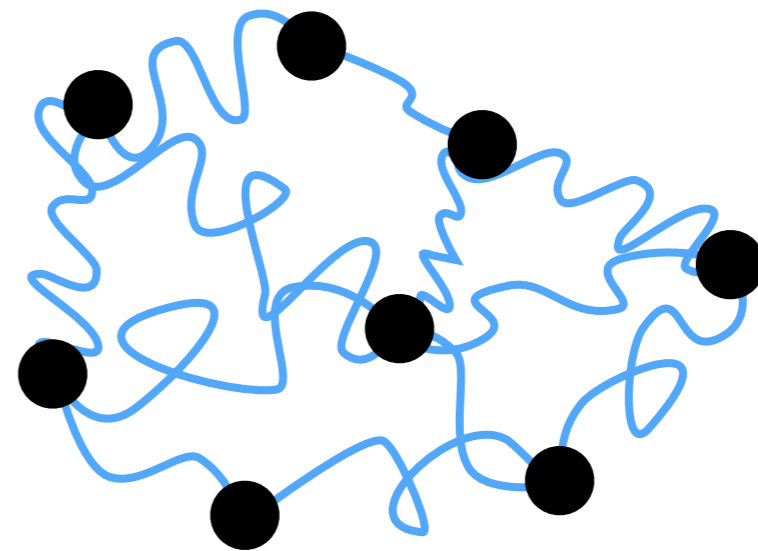
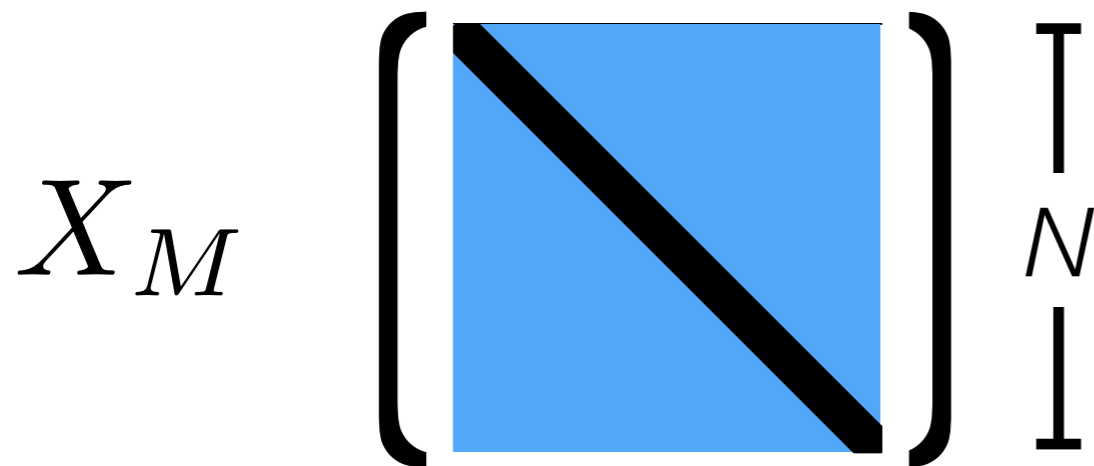
Quote everything in terms of
dimensionful coupling $\lambda = g_{YM}^2 N$
eg. T is actually $\lambda^{-1/3} T$

- 10D SUGRA at low temperature
- Dimensionful coupling, easy scale setting!
- Low T = strong coupling

BFSS Cartoon

Witten hep-th/9510135

$$L = \frac{1}{2g_{YM}^2} \text{Tr} \left\{ (D_t X_M)^2 + i\bar{\psi}^\alpha D_t \gamma_{\alpha\beta}^{10} \psi^\beta + \bar{\psi}^\alpha \gamma_{\alpha\beta}^M [X_M, \psi^\beta] + [X_M, X_{M'}]^2 \right\}$$



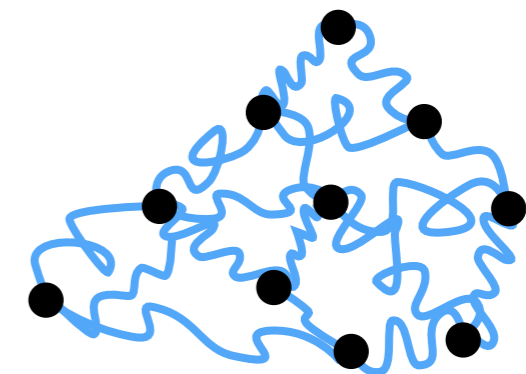
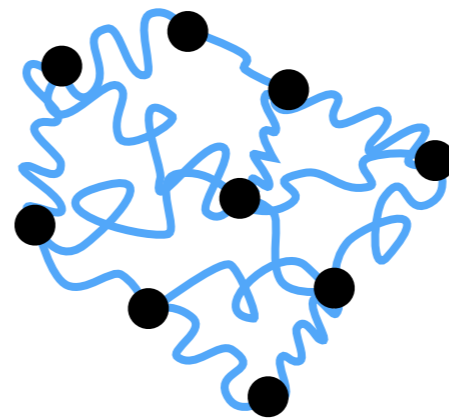
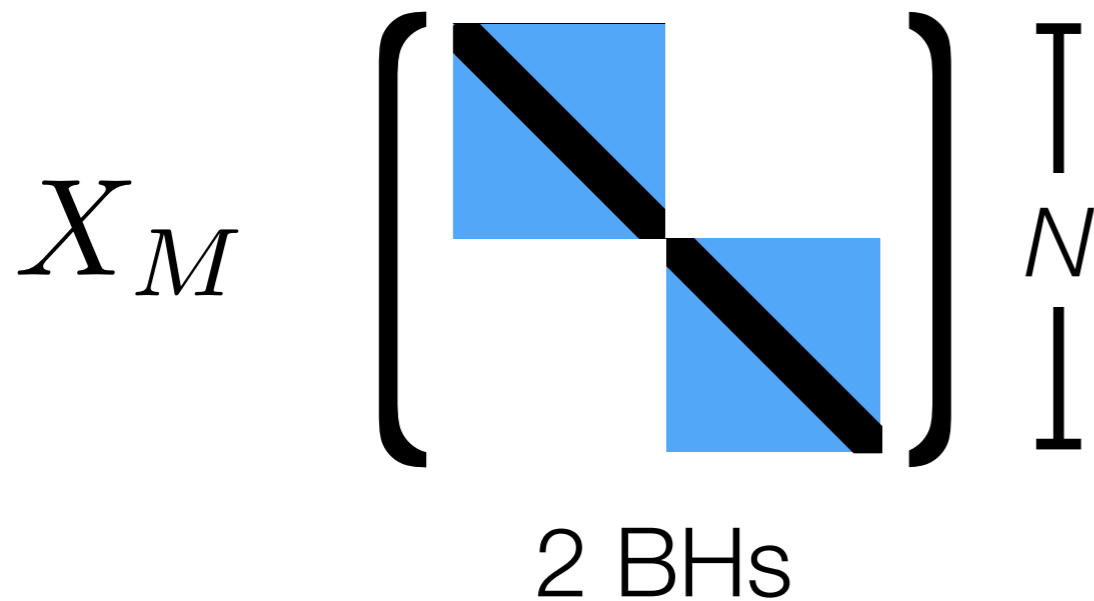
coordinates
couplings

One big bunch ~ black 0-brane ~ BH

BFSS Cartoon

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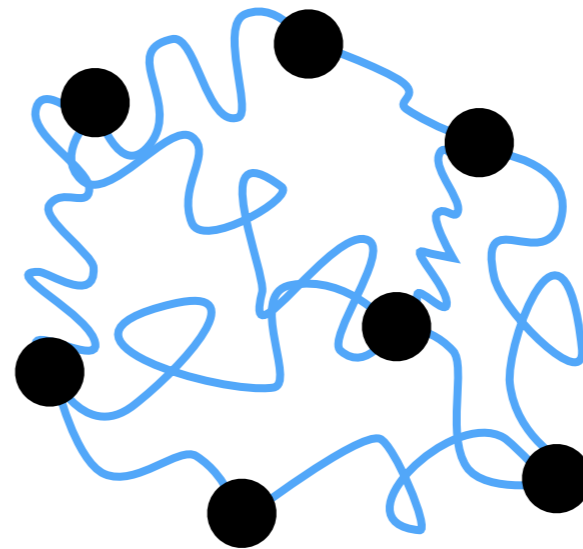
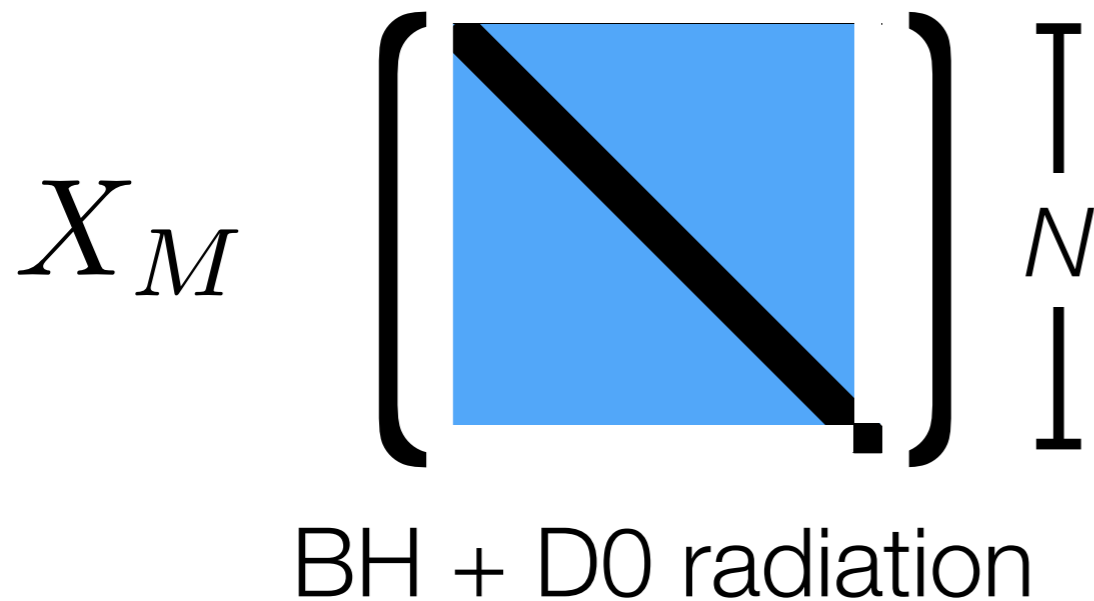


At large N BFSS is a 2nd quantized theory!

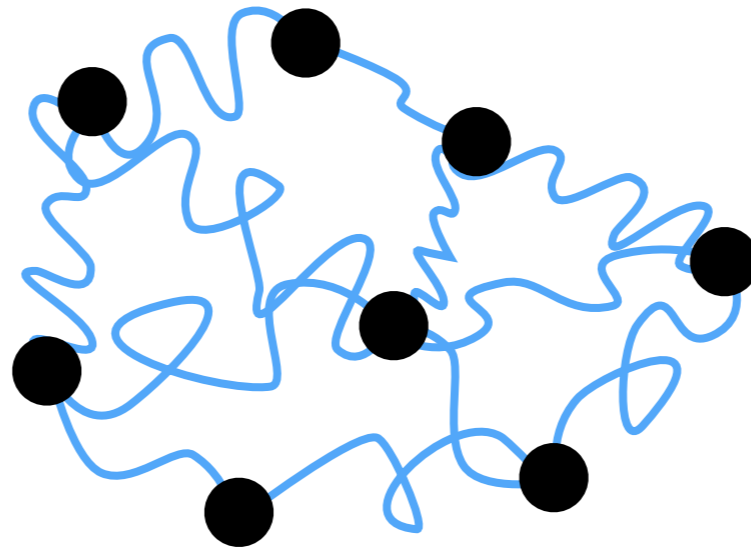
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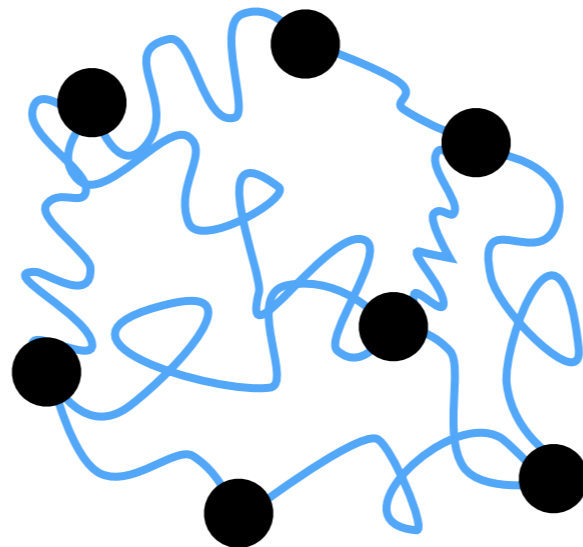
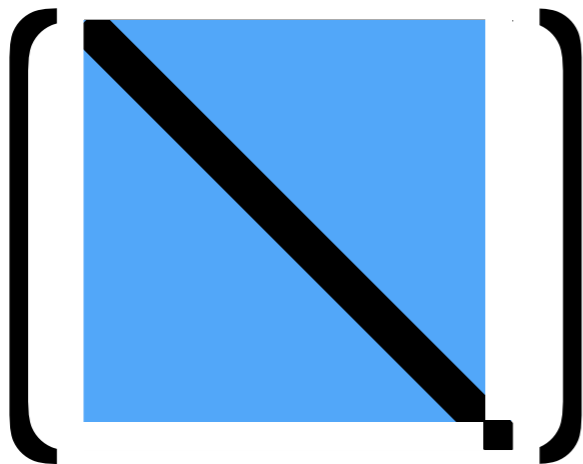
$$L = \frac{1}{2g_{YM}^2} \text{Tr} \left\{ (D_t X_M)^2 + i\bar{\psi}^\alpha D_t \gamma_{\alpha\beta}^{10} \psi^\beta + \bar{\psi}^\alpha \gamma_{\alpha\beta}^M [X_M, \psi^\beta] + [X_M, X_{M'}]^2 \right\}$$



Monte Carlo Study of Metastable State?



$$\text{DOF} \sim N^2$$
$$t_{\text{recurrence}} \sim e^{+N^2}$$



$$\tau \sim e^{+N}$$

$$\text{DOF} \sim (N-1)^2$$
$$+ \# \log(V)$$



Possible Observables

Almost certainly an incomplete list!

- Fast Scrambling arXiv:1512.00019 Gur-Ari, Hanada, Shenker $t_{\text{scramble}} \sim \log N$
- SUGRA 0707.4454 Anagnostopoulos et al.
0803.4273 Catterall+Wiseman
1503.08499 Kadoh, Kamata
1506.01366 Filev, O'Connor
- Finite N 0811.3102 Hanada, Hyakutake, Nishimura, Takeuchi
1311.5603 1603.00538 Hanada, Hyakutake, Ishiki, Nishimura
1606.04948 1606.04951 MCSMC
- Polyakov loop 0811.2081 Hanada, Miwa, Nishimura, Takeuchi
- 2-point functions 1108.5153 Hanada, Nishimura, Sekino, Yoneya, 2009, 2011
- Force 1709.01932 Rinaldi, Berkowitz, Hanada, Maltz, Vranas
- 'Ungauged' Theory 1802.00428 Maldacena, Milekhin
+ talks by Rinaldi (1802.02985) and Buividovich (1711.05556-like?)

Test: BH Internal Energy

$$E/N^2 = \frac{(a_0 T^{2.8} + a_1 T^{4.6} + a_2 T^{5.8} + \dots)}{N^0} + \frac{(b_0 T^{0.4} + b_1 T^{2.2} + \dots)}{N^2} + \mathcal{O}\left(\frac{1}{N^4}\right)$$

$$\underbrace{\hspace{15em}}_{\frac{E_0(T)}{N^0}} + \underbrace{\hspace{15em}}_{\frac{E_1(T)}{N^2}} + \dots$$

Expand in $\frac{\alpha'}{R_{BH}^2} \sim T^{3/5}$

$$a_0 = 7.41$$

hep-th/980242 Itzhaki, Maldacena, Sonnenschein, Yankielowicz

$$b_0 = -5.77$$

1311.7526 Hyakutake

(α') ^{1, 2, and 4} terms vanish

Gross + Witten, Nucl Phys B 277:1 1986

Gross + Sloan, Nucl Phys B291:41-89, 1987

Grisaru, van de Ven, + Zanon PLB 173:423-428, 1986

Green + Vanhove PRD61:104011, 2000

Green, Russo + Vanhove JHEP 02:099, 2007

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$$\underbrace{\hspace{15em}}_{\frac{E_0(T)}{N^0}} + \underbrace{\hspace{15em}}_{\frac{E_1(T)}{N^2}} + \dots$$

't Hooft counting still valid, even in discretized theory

Expand in $\frac{\alpha'}{R_{BH}^2} \sim T^{3/5}$

$(\alpha')^1, 2, \text{ and } 4$ terms vanish

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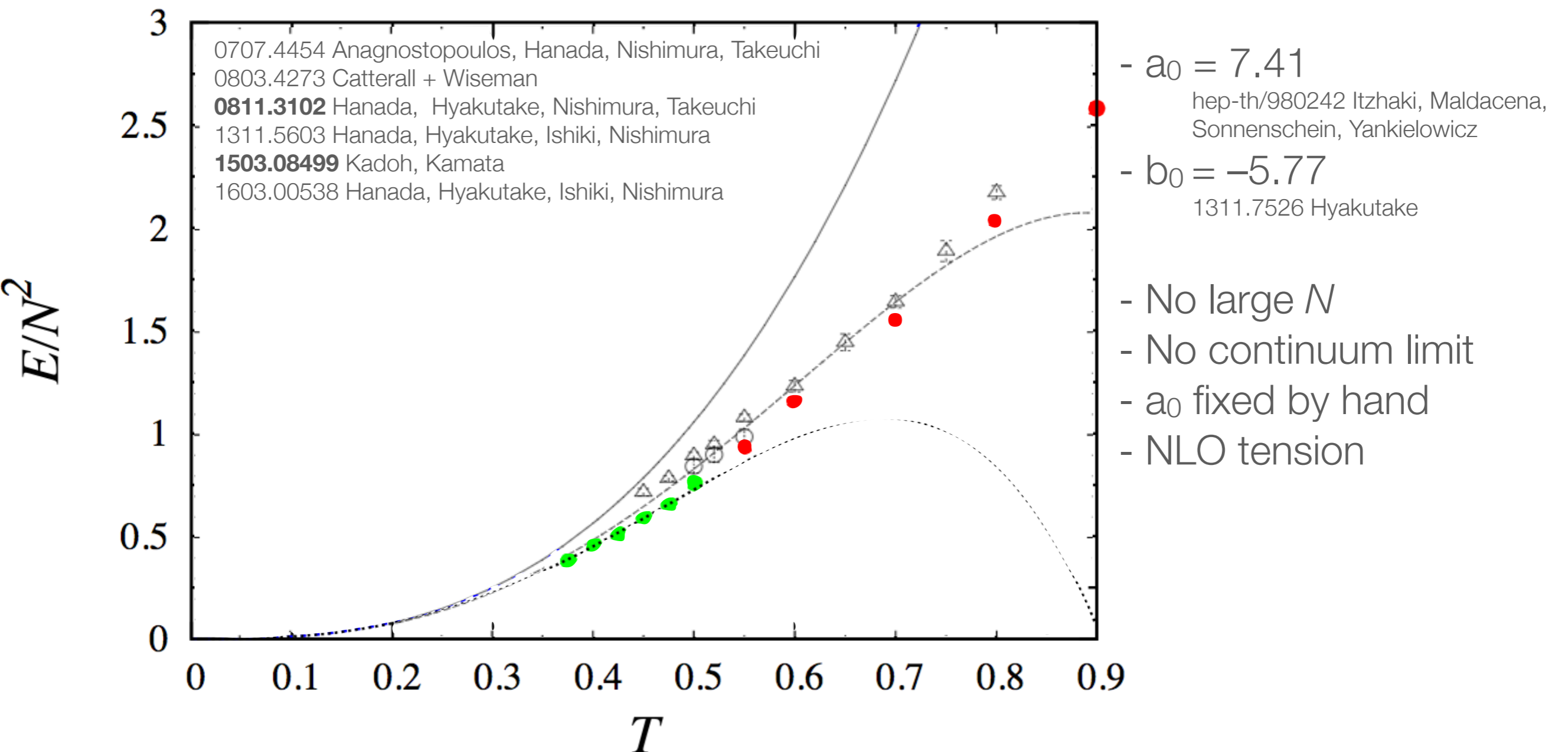
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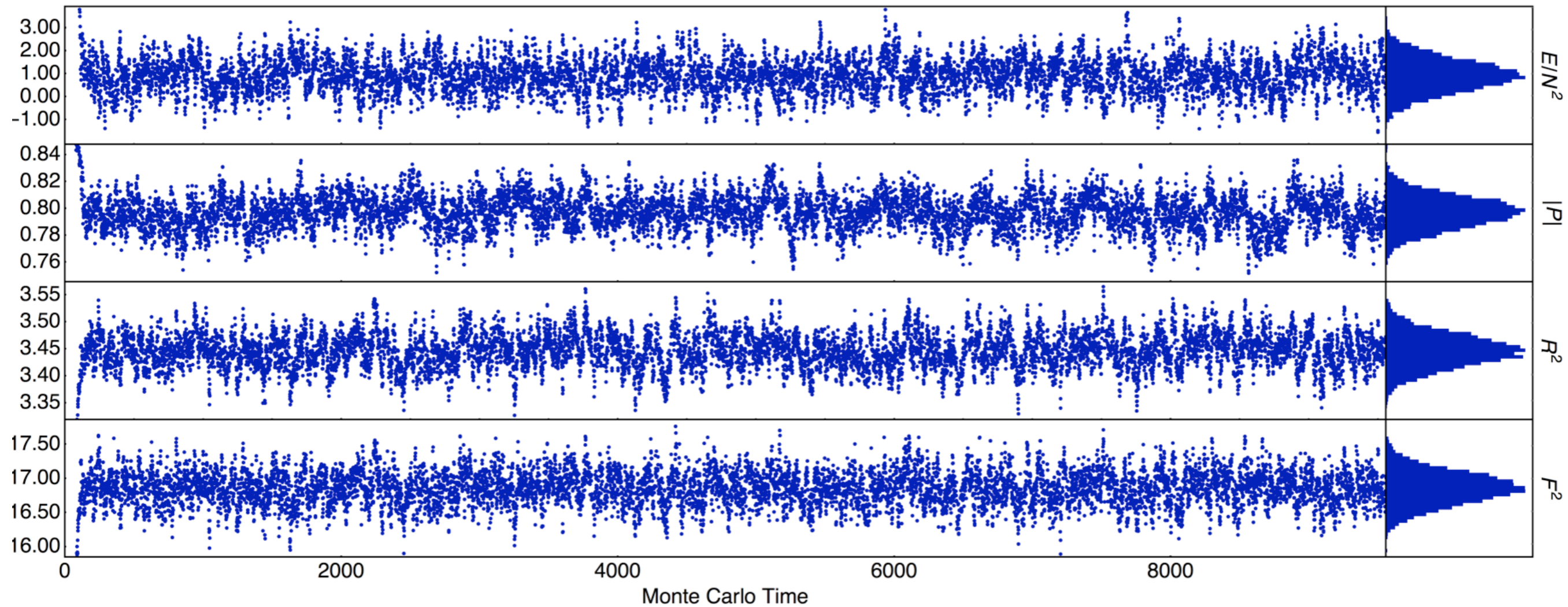
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Example Monte Carlo History

MCSMC 1606.04948 1606.04951

$T=0.5$ $N=24$ $L=32$

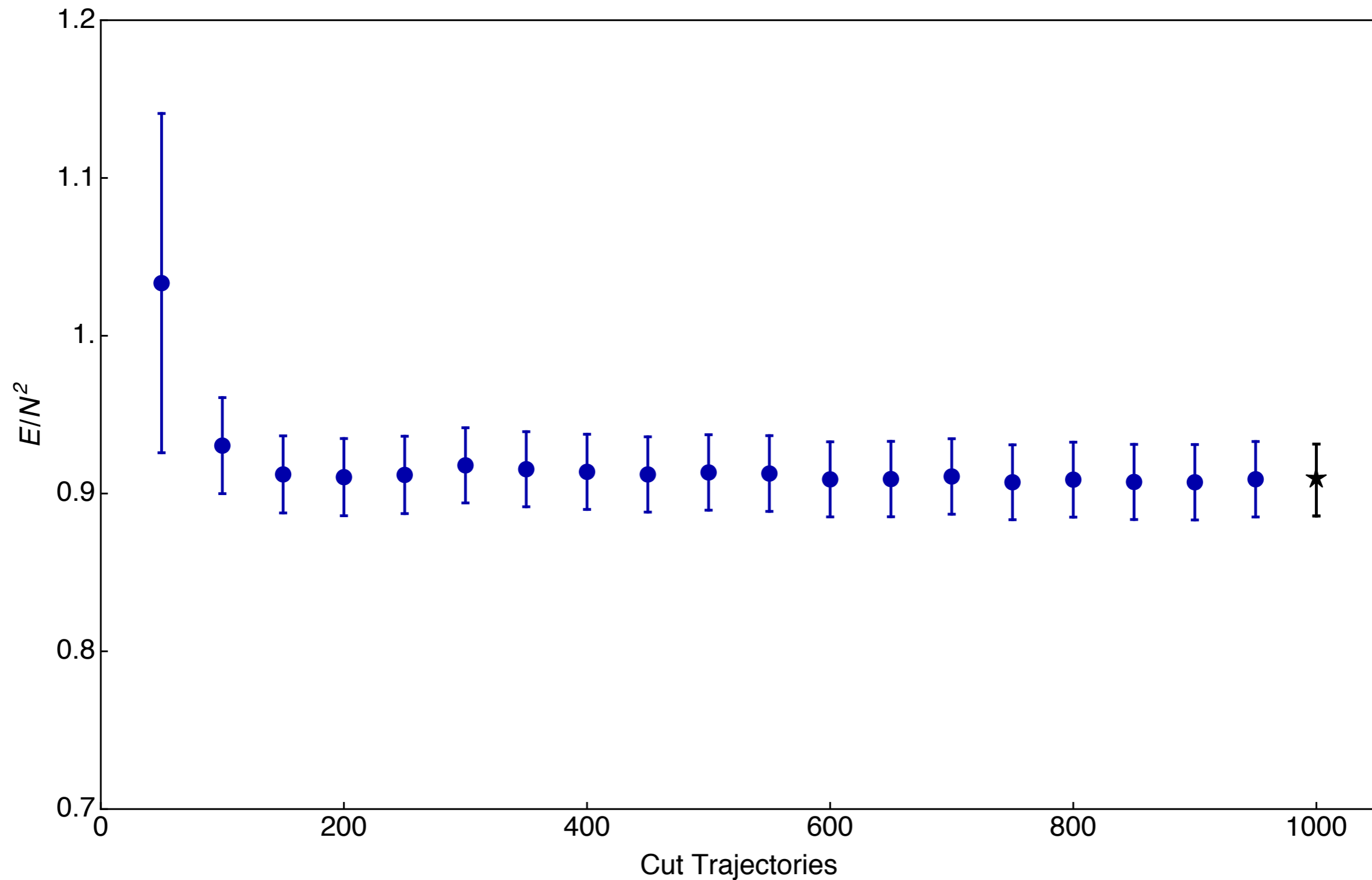


Long correlations can be seen in each observable.

Thermalization Cut

MCSMC 1606.04948 1606.04951

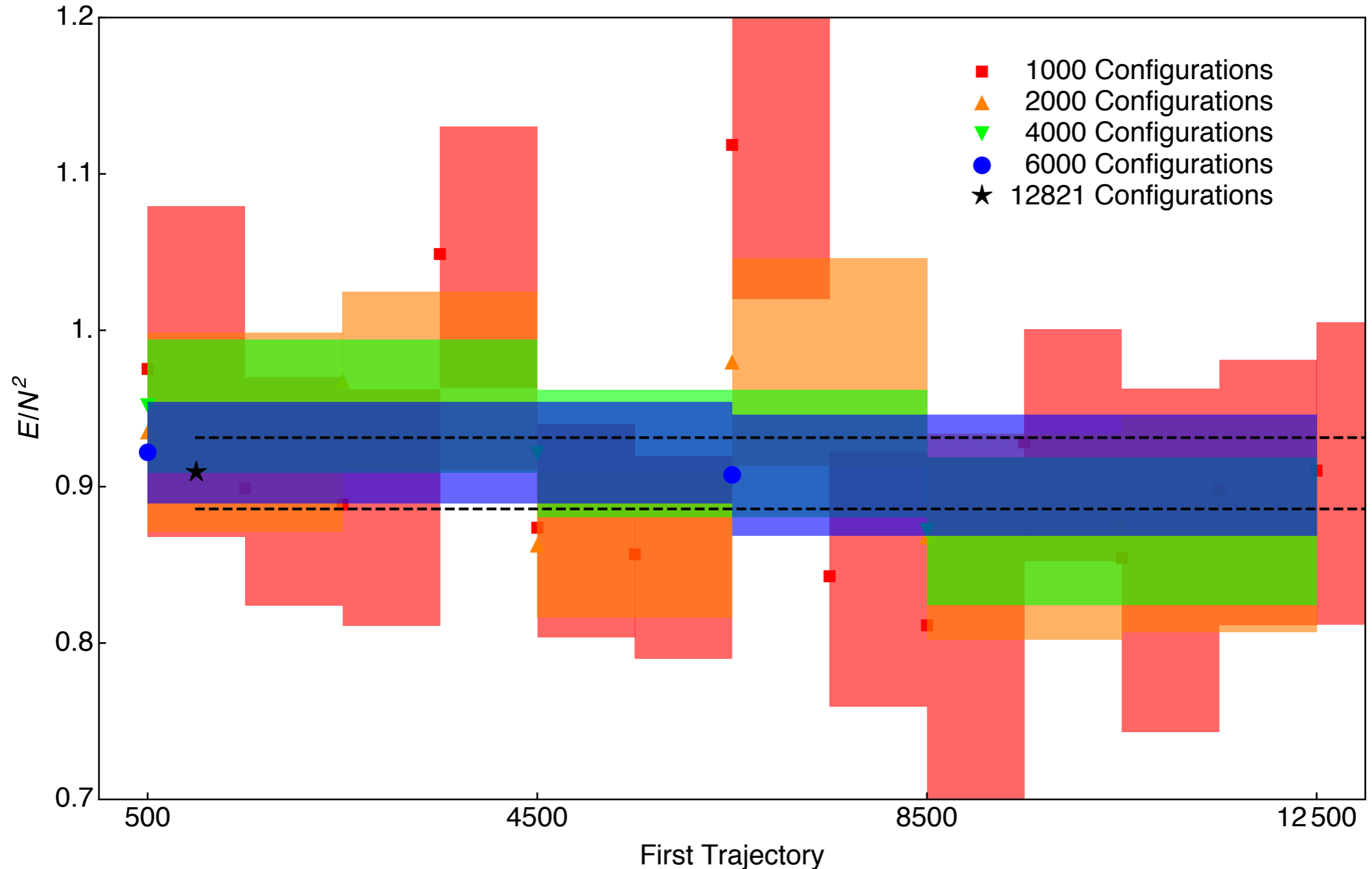
$T=0.5$ $N=16$ $L=32$



Statistical Stability

MCSMC 1606.04948 1606.04951

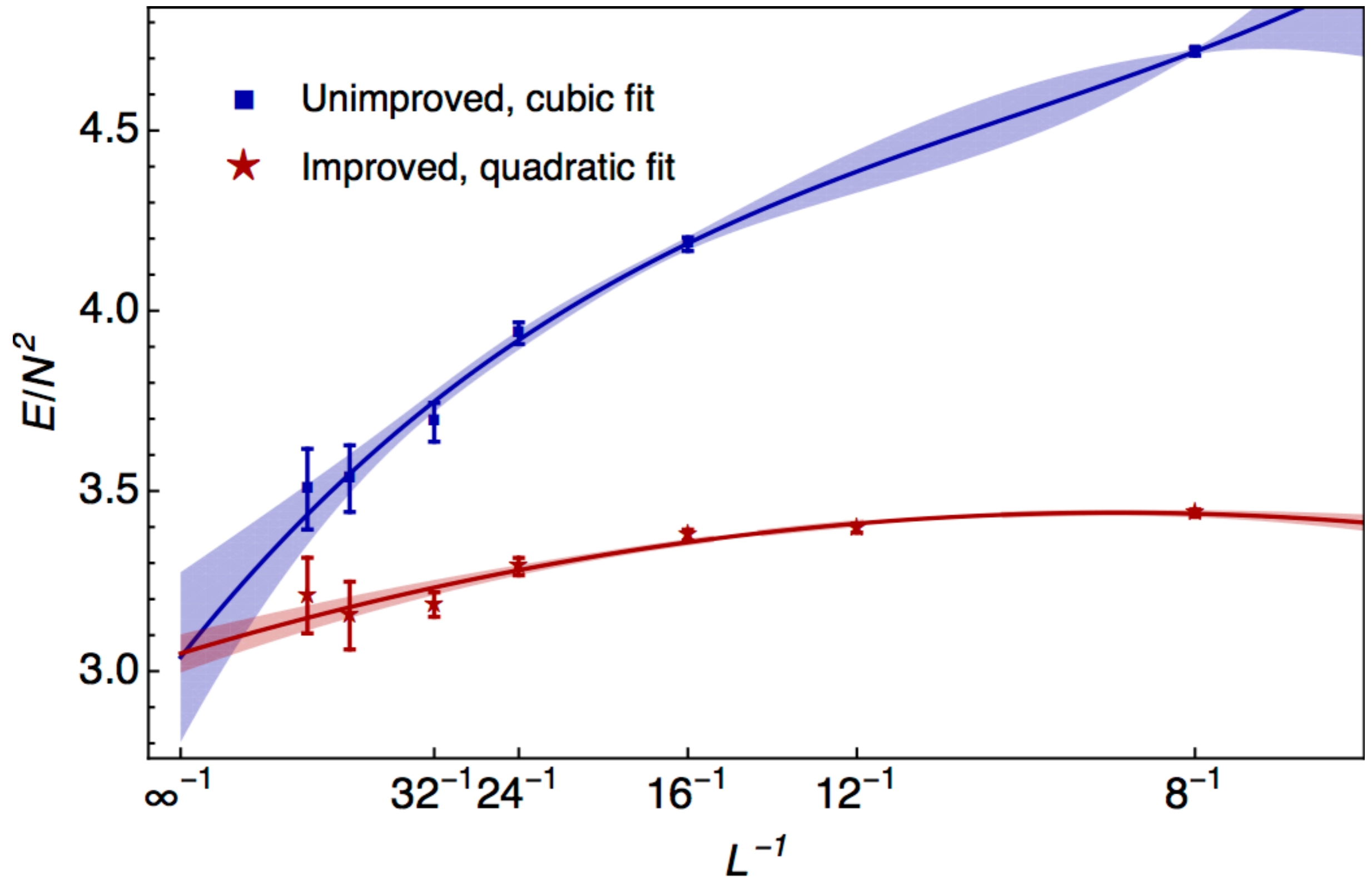
$T=0.5$ $N=16$ $L=32$



Compute!



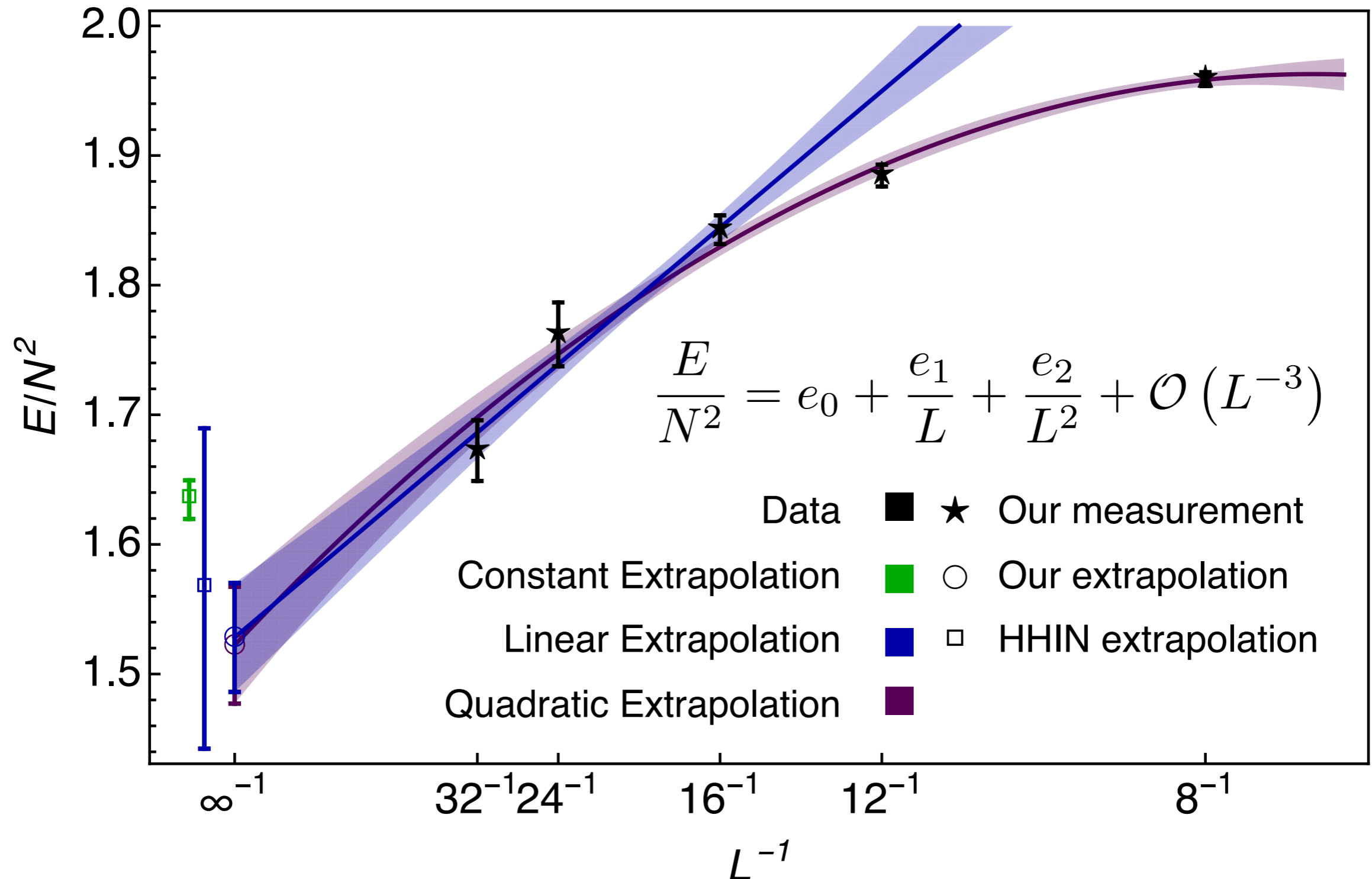
Derivative Improvement



Fixed- N Continuum Extrapolation

MCSMC 1606.04948 1606.04951

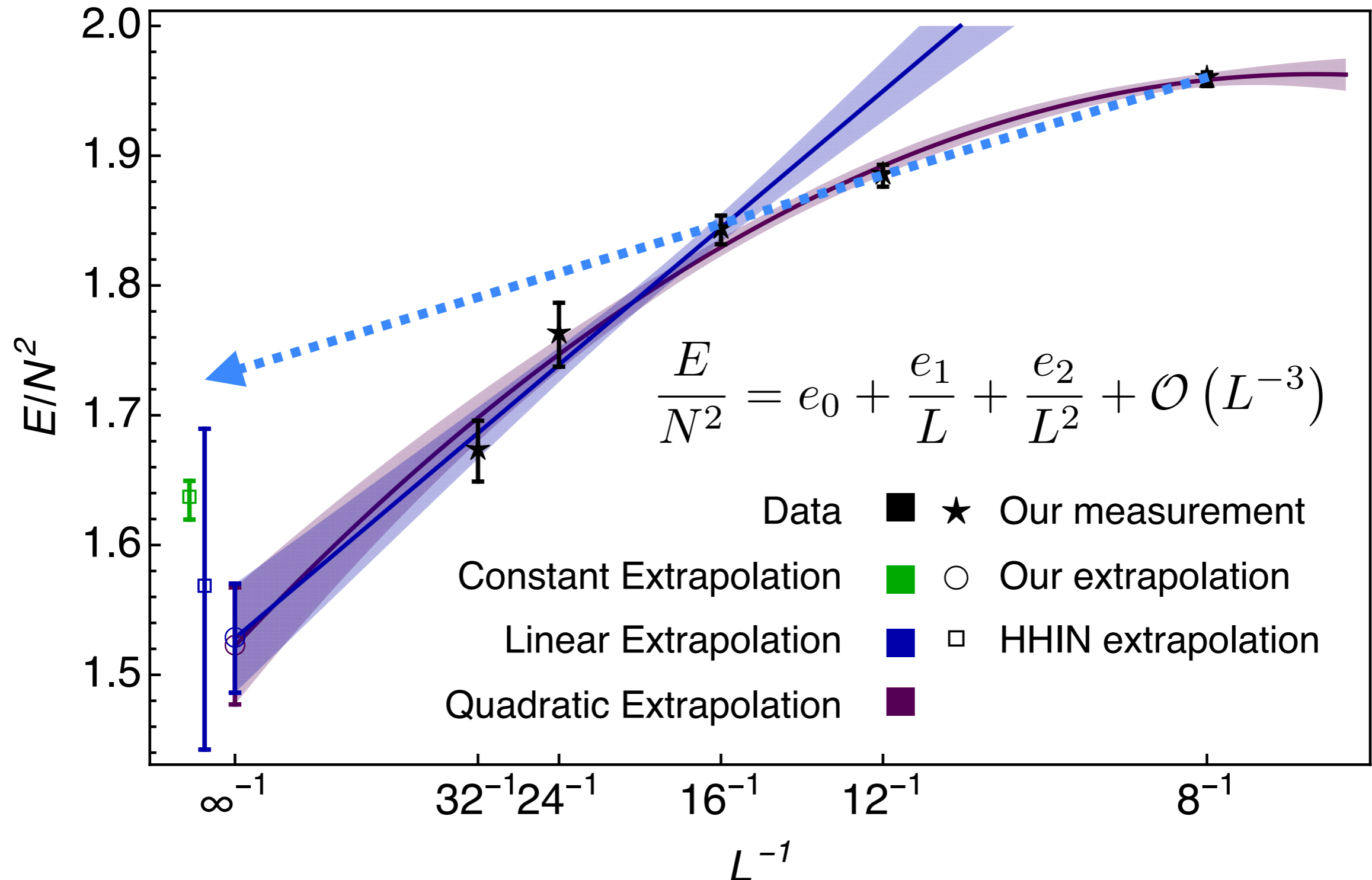
$T=0.7$ $N=16$



Fixed- N Continuum Extrapolation

MCSMC 1606.04948 1606.04951

$T=0.7$ $N=16$



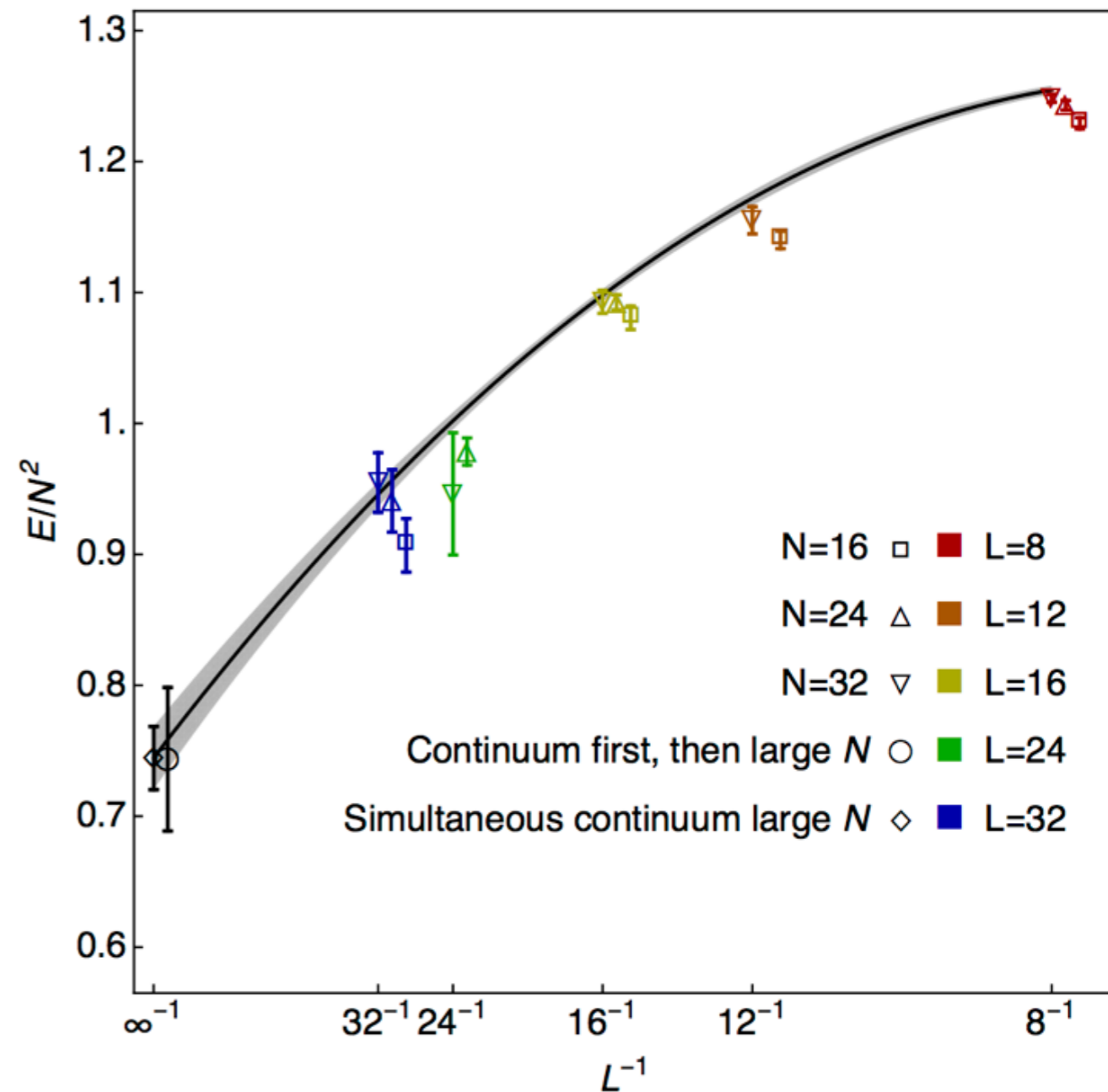
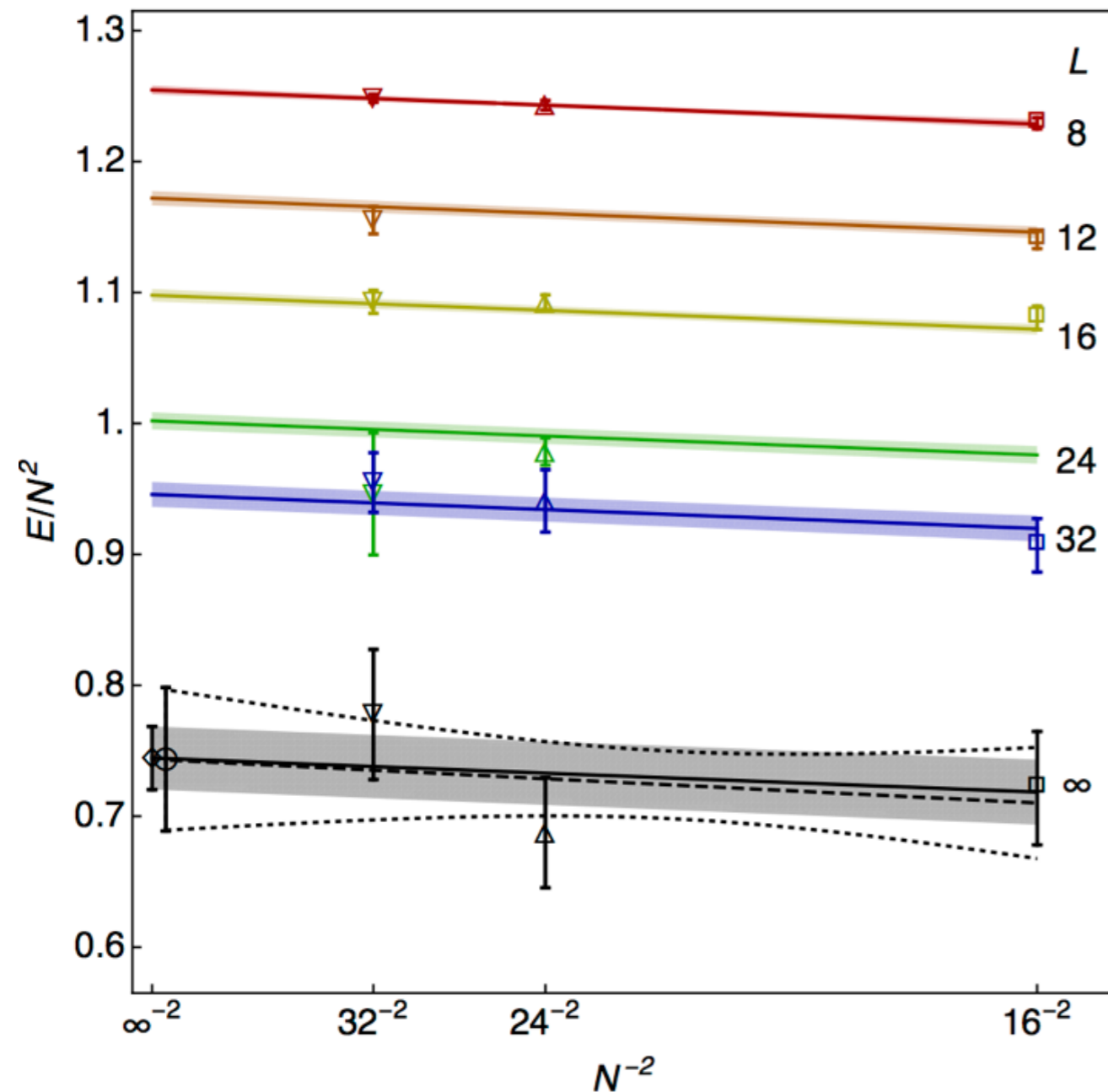
Simultaneous Continuum + Large- N Extrapolation

MCSMC 1606.04948 1606.04951

$$\frac{E}{N^2} = \sum_{ij \geq 0} \frac{e_{ij}}{N^{2i} L^j}$$

$e_{00}, e_{01}, e_{02}, e_{10}$

$T=0.5$



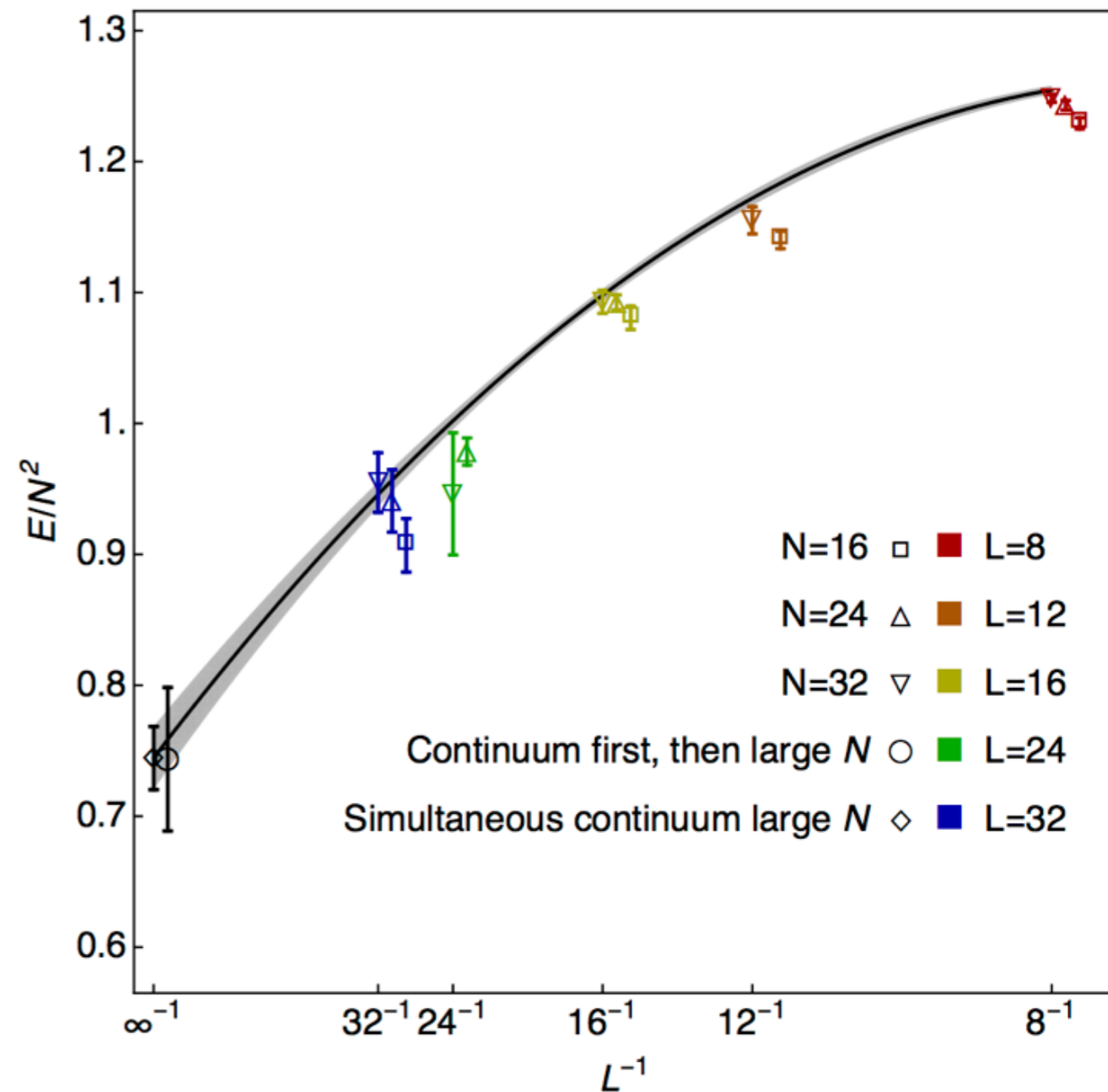
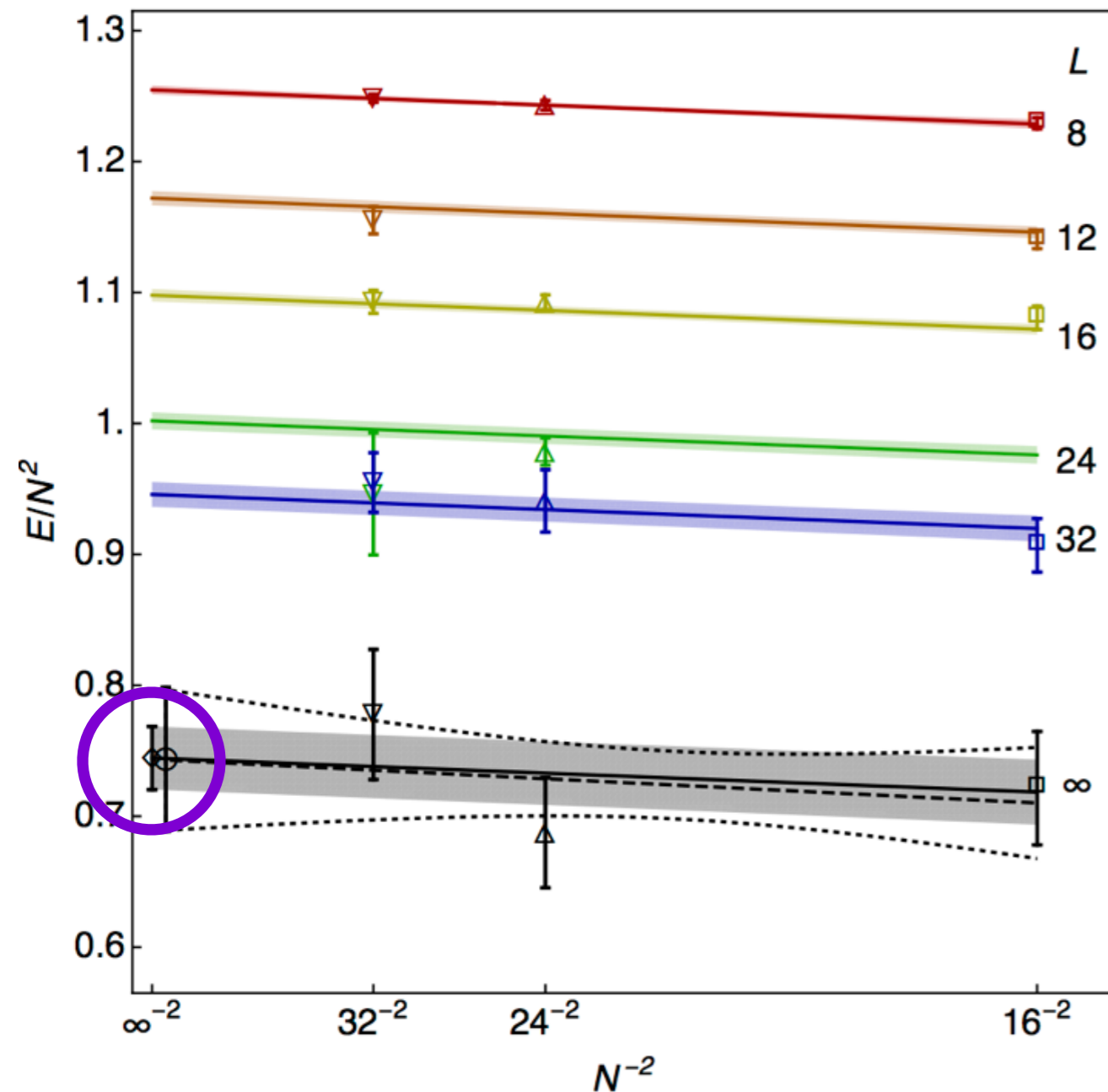
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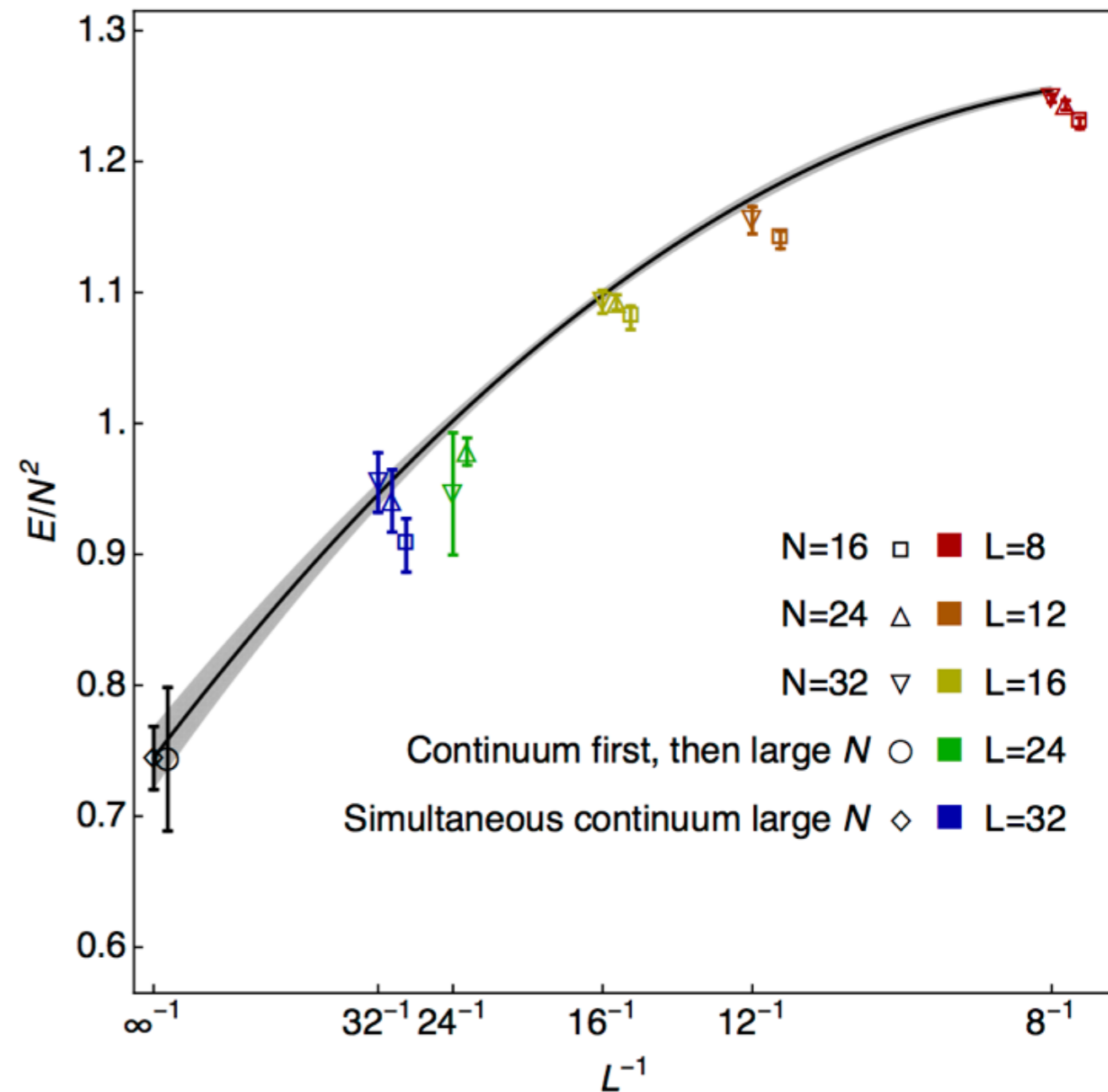
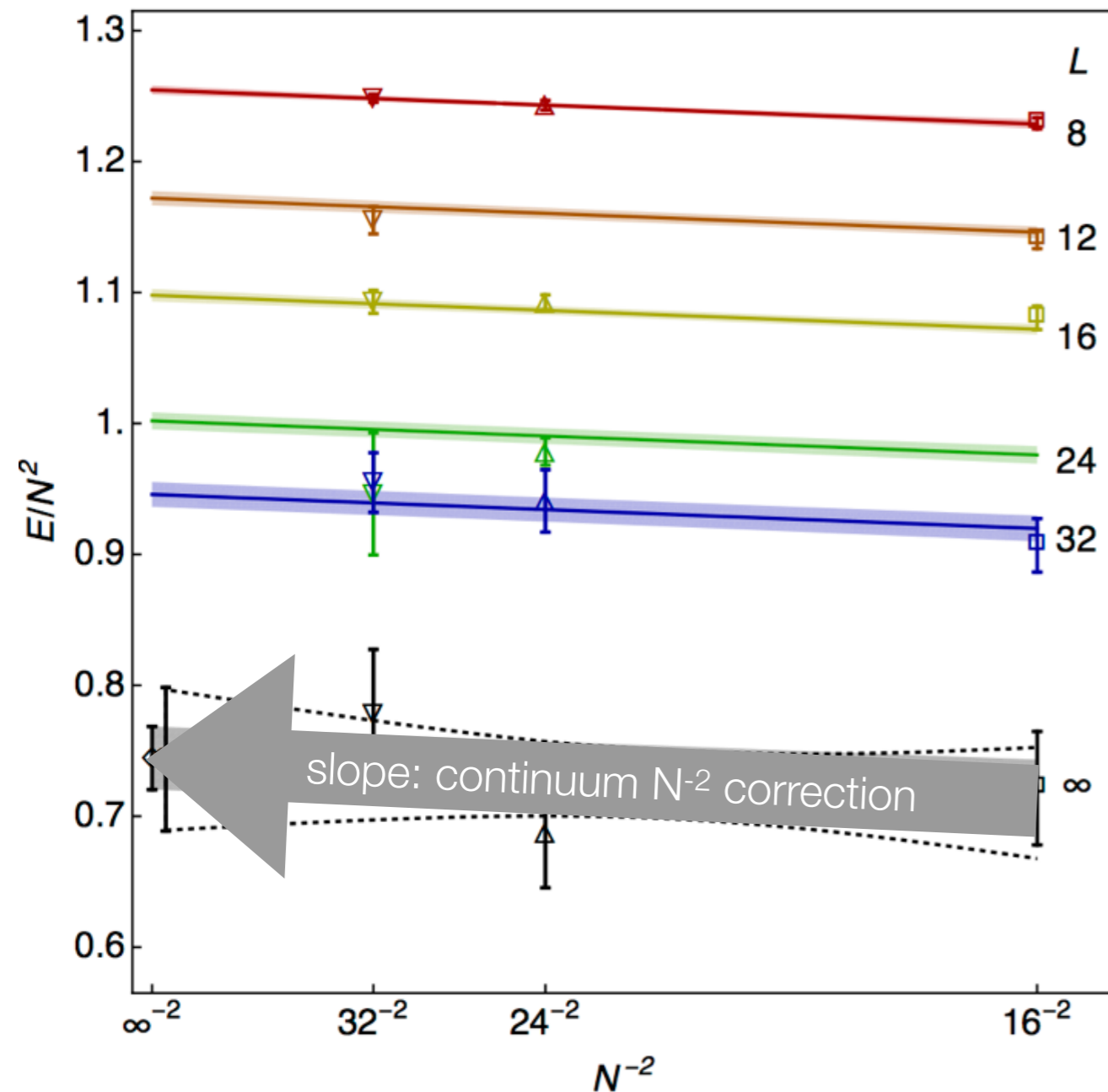
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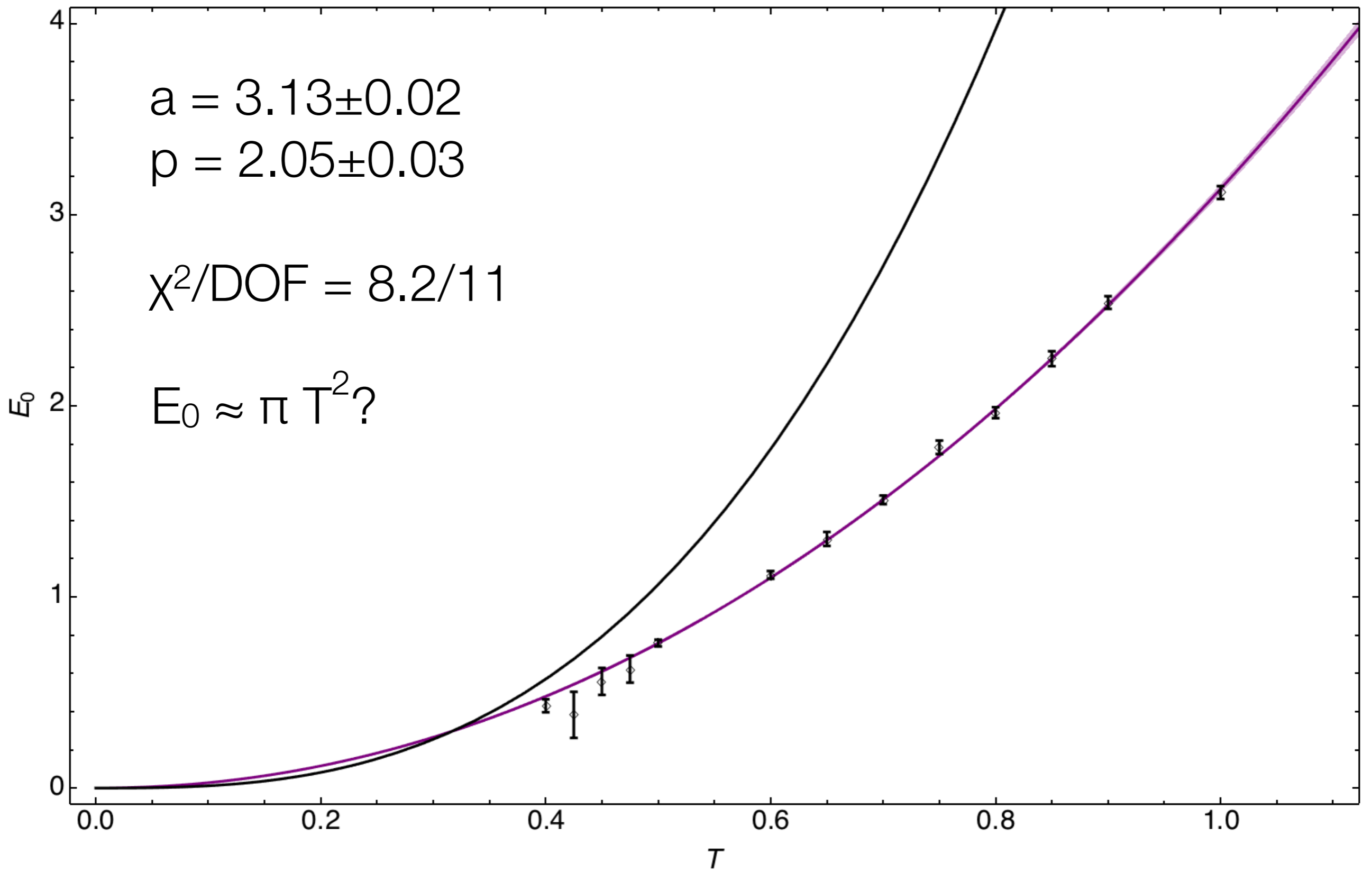
No stringy input: $a T^p$?

$$a = 3.13 \pm 0.02$$

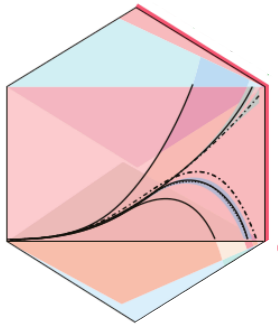
$$p = 2.05 \pm 0.03$$

$$\chi^2/\text{DOF} = 8.2/11$$

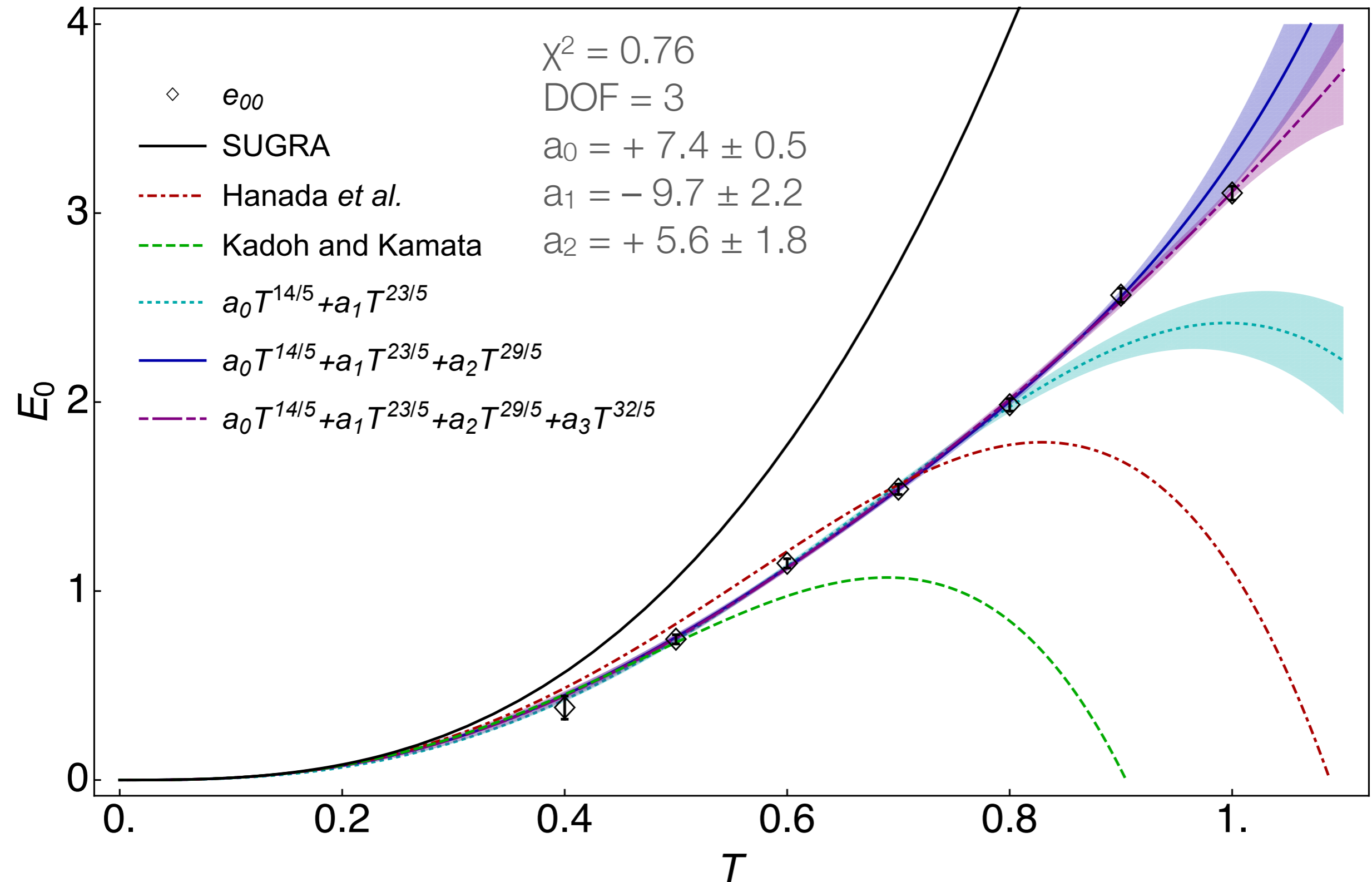
$$E_0 \approx \pi T^2 ?$$



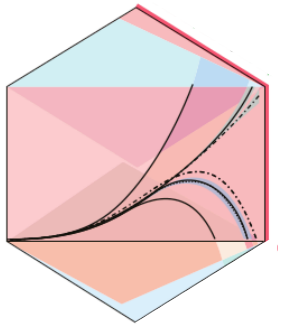
$$E/N^2 = N^0 (a_0 T^{2.8} + a_1 T^{4.6} + a_2 T^{5.8} + \dots) + \mathcal{O}(N^{-2})$$



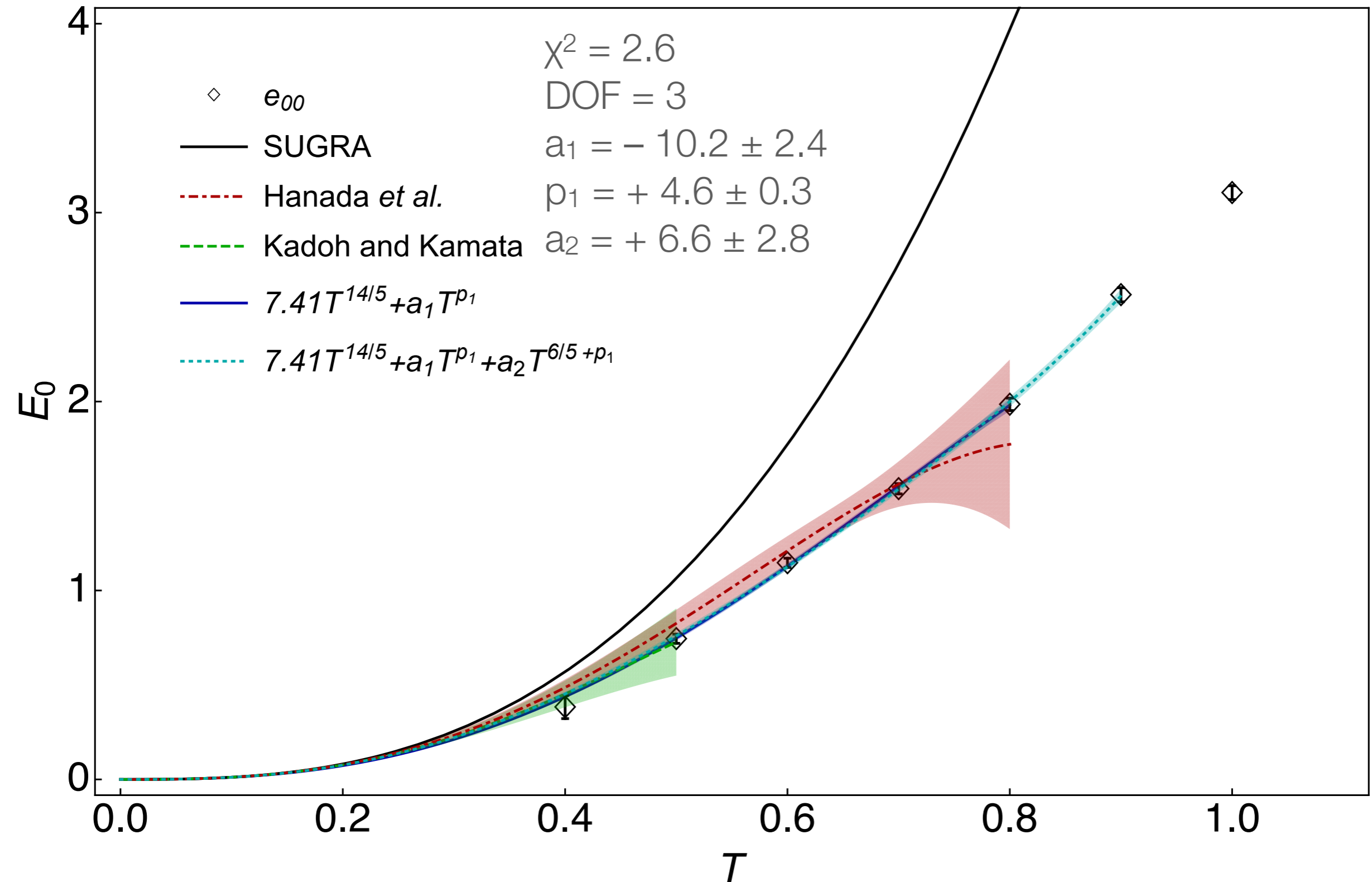
MCSMC 1606.04948 1606.04951



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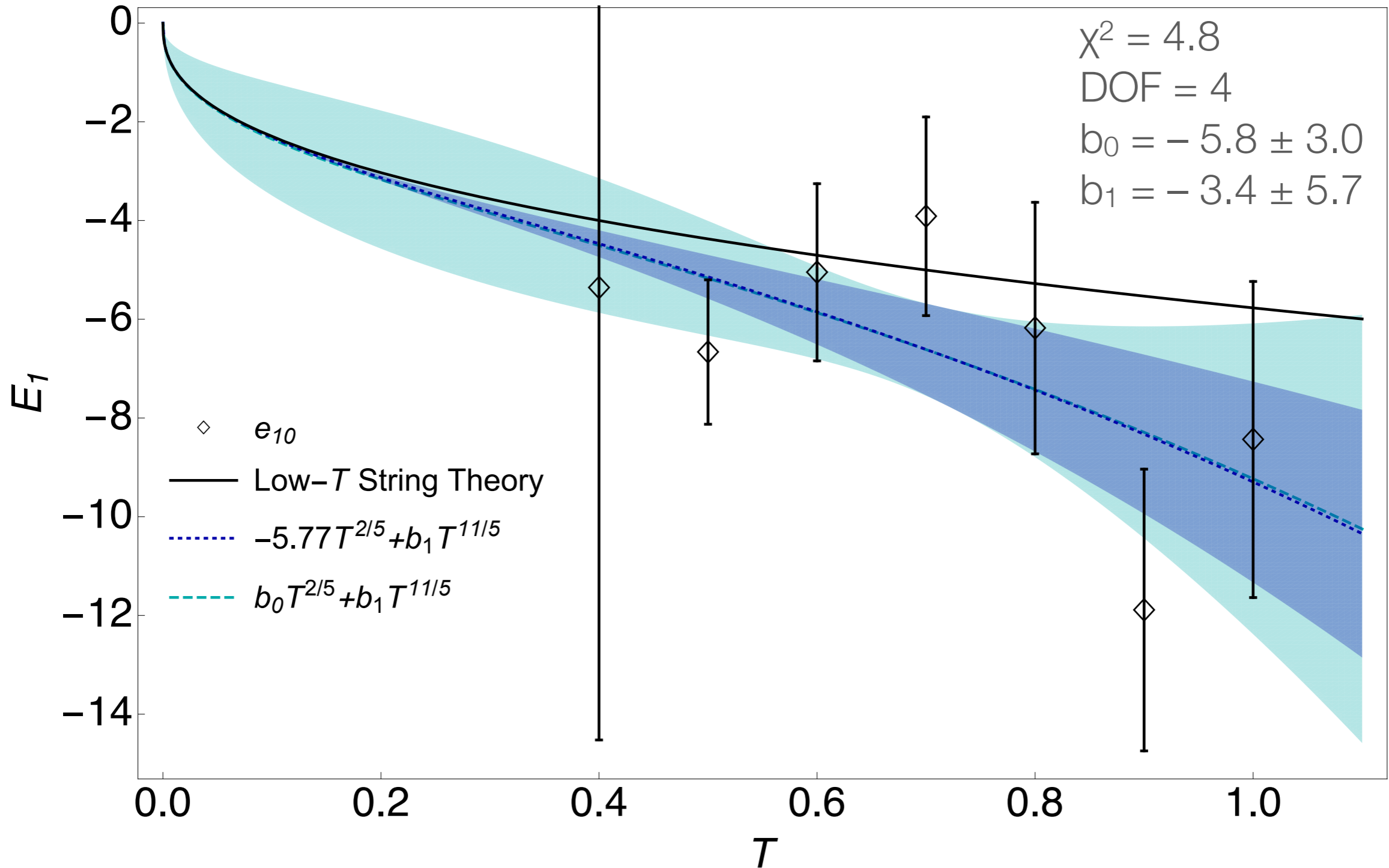
MCSMC 1606.04948 1606.04951



$$\mathcal{O}(N^{-2}) = N^{-2} (b_0 T^{0.4} + b_1 T^{2.2} + \dots)$$

← slope: continuum N^{-2} correction

MCSMC 1606.04948 1606.04951



Summary

Quantum Gravity



Gauge Theory

- 0+1D BFSS reproduces known 10D SUGRA result
- Nontrivial checks of gauge / gravity duality
- Predictions about (quantum!) stringy corrections.

Backup Slides

Phase Quench

