

Probing D0-brane Black Holes

Evan Berkowitz
MCSMC: Monte Carlo String + M-Theory Collaboration
Forschungszentrum Jülich

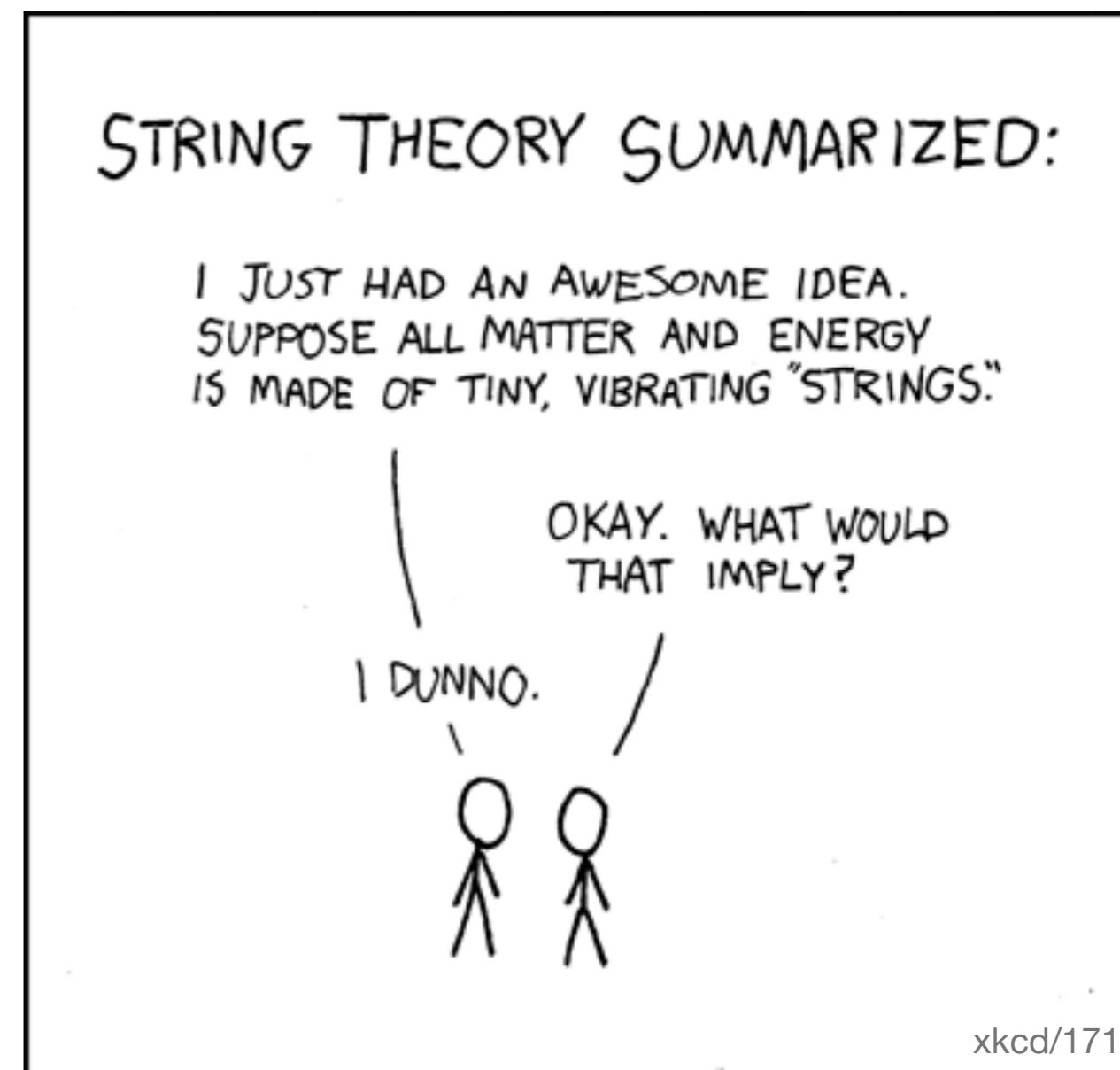
Quantum Gravity meets Lattice QFT
2018-09-03
ECT*

1606.04948 1606.04951 EB, Enrico Rinaldi, Masanori Hanada, Pavlos Vranas,
Goro Ishiki, Shinji Shimasaki
1709.01932 Rinaldi, EB, Hanada, Maltz, and Vranas
+ forthcoming work

Parts of this work were performed under the auspices of the U.S. Department of Energy
by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344

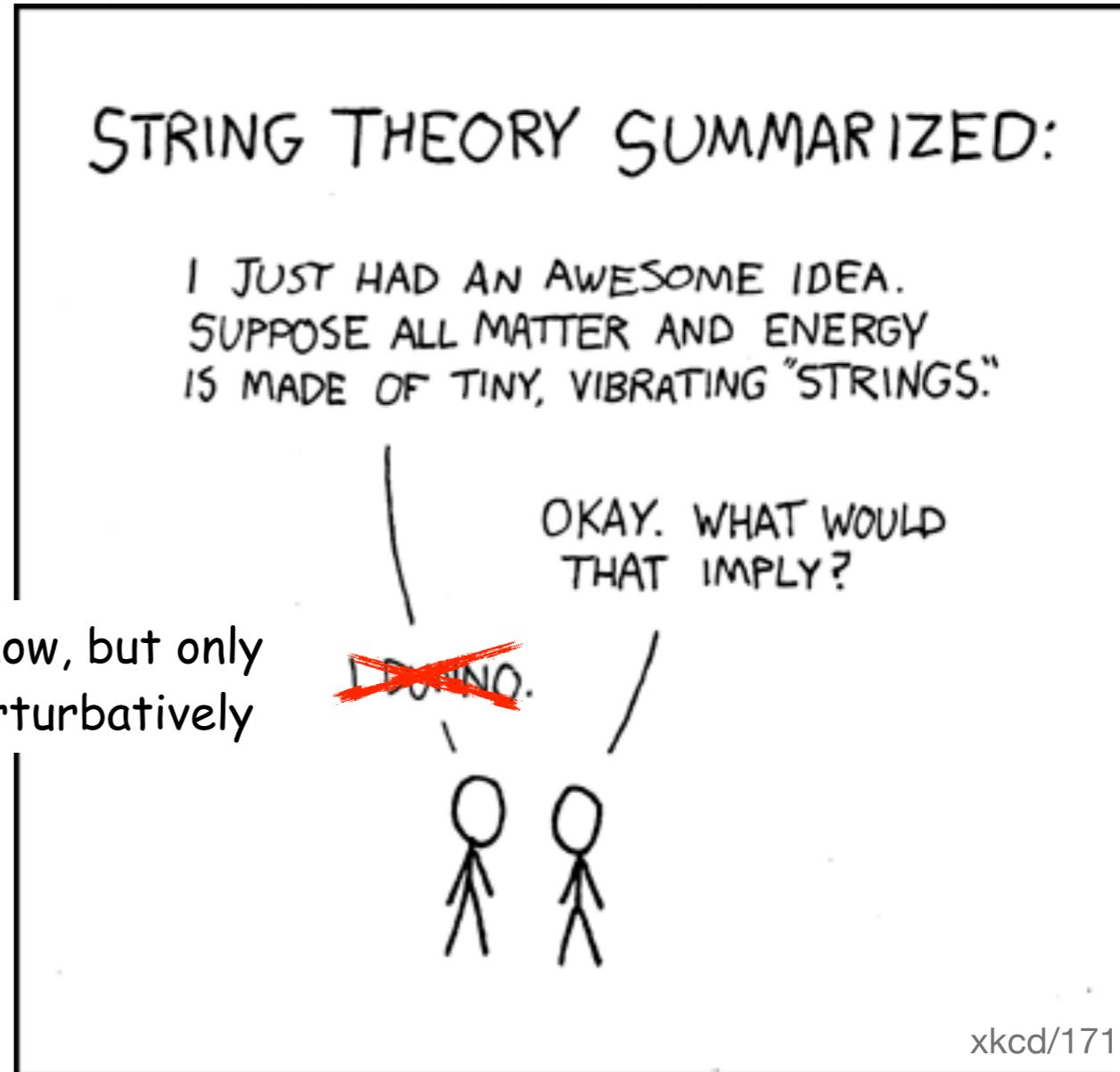
Outline

- Gauge/Gravity Duality & Motivation
- The BFSS / DO Matrix Model
- Monte Carlo, Fitting
- Tests of Holography
- Probes of Geometry



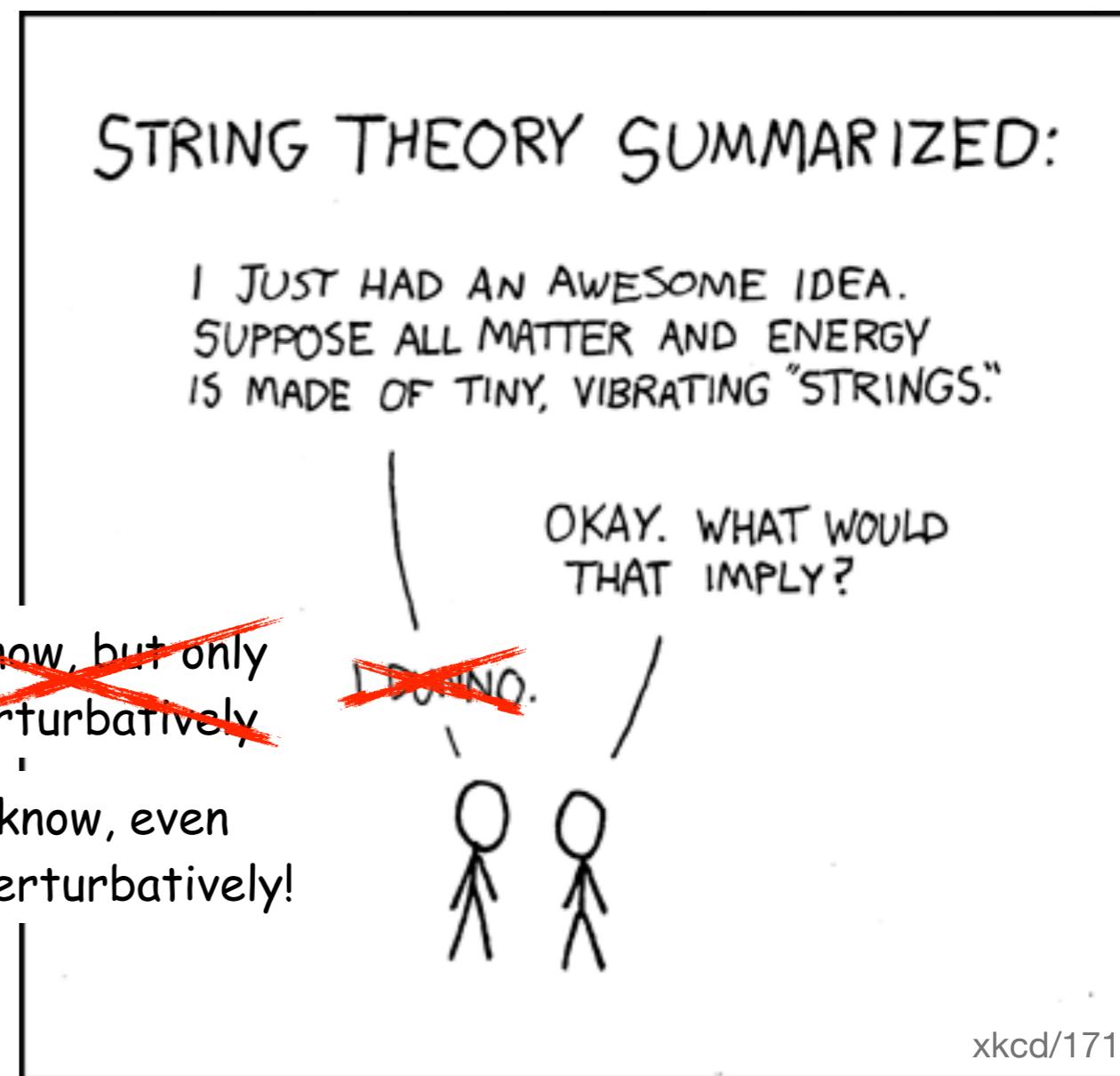
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Do you have the quantum data?

Interstellar

QUANTUM OF SOLACE

A full-body photograph of James Bond (Daniel Craig) standing in a desert landscape. He is wearing a dark suit, white shirt, and blue tie, and is holding a black rifle. The background is a vast, sandy desert under a clear sky.

7F™



COLUMBIA
PICTURES

QUANTUM OF SOLACE - 007 - SCREEN RESOLUTION 1280X1024 WIDESCREEN - THE ORIGINAL PICTURE BELONGS TO COLUMBIA & MGM™ PICTURE - MADE (FAN ART) BY ANTIROBOTIC

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0+1 D0 Brane QM / BFSS Matrix Model

Banks Fischler Shenker Susskind hep-th/9610043

$$L = \frac{1}{2g_{YM}^2} \text{Tr} \left\{ (D_t X_M)^2 + i\bar{\psi}^\alpha D_t \gamma_{\alpha\beta}^{10} \psi^\beta + \bar{\psi}^\alpha \gamma_{\alpha\beta}^M [X_M, \psi^\beta] + [X_M, X_{M'}]^2 \right\}$$

Yukawa Self-interaction

$$D_t \cdot = \partial_t \cdot - i[A_t, \cdot]$$

γ^M left-handed part of 9+1D γs

X_M 9 bosonic

ψ^α 16 fermionic

$N \times N$ matrices

- Obvious nonperturbative definition (discretized quantum mechanics)
 - Defined for all N and g_{YM}
 - Manifestly unitary

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BFSS Conjecture

BFSS Conjecture: This theory \equiv M theory

- 10D SUGRA at low temperature
 - Dimensionful coupling, easy scale setting!
 - Low T = strong coupling

IIA is in here too!

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- Defined for all N and g_{YM}

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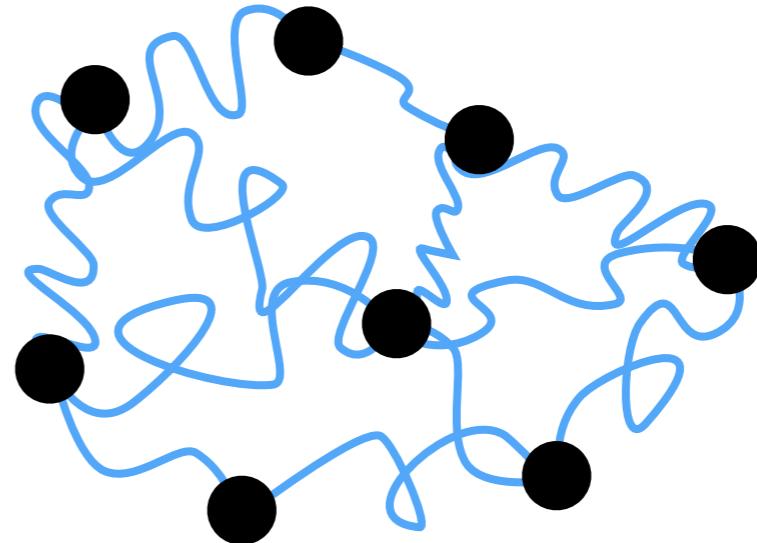
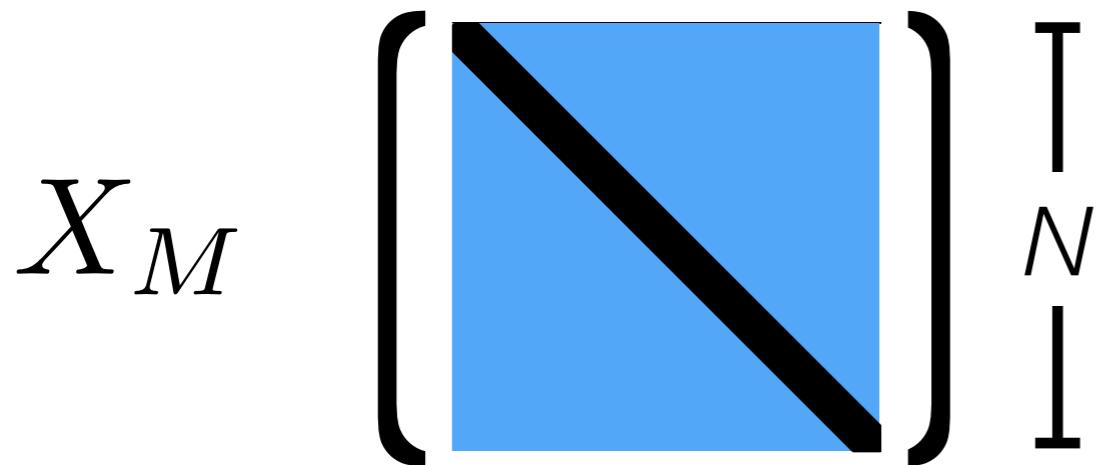
- Low T = strong coupling

Quote everything in terms of
dimensionful coupling $\lambda = g_{YM}^2 N$
eg. T is actually $\lambda^{-1/3} T$

BFSS Cartoon

Witten hep-th/9510135

$$L = \frac{1}{2g_{YM}^2} \text{Tr} \left\{ (D_t X_M)^2 + i\bar{\psi}^\alpha D_t \gamma_{\alpha\beta}^{10} \psi^\beta + \bar{\psi}^\alpha \gamma_{\alpha\beta}^M [X_M, \psi^\beta] + [X_M, X_{M'}]^2 \right\}$$



coordinates
couplings

One big bunch ~ black 0-brane ~ BH

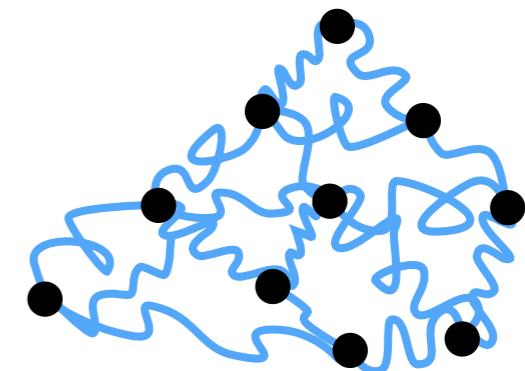
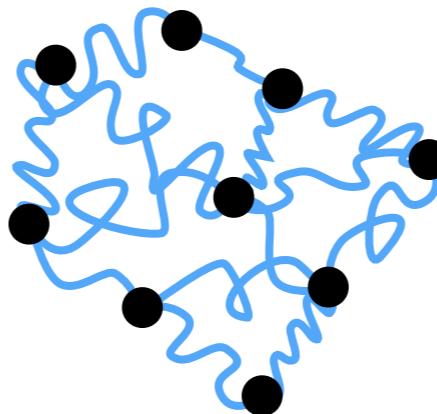
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$$X_M \begin{pmatrix} & \\ & \end{pmatrix} \begin{matrix} T \\ N \\ I \end{matrix}$$

2 BHs

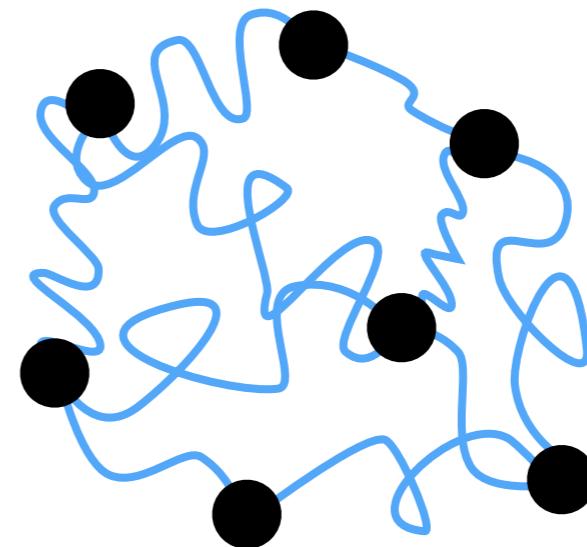
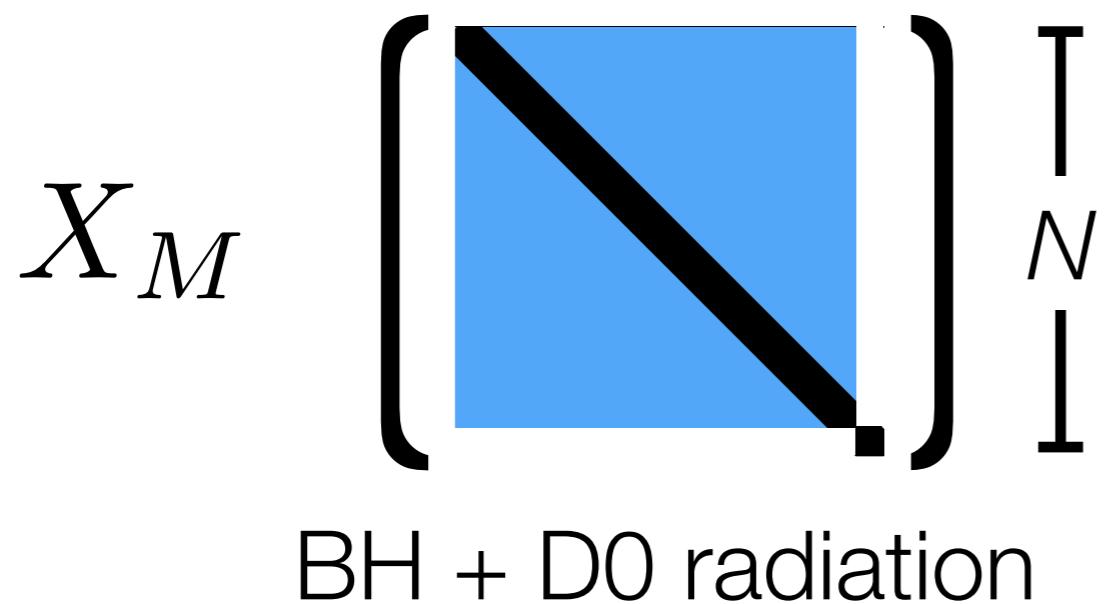


At large N BFSS is a 2nd quantized theory!

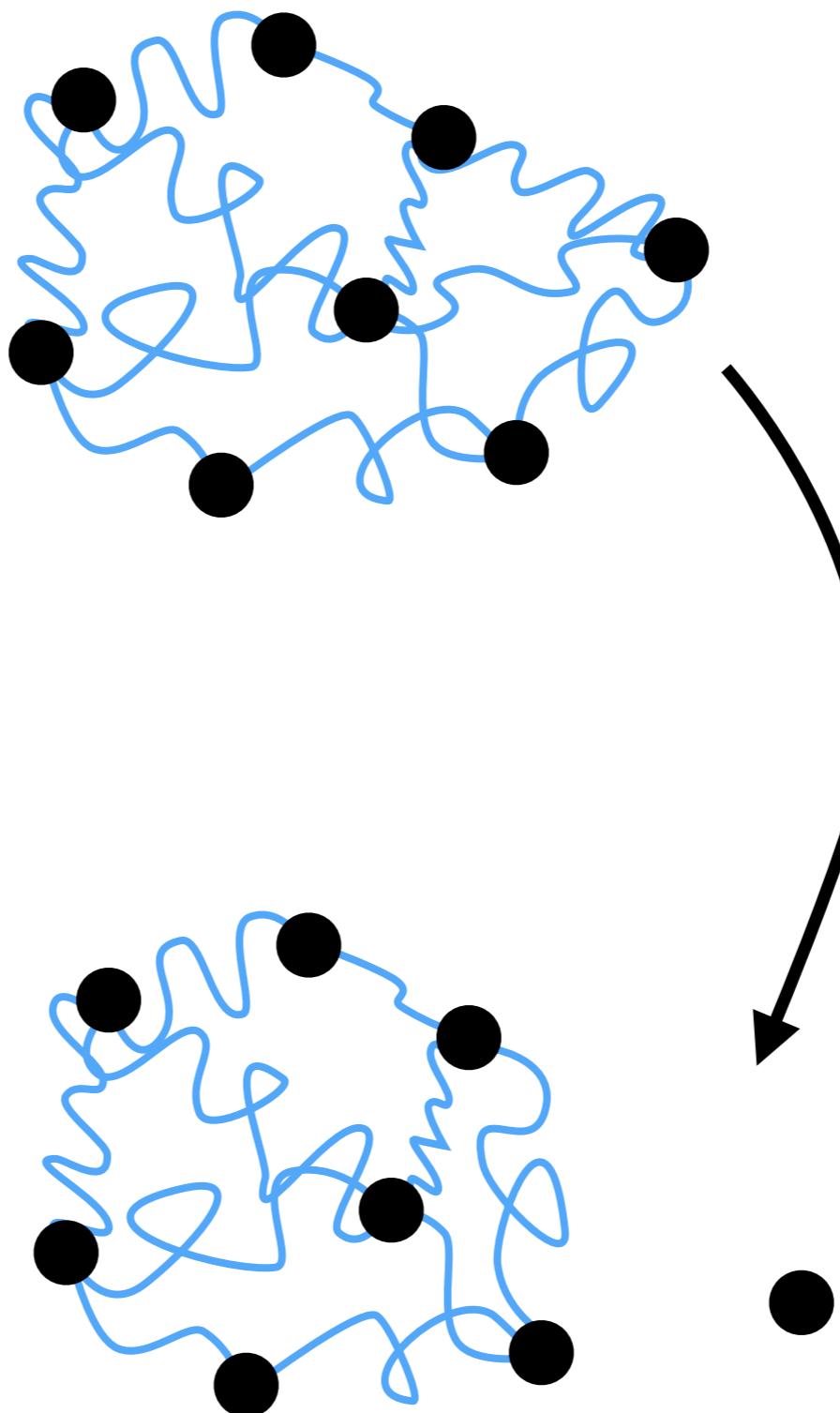
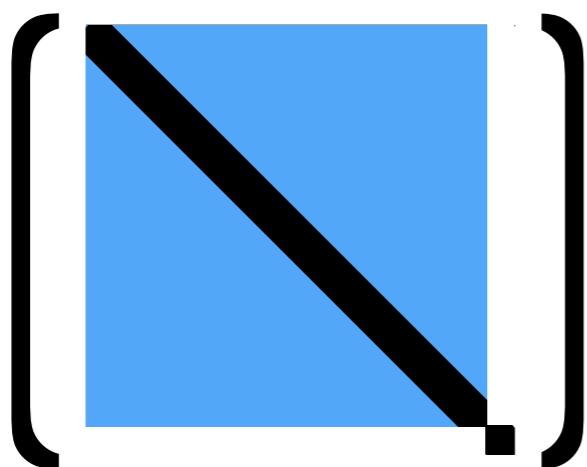
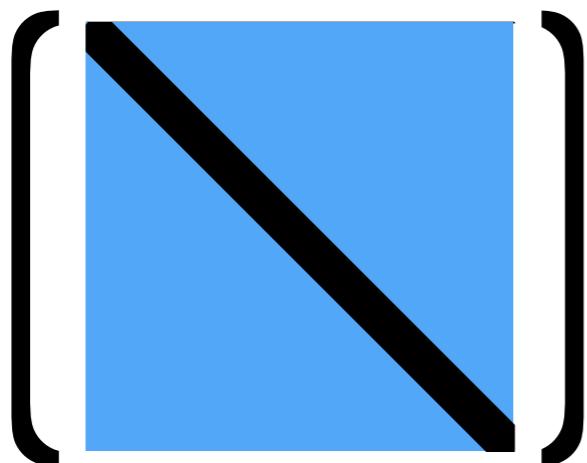
BFSS Cartoon

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Monte Carlo Study of Metastable State?



$\text{DOF} \sim N^2$
 $t_{\text{recurrence}} \sim e^{+N^2}$

$\tau \sim e^{+N}$

$\text{DOF} \sim (N-1)^2$
 $+ \# \log(V)$

Possible Observables

Almost certainly an incomplete list!

Fast Scrambling arXiv:1512.00019 Gur-Ari, Hanada, Shenker $t_{\text{scramble}} \sim \log N$

SUGRA 0707.4454 Anagnostopoulos et al.

0803.4273 Catterall+Wiseman

1503.08499 Kadoh, Kamata

1506.01366 Filev, O'Connor

Finite N 0811.3102 Hanada, Hyakutake, Nishimura, Takeuchi

1311.5603 1603.00538 Hanada, Hyakutake, Ishiki, Nishimura

1606.04948 1606.04951 MCSMC

Polyakov loop 0811.2081 Hanada, Miwa, Nishimura, Takeuchi

2-point functions 1108.5153 Hanada, Nishimura, Sekino, Yoneya, 2009, 2011

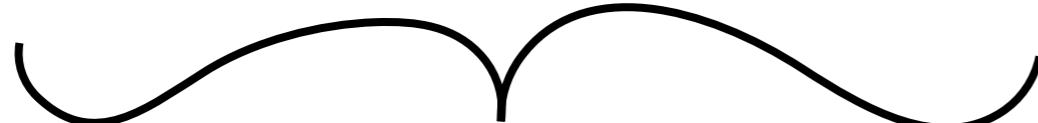
Force **1709.01932 Rinaldi, Berkowitz, Hanada, Maltz, Vranas**

'Ungauged' Theory 1802.00428 Maldacena, Milekhin

+ talks by Rinaldi (1802.02985) and Buividovich (1711.05556-like?)

Test: BH Internal Energy

$$E/N^2 = \frac{(a_0 T^{2.8} + a_1 T^{4.6} + a_2 T^{5.8} + \dots)}{N^0} + \frac{(b_0 T^{0.4} + b_1 T^{2.2} + \dots)}{N^2} + \mathcal{O}\left(\frac{1}{N^4}\right)$$




 $\frac{E_0(T)}{N^0}$ + $\frac{E_1(T)}{N^2}$ + ...

Expand in $\frac{\alpha'}{R_{BH}^2} \sim T^{3/5}$

$$a_0 = 7.41$$

hep-th/980242 Itzhaki, Maldacena, Sonnenschein, Yankielowicz

$$b_0 = -5.77$$

1311.7526 Hyakutake

(α') 1, 2, and 4 terms vanish

Gross + Witten, Nucl Phys B 277:1 1986

Gross + Sloan, Nucl Phys B291:41-89, 1987

Grisaru, van de Ven, + Zanon PLB 173:423-428, 1986

Green + Vanhove PRD61:104011, 2000

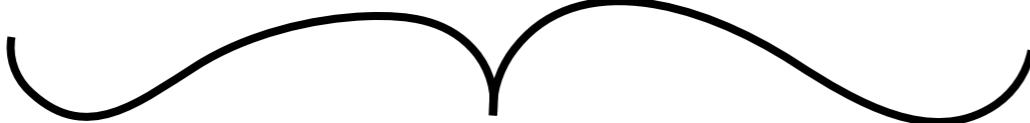
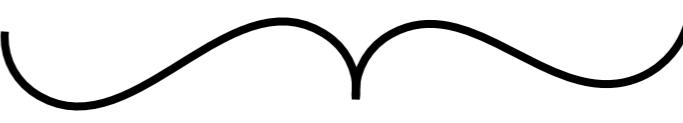
Green, Russo + Vanhove JHEP 02:099, 2007

Hyakutake PTEP 2014:033B04, 2014

Hyakutake JHEP 09:075, 2014

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 +
 
 + ...

$\frac{E_0(T)}{N^0}$

 $\frac{E_1(T)}{N^2}$

+ ...

't Hooft counting still valid, even in discretized theory

Expand in $\frac{\alpha'}{R_{BH}^2} \sim T^{3/5}$

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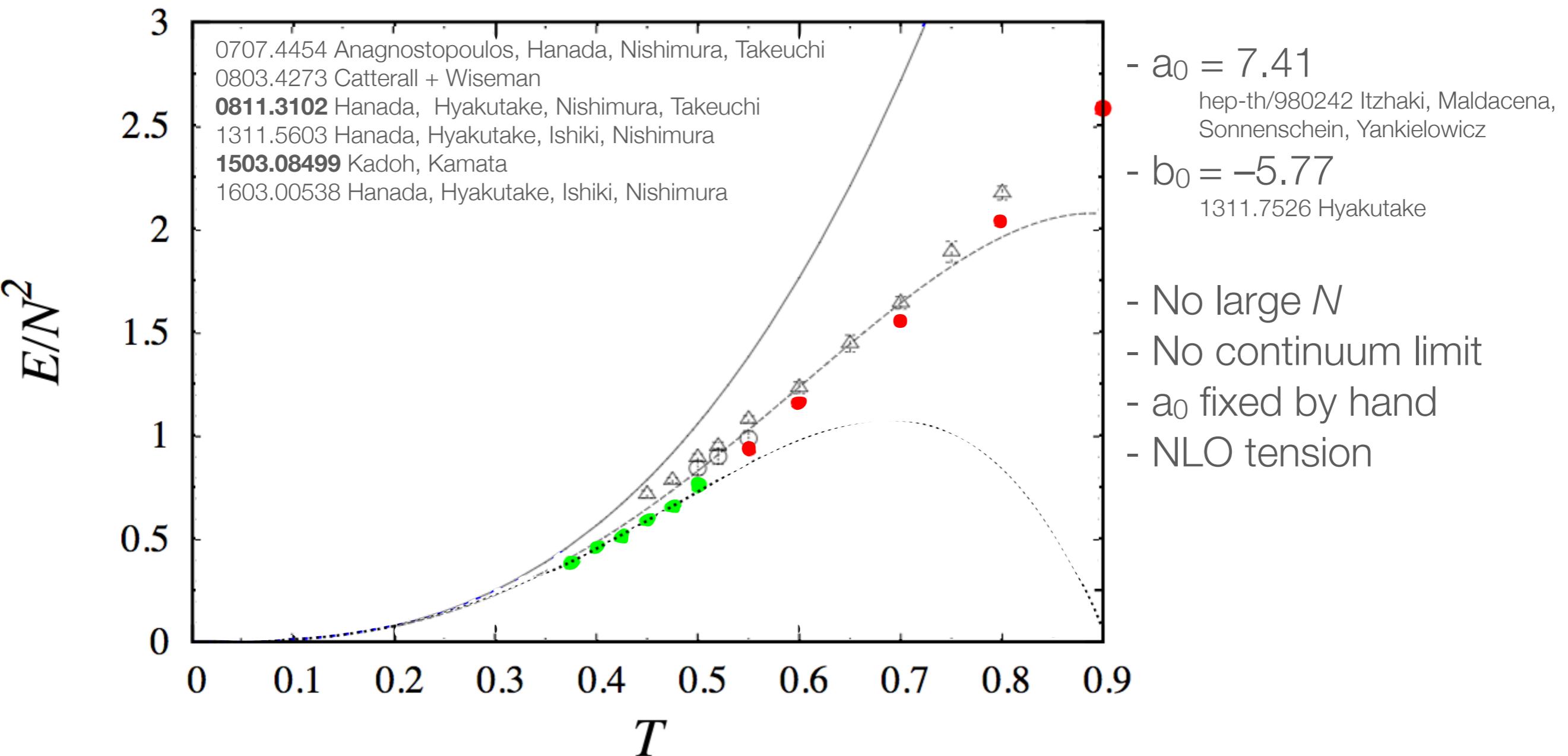
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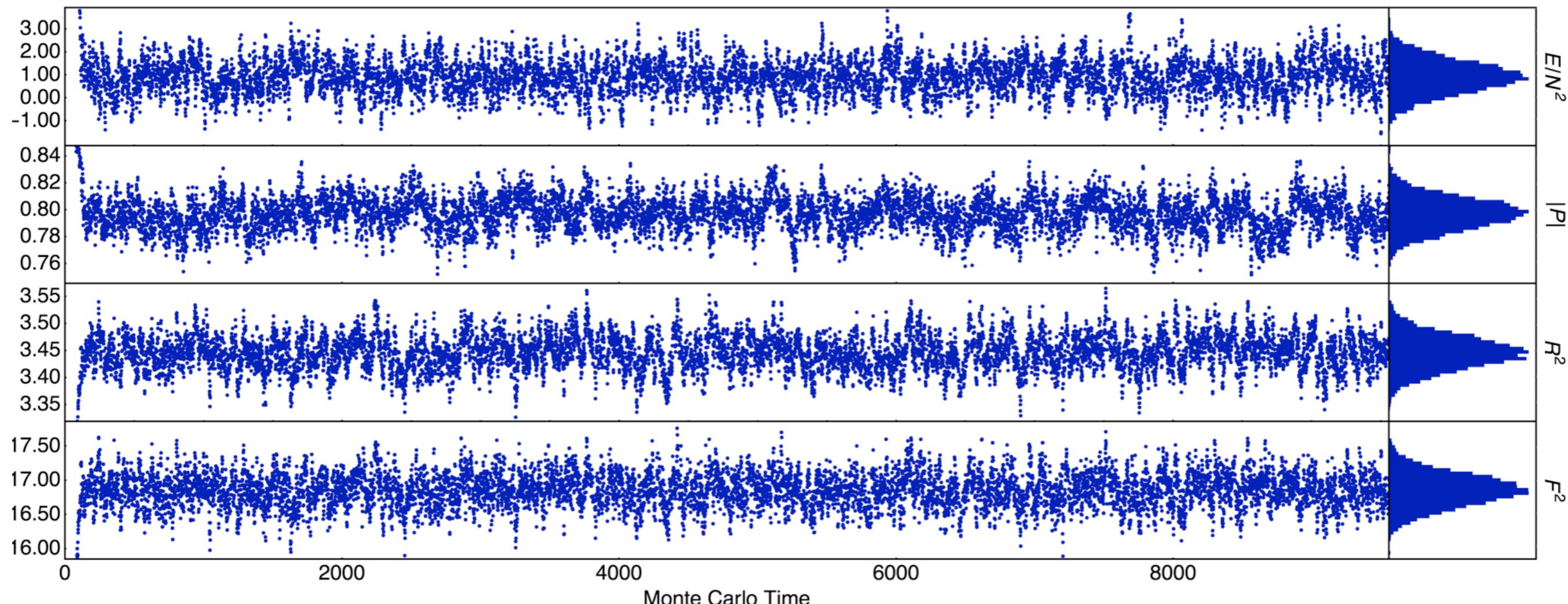
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Example Monte Carlo History

MCSMC 1606.04948 1606.04951

$T=0.5$ $N=24$ $L=32$

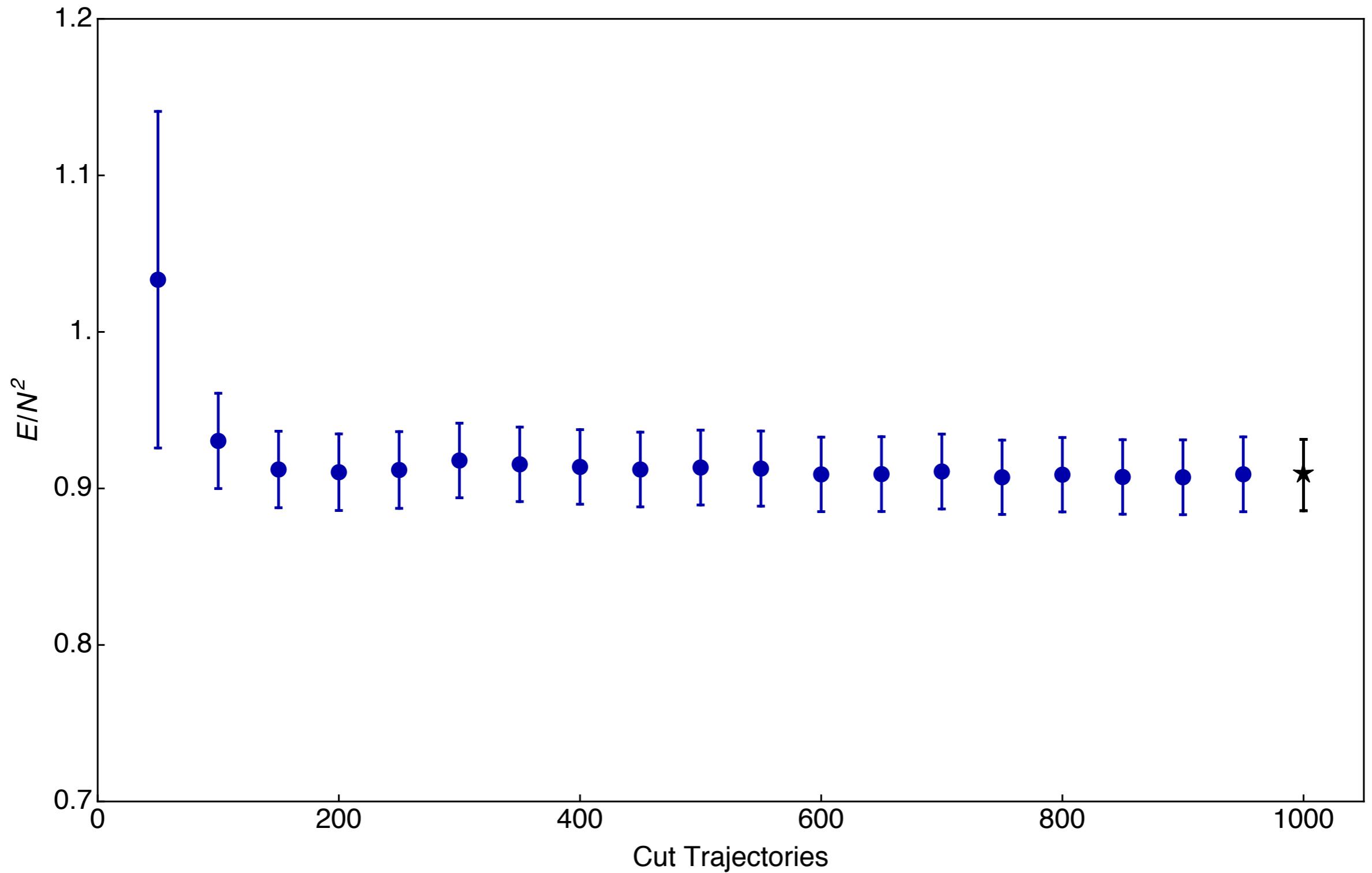


Long correlations can be seen in each observable.

Thermalization Cut

MCSMC 1606.04948 1606.04951

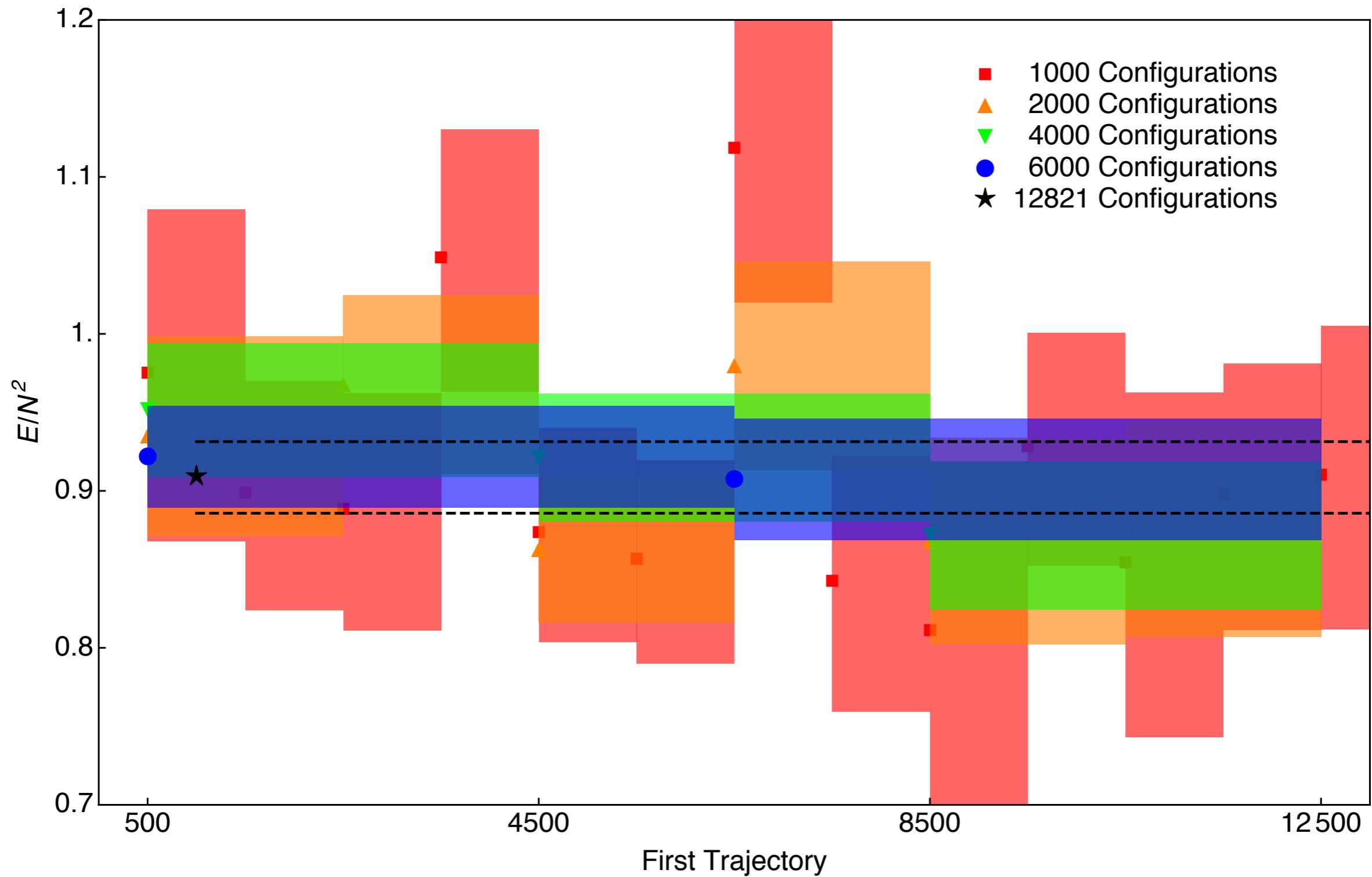
$T=0.5$ $N=16$ $L=32$



Statistical Stability

MCSMC 1606.04948 1606.04951

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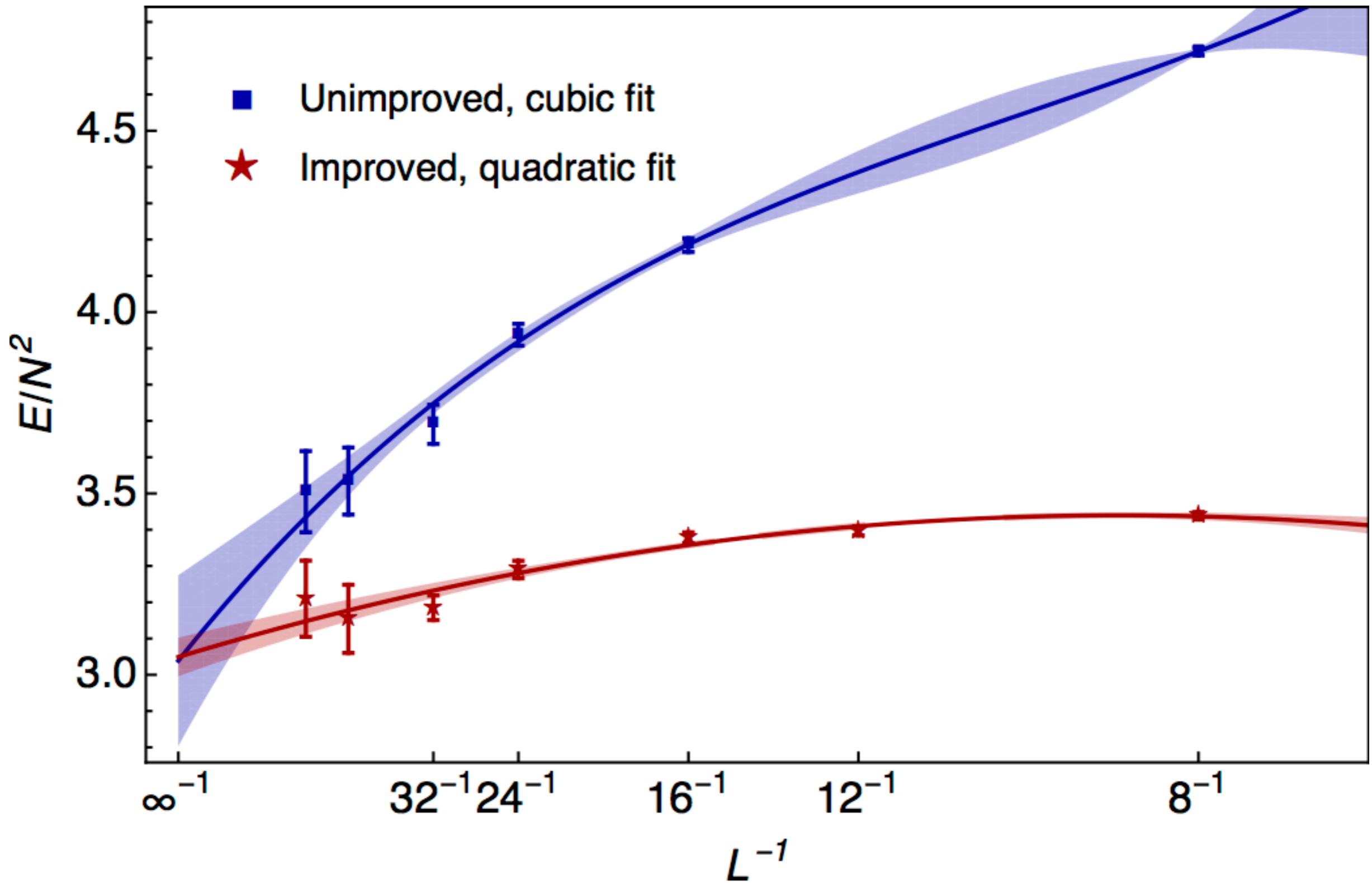
Compute!



Ensembles

T	N	L	action	N_{cfg}	E/N^2	$ P $	R^2	F^2	T	N	L	action	N_{cfg}	E/N^2	$ P $	R^2	F^2		
0.4	24	16	improved	15935	0.827±0.005	0.72770±0.00035	3.2504±0.0015	14.530±0.002	0.8	16	32	improved	20187	2.107±0.024	0.89261±0.00015	3.5452±0.0014	18.131±0.009		
		24	improved	2321	0.719±0.031	0.72888±0.00129	3.3459±0.0039	15.627±0.011			8	improved	22151	2.417±0.006	0.88779±0.00011	3.2416±0.0006	15.010±0.003		
		32	improved	6625	0.657±0.027	0.72721±0.00116	3.4110±0.0020	16.319±0.008			12	improved	18175	2.346±0.009	0.89207±0.00011	3.3553±0.0008	16.155±0.005		
		8	improved	3057	0.903±0.009	0.74150±0.00348	4.8789±0.0967	13.846±0.006			16	improved	20721	2.303±0.010	0.89317±0.00009	3.4232±0.0007	16.868±0.004		
		12	improved	2491	0.907±0.010	0.72754±0.00089	3.1663±0.0024	13.651±0.005			24	improved	9153	2.216±0.020	0.89239±0.00015	3.4968±0.0012	17.681±0.008		
		16	improved	8242	0.835±0.007	0.72732±0.00054	3.2387±0.0012	14.518±0.003			32	improved	13867	2.176±0.028	0.89287±0.00015	3.5366±0.0015	18.134±0.009		
		24	improved	1331	0.692±0.052	0.72919±0.00453	3.3414±0.0025	15.635±0.012			8	improved	19213	2.424±0.007	0.88809±0.00014	3.2394±0.0008	15.012±0.004		
		32	improved	1888	0.629±0.029	0.72849±0.00142	3.4016±0.0018	16.311±0.008			16	improved	13495	2.340±0.017	0.89302±0.00018	3.4216±0.0014	16.869±0.008		
	0.5	16	8	improved	21101	1.229±0.004	0.78847±0.00031	3.1104±0.0026	13.068±0.003		0.9	16	8	unimproved	20411	4.221±0.010	0.90519±0.00009	3.5113±0.0012	17.926±0.005
		12	improved	17201	1.140±0.007	0.79566±0.00032	3.2304±0.0014	14.374±0.003	12		improved	20401	2.895±0.009	0.90433±0.00009	3.3002±0.0008	15.599±0.004			
		16	improved	17933	1.081±0.009	0.79599±0.00035	3.3086±0.0012	15.207±0.004	16		unimproved	20501	2.863±0.011	0.90783±0.00009	3.4048±0.0009	16.679±0.005			
		32	improved	15101	0.907±0.020	0.79689±0.00049	3.4747±0.0017	16.897±0.006	improved		37701	3.710±0.014	0.90689±0.00007	3.5475±0.0007	18.635±0.005				
		24	8	improved	20951	1.243±0.004	0.78964±0.00028	3.0776±0.0007	13.038±0.002		improved	21461	2.796±0.014	0.90856±0.00009	3.4717±0.0010	17.377±0.006			
		16	improved	19765	1.092±0.006	0.79718±0.00020	3.2883±0.0005	15.194±0.002	24		unimproved	21851	3.450±0.028	0.90639±0.00010	3.5807±0.0013	19.001±0.008			
		24	improved	14957	0.979±0.010	0.79741±0.00029	3.3898±0.0006	16.240±0.003	improved		17955	2.716±0.021	0.90826±0.00011	3.5400±0.0014	18.139±0.009				
		32	improved	10469	0.941±0.024	0.79727±0.00051	3.4457±0.0012	16.851±0.007	32		unimproved	12221	3.243±0.049	0.90720±0.00013	3.6037±0.0019	19.209±0.012			
		32	improved	16253	1.248±0.003	0.78995±0.00020	3.0712±0.0006	13.032±0.002	improved		14601	2.673±0.031	0.90849±0.00013	3.5750±0.0017	18.545±0.011				
		8	improved	3569	1.155±0.010	0.79600±0.00049	3.2012±0.0010	14.357±0.004	24		8	improved	24331	2.931±0.006	0.90413±0.00008	3.2958±0.0006	15.613±0.004		
	0.6	16	12	improved	7885	1.093±0.009	0.79730±0.00034	3.2830±0.0007	15.196±0.003		12	improved	17557	2.872±0.010	0.90785±0.00009	3.4025±0.0009	16.707±0.006		
		16	improved	2873	0.946±0.047	0.79852±0.00123	3.3815±0.0032	16.223±0.012	16		improved	24441	2.822±0.010	0.90861±0.00007	3.4658±0.0007	17.384±0.005			
		32	improved	5469	0.955±0.023	0.79833±0.00044	3.4386±0.0011	16.841±0.006	24		improved	8917	2.761±0.023	0.90774±0.00013	3.5349±0.0014	18.156±0.009			
		24	improved	8977	1.339±0.021	0.84184±0.00034	3.4410±0.0020	16.754±0.008	32		improved	16709	2.719±0.028	0.90824±0.00010	3.5663±0.0014	18.538±0.009			
0.6	16	8	improved	27221	1.560±0.005	0.83423±0.00018	3.1410±0.0006	13.728±0.002	1.0	16	8	unimproved	21291	4.719±0.011	0.91705±0.00007	3.5139±0.0010	18.245±0.006		
		12	improved	19051	1.475±0.007	0.84077±0.00021	3.2708±0.0008	15.001±0.003			12	improved	20641	3.439±0.010	0.91672±0.00008	3.3515±0.0009	16.185±0.005		
		16	improved	18141	1.432±0.010	0.84156±0.00023	3.3477±0.0010	15.790±0.004			unimproved	20751	3.397±0.012	0.91968±0.00008	3.4485±0.0010	17.217±0.006			
		24	improved	8977	1.339±0.021	0.84184±0.00034	3.4410±0.0020	16.754±0.008			16	improved	25379	4.185±0.019	0.91907±0.00007	3.5769±0.0010	19.034±0.007		
		32	improved	19017	1.575±0.005	0.83539±0.00024	3.1248±0.0007	13.731±0.003			improved	21641	3.378±0.015	0.92033±0.00008	3.5115±0.0011	17.876±0.007			
	0.7	8	improved	12577	1.276±0.025	0.84212±0.00030	3.4780±0.0012	17.309±0.007		1.0	16	24	unimproved	23391	3.937±0.030	0.91855±0.00008	3.6099±0.0013	19.376±0.009	
		12	improved	19017	1.481±0.007	0.84083±0.00018	3.2602±0.0007	15.012±0.003			improved	17469	3.290±0.024	0.91979±0.00009	3.5755±0.0017	18.600±0.011			
		16	improved	19961	1.429±0.008	0.84205±0.00018	3.3349±0.0006	15.790±0.003			32	unimproved	13503	3.690±0.054	0.91895±0.00012	3.6323±0.0019	19.582±0.013		
		24	improved	25249	1.346±0.009	0.84176±0.00015	3.4262±0.0006	16.753±0.003			improved	15555	3.185±0.034	0.91985±0.00011	3.6068±0.0018	18.971±0.013			
		32	improved	12577	1.276±0.025	0.84212±0.00030	3.4780±0.0012	17.309±0.007			48	unimproved	12026	3.534±0.092	0.92064±0.00014	3.6592±0.0028	19.810±0.021		
		8	improved	19017	1.575±0.005	0.83539±0.00024	3.1248±0.0007	13.731±0.003			improved	5772	3.154±0.094	0.92101±0.00025	3.6431±0.0042	19.401±0.027			
		16	improved	10071	1.442±0.009	0.84182±0.00022	3.3306±0.0006	15.787±0.004			64	unimproved	15024	3.505±0.112	0.92051±0.00015	3.6808±0.0029	19.999±0.020		
		24	improved	30641	1.959±0.005	0.86564±0.00013	3.1941±0.0006	14.377±0.003			improved	7280	3.210±0.						

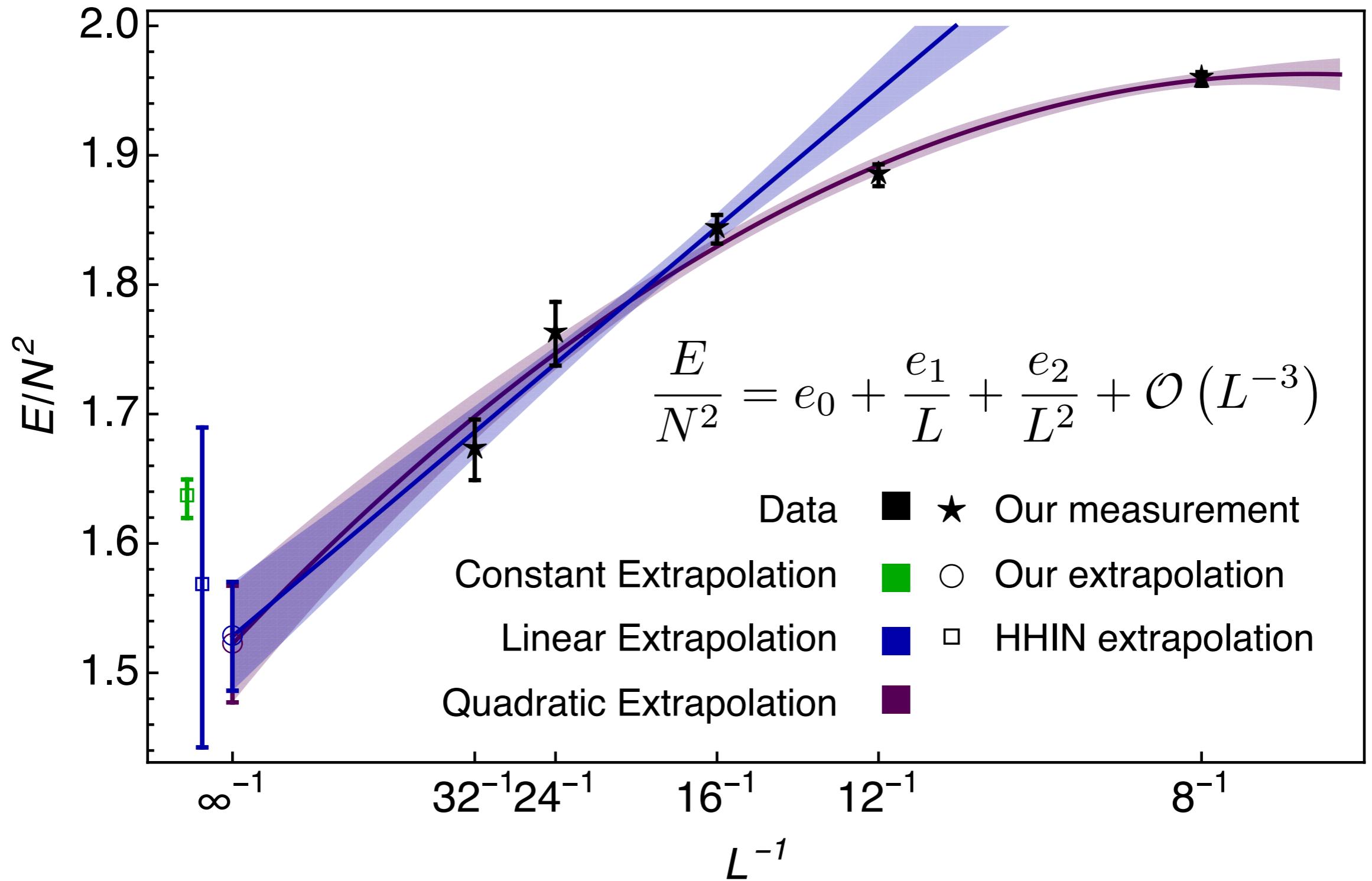
Derivative Improvement



Fixed- N Continuum Extrapolation

MCSMC 1606.04948 1606.04951

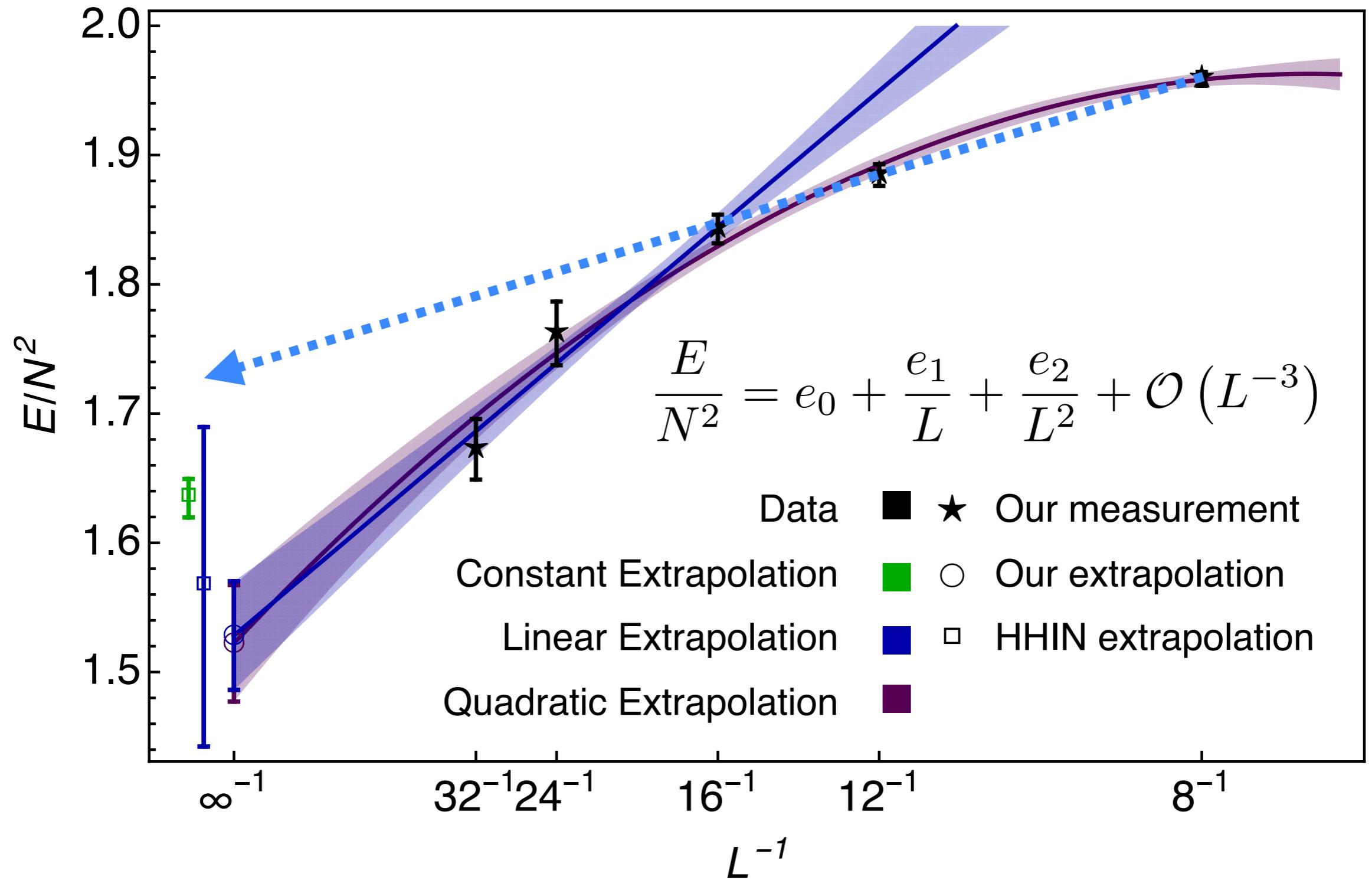
$T=0.7 N=16$



Fixed- N Continuum Extrapolation

MCSMC 1606.04948 1606.04951

$T=0.7 N=16$



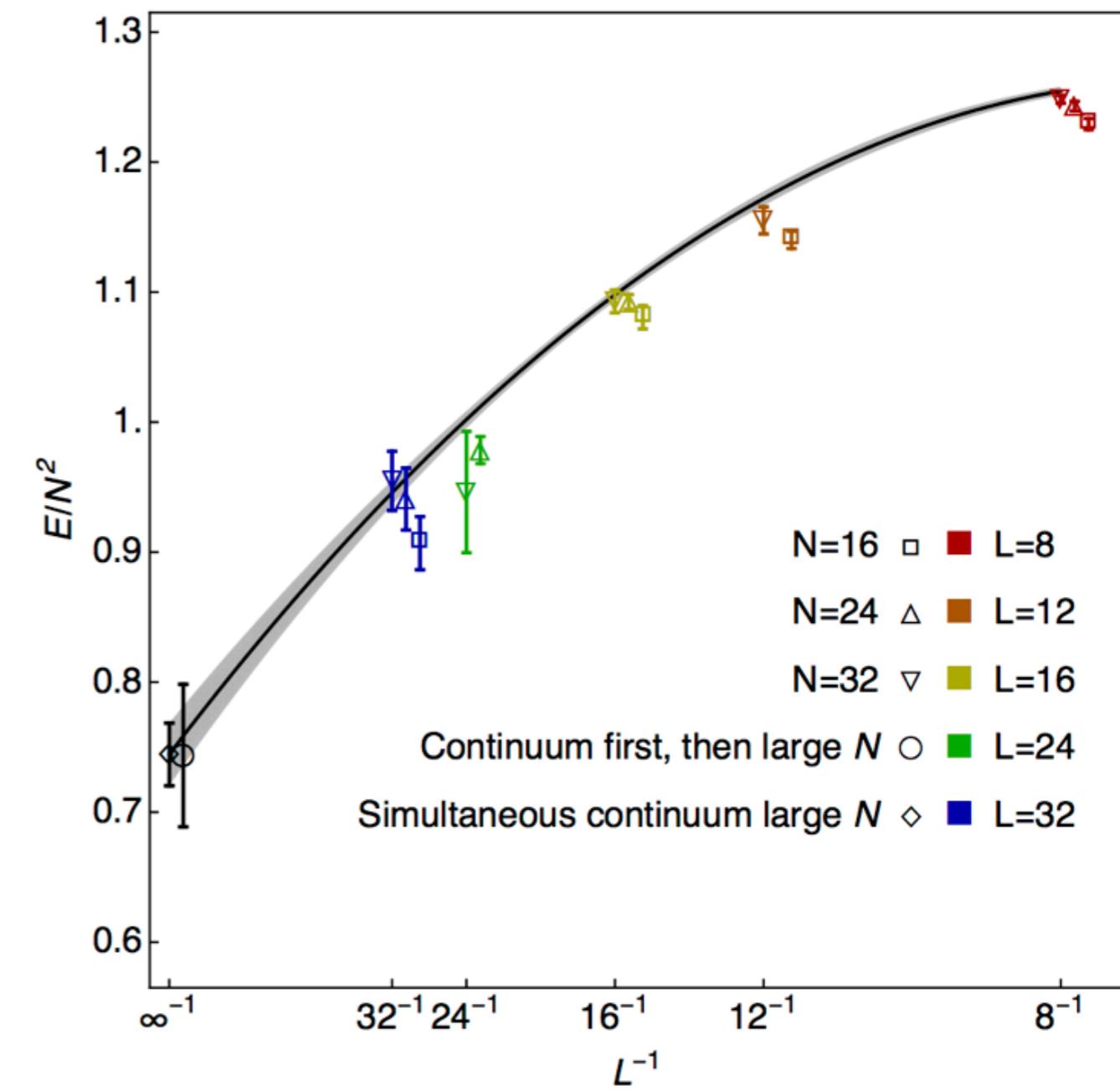
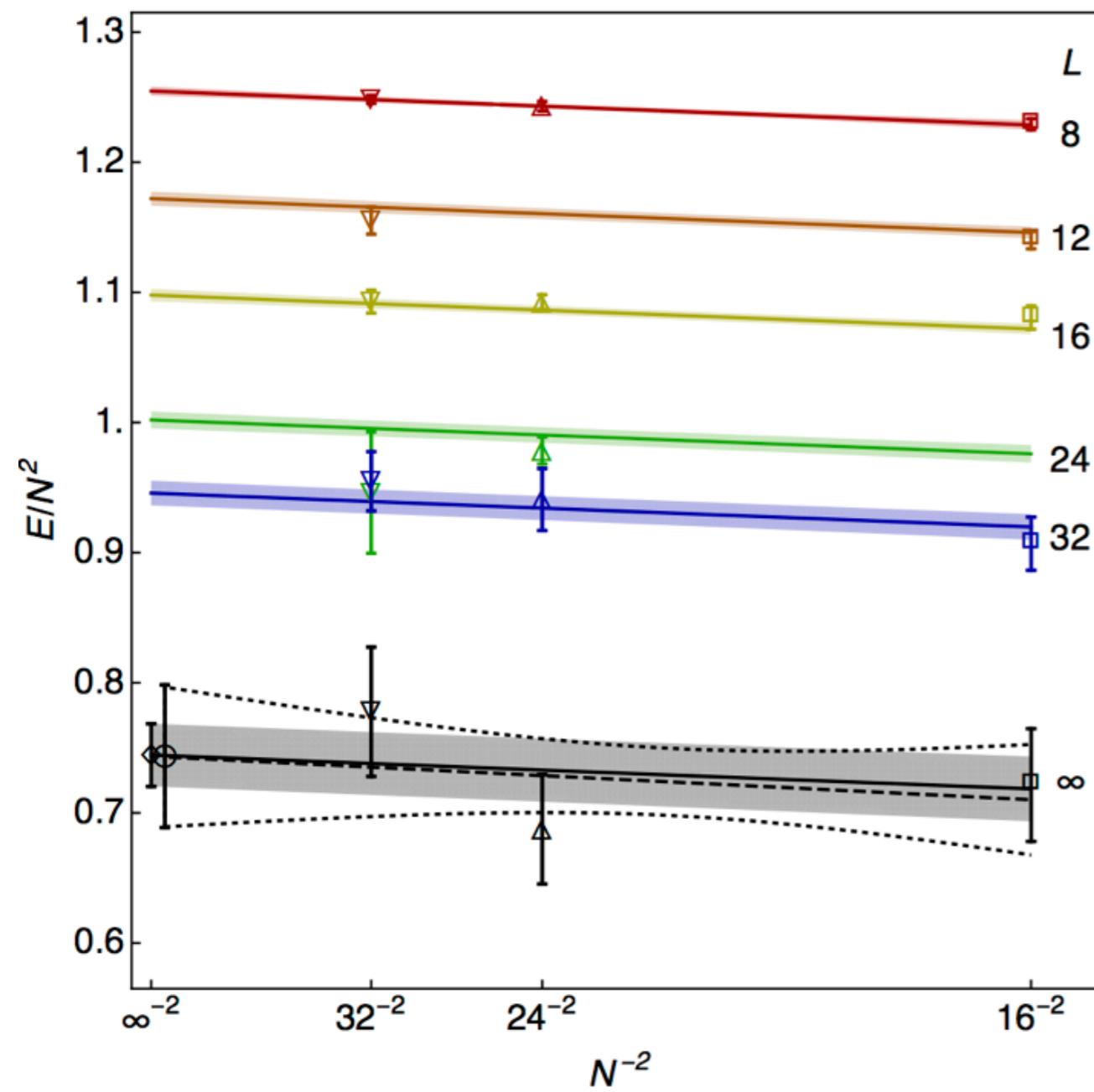
Simultaneous Continuum + Large- N Extrapolation

MCSMC 1606.04948 1606.04951

$$\frac{E}{N^2} = \sum_{ij \geq 0} \frac{e_{ij}}{N^{2i} L^j}$$

$e_{00}, e_{01}, e_{02}, e_{10}$

$T=0.5$



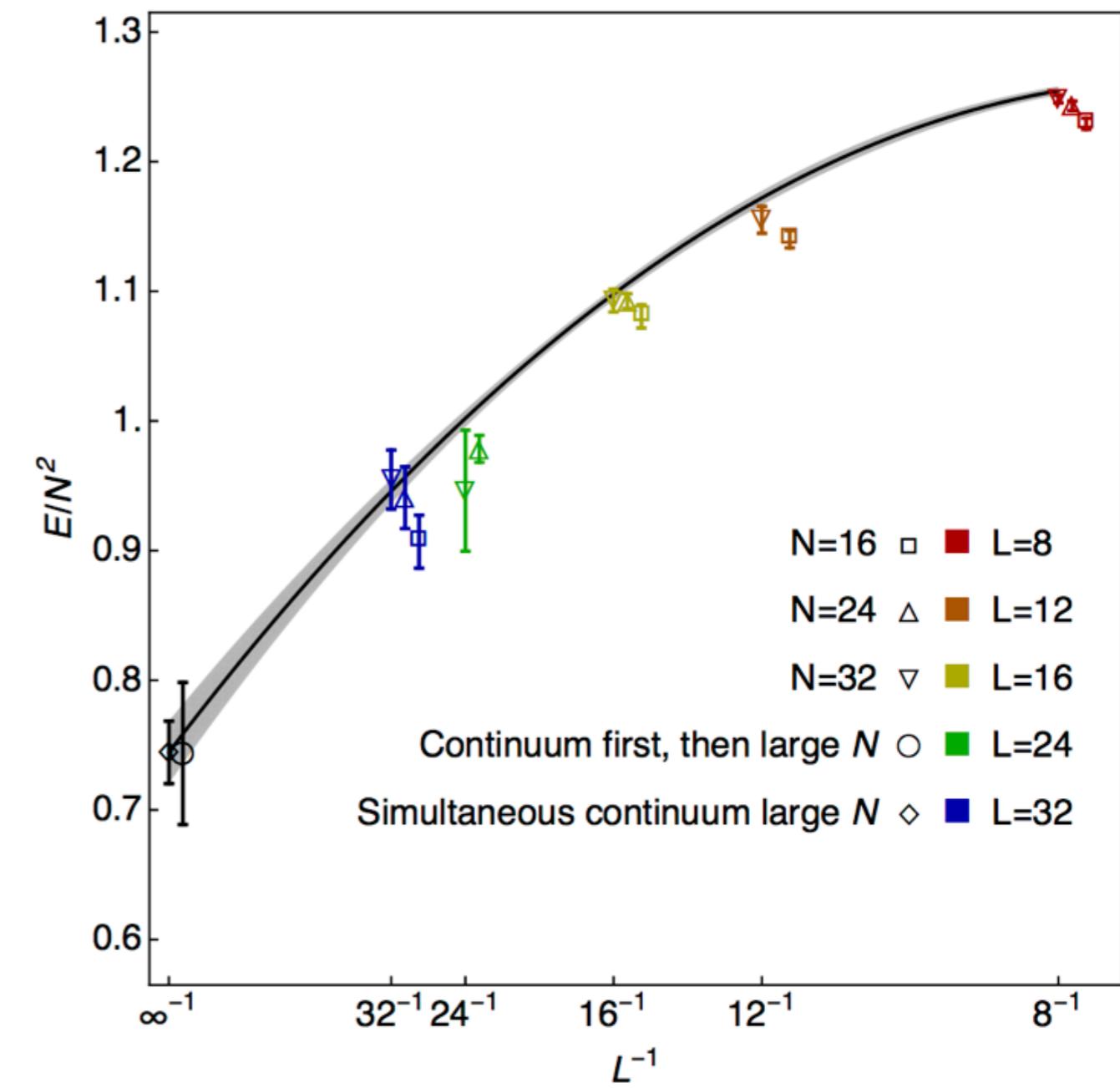
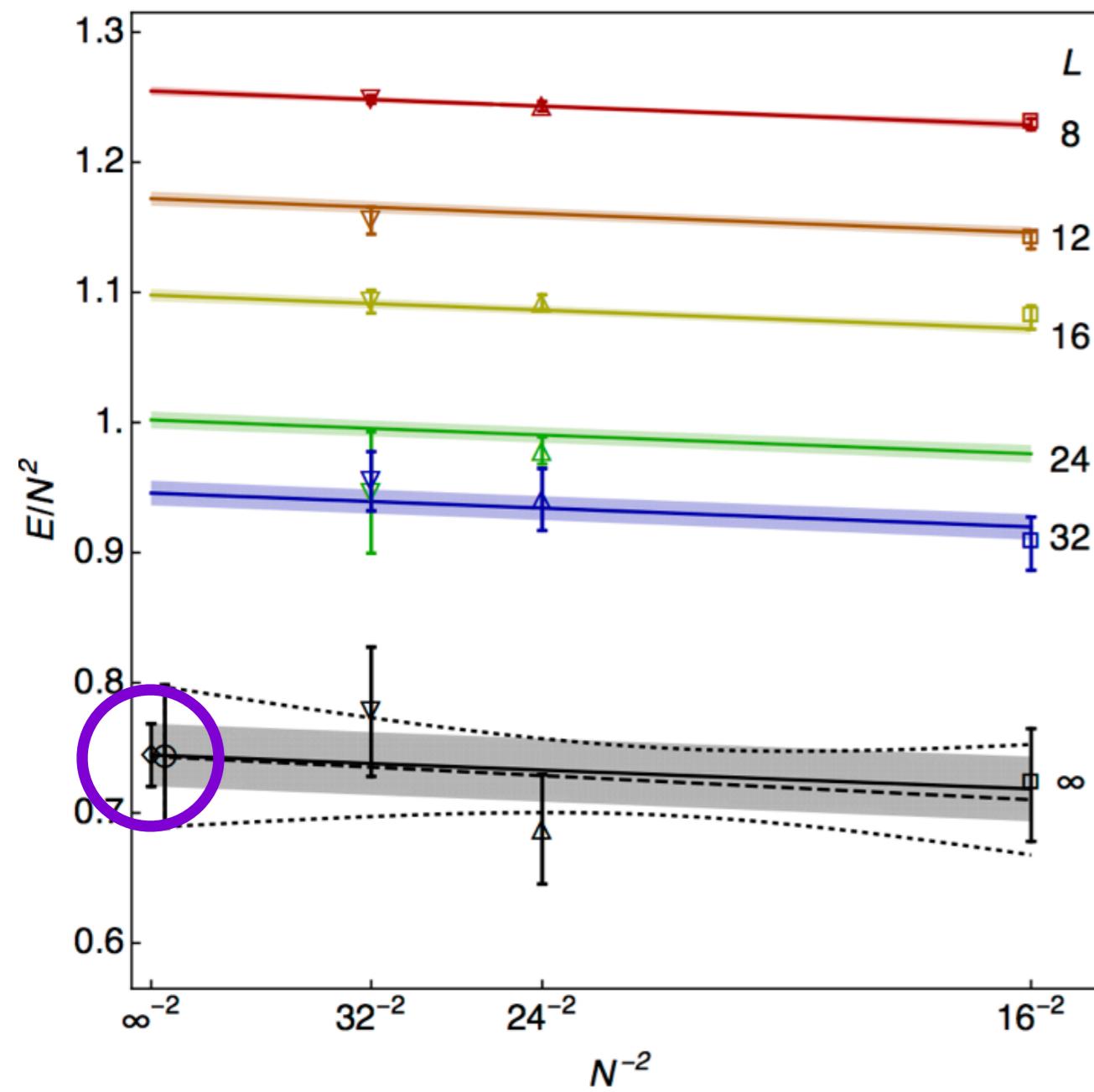
Simultaneous Continuum + Large- N Extrapolation

MCSMC 1606.04948 1606.04951

$$\frac{E}{N^2} = \sum_{ij \geq 0} \frac{e_{ij}}{N^{2i} L^j}$$

e_{00} e_{01}, e_{02}, e_{10}

$T=0.5$



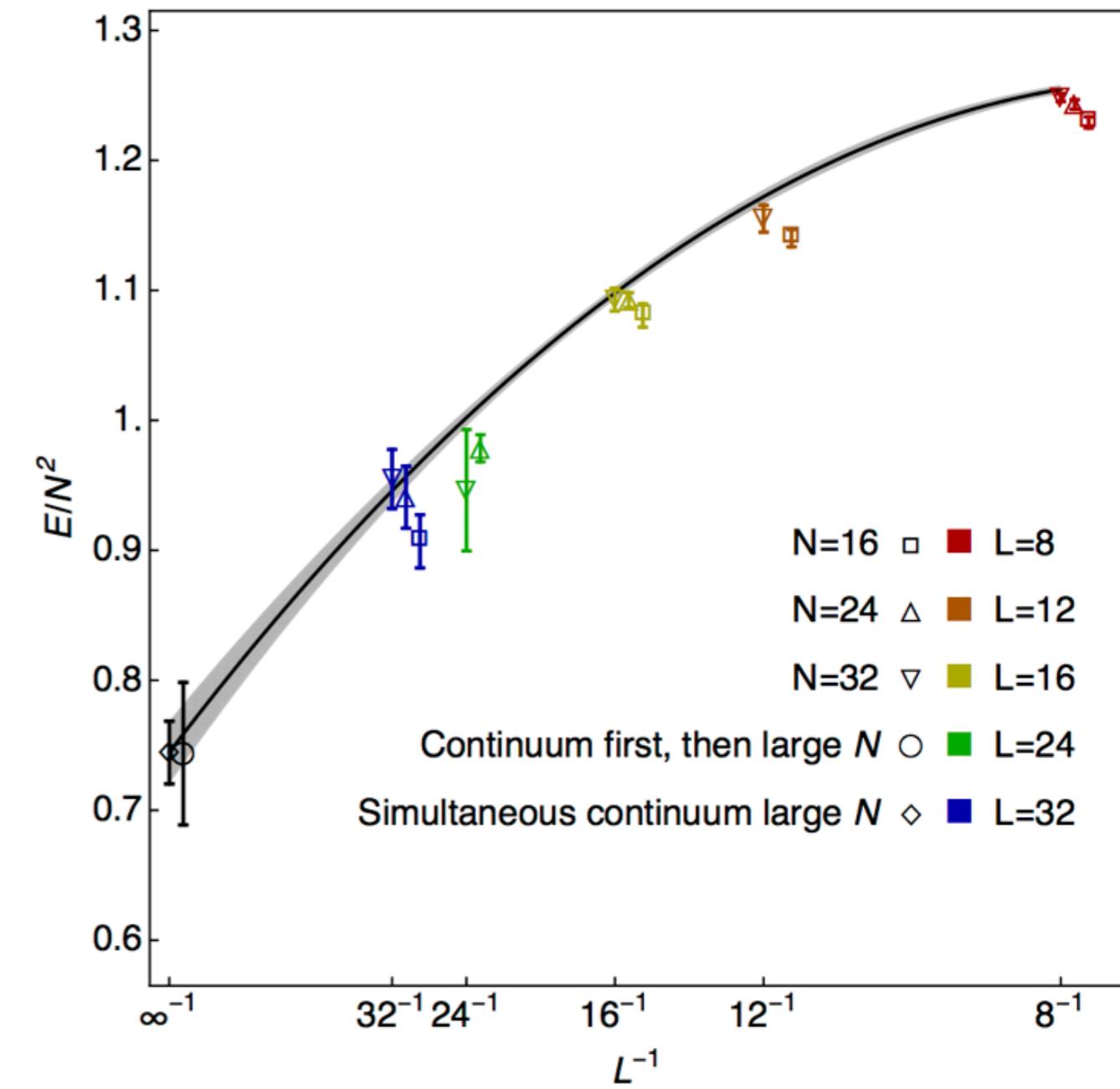
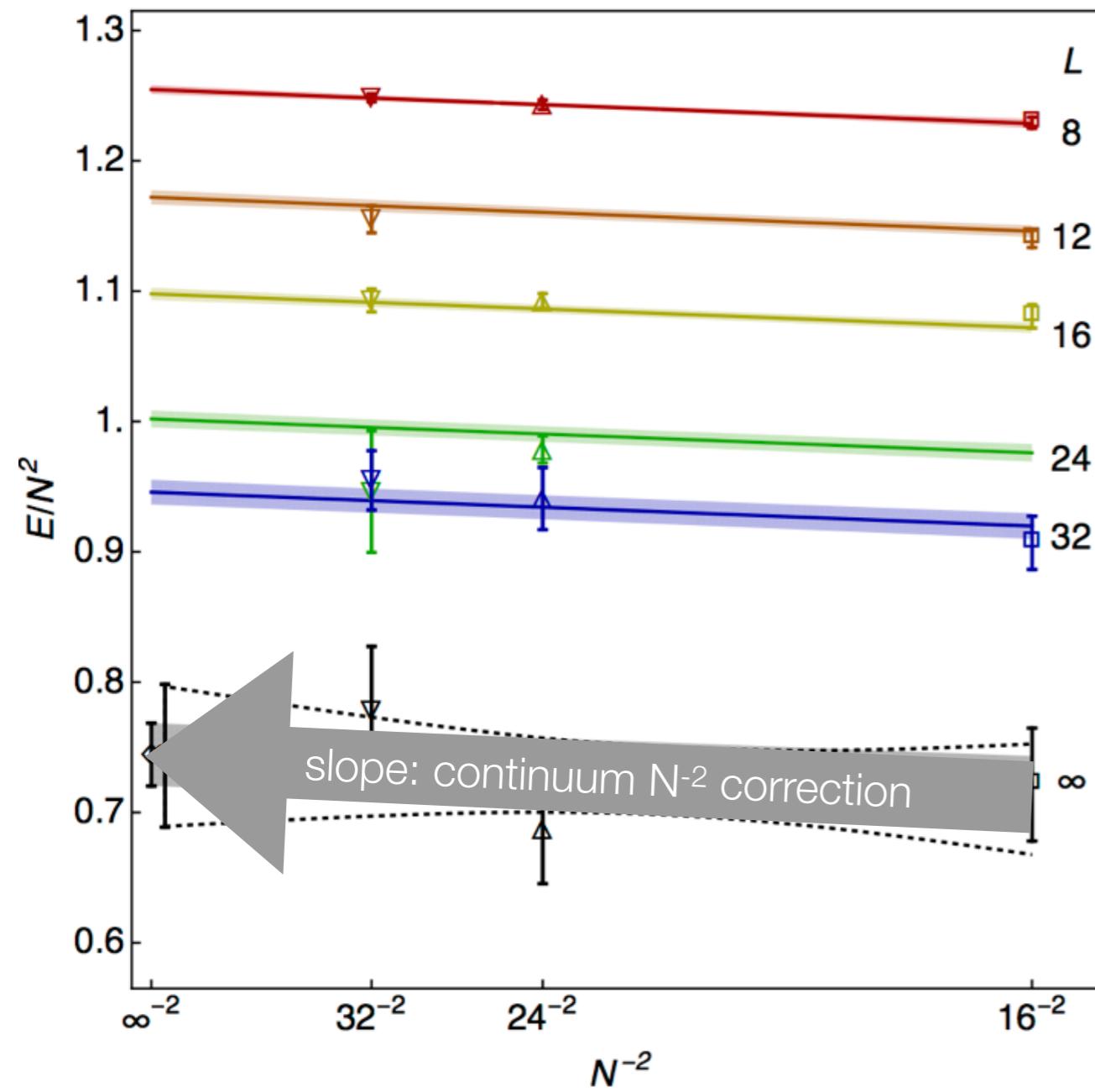
Simultaneous Continuum + Large- N Extrapolation

MCSMC 1606.04948 1606.04951

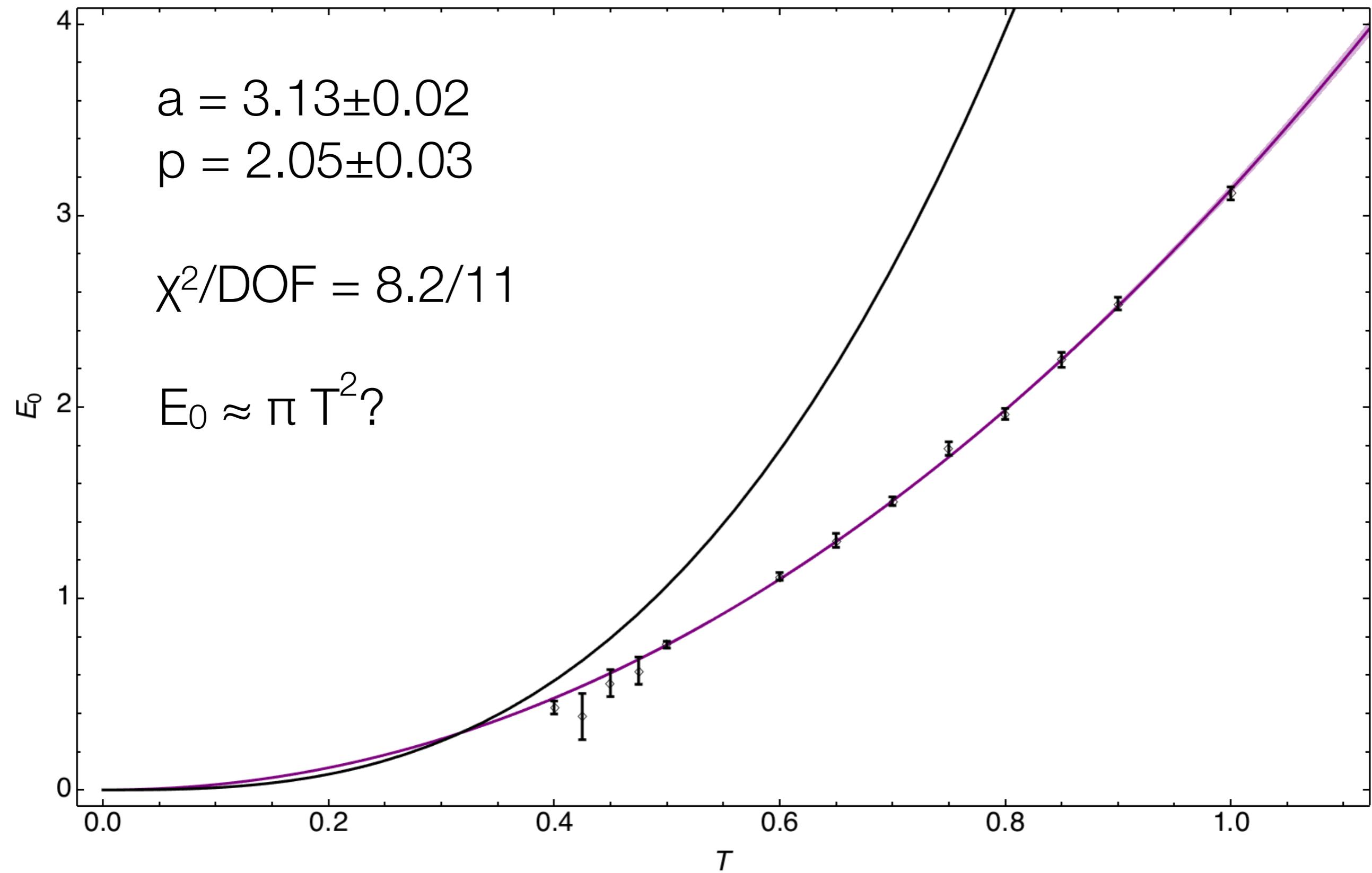
$$\frac{E}{N^2} = \sum_{ij \geq 0} \frac{e_{ij}}{N^{2i} L^j}$$

$e_{00}, e_{01}, e_{02}, e_{10}$

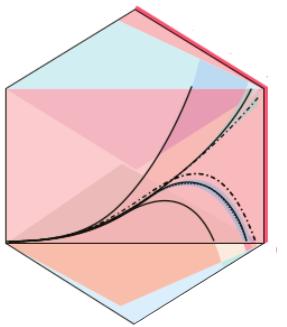
$T=0.5$



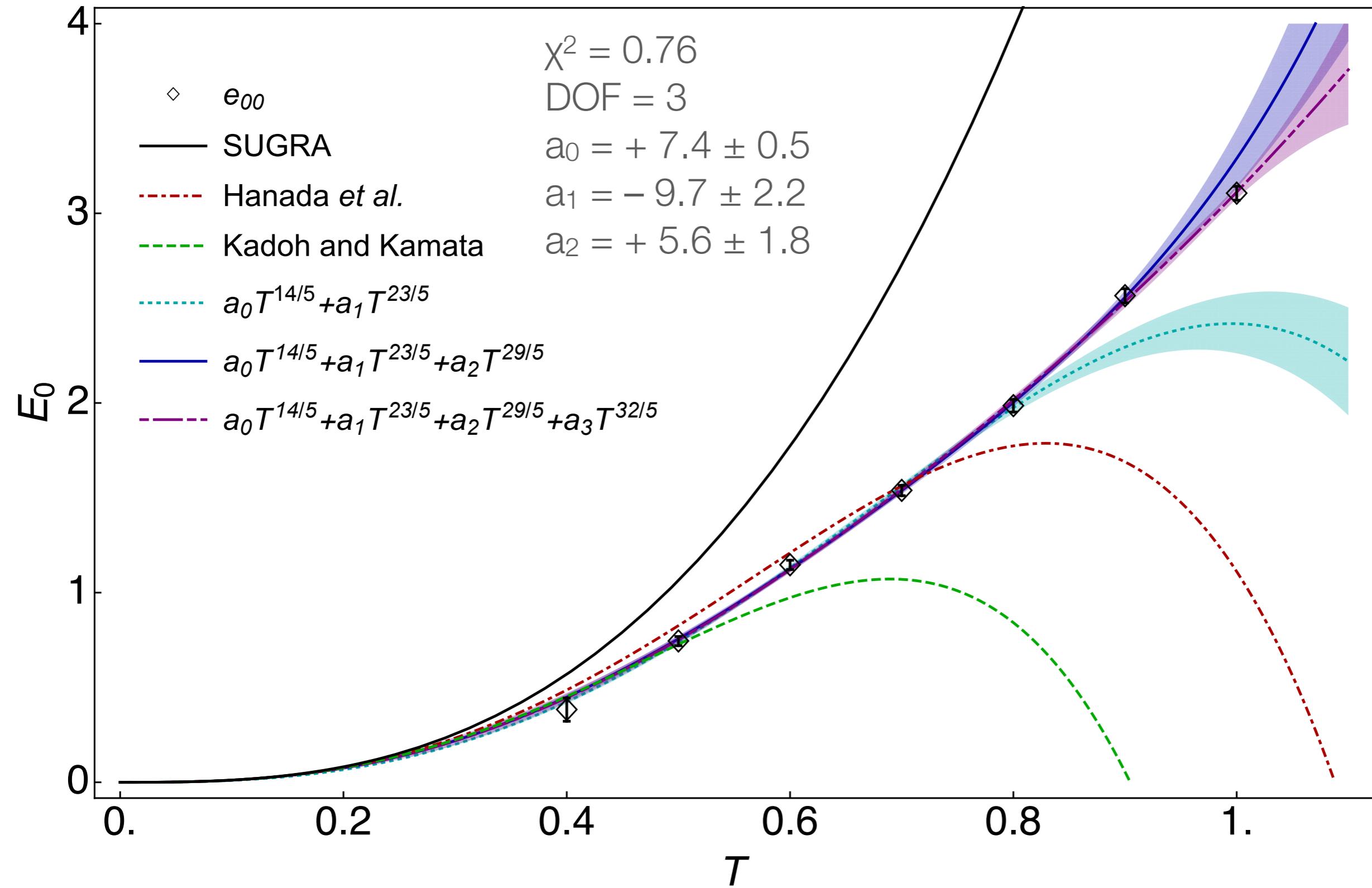
No stringy input: $a T^p$?



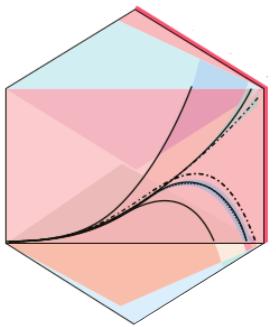
$$E/N^2 = N^0 (a_0 T^{2.8} + a_1 T^{4.6} + a_2 T^{5.8} + \dots) + \mathcal{O}(N^{-2})$$



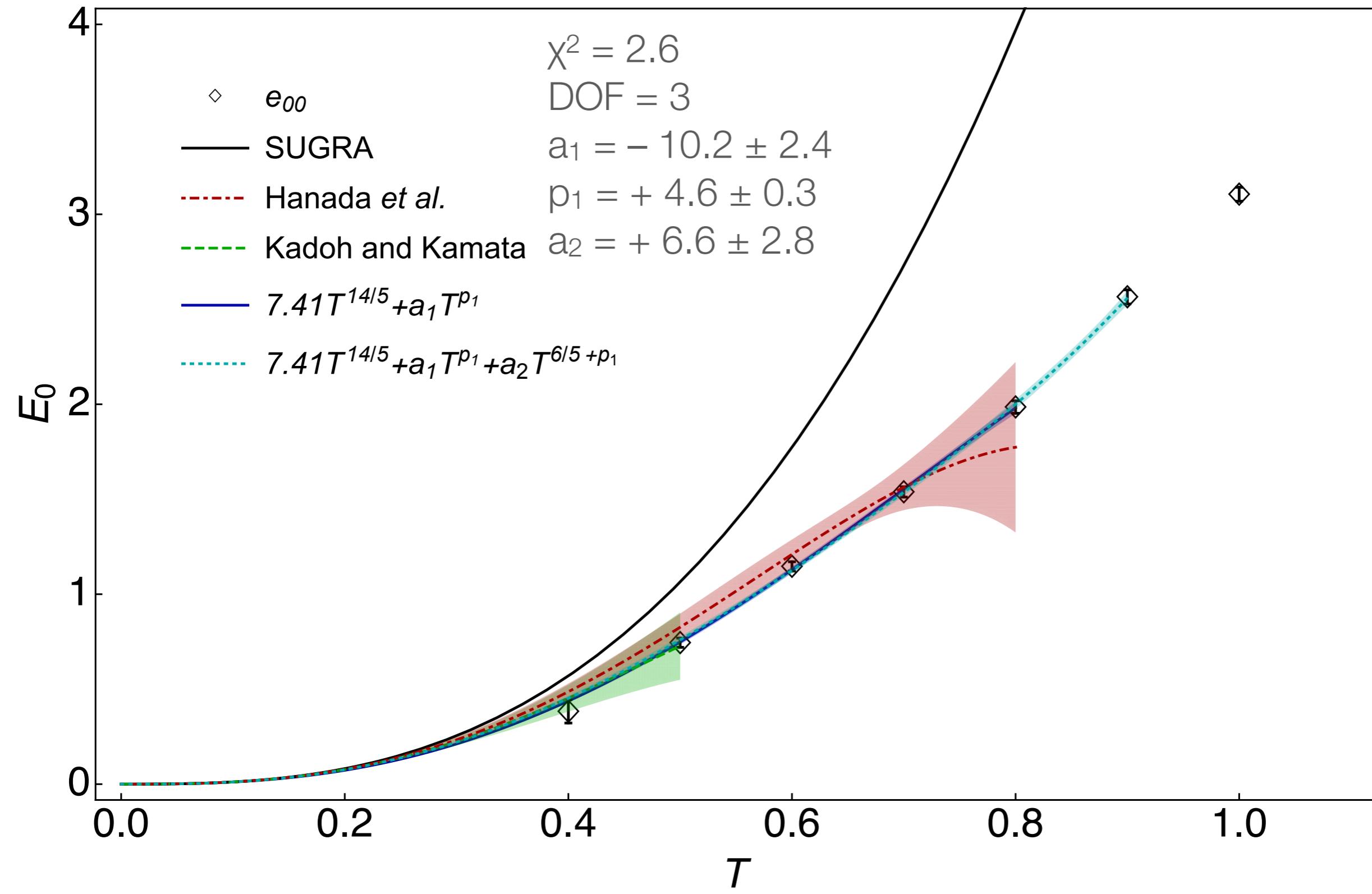
MCSMC 1606.04948 1606.04951



$$E/N^2 = N^0 (a_0 T^{2.8} + a_1 T^{4.6} + a_2 T^{5.8} + \dots) + \mathcal{O}(N^{-2})$$



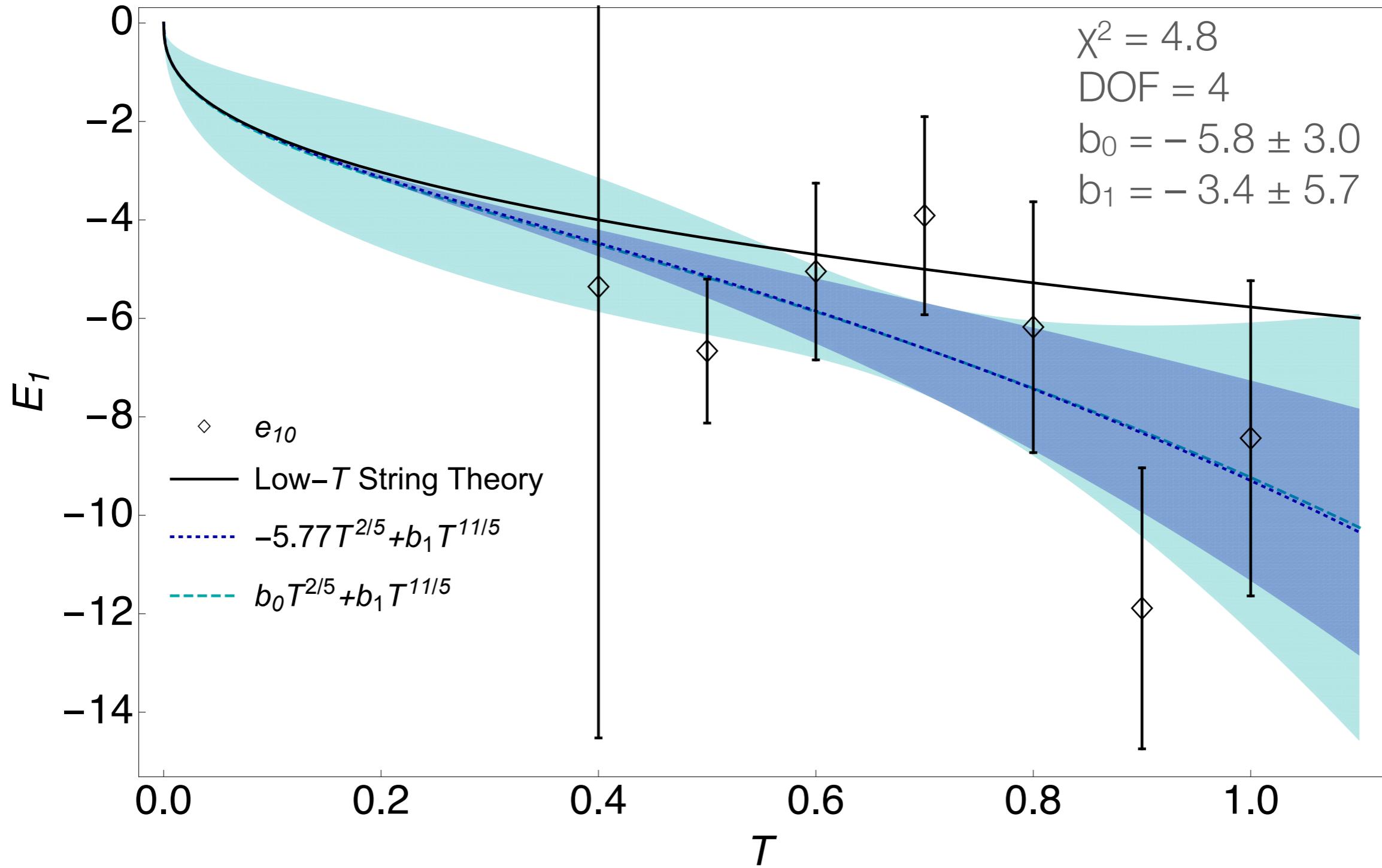
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$$\mathcal{O}(N^{-2}) = N^{-2} (b_0 T^{0.4} + b_1 T^{2.2} + \dots)$$

slope: continuum N^{-2} correction

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Summary

Quantum Gravity

Gauge Theory

- 0+1D BFSS reproduces known 10D SUGRA result
- Nontrivial checks of gauge / gravity duality
- Predictions about (quantum!) stringy corrections.

Backup Slides

Phase Quench

